$$|\operatorname{addInt}| \quad \frac{n_1 \bowtie \operatorname{int32}(.)}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addReal}| \quad \frac{n_1 \bowtie \operatorname{real64}(.)}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addReal}| \quad \frac{n \bowtie \operatorname{real64}(.)}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addReal}| \quad \frac{n \bowtie \operatorname{real64}(.)}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addLeft}| \quad \frac{n \bowtie \operatorname{real64}(.)}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma'} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_2, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_2, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_2, \sigma \rangle}{\operatorname{add}(n_1 n_2), \sigma} \rightarrow \operatorname{add}(n_1 n_2), \sigma} \\ |\operatorname{addLeft}| \quad \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_2, \sigma \rangle}{\operatorname{add$$

$$[\mathsf{mulLeft}] \ \frac{\left\langle E_1,\sigma\right\rangle \to \left\langle I_1,\sigma'\right\rangle}{\left\langle \,\mathsf{mul}(E_1\ E_2),\sigma\right\rangle \to \left\langle \,\mathsf{mul}(I_1\ E_2),\sigma'\right\rangle}$$

$$[\text{init}] \ \frac{w \rhd \text{int32}(\_) \quad h \rhd \text{int32}(\_)}{\langle \operatorname{init}(w \ h), \sigma \rangle \rightarrow \langle \operatorname{user}(\operatorname{string}(\operatorname{init}) \ w \ h), \sigma \rangle}$$

$$[\mathsf{paint}] \ \big\langle \, \mathsf{paint}, \sigma \, \big\rangle \to \big\langle \, \underline{\mathit{user}}(\mathit{string}(\mathsf{paint})), \sigma \, \big\rangle$$

$$[\mathsf{eqInt}] \ \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\left\langle \mathsf{eq}(n_1 \ n_2), \sigma \right\rangle \rightarrow \left\langle \mathsf{eq}(n_1 \ n_2), \sigma \right\rangle}$$

$$[\mathsf{eqReal}] \ \frac{n_1 \rhd \mathit{real64}(\_) \quad n_2 \rhd \mathit{real64}(\_)}{\langle \mathsf{eq}(n_1 \ n_2), \sigma \rangle \to \langle \mathit{eq}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{eqRightInt}] \ \frac{n \rhd \mathsf{int32}(\_) \quad \big\langle E_2, \sigma \big\rangle \to \big\langle I_2, \sigma' \big\rangle}{\big\langle \mathsf{eq}(n \ E_2), \sigma \big\rangle \to \big\langle \mathsf{eq}(n \ I_2), \sigma' \big\rangle}$$

$$[\mathsf{eqRightReal}] \ \frac{n \rhd \mathit{real64}(\_) \quad \langle E_2, \sigma \rangle \rightarrow \langle I_2, \sigma' \rangle}{\langle \mathsf{eq}(n \ E_2), \sigma \rangle \rightarrow \langle \mathsf{eq}(n \ I_2), \sigma' \rangle}$$

$$[\mathsf{eqLeft}] \ \frac{\langle E_1, \sigma \rangle \to \langle I_1, \sigma' \rangle}{\langle \mathsf{eq}(E_1 \ E_2), \sigma \rangle \to \langle \mathsf{eq}(I_1 \ E_2), \sigma' \rangle}$$

$$[\mathsf{divInt}] \ \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\langle \, \mathsf{div}(n_1 \ n_2), \sigma \, \rangle \to \langle \, \mathsf{div}(n_1 \ n_2), \sigma \, \rangle}$$

$$[\mathsf{divReal}] \ \frac{n_1 \rhd \mathit{real64}(\_) \quad n_2 \rhd \mathit{real64}(\_)}{\left\langle \mathsf{div}(n_1 \ n_2), \sigma \right\rangle \rightarrow \left\langle \mathit{div}(n_1 \ n_2), \sigma \right\rangle}$$

$$[\mathsf{divRightInt}] \ \frac{n \vartriangleright \mathsf{int32}(\_) \quad \langle E_2, \sigma \rangle \rightarrow \langle I_2, \sigma' \rangle}{\langle \, \mathsf{div}(n \ E_2), \sigma \, \rangle \rightarrow \langle \, \mathsf{div}(n \ I_2), \sigma' \rangle}$$

$$[\mathsf{divRightReal}] \ \, \frac{n \rhd \mathit{real64}(\_) \quad \big\langle E_2, \sigma \big\rangle \to \big\langle I_2, \sigma' \big\rangle}{\big\langle \operatorname{div}(n \ E_2), \sigma \big\rangle \to \big\langle \operatorname{div}(n \ I_2), \sigma' \big\rangle}$$

