

Version 3: 3 clusters

Simulate data

```
I <- 50
K <- 3
S <- 10

set.seed(123)

d <- matrix(NA, nrow=K, ncol=S)
c <- matrix(150, nrow=K, ncol=S)
for (s in 1:S) {
  d[, s] <- runif(K, 0.05, 1)
}

a <- d*(c-1)+1
b <- (1-d)*(c-2)+1

pi <- as.vector(rdirichlet(1, rep(1, K)))
z <- sample(1:K, size = I, replace = T, prob = pi)

w <- matrix(NA, nrow=I, ncol=S)
for (s in 1:S) {
  w[, s] <- rbeta(I, a[,s][z], b[,s][z])
}

tcn <- matrix(2, nrow=I, ncol=S)
m <- matrix(rep(sample(1:2, size = I, replace = T), S), nrow=I, ncol=S)

calcTheta <- function(m, tcn, w) {
  (m * w) / (tcn * w + 2*(1-w))
}
theta <- calcTheta(m, tcn, w)

n <- replicate(S, rpois(I, 100))
y <- matrix(NA, nrow=I, ncol=S)
for (i in 1:I) {
  for (s in 1:S) {
    y[i, s] <- rbinom(1, n[i, s], theta[i,s])
  }
}
```

JAGS

```
jags.file <- file.path(models.dir, "v3_noConstraints_mode.jags")

test.data <- list("I" = I, "S" = S, "K" = K,
                 "y" = y, "n" = n,
                 "m" = m, "tcn" = tcn)
```

```
jags.m <- jags.model(jags.file, test.data,
                    n.chains = 1,
                    inits = list(".RNG.name" = "base::Wichmann-Hill",
                                ".RNG.seed" = 12))
```

```
## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 500
##   Unobserved stochastic nodes: 611
##   Total graph size: 8511
##
## Initializing model
```

```
params <- c("z", "w", "d", "c")
samps <- coda.samples(jags.m, params, n.iter=6000, thin=5)
s <- summary(samps)
effectiveSize(samps)
```

```
##      c[1,1]      c[2,1]      c[3,1]      c[1,2]      c[2,2]      c[3,2]
## 1038.57439 1070.24286 904.91394 974.74596 920.33897 720.72409
##      c[1,3]      c[2,3]      c[3,3]      c[1,4]      c[2,4]      c[3,4]
## 1224.50562 979.62298 998.51378 1056.46316 991.47035 866.58210
##      c[1,5]      c[2,5]      c[3,5]      c[1,6]      c[2,6]      c[3,6]
## 845.97526 1072.76692 879.91499 964.39917 1041.14976 813.80547
##      c[1,7]      c[2,7]      c[3,7]      c[1,8]      c[2,8]      c[3,8]
## 765.71554 820.63102 935.25693 130.50699 1025.49881 807.74308
##      c[1,9]      c[2,9]      c[3,9]      c[1,10]      c[2,10]      c[3,10]
## 872.13468 1050.98260 784.10374 1138.56893 1458.21907 1071.53502
##      d[1,1]      d[2,1]      d[3,1]      d[1,2]      d[2,2]      d[3,2]
## 1325.54327 865.95751 1124.76216 468.29675 726.70521 723.81648
##      d[1,3]      d[2,3]      d[3,3]      d[1,4]      d[2,4]      d[3,4]
## 1200.00000 794.75409 1087.87327 1061.65181 737.58478 761.52284
##      d[1,5]      d[2,5]      d[3,5]      d[1,6]      d[2,6]      d[3,6]
## 728.16272 1030.45616 954.74738 355.66414 1069.50831 672.81211
##      d[1,7]      d[2,7]      d[3,7]      d[1,8]      d[2,8]      d[3,8]
## 370.80864 767.22357 956.21994 25.02602 1021.41512 782.98112
##      d[1,9]      d[2,9]      d[3,9]      d[1,10]      d[2,10]      d[3,10]
## 1200.00000 1071.62865 857.14673 1011.93822 1007.56314 875.59332
##      w[1,1]      w[2,1]      w[3,1]      w[4,1]      w[5,1]      w[6,1]
## 1200.00000 1577.07550 1092.65131 1200.00000 1200.00000 1107.13555
##      w[7,1]      w[8,1]      w[9,1]      w[10,1]      w[11,1]      w[12,1]
## 1200.00000 924.02811 1200.00000 1200.00000 1200.00000 1349.39125
##      w[13,1]      w[14,1]      w[15,1]      w[16,1]      w[17,1]      w[18,1]
## 1200.00000 1200.00000 1200.00000 1200.00000 1200.00000 1200.00000
##      w[19,1]      w[20,1]      w[21,1]      w[22,1]      w[23,1]      w[24,1]
## 1200.00000 1072.25589 1200.00000 1132.26636 1200.00000 1200.00000
##      w[25,1]      w[26,1]      w[27,1]      w[28,1]      w[29,1]      w[30,1]
## 920.94960 1200.00000 1200.00000 1200.00000 1200.00000 1200.00000
##      w[31,1]      w[32,1]      w[33,1]      w[34,1]      w[35,1]      w[36,1]
## 1200.00000 1415.03389 1200.00000 1074.34389 1200.00000 1606.27843
##      w[37,1]      w[38,1]      w[39,1]      w[40,1]      w[41,1]      w[42,1]
## 1070.41908 1200.00000 962.70830 1200.00000 1200.00000 1200.00000
```

