[intersection] 
$$\frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\langle \operatorname{intersection}(E_1 \ E_2), \sigma \rangle \rightarrow \langle \operatorname{intersection}(I_1 \ E_2), \sigma' \rangle}$$

$$[\mathsf{difference}] \ \frac{\left\langle E_1, \sigma \right\rangle \rightarrow \left\langle I_1, \sigma' \right\rangle}{\left\langle \ \mathsf{difference}(E_1 \ E_2), \sigma \right\rangle \rightarrow \left\langle \ \mathsf{difference}(I_1 \ E_2), \sigma' \right\rangle}$$

[sequenceDone]  $\langle \operatorname{seq}(\operatorname{done} C), \sigma \rangle \rightarrow \langle C, \sigma \rangle$ 

[sequence] 
$$\frac{\langle C_1, \sigma \rangle \to \langle C_1', \sigma' \rangle}{\langle \operatorname{seq}(C_1 \ C_2), \sigma \rangle \to \langle \operatorname{seq}(C_1' \ C_2), \sigma' \rangle}$$

[initialise] 
$$\langle \text{init}, \sigma \rangle \rightarrow \langle \textit{user}(\textit{string}(\text{init}) \_\_\_), \sigma \rangle$$

$$[\text{ne}] \quad \frac{n_1 \rhd \operatorname{int32}(\_) \quad n_2 \rhd \operatorname{int32}(\_)}{\left\langle \operatorname{ne}(n_1 \ n_2), \sigma \right\rangle \to \left\langle \operatorname{ne}(n_1 \ n_2), \sigma \right\rangle}$$

$$[\mathsf{neRight}] \ \frac{n \rhd \mathsf{int32}(\_) \quad \langle E_2, \sigma \rangle \to \langle I_2, \sigma' \rangle}{\langle \mathsf{ne}(n \ E_2), \sigma \rangle \to \langle \mathsf{ne}(n \ I_2), \sigma' \rangle}$$

[neLeft] 
$$\frac{\langle E_1, \sigma \rangle \to \langle I_1, \sigma' \rangle}{\langle \operatorname{ne}(E_1, E_2), \sigma \rangle \to \langle \operatorname{ne}(I_1, E_2), \sigma' \rangle}$$

$$[\mathsf{paint}] \ \big\langle \ \mathsf{paint}, \sigma \, \big\rangle \to \big\langle \ \mathit{user}(\mathit{string}(\mathsf{paint}) \ \_\_ \ \_\_), \sigma \, \big\rangle$$

[sub] 
$$\frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\langle \mathsf{sub}(n_1 \ n_2), \sigma \rangle \rightarrow \langle \mathsf{sub}(n_1 \ n_2), \sigma \rangle}$$

[subRight] 
$$\frac{n \triangleright \mathsf{int32}(\_) \quad \langle E_2, \sigma \rangle \rightarrow \langle I_2, \sigma' \rangle}{\langle \mathsf{sub}(n \ E_2), \sigma \rangle \rightarrow \langle \mathsf{sub}(n \ I_2), \sigma' \rangle}$$

$$[\mathsf{subLeft}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{sub}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{sub}(I_1 \ E_2), \sigma' \right>}$$

[clear] 
$$\langle \text{clear}, \sigma \rangle \rightarrow \langle \textit{user}(\textit{string}(\texttt{clear}) \_\_\_), \sigma \rangle$$

$$[\text{translate}] \ \frac{Z \rhd \text{int32}(\_) \quad x \rhd \text{real64}(\_) \quad y \rhd \text{real64}(\_) \quad z \rhd \text{real64}(\_)}{\left\langle \text{translate}(Z \ x \ y \ z), \sigma \right\rangle \rightarrow \left\langle \text{user}(\text{string}(\text{translate}) \ Z \ x \ y \ z), \sigma \right\rangle}$$

$$[\mathsf{translateExpr}] \ \frac{x \rhd \mathit{real64}(\_) \quad y \rhd \mathit{real64}(\_) \quad z \rhd \mathit{real64}(\_) \quad \langle E_1, \sigma \rangle \to \langle V_1, \sigma \rangle}{\langle \mathsf{translate}(E_1 \ x \ y \ z), \sigma \rangle \to \langle \mathsf{translate}(V_1 \ x \ y \ z), \sigma \rangle}$$

[ifTrue] 
$$\langle$$
 if( $\frac{bool}{C_1}$ (True)  $C_1$   $C_2$ ),  $\sigma \rangle \rightarrow \langle C_1, \sigma \rangle$ 

