

Homework1 Answer

T1

略

T2

$$\begin{aligned}98 &\rightarrow 01100010 \\ -105 &\rightarrow 11101001 \rightarrow 10010110 \rightarrow 10010111 \\ &\quad 01000010 \rightarrow 66 \\ 11101111 &\rightarrow 10010000 \rightarrow 10010001 \rightarrow -17\end{aligned}$$

T3

$$a. 01 + 11_0011 = 00_0001 + 11_0011 = 11_0100 = (-12)_D$$

$$b. 111 + 010_0110 = 111_1111 + 010_0110 = 010_0101 = (37)_D$$

$$c. 1010 + 1101 = 0111 = (7)_D$$

$$d. 0001 + 1110 = (-1)_D$$

T4

$$a. 1110_1011$$

$$b. 0001_1110$$

$$c. 1111_0000$$

$$d. 0000_0001$$

T5

$$4.3 = 100.01_0011_0011 \cdots = (1.0001\ 0011\ 0011 \cdots) \times 2^2$$

0 10000001 00010011001100110011010 (注意末尾两位) (注: 由于题目没说清楚, 所以只写10位的也算对)

示例代码:

```
#include <stdio.h>

union my_union {
    int a;
    float b;
};

int main() {
    union my_union t;
    t.b = 4.3;
    for (int loop = 31; loop >= 0; loop--) {
        putchar((t.a & (1 << loop)) == 0 ? '0' : '1');
    }
    return 0;
}
```

阶码全为1, 当尾数全为1时表示无穷, 正负号由符号位决定。阶码全为1且尾数不全为0则表示NaN

T6

10001001 = 137

$$(1.111110011010010000000000) \times 2^{137-127} = 111_1110_0110.1001 = 2022.5625 = 2022\frac{9}{16}$$

T7

a. 1010_0101 AND 1101_0101 = 1000_0101

b. 1000_1110 OR 1111_0101 = 1111_1111

c. NOT(1111_0001) OR NOT(0101_1010) = 0000_1110 OR 1010_0101 = 1010_1111

d. (x1234 AND X5678) OR (xABCD AND X99EF) = x1230 OR x89CD = x9BFD

e. x6A12 XOR x3A15 = x5007

T8

A	B	C	Q_1	Q_2
0	0	0	1	0
0	0	1	0	0
0	1	0	1	0
0	1	1	0	0
1	0	0	1	0
1	0	1	0	0
1	1	0	1	0
1	1	1	1	1

$$Q_2 = A \text{ AND } B \text{ AND } C$$

T9

- 两种解答
 - 转义字符：000010 010000 101000 001101 → CQoN
 - 非转义字符：010111 000111 010001 011100 101011 100101 110001 110010 → XHRcblxy
- 规避格式符号、仅允许字符的情况下传递信息等。

T10

$$\left(\sum_{i=0}^{23} 2^{-i}\right) \times 2^{254-127} = (2 - 2^{-23}) \times 2^{127} = 2^{128} - 2^{104}$$

T11

随意舍入，不管它

- Mult
 - $A[23 : 31] + B[23 : 31] + 10000001 \rightarrow EXP[8 : 0]$
 - $\{1, A[0 : 23]\} * \{1, B[0 : 23]\} = FRAC[0 : 48]$

- $(FRAC[47]?\{0, EXP, FRAC[23 : 46]\} : \{0, EXP + 00000001, FRAC[24 : 47]\}) \rightarrow C[0 : 32]$

2. Add

- $A \geq B \Rightarrow A[23 : 31] \geq B[23 : 31]$
- $A[23 : 31] - B[23 : 31] \rightarrow SHIFT$
- $\{01, A[0 : 23]\} + (\{01, B[0 : 23]\} \gg SHIFT) \rightarrow FRAC[0 : 25]$
- $(FRAC[24]?\{0, A[23 : 31] + 00000001, FRAC[1 : 24]\} : \{0, A[23 : 31], FRAC[0 : 23]\}) \rightarrow C[0 : 32]$

以上是大致流程，可自行画图。