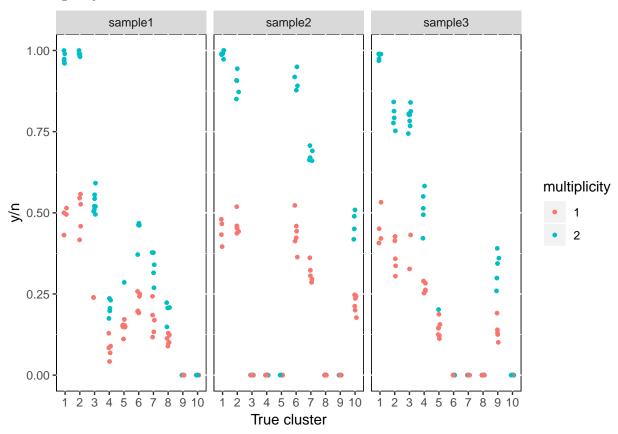
Version 6: Cluster first

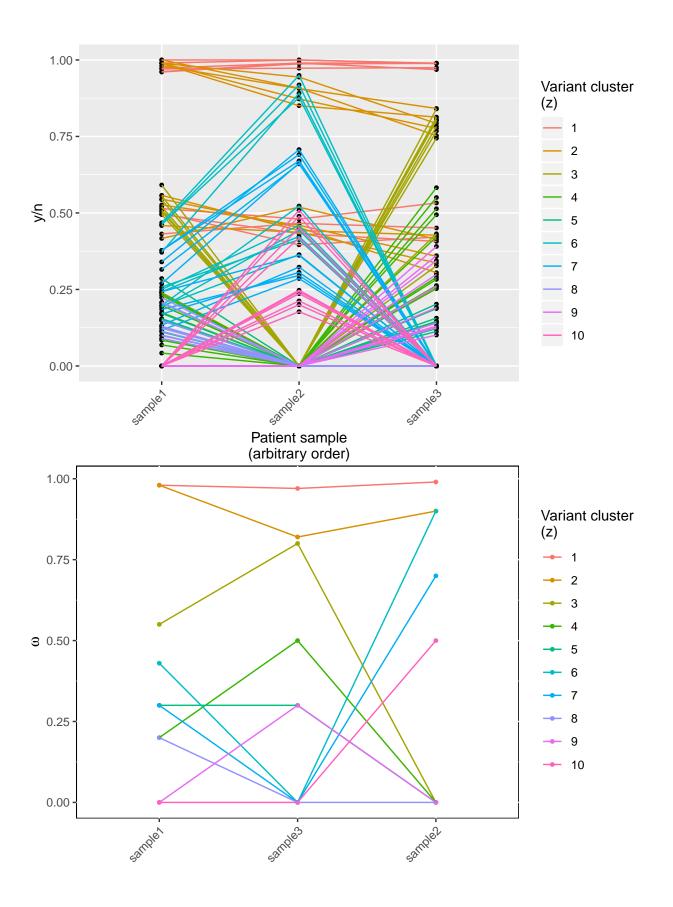
Simulate data

```
I <- 100
K <- 10
S <- 3
set.seed(123)
pi \leftarrow rep(0.1, 10)
\#z \leftarrow sample(1:K, size = I, replace = T, prob = pi)
z <- rep(1:10, each=10)
w \leftarrow matrix(c(0.98, 0.99, 0.97,
               0.98, 0.90, 0.82,
               0.55, 0.00, 0.80,
               0.20, 0.00, 0.50,
               0.30, 0.00, 0.30,
               0.43, 0.90, 0.00,
               0.30, 0.70, 0.00,
               0.20, 0.00, 0.00,
               0.00, 0.00, 0.30,
               0.00, 0.50, 0.00),
             byrow=T,
            nrow=K, ncol=S)
colnames(w) <- paste0("sample", 1:S)</pre>
##
         sample1 sample2 sample3
##
   [1,]
            0.98
                     0.99
                             0.97
                     0.90
                             0.82
## [2,]
            0.98
## [3,]
          0.55
                     0.00
                             0.80
## [4,]
                   0.00
          0.20
                             0.50
## [5,]
            0.30
                     0.00
                             0.30
## [6,]
                  0.90
                             0.00
          0.43
## [7,]
          0.30
                     0.70
                             0.00
## [8,]
            0.20
                     0.00
                             0.00
## [9,]
                     0.00
            0.00
                              0.30
## [10,]
            0.00
                     0.50
                             0.00
tcn <- matrix(2, nrow=I, ncol=S)</pre>
m <- matrix(rep(sample(1:2, size = I, replace = T), S),</pre>
            nrow=I, ncol=S)
W \leftarrow w[z,]
calcTheta <- function(m, tcn, w) {</pre>
  (m * w) / (tcn * w + 2*(1-w))
theta <- calcTheta(m, tcn, W)
n <- replicate(S, rpois(I, 100))</pre>
y <- matrix(NA, nrow=I, ncol=S)
```

Visualize densities of simulated data

Clustering is by ω





functions

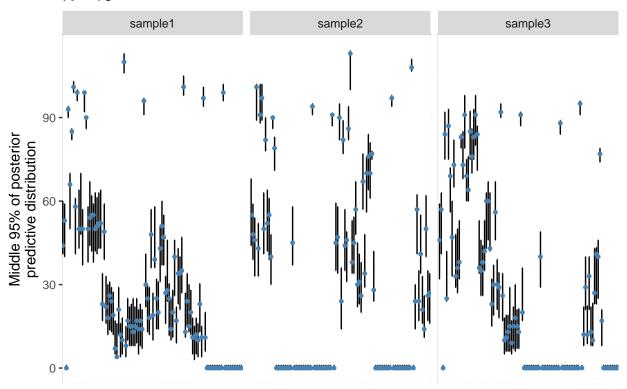
```
runMCMC <- function(data, K, jags.file, inits, params, n.iter, thin) {</pre>
  data$K <- K
  jags.m <- jags.model(jags.file, data,</pre>
                          n.chains = 1,
                          inits = inits,
                          n.adapt = 1000)
  samps <- coda.samples(jags.m, params, n.iter=n.iter, thin=thin)</pre>
  samps
}
getParamChain <- function(samps, param) {</pre>
  chains <- do.call(rbind, samps)</pre>
  chain <- chains[, grep(param, colnames(chains))]</pre>
}
reshapeW <- function(w, S, K) {</pre>
  w.mat <- matrix(w, nrow = K)</pre>
  colnames(w.mat) <- paste0("sample", 1:S)</pre>
  w.mat
}
calcLogLik <- function(z.iter, w.iter, data) {</pre>
  W <- w.iter[z.iter, ]</pre>
  theta <- calcTheta(data$m, data$tcn, W)
  sum(dbinom(data$y, data$n, theta, log=T))
}
calcChainLogLik <- function(samps, data, K) {</pre>
  z.chain <- getParamChain(samps, "z")</pre>
  w.chain <- getParamChain(samps, "w")</pre>
  lik \leftarrow c()
  for(iter in 1:nrow(z.chain)) {
    z.iter <- z.chain[iter,]</pre>
    w.iter <- reshapeW(w.chain[iter,], data$S, K)</pre>
    lik <- c(lik, calcLogLik(z.iter, w.iter, data))</pre>
  }
  mean(lik)
calcBIC <- function(n, k, ll) log(n)*k - 2*ll
```

Cluster - JAGS

```
n.iter = 10000
thin = 7
K <- 10
samps <- runMCMC(test.data, K, jags.file, inits, params, n.iter, thin)</pre>
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
##
  Graph information:
      Observed stochastic nodes: 300
##
      Unobserved stochastic nodes: 431
##
##
      Total graph size: 4196
##
## Initializing model
z.chain <- getParamChain(samps, "z")</pre>
w.chain <- getParamChain(samps, "w")</pre>
mcmc_vals <- summary(samps)$statistics</pre>
mcmc_w <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "Mean"]</pre>
mcmc_w <- matrix(mcmc_w, nrow=K)</pre>
colnames(mcmc_w) <- paste0("sample", 1:S)</pre>
```

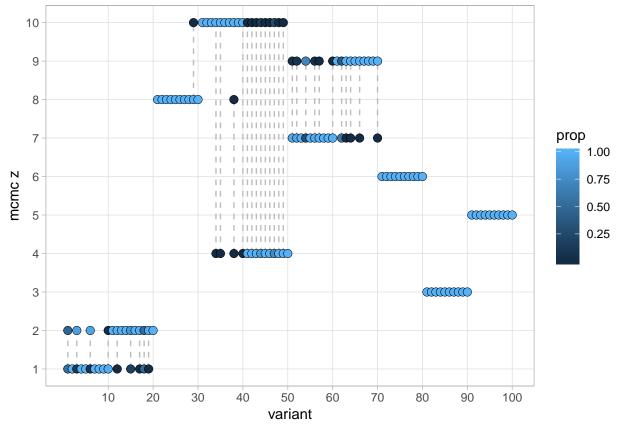
PPD

K = 10



observation index (column-major order)

```
plot.z <- function(samps, z) {</pre>
  mcmc vals <- summary(samps)$statistics</pre>
  mcmc_z <- as.vector(mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])</pre>
  plot(z, mcmc_z, type = "p")
  z_comp <- data.frame(z, mcmc_z)</pre>
z.chain.to.tb <- function(z.chain) {</pre>
  z.chain.tb <- z.chain %>%
    as_tibble() %>%
    mutate(iter=1:nrow(z.chain)) %>%
    gather(variant, mcmc_z, -c(iter))
  z.chain.tb <- z.chain.tb %>%
    mutate(variant = as.integer(gsub(".*\\[(.*)\\].*", "\\1", z.chain.tb$variant))) %>%
    mutate(true_z = rep(1:10, each=nrow(z.chain)*10)) %>%
    group_by(variant, mcmc_z) %>%
    mutate(count = n())
  z.chain.tb_simp <- distinct(select(z.chain.tb, -c(iter)))</pre>
  z.chain.tb_simp %>%
    group_by(variant) %>%
