

# **Artificial Intelligence and Machine Learning**

**Barbara Caputo**

# Learning highly non-linear functions

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$f: X \rightarrow Y$

- $f$  might be non-linear function
- $X$  (vector of) continuous and/or discrete vars
- $Y$  (vector of) continuous and/or discrete vars

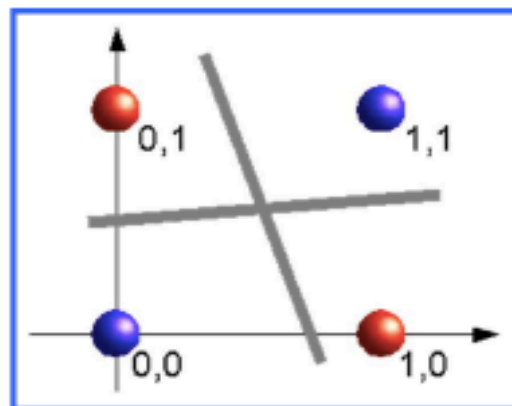
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The XOR gate



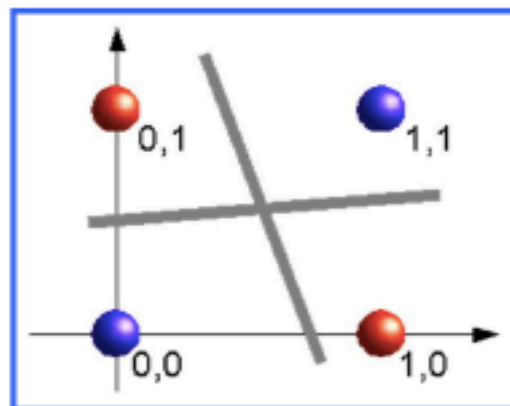
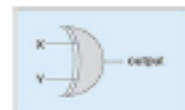
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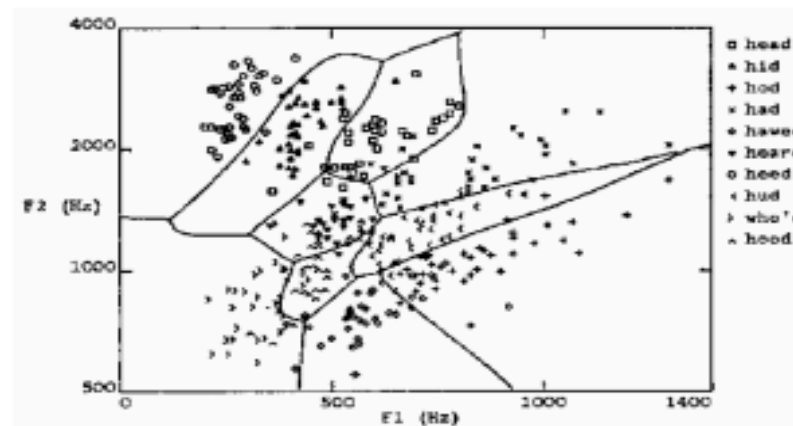
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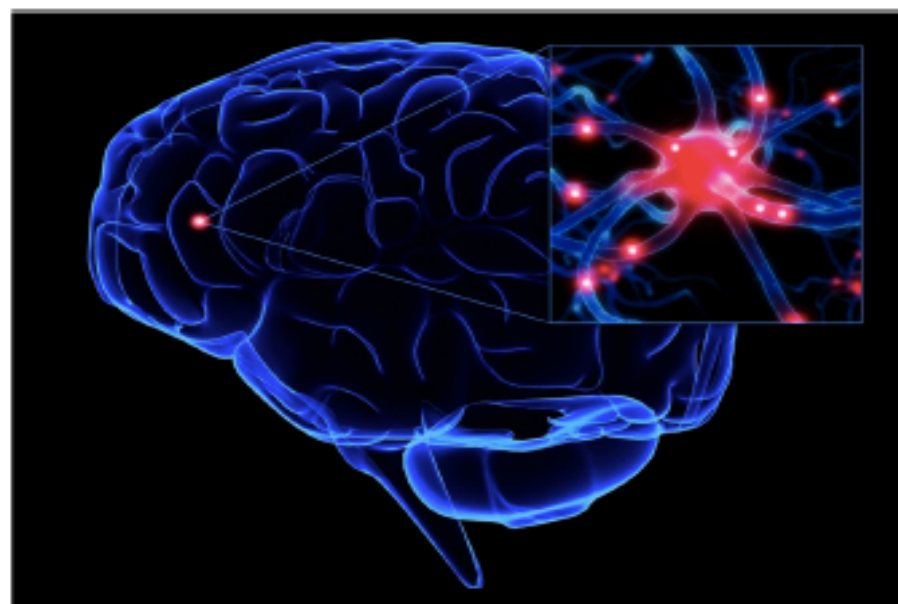


Speech recognition



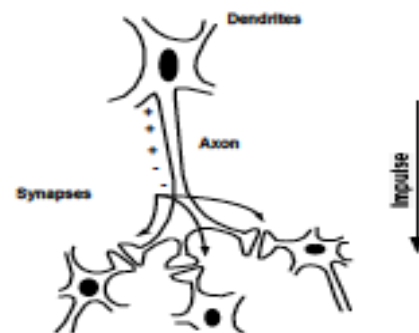
# Our brain is very good at this ...

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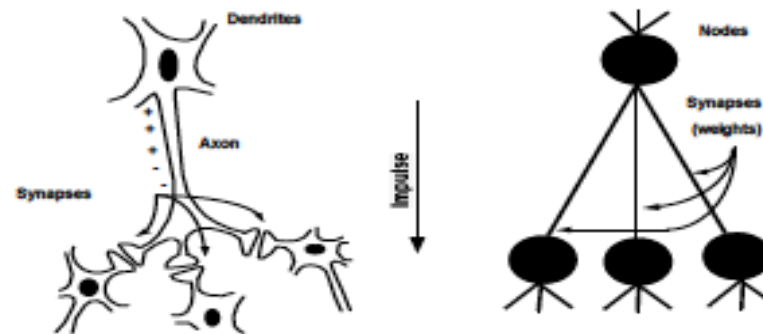


# How a neuron works

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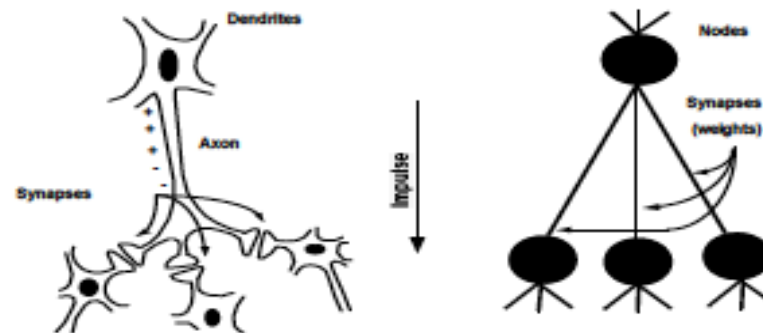


# How a neuron works





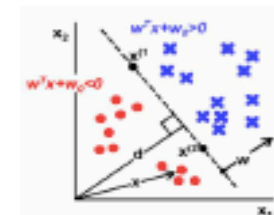
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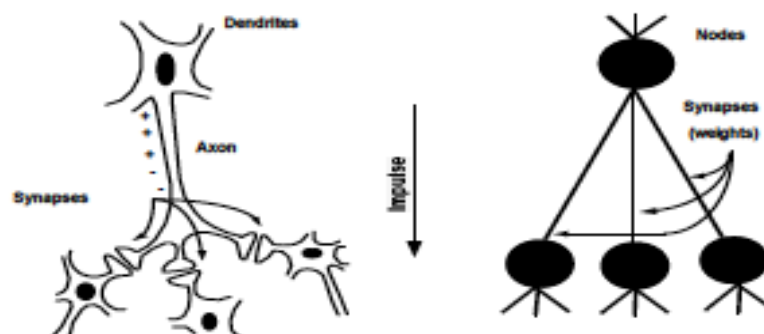
- Activation function:

$$X = \sum_{i=1}^M x_i w_i$$

$$Y = \begin{cases} +1, & \text{if } X \geq \omega_0 \\ -1, & \text{if } X < \omega_0 \end{cases}$$

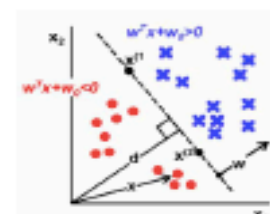


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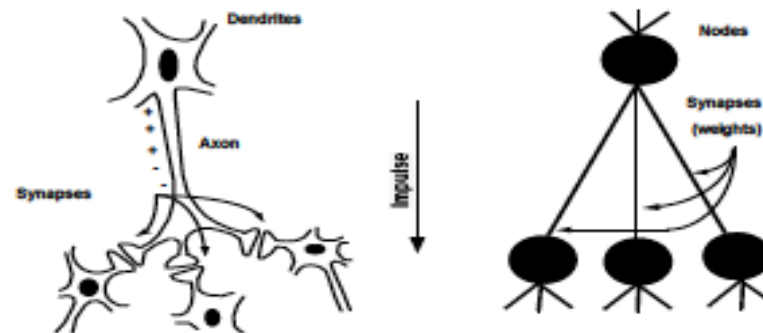
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- An mathematical expression

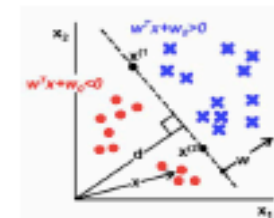
$$p(y=1|x) = \frac{1}{1 + \exp\left\{-\sum_{i=1}^M w_i x_i - \theta_0\right\}} = \frac{1}{1 + e^{-w^T x}}$$

# How a neuron works



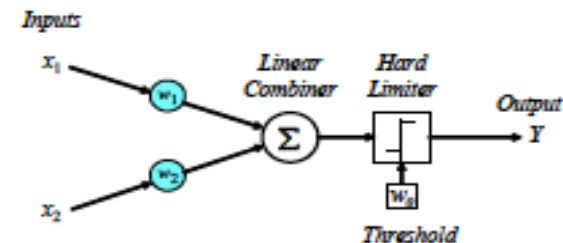
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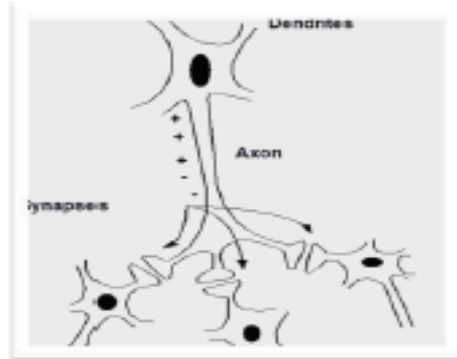
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# Perceptron and Neural Nets



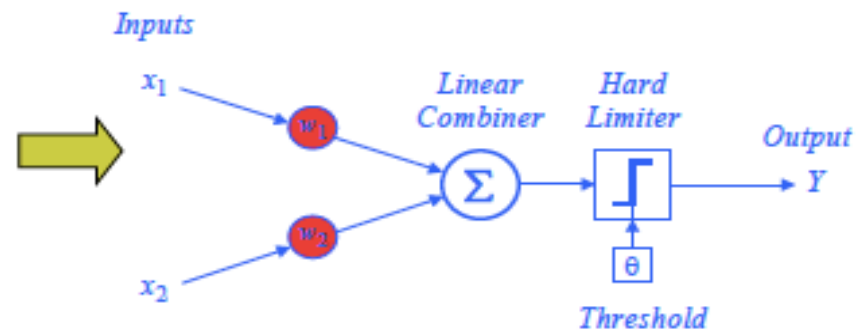
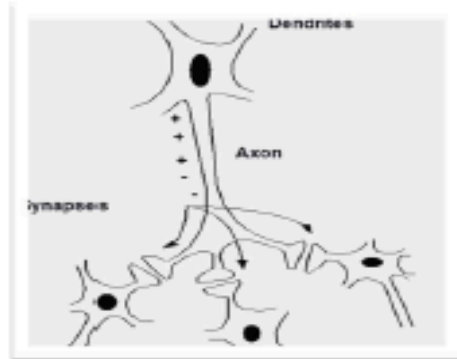
- From biological neuron to artificial neuron (perceptron)