$$[\mathsf{divLeft}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{div}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{div}(I_1 \ E_2), \sigma' \right>}$$

$$[\mathsf{printlnSingleStr}] \ \frac{s \rhd \mathit{string}(\_)}{\left\langle \, \mathsf{println}(s), \sigma \, \right\rangle \rightarrow \left\langle \, \mathsf{seq}(\mathit{user}(\mathit{string}(\mathsf{print}) \, \, s) \, \, \mathit{user}(\mathit{string}(\mathsf{printNewLineChar}))), \sigma \, \right\rangle}$$

$$[\mathsf{printInSingleInt}] \ \frac{n \rhd \mathit{int32}(\_)}{\big\langle \, \mathsf{printIn}(n), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\mathit{user}(\mathit{string}(\mathtt{print}) \ n) \ \mathit{user}(\mathit{string}(\mathtt{printNewLineChar}))), \sigma \, \big\rangle}$$

$$[\mathsf{printInSingleReal}] \ \frac{n \rhd \mathit{real64}(\_)}{\big\langle \, \mathsf{printIn}(n), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\mathit{user}(\mathit{string}(\mathtt{print}) \ n) \ \mathit{user}(\mathit{string}(\mathtt{printNewLineChar}))), \sigma \, \big\rangle}$$

$$[\mathsf{printInSingleBool}] \ \ \frac{b \rhd \mathit{bool}(\_)}{\big\langle \, \mathsf{printIn}(b), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\mathit{\underline{user}}(\mathsf{\underline{string}}(\mathsf{print}) \ b) \ \, \mathit{\underline{user}}(\mathsf{\underline{string}}(\mathsf{printNewLineChar}))), \sigma \, \big\rangle}$$

$$[\mathsf{printlnMultiStr}] \ \frac{s \rhd \mathit{string}(\_)}{\left\langle \ \mathsf{println}(s \ E), \sigma \right\rangle \rightarrow \left\langle \mathit{seq}(\underbrace{\mathit{user}(\mathit{string}(\mathtt{print}) \ s) \ E), \sigma} \right\rangle}$$

$$[\mathsf{printlnMultiInt}] \; \frac{n \rhd \mathsf{int32}(\_)}{\big\langle \, \mathsf{println}(n \; E), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\underbrace{\mathsf{user}(\mathsf{string}(\mathsf{print}) \; n) \; E), \sigma \, \big\rangle}$$

$$[\mathsf{printlnMultiReal}] \; \frac{n \rhd \mathit{real64}(\_)}{\big\langle \; \mathsf{println}(n \; E), \sigma \, \big\rangle \to \big\langle \; \mathsf{seq}(\mathit{user}(\mathsf{string}(\mathsf{print}) \; n) \; E), \sigma \, \big\rangle}$$

$$[\mathsf{printInMultiBool}] \ \frac{b \rhd \mathit{bool}(\_)}{\big\langle \, \mathsf{printIn}(b \ E), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\mathit{user}(\mathsf{string}(\mathsf{print}) \ b) \ E), \sigma \, \big\rangle}$$

$$[\mathsf{printInResolve}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{printIn}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{printIn}(I_1 \ E_2), \sigma' \right>}$$

$$[\mathsf{printlnResolve}] \ \frac{\langle E,\sigma \rangle \to \langle I,\sigma' \rangle}{\langle \, \mathsf{println}(E),\sigma \rangle \to \langle \, \mathsf{println}(I),\sigma' \rangle}$$

$$[\mathsf{modInt}] \ \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\langle \ \mathsf{mod}(n_1 \ n_2), \sigma \rangle \to \langle \ \mathsf{mod}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{modRightInt}] \ \frac{n \rhd \mathsf{int32}(\_) \quad \big\langle E_2, \sigma \big\rangle \to \big\langle I_2, \sigma' \big\rangle}{\big\langle \operatorname{mod}(n \ E_2), \sigma \big\rangle \to \big\langle \operatorname{mod}(n \ I_2), \sigma' \big\rangle}$$

$$[\mathsf{modLeft}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{mod}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{mod}(I_1 \ E_2), \sigma' \right>}$$

$$[\mathsf{neInt}] \ \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\langle \, \mathsf{ne}(n_1 \ n_2), \sigma \, \rangle \to \langle \, \mathsf{ne}(n_1 \ n_2), \sigma \, \rangle}$$