    mutate(prop = count/sum(count))
}
z.chain.tb <- z.chain.to.tb(z.chain)</pre>
z.chain.tb
## # A tibble: 135 x 5
## # Groups:
              variant [100]
##
      variant mcmc_z true_z count
                                     prop
##
        <int> <dbl> <int> <int> <dbl>
## 1
            1
                    2
                          1
                               657 0.460
## 2
                               771 0.540
            1
                    1
                           1
## 3
            2
                    1
                           1 1428 1
                           1 1260 0.882
## 4
            3
                   2
## 5
            3
                    1
                           1
                              168 0.118
                           1 1428 1
## 6
            4
                    1
                           1 1428 1
## 7
            5
                    1
            6
                    2
                           1 1315 0.921
## 8
## 9
                           1 113 0.0791
            6
                    1
            7
                           1 1428 1
## 10
                    1
## # ... with 125 more rows
z.seg.tb <- tibble(variant = numeric(),</pre>
                     mcmc z 1 = numeric(),
                     mcmc_z_2 = numeric())
for (i in 1:ncol(z.chain)) {
  z.vals <- as.integer(names(table(z.chain[,i])))</pre>
  if (length(z.vals) > 1) {
    z.seg.tb[i, ] \leftarrow c(i, z.vals[1], z.vals[2])
  } else {
    z.seg.tb[i, ] \leftarrow c(i, z.vals, z.vals)
  }
}
```



```
#gsave(file.path(figs.dir, "zplot.pdf"), z.plot, width=14, height=6)

# mcmc_vals <- summary(samps)$statistics
# mcmc_z <- as.vector(mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])
# plot.z(samps, z)

z.map.tb <- z.chain.tb %>%
    group_by(variant) %>%
    filter(prop == max(prop))
z.map.tb
```

```
## # A tibble: 100 x 5
## # Groups:
              variant [100]
##
     variant mcmc z true z count prop
##
        <int> <dbl> <int> <int> <dbl>
##
   1
           1
                  1
                         1
                            771 0.540
##
  2
           2
                  1
                         1 1428 1
## 3
           3
                  2
                         1 1260 0.882
                         1 1428 1
           4
## 4
                  1
## 5
           5
                  1
                         1 1428 1
## 6
           6
                  2
                         1 1315 0.921
## 7
           7
                  1
                         1 1428 1
                         1 1428 1
## 8
           8
                  1
           9
                         1 1428 1
## 9
                  1
## 10
                         1 1381 0.967
          10
                  1
## # ... with 90 more rows
z.map <- z.map.tb$mcmc_z</pre>
z.map
               2 1 1 2 1 1 1 1 2 2 2 2 2
                                                                   8
                                                                     8
                                                                        8
##
    [1]
            1
                                                   2
                                                       2
                                                          2
                                                             2
                                                                2
         1
                  8
                     8 8 8 10 10 10 10 10 10 10 10 10 10
                     7 7 7 9 7 7 7 7 7 9
## [47] 4
                                                    7
                                                          9
                                                             9 9 9 9
            4 4
                 4
                                                       9
   [70] 9
            6 6 6 6 6 6 6 6 6 3 3 3 3 3
                                                       3
                                                          3 3 3 3 5 5
## [93] 5 5 5 5 5 5 5 5
z.map.ind <- which(apply(z.chain, 1, function(x) all(x == z.map)))
w.chain.map <- w.chain[z.map.ind, ]</pre>
w.map.tb <- w.chain.map %>%
  as tibble() %>%
 mutate(iter=1:nrow(w.chain.map)) %>%
  gather(ind, mcmc_w, -c(iter)) %>%
  group by(ind) %>%
  summarize(mean_w = mean(mcmc_w))
w.map.tb <- w.map.tb %>%
  mutate(cluster = as.integer(gsub(".*\\[(.*)\\,.*", "\\1", w.map.tb$ind))) %>%
  mutate(sample = as.integer(gsub(".*\\,(.*)\\]", "\\1", w.map.tb$ind))) %>%
  arrange(cluster)
#w.map.tb
w.map <- matrix(data=w.map.tb$mean_w, nrow=10, ncol=3, byrow=TRUE)
w.map
##
               [,1]
                           [,2]
                                       [,3]
## [1,] 0.973637944 0.988597020 0.9820710869
   [2,] 0.986416825 0.898308330 0.7872189454