# Perceptron and Neural Nets



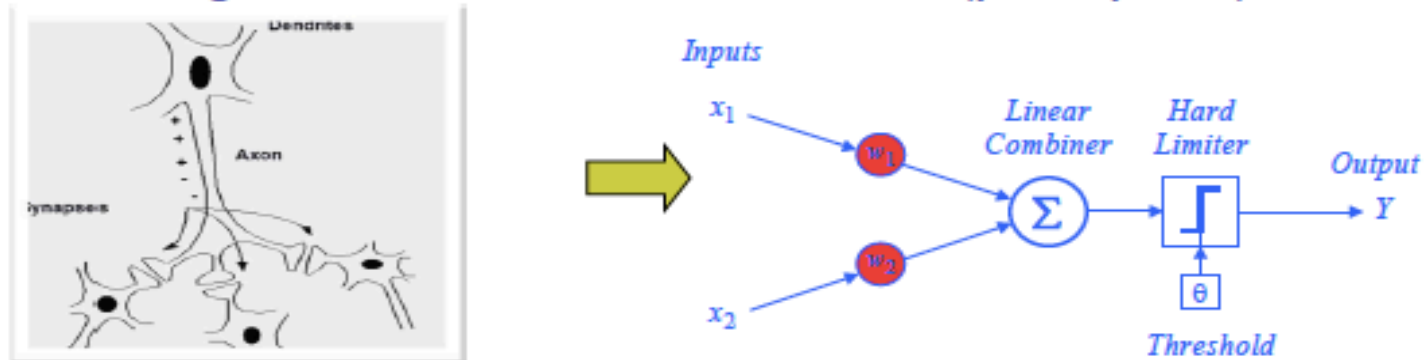
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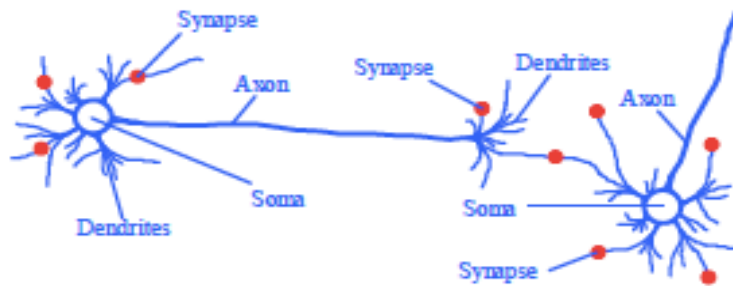
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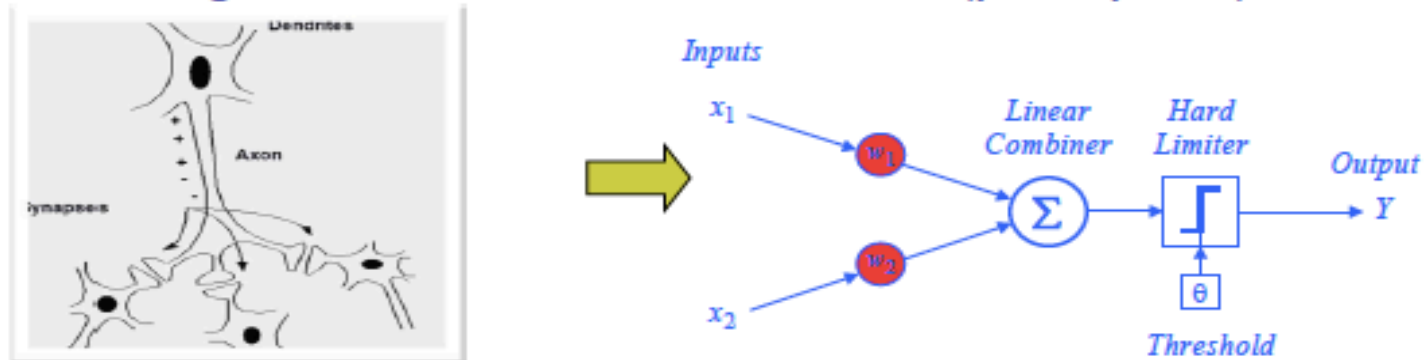
- From biological neuron network to artificial neuron networks



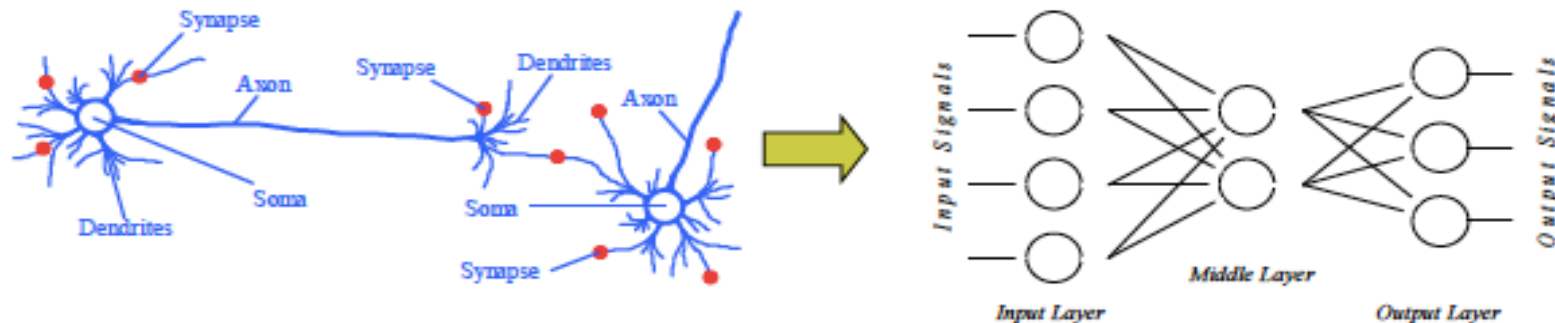
# Perceptron and Neural Nets



- From biological neuron to artificial neuron (perceptron)



- From biological neuron network to artificial neuron networks



# Jargon Pseudo-Correspondence

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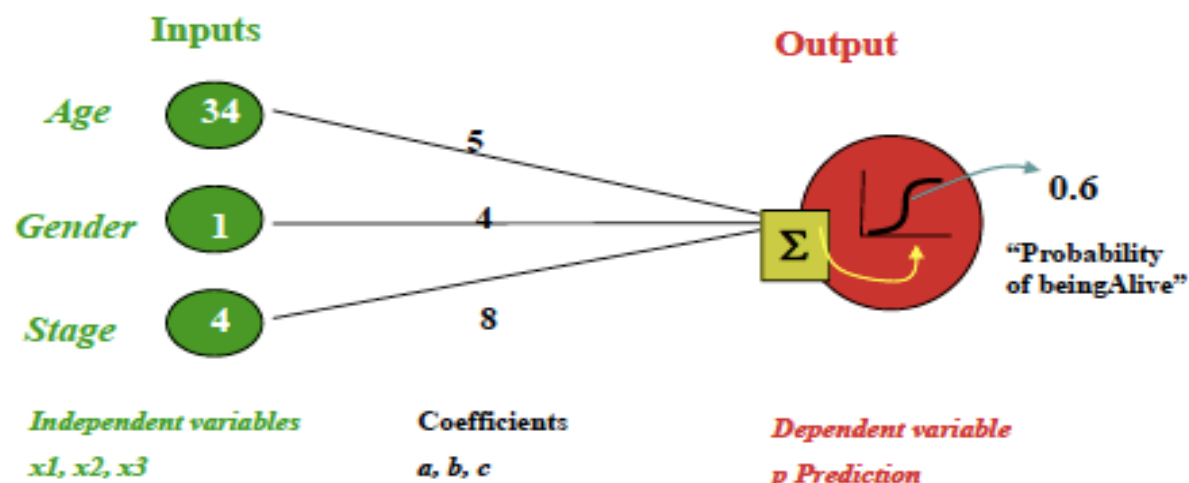
- Independent variable = input variable
- Dependent variable = output variable
- Coefficients = “weights”
- Estimates = “targets”

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## Logistic Regression Model (the sigmoid unit)

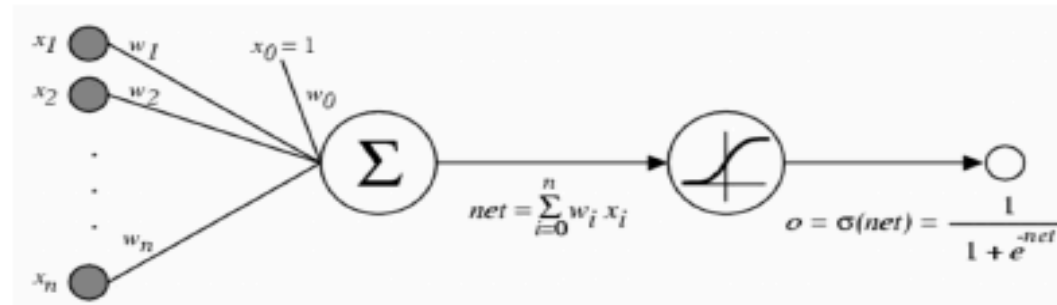


# A perceptron learning algorithm

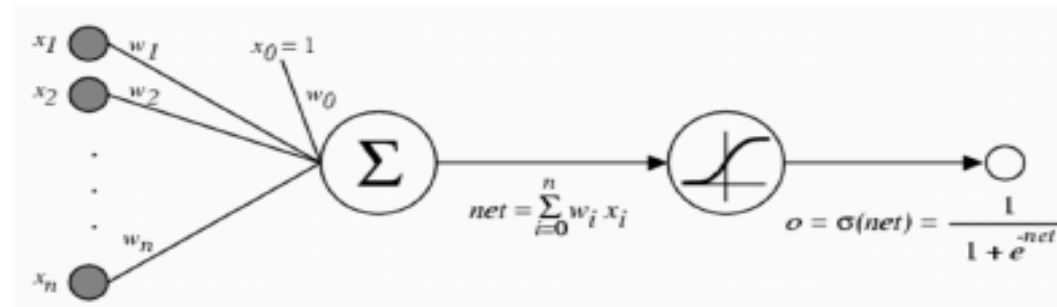
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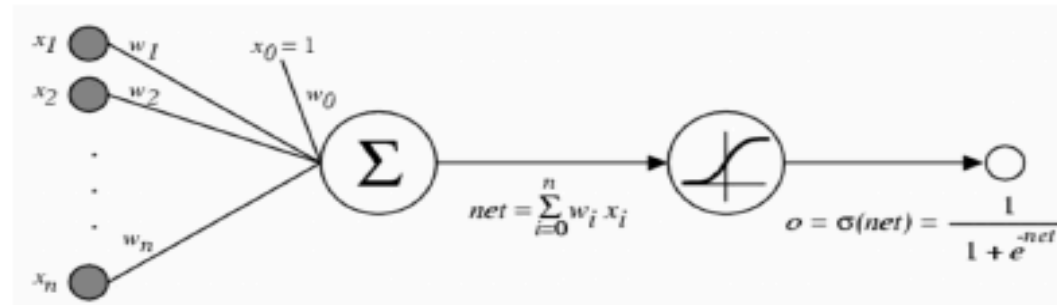


# A perceptron learning algorithm



- Recall the nice property of sigmoid function  $\frac{d\sigma}{dt} = \sigma(1 - \sigma)$
- Consider regression problem  $f: X \rightarrow Y$ , for scalar  $Y$ :  $y = f(x) + \epsilon$