$$[\mathsf{neReal}] \ \frac{n_1 \rhd \mathit{real64}(\_)}{\langle \mathsf{ne}(n_1 \ n_2), \sigma \rangle \to \langle \mathit{ne}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{neRightInt}] \ \, \frac{n \vartriangleright \mathsf{int32}(\_) \quad \big\langle \, E_2, \sigma \, \big\rangle \to \big\langle \, I_2, \sigma' \, \big\rangle }{\big\langle \, \mathsf{ne}(n \ E_2), \sigma \, \big\rangle \to \big\langle \, \mathsf{ne}(n \ I_2), \sigma' \, \big\rangle }$$

$$[\mathsf{neRightReal}] \ \, \frac{n \rhd \mathit{real64}(\_) \quad \big\langle \, E_2, \sigma \, \big\rangle \to \big\langle \, I_2, \sigma' \, \big\rangle }{\big\langle \, \mathsf{ne}(n \ E_2), \sigma \, \big\rangle \to \big\langle \, \mathsf{ne}(n \ I_2), \sigma' \, \big\rangle }$$

$$[\mathsf{neLeft}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{ne}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{ne}(I_1 \ E_2), \sigma' \right>}$$

$$[\mathsf{negInt}] \ \frac{n \rhd \mathsf{int32}(\_)}{\langle \mathsf{neg}(n), \sigma \rangle \to \langle \mathsf{neg}(n), \sigma \rangle}$$

$$[\mathsf{negReal}] \ \frac{n \rhd \mathit{real64}(\_)}{\langle \, \mathsf{neg}(n), \sigma \, \rangle \to \langle \, \mathit{neg}(n), \sigma \, \rangle}$$

$$[\mathsf{negResolve}] \ \frac{\left< E, \sigma \right> \rightarrow \left< I, \sigma' \right>}{\left< \mathsf{neg}(E), \sigma \right> \rightarrow \left< \mathsf{neg}(I), \sigma' \right>}$$