## [3,] 0.001522582 0.001459451 0.3172062772
## [4,] 0.298899414 0.001986741 0.2629240648
## [5,] 0.001516133 0.456360105 0.0009553129
## [6,] 0.204992711 0.001354114 0.0010398326
## [7,] 0.446984100 0.906262831 0.0012807779
## [8,] 0.526633332 0.001433847 0.7948906517
## [9,] 0.333174387 0.666250526 0.0011254626
## [10,] 0.195689330 0.001694563 0.5222219276
```

Admat

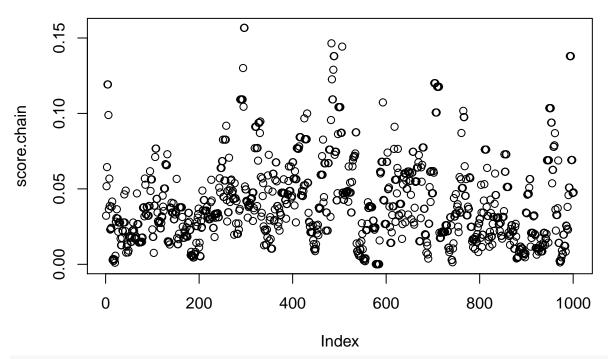
```
rand.admat <- function(admat) {</pre>
  for(col in 1:ncol(admat)) {
    ind.0 <- which(admat[,col] == 0) # possible positions (0's)</pre>
    rand.ind <- sample(ind.0, size=1)</pre>
    admat[rand.ind,col] <- 1</pre>
  }
  while (sum(admat[1, ]) == 0) {
    admat <- mutate.admat(admat)</pre>
  admat
}
base.admat <- function(w, zero.thresh=0.01) {</pre>
  cluster.sample.presence <- apply(w, 1, function(x) which(x>zero.thresh))
  K \leftarrow nrow(w)
  S \leftarrow ncol(w)
  all.samples <- 1:S
  admat <- matrix(data=0, nrow=(1+K), ncol=K) # rows=from is root + 1:K, cols=to is 1:K
  # fill in restraints
  # can go from root to anyone, skip and start at nrow=2 (cluster 1)
  for (from in 2:(K+1)) {
    for (to in 1:K) {
      # can't go to self
      if ((from-1) == to) {
        admat[from, to] <- NA
        #print(c(from, to, "self"))
        next
      }
      # hierarchy restraints
      from.samples <- cluster.sample.presence[[from-1]]</pre>
      to.samples <- cluster.sample.presence[[to]]</pre>
      ## no restraints if same sample presence
      if (setequal(from.samples, to.samples)) {
        #print(c(from, to, "same"))
        next
      }
      ## restraint if # from.samples < # to.samples
      if(length(from.samples) < length(to.samples)) {</pre>
        #print(c(from, to, "from set is smaller than to set"))
        admat[from, to] <- NA
        next
      }
      ## no restraints if to.samples is subset of from.samples
      if (all(to.samples %in% from.samples)) {
        #print(c(from, to, "subset"))
```

```
} else {
         #print(c(from, to, "not subset"))
         admat[from, to] <- NA
    }
  }
  admat
init.admat <- function(w, zero.thresh) {</pre>
  base <- base.admat(w, zero.thresh)</pre>
  rand.admat(base)
}
mutate.admat <- function(admat) {</pre>
  # choose a column to mutate
  K <- ncol(admat)</pre>
  rand.k <- sample(1:K, size=1)</pre>
  # mutate
  possiblePos <- which(!is.na(admat[,rand.k]) & admat[,rand.k] != 1)</pre>
  ind.1 <- which(admat[,rand.k] == 1)</pre>
  new.1 <- sample(possiblePos, size=1)</pre>
  new.admat <- admat</pre>
  new.admat[ind.1,rand.k] <- 0</pre>
  new.admat[new.1,rand.k] <- 1</pre>
  while (sum(new.admat[1, ]) == 0) {
    new.admat <- mutate.admat(admat)</pre>
  }
  new.admat
}
getChildrenWSum <- function(admat, w, row) {</pre>
  curr.row <- admat[row,]</pre>
  children <- which(curr.row == 1)</pre>
  children.w <- w[children,]</pre>
  if(length(children) > 1) {
    return(colSums(children.w))
  } else {
    return(children.w)
  }
}
score.admat <- function(admat, w) {</pre>
  S \leftarrow ncol(w)
  # root, MCF=1.0
  children.w.sum <- getChildrenWSum(admat, w, 1)</pre>
  score <- log(sum(1 >= children.w.sum) / S)
```

```
for(i in 2:nrow(admat)) {
            if(all(is.na(admat[i,]))) next #leaf
            curr.child.sum <- getChildrenWSum(admat, w, i)</pre>
            curr.parent.mcf <- w[i-1, ]</pre>
            curr.score <- log(sum(curr.parent.mcf >= curr.child.sum) / S)
            score <- score + curr.score</pre>
      }
      score
}
true.admat <- base.admat(w, zero.thresh = 0.01)</pre>
true.admat[1,1] <- true.admat[2,2] <- true.admat[3,3] <- true.admat[3,6] <-</pre>
      true.admat[4,4] \leftarrow true.admat[4,5] \leftarrow true.admat[5,8] \leftarrow true.admat[6,9] \leftarrow true.admat
      true.admat[7,7] <- true.admat[8,10] <- 1
true.admat
                            [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
##
       [1,]
                                  1
                                                  0
                                                                 0
                                                                                 0
                                                                                               0
                                                                                                              0
                                                                                                                              0
                                                                                                                                             0
                                                                                                                                                            0
