

5.

$$y = 3x^5 - 10x^3 + 15$$

$$y' = 15x^4 - 30x^2$$

$$\begin{aligned} y'' &= 60x^3 - 60x \\ &= 60x(x^2 - 1) \\ &= 60x(x-1)(x+1) \end{aligned}$$

$$y'' \quad \begin{array}{c} - \quad + \quad - \quad + \\ \hline -1 \quad 0 \quad 1 \end{array}$$

The function is concave up over the interval $x \in (-1, 0) \cup (1, \infty)$ and concave down over the interval $x \in (-\infty, -1) \cup (0, 1)$

6.

$$\begin{aligned} f'(x) &> 0 && \text{over } x \in (-5, 2) \cup (8, \infty) \\ f'(x) &< 0 && \text{over } x \in (-\infty, -5) \cup (2, 8) \\ f''(x) &> 0 && \text{over } x \in (-\infty, -2) \cup (5, \infty) \\ f''(x) &< 0 && \text{over } x \in (-2, 5) \end{aligned}$$

