

### Chap 1.030 One-Sided Limits

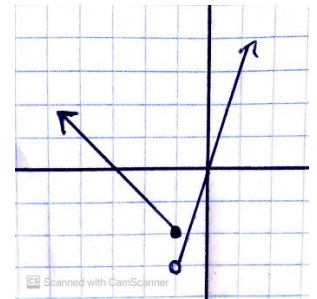
Recall this statement about limits from an earlier lesson

$$\text{If } \lim_{x \rightarrow a^-} f(x) = b \text{ and if } \lim_{x \rightarrow a^+} f(x) = b \text{ then } \lim_{x \rightarrow a} f(x) = b$$

However, if  $\lim_{x \rightarrow a^-} f(x)$  exists and if  $\lim_{x \rightarrow a^+} f(x)$  exists but  $\lim_{x \rightarrow a^-} f(x) \neq \lim_{x \rightarrow a^+} f(x)$ , then  $\lim_{x \rightarrow a} f(x)$  does not exist.

#### Example 1

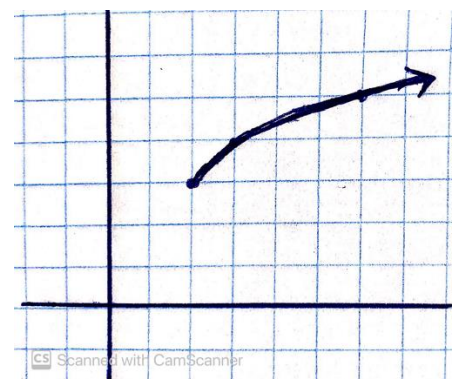
Given that  $f(x) = \begin{cases} -x - 3, & x \leq -1 \\ 3x, & x > -1 \end{cases}$ , use a graphing approach to determine  $\lim_{x \rightarrow -1} f(x)$  or justify that it does not exist.



#### Example 2

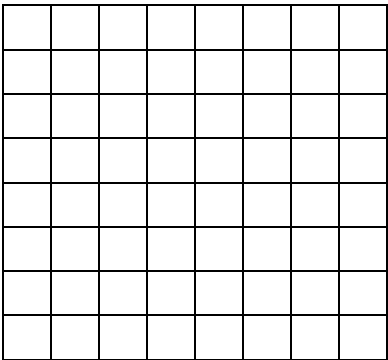
Evaluate the following using a graphing approach

$$\lim_{x \rightarrow 2} (\sqrt{x-2} + 3)$$



**Example 3**

Evaluate  $\lim_{x \rightarrow 0} |x|$



**Example 4**

Evaluate  $\lim_{x \rightarrow 4} \frac{|x-4|}{x-4}$

