



Public-Key Cryptography and Message Authentication

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Public-Key Cryptography Principles

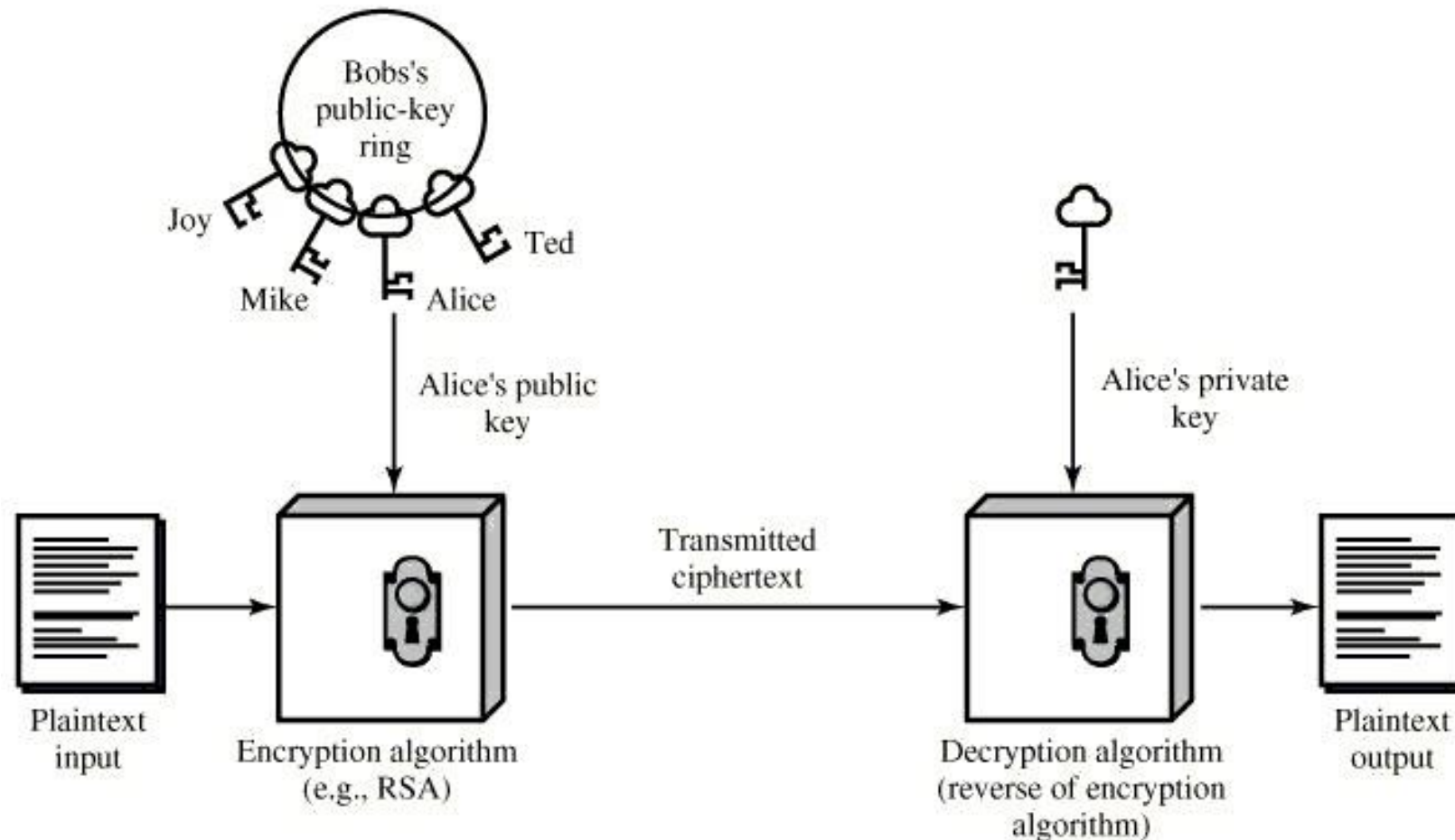
The use of two keys has consequences in: key distribution, confidentiality and authentication.