##
       [2,]
                              NA
                                                  1
                                                                  0
                                                                                 0
                                                                                               0
                                                                                                              0
                                                                                                                              0
                                                                                                                                             0
                                                                                                                                                            0
                                                                                                                                                                              0
## [3,]
                                  0
                                               NA
                                                                 1
                                                                                 0
                                                                                               0
                                                                                                              1
                                                                                                                              0
                                                                                                                                             0
                                                                                                                                                            0
                                                                                                                                                                              0
## [4,]
                              NA
                                               NA
                                                               NA
                                                                                                           NA
                                                                                                                           NA
                                                                                                                                             0
                                                                                                                                                            0
                                                                                                                                                                          NA
                                                                                1
                                                                                               1
## [5,]
                               NA
                                               NA
                                                                 0
                                                                              NA
                                                                                               0
                                                                                                           NA
                                                                                                                          NA
                                                                                                                                             1
                                                                                                                                                            0
                                                                                                                                                                          NA
## [6,]
                                            NA
                                                                 0
                                                                              0
                                                                                                           NA
                                                                                                                          NA
                                                                                                                                            0
                                                                                                                                                                          NA
                               NA
                                                                                            NA
                                                                                                                                                           1
## [7,]
                               NA
                                           NA
                                                              NA
                                                                             NA
                                                                                            NA
                                                                                                           NA
                                                                                                                          1
                                                                                                                                                        NΑ
                                                                                                                                                                           0
## [8,]
                                           NA
                                                                                                             0
                                                                                                                                            0
                                                                                                                                                                             1
                                NA
                                                              NA
                                                                             NA
                                                                                            NA
                                                                                                                      NΑ
                                                                                                                                                        NA
## [9,]
                                                                                            NA
                                                                                                           NA
                                                                                                                         NA
                                                                                                                                                                          NA
                                NA
                                              NA
                                                              NA
                                                                             NA
                                                                                                                                          NA
                                                                                                                                                        NA
## [10,]
                                                                                                                          NA
                                                                                                                                                                          NA
                                NA
                                               NA
                                                               NΑ
                                                                             NΑ
                                                                                            NA
                                                                                                           NA
                                                                                                                                          NA
                                                                                                                                                        NΑ
## [11,]
                                NA
                                              NA
                                                              NA
                                                                             NA
