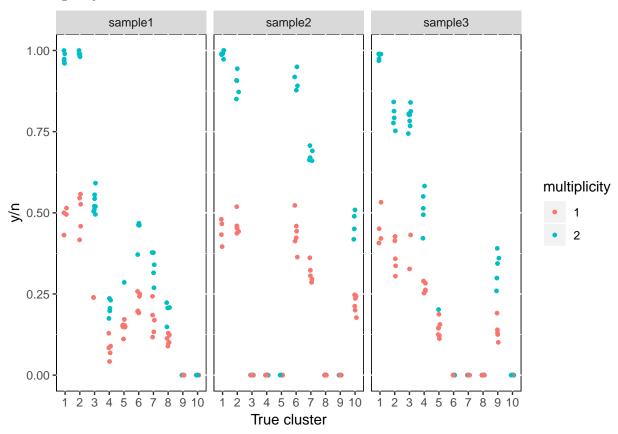
Version 6: Cluster first

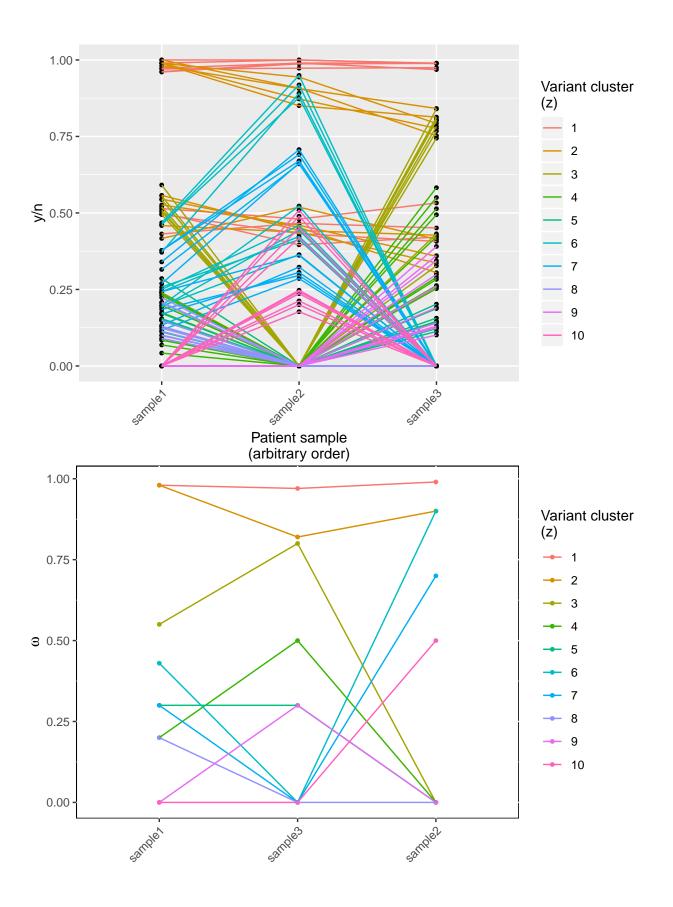
Simulate data

```
I <- 100
K <- 10
S <- 3
set.seed(123)
pi \leftarrow rep(0.1, 10)
\#z \leftarrow sample(1:K, size = I, replace = T, prob = pi)
z <- rep(1:10, each=10)
w \leftarrow matrix(c(0.98, 0.99, 0.97,
               0.98, 0.90, 0.82,
               0.55, 0.00, 0.80,
               0.20, 0.00, 0.50,
               0.30, 0.00, 0.30,
               0.43, 0.90, 0.00,
               0.30, 0.70, 0.00,
               0.20, 0.00, 0.00,
               0.00, 0.00, 0.30,
               0.00, 0.50, 0.00),
             byrow=T,
            nrow=K, ncol=S)
colnames(w) <- paste0("sample", 1:S)</pre>
##
         sample1 sample2 sample3
##
   [1,]
            0.98
                     0.99
                             0.97
                     0.90
                             0.82
## [2,]
            0.98
## [3,]
          0.55
                     0.00
                             0.80
## [4,]
                   0.00
          0.20
                             0.50
## [5,]
            0.30
                     0.00
                             0.30
## [6,]
                  0.90
                             0.00
          0.43
## [7,]
          0.30
                     0.70
                             0.00
## [8,]
            0.20
                     0.00
                             0.00
## [9,]
                     0.00
            0.00
                              0.30
## [10,]
            0.00
                     0.50
                             0.00
tcn <- matrix(2, nrow=I, ncol=S)</pre>
m <- matrix(rep(sample(1:2, size = I, replace = T), S),</pre>
            nrow=I, ncol=S)
W \leftarrow w[z,]
calcTheta <- function(m, tcn, w) {</pre>
  (m * w) / (tcn * w + 2*(1-w))
theta <- calcTheta(m, tcn, W)
n <- replicate(S, rpois(I, 100))</pre>
y <- matrix(NA, nrow=I, ncol=S)
```