The scheme has six ingredients

Plaintext	Encryption algorithm	Public and private key	Ciphertext	Decryption algorithm
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- Public key like Bank Account Number and Private key is like a PIN

Encryption using Public-Key system



(a) Encryption

Authentication using Public-Key System

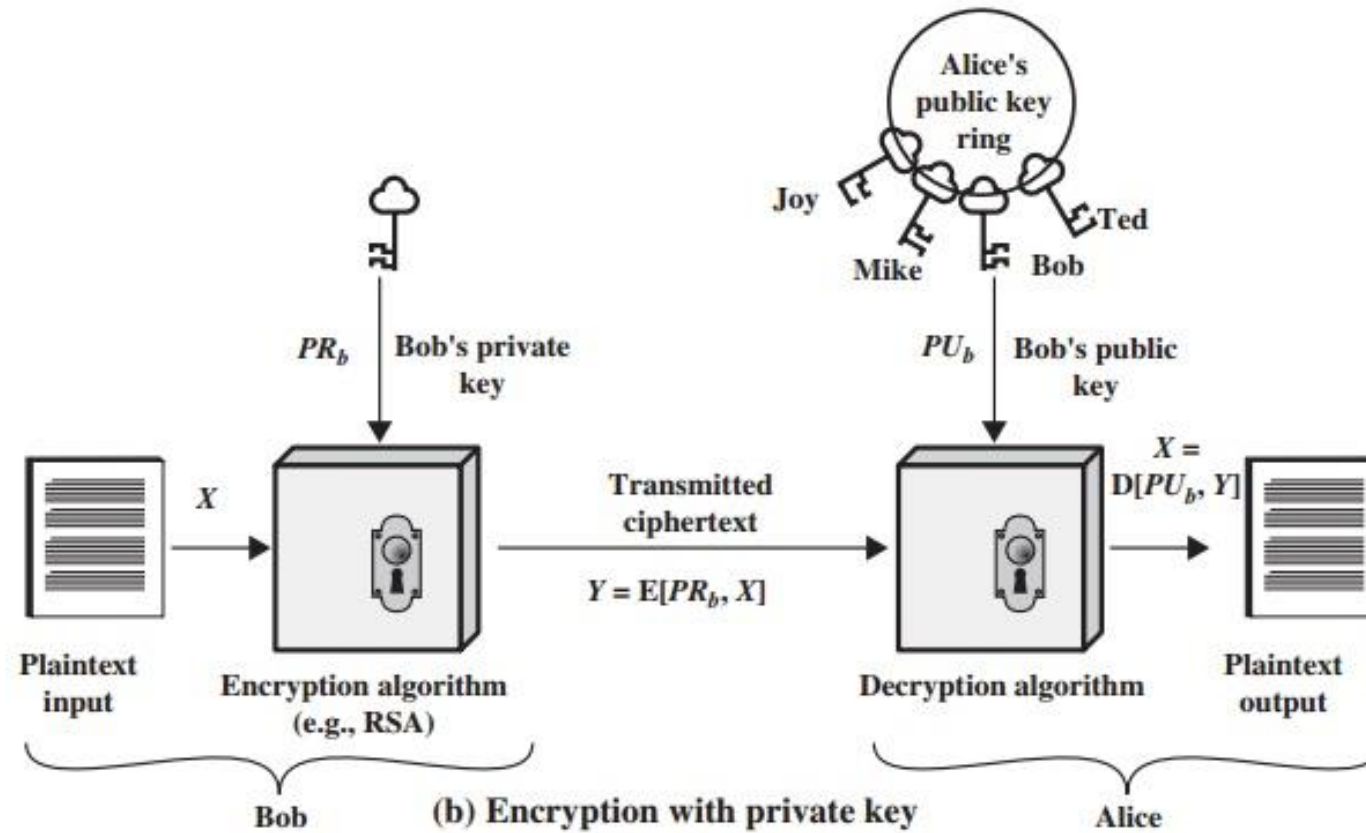
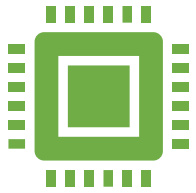
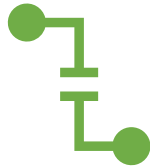


