

## Version 6: Cluster first

### Simulate data

```
I <- 100
K <- 10
S <- 3

set.seed(123)

pi <- rep(0.1, 10)
#z <- sample(1:K, size = I, replace = T, prob = pi)
z <- rep(1:10, each=10)
w <- matrix(c(0.98, 0.99, 0.97,
              0.98, 0.90, 0.82,
              0.55, 0.00, 0.80,
              0.20, 0.00, 0.50,
              0.30, 0.00, 0.30,
              0.43, 0.90, 0.00,
              0.30, 0.70, 0.00,
              0.20, 0.00, 0.00,
              0.00, 0.00, 0.30,
              0.00, 0.50, 0.00),
            byrow=T,
            nrow=K, ncol=S)

colnames(w) <- paste0("sample", 1:S)
w

##      sample1 sample2 sample3
## [1,]    0.98    0.99    0.97
## [2,]    0.98    0.90    0.82
## [3,]    0.55    0.00    0.80
## [4,]    0.20    0.00    0.50
## [5,]    0.30    0.00    0.30
## [6,]    0.43    0.90    0.00
## [7,]    0.30    0.70    0.00
## [8,]    0.20    0.00    0.00
## [9,]    0.00    0.00    0.30
## [10,]   0.00    0.50    0.00

tcn <- matrix(2, nrow=I, ncol=S)
m <- matrix(rep(sample(1:2, size = I, replace = T), S),
            nrow=I, ncol=S)
W <- w[z, ]
calcTheta <- function(m, tcn, w) {
  (m * w) / (tcn * w + 2*(1-w))
}

theta <- calcTheta(m, tcn, W)

n <- replicate(S, rpois(I, 100))
y <- matrix(NA, nrow=I, ncol=S)
```

```

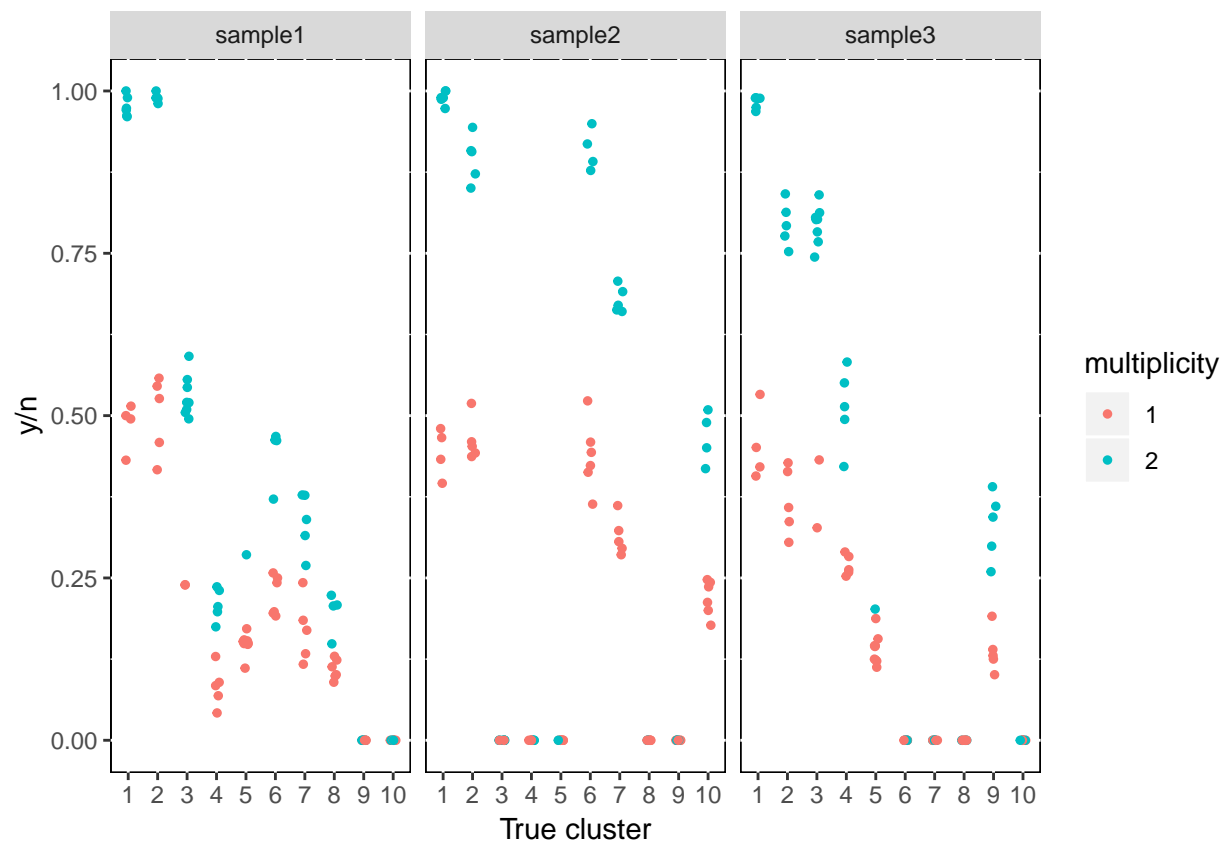
for (i in 1:I) {
  for (s in 1:S) {
    y[i, s] <- rbinom(1, n[i, s], theta[i,s])
  }
}

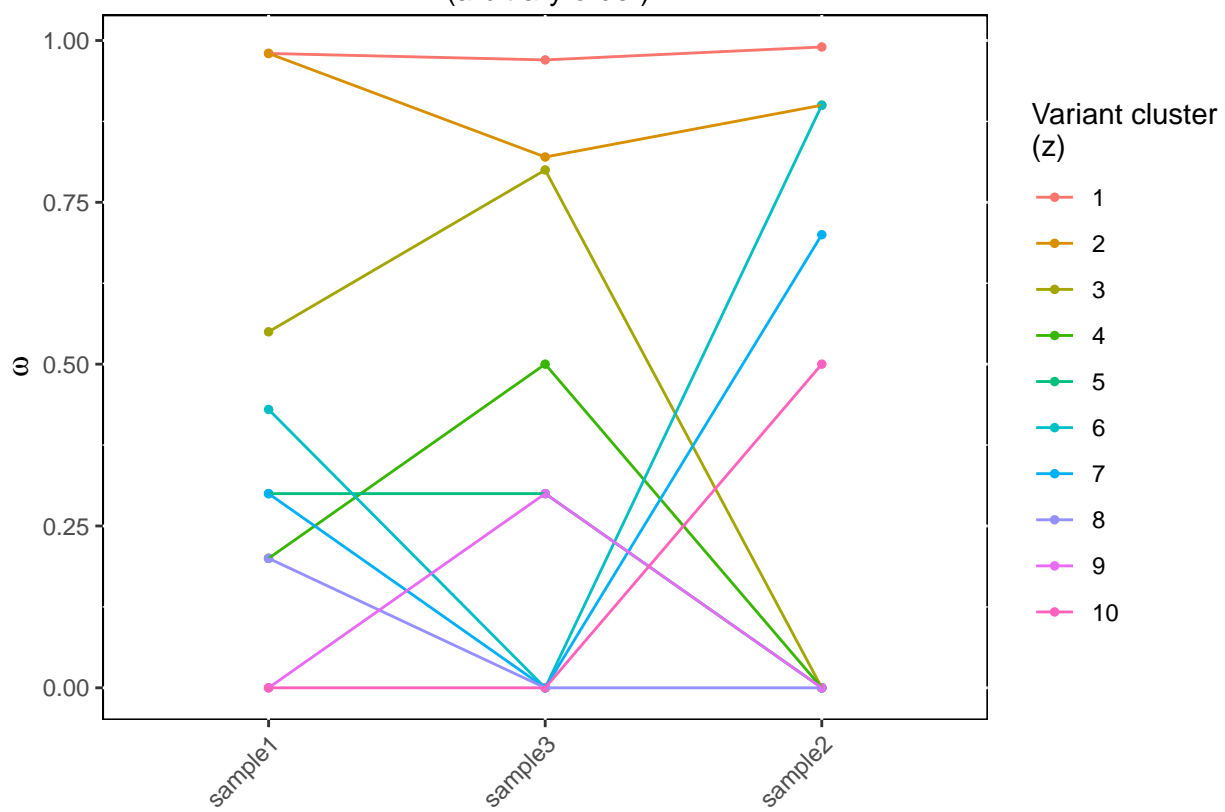
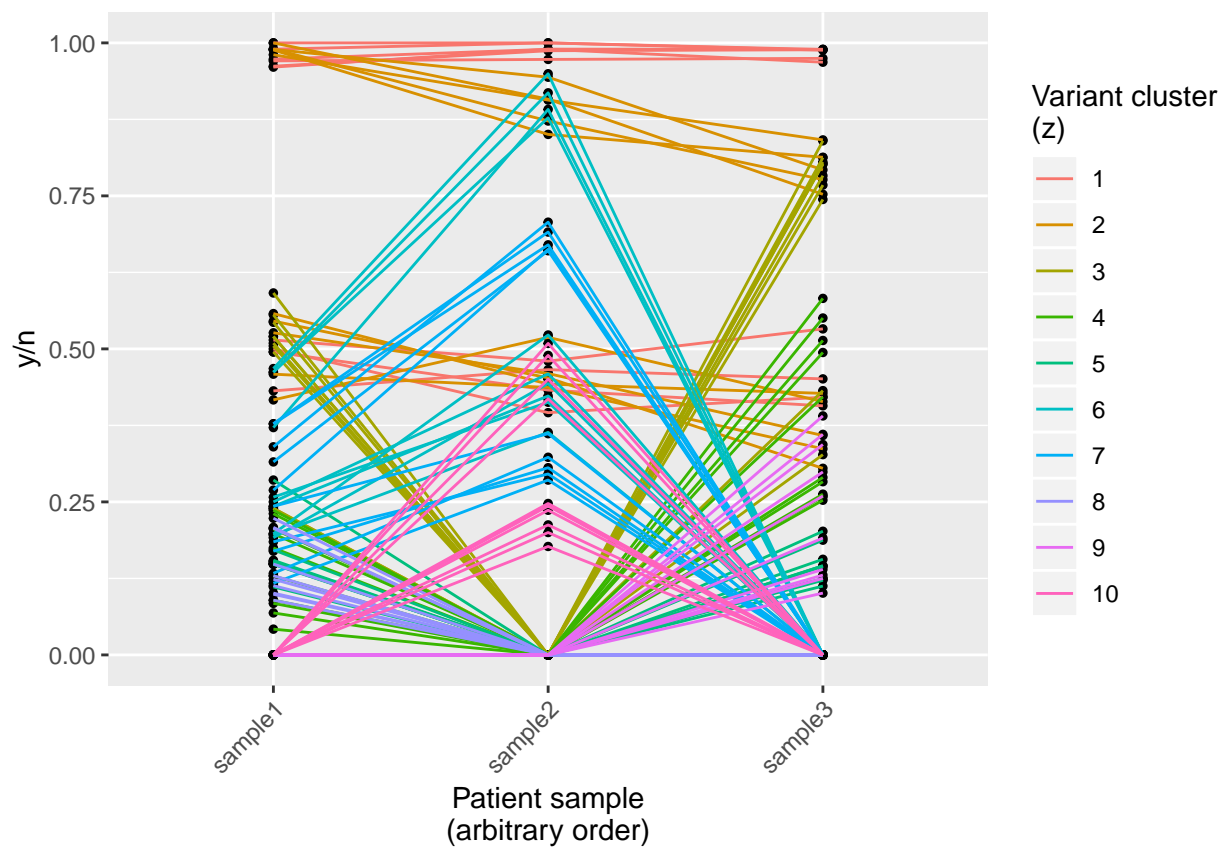
test.data <- list("I" = I, "S" = S, "K" = K,
                 "y" = y, "n" = n,
                 "m" = m, "tcn" = tcn)