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[\mathsf{printlnElemStr}] \; \frac{s \rhd \mathsf{string}(\_)}{\big\langle \; \mathsf{printlnElem}(s \; E), \sigma \, \big\rangle \to \big\langle \; \mathsf{seq}(\underbrace{\mathsf{user}(\mathsf{string}(\mathsf{print}) \; \mathsf{string}(\_)) \; \mathsf{seq}(\underbrace{\mathsf{user}(\mathsf{string}(\mathsf{print}) \; s) \; E)), \sigma \, \big\rangle}
[\mathsf{printlnElemInt}] \; \frac{n \rhd \mathsf{int}32(\_)}{\big\langle \; \mathsf{printlnElem}(n \; E), \sigma \, \big\rangle \to \big\langle \; \mathsf{seq}(\underbrace{\mathsf{user}(\mathsf{string}(\mathsf{print}) \; \mathsf{string}(\ )) \; \mathsf{seq}(\underbrace{\mathsf{user}(\mathsf{string}(\mathsf{print}) \; n) \; E)), \sigma \, \big\rangle}
[\mathsf{printlnElemReal}] \ \frac{n \rhd \mathit{real64}(\_)}{\big\langle \, \mathsf{printlnElem}(n \ E), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\mathit{user}(\mathit{string}(\mathsf{print}) \ \mathit{string}(\ )) \ \mathsf{seq}(\mathit{user}(\mathit{string}(\mathsf{print}) \ n) \ E)), \sigma \, \big\rangle}
[\mathsf{printlnElemBool}] \ \frac{b \rhd \mathit{bool}(\_)}{\big\langle \, \mathsf{printlnElem}(b \ E), \sigma \, \big\rangle \to \big\langle \, \mathsf{seq}(\mathit{user}(\mathit{string}(\mathsf{print}) \ \mathit{string}(\ )) \ \mathsf{seq}(\mathit{user}(\mathit{string}(\mathsf{print}) \ b) \ E)), \sigma \, \big\rangle}
[printlnElemLast]
 \frac{s \rhd \textit{string}(\_)}{\left\langle \textit{printlnElem}(s), \sigma \right\rangle \rightarrow \left\langle \textit{seq}(\textit{seq}(\textit{user}(\textit{string}(\textit{print}) \, \textit{string}(\ )) \, \textit{user}(\textit{string}(\textit{print}) \, s)) \, \, \textit{user}(\textit{string}(\textit{printNewLineChar}))), \sigma \right\rangle}
[printlnElemLastInt]
 \frac{n \rhd \mathsf{int}32(\_)}{\big\langle \mathsf{printlnElem}(n), \sigma \big\rangle \to \big\langle \mathsf{seq}(\mathsf{seq}(\mathsf{user}(\mathsf{string}(\mathsf{print}) \ \mathsf{string}(\ )) \ \mathsf{user}(\mathsf{string}(\mathsf{print}) \ n)) \ \mathsf{user}(\mathsf{string}(\mathsf{printNewLineChar}))), \sigma \big\rangle}
 [printlnElemLastReal]
 \frac{n \rhd \mathit{real64}(\_)}{\big\langle \mathit{printlnElem}(n), \sigma \big\rangle \to \big\langle \mathit{seq}(\mathit{user}(\mathit{string}(\mathit{print}) \ \mathit{string}(\ )) \ \mathit{user}(\mathit{string}(\mathit{print}) \ n)) \ \mathit{user}(\mathit{string}(\mathit{printNewLineChar}))), \sigma \big\rangle}
 [printlnElemLastBool]
 \frac{b \rhd bool(\_)}{\left\langle \operatorname{printlnElem}(b), \sigma \right\rangle \rightarrow \left\langle \operatorname{seq}(\operatorname{ser}(\operatorname{string}(\operatorname{print}) \operatorname{string}(\ )) \operatorname{user}(\operatorname{string}(\operatorname{print}) \operatorname{b}) \right\rangle \operatorname{user}(\operatorname{string}(\operatorname{printNewLineChar})), \sigma \right\rangle}
[\mathsf{printInElemLastResolve}] \ \ \frac{\left< E, \sigma \right> \to \left< I, \sigma' \right>}{\left< \mathsf{printInElem}(E), \sigma \right> \to \left< \mathsf{printInElem}(I), \sigma' \right>}
[\mathsf{printInElemResolve}] \ \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right>}{\left< \mathsf{printInElem}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{printInElem}(I_1 \ E_2), \sigma' \right>}
[\mathsf{gtInt}] \ \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\left\langle \, \mathsf{gt}(n_1 \ n_2), \sigma \, \right\rangle \to \left\langle \, \mathsf{gt}(n_1 \ n_2), \sigma \, \right\rangle}
[\mathsf{gtReal}] \ \frac{n_1 \rhd \mathit{real64}(\_)}{\left\langle \mathsf{gt}(n_1 \ n_2), \sigma \right\rangle \rightarrow \left\langle \mathit{gt}(n_1 \ n_2), \sigma \right\rangle}
[gtRightInt] \frac{n > int32(\_) \quad \langle E_2, \sigma \rangle \rightarrow \langle I_2, \sigma' \rangle}{\langle \operatorname{gt}(n \ E_2), \sigma \rangle \rightarrow \langle \operatorname{gt}(n \ I_2), \sigma' \rangle}
[\mathsf{gtRightReal}] \ \frac{n \rhd \mathit{real64}(\_) \ \langle E_2, \sigma \rangle \to \langle I_2, \sigma' \rangle}{\langle \mathsf{gt}(n \ E_2), \sigma \rangle \to \langle \mathsf{gt}(n \ I_2), \sigma' \rangle}
[gtLeft] \frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\langle \operatorname{gt}(E_1 \ E_2), \sigma \rangle \rightarrow \langle \operatorname{gt}(I_1 \ E_2), \sigma' \rangle}
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[expInt] 
$$\frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\left\langle \exp(n_1 \ n_2), \sigma \right\rangle \rightarrow \left\langle \exp(n_1 \ n_2), \sigma \right\rangle}$$

[expReal] 
$$\frac{n_1 \rhd real64(\_) \quad n_2 \rhd real64(\_)}{\langle \exp(n_1 \ n_2), \sigma \rangle \rightarrow \langle \exp(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{powResolve}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right> \ \left< E_2, \sigma \right> \rightarrow \left< I_2, \sigma' \right>}{\left< \exp(E_1 \ E_2), \sigma \right> \rightarrow \left< \exp(I_1 \ I_2), \sigma' \right>}$$

$$[\mathsf{int2real}] \ \frac{n \rhd \mathsf{int32}(\_)}{\big\langle \, \mathsf{int2real}(n), \sigma \, \big\rangle \to \big\langle \, \mathit{user}(\mathsf{string}(\mathsf{int2real}) \, \, n), \sigma \, \big\rangle}$$