Visualize densities of simulated data

Clustering is by ω





functions

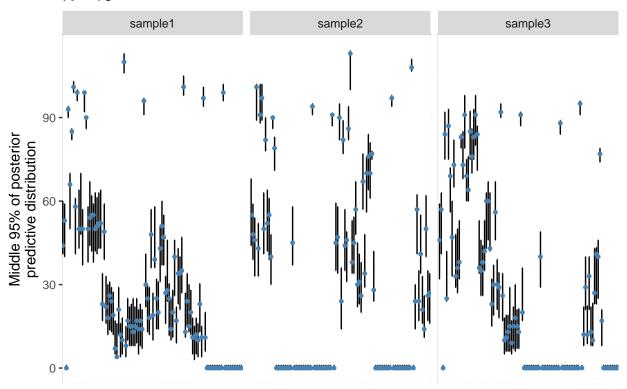
```
runMCMC <- function(data, K, jags.file, inits, params, n.iter, thin) {</pre>
  data$K <- K
  jags.m <- jags.model(jags.file, data,</pre>
                          n.chains = 1,
                          inits = inits,
                          n.adapt = 1000)
  samps <- coda.samples(jags.m, params, n.iter=n.iter, thin=thin)</pre>
  samps
}
getParamChain <- function(samps, param) {</pre>
  chains <- do.call(rbind, samps)</pre>
  chain <- chains[, grep(param, colnames(chains))]</pre>
}
reshapeW <- function(w, S, K) {</pre>
  w.mat <- matrix(w, nrow = K)</pre>
  colnames(w.mat) <- paste0("sample", 1:S)</pre>
  w.mat
}
calcLogLik <- function(z.iter, w.iter, data) {</pre>
  W <- w.iter[z.iter, ]</pre>
  theta <- calcTheta(data$m, data$tcn, W)
  sum(dbinom(data$y, data$n, theta, log=T))
}
calcChainLogLik <- function(samps, data, K) {</pre>
  z.chain <- getParamChain(samps, "z")</pre>
  w.chain <- getParamChain(samps, "w")</pre>
  lik \leftarrow c()
  for(iter in 1:nrow(z.chain)) {
    z.iter <- z.chain[iter,]</pre>
    w.iter <- reshapeW(w.chain[iter,], data$S, K)</pre>
    lik <- c(lik, calcLogLik(z.iter, w.iter, data))</pre>
  }
  mean(lik)
calcBIC <- function(n, k, ll) log(n)*k - 2*ll
```

Cluster - JAGS

```
n.iter = 10000
thin = 7
K <- 10
samps <- runMCMC(test.data, K, jags.file, inits, params, n.iter, thin)</pre>
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
##
  Graph information:
      Observed stochastic nodes: 300
##
      Unobserved stochastic nodes: 431
##
##
      Total graph size: 4196
##
## Initializing model
z.chain <- getParamChain(samps, "z")</pre>
w.chain <- getParamChain(samps, "w")</pre>
mcmc_vals <- summary(samps)$statistics</pre>
mcmc_w <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "Mean"]</pre>
mcmc_w <- matrix(mcmc_w, nrow=K)</pre>
colnames(mcmc_w) <- paste0("sample", 1:S)</pre>
```