                                                                                            NA
                                                                                                           NA
                                                                                                                          NA
                                                                                                                                          NA
                                                                                                                                                        NA
score.admat(true.admat, w)
## [1] 0
count.from.nodes <- function(admat) {</pre>
      sum(rowSums(admat, na.rm = T) > 0)
}
subset.w.chain <- function(w.chain.tb, k, s) {</pre>
      # returns list -- each item of list is a sample
      if(length(s) == 1) return(list(w.chain.tb[paste0("w[", k,",", s, "]")]))
      lapply(s, function(sample) w.chain.tb[paste0("w[", k,",", sample, "]")])
}
get.w.chain.sum <- function(w.chain.list) {</pre>
      if(dim(w.chain.list[[1]])[2] > 1) return(lapply(w.chain.list, rowSums))
      w.chain.list
}
get.children <- function(admat, parent.node) {</pre>
      # parent.node: root=1, clusters start at 2
      # returns children clusters
      which(admat[parent.node, ] == 1)
}
```

```
get.children.w.sum.chain <- function(admat, w.chain.tb, parent.node, S) {</pre>
  # parent.node: root=1, clusters start at 2
  children <- get.children(admat, parent.node)</pre>
  children.w <- subset.w.chain(w.chain.tb, k=children, s=1:S)
  get.w.chain.sum(children.w)
rule.chain.freq <- function(parent.chain, child.chain) {</pre>
  rule <- mapply(function(parent, child) parent > child, parent=parent.chain, child=child.chain)
  sum(rule) / prod(dim(rule))
score.admat.chain <- function(admat, w.chain) {</pre>
  w.ind <- colnames(w.chain)</pre>
  k.vec \leftarrow gsub("^w\[(.*)\],.*", "\1", w.ind)
  K <- length(unique(k.vec))</pre>
  S <- length(k.vec) / K
  total.obs <- nrow(w.chain) * S
  #numFromNodes <- count.from.nodes(admat)</pre>
  w.chain.tb <- as_tibble(w.chain)</pre>
  # root, MCF=1.0
  children.w.sum <- get.children.w.sum.chain(admat, w.chain.tb, 1, S)
  #parent.w <- subset.w.chain(w.chain.tb, 1, 1:S)</pre>
  rule.freq <- rule.chain.freq(parent.chain=1, child.chain=children.w.sum)
  #score <- log(rule.freq)
  score <- rule.freq</pre>
  for(i in 2:nrow(admat)) {
    if(sum(admat[i,], na.rm=T) == 0) next #leaf
    curr.child.sum <- get.children.w.sum.chain(admat, w.chain.tb, i, S)</pre>
    parent.w <- subset.w.chain(w.chain.tb, i-1, 1:S)</pre>
    curr.freq <- rule.chain.freq(parent.chain=parent.w, child.chain=curr.child.sum)</pre>
    #score <- score + log(curr.freq)</pre>
    score <- score * curr.freq</pre>
  }
  score
#score.admat.chain(admat, w.chain)
check.base.admat <- function(admat, base) {</pre>
 all(which(is.na(admat)) == which(is.na(base)))
set.seed(1234)
mcmc_vals <- summary(samps)$statistics</pre>
mcmc_w <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "Mean"]</pre>
```

```
mcmc_w <- matrix(mcmc_w, nrow=K)</pre>
colnames(mcmc_w) <- paste0("sample", 1:S)</pre>
answer <- base.admat(mcmc_w)</pre>
answer[1,1] \leftarrow answer[2,2] \leftarrow answer[3,7] \leftarrow answer[3,8] \leftarrow
  answer[5,3] \leftarrow answer[8,9] \leftarrow answer[9,4] \leftarrow answer[9,10] \leftarrow
  answer[10,5] \leftarrow answer[11,6] \leftarrow 1
score.admat.chain(answer, w.chain)
## [1] 0.04002832
admat.chain <- list(init.admat(mcmc_w, zero.thresh=0.01))</pre>
score.chain <- c()</pre>
numAccept = 0
#2*2*6*5*8*4*5*4*5
numIter <- 1000
for (i in 1:numIter) {
  P.prev <- score.admat.chain(admat.chain[[i]], w.chain)</pre>
  score.chain[i] <- P.prev</pre>
  #admat.star <- mutate.admat(admat.chain[[i]])</pre>
  #P.star <- score.admat.chain(admat.star, w.chain)</pre>
  # if(P.prev == 0 & P.star == 0) {
  # admat.chain[[i+1]] <- admat.star</pre>
  # numAccept <- numAccept + 1</pre>
      next
  # }
  P.star <- 0
  while (P.star == 0) {
    admat.star <- mutate.admat(admat.chain[[i]])</pre>
    P.star <- score.admat.chain(admat.star, w.chain)
  }
  r <- P.star / P.prev
  u \leftarrow runif(1,0,1)
  if(u <= r) {
    admat.chain[[i+1]] <- admat.star</pre>
    numAccept <- numAccept + 1</pre>
  } else {
    admat.chain[[i+1]] <- admat.chain[[i]]</pre>
score.chain[i+1] <- score.admat.chain(admat.chain[[i+1]], w.chain)</pre>
acceptRate <- numAccept/(numIter)</pre>
acceptRate
## [1] 0.744
plot(score.chain)
```



```
max(score.chain)
```

```
## [1] 0.1567209
```

```
max.score.ind <- which(score.chain == max(score.chain))
if(length(max.score.ind) > 1) max.score.ind <- max.score.ind[1]