```

## Visualize densities of simulated data

Clustering is by  $\omega$





## functions

```
runMCMC <- function(data, K, jags.file, inits, params, n.iter, thin) {
  data$K <- K
  jags.m <- jags.model(jags.file, data,
    n.chains = 1,
    inits = inits,
    n.adapt = 1000)
  samps <- coda.samples(jags.m, params, n.iter=n.iter, thin=thin)
  samps
}

getParamChain <- function(samps, param) {
  chains <- do.call(rbind, samps)
  chain <- chains[, grep(param, colnames(chains))]
}

reshapeW <- function(w, S, K) {
  w.mat <- matrix(w, nrow = K)
  colnames(w.mat) <- paste0("sample", 1:S)
  w.mat
}

calcLogLik <- function(z.iter, w.iter, data) {
  W <- w.iter[z.iter, ]
  theta <- calcTheta(data$m, data$tcn, W)
  sum(dbinom(data$y, data$n, theta, log=T))
}

calcChainLogLik <- function(samps, data, K) {
  z.chain <- getParamChain(samps, "z")
  w.chain <- getParamChain(samps, "w")
  lik <- c()
  for(iter in 1:nrow(z.chain)) {
    z.iter <- z.chain[iter,]
    w.iter <- reshapeW(w.chain[iter,], data$S, K)
    lik <- c(lik, calcLogLik(z.iter, w.iter, data))
  }
  mean(lik)
}

calcBIC <- function(n, k, ll) log(n)*k - 2*ll
```