PPD

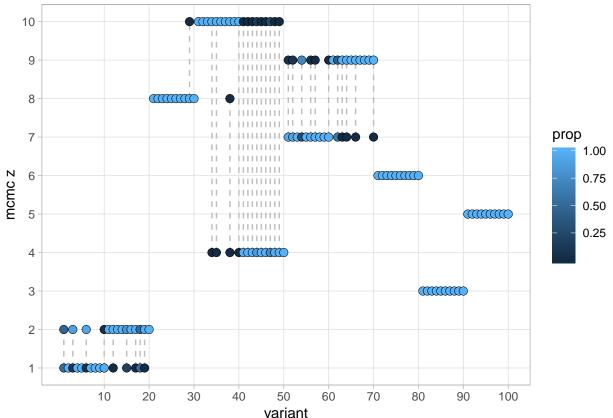
K = 10



observation index (column-major order)

```
plot.z <- function(samps, z) {</pre>
  mcmc vals <- summary(samps)$statistics</pre>
  mcmc_z <- as.vector(mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])</pre>
  plot(z, mcmc_z, type = "p")
  z_comp <- data.frame(z, mcmc_z)</pre>
z.chain.to.tb <- function(z.chain) {</pre>
  z.chain.tb <- z.chain %>%
    as tibble() %>%
    mutate(iter=1:nrow(z.chain)) %>%
    gather(variant, mcmc_z, -c(iter))
  z.chain.tb <- z.chain.tb %>%
    mutate(variant = as.integer(gsub(".*\\[(.*)\\].*", "\\1", z.chain.tb$variant))) %>%
    mutate(true_z = rep(1:10, each=nrow(z.chain)*10)) %>%
    group_by(variant, mcmc_z) %>%
    mutate(count = n()) %>%
    ungroup() %>%
    mutate(iter = NULL)
  z.chain.tb_simp <- distinct(z.chain.tb)</pre>
  z.chain.tb_simp <- z.chain.tb_simp %>%
    group_by(variant) %>%
    mutate(prop = count/sum(count))
  z.chain.tb_simp
}
z.chain.tb <- z.chain.to.tb(z.chain)</pre>
z.chain.tb
## # A tibble: 135 x 5
## # Groups: variant [100]
      variant mcmc_z true_z count
##
                                    prop
##
        <int> <dbl> <int> <int> <dbl>
## 1
          1
                   2
                         1
                             657 0.460
## 2
                              771 0.540
            1
                   1
                          1
## 3
            2
                   1
                          1 1428 1
           3
                         1 1260 0.882
## 4
                  2
## 5
           3
                  1
                         1 168 0.118
                          1 1428 1
## 6
           4
                   1
                          1 1428 1
## 7
            5
                   1
## 8
            6
                   2
                          1 1315 0.921
            6
                             113 0.0791
## 9
                   1
                          1
            7
## 10
                          1 1428 1
## # ... with 125 more rows
z.seg.tb <- tibble(variant = numeric(),</pre>
                    mcmc_z_1 = numeric(),
                    mcmc_z_2 = numeric())
for (i in 1:ncol(z.chain)) {
  z.vals <- as.integer(names(table(z.chain[,i])))</pre>
  if (length(z.vals) > 1) {
    z.seg.tb[i, ] \leftarrow c(i, z.vals[1], z.vals[2])
```

```
} else {
    z.seg.tb[i, ] <- c(i, z.vals, z.vals)</pre>
  }
}
#z.seq.tb
z.plot <- ggplot(z.chain.tb, aes(variant, mcmc_z)) +</pre>
  ylab("mcmc z") +
  xlab("variant") +
  theme_light() +
  scale_y_continuous(breaks = 1:K, minor_breaks=NULL) +
  scale_x_continuous(breaks = seq(10,100,10), minor_breaks=NULL) +
  geom_segment(data = z.seg.tb,
               aes(x=variant, xend=variant,
                   y=mcmc_z_1, yend=mcmc_z_2),
                   color="gray", linetype=2) +
  geom_point(aes(y=mcmc_z, fill=prop),
             pch=21, size=3, stroke=0)
z.plot
```

