

Version 6: Cluster first

Simulate data

```
I <- 100
K <- 10
S <- 3

set.seed(123)

pi <- rep(0.1, 10)
#z <- sample(1:K, size = I, replace = T, prob = pi)
z <- rep(1:10, each=10)
w <- matrix(c(0.98, 0.99, 0.97,
              0.98, 0.90, 0.82,
              0.55, 0.00, 0.80,
              0.20, 0.00, 0.50,
              0.30, 0.00, 0.30,
              0.43, 0.90, 0.00,
              0.30, 0.70, 0.00,
              0.20, 0.00, 0.00,
              0.00, 0.00, 0.30,
              0.00, 0.50, 0.00),
            byrow=T,
            nrow=K, ncol=S)

colnames(w) <- paste0("sample", 1:S)

tcn <- matrix(2, nrow=I, ncol=S)
m <- matrix(rep(sample(1:2, size = I, replace = T), S),
            nrow=I, ncol=S)
W <- w[z, ]
calcTheta <- function(m, tcn, w) {
  (m * w) / (tcn * w + 2*(1-w))
}

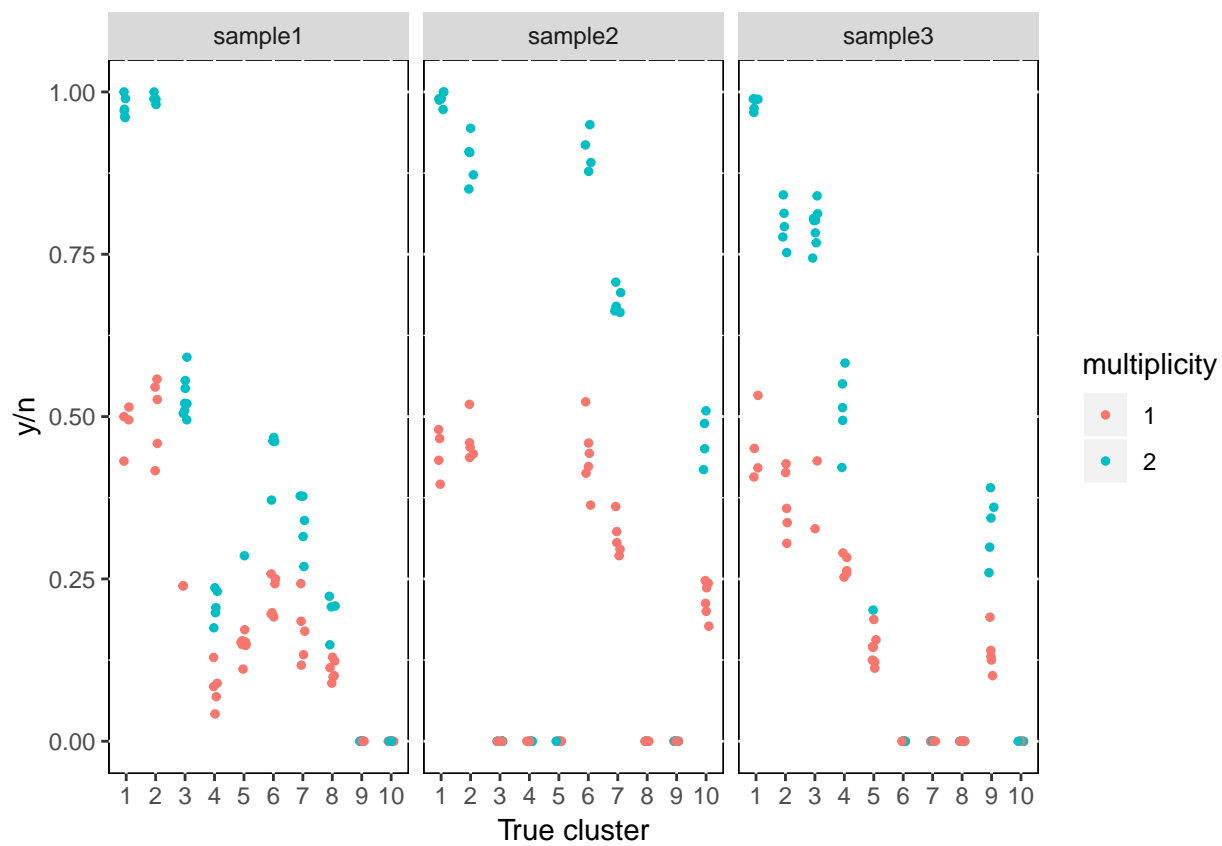
theta <- calcTheta(m, tcn, W)

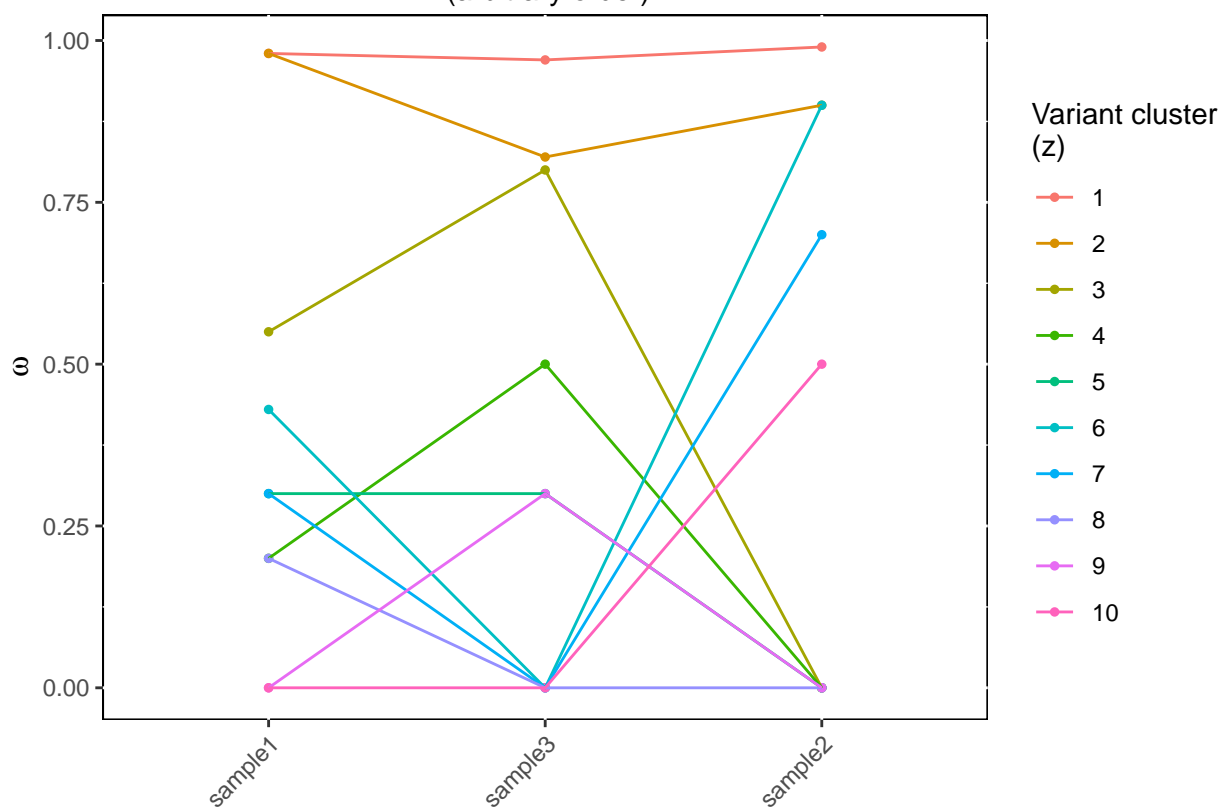
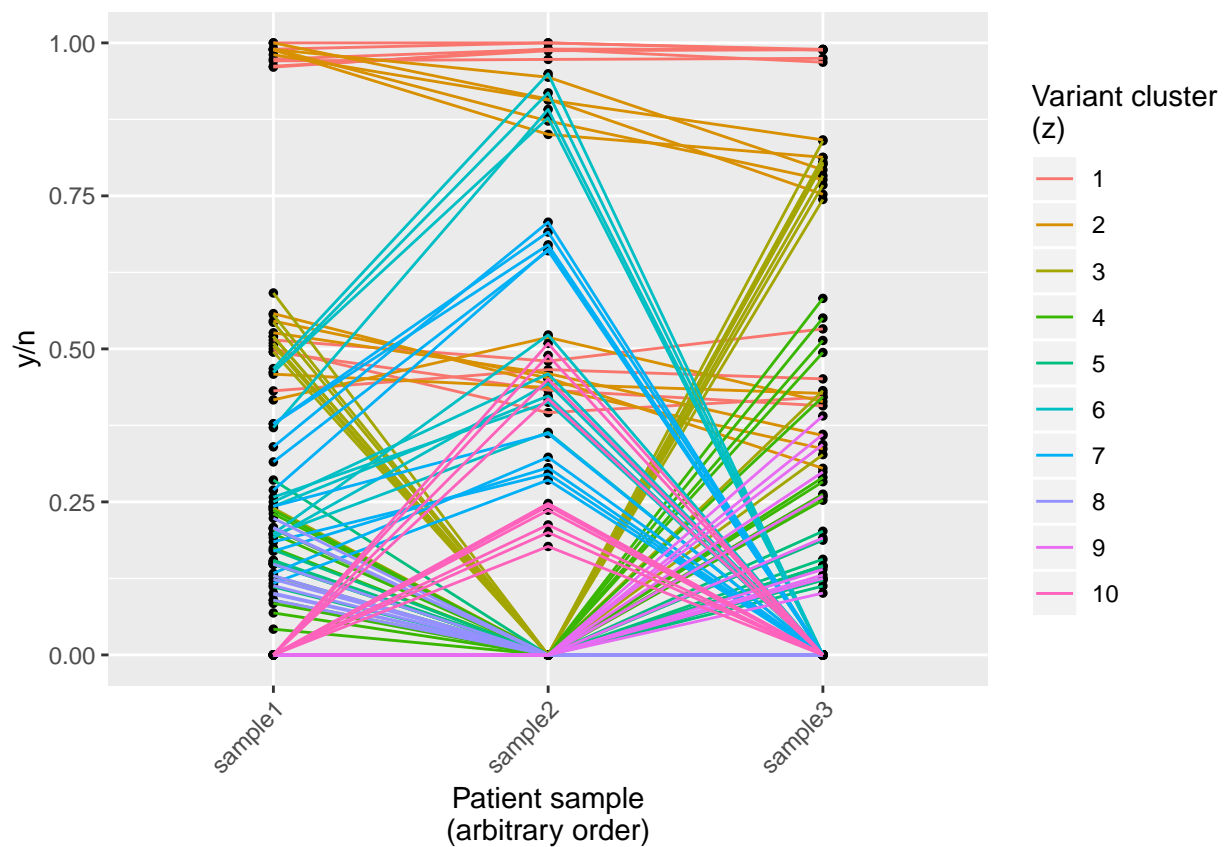
n <- replicate(S, rpois(I, 100))
y <- matrix(NA, nrow=I, ncol=S)
for (i in 1:I) {
  for (s in 1:S) {
    y[i, s] <- rbinom(1, n[i, s], theta[i,s])
  }
}

test.data <- list("I" = I, "S" = S, "K" = K,
                 "y" = y, "n" = n,
                 "m" = m, "tcn" = tcn)
```