Figure 9.1 Public-Key Cryptography

Applications for Public-Key Cryptosystems



Encryption/decryption



Digital signature



Key exchange

Requirements for Public-Key Cryptography

-
- Computationally easy for a party B to generate a pair (public key K_{Ub} , private key K_{Rb})
 - Easy for sender to generate ciphertext:
 - Easy for the receiver to decrypt ciphertext using private key:

$$C = E_{K_{Ub}}(M)$$

$$M = D_{K_{Rb}}(C) = D_{K_{Rb}}[E_{K_{Ub}}(M)]$$

Public-Key Cryptographic Algorithms

RSA

- Integer factoring
- Key sharing

Diffie-Hellman

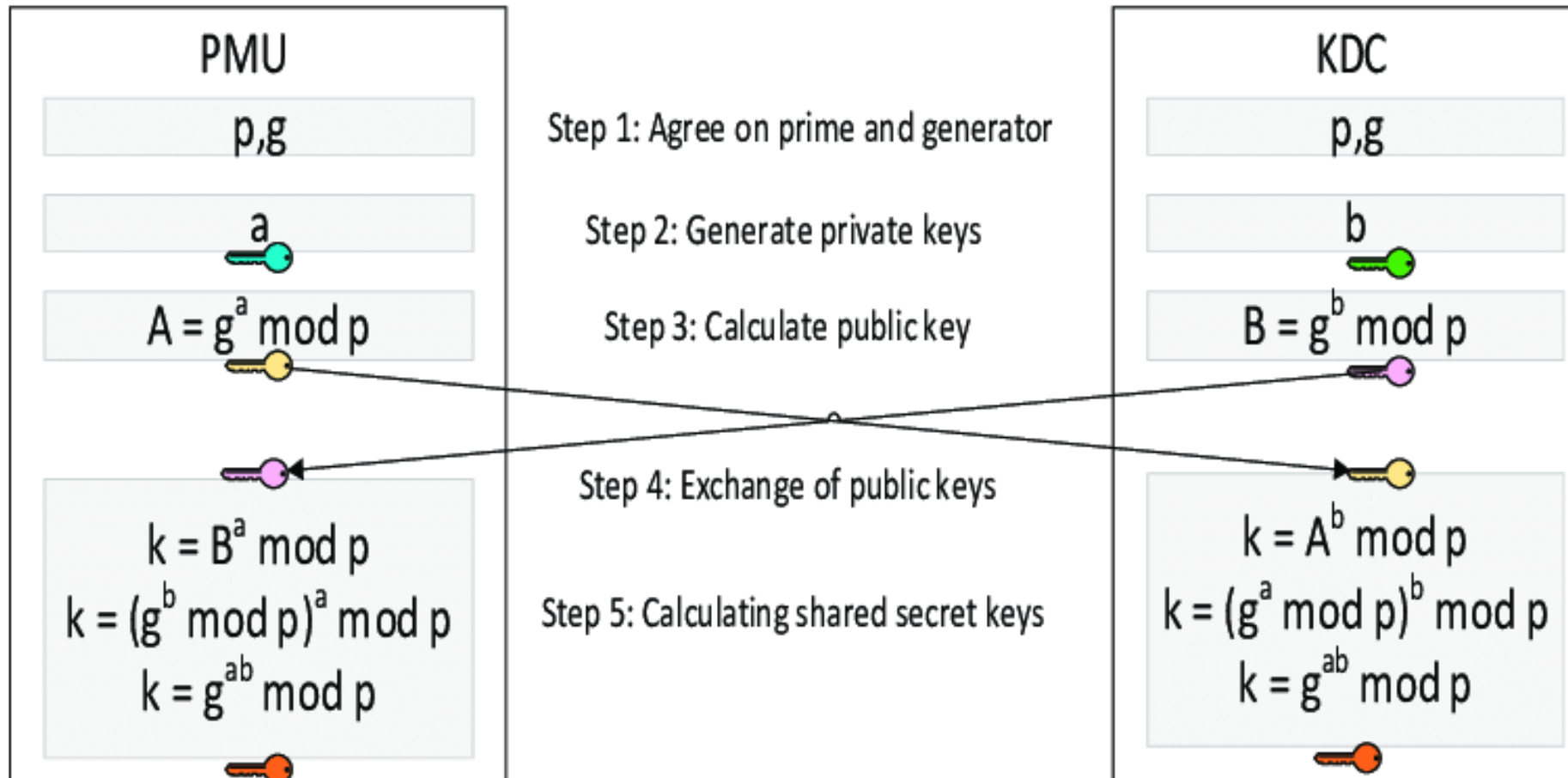
Digital Signature Standard (DSS)

- Makes use of the SHA-1
- Not for encryption or key exchange

Elliptic-Curve Cryptography (ECC)

- Good for smaller bit size
- Low confidence level, compared with RSA
- Very complex