max.admat <- admat.chain[[max.score.ind]]
max.admat</pre>
```

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
##
     [1,]
              1
                    0
                          0
                                0
                                     0
                                            0
                                                 0
                                                             0
    [2,]
                                            0
                                                 0
                                                             0
                                                                    0
##
             NA
                    1
                          1
                                      0
                                                       1
    [3,]
             0
                          0
                                           0
                                                       0
                                                                    0
##
                   NA
                                0
                                     1
                                                 1
                                                             1
    [4,]
                   NA
                        NA
                                          NA
                                                      NA
                                                                   NA
##
             NA
                              NA
                                    NA
                                                NA
                                                            NA
##
    [5,]
             NA
                   NA
                         0
                              NA
                                    NA
                                           1
                                                NA
                                                       0
                                                            NA
                                                                    0
    [6,]
##
             NA
                   NA
                        NA
                              NA
                                    NA
                                          NA
                                                NA
                                                      NA
                                                            NA
                                                                   NA
    [7,]
                                                                   NA
##
             {\tt NA}
                   {\tt NA}
                        NA
                              NA
                                    NA
                                          {\tt NA}
                                                NA
                                                      NA
                                                            NA
    [8,]
##
             NA
                   NA
                        NA
                              NA
                                     0
                                           0
                                                NA
                                                      NA
                                                             0
                                                                   NA
##
    [9,]
             NA
                   NA
                               0
                                           0
                                                NA
                                                      NA
                                                                    1
                         0
                                    NA
                                                            NA
## [10,]
             NA
                   NA
                        NA
                              NA
                                     0
                                            0
                                                 0
                                                      NA
                                                            NA
                                                                   NA
## [11,]
             NA
                   NA
                         0
                               0
                                    NA
                                            0
                                                NA
                                                       0
                                                            NA
                                                                   NA
```