$$[\mathsf{int2realResolve}] \ \frac{\langle E, \sigma \rangle \to \langle I, \sigma' \rangle}{\langle \mathsf{int2real}(E), \sigma \rangle \to \langle \mathit{user}(\mathsf{string}(\mathsf{int2real}) \ I), \sigma' \rangle}$$

$$[\mathsf{geInt}] \ \frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\left\langle \mathsf{ge}(n_1 \ n_2), \sigma \right\rangle \to \left\langle \mathsf{ge}(n_1 \ n_2), \sigma \right\rangle}$$

$$[\mathsf{geReal}] \ \frac{n_1 \rhd \mathit{real64}(\_)}{\langle \mathsf{ge}(n_1 \ n_2), \sigma \rangle \to \langle \mathit{ge}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{geRightInt}] \ \frac{n \rhd \mathsf{int32}(\_) \quad \big\langle E_2, \sigma \big\rangle \to \big\langle I_2, \sigma' \big\rangle}{\big\langle \mathsf{ge}(n \ E_2), \sigma \big\rangle \to \big\langle \mathsf{ge}(n \ I_2), \sigma' \big\rangle}$$

[geRightReal] 
$$\frac{n \rhd real64(\_) \quad \langle E_2, \sigma \rangle \rightarrow \langle I_2, \sigma' \rangle}{\langle \operatorname{ge}(n E_2), \sigma \rangle \rightarrow \langle \operatorname{ge}(n I_2), \sigma' \rangle}$$

$$[\mathsf{geLeft}] \ \frac{\langle E_1, \sigma \rangle \to \langle I_1, \sigma' \rangle}{\langle \mathsf{ge}(E_1 \ E_2), \sigma \rangle \to \langle \mathsf{ge}(I_1 \ E_2), \sigma' \rangle}$$

$$[\mathsf{real2int}] \ \frac{n \rhd \mathit{real64}(\_)}{\big\langle \, \mathsf{real2int}(n), \sigma \, \big\rangle \to \big\langle \, \mathit{user}(\mathit{string}(\mathtt{real2int}) \, \, n), \sigma \, \big\rangle}$$

$$[\mathsf{real2intResolve}] \ \frac{\left< E, \sigma \right> \rightarrow \left< I, \sigma' \right>}{\left< \mathsf{real2int}(E), \sigma \right> \rightarrow \left< \textit{user}(\textit{string}(\texttt{real2int}) \ I), \sigma' \right>}$$

$$[\mathsf{sequenceDone}] \ \big\langle \ \mathsf{seq}( \ \ \ \ \ \ \ \ \ \ \ ) \ \ \rightarrow \ \big\langle \ \ \ \ \ \ \ \ \big\rangle$$

$$[\mathsf{sequence}] \ \frac{\left< \ C_1, \sigma \right> \rightarrow \left< \ C_1', \sigma' \right>}{\left< \ \mathsf{seq}(\ C_1 \ \ C_2), \sigma \right> \rightarrow \left< \ \mathsf{seq}(\ C_1' \ \ C_2), \sigma' \right>}$$

$$[\mathsf{box}] \ \frac{x \rhd \mathit{real64}(\_) \quad y \rhd \mathit{real64}(\_) \quad z \rhd \mathit{real64}(\_)}{\left\langle \mathsf{box}(x \ y \ z), \sigma \right\rangle \rightarrow \left\langle \mathit{user}(\mathit{string}(\mathsf{box}) \ x \ y \ z), \sigma \right\rangle}$$

$$[\mathsf{break}] \ \langle \, \mathsf{break}, \sigma \, \rangle \to \langle \, \mathit{done}, \sigma \, \rangle$$

[ltInt] 
$$\frac{n_1 \rhd int32(\_)}{\langle \operatorname{lt}(n_1 \ n_2), \sigma \rangle \to \langle \operatorname{lt}(n_1 \ n_2), \sigma \rangle}$$

[ItReal] 
$$\frac{n_1 \rhd real64(\_) \quad n_2 \rhd real64(\_)}{\langle \operatorname{It}(n_1 \ n_2), \sigma \rangle \to \langle \operatorname{It}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{ltRightInt}] \ \frac{n \rhd \mathsf{int32}(\_) \ \left\langle E_2, \sigma \right\rangle \to \left\langle I_2, \sigma' \right\rangle}{\left\langle \mathsf{lt}(n \ E_2), \sigma \right\rangle \to \left\langle \mathsf{lt}(n \ I_2), \sigma' \right\rangle}$$