Diffie-Hellman Key Exchange



Example

Step 1

Alice and Bob
get public
numbers

$P = 23,$
 $G = 9$

Step 2

Alice selected
a private key
 $a = 4$ and
Bob selected a
private key $b = 3$

Step 3

Alice and Bob
compute public
values

- Alice:
 $x = (9^4 \bmod 23) = (6561 \bmod 23) = 6$
- Bob:
 $y = (9^3 \bmod 23) = (729 \bmod 23) = 16$

Step 4

Alice and Bob
exchange
public numbers

Step 5

Alice receives
public key $y = 16$ and

- Bob receives
public key
 $x = 6$

Step 6

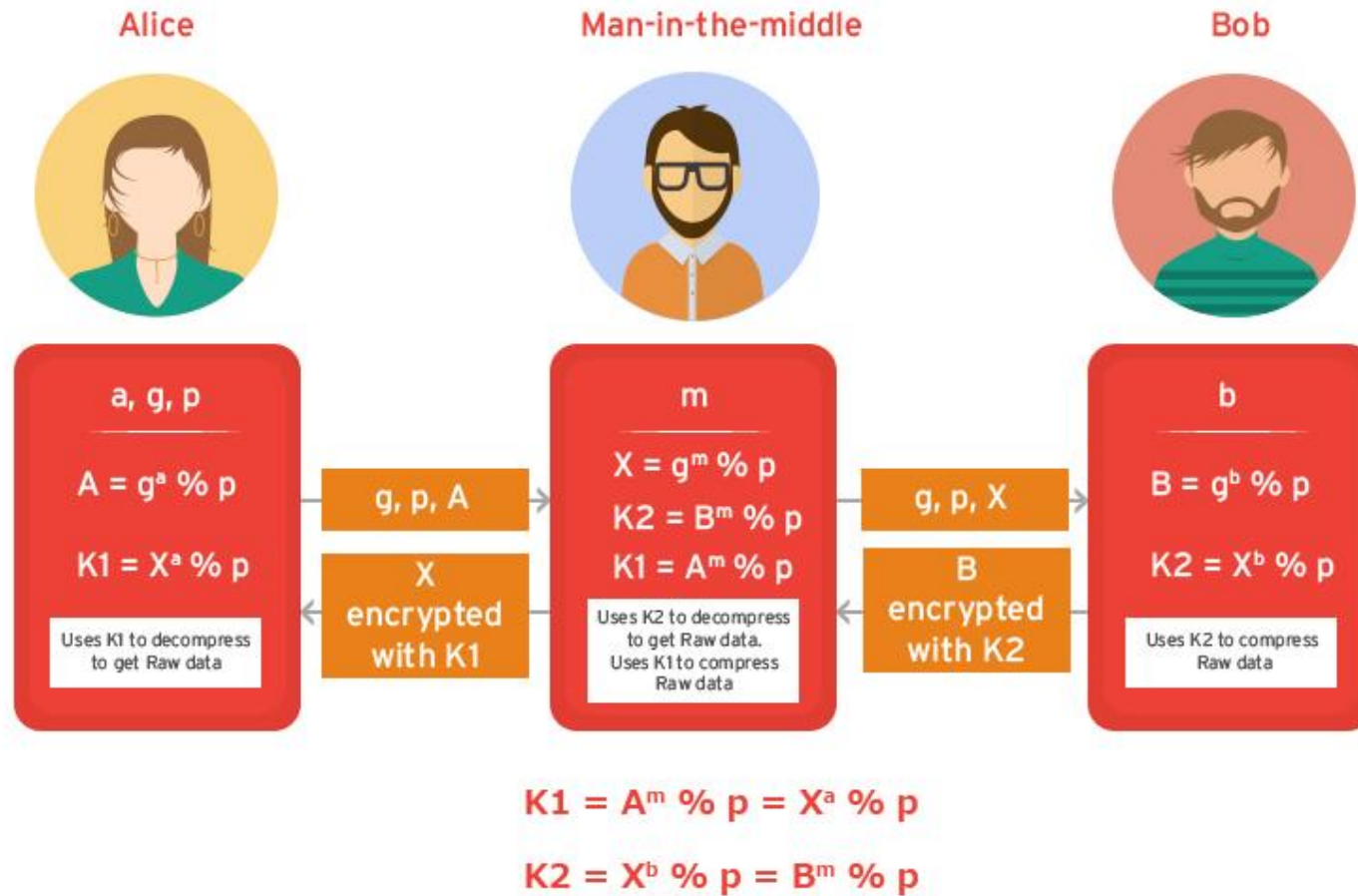
Alice and Bob
compute
symmetric keys

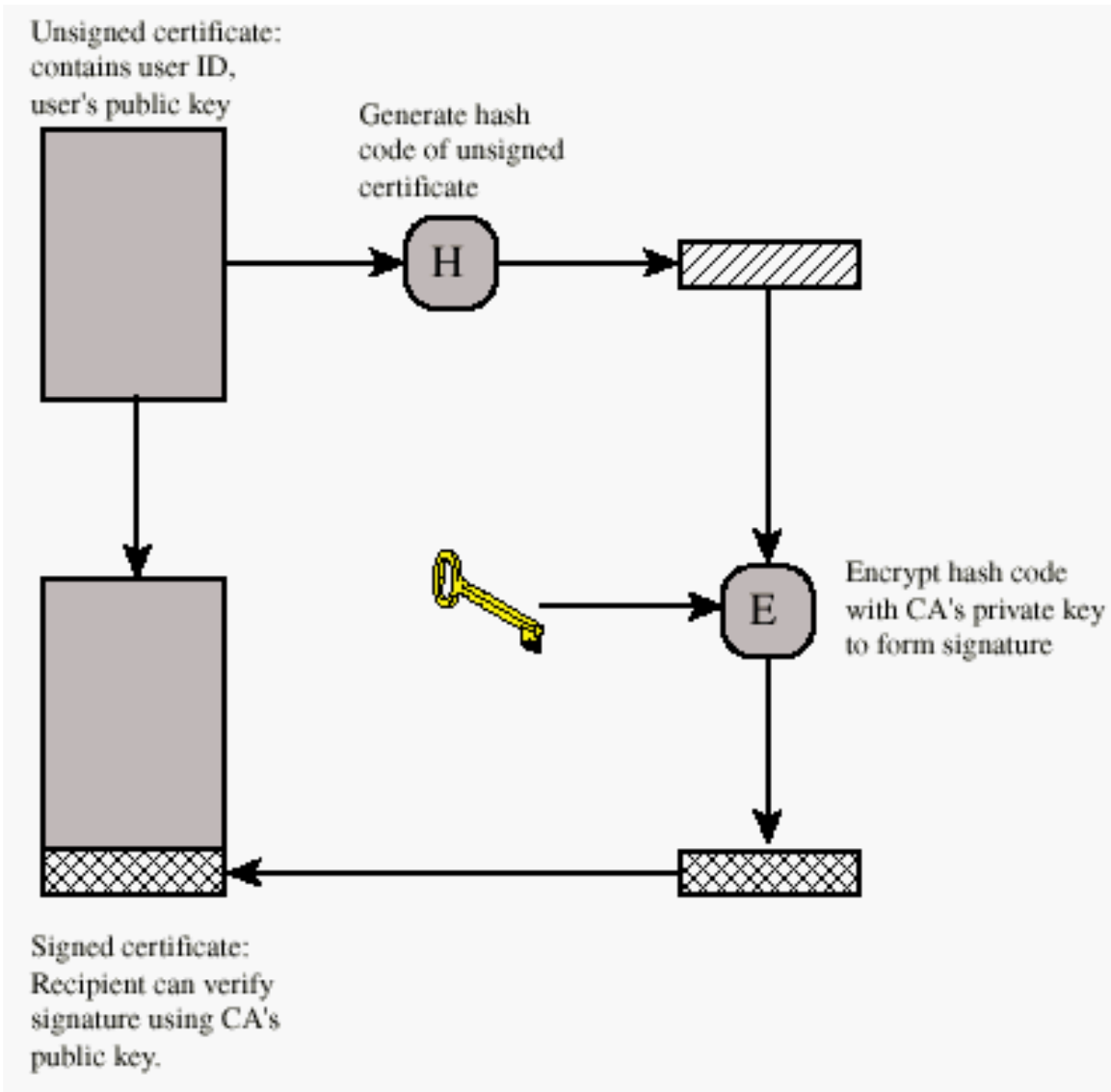
- Alice:
 $ka = y^a \bmod p$
 $= 65536 \bmod 23 = 9$
- Bob:
 $kb = x^b \bmod p$
 $= 216 \bmod 23 = 9$

Step 7

is the shared
secret.