##	w[43,1]	w[44,1]	w[45,1]	w[46,1]	w[47,1]	w[48,1]
##	1200.00000	1200.00000	1260.54662	1200.00000	1200.00000	1200.00000
##	w[49,1]	w[50,1]	w[1,2]	w[2,2]	w[3,2]	w[4,2]
##	1200.00000	1200.00000	740.45792	1200.00000	1200.00000	1075.80174
##	w[5,2]	w[6,2]	w[7,2]	w[8,2]	w[9,2]	w[10,2]
##	1013.57829	1200.00000	1200.00000	1048.12661	1200.00000	1200.00000
##	w[11,2]	w[12,2]	w[13,2]	w[14,2]	w[15,2]	w[16,2]
##	1025.90684	1200.00000	1200.00000	1200.00000	1009.04361	996.45851
##	w[17,2]	w[18,2]	w[19,2]	w[20,2]	w[21,2]	w[22,2]
##	1020.31224	1199.31546	1200.00000	1200.00000	1200.00000	1209.98244
##	w[23,2]	w[24,2]	w[25,2]	w[26,2]	w[27,2]	w[28,2]
##	1023.95948	1200.00000	1010.07077	1084.27170	1200.00000	1328.11204
##	w[29,2]	w[30,2]	w[31,2]	w[32,2]	w[33,2]	w[34,2]
##	1200.00000	1033.84407	1200.00000	1092.36526	1073.67452	1200.00000
##	w[35,2]	w[36,2]	w[37,2]	w[38,2]	w[39,2]	w[40,2]
##	844.16729	1200.00000	1200.00000	1200.00000	1391.15535	1200.00000
##	w[41,2]	w[42,2]	w[43,2]	w[44,2]	w[45,2]	w[46,2]
##	964.20521	1200.00000	1013.16406	1200.00000	1025.89716	1200.00000
##	w[47,2]	w[48,2]	w[49,2]	w[50,2]	w[1,3]	w[2,3]
##	959.91023	1100.79834	1200.00000	1200.00000	1200.00000	1200.00000
##	w[3,3]	w[4,3]	w[5,3]	w[6,3]	w[7,3]	w[8,3]
##	1366.27706	1200.00000	1200.00000	1342.21806	1200.00000	1200.00000
##	w[9,3]	w[10,3]	w[11,3]	w[12,3]	w[13,3]	w[14,3]
##	1200.00000	1200.00000	946.84027	1200.00000	1200.00000	1345.54245
##	w[15,3]	w[16,3]	w[17,3]	w[18,3]	w[19,3]	w[20,3]
##	1367.19412	1200.00000	1053.37926	1006.28949	1077.40161	1200.00000
##	w[21,3]	w[22,3]	w[23,3]	w[24,3]	w[25,3]	w[26,3]
##	1200.00000	1200.00000	1200.00000	1083.33949	1050.39143	1200.00000
##	w[27,3]	w[28,3]	w[29,3]	w[30,3]	w[31,3]	w[32,3]
##	1200.00000	899.55833	1200.00000	1098.44913	1200.00000	1102.45506
##	w[33,3]	w[34,3]	w[35,3]	w[36,3]	w[37,3]	w[38,3]
##	1200.00000	1200.00000	1200.00000	1200.00000	1041.01619	1052.96341
##	w[39,3]	w[40,3]	w[41,3]	w[42,3]	w[43,3]	w[44,3]
##	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000
##	w[45,3]	w[46,3]	w[47,3]	w[48,3]	w[49,3]	w[50,3]
##	1038.97341	1200.00000	1534.78310	1200.00000	1622.74212	1200.00000
##	w[1,4]	w[2,4]	w[3,4]	w[4,4]	w[5,4]	w[6,4]
##	1200.00000	1200.00000	663.26370	1200.00000	1200.00000	1200.00000
##	w[7,4]	w[8,4]	w[9,4]	w[10,4]	w[11,4]	w[12,4]
##	1032.30069	1200.00000	1200.00000	1434.16942	1200.00000	1200.00000
##	w[13,4]	w[14,4]	w[15,4]	w[16,4]	w[17,4]	w[18,4]
##	1200.00000	1200.00000	1200.00000	1191.85351	1105.58336	1200.00000
##	w[19,4]	w[20,4]	w[21,4]	w[22,4]	w[23,4]	w[24,4]
##	1200.00000	1315.11703	1200.00000	992.60836	1200.00000	1200.00000
##	w[25,4]	w[26,4]	w[27,4]	w[28,4]	w[29,4]	w[30,4]
##	1030.95606	1040.88384	1200.00000	1016.36964	1200.00000	934.37685
##	w[31,4]	w[32,4]	w[33,4]	w[34,4]	w[35,4]	w[36,4]
##	1200.00000	1077.08401	1200.00000	1200.00000	1200.00000	1200.00000
##	w[37,4]	w[38,4]	w[39,4]	w[40,4]	w[41,4]	w[42,4]
##	1091.06944	1042.37510	1200.00000	1200.00000	1200.00000	1379.90805
##	w[43,4]	w[44,4]	w[45,4]	w[46,4]	w[47,4]	w[48,4]
##	1018.15078	1200.00000	1063.41188	1200.00000	1200.00000	1200.00000
##	w[49,4]	w[50,4]	w[1,5]	w[2,5]	w[3,5]	w[4,5]
##	1200.00000	1071.68805	1200.00000	1200.00000	1200.00000	995.63561