$$[\mathsf{ltRightReal}] \ \frac{n \rhd \mathit{real64}(\_) \ \ \big\langle E_2, \sigma \big\rangle \to \big\langle I_2, \sigma' \big\rangle}{\big\langle \, \mathsf{lt}(n \ E_2), \sigma \big\rangle \to \big\langle \, \mathsf{lt}(n \ I_2), \sigma' \big\rangle}$$

$$[\mathsf{ltLeft}] \ \frac{\left\langle E_1, \sigma \right\rangle \to \left\langle I_1, \sigma' \right\rangle}{\left\langle \, \mathsf{lt}(E_1 \ E_2), \sigma \right\rangle \to \left\langle \, \mathsf{lt}(I_1 \ E_2), \sigma' \right\rangle}$$

$$[\mathsf{cube}] \ \frac{e \rhd \mathit{real64}(\_)}{\left< \mathsf{cube}(e), \sigma \right> \rightarrow \left< \mathit{user}(\mathit{string}(\mathsf{cube}) \ e), \sigma \right>}$$

$$[\mathsf{cubeResolve}] \ \frac{\langle E, \sigma \rangle \to \langle I, \sigma' \rangle}{\langle \mathsf{cube}(E), \sigma \rangle \to \langle \mathsf{cube}(I), \sigma' \rangle}$$

[ifTrue] 
$$\langle$$
 if( $bool(True) \ C_1 \ C_2), \sigma \rangle \rightarrow \langle \ C_1, \sigma \rangle$ 

[ifTrue] 
$$\langle$$
 if( $\frac{bool}{C}$ , $\sigma \rangle \rightarrow \langle C, \sigma \rangle$ 

[ifFalse] 
$$\langle$$
 if( $\frac{bool}{False}$ )  $C_1$   $C_2$ ),  $\sigma \rangle \rightarrow \langle C_2, \sigma \rangle$ 

[ifFalse] 
$$\langle$$
 if( $bool(False) C), \sigma \rangle \rightarrow \langle done, \sigma \rangle$ 

$$[\mathsf{ifResolve}] \ \frac{\langle E, \sigma \rangle \to \langle E', \sigma' \rangle}{\langle \mathsf{if}(E \ C_1 \ C_2), \sigma \rangle \to \langle \mathsf{if}(E' \ C_1 \ C_2), \sigma' \rangle}$$

$$[\mathsf{ifResolve}] \ \frac{\langle E, \sigma \rangle \to \langle E', \sigma' \rangle}{\langle \mathsf{if}(E \ C), \sigma \rangle \to \langle \mathsf{if}(E' \ C \ \mathit{done}), \sigma' \rangle}$$

[leInt] 
$$\frac{n_1 \rhd \mathsf{int32}(\_)}{\langle \mathsf{le}(n_1 \ n_2), \sigma \rangle \to \langle \mathsf{le}(n_1 \ n_2), \sigma \rangle}$$

[leReal] 
$$\frac{n_1 \rhd real64(\_) \quad n_2 \rhd real64(\_)}{\langle \operatorname{le}(n_1 \ n_2), \sigma \rangle \rightarrow \langle \operatorname{le}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{leRightInt}] \ \, \frac{n \rhd \mathit{int32}(\_) \ \, \left\langle \, E_2, \sigma \, \right\rangle \to \left\langle \, I_2, \sigma' \, \right\rangle }{\left\langle \, \mathsf{le}(n \ E_2), \sigma \, \right\rangle \to \left\langle \, \mathsf{le}(n \ I_2), \sigma' \, \right\rangle }$$

$$[\mathsf{leRightReal}] \ \, \frac{n \rhd \textit{real64}(\_) \ \ \langle \textit{E}_2, \sigma \, \rangle \rightarrow \langle \textit{I}_2, \sigma' \, \rangle}{\langle \, \mathsf{le}(\textit{n} \; \textit{E}_2), \sigma \, \rangle \rightarrow \langle \, \mathsf{le}(\textit{n} \; \textit{I}_2), \sigma' \, \rangle}$$

$$[\mathsf{leLeft}] \ \frac{\left\langle E_1, \sigma \right\rangle \rightarrow \left\langle I_1, \sigma' \right\rangle}{\left\langle \left| \mathsf{le}(E_1 \ E_2), \sigma \right\rangle \rightarrow \left\langle \left| \mathsf{le}(I_1 \ E_2), \sigma' \right\rangle \right.}$$

$$[\mathsf{sphere}] \ \frac{r \rhd \mathit{real64}(\_)}{\big\langle \mathsf{sphere}(r), \sigma \big\rangle \to \big\langle \mathit{user}(\mathit{string}(\mathsf{sphere}) \ r), \sigma \big\rangle}$$

$$[\text{cylinder}] \ \frac{r \rhd \textit{real64}(\_) \quad h \rhd \textit{real64}(\_)}{\left\langle \text{cylinder}(r \ h), \sigma \right\rangle \rightarrow \left\langle \textit{user}(\textit{string}(\text{cylinder}) \ r \ h), \sigma \right\rangle}$$