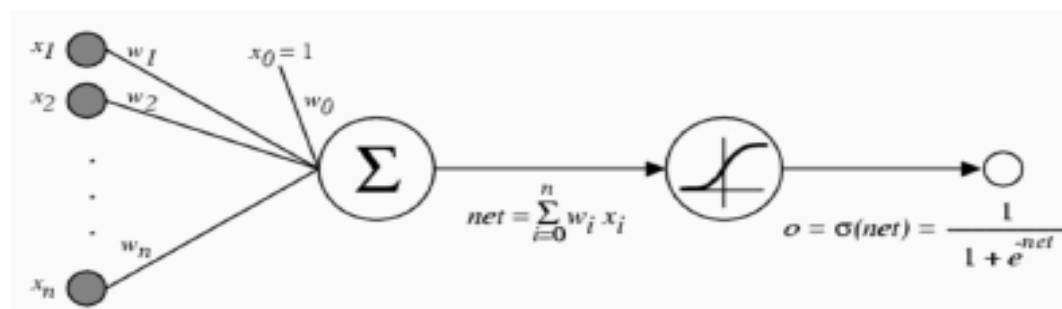
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- We used to maximize the conditional data likelihood

$$\vec{w} = \arg \max_{\vec{w}} \ln \prod_i P(y_i | x_i; \vec{w})$$

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- Here ...

$$\vec{w} = \arg \min_{\vec{w}} \sum_i \frac{1}{2} (y_i - \hat{f}(x_i; \vec{w}))^2$$

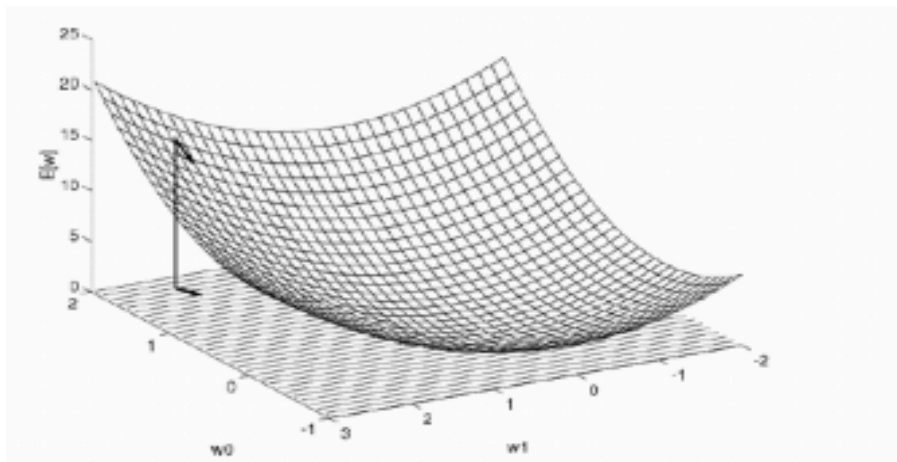
# Gradient Descent

$x_d$  = input

$t_d$  = target output

$o_d$  = observed unit  
output

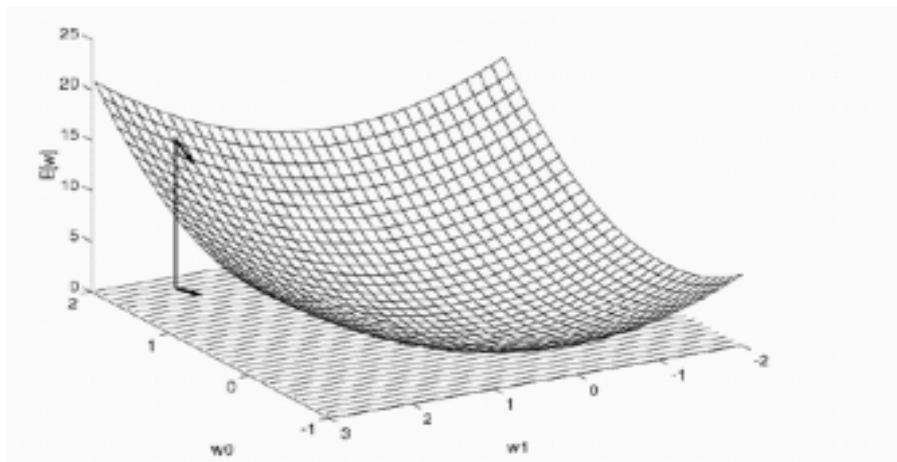
$w_i$  = weight  $i$





# Gradient Descent

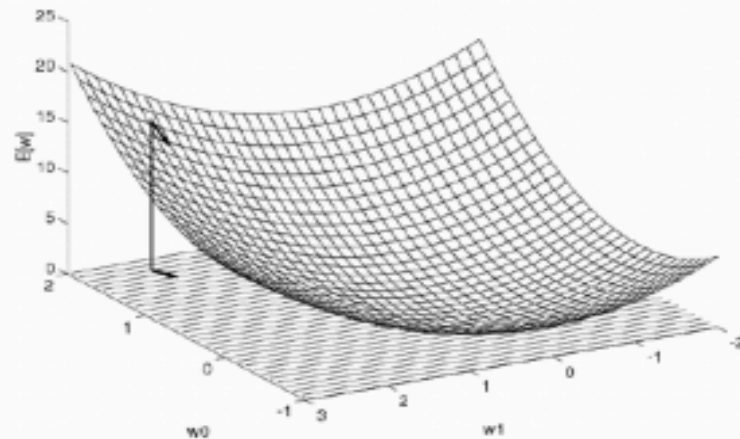
$x_d$  = input  
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$$\begin{aligned} \frac{\partial E[\vec{w}]}{\partial w_j} &= \frac{\partial}{\partial w_i} \frac{1}{2} \sum (t_d - o_d)^2 \\ &= \end{aligned}$$

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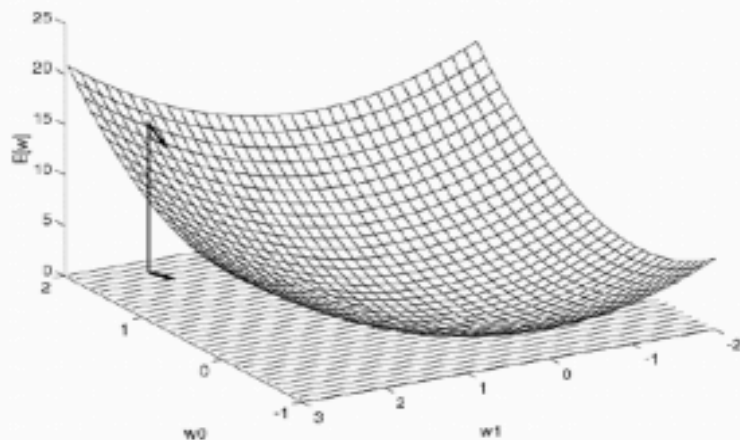
Gradient

$$\nabla E[\vec{w}] \equiv \left[ \frac{\partial E}{\partial w_0}, \frac{\partial E}{\partial w_1}, \dots, \frac{\partial E}{\partial w_n} \right]$$

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Gradient

$$\nabla E[\vec{w}] \equiv \left[ \frac{\partial E}{\partial w_0}, \frac{\partial E}{\partial w_1}, \dots, \frac{\partial E}{\partial w_n} \right]$$

Training rule:

$$\Delta \vec{w} = -\eta \nabla E[\vec{w}]$$

i.e.,

$$\Delta w_i = -\eta \frac{\partial E}{\partial w_i}$$

$$\begin{aligned} \frac{\partial E[\vec{w}]}{\partial w_j} &= \frac{\partial}{\partial w_i} \frac{1}{2} \sum (t_d - o_d)^2 \\ &= \end{aligned}$$

# The perceptron learning rules

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$x_d$  = input  
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 $w_i$  = weight i

$$\frac{\partial E_D(\vec{w})}{\partial w_j} = \frac{\partial}{\partial w_i} \frac{1}{2} \sum_d (t_d - o_d)^2$$

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**Batch mode:**

**Do until converge:**

1. compute gradient  $\nabla E_D[\vec{w}]$
2.  $\vec{w} = \vec{w} - \eta \nabla E_D[\vec{w}]$

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 &= \sum_d (t_d - o_d) \left( -\frac{\partial o_d}{\partial w_i} \right) \\
 &= - \sum_d (t_d - o_d) \frac{\partial o_d}{\partial net_i} \frac{\partial net_d}{\partial w_i} \\
 &= - \sum_d (t_d - o_d) o_d (1 - o_d) x_d^i
 \end{aligned}$$

**Batch mode:**

**Do until converge:**

1. compute gradient  $\nabla E_D[\vec{w}]$
2.  $\vec{w} = \vec{w} - \eta \nabla E_D[\vec{w}]$

**Incremental mode:**

**Do until converge:**

- For each training example  $d$  in  $D$

1. compute gradient  $\nabla E_d[\vec{w}]$
2.  $\vec{w} = \vec{w} - \eta \nabla E_d[\vec{w}]$

**where**

$$\nabla E_d[\vec{w}] = -(t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

# MLE vs MAP

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- Maximum conditional likelihood estimate

$$\vec{w} = \arg \max_{\vec{w}} \ln \prod_i P(y_i | x_i; \vec{w})$$

# MLE vs MAP

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$$\vec{w} = \arg \max_{\vec{w}} \ln \prod_i P(y_i | x_i; \vec{w})$$

$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

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$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

- Maximum a posteriori estimate

$$\vec{w} = \arg \max_{\vec{w}} \ln p(\vec{w}) \prod_i P(y_i | x_i; \vec{w})$$



# MLE vs MAP



- Maximum conditional likelihood estimate

$$\vec{w} = \arg \max_{\vec{w}} \ln \prod_i P(y_i | x_i; \vec{w})$$

$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

- Maximum a posteriori estimate

$$\vec{w} = \arg \max_{\vec{w}} \ln p(\vec{w}) \prod_i P(y_i | x_i; \vec{w})$$

$$\vec{w} \leftarrow \vec{w} + \eta \left( \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d - \lambda \vec{w} \right)$$

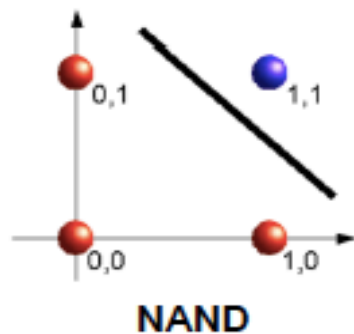
**Five mins break!**

**What decision surface does a  
perceptron define?**

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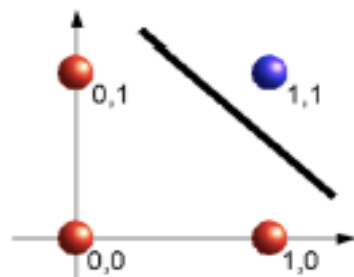


# What decision surface does a perceptron define?



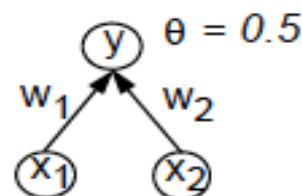
x	y	Z (color)
0	0	1
0	1	1
1	0	1
1	1	0

# What decision surface does a perceptron define?



NAND

x	y	Z (color)
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0	1	1
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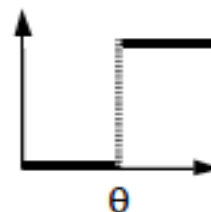
$$f(x_1w_1 + x_2w_2) = y$$

$$f(0w_1 + 0w_2) = 1$$

$$f(0w_1 + 1w_2) = 1$$

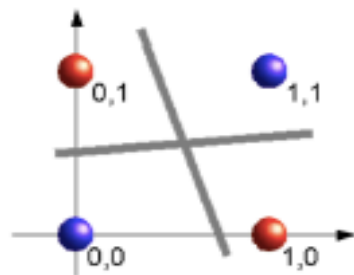
$$f(1w_1 + 0w_2) = 1$$

$$f(1w_1 + 1w_2) = 0$$



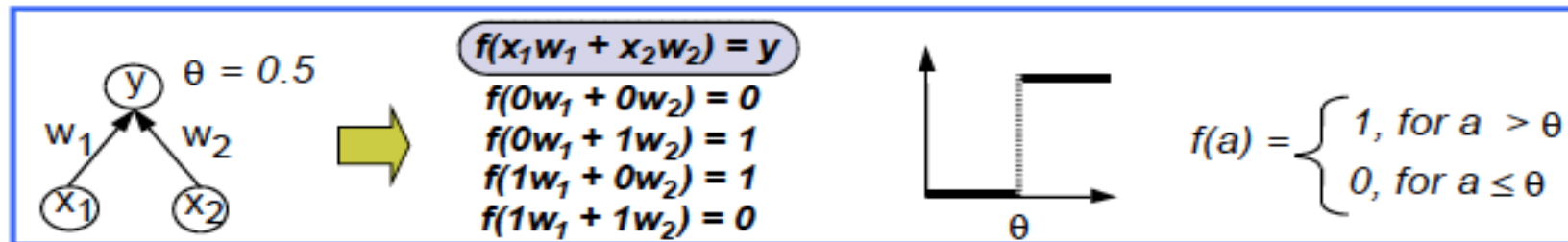
$$f(a) = \begin{cases} 1, & \text{for } a > \theta \\ 0, & \text{for } a \leq \theta \end{cases}$$

