Homework 1

T1

Adapted from P20 1.5

Say we had a "black box," which takes two numbers as input and outputs their sum. See Figure 1.10a.

Say we had another box capable of multiplying two numbers together. See Figure 1.10b.

We can connect these boxes together to calculate $p \times (m + n)$. See Figure 1.10c.

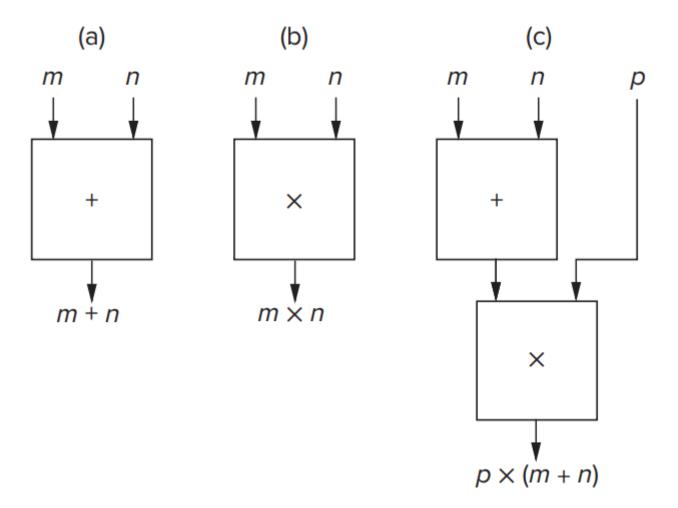


Figure 1.10 from page 20

Assume we have an unlimited number of these boxes. Show how to connect them together to calculate:

- a. ax + b
- b. The average of the four input numbers w, x, y, and z
- c. x^2-y^2
- d. a^6

T2

- (1) Convert these decimal numbers to eight-bit 2's complement binary numbers.
- a. 98
- b. -105
- (2) Convert the following eight-bit 2's complement binary numbers to decimal.
- c. 01000010
- d. 11101111

T3

Add the following 2's complement binary numbers. Also express the answer in **decimal**.

0924更改:每个数字都是完整独立的补码。

- a. 01 + 110011
- b. 111 + 0100110
- c. 1010 + 1101
- d. 0001 + 1110

T4

Without changing their values, convert the following 2's complement binary numbers into **eight-bit** 2's complement numbers.

a. 101011

- b. 011110
- c. 11111111110000
- d. 00001

T5

Write IEEE floating point representation of $(4.3)_D$. If you cannot represent accurately, please try to represent a number which has the closest difference to $(4.3)_D$. (Actually you may just write the first ten digits of the fractional part.)

Can you try to write code in C language to confirm your correctness? (Tips: type float in C language follows the rule of IEEE floating) (0924更改: 代码提示在git上)

What if the exponent bits are all 1? Search for information about that.

T6

Write the decimal quivalents for the IEEE floating point number below.

0 10001001 11111001101001000000000

T7

- (1) Compute the following. Write answers in binary.
- a. 10100101 AND 11010101
- b. 10001110 OR 11110101
- c. NOT(11110001) OR NOT(01011010)
- (2) Compute the following. Write answers in hexadecimal.
- d. (x1234 AND X5678) OR (xABCD AND X99EF)
- e. x6A12 XOR x3A15

Fill in the truth table for the equations given

$$Q_1 = (A \ AND \ B) \ OR \ NOT(C)$$

 $Q_2 = NOT(NOT(A) \ OR \ NOT(B)) \ AND \ C$

Express Q2 another way (contains only AND)

T9

Steps to convert ASCII string to base64:

- 1. Write the ASCII string as bit stream.
- 2. Divide each 24 bits into one group. In each group, divide the bits into 4 subgroups and convert each subgroup using the following rule:
 - 0-25 corresponds to A-Z
 - 26-51 corresponds to a-z
 - 52-61 corresponds to 0-9
 - 62 corresponds to + and 63 corresponds to /.
- 3. If the subgroup is less than 6 bits, add 0 to its lower position.
- 4. If the last group is 8 bits, add "==" to the end of the encoded string. If the last subgroup is 16 bits, add just one "=".

For example, in order to convert "M", first write it as binary:01001101. The first subgroup is 010011(19), corresponds to "T". Thelast subgroup is 010000(added 4 zeros), corresponds to "Q" (16). Since the last package is 8 bits, we should add "==" at the end of the encoded string to indicate this. The final base64 encoding is "TQ==".

(1) Convert ASCII string "\t\n\r" to base64.

0924更改:当转义字符使用。另外,题目描述中group和package应该是一个东西。

(2) Write a scenario where base64 encoding can be used.

T10

What is the largest positive number that can be represented by an IEEE floating point number (Normalized Form).

T11

Consider the situation: We want to calculate 0.11×0.022 ; however, we can only calculate integer numbers. How can we do that?

Obvioulsy we can calculate 11×22 and add dot to the number. However, to determine where to put the dot may be difficult. If we can easily transform the value into 1.1×10^{-1} and 2.2×10^{-2} , just calculate 1.1×1.1 and $10^{-1} \times 10^{-2}$ (just add -1 and -2), then put them together. However, 0.95×0.081 makes difference, for $9.5 \times 8.1 = 76.95$, which is greater than 10. So we may convert 76.95 into 7.695×10^1 and adjust the exponent by increasing 1. So the answer is $7.695 \times 10^1 \times 10^{-3} = 7.695 \times 10^{-2}$.

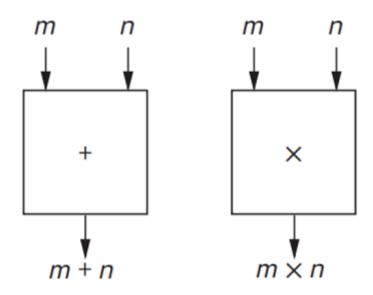
Now we have two positive float numbers A and B, they follow the rule of 32bit IEEE floating point. For simplicity, we can use A[0] as the lowest bit of A, A[31] as the highest, and A[2:5] as array of A[4], A[3] and A[2], A[5] is not included. If we attempt to combine two numbers together, we can use big brackets.

For example: if A=0 11110000 00000000 00000000 0000111, then A[0]=1, A[31]=0, and A[2:5]=001, $\{101,A[2:5]\}=101001$, array in order that high bits are on the left.

- We're required to multiply A and B, result as C; please represent one possible algorithm in the format of "Black Box" same as T1.
 - We assume that 1 < A, B < 100;
 - If you want to multiply two unsigned numbers, we have given you mult boxs which apply to two unsigned integers of 24 bits, give the output in 48 bits.

For example, if input numbers are in two bits, like 10 and 11, then the output is 0110; and input 11 and 11 makes 1001. 24-bit inputs are similar.

Also, you can also use add boxes of any bits



- o You can also use a selector box, which takes 3 inputs, a, b, and sel
 - if sel == 0, output = a
 - if sel == 1, output = b

0924更改:可以自行设计使用减法器,与加法器类似。提示:只需要一个 selector box 元件。

• How about addition? Also assume 1 < A, B < 100. You can use Shift Left or Shift Right if you want. You're encouraged to challenge yourself.

0924更改:假设A>=B以简化答案;另外,可以写流程图。第二问写不出来没有影响。提示:只需要一个 selector box 元件。