## Cluster – JAGS

```
jags.file <- file.path(models.dir, "w.jags")
inits <- list(".RNG.name" = "base::Wichmann-Hill",
  ".RNG.seed" = 123)
test.data <- list("I" = I, "S" = S,
  "y" = y, "n" = n,
  "m" = m, "tcn" = tcn)
params <- c("z", "w", "ystar")
```

```

n.iter = 10000
thin = 7
K <- 10

samps <- runMCMC(test.data, K, jags.file, inits, params, n.iter, thin)

## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 300
##   Unobserved stochastic nodes: 431
##   Total graph size: 4196
##
## Initializing model

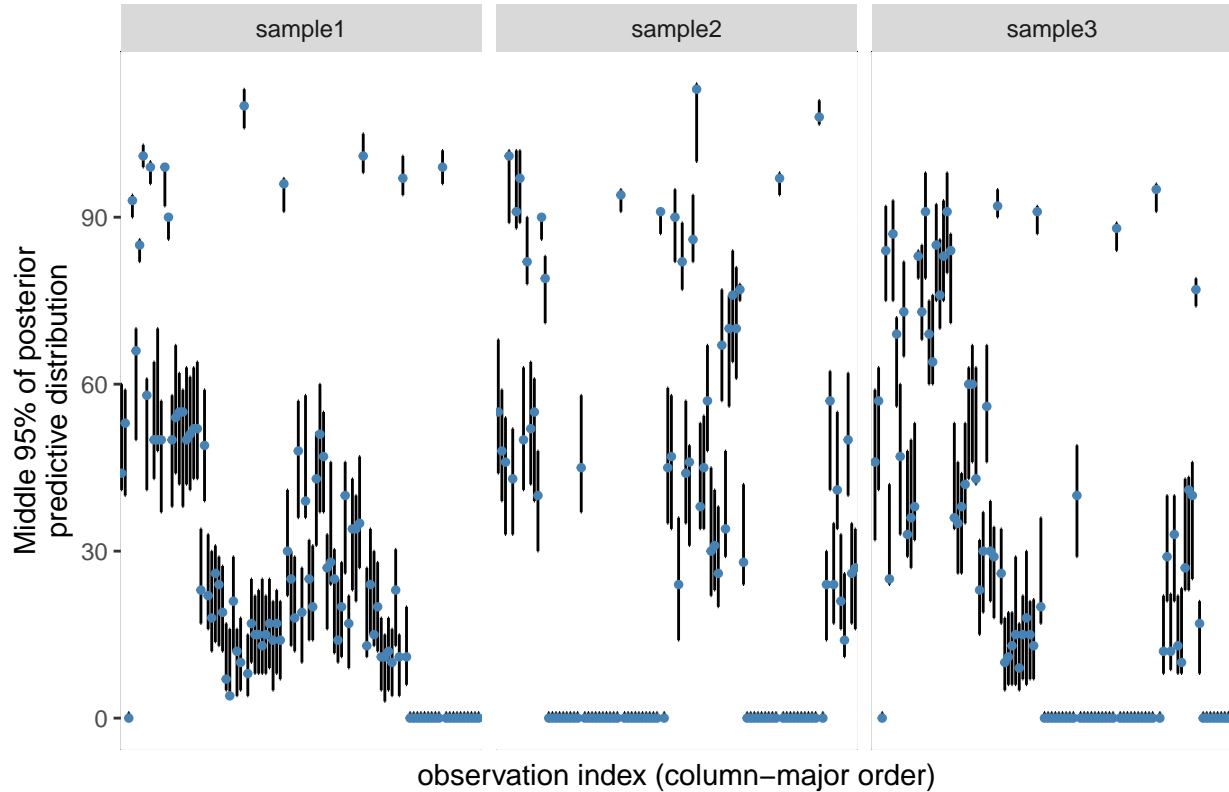
z.chain <- getParamChain(samps, "z")
w.chain <- getParamChain(samps, "w")

mcmc_vals <- summary(samps)$statistics
mcmc_w <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "Mean"]
mcmc_w <- matrix(mcmc_w, nrow=K)
colnames(mcmc_w) <- paste0("sample", 1:S)