# What decision surface does a perceptron define?



NAND

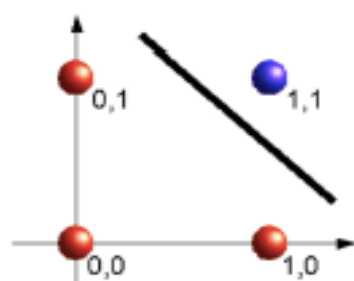
x	y	Z (color)
0	0	0
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some possible values for  $w_1$  and  $w_2$

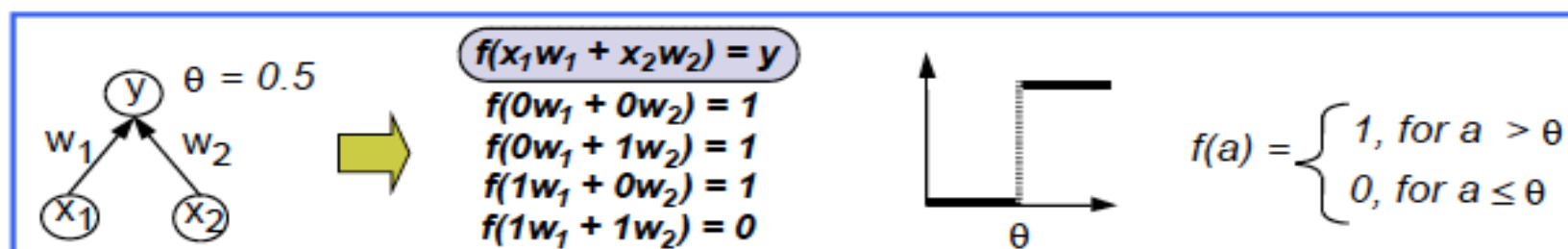
$w_1$	$w_2$

# What decision surface does a perceptron define?



NAND

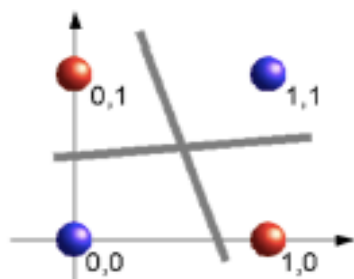
x	y	Z (color)
0	0	1
0	1	1
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some possible values for  $w_1$  and  $w_2$

$w_1$	$w_2$
0.20	0.35
0.20	0.40
0.25	0.30
0.40	0.20

# What decision surface does a perceptron define?

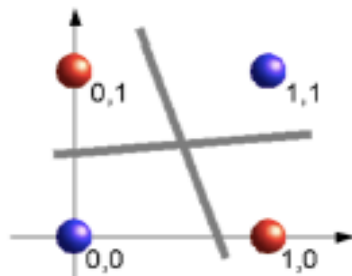


NAND

x	y	Z (color)
0	0	0
0	1	1
1	0	1
1	1	0

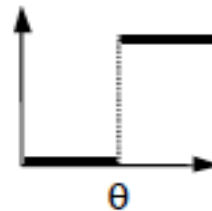
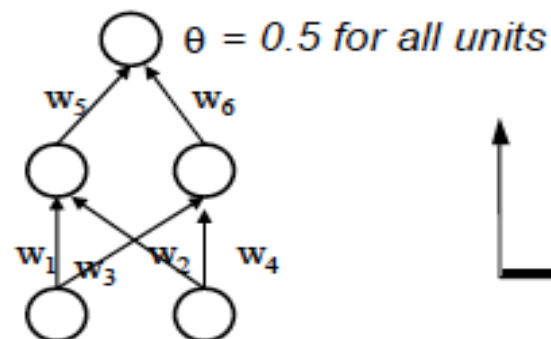


# What decision surface does a perceptron define?



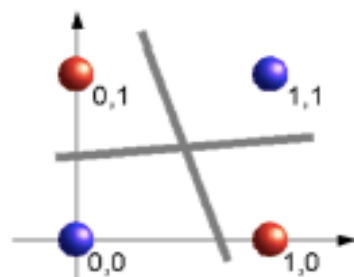
NAND

x	y	Z (color)
0	0	0
0	1	1
1	0	1
1	1	0



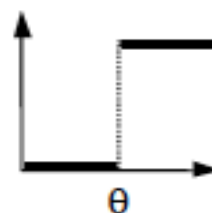
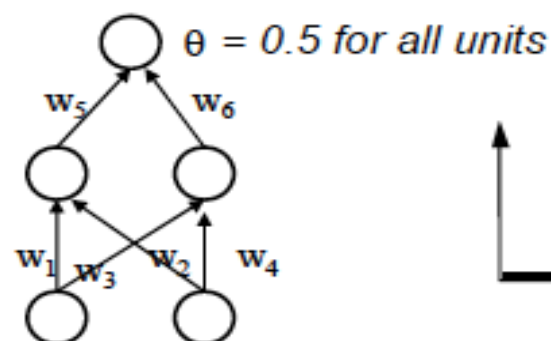
$$f(a) = \begin{cases} 1, & \text{for } a > \theta \\ 0, & \text{for } a \leq \theta \end{cases}$$

# What decision surface does a perceptron define?



NAND

x	y	Z (color)
0	0	0
0	1	1
1	0	1
1	1	0



$$f(a) = \begin{cases} 1, & \text{for } a > \theta \\ 0, & \text{for } a \leq \theta \end{cases}$$

a possible set of values for  $(w_1, w_2, w_3, w_4, w_5, w_6)$ :  
 $(0.6, -0.6, -0.7, 0.8, 1, 1)$

