1 amu = 931.50 MeV/c² Particle rest masses: Electron 5.486 x 10 $^{-4}$ u Proton 1.007276 u Neutron 1.008665 u

- 1. Which of the following reactions is forbidden because it would involve the non-conservation of charge?
 - (a) $p+p \rightarrow p+p+\pi^0$
 - (b) $p + p \to p + p + \pi^{+} + \pi^{-}$
 - (c) $p + p \rightarrow p + p + \pi^{+} + \pi^{-} + \pi^{+}$
- 2. Which of the following reactions is forbidden because baryon number is not conserved?
 - (a) $p + p \rightarrow \pi^+ + p + n$
 - (b) $p+p \rightarrow \pi^+ + p + n + n$
 - (c) $p + p \rightarrow p + p + \pi^{0} + \pi^{0}$
- 3. Why is the decay $\Lambda^0 \rightarrow p + \pi^- + \pi^0$ forbidden?
- 4. The strong interaction conserves quark flavour. Analyse each of the following strong interactions in terms of their constituent quarks and confirm that quark flavour is conserved.
 - (a) $\pi^- + p \rightarrow K^0 + \Lambda^0$
 - (b) $\pi^+ + p \rightarrow K^+ + \Sigma^+$
- 5. An electron-positron pair bound by their Coulomb attraction is called *positronium*. Show that when positronium decays from rest to two photons, the photons have equal energy. What is the wavelength of each photon?

 $[2.42 \times 10^{-12} \,\mathrm{m}]$

- 6. Find:
 - (a) An *approximate* expression for the mass of a nucleus of mass number A.
 - (b) An expression for the volume of the nucleus in terms of A.
 - (c) An estimate of the nuclear density (in kg m⁻³).

 $[3 \times 10^{17} \text{ kg m}^{-3}]$

- 7. The compressed core of a star formed in the wake of a supernova explosion can consist of pure nuclear material (neutrons) and is called a pulsar or neutron star. Use the result from 6(c) to calculate the mass of a sugar lump sized piece of neutron star.
- 8. $\frac{60}{28}$ *Ni* has an atomic mass of 59.930789u.
 - (a) What is its nuclear mass?
 - (b) What is the binding energy per nucleon?

[59.9154u; 8.78MeV]

- 9. Which of the pair of nuclei, ${}^{41}_{20}$ Ca and ${}^{41}_{19}$ K is unstable with respect to the other (atomic masses 40.962278u and 40.961825u)? What decay mode/modes are possible and how much energy is released in each allowed mode?
- 10. (a) Show that ${}^{8}_{4}$ Be can decay into two α particles with an energy release of 0.1 MeV, but that ${}^{12}_{6}$ C cannot decay into three α particles.
 - (b) Find the energy released in the following reaction (including the energy of the photon):

$$_{1}^{2}H + _{2}^{4}He \rightarrow _{3}^{6}Li + \gamma$$
.

Binding energies: ${}^{8}_{4}Be = 56.50 \text{MeV}$; ${}^{12}_{6}C = 92.16 \text{MeV}$; ${}^{2}_{1}H = 2.22 \text{MeV}$; ${}^{4}_{2}He = 28.30 \text{MeV}$ and ${}^{6}_{3}Li = 31.99 \text{MeV}$.

[1.47MeV]

11. Two Th isotopes, $^{224}_{90}$ Th and $^{230}_{90}$ Th, decay by emitting α particles with energies of 7.31 MeV and 4.77MeV respectively. For each isotope calculate the range r_c at which the α particle leaves the Coulomb potential barrier. Estimate the ratio of the half lives for these two isotopes.

(this last question is optional, but a good practice of what we saw in the lectures)