Visualize densities of simulated data

Clustering is by ω





functions

```
runMCMC <- function(data, K, jags.file, inits, params, n.iter, thin) {
  data$K <- K
  jags.m <- jags.model(jags.file, data,
    n.chains = 1,
    inits = inits,
    n.adapt = 1000)
  samps <- coda.samples(jags.m, params, n.iter=n.iter, thin=thin)
  samps
}

getParamChain <- function(samps, param) {
  chains <- do.call(rbind, samps)
  chain <- chains[, grep(param, colnames(chains))]
}

reshapeW <- function(w, S, K) {
  w.mat <- matrix(w, nrow = K)
  colnames(w.mat) <- paste0("sample", 1:S)
  w.mat
}

calcLogLik <- function(z.iter, w.iter, data) {
  W <- w.iter[z.iter, ]
  theta <- calcTheta(data$m, data$tcn, W)
  sum(dbinom(data$y, data$n, theta, log=T))
}

calcChainLogLik <- function(samps, data, K) {
  z.chain <- getParamChain(samps, "z")
  w.chain <- getParamChain(samps, "w")
  lik <- c()
  for(iter in 1:nrow(z.chain)) {
    z.iter <- z.chain[iter,]
    w.iter <- reshapeW(w.chain[iter,], data$S, K)
    lik <- c(lik, calcLogLik(z.iter, w.iter, data))
  }
  mean(lik)
}

calcBIC <- function(n, k, ll) log(n)*k - 2*ll
```