# Non Linear Separation

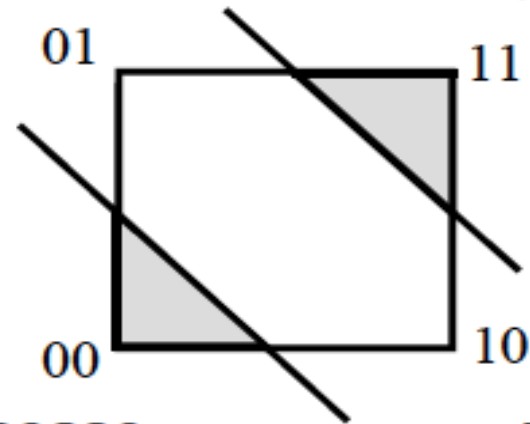


## Meningitis

No cough  
Headache

## Flu

Cough  
Headache



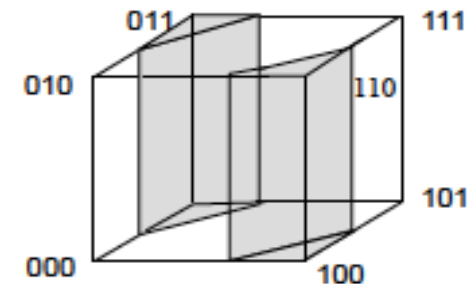
■ No treatment  
□ Treatment

## No disease

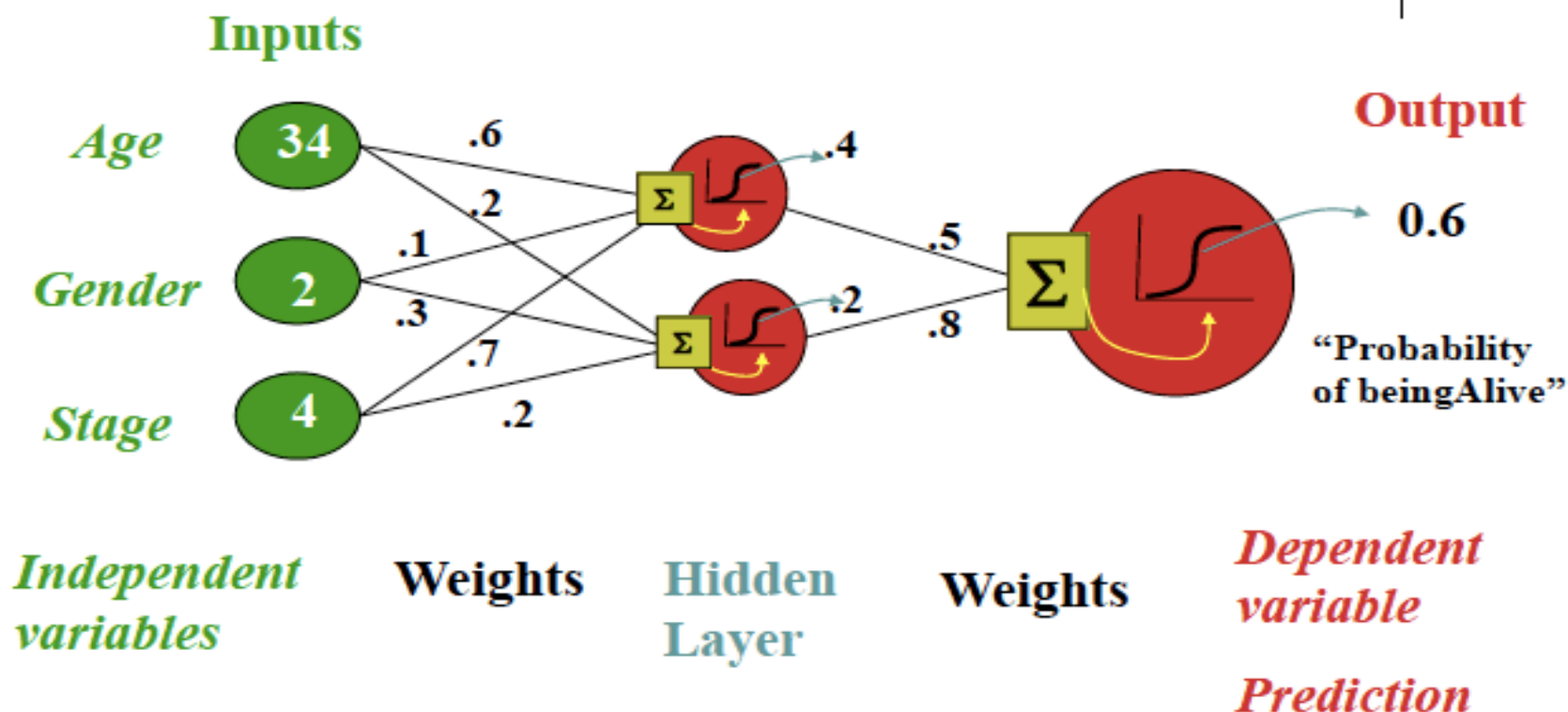
No cough  
No headache

## Pneumonia

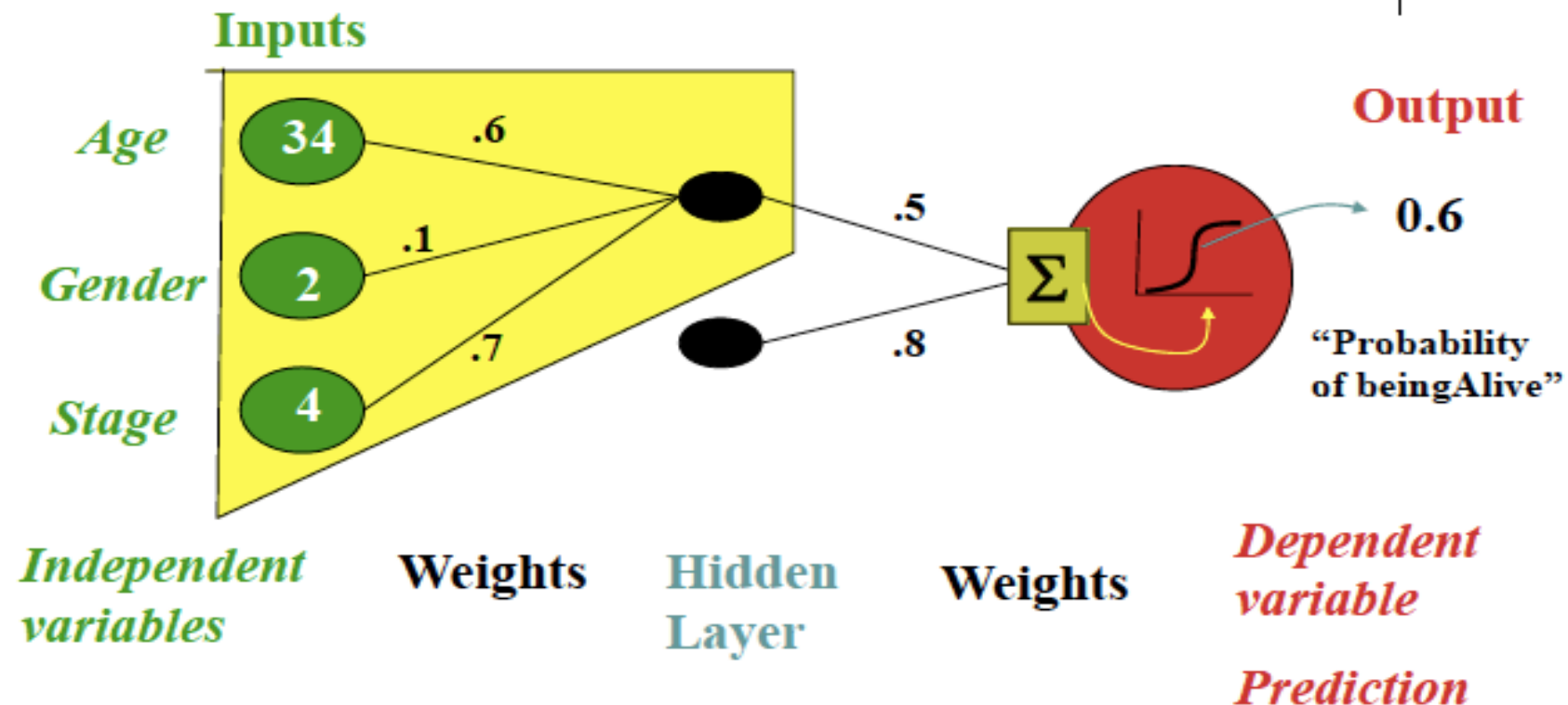
Cough  
No headache

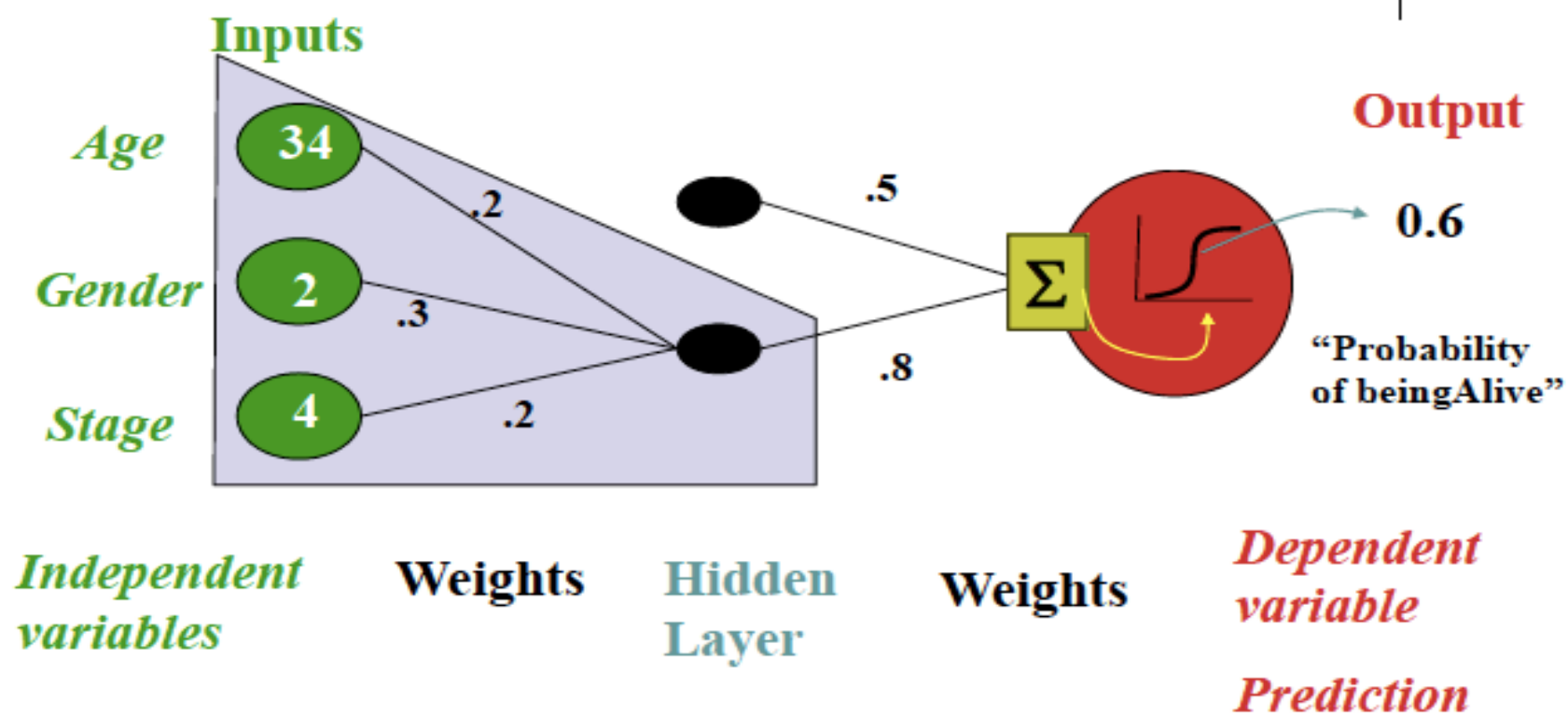


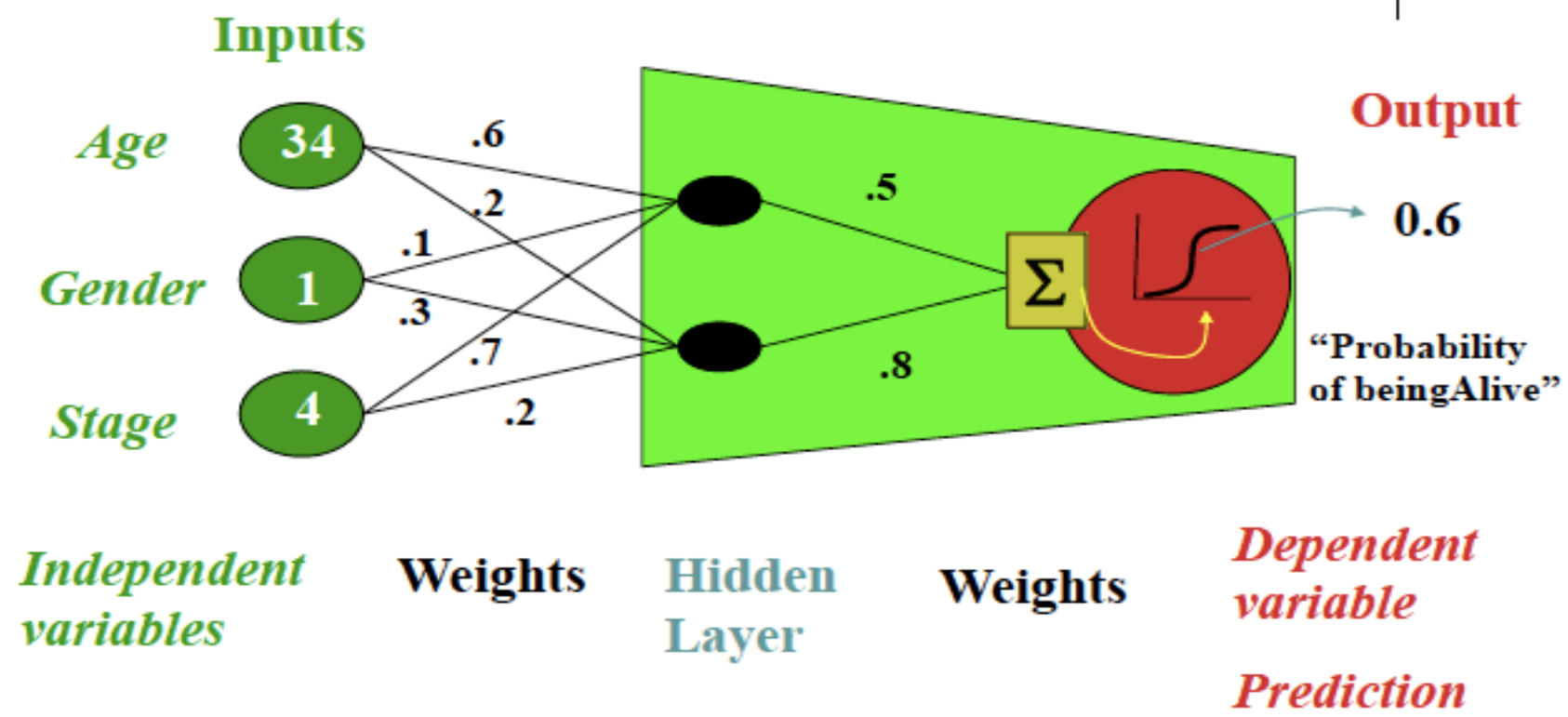
# Neural Network Model



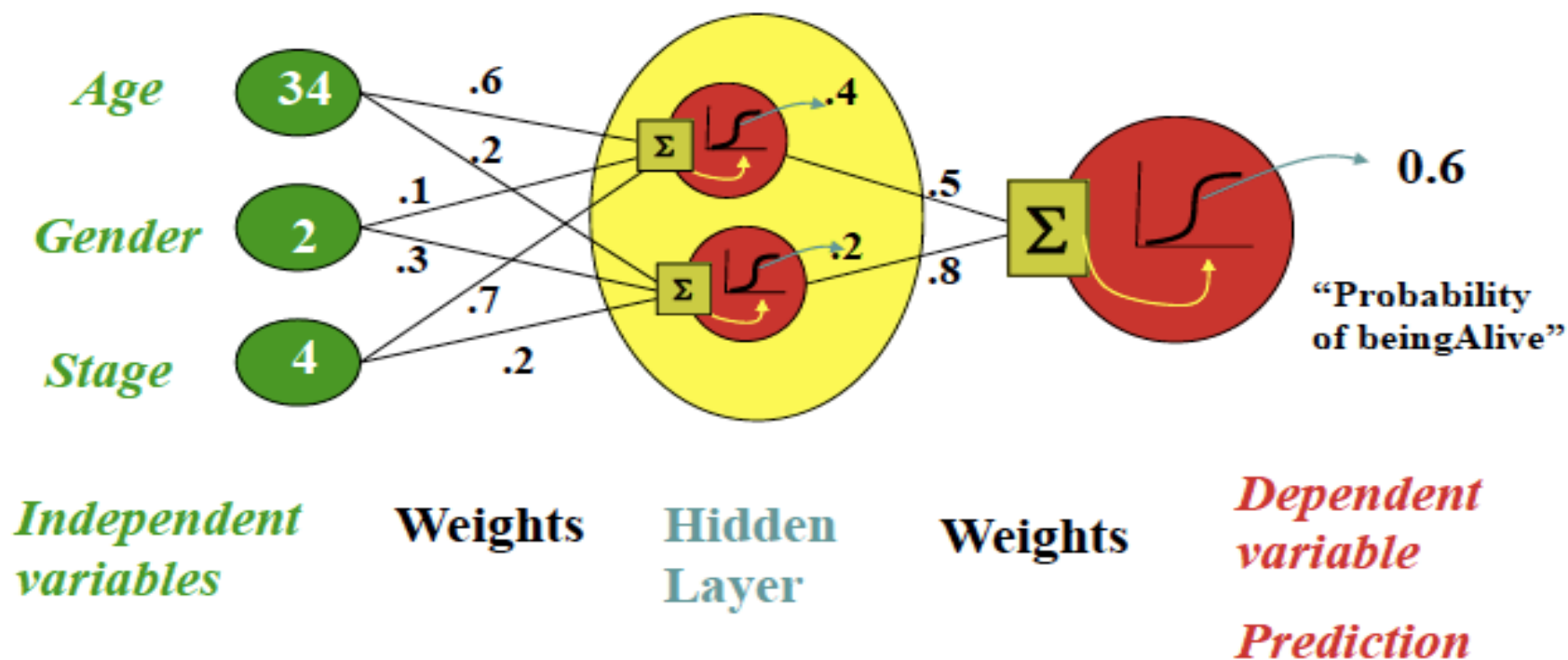
# “Combined logistic models”