[ifFalse] 
$$\langle$$
 if( $\frac{bool}{False})$   $C_1$   $C_2$ ),  $\sigma \rangle \rightarrow \langle C_2, \sigma \rangle$ 

$$[\mathsf{ifResolve}] \ \frac{\left\langle \, E,\sigma \, \right\rangle \to \left\langle \, E',\sigma' \, \right\rangle}{\left\langle \, \mathsf{if}(E \ C_1 \ C_2),\sigma \, \right\rangle \to \left\langle \, \mathsf{if}(E' \ C_1 \ C_2),\sigma' \, \right\rangle}$$

[variable] 
$$\frac{\gcd(\sigma\ R)\rhd Z}{\langle \operatorname{deref}(R),\sigma\rangle \to \langle\ Z,\sigma\rangle}$$

$$[\mathsf{cube}] \ \frac{a \rhd \mathit{real64}(\_)}{\big\langle \mathsf{cube}(a), \sigma \big\rangle \to \big\langle \mathit{user}(\mathit{string}(\mathsf{cube}) \ a), \sigma \big\rangle}$$

$$[\mathsf{cylinder}] \ \frac{r \rhd \mathit{real64}(\_) \quad h \rhd \mathit{real64}(\_)}{\big\langle \mathsf{cylinder}(r \ h), \sigma \big\rangle \to \big\langle \mathit{user}(\mathit{string}(\mathsf{cylinder}) \ r \ h), \sigma \big\rangle}$$

[while] 
$$\langle \mathsf{while}(E \ C), \sigma \rangle \rightarrow \langle \mathsf{if}(E \ \mathsf{seq}(C \ \mathsf{while}(E \ C)) \ \mathsf{done}), \sigma \rangle$$

$$[\mathsf{sphere}] \ \frac{r \rhd \mathit{real64}(\_)}{\left\langle \mathsf{sphere}(r), \sigma \right\rangle \rightarrow \left\langle \mathit{user}(\mathit{string}(\mathsf{sphere}) \ r), \sigma \right\rangle}$$

$$[\mathsf{assignInt}] \ \frac{n \vartriangleright \mathsf{int32}(\_)}{\big\langle \, \mathsf{assign}(X \ n), \sigma \, \big\rangle \to \big\langle \, \mathsf{done}, \, \mathsf{put}(\sigma \ X \ n) \, \big\rangle}$$

[assignStr] 
$$\frac{s \triangleright string(\_)}{\langle assign(X \ s), \sigma \rangle \rightarrow \langle done, put(\sigma \ X \ s) \rangle}$$

[assignResolve] 
$$\frac{\langle E, \sigma \rangle \rightarrow \langle I, \sigma' \rangle}{\langle \operatorname{assign}(X \ E), \sigma \rangle \rightarrow \langle \operatorname{assign}(X \ I), \sigma' \rangle}$$

$$[\mathsf{cone}] \ \frac{r \rhd \mathit{real64}(\_) \quad h \rhd \mathit{real64}(\_)}{\langle \mathsf{cone}(r \ h), \sigma \rangle \rightarrow \langle \mathit{user}(\mathsf{string}(\mathsf{cone}) \ r \ h), \sigma \rangle}$$

$$[\mathsf{torus}] \ \frac{r \rhd \mathit{real64}(\_) \quad R \rhd \mathit{real64}(\_)}{\left\langle \mathsf{torus}(r \ R), \sigma \right\rangle \rightarrow \left\langle \mathit{user}(\mathit{string}(\mathsf{torus}) \ r \ R), \sigma \right\rangle}$$

$$[\mathsf{gt}] \quad \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\langle \mathsf{gt}(n_1 \ n_2), \sigma \rangle \rightarrow \langle \mathsf{gt}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{gtRight}] \ \frac{n \rhd \mathsf{int32}(\_) \ \left\langle E_2, \sigma \right\rangle \rightarrow \left\langle I_2, \sigma' \right\rangle}{\left\langle \, \mathsf{gt}(n \ E_2), \sigma \right\rangle \rightarrow \left\langle \, \mathsf{gt}(n \ I_2), \sigma' \right\rangle}$$

$$[\mathsf{gtLeft}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{gt}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{gt}(I_1 \ E_2), \sigma' \right>}$$

$$[\mathsf{pyramid}] \ \frac{a \rhd \mathit{real64}(\_)}{\big\langle \, \mathsf{pyramid}(a \ h), \sigma \, \big\rangle \to \big\langle \, \mathit{user}(\mathit{string}(\mathsf{pyramid}) \ a \ h), \sigma \, \big\rangle}$$

$$[\mathsf{tetrahedron}] \ \frac{a \rhd \mathit{real64}(\_)}{\big\langle \mathsf{tetrahedron}(a), \sigma \big\rangle \to \big\langle \mathit{user}(\mathsf{string}(\mathsf{tetrahedron}) \ a), \sigma \big\rangle}$$

$$[\mathrm{union}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathrm{union}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathrm{union}(I_1 \ E_2), \sigma' \right>}$$