Cluster – JAGS

```
jags.file <- file.path(models.dir, "w.jags")
inits <- list(".RNG.name" = "base::Wichmann-Hill",
  ".RNG.seed" = 123)
test.data <- list("I" = I, "S" = S,
  "y" = y, "n" = n,
  "m" = m, "tcn" = tcn)
params <- c("z", "w", "ystar")
```

```

n.iter = 10000
thin = 7
K <- 10

samps <- runMCMC(test.data, K, jags.file, inits, params, n.iter, thin)

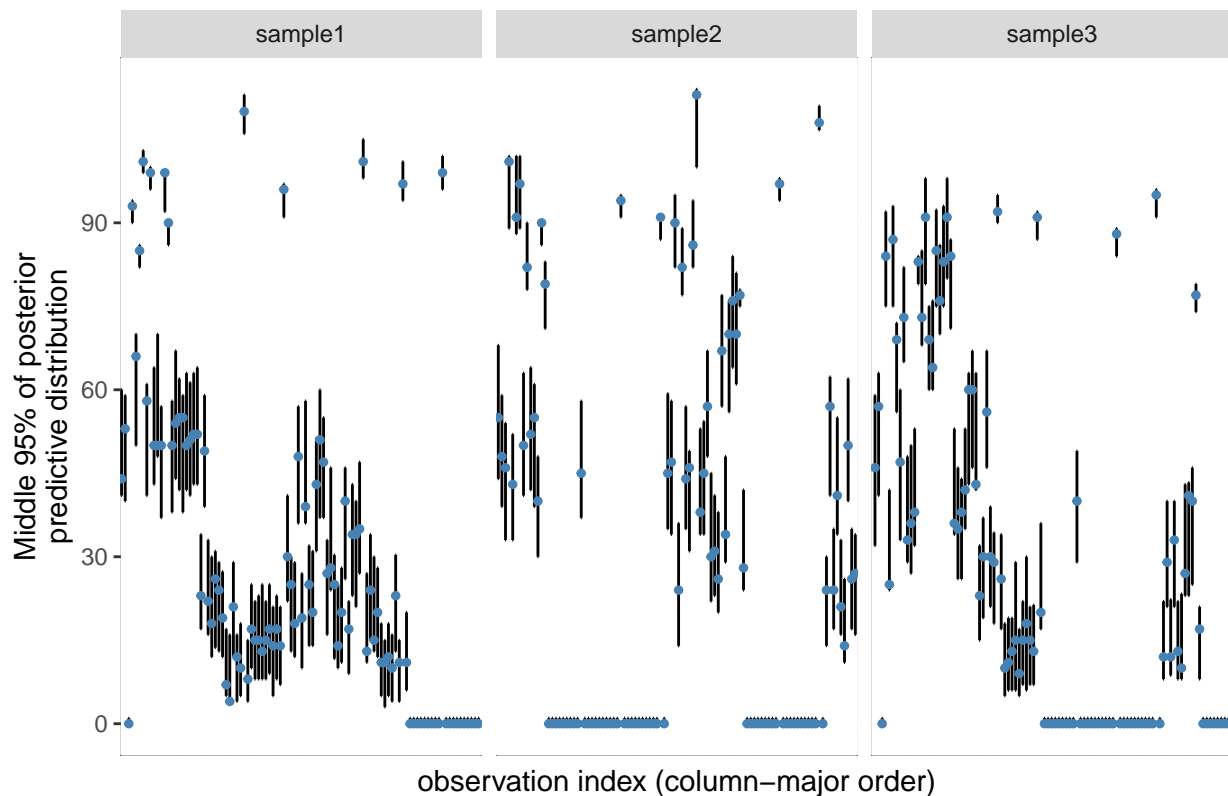
## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 300
##   Unobserved stochastic nodes: 431
##   Total graph size: 4196
##
## Initializing model

z.chain <- getParamChain(samps, "z")
w.chain <- getParamChain(samps, "w")