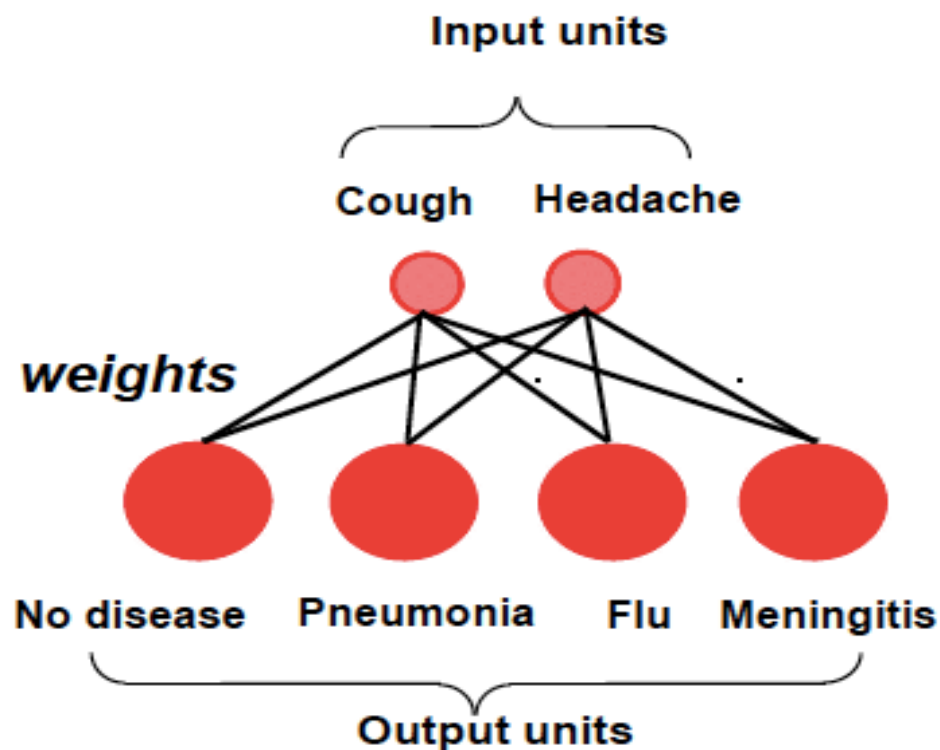
# Not really, no target for hidden units...





# Recall perceptrons

$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

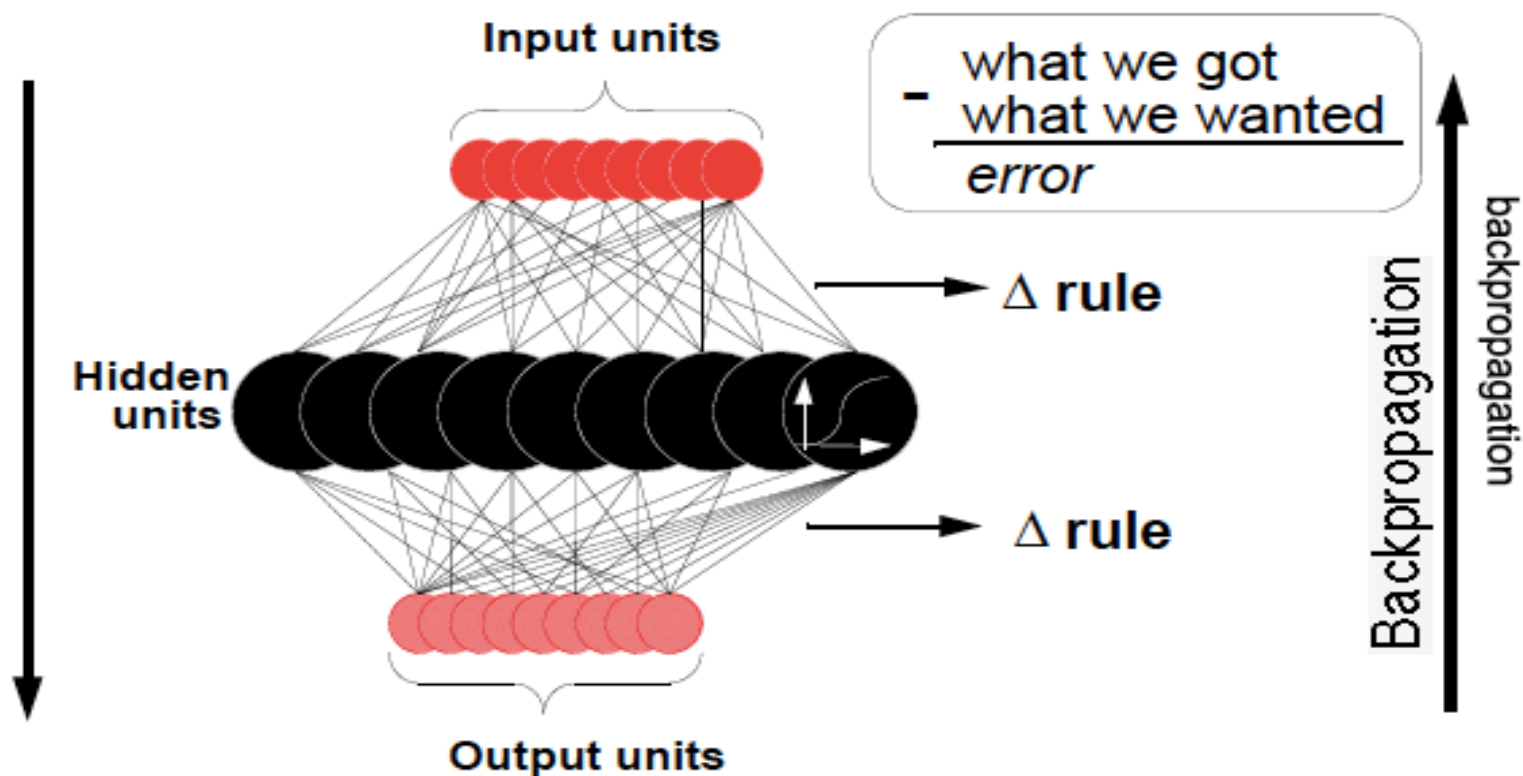


**$\Delta$  rule**

*change weights to  
decrease the error*

$$= \frac{\text{what we got} - \text{what we wanted}}{\text{error}}$$

# Hidden Units and Backpropagation



# Backpropagation Algorithm

---

$x_d$  = input  
 $t_d$  = target output  
 $o_d$  = observed unit  
output  
 $w_i$  = weight  $i$

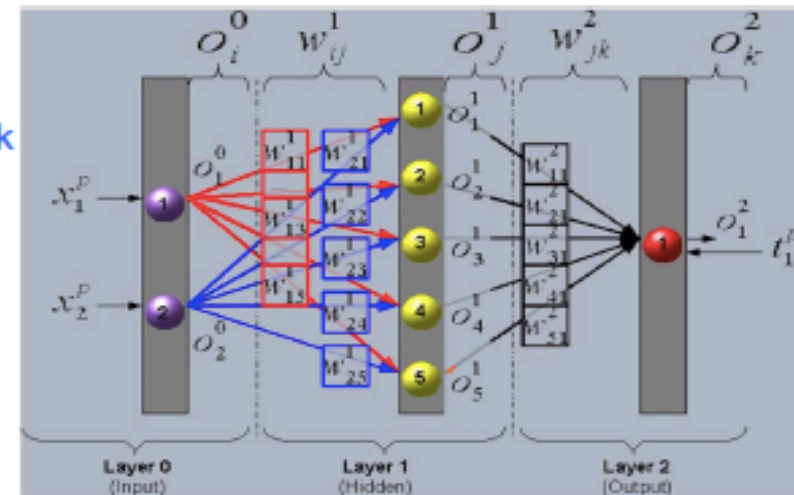
# Backpropagation Algorithm

$x_d$  = input  
 $t_d$  = target output  
 $o_d$  = observed unit output  
 $w_i$  = weight i

$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

- Initialize all weights to small random numbers
- Until convergence, Do

- Input the training example to the network and compute the network outputs



# Backpropagation Algorithm

$x_d$  = input  
 $t_d$  = target output  
 $o_d$  = observed unit  
 output  
 $w_i$  = weight i

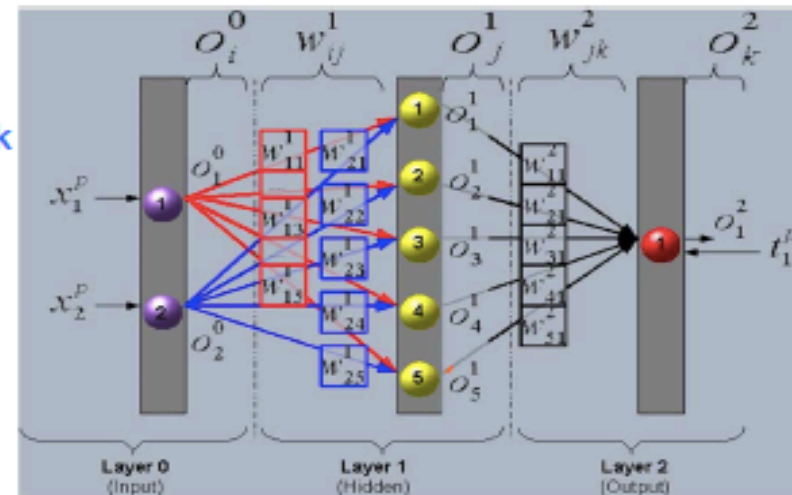
$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

- Initialize all weights to small random numbers
- Until convergence, Do

1. Input the training example to the network and compute the network outputs

1. For each output unit  $k$

$$\delta_k \leftarrow o_k^2 (1 - o_k^2) (t - o_k^2)$$



# Backpropagation Algorithm

$x_d$  = input  
 $t_d$  = target output  
 $o_d$  = observed unit output  
 $w_i$  = weight  $i$

$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

- Initialize all weights to small random numbers
- Until convergence, Do

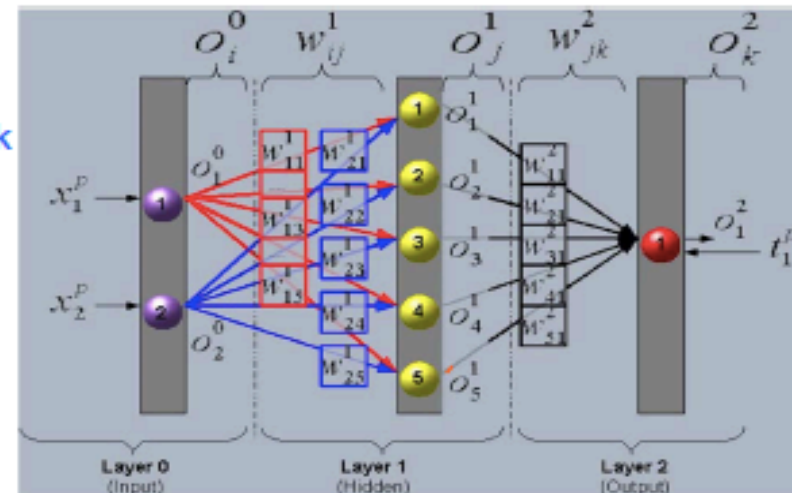
- Input the training example to the network and compute the network outputs

- For each output unit  $k$

$$\delta_k \leftarrow o_k^2 (1 - o_k^2) (t_k - o_k^2)$$

- For each hidden unit  $h$

$$\delta_h \leftarrow o_h^1 (1 - o_h^1) \sum_{k \in \text{outputs}} w_{h,k} \delta_k$$



# Backpropagation Algorithm

$x_d$  = input  
 $t_d$  = target output  
 $o_d$  = observed unit output  
 $w_i$  = weight i

$$\vec{w} \leftarrow \vec{w} + \eta \sum_d (t_d - o_d) o_d (1 - o_d) \vec{x}_d$$

- Initialize all weights to small random numbers
- Until convergence, Do

- Input the training example to the network and compute the network outputs

- For each output unit  $k$

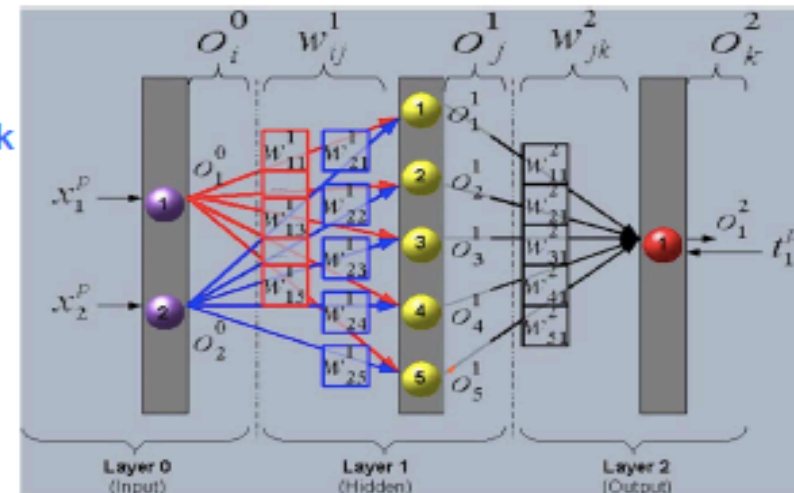
$$\delta_k \leftarrow o_k^2 (1 - o_k^2) (t_k - o_k^2)$$

- For each hidden unit  $h$

$$\delta_h \leftarrow o_h^1 (1 - o_h^1) \sum_{k \in \text{outputs}} w_{h,k} \delta_k$$

- Update each network weight  $w_{ij}$

$$w_{i,j} \leftarrow w_{i,j} + \Delta w_{i,j} \text{ where } \Delta w_{i,j} = \eta \delta_j x_i^j$$



# More on Backpropatation

---



- It is doing gradient descent over entire network weight vector
- Easily generalized to arbitrary directed graphs
- Will find a local, not necessarily global error minimum
  - In practice, often works well (can run multiple times)





## More on Backpropatation

---

- It is doing gradient descent over entire network weight vector
- Easily generalized to arbitrary directed graphs
- Will find a local, not necessarily global error minimum
  - In practice, often works well (can run multiple times)
- Often include weight *momentum*  $\alpha$

$$\Delta w_{i,j}(t) = \eta \delta_j x_{i,j} + \alpha \Delta w_{i,j}(t-1)$$

- Minimizes error over *training* examples
  - Will it generalize well to subsequent testing examples?
- Training can take thousands of iterations,  $\rightarrow$  very slow!
- Using network after training is very fast

# Artificial neural networks – what you should know

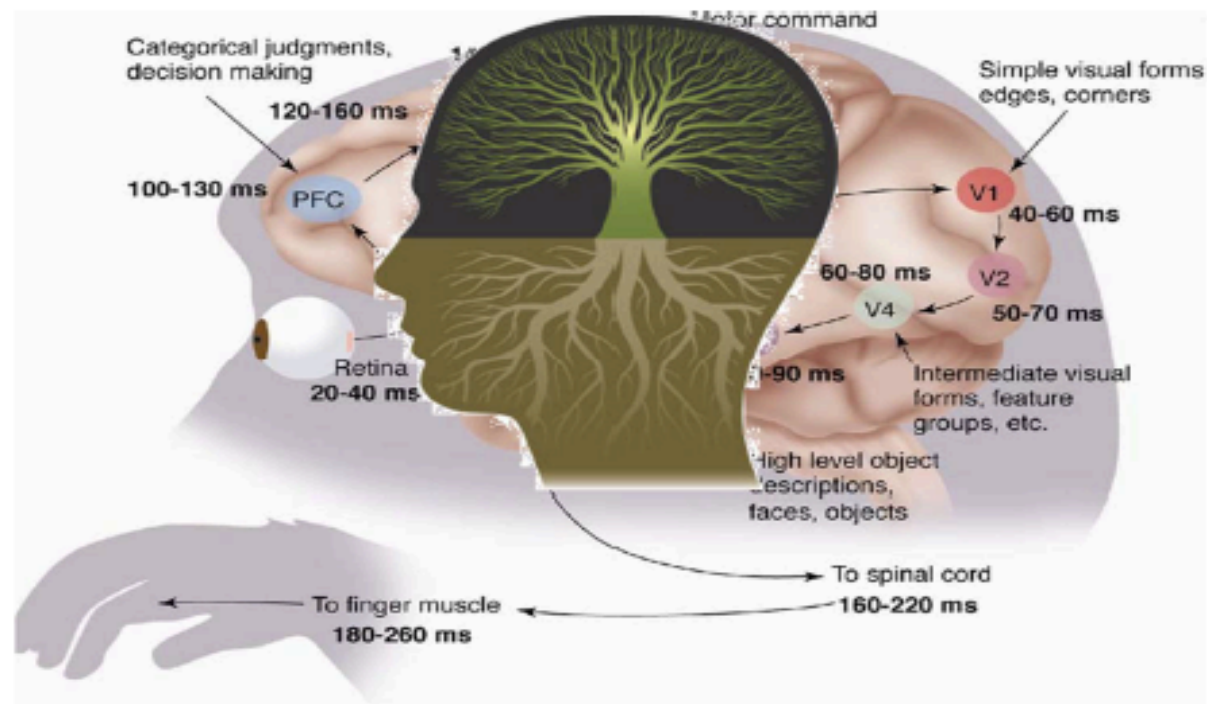
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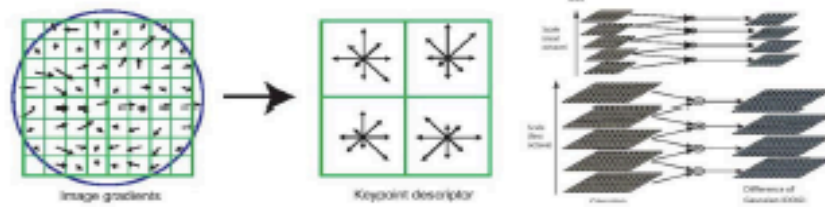
- Highly expressive non-linear functions
- Highly parallel network of logistic function units
- Minimizing sum of squared training errors
  - Gives MLE estimates of network weights if we assume zero mean Gaussian noise on output values
- Minimizing sum of sq errors plus weight squared (regularization)
  - MAP estimates assuming weight priors are zero mean Gaussian
- Gradient descent as training procedure
  - How to derive your own gradient descent procedure
- Discover useful representations at hidden units
- Local minima is greatest problem
- Overfitting, regularization, early stopping

**Five mins break!**

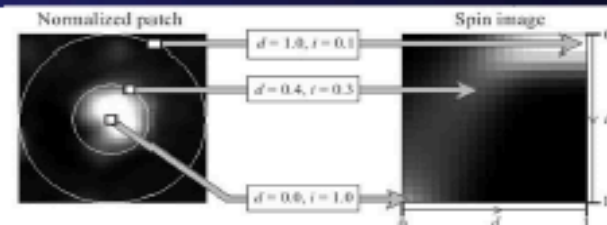
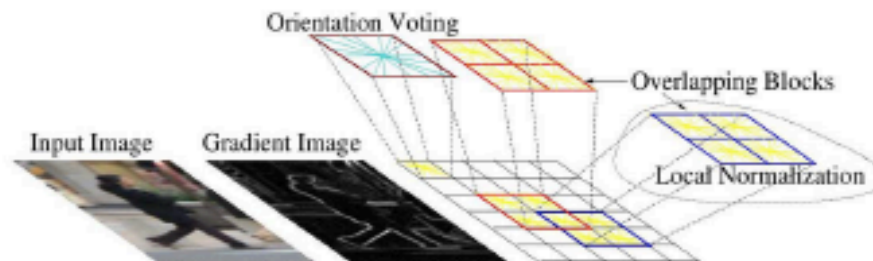
# Modern ANN topics: “Deep” Learning



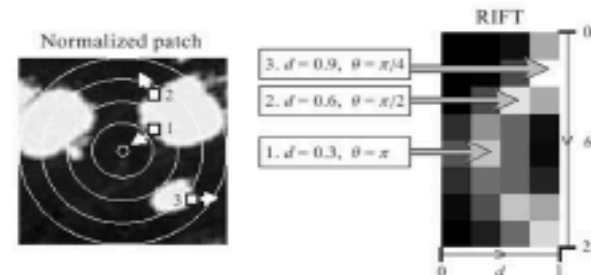
# Computer vision features



**SIFT**



**Spin image**



**Drawbacks of feature engineering**

1. Needs expert knowledge
2. Time consuming hand-tuning



(e)

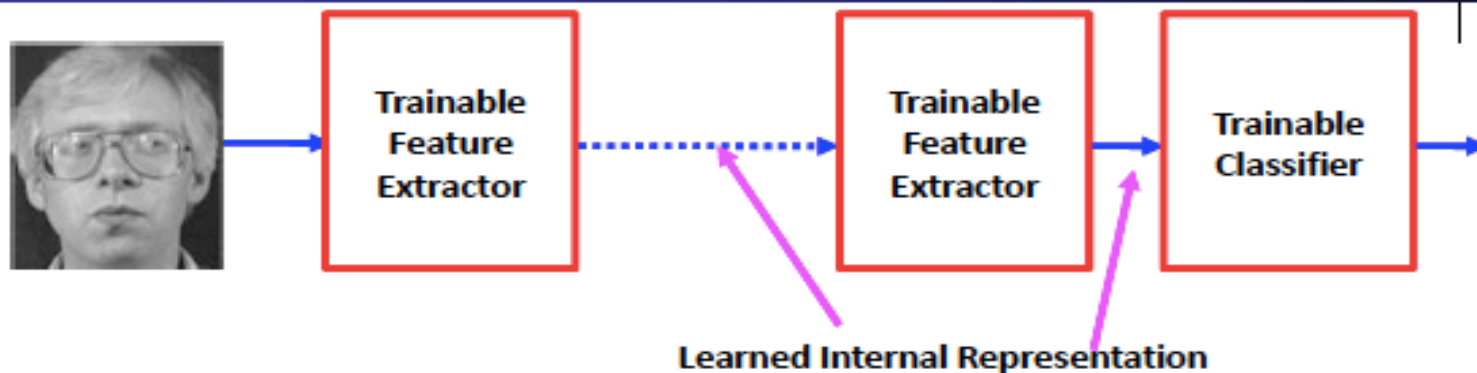
# Using ANN to hierarchical representation



## Good Representations are hierarchical

- **In Language: hierarchy in syntax and semantics**
  - Words->Parts of Speech->Sentences->Text
  - Objects,Actions,Attributes...-> Phrases -> Statements -> Stories
- **In Vision: part-whole hierarchy**
  - Pixels->Edges->Textons->Parts->Objects->Scenes

# “Deep” learning: learning hierarchical representations



- **Deep Learning:** learning a hierarchy of internal representations
- From low-level features to mid-level invariant representations, to object identities
- Representations are increasingly invariant as we go up the layers
- **using multiple stages gets around the specificity/invariance dilemma**

