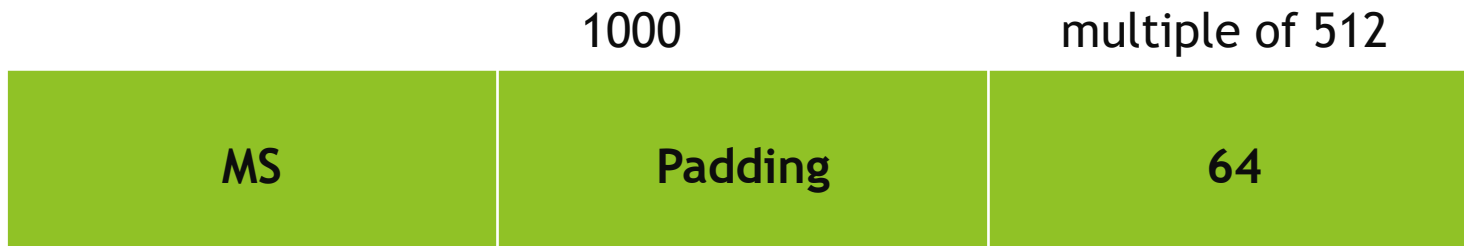


MD5

# MD5



$$P. T. = 512 - 64 = \underline{448}$$

$MS < 448 \rightarrow \text{Append } 64$

$PT \rightarrow 1024 - 64 = 960 \rightarrow \text{Append } 960$

# MD5 Cont...

$$F(B, C, D) = (B \wedge C) \vee (\neg B \wedge D)$$

$$G(B, C, D) = (B \wedge D) \vee (C \wedge \neg D)$$

$$H(B, C, D) = B \oplus C \oplus D$$

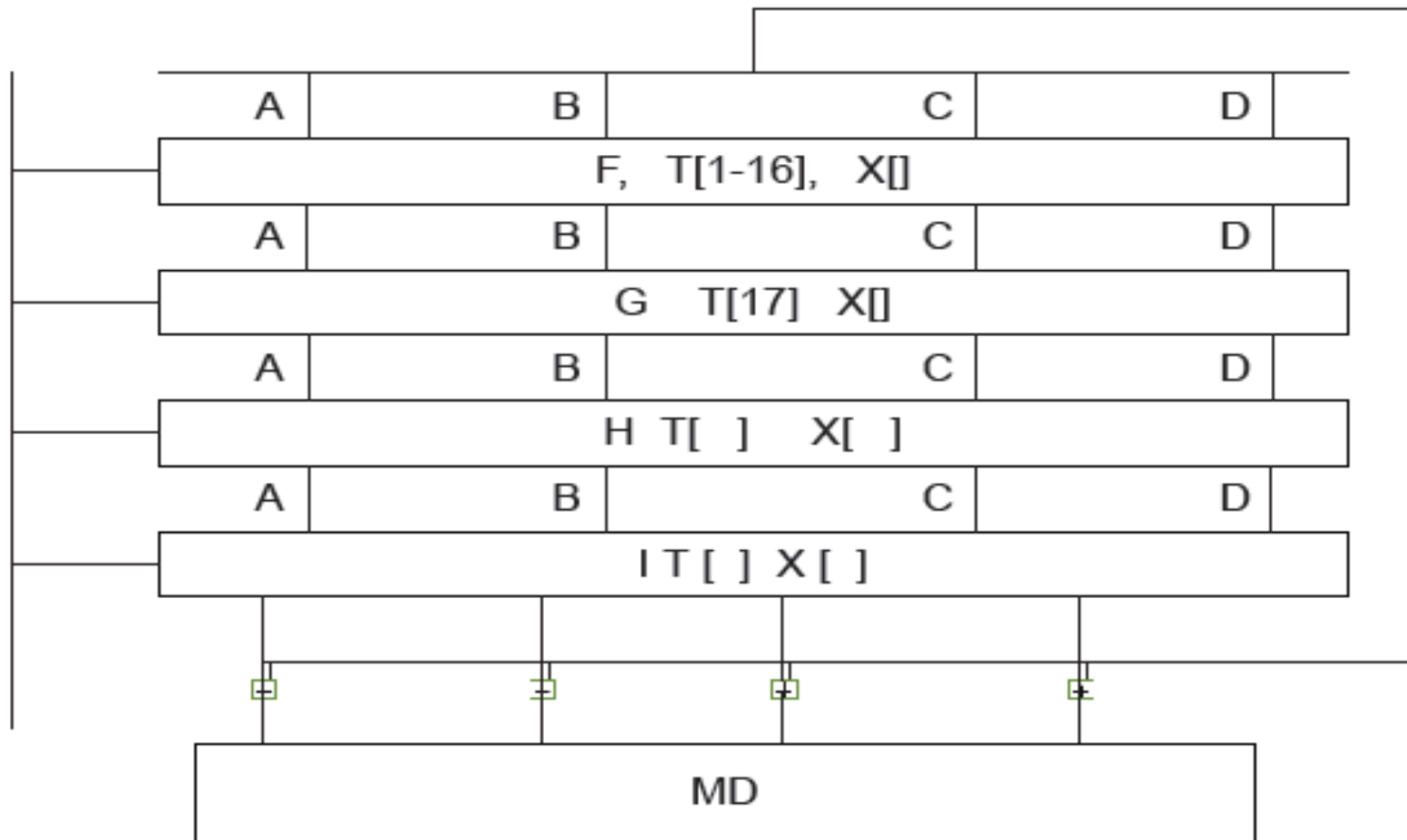
$$I(B, C, D) = C \oplus (B \vee \neg D)$$

$$A \leftarrow B \oplus ((A \oplus F_u(B, C, D) \oplus X[i] \oplus T[i]) \ll LS)$$



Circular left shift

## MD5 Cont...



## *Property 1:*

- ▶ **Collision-resistance:** The first property that we need from a cryptographic hash function is that it's collision-resistant. A collision occurs when two distinct inputs produce the same output. A hash function  $H(.)$  is collision-resistant if nobody can find a collision.
- ▶ **Collision-resistance:** A hash function  $H$  is said to be collision resistant if it is infeasible to find two values,  $x$  and  $y$ , such that  $x \neq y$ , yet  $H(x) = H(y)$ .

## Property 2:

- ▶ **Hiding** The second property that we want from our hash functions is that it's *hiding* . The hiding property asserts that if we're given the output of the hash function  $y = H(x)$  , there's no feasible way to figure out what the input,  $x$  , was.
- ▶ **Hiding.** A hash function  $H$  is hiding if: when a secret value  $r$  is chosen from a probability distribution that has *high min-entropy* , then given  $H(r \parallel x)$  it is infeasible to find  $x$  .
- ▶ In information-theory, *min-entropy* is a measure of how predictable an outcome is, and high min-entropy captures the intuitive idea that the distribution (i.e., random variable) is very spread out.

**Commitment scheme.** A commitment scheme consists of two algorithms:

- ▶ **com** := **commit**( *msg*, *nonce* ) The commit function takes a message and secret random value, called a nonce, as input and returns a commitment.
- ▶ **verify**( *com*, *msg*, *nonce* ) The verify function takes a commitment, nonce, and message as input. It returns true if  $com == \text{commit}(msg, nonce)$  and false otherwise.

We require that the following two security properties hold:

- ▶ **Hiding** : Given *com* , it is infeasible to find *msg*
- ▶ **Binding** : It is infeasible to find two pairs (*msg*, *nonce*) and (*msg'*, *nonce'*) such that  $msg \neq msg'$  and  $\text{commit}(msg, nonce) == \text{commit}(msg', nonce')$

- ▶ Take another look at the two properties that we require of our commitment schemes. If we substitute the instantiation of *commit* and *verify* as well as  $H(\text{nonce} \parallel \text{msg})$  for *com* , then these properties become:
- ▶ **Hiding** : Given  $H(\text{nonce} \parallel \text{msg})$  , it is infeasible to find *msg*
- ▶ **Binding** : It is infeasible to find two pairs  $(\text{msg}, \text{nonce})$  and  $(\text{msg}', \text{nonce}')$  such that  $\text{msg} \neq \text{msg}'$  and  $H(\text{nonce} \parallel \text{msg}) = H(\text{nonce}' \parallel \text{msg}')$



## Property 3:

**Puzzle friendliness.** The third security property we're going to need from hash functions is that they are puzzle-friendly. This property is a bit complicated. We will first explain what the technical requirements of this property are and then give an application that illustrates why this property is useful.

**Puzzle friendliness.** A hash function  $H$  is said to be puzzle-friendly if for every possible  $n$ -bit output value  $y$ , if  $k$  is chosen from a distribution with high min-entropy, then it is infeasible to find  $x$  such that  $H(k \parallel x) = y$  in time significantly less than  $2^n$ .

**Search puzzle.** A search puzzle consists of

- ▶ a hash function,  $H$ ,
- ▶ a value,  $id$  (which we call the *puzzle-ID*), chosen from a high min-entropy distribution
- ▶ and a target set  $Y$

A solution to this puzzle is a value,  $x$ , such that

$$H(id \parallel x) \in Y.$$