```

PPD

K = 10



Z

```

plot.z <- function(samps, z) {
  mcmc_vals <- summary(samps)$statistics
  mcmc_z <- as.vector(mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])
}

```

```

plot(z, mcmc_z, type = "p")
z_comp <- data.frame(z, mcmc_z)
#plot.new()
#grid.table(z_comp, rows=NULL)
#z_mapping <- distinct(round(z_comp, 0))
#z_mapping <- z_mapping[order(z_mapping$mcmc_z), ]
#plot.new()
#grid.table(z_mapping, rows=NULL)
}

z.chain.to.tb <- function(z.chain) {
  z.chain.tb <- z.chain %>%
    as_tibble() %>%
    mutate(iter=1:nrow(z.chain)) %>%
    gather(variant, mcmc_z, -c(iter))
  z.chain.tb <- z.chain.tb %>%
    mutate(variant = as.integer(gsub(".*\\[(.*)\\].*", "\\1", z.chain.tb$variant))) %>%
    mutate(true_z = rep(1:10, each=nrow(z.chain)*10)) %>%
    group_by(variant, mcmc_z) %>%
    mutate(count = n())
  z.chain.tb_simp <- distinct(select(z.chain.tb, -c(iter)))
  z.chain.tb_simp %>%
    group_by(variant) %>%
    mutate(prop = count/sum(count))
}

z.chain.tb <- z.chain.to.tb(z.chain)
z.chain.tb

```

```

## # A tibble: 135 x 5
## # Groups:   variant [100]
##   variant mcmc_z true_z count  prop
##   <int>   <dbl> <int> <int> <dbl>
## 1      1      2      1    657 0.460
## 2      1      1      1    771 0.540
## 3      2      1      1   1428 1
## 4      3      2      1   1260 0.882
## 5      3      1      1    168 0.118
## 6      4      1      1   1428 1
## 7      5      1      1   1428 1
## 8      6      2      1   1315 0.921
## 9      6      1      1    113 0.0791
## 10     7      1      1   1428 1
## # ... with 125 more rows