```

## PPD

K = 10



## Z

```

plot.z <- function(samps, z) {
  mcmc_vals <- summary(samps)$statistics
  mcmc_z <- as.vector(mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])
  plot(z, mcmc_z, type = "p")
  z_comp <- data.frame(z, mcmc_z)
}

z.chain.to.tb <- function(z.chain) {
  z.chain.tb <- z.chain %>%
    as_tibble() %>%
    mutate(iter=1:nrow(z.chain)) %>%
    gather(variant, mcmc_z, -c(iter))
  z.chain.tb <- z.chain.tb %>%
    mutate(variant = as.integer(gsub(".*\\[(.*)\\].*", "\\1", z.chain.tb$variant))) %>%
    mutate(true_z = rep(1:10, each=nrow(z.chain)*10)) %>%
    group_by(variant, mcmc_z) %>%
    mutate(count = n())
  z.chain.tb_simp <- distinct(select(z.chain.tb, -c(iter)))
  z.chain.tb_simp %>%
    group_by(variant) %>%
    mutate(prop = count/sum(count))
}

z.chain.tb <- z.chain.to.tb(z.chain)
z.chain.tb

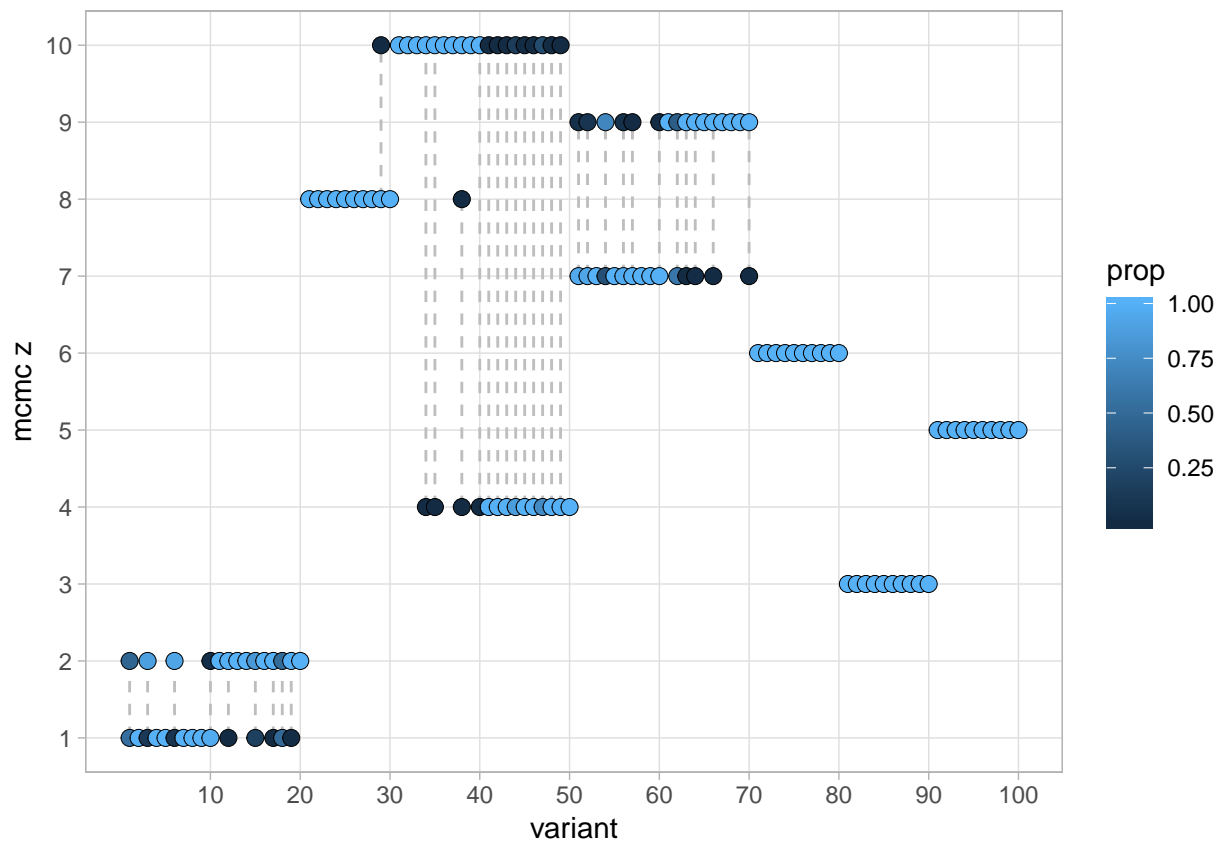
## # A tibble: 135 x 5
## # Groups:   variant [100]
##   variant mcmc_z true_z count  prop
##   <int>   <dbl> <int> <int> <dbl>
## 1     1     2     1    657 0.460
## 2     1     1     1    771 0.540
## 3     2     1     1   1428 1
## 4     3     2     1   1260 0.882
## 5     3     1     1    168 0.118
## 6     4     1     1   1428 1
## 7     5     1     1   1428 1
## 8     6     2     1   1315 0.921
## 9     6     1     1    113 0.0791
## 10    7     1     1   1428 1
## # ... with 125 more rows

z.seg.tb <- tibble(variant = numeric(),
                   mcmc_z_1 = numeric(),
                   mcmc_z_2 = numeric())
for (i in 1:ncol(z.chain)) {
  z.vals <- as.integer(names(table(z.chain[,i])))
  if (length(z.vals) > 1) {
    z.seg.tb[i, ] <- c(i, z.vals[1], z.vals[2])
  } else {
    z.seg.tb[i, ] <- c(i, z.vals, z.vals)
  }
}

```

```
#z.seg.tb
z.plot <- ggplot(z.chain.tb, aes(variant, mcmc_z)) +
  ylab("mcmc z") +
  xlab("variant") +
  theme_light() +
  scale_y_continuous(breaks = 1:K, minor_breaks=NULL) +
  scale_x_continuous(breaks = seq(10,100,10), minor_breaks=NULL) +
  geom_segment(data = z.seg.tb,
    aes(x=variant, xend=variant,
        y=mcmc_z_1, yend=mcmc_z_2),
    color="gray", linetype=2) +
  geom_point(aes(y=mcmc_z, fill=prop),
    pch=21, size=3, stroke=0)
```