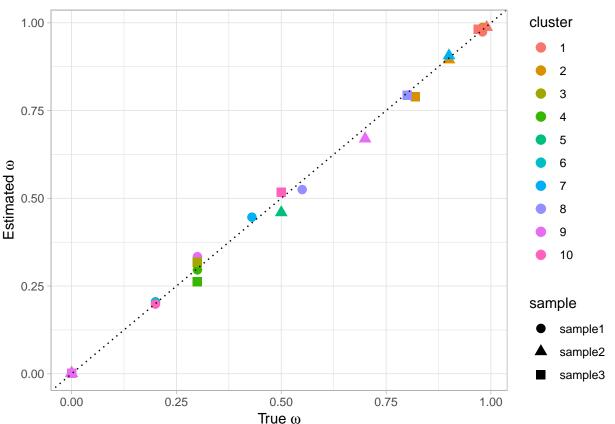


 $\#gsave(file.path(figs.dir, "z_plot.pdf"), z.plot, width=14, height=6)$

```
z.map.tb <- z.chain.tb %>%
group_by(variant) %>%
filter(prop == max(prop))
z.map.tb
```

```
## # A tibble: 100 x 5
## # Groups:
             variant [100]
##
     variant mcmc_z true_z count prop
##
       <int> <dbl> <int> <int> <dbl>
## 1
                  1
                        1
                           771 0.540
## 2
           2
                  1
                         1 1428 1
## 3
           3
                  2
                         1 1260 0.882
                         1 1428 1
## 4
           4
                  1
## 5
           5
                  1
                         1 1428 1
## 6
           6
                  2
                         1 1315 0.921
## 7
           7
                  1
                         1 1428 1
                         1 1428 1
## 8
           8
                  1
           9
                         1 1428 1
## 9
                  1
                         1 1381 0.967
## 10
          10
                  1
## # ... with 90 more rows
z.map <- z.map.tb$mcmc_z</pre>
z.map
               2
                                                    2
                                                       2
                                                          2
                                                             2
                                                                2
                                                                   8
                                                                     8
##
    [1]
            1
         1
                  8 8 8 8 10 10 10 10 10 10 10 10 10 10
                     7 7 7 9 7 7 7 7 7 9
                                                    7
## [47] 4
                                                       9
                                                          9
                                                             9 9 9 9
            4
              4
   [70] 9
            6 6 6 6 6 6 6 6 6 3 3 3 3 3
                                                       3 3 3 3 5 5
## [93] 5 5 5 5 5 5 5 5
z.map.ind <- which(apply(z.chain, 1, function(x) all(x == z.map)))
\omega
mcmc_vals <- summary(samps)$statistics</pre>
mcmc_w <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "Mean"]</pre>
mcmc_w <- matrix(mcmc_w, nrow=K)</pre>
colnames(mcmc_w) <- paste0("sample", 1:S)</pre>
round(mcmc w, 2)
##
        sample1 sample2 sample3
                   0.99
                           0.98
## [1,]
           0.97
## [2,]
           0.99
                   0.89
                           0.79
## [3,]
                   0.00
           0.00
                           0.32
## [4,]
          0.30
                   0.00
                          0.26
## [5,]
         0.00
                   0.46
                          0.00
## [6,]
          0.21
                   0.00
                          0.00
## [7,]
           0.45
                   0.91
                          0.00
## [8,]
          0.52
                   0.00
                          0.79
## [9,]
           0.33
                   0.67
                           0.00
## [10,]
           0.20
                   0.00
                          0.52
mcmc_w_sd <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "SD"]</pre>
mcmc_w_sd <- matrix(mcmc_w_sd, nrow=K)</pre>
colnames(mcmc_w_sd) <- paste0("sample", 1:S)</pre>
# order true w based on mcmc cluster numbering
mcmc_cluster_numbering <- matrix(z.map, nrow = 10)</pre>
get_mode <- function(v) {</pre>
  uniqv <- unique(v)</pre>
```

```
uniqv[which.max(tabulate(match(v, uniqv)))]
}
mcmc_cluster_numbering <- apply(mcmc_cluster_numbering, 2, get_mode)</pre>
true_to_mcmc_w_ordering <- match(1:K, mcmc_cluster_numbering)</pre>
w_ordered <- w[true_to_mcmc_w_ordering, ]</pre>
# scatter
mcmc w tb <- mcmc w %>%
  as_tibble() %>%
  mutate(cluster=1:K) %>%
  gather("sample", "mcmc_w", -c(cluster))
w_master <- w_ordered %>%
  as_tibble() %>%
  mutate(cluster=1:K) %>%
  gather("sample", "true_w", -c(cluster)) %>%
  left_join(mcmc_w_tb, by=c("cluster", "sample")) %>%
  mutate(cluster=factor(cluster),
         sample=factor(sample))
ggplot(w_master, aes(true_w, mcmc_w)) +
  geom_point(size=3, aes(color = cluster, shape = sample)) +
  geom_abline(slope=1, intercept=0, linetype="dotted") +
  xlab(expression("True "*omega)) +
  ylab(expression("Estimated "*omega)) +
  theme_light()
```