[while] 
$$\langle \mathsf{while}(E \ C), \sigma \rangle \rightarrow \langle \mathsf{if}(E \ \mathsf{seq}(C \ \mathsf{while}(E \ C)) \ \mathsf{done}), \sigma \rangle$$

$$[\mathsf{not}] \ \frac{n \rhd \mathit{bool}(\_)}{\langle \, \mathsf{not}(n), \sigma \, \rangle \to \langle \, \mathit{not}(n), \sigma \, \rangle}$$

$$[\mathsf{notResolve}] \ \frac{\langle E, \sigma \rangle \to \langle I, \sigma' \rangle}{\langle \mathsf{not}(E), \sigma \rangle \to \langle \mathsf{not}(I), \sigma' \rangle}$$

$$[\mathsf{for}] \quad \langle \, \mathsf{for}(E_1 \ E_2 \ E_3 \ C), \sigma \, \rangle \rightarrow \langle \, \mathsf{seq}(E_1 \ \mathsf{while}(E_2 \ \mathsf{seq}(C \ E_3))), \sigma \, \rangle$$

$$[\mathsf{cone}] \ \frac{r \rhd \mathit{real64}(\_) \quad h \rhd \mathit{real64}(\_)}{\left\langle \mathsf{cone}(r \ h), \sigma \right\rangle \rightarrow \left\langle \mathit{user}(\mathit{string}(\mathsf{cone}) \ r \ h), \sigma \right\rangle}$$

[and] 
$$\frac{n_1 \rhd bool(\_)}{\langle \operatorname{and}(n_1 \ n_2), \sigma \rangle \to \langle \operatorname{and}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{andResolve}] \ \frac{\langle \, E_1,\sigma \, \rangle \to \langle \, I_1,\sigma' \, \rangle \quad \langle \, E_2,\sigma \, \rangle \to \langle \, I_2,\sigma' \, \rangle}{\langle \, \mathsf{and}(E_1 \ E_2),\sigma \, \rangle \to \langle \, \mathsf{and}(I_1 \ I_2),\sigma' \, \rangle}$$

$$[\mathsf{torus}] \ \frac{r \rhd \mathit{real64}(\_)}{\big\langle \mathsf{torus}(r \ R), \sigma \big\rangle \to \big\langle \mathit{user}(\mathit{string}(\mathsf{torus}) \ r \ R), \sigma \big\rangle}$$

$$[or] \quad \frac{n_1 \rhd bool(\_)}{\langle or(n_1 \ n_2), \sigma \rangle \rightarrow \langle or(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{orResolve}] \ \frac{\left< E_1, \sigma \right> \rightarrow \left< I_1, \sigma' \right> \ \left< E_2, \sigma \right> \rightarrow \left< I_2, \sigma' \right>}{\left< \mathsf{or}(E_1 \ E_2), \sigma \right> \rightarrow \left< \mathsf{or}(I_1 \ I_2), \sigma' \right>}$$

$$[\mathsf{tetrahedron}] \ \frac{e \rhd \mathit{real64}(\_)}{\big\langle \mathsf{tetrahedron}(e), \sigma \big\rangle \to \big\langle \mathit{user}(\mathsf{string}(\mathsf{tetrahedron})\ e), \sigma \big\rangle }$$

$$[\mathsf{xor}] \ \frac{n_1 \rhd \mathsf{bool}(\_) \quad n_2 \rhd \mathsf{bool}(\_)}{\left\langle \mathsf{xor}(n_1 \ n_2), \sigma \right\rangle \to \left\langle \mathsf{xor}(n_1 \ n_2), \sigma \right\rangle}$$

$$[\text{xorResolve}] \ \frac{\left< \, E_1, \sigma \, \right> \rightarrow \left< \, I_1, \sigma' \, \right> \ \left< \, E_2, \sigma \, \right> \rightarrow \left< \, I_2, \sigma' \, \right> }{\left< \, \text{xor}(E_1 \ E_2), \sigma \, \right> \rightarrow \left< \, \text{xor}(I_1 \ I_2), \sigma' \, \right>}$$