```

```

z.seg.tb <- tibble(variant = numeric(),
                   mcmc_z_1 = numeric(),
                   mcmc_z_2 = numeric())
for (i in 1:ncol(z.chain)) {
  z.vals <- as.integer(names(table(z.chain[,i])))
  if (length(z.vals) > 1) {
    z.seg.tb[i, ] <- c(i, z.vals[1], z.vals[2])
  } else {
    z.seg.tb[i, ] <- c(i, z.vals, z.vals)
  }
}

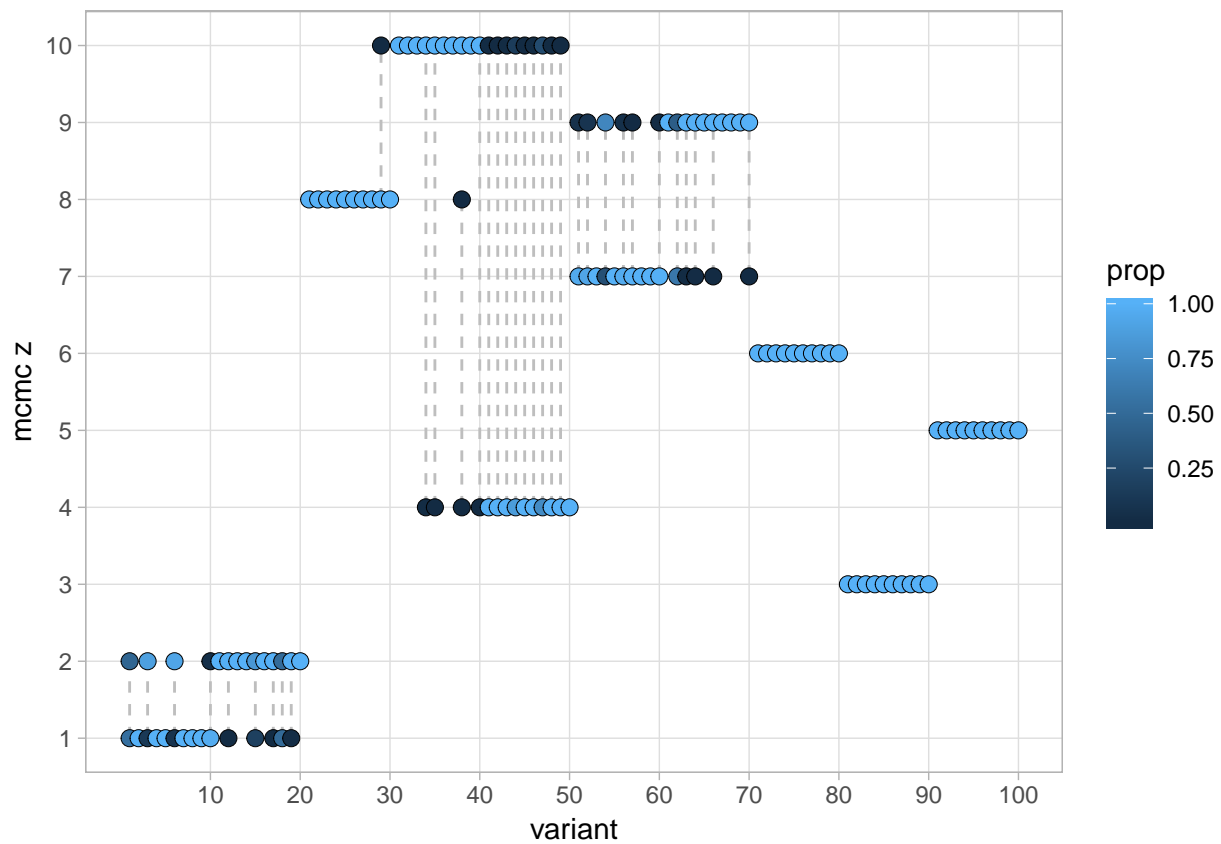
```

```

}
}
#z.seg.tb
z.plot <- ggplot(z.chain.tb, aes(variant, mcmc_z)) +
  ylab("mcmc z") +
  xlab("variant") +
  theme_light() +
  scale_y_continuous(breaks = 1:K, minor_breaks=NULL) +
  scale_x_continuous(breaks = seq(10,100,10), minor_breaks=NULL) +
  geom_segment(data = z.seg.tb,
    aes(x=variant, xend=variant,
        y=mcmc_z_1, yend=mcmc_z_2),
    color="gray", linetype=2) +
  geom_point(aes(y=mcmc_z, fill=prop),
    pch=21, size=3, stroke=0)

```

z.plot



```

ggsave(file.path(figs.dir, "zplot.pdf"), z.plot, width=14, height=6)

# mcmc_vals <- summary(samps)$statistics
# mcmc_z <- as.vector(mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])
# plot.z(samps, z)

z.map.tb <- z.chain.tb %>%
  group_by(variant) %>%
  filter(prop == max(prop))