Admat functions

```
rand.admat <- function(admat) {</pre>
  for(col in 1:ncol(admat)) {
    ind.0 <- which(admat[,col] == 0) # possible positions (0's)</pre>
    rand.ind <- sample(ind.0, size=1)</pre>
    admat[rand.ind,col] <- 1</pre>
  }
  while (sum(admat[1, ]) == 0) {
    admat <- mutate.admat(admat)</pre>
  admat
}
base.admat <- function(w, zero.thresh=0.01) {</pre>
  cluster.sample.presence <- apply(w, 1, function(x) which(x>zero.thresh))
  K \leftarrow nrow(w)
  S \leftarrow ncol(w)
  all.samples <- 1:S
  admat <- matrix(data=0, nrow=(1+K), ncol=K) # rows=from is root + 1:K, cols=to is 1:K
  # fill in restraints
  # can go from root to anyone, skip and start at nrow=2 (cluster 1)
  for (from in 2:(K+1)) {
    for (to in 1:K) {
      # can't go to self
      if ((from-1) == to) {
        admat[from, to] <- NA
        #print(c(from, to, "self"))
        next
      }
      # hierarchy restraints
      from.samples <- cluster.sample.presence[[from-1]]</pre>
      to.samples <- cluster.sample.presence[[to]]</pre>
      ## no restraints if same sample presence
      if (setequal(from.samples, to.samples)) {
        #print(c(from, to, "same"))
        next
      }
      ## restraint if # from.samples < # to.samples</pre>
      if(length(from.samples) < length(to.samples)) {</pre>
        #print(c(from, to, "from set is smaller than to set"))
        admat[from, to] <- NA
        next
      }
```

```
## no restraints if to.samples is subset of from.samples
      if (all(to.samples %in% from.samples)) {
         #print(c(from, to, "subset"))
        next
      } else {
         #print(c(from, to, "not subset"))
        admat[from, to] <- NA
      }
    }
  }
  admat
}
init.admat <- function(w, zero.thresh) {</pre>
  base <- base.admat(w, zero.thresh)</pre>
  rand.admat(base)
}
mutate.admat <- function(admat, ncol.to.mutate) {</pre>
  # choose a column(s) to mutate
  K <- ncol(admat)</pre>
  rand.ks <- sample(1:K, size=ncol.to.mutate)</pre>
  # mutate columns
  new.admat <- admat</pre>
  for (rand.k in rand.ks) {
    ## possible positions (0's)
    possiblePos <- which(!is.na(admat[, rand.k]) & admat[, rand.k] != 1)</pre>
    ## current position with 1
    ind.1 <- which(admat[, rand.k] == 1)</pre>
    ## select new position
    if (length(possiblePos) == 1) {
      new.1 <- possiblePos</pre>
    } else {
      new.1 <- sample(possiblePos, size=1)</pre>
    }
    new.admat[ind.1, rand.k] <- 0</pre>
    new.admat[new.1, rand.k] <- 1</pre>
  }
  while (sum(new.admat[1, ]) == 0) {
    new.admat <- mutate.admat(admat)</pre>
  }
  new.admat
}
```

SCHISM tree scoring

```
decide.ht <- function(pval, alpha=0.05) {</pre>
  # 1 signals rejection event for null of i \rightarrow j
  if (pval <= alpha) return(1)</pre>
  else return(0)
}
create.cpov <- function(mcmc_w, mcmc_w_sd, alpha=0.05) {</pre>
  cpov <- base.admat(mcmc_w, zero.thresh = 0.01)</pre>
  S <- ncol(mcmc_w) # number of samples
  # root can go to anyone -- all 0's (default base admat value)
  for (r in 2:nrow(cpov)) {
    for (c in 1:ncol(cpov)) {
      if (is.na(cpov[r,c])) next # skip restricted position
      from <- r-1 # 'from' cluster node
      to <- c # 'to' cluster node
      statistic <- 0
      pval <- 0
      for(s in 1:S) {
        d <- mcmc_w[from,s] - mcmc_w[to,s]</pre>
        d_sd \leftarrow sqrt((mcmc_w_sd[from,s])^2 + (mcmc_w_sd[to,s])^2)
        I \leftarrow sum(d < 0)
        statistic <- statistic + (d / d_sd)^2 * I
        for (k in 0:S) {
        pval <- pval + ((1 - pchisq(statistic, k)) * choose(S, k) / (2^S))</pre>
        }
      cpov[r,c] <- decide.ht(pval, alpha)</pre>
    }
  }
  cpov
calc.topology.cost <- function(admat, cpov) {</pre>
  TC <- 0
  edges <- which(admat == 1, arr.ind=T)</pre>
  for (i in 1:nrow(edges)) {
    TC <- TC + cpov[edges[i,1], edges[i,2]]</pre>
  TC
}
calc.mass.cost <- function(admat, mcmc_w) {</pre>
```

```
numChildren <- rowSums(admat, na.rm = T)</pre>
  nodes <- which(numChildren > 0, arr.ind = T) # not leaves
  mc.node <- rep(0, length(nodes))</pre>
  for (i in 1:length(nodes)) {
    node <- nodes[i]</pre>
    # root node: MCF = 1
    parent.w <- rep(1, ncol(mcmc_w))</pre>
    # not root node: look up MCF in mcmc_w
    if (node != 1) {
      parent.w <- mcmc_w[node-1,]</pre>
    kids <- which(admat[node,] == 1, arr.ind = T)</pre>
    if (numChildren[node] > 1) {
       children.w <- colSums(mcmc_w[kids,])</pre>
    } else {
      children.w <- mcmc_w[kids,]</pre>
    }
    mc.s <- ifelse(parent.w >= children.w, 0, children.w - parent.w)
    mc.node[i] <- sqrt(sum(mc.s^2))</pre>
  sum(mc.node)
}
calc.tree.fitness <- function(admat, cpov, mcmc_w, scaling.coeff=5) {</pre>
  TC <- calc.topology.cost(admat, cpov)</pre>
  MC <- calc.mass.cost(admat, mcmc_w)</pre>
  Z \leftarrow TC + MC
  fitness <- exp(-scaling.coeff * Z)</pre>
  fitness
```

Tree MCMC

```
answer[from, to] <- 1</pre>
# }
answer[1,1] \leftarrow answer[2,2] \leftarrow answer[5,3] \leftarrow answer[9,4] \leftarrow answer[10,5] \leftarrow answer[11,6] \leftarrow answer[3,7]
          [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
##
   [1,]
                              0
             1
                   0
                        0
                                   0
                                         0
                                               0
##
    [2,]
            NA
                  1
                        0
                              0
                                   0
                                         0
                                               0
                                                    0
                                                          0
                                                                 0
## [3,]
                                                          0
                                                                 0
            0
                 NA
                        Λ
                              0
                                   0
                                         0
                                               1
                                                    1
## [4,]
                 NA
                                        NA
                                                               NA
           NA
                       NA
                             NA
                                  NA
                                             NA
                                                   NA
                                                         NA
## [5,]
                                         0
            NA
                 NA
                             NA
                                  NA
                                             NA
                                                    0
                                                         NA
                                                                0
                        1
## [6,]
           NA
                 NA
                       NA
                             NA
                                  NA
                                        NA
                                             NA
                                                   NA
                                                         NA
                                                               NA
## [7,]
           NA
                NA
                       NA
                            NA
                                  NA
                                        NA
                                             NA
                                                   NA
                                                         NA
                                                               NA
## [8,]
           NA
                NA
                       NA
                             NA
                                   0
                                         0
                                             NA
                                                   NA
                                                         1
                                                               NA
## [9,]
                        0
                                         0
                                                   NA
                                                         NA
            NA
                 NA
                             1
                                  NA
                                             NA
                                                                1
## [10,]
            NA
                 NA
                       NA
                             NA
                                   1
                                         0
                                              0
                                                   NA
                                                         NA
                                                               NA
## [11,]
            NA
                 NA
                        0
                              0
                                  NA
                                         1
                                             NA
                                                    0
                                                         NA
                                                               NA
cpov <- create.cpov(mcmc w, mcmc w sd)</pre>
calc.tree.fitness(answer, cpov, mcmc_w)
## [1] 0.6366176
calc.tree.fitness(answer, cpov, w_ordered)
## [1] 1
#admat.chain <- list(init.admat(mcmc_w, zero.thresh=0.01))</pre>
# start at best
best.admat.mcmc <- base.admat(mcmc w)</pre>
best.admat.mcmc[1,1] <- best.admat.mcmc[2,2] <- best.admat.mcmc[3,7] <-
  best.admat.mcmc[3,8] <- best.admat.mcmc[5,6] <- best.admat.mcmc[8,9] <-
  best.admat.mcmc[9,4] \leftarrow best.admat.mcmc[9,10] \leftarrow best.admat.mcmc[10,5] \leftarrow
  best.admat.mcmc[11,3] <- 1
admat.chain <- list(best.admat.mcmc)</pre>
score.chain <- c()</pre>
numAccept = 0
ncol.to.mutate <- 1</pre>
numIter <- 1000
for (i in 1:numIter) {
  fit.prev <- calc.tree.fitness(admat.chain[[i]], cpov, mcmc_w)</pre>
  score.chain[i] <- fit.prev</pre>
  admat.star <- mutate.admat(admat.chain[[i]], ncol.to.mutate)</pre>
  fit.star <- calc.tree.fitness(admat.star, cpov, mcmc_w)</pre>
  r <- fit.star / fit.prev
  u <- runif(1,0,1)
  if(u <= r) {
    admat.chain[[i+1]] <- admat.star</pre>
    numAccept <- numAccept + 1</pre>
  } else {
```

```
admat.chain[[i+1]] <- admat.chain[[i]]</pre>
 }
}
score.chain[i+1] <- calc.tree.fitness(admat.chain[[i+1]], cpov, mcmc_w)</pre>
acceptRate <- numAccept/(numIter)</pre>
acceptRate
## [1] 0.315
max(score.chain)
## [1] 0.8652116
max.score.ind <- which(score.chain == max(score.chain))</pre>
if(length(max.score.ind) > 1) max.score.ind <- max.score.ind[1]</pre>
max.admat <- admat.chain[[max.score.ind]]</pre>
max.admat
         [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
##
   [1,]
##
                            0
                                 0
                                      0
## [2,]
                                                      0
                                                            0
           NA
                 1
                      0
                            0
                                 0
                                      0
                                           0
                                                 0
## [3,]
           0
                NA
                      0
                            0
                                 0
                                      0
                                           1
                                                1
                                                      0
                                                            0
## [4,]
                NA
                     NA
                                     NA
                                                           NA
           NA
                           NA
                                NA
                                          NA
                                                NA
                                                     NA
## [5,]
          NA
               NA
                      0
                          NA
                                NA
                                     1
                                          NA
                                                0
                                                     NA
                                                            0
## [6,]
           NA
               NA
                     NA
                          NA
                                NA
                                     NA
                                          NA
                                                NA
                                                     NA
                                                           NA
## [7,]
          NA
               NA
                     NA
                          NA
                                NA
                                     NA
                                          NA
                                                NA
                                                    NA
                                                           NA
## [8,]
               NA
                     NA
          NA
                          NA
                                0
                                     0
                                          NA
                                                NA
                                                     1
                                                           NA
## [9,]
          NA
               NA
                     0
                          1
                                NA
                                      0
                                          NA
                                                NA
                                                     NA
                                                           1
## [10,]
           NA
                NA
                     NA
                           NA
                                1
                                      0
                                          0
                                                NA
                                                     NA
                                                           NA
## [11,]
                NA
                            0
                                NA
                                      0
                                                     NA
                                                           NA
           NA
                      1
                                          NA
                                                 0
score_chain_master <- tibble(fitness = score.chain,</pre>
                              iter = 1:length(score.chain),
                              label = paste0("col mutated = ",
                                              ncol.to.mutate,
                                              "; acceptance rate = ",
                                              acceptRate))
```

