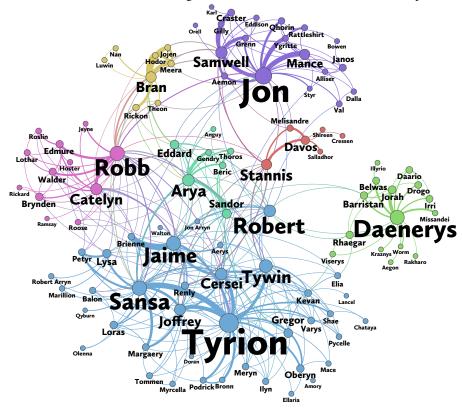


Network Visualization

In these exercises, we will analyze a weighted social network of book series *A Song of Ice and Fire*, on which the popular TV show *Game of Thrones* is based. This network was published in Math Horizons Magazine, and is based on the third book, A Storm of Swords, on which the third and fourth season of the TV series are based. More information, including the data, is available online. The network published is the following:



Exercise 1 Look through the paper to get an idea of what this network represents. What do the nodes and edges represent?

Solution: Nodes represent characters and edges the number of times they are mentioned together.

The data as published online can be loaded in R as follows (you can find the data file on the *Companion Website*:

```
Data <- read.csv("stormofswords.csv")</pre>
```

Exercise 2 Look at the data in RStudio using the "View" function. This matrix encodes a network. Can you figure out how? What do the rows stand for and what do the columns stand for? Solution: Each row indicates an edge. The first and second columns indicate the nodes an edge is connected to and the third column indicates the strength of connection.

This structure is known as an *edgelist* encoding a network, which can also be used as input for qgraph:

```
library("qgraph")
qgraph(Data, directed = FALSE)
```

Exercise 3 When plotting an undirected graph using an adjacency or weights matrix as input we normally do not have to set the directed argument. Now that we use an edgelist, however, I do. Why?

Solution: An edgelist does not know if edges are directed (one-way) or undirected, so we needed to specify that.

Now load the following dataset also available on the Companion Website:

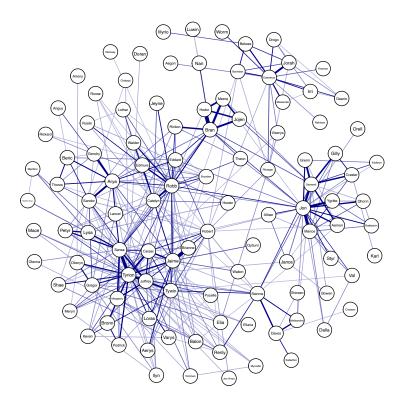
```
Data2 <- read.csv("stormofswords_wmat.csv")</pre>
```

This dataset represents the same network, but in a different way. This representation is called a *weights matrix*.

Exercise 4 Investigate the new data using View(Data2). Can you figure out how this weights matrix encodes a network. Use Data2 as input to qgraph(). Do you obtain the same network? Do you still need to use the directed argument?

Solution: When the weights matrix is symmetrical, it is automatically treated as undirected. Hence, we no longer needed the directed argument.

The plotted network is plotted using a circular layout. This circular layout, however, is hard to interpret and read in such networks with many nodes. In addition, we may prefer plotting edges with a different color than green when they represent values that can only be positive. Finally, the nodes are very large and we might want to make them smaller:



Exercise 5 Recreate the plot above, changing the layout to a spring layout, the edge color to "darkblue" and the node size to 3. Look at the qgraph help page to figure out the commands needed (?qgraph). Note: your computer might generate a different spring layout (nodes placed on different locations).

Solution: qgraph(Data, directed = FALSE, layout = "spring",posCol = "darkblue", vsize = 3).

qgraph uses three arguments that need to be known to interpret a network: minimum, cut, and maximum. These are set automatically, and can be shown using the argument details = TRUE.

Exercise 6 What values did qgraph set to cut and maximum? Note: minimum is always set to 0 by default and not shown with details = TRUE unless it differs from 0.

Solution: qgraph set cut to 14 and maximum to 96.

The minimum argument can be used to *hide* edges with an absolute (negative edges are treated as positive) weight below some value. Note that these edges are only visually hidden, not removed in further analyses (which can be done using the threshold argument). This argument is useful when plotting dense graphs (e.g., correlation networks) but *not* recommended in the networks estimated in this textbook.

Exercise 7 Set the minimum argument to 1, 10 and 20 while using a spring layout. How does the network change? Do the same using the threshold argument. Can you explain why the layout remains the same using minimum but changes using threshold?

Solution: Minimum does not remove edges, hence the layout is the same. The networks only visually differ.

Edges drawn in qgraph are drawn more wider and more saturated the stronger the absolute edge weight is. In large networks, it might be useful to split the scaling of width and color. This is what the cut argument does: edges with an absolute edge weight under the cutoff will be drawn of the smallest width and vary only in color. Edges with an absolute edge weight over the cutoff value will always be drawn fully saturated (green or red by default), and will be drawn thicker the stronger they are. You can disable this behavior by setting cut = 0, which will ensure that edges all scale in color and width. qgraph automatically sets a cutoff value when there are 20 or more nodes in the network. We recommend setting cut = 0 unless you specifically want this behavior.

Exercise 8 Set the cut argument to 50, 10 and 1 while using a spring layout. How does the network change? Now set the cut argument to 0. What happened?

Solution: The higher cut is set, the less edges are highlighted. Setting cut to 0 disabled the cutoff.

The scaling of edges is chosen based on the strongest absolute edge in the network. This is because networks highly differ in their weights. This social network is based on the number of interactions. The characters "Bran" and "Hodor" interacted the most (96 times), leading to a strongest edge weight of 96. A network based on (partial) correlations, however, can never have a stronger edge weight than 1 (and usually features weaker edges). The maximum argument can be used to overwrite the "largest edge" to which the color and width of edges scale to. Its value is treated as the weight of an invisible edge, and is automatically set to the largest edge weight in the network. Setting maximum higher will make edges scale to that value instead of the strongest edge.

Exercise 9 Set the maximum argument to 200. What happened? Now set maximum back to its default and subsequently to 10. Why doesn't maximum = 10 change the network from its default value, but maximum = 200 does?

Solution: Setting maximum below the strongest edge in the network does nothing: the edge weight width and saturation scale to is still the strongest edge weight and not the maximum score then.

Exercise 10 What would be a good setting for maximum when drawing networks based on (partial) correlations?

Solution: 1