##	w[5,5]	w[6,5]	w[7,5]	w[8,5]	w[9,5]	w[10,5]
##	1091.08595	1200.00000	1176.18331	1200.00000	1081.65478	1200.00000
##	w[11,5]	w[12,5]	w[13,5]	w[14,5]	w[15,5]	w[16,5]
##	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000
##	w[17,5]	w[18,5]	w[19,5]	w[20,5]	w[21,5]	w[22,5]
##	1200.00000	1052.05375	1200.00000	1093.46578	1200.00000	1200.00000
##	w[23,5]	w[24,5]	w[25,5]	w[26,5]	w[27,5]	w[28,5]
##	1200.00000	1200.00000	1096.28879	1200.00000	1014.98430	1200.00000
##	w[29,5]	w[30,5]	w[31,5]	w[32,5]	w[33,5]	w[34,5]
##	1200.00000	1200.00000	1200.00000	1096.01648	1200.00000	1091.75678
##	w[35,5]	w[36,5]	w[37,5]	w[38,5]	w[39,5]	w[40,5]
##	1200.00000	1095.40552	1200.00000	1200.00000	1200.00000	1200.00000
##	w[41,5]	w[42,5]	w[43,5]	w[44,5]	w[45,5]	w[46,5]
##	1200.00000	1200.00000	1102.70155	1200.00000	1075.54504	1200.00000
##	w[47,5]	w[48,5]	w[49,5]	w[50,5]	w[1,6]	w[2,6]
##	1443.44612	1200.00000	1200.00000	1200.00000	1022.92595	1033.12779
##	w[3,6]	w[4,6]	w[5,6]	w[6,6]	w[7,6]	w[8,6]
##	1200.00000	1200.00000	1200.00000	1029.05511	1200.00000	1200.00000
##	w[9,6]	w[10,6]	w[11,6]	w[12,6]	w[13,6]	w[14,6]
##	1200.00000	1343.43594	1200.00000	1200.00000	1200.00000	1200.00000
##	w[15,6]	w[16,6]	w[17,6]	w[18,6]	w[19,6]	w[20,6]
##	1200.00000	1200.00000	1037.17498	1051.89056	1060.54003	1102.98577
##	w[21,6]	w[22,6]	w[23,6]	w[24,6]	w[25,6]	w[26,6]
##	1049.94824	1200.00000	1341.21469	1467.86014	1200.00000	1200.00000
##	w[27,6]	w[28,6]	w[29,6]	w[30,6]	w[31,6]	w[32,6]
##	1200.00000	1200.00000	1393.10450	1200.00000	1200.00000	1200.00000
##	w[33,6]	w[34,6]	w[35,6]	w[36,6]	w[37,6]	w[38,6]
##	1200.00000	1200.00000	1200.00000	1200.00000	1407.10128	1078.74392
##	w[39,6]	w[40,6]	w[41,6]	w[42,6]	w[43,6]	w[44,6]
##	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000
##	w[45,6]	w[46,6]	w[47,6]	w[48,6]	w[49,6]	w[50,6]
##	1200.00000	1200.00000	1016.79491	1206.67672	1200.00000	1200.00000
##	w[1,7]	w[2,7]	w[3,7]	w[4,7]	w[5,7]	w[6,7]
##	1200.00000	1003.06941	1050.54487	1200.00000	1200.00000	1200.00000
##	w[7,7]	w[8,7]	w[9,7]	w[10,7]	w[11,7]	w[12,7]
##	955.38052	1040.17202	1200.00000	1200.00000	1228.22753	1200.00000
##	w[13,7]	w[14,7]	w[15,7]	w[16,7]	w[17,7]	w[18,7]
##	1200.00000	1200.00000	1200.00000	1039.41240	1200.00000	1200.00000
##	w[19,7]	w[20,7]	w[21,7]	w[22,7]	w[23,7]	w[24,7]
##	1200.00000	1029.50947	1200.00000	1023.66052	1200.00000	1046.04136
##	w[25,7]	w[26,7]	w[27,7]	w[28,7]	w[29,7]	w[30,7]
##	979.88836	1200.00000	1351.66439	1021.55923	1200.00000	893.59118
##	w[31,7]	w[32,7]	w[33,7]	w[34,7]	w[35,7]	w[36,7]
##	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000
##	w[37,7]	w[38,7]	w[39,7]	w[40,7]	w[41,7]	w[42,7]
##	1200.00000	1077.12873	1200.00000	1200.00000	1200.00000	1216.35301
##	w[43,7]	w[44,7]	w[45,7]	w[46,7]	w[47,7]	w[48,7]
##	1200.00000	1200.00000	1096.77946	1200.00000	1432.77977	1200.00000
##	w[49,7]	w[50,7]	w[1,8]	w[2,8]	w[3,8]	w[4,8]
##	1200.00000	1193.92503	1005.03724	1200.00000	901.71348	1151.24623
##	w[5,8]	w[6,8]	w[7,8]	w[8,8]	w[9,8]	w[10,8]
##	1200.00000	1123.89977	1134.69527	1200.00000	1069.72484	1200.00000
##	w[11,8]	w[12,8]	w[13,8]	w[14,8]	w[15,8]	w[16,8]
##	1200.00000	1200.00000	1007.26129	1200.00000	1200.00000	1200.00000

