



Thermodynamic potentials

Maxwell relations

Internal energy U

$$dU = TdS - pdV$$

$$U = U(S, V)$$

$$dU = \left(\frac{\partial U}{\partial S} \right)_V dS + \left(\frac{\partial U}{\partial V} \right)_S dV$$

$$T = \left(\frac{\partial U}{\partial S} \right)_V \text{ and } -p = \left(\frac{\partial U}{\partial V} \right)_S$$

$$\left(\frac{\partial T}{\partial V} \right)_S = - \left(\frac{\partial p}{\partial S} \right)_V \quad \text{Maxwell Relat}^o$$

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recommend to have on  
the cheat sheet

# Enthalpy $H$

$$H \equiv U + pV$$

$$dH = dU + pdV + Vdp = TdS + Vdp$$

$$dU = TdS - pdV$$

$$H = H(S, p)$$

$$dH = \left( \frac{\partial H}{\partial S} \right)_p dS + \left( \frac{\partial H}{\partial p} \right)_S dp$$

$$T = \left( \frac{\partial H}{\partial S} \right)_p \text{ and } V = \left( \frac{\partial H}{\partial p} \right)_S$$

$$\left( \frac{\partial T}{\partial p} \right)_S = \left( \frac{\partial V}{\partial S} \right)_p$$

# Helmholtz Free Energy $F$

$$F \equiv U - TS$$

$$dF = dU - TdS - SdT = -SdT - pdV$$

$$dU = TdS - pdV$$

$$F = F(T, V)$$

$$dF = \left( \frac{\partial F}{\partial T} \right)_V dT + \left( \frac{\partial F}{\partial V} \right)_T dV$$

$$-S = \left( \frac{\partial F}{\partial T} \right)_V \text{ and } -p = \left( \frac{\partial F}{\partial V} \right)_T$$

$$\left( \frac{\partial S}{\partial V} \right)_T = \left( \frac{\partial p}{\partial T} \right)_V$$

# Gibbs Free Energy $G$

$$G \equiv H - TS = U + pV - TS$$

$$dG = dH - TdS - SdT = dU + pdV + Vdp - TdS - SdT$$

$$dU = TdS - pdV$$

$$dG = -SdT + Vdp$$

$$G = G(T, p)$$

$$dG = \left( \frac{\partial G}{\partial T} \right)_p dT + \left( \frac{\partial G}{\partial p} \right)_T dp$$

$$-S = \left( \frac{\partial G}{\partial T} \right)_p \text{ and } V = \left( \frac{\partial G}{\partial p} \right)_T$$

$$\left( \frac{\partial S}{\partial p} \right)_T = - \left( \frac{\partial V}{\partial T} \right)_p$$

# Summary

$$dU = TdS - pdV$$

$$dH = TdS + Vdp$$

$$dF = -SdT - pdV$$

$$dG = -SdT + Vdp$$

# Summary 2

$$dU \rightarrow \left( \frac{\partial T}{\partial V} \right)_S = - \left( \frac{\partial p}{\partial S} \right)_V$$

$$dH \rightarrow \left( \frac{\partial T}{\partial p} \right)_S = \left( \frac{\partial V}{\partial S} \right)_p$$

$$dF \rightarrow \left( \frac{\partial p}{\partial T} \right)_V = \left( \frac{\partial S}{\partial V} \right)_T$$

$$dG \rightarrow \left( \frac{\partial V}{\partial T} \right)_p = - \left( \frac{\partial S}{\partial p} \right)_T$$