z.plot



```
#gsave(file.path(figs.dir, "zplot.pdf"), z.plot, width=14, height=6)

# mcmc_vals <- summary(samps)$statistics
# mcmc_z <- as.vector(mcmc_vals[subscr(rownames(mcmc_vals), 1, 1) == "z", "Mean"])
# plot.z(samps, z)
```

```
z.map.tb <- z.chain.tb %>%
  group_by(variant) %>%
  filter(prop == max(prop))
z.map.tb
```

```
## # A tibble: 100 x 5
## # Groups:   variant [100]
##   variant mcmc_z true_z count  prop
##   <int>   <dbl>   <int> <int> <dbl>
## 1       1       1       1     771 0.540
## 2       2       1       1    1428 1
## 3       3       2       1    1260 0.882
## 4       4       1       1    1428 1
## 5       5       1       1    1428 1
## 6       6       2       1    1315 0.921
## 7       7       1       1    1428 1
## 8       8       1       1    1428 1
## 9       9       1       1    1428 1
## 10      10       1       1    1381 0.967
## # ... with 90 more rows
```

```
z.map <- z.map.tb$mcmc_z
z.map
```

```
## [1] 1 1 2 1 1 2 1 1 1 1 2 2 2 2 2 2 2 2 2 8 8 8
## [24] 8 8 8 8 8 8 8 10 10 10 10 10 10 10 10 10 4 4 4 4 4 4
## [47] 4 4 4 4 7 7 7 9 7 7 7 7 7 9 7 9 9 9 9 9 9 9
## [70] 9 6 6 6 6 6 6 6 6 6 6 3 3 3 3 3 3 3 3 3 5 5
## [93] 5 5 5 5 5 5 5 5
```

```
z.map.ind <- which(apply(z.chain, 1, function(x) all(x == z.map)))
w.chain.map <- w.chain[z.map.ind, ]
w.map.tb <- w.chain.map %>%
  as_tibble() %>%
  mutate(iter=1:nrow(w.chain.map)) %>%
  gather(ind, mcmc_w, -c(iter)) %>%
  group_by(ind) %>%
  summarize(mean_w = mean(mcmc_w))
w.map.tb <- w.map.tb %>%
  mutate(cluster = as.integer(gsub(".*\\[(.*)\\],.*", "\\1", w.map.tb$ind))) %>%
  mutate(sample = as.integer(gsub(".*\\,(.*)\\]", "\\1", w.map.tb$ind))) %>%
  arrange(cluster)
#w.map.tb
w.map <- matrix(data=w.map.tb$mean_w, nrow=10, ncol=3, byrow=TRUE)
w.map
```

```
##           [,1]           [,2]           [,3]
## [1,] 0.973637944 0.988597020 0.9820710869
## [2,] 0.986416825 0.898308330 0.7872189454
## [3,] 0.001522582 0.001459451 0.3172062772
## [4,] 0.298899414 0.001986741 0.2629240648
## [5,] 0.001516133 0.456360105 0.0009553129
## [6,] 0.204992711 0.001354114 0.0010398326
## [7,] 0.446984100 0.906262831 0.0012807779
## [8,] 0.526633332 0.001433847 0.7948906517
## [9,] 0.333174387 0.666250526 0.0011254626
## [10,] 0.195689330 0.001694563 0.5222219276
```



## Admat

```
rand.admat <- function(admat) {
  for(col in 1:ncol(admat)) {
    ind.0 <- which(admat[,col] == 0) # possible positions (0's)
    rand.ind <- sample(ind.0, size=1)
    admat[rand.ind,col] <- 1
  }

  while (sum(admat[1,]) == 0) {
    admat <- mutate.admat(admat)
  }

  admat
}

base.admat <- function(w, zero.thresh=0.01) {
  cluster.sample.presence <- apply(w, 1, function(x) which(x>zero.thresh))
  K <- nrow(w)
  S <- ncol(w)
  all.samples <- 1:S
  admat <- matrix(data=0, nrow=(1+K), ncol=K) # rows=from is root + 1:K, cols=to is 1:K

  # fill in restraints
  # can go from root to anyone, skip and start at nrow=2 (cluster 1)
  for (from in 2:(K+1)) {
    for (to in 1:K) {

      # can't go to self
      if ((from-1) == to) {
        admat[from, to] <- NA
        #print(c(from, to, "self"))
        next
      }

      # hierarchy restraints
      from.samples <- cluster.sample.presence[[from-1]]
      to.samples <- cluster.sample.presence[[to]]

      ## no restraints if same sample presence
      if (setequal(from.samples, to.samples)) {
        #print(c(from, to, "same"))
        next
      }

      ## restraint if # from.samples < # to.samples
      if (length(from.samples) < length(to.samples)) {
        #print(c(from, to, "from set is smaller than to set"))
        admat[from, to] <- NA
        next
      }

      ## no restraints if to.samples is subset of from.samples
      if (all(to.samples %in% from.samples)) {
        #print(c(from, to, "subset"))
      }
    }
  }
}
```

```

    next
  } else {
    #print(c(from, to, "not subset"))
    admat[from, to] <- NA
  }
}
admat
}

init.admat <- function(w, zero.thresh) {
  base <- base.admat(w, zero.thresh)
  rand.admat(base)
}

mutate.admat <- function(admat) {
  # choose a column to mutate
  K <- ncol(admat)
  rand.k <- sample(1:K, size=1)

  # mutate
  ## possible positions (0's)
  possiblePos <- which(!is.na(admat[, rand.k]) & admat[, rand.k] != 1)
  ## current position with 1
  ind.1 <- which(admat[, rand.k] == 1)
  ## select new position
  if (length(possiblePos) == 1) {
    new.1 <- possiblePos
  } else {
    new.1 <- sample(possiblePos, size=1)
  }

  new.admat <- admat
  new.admat[ind.1, rand.k] <- 0
  new.admat[new.1, rand.k] <- 1

  while (sum(new.admat[1, ]) == 0) {
    new.admat <- mutate.admat(admat)
  }
  new.admat
}

decide.ht <- function(pval, alpha=0.05) {
  # 1 signals rejection event for null of i -> j
  if (pval <= alpha) return(1)
  else return(0)
}

create.cpov <- function(mcmc_w, mcmc_w_sd, alpha=0.05) {
  cpov <- base.admat(mcmc_w, zero.thresh = 0.01)
  S <- ncol(mcmc_w) # number of samples

  # root can go to anyone -- all 0's (default base admat value)