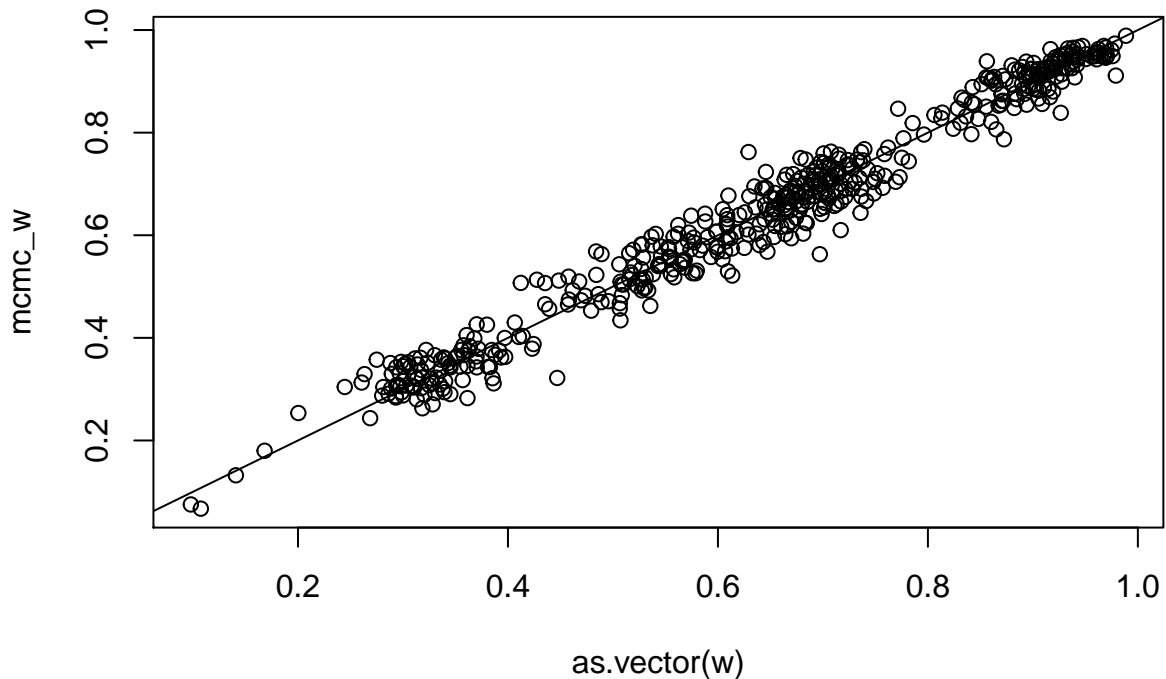
##	w[17,8]	w[18,8]	w[19,8]	w[20,8]	w[21,8]	w[22,8]
##	1200.00000	1200.00000	1200.00000	1072.65126	998.44288	1200.00000
##	w[23,8]	w[24,8]	w[25,8]	w[26,8]	w[27,8]	w[28,8]
##	1200.00000	1391.03203	1200.00000	978.96024	1200.00000	1200.00000
##	w[29,8]	w[30,8]	w[31,8]	w[32,8]	w[33,8]	w[34,8]
##	1200.00000	1303.52084	1333.51453	1200.00000	1200.00000	1200.00000
##	w[35,8]	w[36,8]	w[37,8]	w[38,8]	w[39,8]	w[40,8]
##	1200.00000	1200.00000	1200.00000	1200.00000	1082.40570	1080.84971
##	w[41,8]	w[42,8]	w[43,8]	w[44,8]	w[45,8]	w[46,8]
##	1093.81605	1200.00000	1005.53544	555.66366	1200.00000	1200.00000
##	w[47,8]	w[48,8]	w[49,8]	w[50,8]	w[1,9]	w[2,9]
##	1085.96374	1114.90339	1200.00000	1200.00000	1726.98874	1200.00000
##	w[3,9]	w[4,9]	w[5,9]	w[6,9]	w[7,9]	w[8,9]
##	1251.07462	1200.00000	1341.65817	1200.00000	1264.26361	1103.15745
##	w[9,9]	w[10,9]	w[11,9]	w[12,9]	w[13,9]	w[14,9]
##	1200.00000	1200.00000	1460.97943	1200.00000	956.76805	1200.00000
##	w[15,9]	w[16,9]	w[17,9]	w[18,9]	w[19,9]	w[20,9]
##	1473.27365	1200.00000	1200.00000	1200.00000	1200.00000	1200.00000
##	w[21,9]	w[22,9]	w[23,9]	w[24,9]	w[25,9]	w[26,9]
##	1200.00000	1278.52651	1200.00000	2315.34476	1162.68442	1200.00000
##	w[27,9]	w[28,9]	w[29,9]	w[30,9]	w[31,9]	w[32,9]
##	1083.94337	1200.00000	1091.91372	1200.00000	912.60379	1200.00000
##	w[33,9]	w[34,9]	w[35,9]	w[36,9]	w[37,9]	w[38,9]
##	1092.90197	1200.00000	1200.00000	1200.00000	1200.00000	1031.77439
##	w[39,9]	w[40,9]	w[41,9]	w[42,9]	w[43,9]	w[44,9]
##	1242.37922	1200.00000	1200.00000	1103.78365	1200.00000	1200.00000
##	w[45,9]	w[46,9]	w[47,9]	w[48,9]	w[49,9]	w[50,9]
##	1200.00000	1200.00000	1200.00000	1096.43348	1200.00000	1200.00000
##	w[1,10]	w[2,10]	w[3,10]	w[4,10]	w[5,10]	w[6,10]
##	1352.75119	1200.00000	1200.00000	1200.00000	1200.00000	1229.04209
##	w[7,10]	w[8,10]	w[9,10]	w[10,10]	w[11,10]	w[12,10]
##	1200.00000	1200.00000	1200.00000	1041.16898	995.65107	1200.00000
##	w[13,10]	w[14,10]	w[15,10]	w[16,10]	w[17,10]	w[18,10]
##	1073.34221	1200.00000	1200.00000	1470.89847	1200.00000	1200.00000
##	w[19,10]	w[20,10]	w[21,10]	w[22,10]	w[23,10]	w[24,10]
##	1200.00000	1096.88128	1085.29892	1200.00000	1041.69551	1200.00000
##	w[25,10]	w[26,10]	w[27,10]	w[28,10]	w[29,10]	w[30,10]
##	1200.00000	1200.00000	1025.70812	1200.00000	1200.00000	1142.45649
##	w[31,10]	w[32,10]	w[33,10]	w[34,10]	w[35,10]	w[36,10]
##	1200.00000	1200.00000	1200.00000	1200.00000	1104.29837	1200.00000
##	w[37,10]	w[38,10]	w[39,10]	w[40,10]	w[41,10]	w[42,10]
##	1200.00000	1186.26087	1200.00000	1145.59222	1097.41677	1200.00000
##	w[43,10]	w[44,10]	w[45,10]	w[46,10]	w[47,10]	w[48,10]
##	1200.00000	1200.00000	1200.00000	1351.71657	1200.00000	1090.61599
##	w[49,10]	w[50,10]	z[1]	z[2]	z[3]	z[4]
##	1138.22282	1200.00000	0.00000	0.00000	0.00000	0.00000
##	z[5]	z[6]	z[7]	z[8]	z[9]	z[10]
##	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000
##	z[11]	z[12]	z[13]	z[14]	z[15]	z[16]
##	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000
##	z[17]	z[18]	z[19]	z[20]	z[21]	z[22]
##	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000
##	z[23]	z[24]	z[25]	z[26]	z[27]	z[28]
##	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000

```
##      z[29]      z[30]      z[31]      z[32]      z[33]      z[34]
##      0.00000    0.00000    0.00000    0.00000    0.00000    0.00000
##      z[35]      z[36]      z[37]      z[38]      z[39]      z[40]
##      0.00000    0.00000    0.00000    0.00000    0.00000    0.00000
##      z[41]      z[42]      z[43]      z[44]      z[45]      z[46]
##      0.00000    0.00000    0.00000    0.00000    0.00000    0.00000
##      z[47]      z[48]      z[49]      z[50]
##      0.00000    0.00000    0.00000    0.00000
```

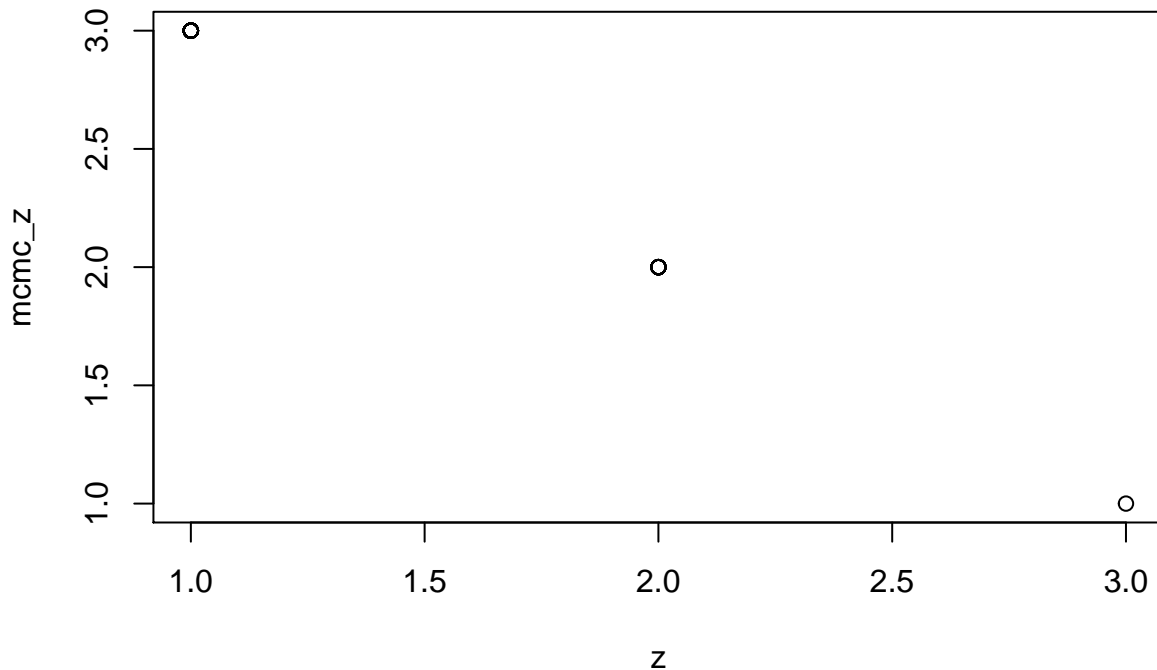
```
pdf(file.path(trace.dir, paste0(runName, "_trace.pdf")))
plot(samps)
dev.off()
```

```
## pdf
## 2
```

```
mcmc_cals <- s$statistics
mcmc_w <- mcmc_cals[substr(rownames(mcmc_cals), 1, 1) == "w", "Mean"]
plot(as.vector(w), mcmc_w, type = "p")
abline(a=0, b=1)
```



```
mcmc_z <- as.vector(mcmc_cals[substr(rownames(mcmc_cals), 1, 1) == "z", "Mean"])
#mcmc_z <- round(mcmc_z, 0)
plot(z, mcmc_z, type = "p")
```



```

mcmc_d<- mcmc_cals[substr(rownames(mcmc_cals), 1, 1) == "d", "Mean"]
mcmc_d <- matrix(mcmc_d, nrow=K)
mcmc_c <- mcmc_cals[substr(rownames(mcmc_cals), 1, 1) == "c", "Mean"]
mcmc_c <- matrix(mcmc_c, nrow=K)

mcmc_a <- mcmc_d*(mcmc_c-1)+1
mcmc_b <- (1-mcmc_d)*(mcmc_c-2)+1

p <- seq(0, 1, length = 100)
colors <- c("#000000", "#DCA200", "#8FA7ED", "#9D847A", "#A47901")
for (s in 1:S) {
  for (k in 1:K) {
    if (k == 1) {
      # plot mcmc
      plot(p, dbeta(p, mcmc_a[k,s], mcmc_b[k,s]),
           main = paste0("S", s),
           ylab = "density", xlab = "w", type = "l", col = colors[k],
           ylim = c(0, 20))
      # plot truth
      lines(p, dbeta(p, a[k,s], b[k,s]), type = "l", col = colors[k], lty=2)
      # add legend
      allU <- round(as.vector(rbind(mcmc_d[,s], d[,s])), digits = 2)
      legend(x = "topleft",
             legend = paste0(c("mean k", "true k"), rep(1:K, each=2), ", mode = ", allU),
             col = colors[rep(1:K, each=2)],
             lty = rep(1:2, K),
             cex=0.8)
    } else {
      # plot mcmc
      lines(p, dbeta(p, mcmc_a[k,s], mcmc_b[k,s]),
            type = "l", col = colors[k])
      # plot truth

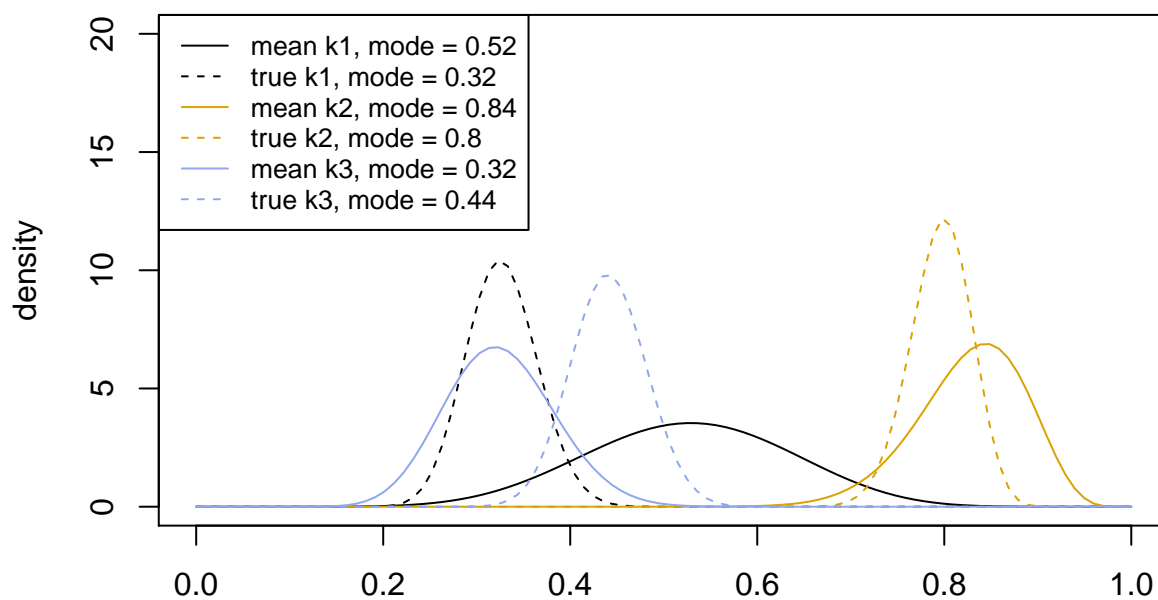
```

```

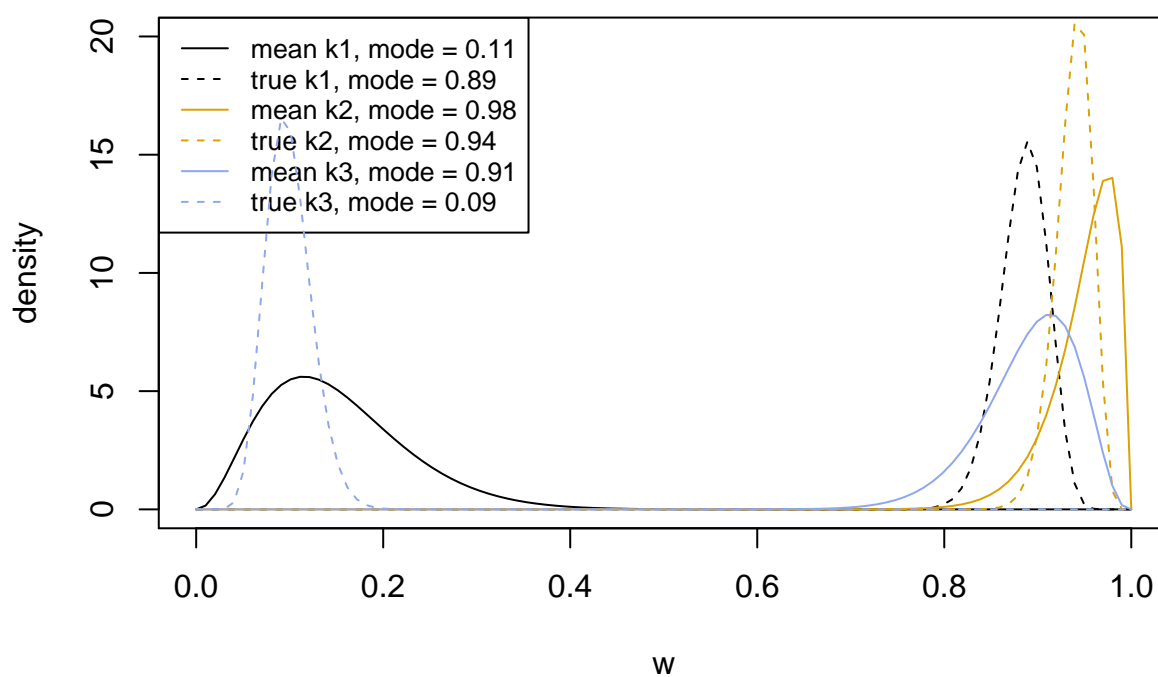
    lines(p, dbeta(p, a[k,s], b[k,s]), type = "l", col = colors[k], lty=2)
  }
}
}