```

```
z.map.tb
```

```
## # A tibble: 100 x 5
## # Groups:   variant [100]
##   variant mcmc_z true_z count  prop
##   <int>   <dbl> <int> <int> <dbl>
## 1       1       1       1     771 0.540
## 2       2       1       1    1428 1
## 3       3       2       1    1260 0.882
## 4       4       1       1    1428 1
## 5       5       1       1    1428 1
## 6       6       2       1    1315 0.921
## 7       7       1       1    1428 1
## 8       8       1       1    1428 1
## 9       9       1       1    1428 1
## 10      10       1       1    1381 0.967
## # ... with 90 more rows
```

```
z.map <- z.map.tb$mcmc_z
z.map
```

```
## [1] 1 1 2 1 1 2 1 1 1 1 2 2 2 2 2 2 2 2 8 8 8
## [24] 8 8 8 8 8 8 8 10 10 10 10 10 10 10 10 4 4 4 4 4
## [47] 4 4 4 4 7 7 7 7 7 7 7 7 9 7 9 9 9 9 9 9
## [70] 9 6 6 6 6 6 6 6 6 6 3 3 3 3 3 3 3 3 3 3 5 5
## [93] 5 5 5 5 5 5 5 5
```

```
z.map.ind <- which(apply(z.chain, 1, function(x) all(x == z.map)))
w.chain.map <- w.chain[z.map.ind, ]
w.map.tb <- w.chain.map %>%
  as_tibble() %>%
  mutate(iter=1:nrow(w.chain.map)) %>%
  gather(ind, mcmc_w, -c(iter)) %>%
  group_by(ind) %>%
  summarize(mean_w = mean(mcmc_w))
w.map.tb <- w.map.tb %>%
  mutate(cluster = as.integer(gsub(".*\\[(.*)\\],.*", "\\1", w.map.tb$ind))) %>%
  mutate(sample = as.integer(gsub(".*\\,(.*)\\]", "\\1", w.map.tb$ind))) %>%
  arrange(cluster)
#w.map.tb
w.map <- matrix(data=w.map.tb$mean_w, nrow=10, ncol=3, byrow=TRUE)
w.map
```

```
##           [,1]           [,2]           [,3]
## [1,] 0.973637944 0.988597020 0.9820710869
## [2,] 0.986416825 0.898308330 0.7872189454
## [3,] 0.001522582 0.001459451 0.3172062772
## [4,] 0.298899414 0.001986741 0.2629240648
## [5,] 0.001516133 0.456360105 0.0009553129
## [6,] 0.204992711 0.001354114 0.0010398326
## [7,] 0.446984100 0.906262831 0.0012807779
## [8,] 0.526633332 0.001433847 0.7948906517
## [9,] 0.333174387 0.666250526 0.0011254626
## [10,] 0.195689330 0.001694563 0.5222219276
```



```

# presence of clusters in samples
cluster.sample.presence <- apply(w, 1, function(x) which(x>0.01))
cluster.sample.presence

## [[1]]
## sample1 sample2 sample3
##      1      2      3
##
## [[2]]
## sample1 sample2 sample3
##      1      2      3
##
## [[3]]
## sample1 sample3
##      1      3
##
## [[4]]
## sample1 sample3
##      1      3
##
## [[5]]
## sample1 sample3
##      1      3
##
## [[6]]
## sample1 sample2
##      1      2
##
## [[7]]
## sample1 sample2
##      1      2
##
## [[8]]
## sample1
##      1
##
## [[9]]
## sample3
##      3
##
## [[10]]
## sample2
##      2

all.samples <- 1:S
admat <- matrix(data=0, nrow=11, ncol=10) # rows=from is root + 1:K, cols=to is 1:K

# fill in restraints
# can go from root to anyone, skip and start at nrow=2 (cluster 1)
for (from in 2:(K+1)) {
  for (to in 1:K) {

    # can't go to self
    if ((from-1) == to) {

```

```

    admat[from, to] <- NA
    #print(c(from, to, "self"))
    next
  }
  # hierarchy restraints
  from.samples <- cluster.sample.presence[[from-1]]
  to.samples <- cluster.sample.presence[[to]]

  ## no restraints if same sample presence
  if (setequal(from.samples, to.samples)) {
    #print(c(from, to, "same"))
    next
  }

  ## restraint if # from.samples < # to.samples
  if(length(from.samples) < length(to.samples)) {
    #print(c(from, to, "from set is smaller than to set"))
    admat[from, to] <- NA
    next
  }

  ## no restraints if to.samples is subset of from.samples
  if (all(to.samples %in% from.samples)) {
    #print(c(from, to, "subset"))
    next
  } else {
    #print(c(from, to, "not subset"))
    admat[from, to] <- NA
  }
}
}

admat

```

```

##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,]    0    0    0    0    0    0    0    0    0    0
## [2,]   NA    0    0    0    0    0    0    0    0    0
## [3,]    0   NA    0    0    0    0    0    0    0    0
## [4,]   NA   NA   NA    0    0   NA   NA    0    0   NA
## [5,]   NA   NA    0   NA    0   NA   NA    0    0   NA
## [6,]   NA   NA    0    0   NA   NA   NA    0    0   NA
## [7,]   NA   NA   NA   NA   NA   NA    0    0   NA    0
## [8,]   NA   NA   NA   NA   NA    0   NA    0   NA    0
## [9,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [10,]  NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [11,]  NA   NA   NA   NA   NA   NA   NA   NA   NA   NA

```