```

```

for (r in 2:nrow(cpov)) {
  for (c in 1:ncol(cpov)) {

    if (is.na(cpov[r,c])) next # skip restricted position

    from <- r-1 # 'from' cluster node
    to <- c # 'to' cluster node

    statistic <- 0
    pval <- 0

    for(s in 1:S) {
      d <- mcmc_w[from,s] - mcmc_w[to,s]
      d_sd <- sqrt((mcmc_w_sd[from,s])^2 + (mcmc_w_sd[to,s])^2)
      I <- sum(d < 0)
      statistic <- statistic + (d / d_sd)^2 * I

      for (k in 0:S) {
        pval <- pval + ((1 - pchisq(statistic, k)) * choose(S, k) / (2^S))
      }
    }
    cpov[r,c] <- decide.ht(pval, alpha)
  }
}
cpov
}

calc.topology.cost <- function(admat, cpov) {

  TC <- 0
  edges <- which(admat == 1, arr.ind=T)
  for (i in 1:nrow(edges)) {
    TC <- TC + cpov[edges[i,1], edges[i,2]]
  }

  TC
}

calc.mass.cost <- function(admat, mcmc_w) {

  numChildren <- rowSums(admat, na.rm = T)
  nodes <- which(numChildren > 0, arr.ind = T) # not leaves
  mc.node <- rep(0, length(nodes))

  for (i in 1:length(nodes)) {
    node <- nodes[i]

    # root node: MCF = 1
    parent.w <- rep(1, ncol(mcmc_w))
    # not root node: look up MCF in mcmc_w
    if (node != 1) {
      parent.w <- mcmc_w[node-1,]
    }
  }
}

```

```

kids <- which(admat[node,] == 1, arr.ind = T)
if (numChildren[node] > 1) {
  children.w <- colSums(mcmc_w[kids,])
} else {
  children.w <- mcmc_w[kids,]
}

mc.s <- ifelse(parent.w >= children.w, 0, children.w - parent.w)
mc.node[i] <- sqrt(sum(mc.s^2))
}

sum(mc.node)
}

calc.tree.fitness <- function(admat, cpov, mcmc_w, scaling.coeff=5) {
  TC <- calc.topology.cost(admat, cpov)
  MC <- calc.mass.cost(admat, mcmc_w)
  Z <- TC + MC
  fitness <- exp(-scaling.coeff * Z)
  fitness
}

set.seed(1234)

mcmc_vals <- summary(samps)$statistics
mcmc_w <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "Mean"]
mcmc_w <- matrix(mcmc_w, nrow=K)
colnames(mcmc_w) <- paste0("sample", 1:S)

mcmc_w_sd <- mcmc_vals[substr(rownames(mcmc_vals), 1, 1) == "w", "SD"]
mcmc_w_sd <- matrix(mcmc_w_sd, nrow=K)
colnames(mcmc_w_sd) <- paste0("sample", 1:S)

answer <- base.admat(mcmc_w)
answer[1,1] <- answer[2,2] <- answer[3,7] <- answer[3,8] <-
  answer[5,3] <- answer[8,9] <- answer[9,4] <- answer[9,10] <-
  answer[10,5] <- answer[11,6] <- 1
answer

##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,]    1    0    0    0    0    0    0    0    0    0
## [2,]   NA    1    0    0    0    0    0    0    0    0
## [3,]    0   NA    0    0    0    0    1    1    0    0
## [4,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [5,]   NA   NA    1   NA   NA    0   NA    0   NA    0
## [6,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [7,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [8,]   NA   NA   NA   NA    0    0   NA   NA    1   NA
## [9,]   NA   NA    0    1   NA    0   NA   NA   NA    1
## [10,]  NA   NA   NA   NA    1    0    0   NA   NA   NA
## [11,]  NA   NA    0    0   NA    1   NA    0   NA   NA