# “Deep” models

---



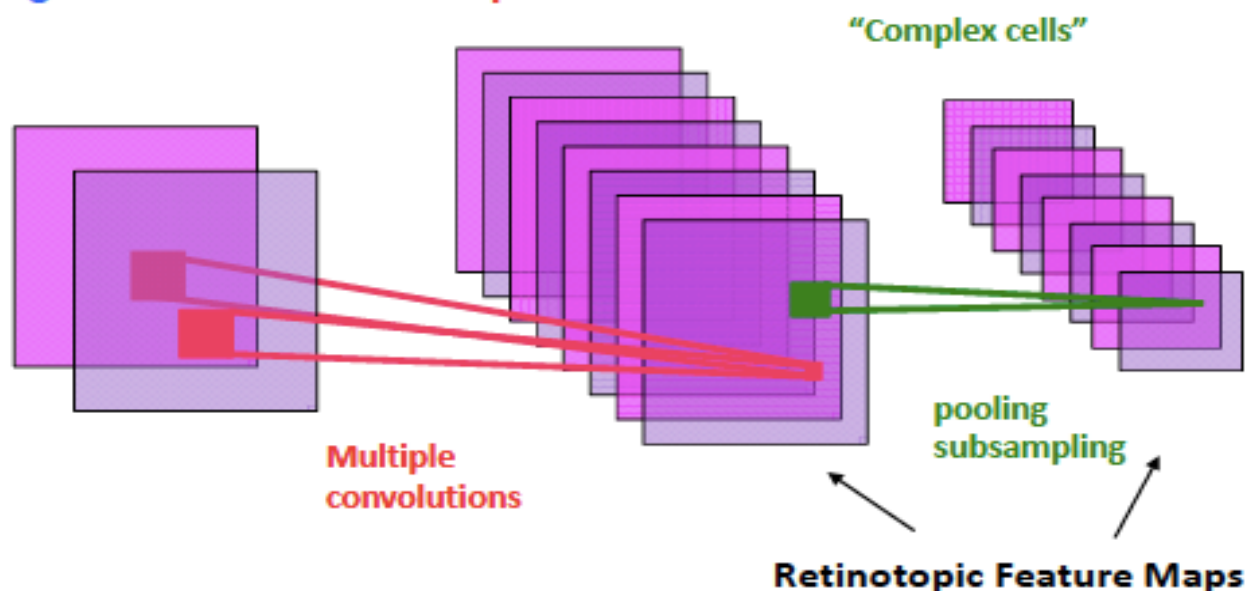
- Neural Networks: Feed-forward\*
  - You have seen it
- Autoencoders (multilayer neural net with target output = input)
  - Probabilistic -- Directed: PCA, Sparse Coding
  - Probabilistic -- Undirected: MRFs and RBMs\*
- Recursive Neural Networks\*
- Convolutional Neural Nets



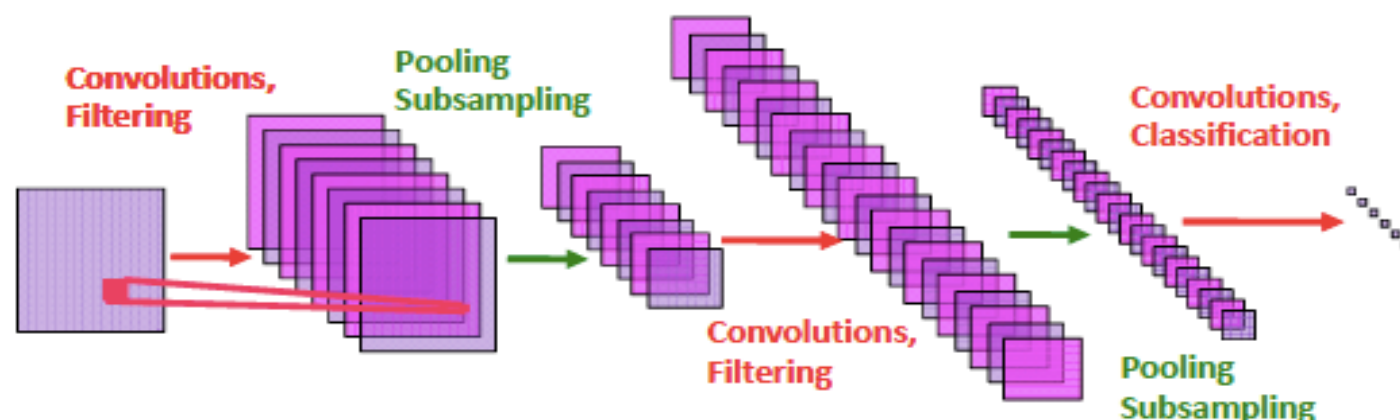
# Filtering + NonLinearity + Pooling = 1 stage of a Convolutional Net



- [Hubel & Wiesel 1962]:
  - **simple cells** detect local features
  - **complex cells** “pool” the outputs of simple cells within a retinotopic neighborhood.



# Convolutional Network: Multi-Stage Trainable Architecture



## • Hierarchical Architecture

- ▶ Representations are more global, more invariant, and more abstract as we go up the layers

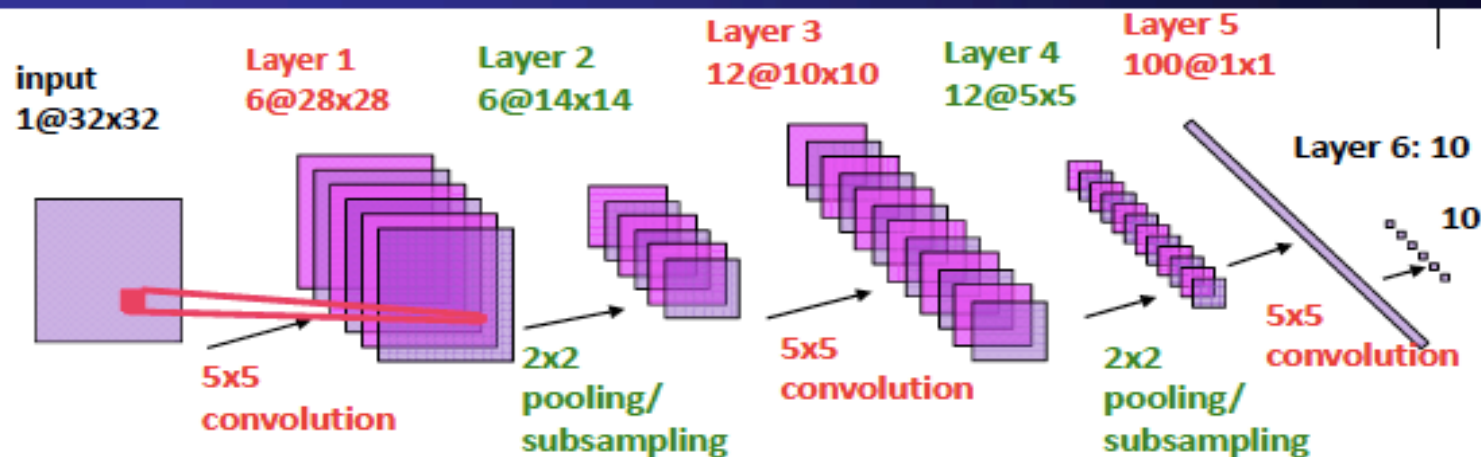
## • Alternated Layers of Filtering and Spatial Pooling

- ▶ Filtering detects conjunctions of features
- ▶ Pooling computes local disjunctions of features

## • Fully Trainable

- ▶ All the layers are trainable

# Convolutional Net Architecture for Hand-writing recognition



- Convolutional net for handwriting recognition (400,000 synapses)
  - Convolutional layers (simple cells): all units in a feature plane share the same weights
  - Pooling/subsampling layers (complex cells): for invariance to small distortions.
  - Supervised gradient-descent learning using back-propagation
  - The entire network is trained end-to-end. All the layers are trained simultaneously.
  - [LeCun et al. Proc IEEE, 1998]

# Application: MNIST Handwritten Digit Dataset



3 6 8 1 7 9 6 6 4 1  
6 7 5 7 8 6 3 4 8 5  
2 1 7 9 7 1 2 8 4 6  
4 8 1 9 0 1 8 8 9 4  
7 6 1 8 6 4 1 5 6 0  
7 5 9 2 6 6 8 1 9 7  
2 2 2 2 2 3 4 4 8 0  
0 2 3 8 0 7 3 8 5 7  
0 1 4 6 4 6 0 2 4 3  
7 1 2 8 1 6 9 8 6 1

0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1	1	1
2	2	2	2	2	2	2	2	2	2
3	3	3	3	3	3	3	3	3	3
4	4	4	4	4	4	4	4	4	4
5	5	5	5	5	5	5	5	5	5
6	6	6	6	6	6	6	6	6	6
7	7	7	7	7	7	7	7	7	7
8	8	8	8	8	8	8	8	8	8
9	9	9	9	9	9	9	9	9	9

Handwritten Digit Dataset MNIST: 60,000 training samples, 10,000 test samples

# Results on MNIST Handwritten Digits



CLASSIFIER	DEFORMATION	PREPROCESSING	ERROR (%)	Reference
linear classifier (1-layer NN)		none	12.00	LeCun et al. 1998
linear classifier (1-layer NN)		deskewing	8.40	LeCun et al. 1998
pairwise linear classifier		deskewing	7.80	LeCun et al. 1998
K-nearest-neighbors, (L2)		none	3.09	Kenneth Wilder, U. Chicago
K-nearest-neighbors, (L2)		deskewing	2.40	LeCun et al. 1998
K-nearest-neighbors, (L2)		deskew, clean, blur	1.80	Kenneth Wilder, U. Chicago
K-NN L3, 2 pixel jitter		deskew, clean, blur	1.22	Kenneth Wilder, U. Chicago
K-NN, shape context matching		shape context feature	0.83	Belongie et al. IEEE PAMI 2002
40 PCA + quadratic classifier		none	3.30	LeCun et al. 1998
1000 RBF + linear classifier		none	3.60	LeCun et al. 1998
K-NN, Tangent Distance		subsamp 16x16 pixels	1.10	LeCun et al. 1998
SVM, Gaussian Kernel		none	1.40	
SVM deg 4 polynomial		deskewing	1.10	LeCun et al. 1998
Reduced Set SVM deg 5 poly		deskewing	1.00	LeCun et al. 1998
Virtual SVM deg-9 poly	Affine	none	0.80	LeCun et al. 1998
V-SVM, 2-pixel jittered		none	0.68	DeCoste and Scholkopf, MLJ2002
V-SVM, 2-pixel jittered		deskewing	0.58	DeCoste and Scholkopf, MLJ2002
2-layer NN, 300 HU, MSE		none	4.70	LeCun et al. 1998
2-layer NN, 300 HU, MSE,	Affine	none	3.60	LeCun et al. 1998
2-layer NN, 300 HU		deskewing	1.60	LeCun et al. 1998
3-layer NN, 500+ 150 HU		none	2.95	LeCun et al. 1998
3-layer NN, 500+ 150 HU	Affine	none	2.45	LeCun et al. 1998
3-layer NN, 500+ 300 HU, CE, reg		none	1.53	Hinton, unpublished, 2005
2-layer NN, 800 HU, CE		none	1.60	Simard et al., ICDAR 2003
2-layer NN, 800 HU, CE	Affine	none	1.10	Simard et al., ICDAR 2003
2-layer NN, 800 HU, MSE	Elastic	none	0.90	Simard et al., ICDAR 2003
2-layer NN, 800 HU, CE	Elastic	none	0.70	Simard et al., ICDAR 2003
Convolutional net LeNet-1		subsamp 16x16 pixels	1.70	LeCun et al. 1998
Convolutional net LeNet-4		none	1.10	LeCun et al. 1998
Convolutional net LeNet-5,		none	0.95	LeCun et al. 1998
Conv. net LeNet-5,	Affine	none	0.80	LeCun et al. 1998
Boosted LeNet-4	Affine	none	0.70	LeCun et al. 1998
Conv. net, CE	Affine	none	0.60	Simard et al., ICDAR 2003
Conv net, CE	Elastic	none	0.40	Simard et al., ICDAR 2003

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# Weaknesses & Criticisms

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- Learning everything. Better to encode prior knowledge about structure of images.
- Not clear if an explicit global objective is indeed optimized, making theoretical analysis difficult
  - Many (arbitrary) approximations are introduced
  - Many different loss functions, gate functions, transformation functions are used
  - Many different implementation exist
- Comparison is based on the end empirical results on downstream task, not the actual direct task DNN is designed to compute, make verification and tuning of components of DNN very hard.

**That's all!**