Mutate 2 columns

```
admat.chain <- list(best.admat.mcmc)
score.chain <- c()
numAccept = 0
ncol.to.mutate <- 2
numIter <- 1000
for (i in 1:numIter) {
   fit.prev <- calc.tree.fitness(admat.chain[[i]], cpov, mcmc_w)
   score.chain[i] <- fit.prev

   admat.star <- mutate.admat(admat.chain[[i]], ncol.to.mutate)
   fit.star <- calc.tree.fitness(admat.star, cpov, mcmc_w)

r <- fit.star / fit.prev
u <- runif(1,0,1)
if(u <= r) {</pre>
```

```
admat.chain[[i+1]] <- admat.star</pre>
    numAccept <- numAccept + 1</pre>
  } else {
    admat.chain[[i+1]] <- admat.chain[[i]]</pre>
  }
score.chain[i+1] <- calc.tree.fitness(admat.chain[[i+1]], cpov, mcmc_w)</pre>
acceptRate <- numAccept/(numIter)</pre>
acceptRate
## [1] 0.152
score_chain_master <- rbind(score_chain_master,</pre>
                              tibble(fitness = score.chain,
                                      iter = 1:length(score.chain),
                                      label = paste0("col mutated = ",
                                                       ncol.to.mutate,
                                                       "; acceptance rate = ",
                                                       acceptRate)))
```

