LM: Square root SAM (NSAM)

* Summary of L10: Smoothing and mapping

SLAM as a Factor graph (prev. Bayes network)

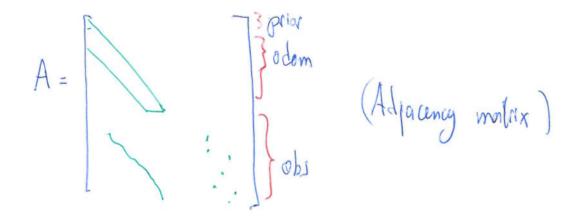
0* = org max p(X, MIE, u) = org nuln 1 Z 11.112; 5

odometry, observation and prin pertors

8* = ang min 11 AS - b112 (LLSQ)

1) 1st order Taylor

2) 11 ell= 11 Z-T2 ell=



AS=5 Iteratively volved in til concerjence,

* ATA = 1 (Information marking) we presented SAU as a MAP estimator of xor, m arg max P(X, M, Z, W) (-log) Unearization. agmin 11 AS-6112 (In fact, all the factors express a distribution as well. $||A J-b||_2^2 = (AS-b)^T (AS-b)$ = 2, 4, 41 - 1, 42 P - P, 42 + P, P = et , b = A m $= \partial^{T} \underbrace{A^{T}A}_{\Lambda} J - Z \partial^{T} A^{T}A \mu + \mu^{T} A^{T}A \mu =$ (Generalin porm of the ana f of $= (\beta - \mu)^{\mathsf{T}} \mathsf{A}^{\mathsf{T}} \mathsf{A} (\beta - \mu)$ the state. * Normal equation ATAS = ATB J= (ATA)-1 AT b inwhan O(n3)

A is sparse -> exploit by sotA linear algebra.

$$\Lambda = A^T A = L \cdot L^T = R^T R$$

(Information notice) DJ DJ

chal
$$A^{T}AS = A^{T}b$$

 $R^{T}RS = A^{T}b$

Hence, square root methods

$$\begin{bmatrix} R^{\mathsf{T}} \cdot g = A^{\mathsf{T}} b \\ R \cdot \delta = g \end{bmatrix}$$

Solved efficiently by back-rubitation

3)
$$6y_1 - 7y_2 + 3y_3 = 5$$

 $6-2 - 7.\frac{5}{7} + 3y_3 - 5 \Rightarrow y_3 = \frac{5-12-5}{3} = 4$

Cholenky Jactorization regumen to solve 2 systems by backenstitution

QR fectorization

$$Q^T A = \begin{bmatrix} R \\ O \end{bmatrix}$$

a: orthonormal matrix (square)

$$= \| \begin{bmatrix} R \\ O \end{bmatrix} S - \begin{bmatrix} d \\ e \end{bmatrix} \|_{2}^{2} = \| R J - d \|_{2}^{2} + \| e \|_{2}^{2}$$

RJ= J J Back Andstration.

No need to calculate $\Lambda = A^T A$ l for donce malitar) Compulationally equivalent & Choles Ky

Is R the same as for C'holes by?

$$\Lambda = A^{T}A = (QR)^{T}AR = R^{T}Q^{T}QR = R^{T}R$$

Cholesky with privine diagonal terms is unique.

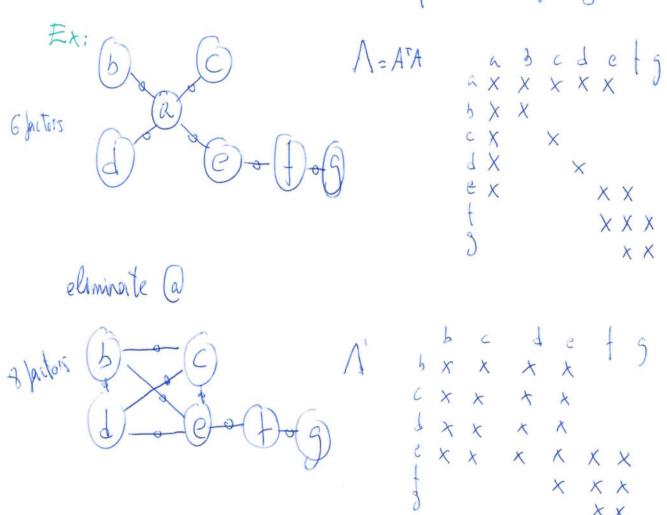
** Ordering of nodes to enhance solutions

Every graph has an aptimal ordering of modes:

- fewer edges when eliminately nodes

(equivalent to backmostitution in linear algebra)

- fewer fill-ins in the square root factorization.



New information mailix is denser than expected.

Adjacency meilix fair more (factors) rows A'8x6

while before A_{6x7}

* Minimum order degree

Intuition: The number of edges captures how connected the node is and we want to minimize that.

Permitte the nodes on a non-decreasing order (heuristic) (Solving the optimal ordering is NP-hard)

$$\frac{1}{2}$$
 $\frac{1}{2}$
 $\frac{1}$

colpum (ATA) Choluky culpum (A) BR

COLAMD heuristic for ordering noder (Danis' 2001)

As reported in Dellaert' 2006 they performed better thing thought and colomal. But it is problem dependent.