Diffie-Hellman Key Exchange





Key Management Public-Key Certificate Use

Message Security Requirements (attacks)

- Disclosure
- Traffic analysis
- Masquerade
- Content modification
- Sequence modification
- Timing modification
- Source repudiation
- Destination repudiation

Approaches to Message Authentication

Authentication Using Conventional Encryption

- Only the sender and receiver should share a key

Message Authentication without Message Encryption

- An authentication tag is generated and appended to each message

Message Authentication Code

- Calculate the MAC as a function of the message and the key.
 $MAC = F(K, M)$

MAC Authentication

- concerned of message origin authentication, not confidentiality.
- symmetric key cryptographic technique
- sender and receiver share a symmetric key K .
- MAC is an encrypted checksum generated
- Similar to hash, fixed length output.

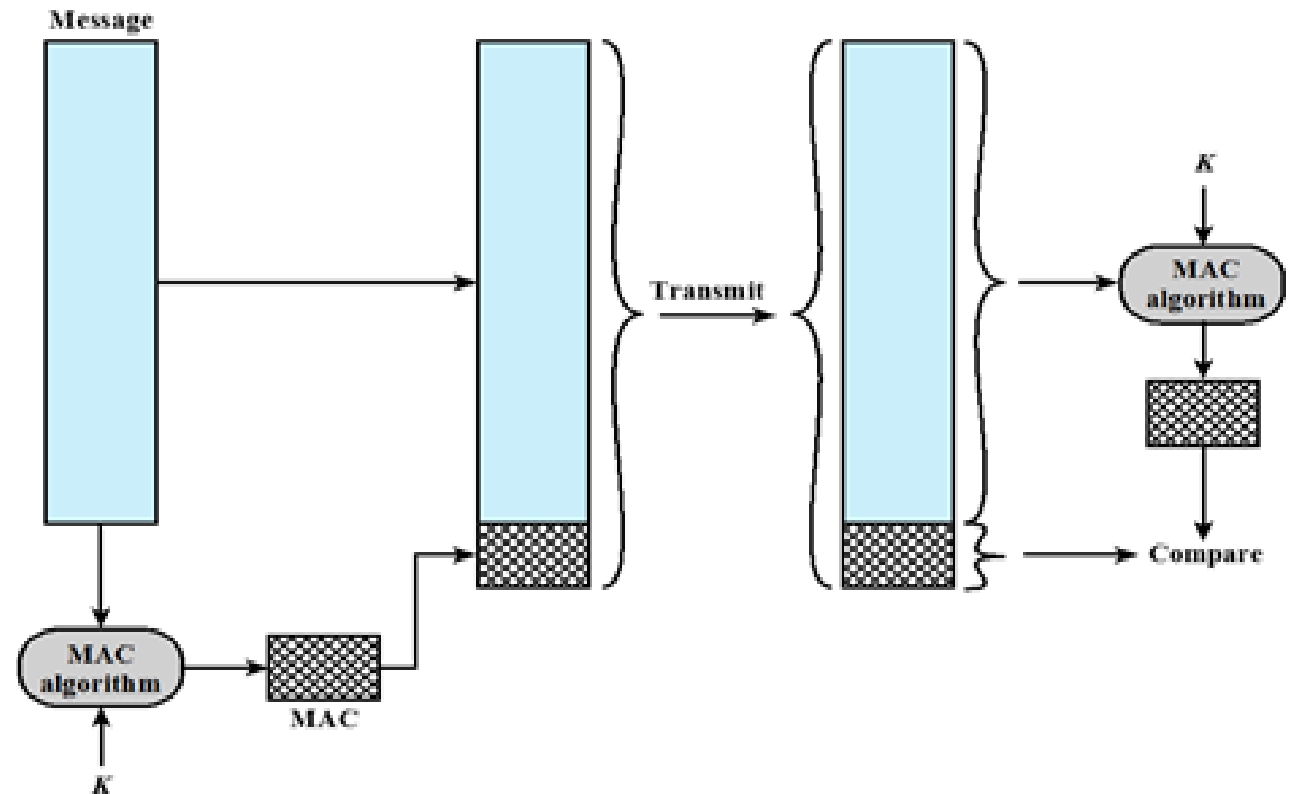


Figure 2.3 Message Authentication Using a Message Authentication Code (MAC).

References

- William Stallings, Network Security Essentials : Applications and Standards, ISBN: 9788131761755, 8131761754
- Thanks to the many unknown sources from where some information is adopted.