```

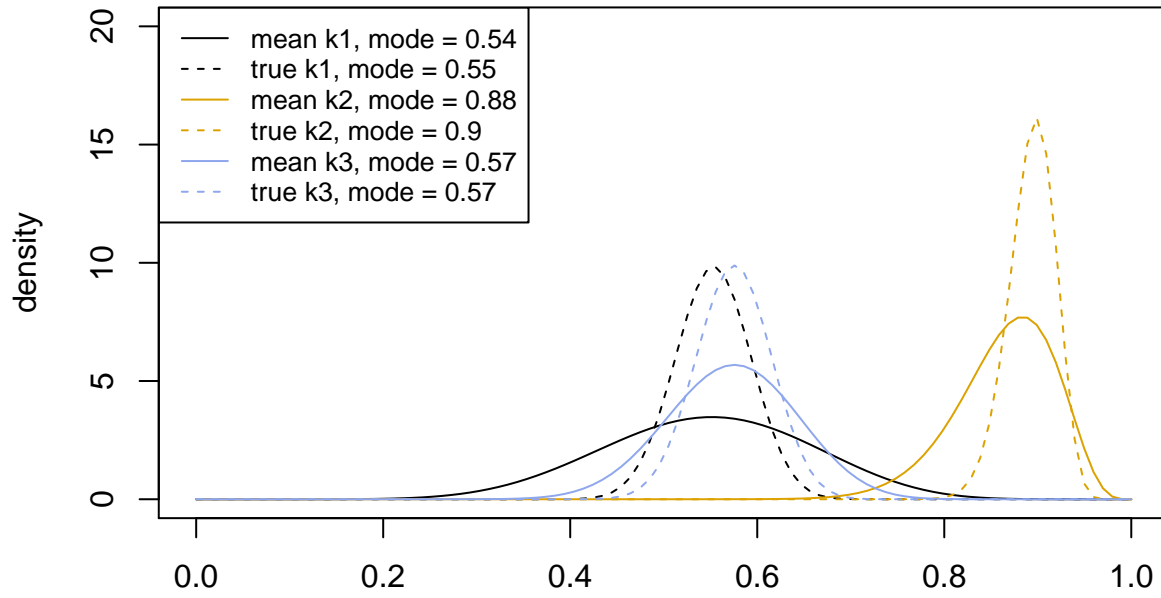
S1



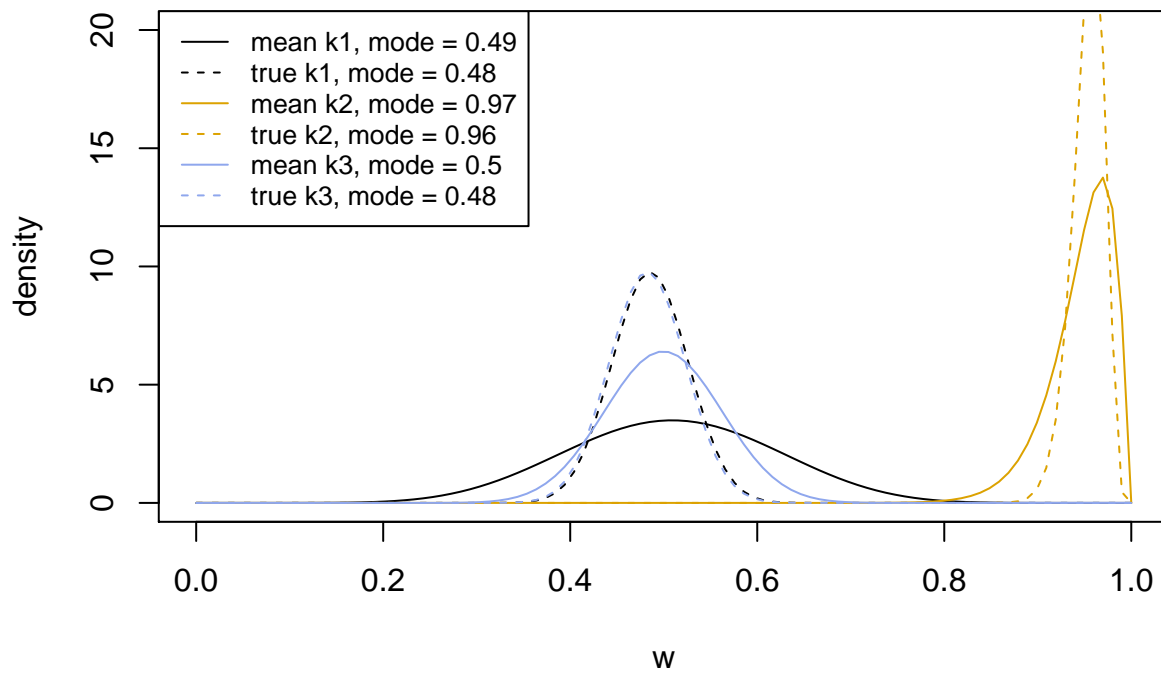
S2



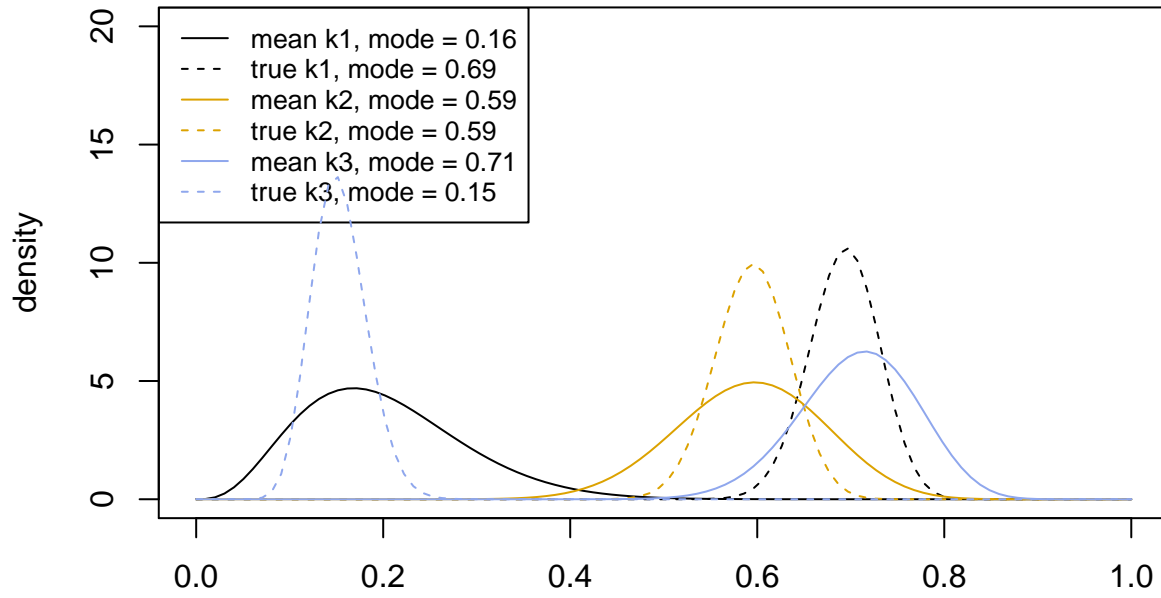
S3



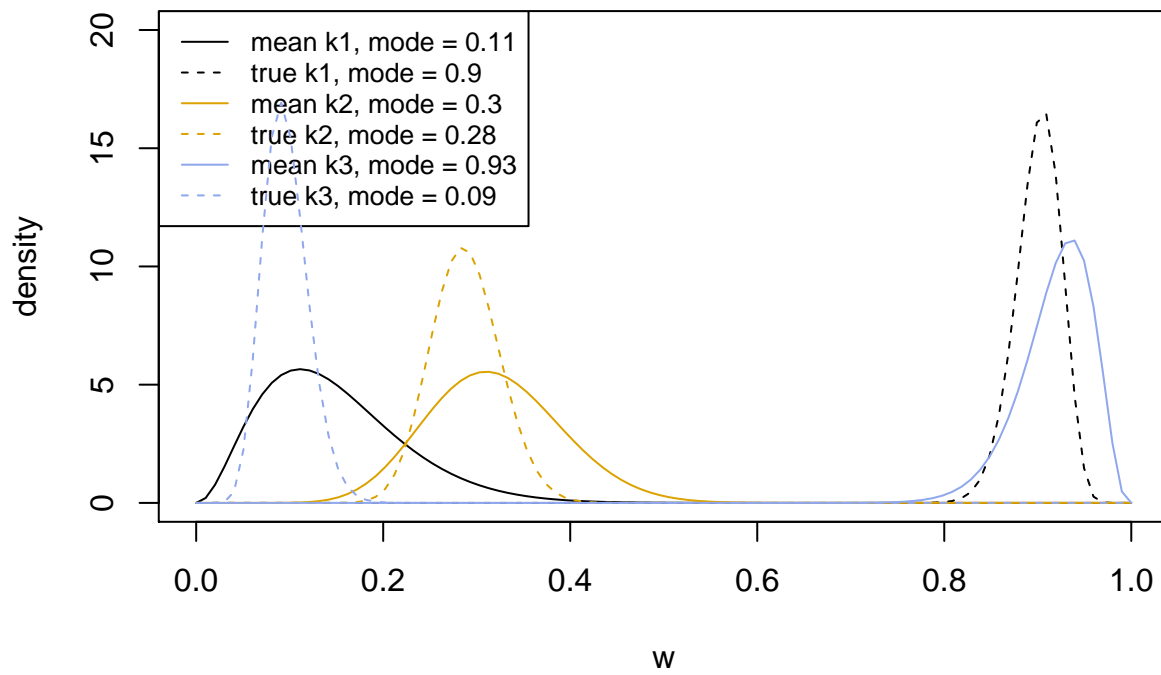
S4



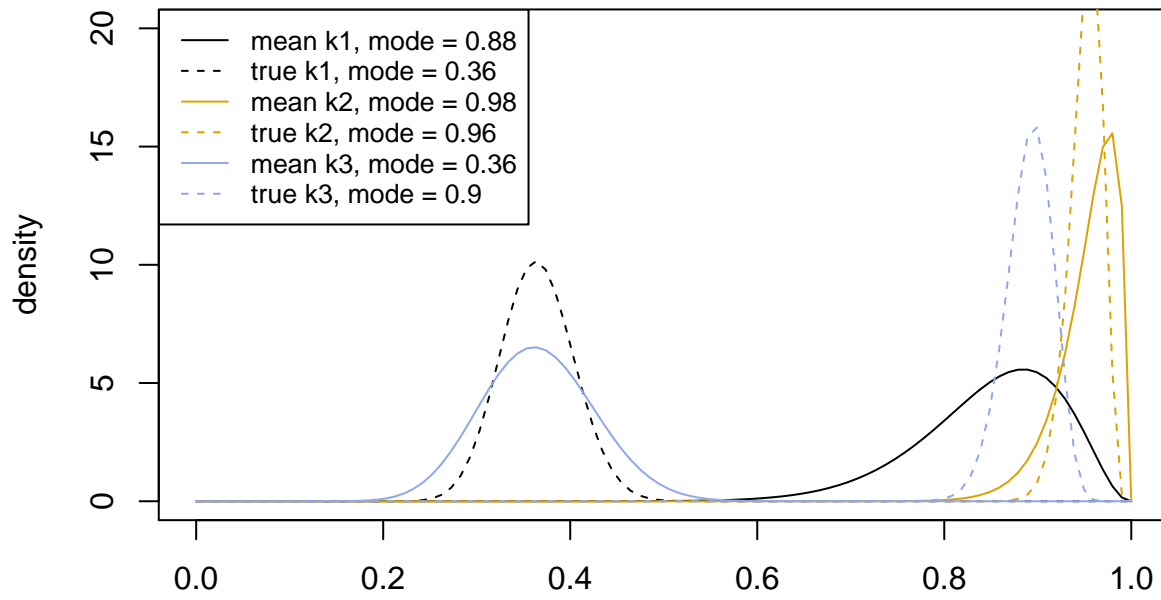