```

```

cpov <- create.cpov(mcmc_w, mcmc_w_sd)

calc.tree.fitness(answer, cpov, mcmc_w)

## [1] 0.6366176

admat.chain <- list(init.admat(mcmc_w, zero.thresh=0.01))
score.chain <- c()

numAccept = 0

numIter <- 1000
for (i in 1:numIter) {
  fit.prev <- calc.tree.fitness(admat.chain[[i]], cpov, mcmc_w)
  score.chain[i] <- fit.prev

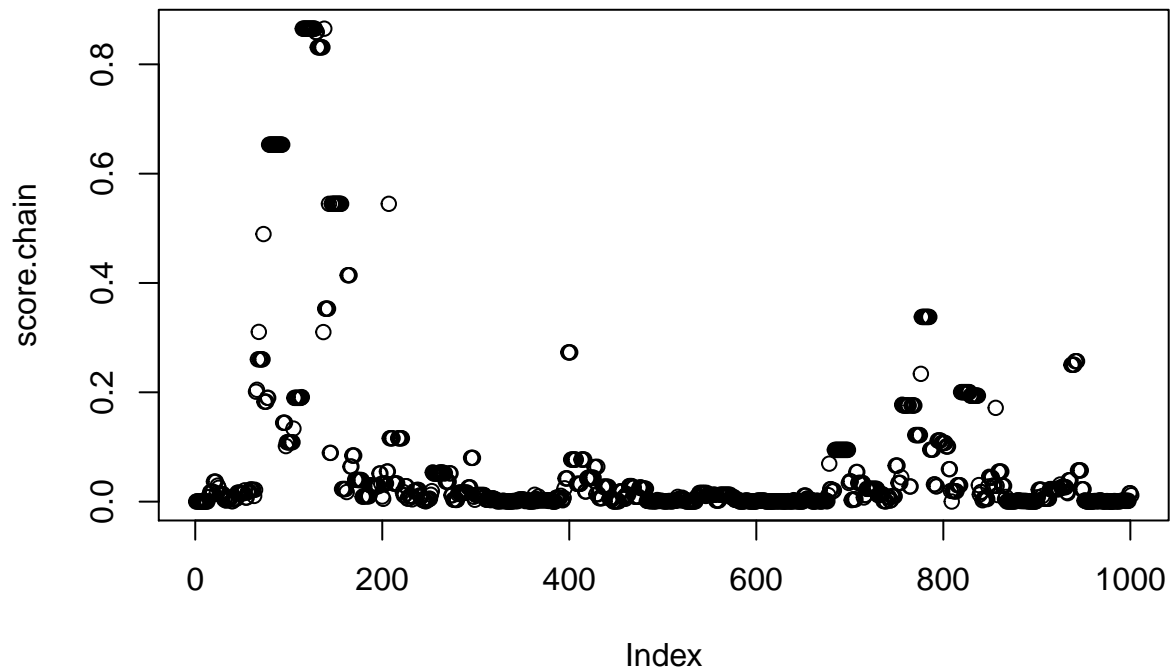
  fit.star <- 0
  while (fit.star < 0.0001) {
    admat.star <- mutate.admat(admat.chain[[i]])
    fit.star <- calc.tree.fitness(admat.star, cpov, mcmc_w)
  }

  r <- fit.star / fit.prev
  u <- runif(1,0,1)
  if(u <= r) {
    admat.chain[[i+1]] <- admat.star
    numAccept <- numAccept + 1
  } else {
    admat.chain[[i+1]] <- admat.chain[[i]]
  }
}
score.chain[i+1] <- calc.tree.fitness(admat.chain[[i+1]], cpov, mcmc_w)
acceptRate <- numAccept/(numIter)
acceptRate

## [1] 0.496

plot(score.chain)

```



```
max(score.chain)
```

```
## [1] 0.8652116
```

```
max.score.ind <- which(score.chain == max(score.chain))
if(length(max.score.ind) > 1) max.score.ind <- max.score.ind[1]
max.admat <- admat.chain[[max.score.ind]]
max.admat
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## [1,]    1    0    0    0    0    0    0    0    0    0
## [2,]   NA    1    0    0    0    0    0    0    0    0
## [3,]    0   NA    0    0    0    0    1    1    0    0
## [4,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [5,]   NA   NA    0   NA   NA    1   NA    0   NA    0
## [6,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [7,]   NA   NA   NA   NA   NA   NA   NA   NA   NA   NA
## [8,]   NA   NA   NA   NA    0    0   NA   NA    1   NA
## [9,]   NA   NA    0    1   NA    0   NA   NA   NA    1
## [10,]  NA   NA   NA   NA    1    0    0   NA   NA   NA
## [11,]  NA   NA    1    0   NA    0   NA    0   NA   NA
```