[pyramid] 
$$\frac{e \rhd real64(\_) \quad h \rhd real64(\_)}{\left\langle \operatorname{pyramid}(e \ h), \sigma \right\rangle \rightarrow \left\langle \operatorname{user}(\operatorname{string}(\operatorname{pyramid}) \ e \ h), \sigma \right\rangle}$$

[assignInt] 
$$\frac{n \rhd \mathsf{int32}(\_)}{\left\langle \mathsf{assign}(X \ n), \sigma \right\rangle \to \left\langle \mathsf{done}, \mathsf{put}(\sigma \ X \ n) \right\rangle}$$

[assignReal] 
$$\frac{n \triangleright real64(\_)}{\langle \operatorname{assign}(X \ n), \sigma \rangle \rightarrow \langle \operatorname{done}, \operatorname{put}(\sigma \ X \ n) \rangle}$$

$$[\mathsf{assignStr}] \ \frac{s \rhd \mathit{string}(\_)}{\left\langle \mathsf{assign}(X\ s), \sigma \right\rangle \rightarrow \left\langle \mathit{done}, \mathit{put}(\sigma\ X\ s) \right\rangle}$$

[assignBool] 
$$\frac{b \rhd bool(\_)}{\langle \operatorname{assign}(X \ b), \sigma \rangle \to \langle \operatorname{done}, \operatorname{put}(\sigma \ X \ b) \rangle}$$

$$[\mathsf{assignResolve}] \ \frac{\langle E, \sigma \rangle \to \langle I, \sigma' \rangle}{\langle \mathsf{assign}(X \ E), \sigma \rangle \to \langle \mathsf{assign}(X \ I), \sigma' \rangle}$$

[subInt] 
$$\frac{n_1 \rhd \mathsf{int32}(\_) \quad n_2 \rhd \mathsf{int32}(\_)}{\left\langle \mathsf{sub}(n_1 \ n_2), \sigma \right\rangle \rightarrow \left\langle \mathsf{sub}(n_1 \ n_2), \sigma \right\rangle}$$

[subReal] 
$$\frac{n_1 \rhd real64(\_) \quad n_2 \rhd real64(\_)}{\langle \operatorname{sub}(n_1 \ n_2), \sigma \rangle \to \langle \operatorname{sub}(n_1 \ n_2), \sigma \rangle}$$

$$[\mathsf{subRightInt}] \ \frac{n \rhd \mathsf{int32}(\_) \ \ \big\langle \ E_2, \sigma \ \big\rangle \to \big\langle \ I_2, \sigma' \ \big\rangle}{\big\langle \ \mathsf{sub}(n \ E_2), \sigma \ \big\rangle \to \big\langle \ \mathsf{sub}(n \ I_2), \sigma' \big\rangle}$$

[subRightReal] 
$$\frac{n \rhd real64(\_) \quad \langle E_2, \sigma \rangle \rightarrow \langle I_2, \sigma' \rangle}{\langle \operatorname{sub}(n \ E_2), \sigma \rangle \rightarrow \langle \operatorname{sub}(n \ I_2), \sigma' \rangle}$$

[subLeft] 
$$\frac{\langle E_1, \sigma \rangle \rightarrow \langle I_1, \sigma' \rangle}{\langle \mathsf{sub}(E_1 \ E_2), \sigma \rangle \rightarrow \langle \mathsf{sub}(I_1 \ E_2), \sigma' \rangle}$$

$$[\text{translate}] \ \frac{Z \rhd \text{int32}(\_) \quad x \rhd \text{real64}(\_) \quad y \rhd \text{real64}(\_) \quad z \rhd \text{real64}(\_)}{\left\langle \text{translate}(Z \ x \ y \ z), \sigma \right\rangle \rightarrow \left\langle \text{user}(\text{string}(\text{translate}) \ Z \ x \ y \ z), \sigma \right\rangle}$$

$$[\text{translateResolve}] \ \frac{\left< \, E_1, \sigma \, \right> \to \left< \, V_1, \sigma \, \right> \ \left< \, E_2, \sigma \, \right> \to \left< \, V_2, \sigma \, \right> \ \left< \, E_3, \sigma \, \right> \to \left< \, V_3, \sigma \, \right> \ \left< \, E_4, \sigma \, \right> \to \left< \, V_4, \sigma \, \right> }{\left< \, \text{translate}(E_1 \ E_2 \ E_3 \ E_4), \sigma \, \right> \to \left< \, \text{translate}(V_1 \ V_2 \ V_3 \ V_4), \sigma \, \right> }$$