S5



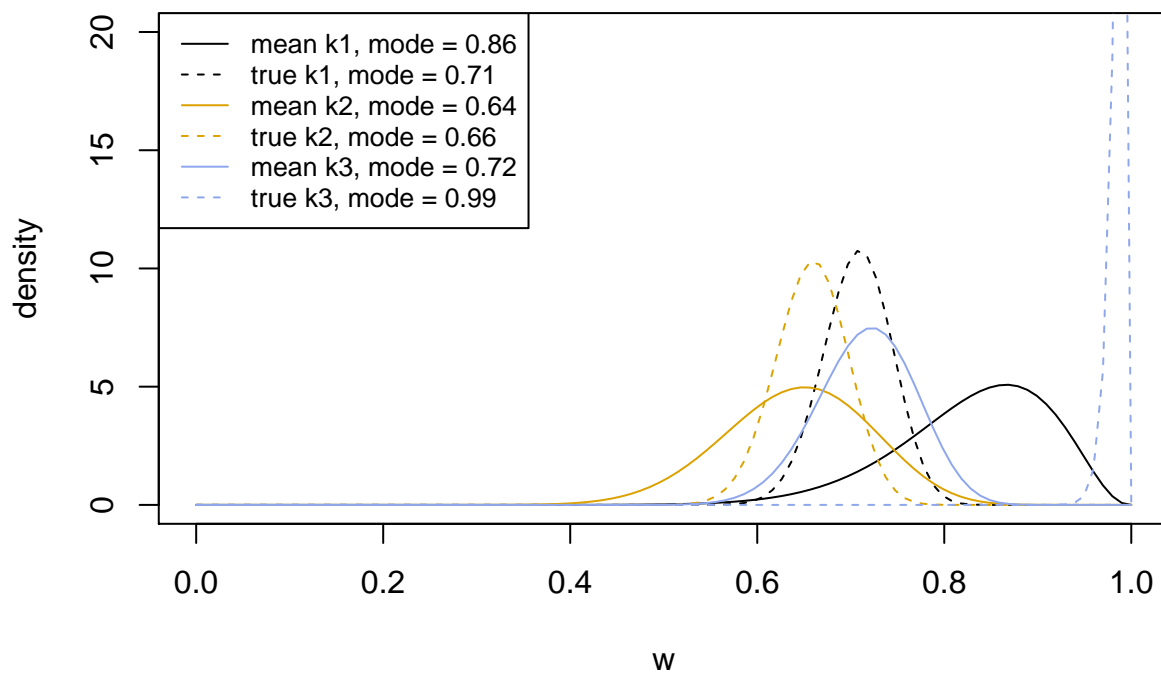
S6



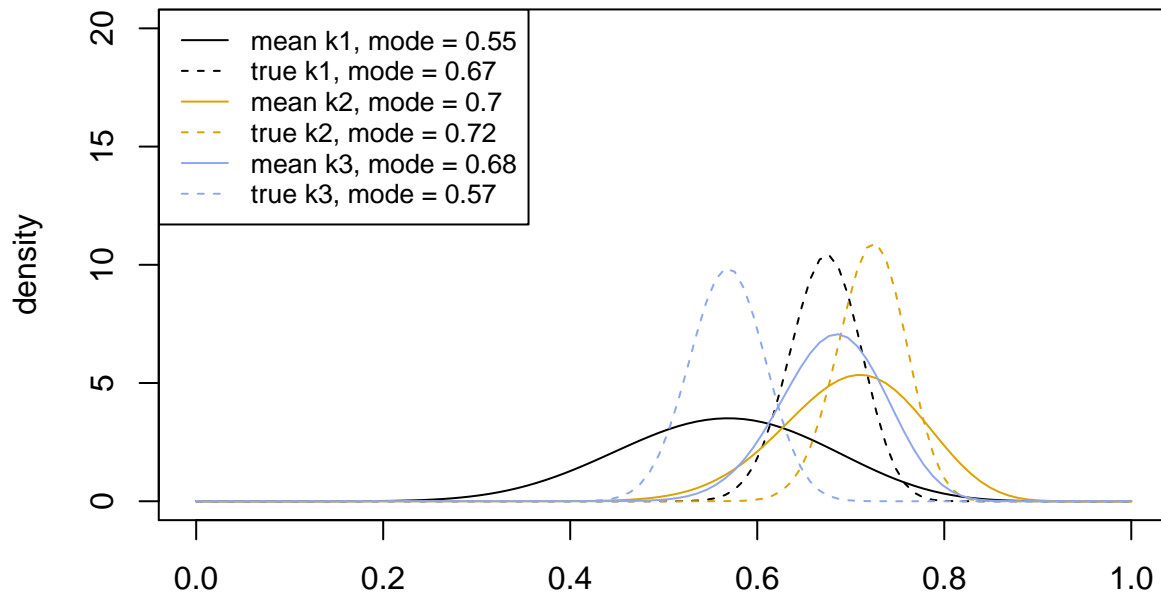
S7



S8



S9



S10