Mutate 3 columns

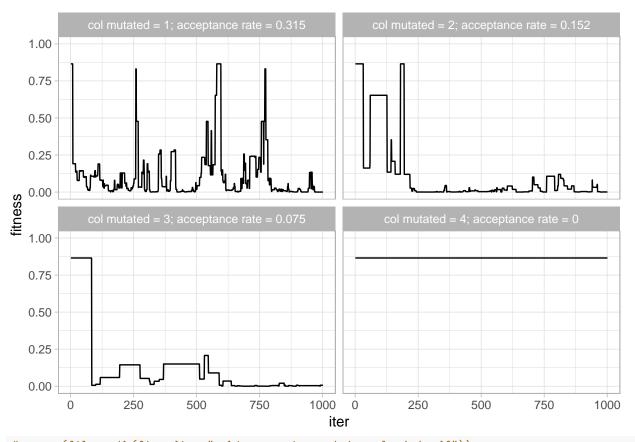
```
admat.chain <- list(best.admat.mcmc)</pre>
score.chain <- c()</pre>
numAccept = 0
ncol.to.mutate <- 3</pre>
numIter <- 1000
for (i in 1:numIter) {
  fit.prev <- calc.tree.fitness(admat.chain[[i]], cpov, mcmc_w)</pre>
  score.chain[i] <- fit.prev</pre>
    admat.star <- mutate.admat(admat.chain[[i]], ncol.to.mutate)</pre>
    fit.star <- calc.tree.fitness(admat.star, cpov, mcmc_w)</pre>
  r <- fit.star / fit.prev
  u <- runif(1,0,1)
  if(u <= r) {
    admat.chain[[i+1]] <- admat.star</pre>
    numAccept <- numAccept + 1</pre>
  } else {
    admat.chain[[i+1]] <- admat.chain[[i]]</pre>
  }
score.chain[i+1] <- calc.tree.fitness(admat.chain[[i+1]], cpov, mcmc_w)</pre>
acceptRate <- numAccept/(numIter)</pre>
acceptRate
## [1] 0.075
```

ncol.to.mutate,

```
"; acceptance rate = ", acceptRate)))
```

Mutate 4 columns

```
admat.chain <- list(best.admat.mcmc)</pre>
score.chain <- c()</pre>
numAccept = 0
ncol.to.mutate <- 4</pre>
numIter <- 1000
for (i in 1:numIter) {
  fit.prev <- calc.tree.fitness(admat.chain[[i]], cpov, mcmc_w)</pre>
  score.chain[i] <- fit.prev</pre>
    admat.star <- mutate.admat(admat.chain[[i]], ncol.to.mutate)</pre>
    fit.star <- calc.tree.fitness(admat.star, cpov, mcmc_w)</pre>
  r <- fit.star / fit.prev
  u <- runif(1,0,1)
  if(u <= r) {
    admat.chain[[i+1]] <- admat.star</pre>
    numAccept <- numAccept + 1</pre>
  } else {
    admat.chain[[i+1]] <- admat.chain[[i]]</pre>
  }
}
score.chain[i+1] <- calc.tree.fitness(admat.chain[[i+1]], cpov, mcmc_w)</pre>
acceptRate <- numAccept/(numIter)</pre>
acceptRate
## [1] 0
score_chain_master <- rbind(score_chain_master,</pre>
                               tibble(fitness = score.chain,
                                      iter = 1:length(score.chain),
                                      label = paste0("col mutated = ",
                                                       ncol.to.mutate,
                                                       "; acceptance rate = ",
                                                       acceptRate)))
ggplot(score_chain_master, aes(x = iter, y = fitness)) +
  geom_line() +
  facet_wrap(~label) +
  ylim(0,1) +
  theme light()
```



 ${\it \#ggsave} (file.path(figs.dir, "schism_scoring_mutate_cols_1-4.pdf"))$

```
restrictions <- base.admat(mcmc_w)

calc_possible_trees_restrictions <- function(restrictions) {
  prod(apply(restrictions, 2, function(x) sum(!is.na(x))))
}

formatC(calc_possible_trees_restrictions(restrictions))</pre>
```

```
## [1] "1.92e+06"

calc_all_trees <- function(K) {
  total_possible <- (K+1)^K
  no_root <- K^K
  actual_trees <- total_possible - no_root
  actual_trees
}

formatC(calc_all_trees(K))</pre>
```

[1] "1.594e+10"