

## First Derivative Test

For finding local minimum and maximum

The First Derivative Test is a consequence of the Increasing/Decreasing Test (see my earlier video).

### **First Derivative Test:**

Suppose that  $c$  is a critical number of a continuous function  $f$ :

- (a) If  $f'$  changes from positive to negative at  $c$ , then  $f$  has a local maximum at  $c$ .
- (b) If  $f'$  changes from negative to positive at  $c$ , then  $f$  has a local minimum at  $c$ .
- (c) If  $f'$  does not change sign at  $c$  (for example, if  $f'$  is positive on both sides of  $c$  or negative on both sides), then  $f$  has no local maximum or minimum at  $c$ .

4 Scenarios:

