# **Optimization Bio Computation**

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#### 1 INTRODUCTION

As mentioned in the title, I chose Optimization as my further work to carry on from worksheet 3 which indicates the implementation of Genetic Algorithm using maximization function such as Counting One's function and two minimization functions as below:

$$f(x) = 10n + \sum_{i=1}^{n} x_i^2 - 10.\cos(2\pi x_i)$$
 Where -5.12 \le x\_i \le 5.12, and use n=10, 20

Figure 1.0 Rastrigin minimization function

$$f(x) = -20 \exp\left(-0.2 \sqrt{\frac{1}{D} \sum_{i=1}^{D} x^2}\right) - \exp\left(\frac{1}{D} \sum_{i=1}^{D} \cos 2\pi x_i\right)$$

Figure 1.1 Ackley minimization function

By working on the optimization, my approach is to develop some new operators to compare with the initial algorithm, and from that, I can notice which operator works better in terms of competitive performance. In my code, the initial selection method required in the worksheet is called Tournament selection and compare against that selection method is the Roulette Wheel selection that I have created. I have also executed my code over 10 runs to record the average fitness and plotted images which will be shown in the Experimentation section. Additionally, I have altered the Crossover process to make it work since the Crossover method in the worksheet resulting wrong answers to me.

Besides, I will also research the differences between Tournament selection and Roulette Wheel selection and what changes in the algorithm implementation are going to apply to maximization and minimization functions and also identify examples where using AI for a task that has raised ethical issues and state them, and all of that will be enclosed in the background research section. After this assignment, I expect to advance and expand my knowledge as well as my understanding of how Genetic Algorithms work and also the performance of the process inside GAs including Selection, Crossover and Mutation.

### 2 BACKGROUND RESEARCH

### 2.1 Introduction to Genetic Algorithms

Genetic algorithms are a type of optimization algorithm, meaning they are used to find the maximum or minimum of a function (Jenna Carr, 2014). According to this assignment, we are going to apply a Genetic Algorithm on Maximization (Counting One's function) and Minimizations which are Rastrigin and Ackley functions.

According to Jadaan, Rajamani, & Rao (2008), I can summarise the Genetic Algorithm's steps as following:

- SELECTION: this first step in GAs is required to select two random parents for reproduction. Depending on the optimization function that selection method will work differrent. For example, the inidividuals with higher fitness are likely to be selected for mating in terms of Maximization and those with lower fitness will be selected when working with minimization.
- RECOMBINATION: this step requires the crossover process to create new better individual's representation of gene from its' parent's representation by using one point swapping
- MUTATION: once the offspring population is created after crossover, the mutation operator is used to vary the chromosomes inside the individual's representation by using bit flipping.
- EVALUATION: build rule-base from genome and try on the problem to calculate individual's fitness from fitness function.
- REPLACEMENT: after one generation finishes, the parent population will be replaced by the offspring population to maintain the next cycle.

The Genetic Algorithm stops when the population converges towards the optimal solution.

The visual process of Genetic Algorithm is displayed below:

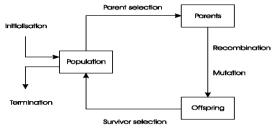


Figure 1.2 Schematic of Genetic Algorithm

#### 2.2 Selection Methods:

In this assignment, the two commonly used Selection methods that I am talking about are Tournament selection and Roulette Wheel selection.

#### **Tournament selection:**

According to Wikipedia, Tournament selection is the method to select an individual from a population of individuals in a Genetic Algorithm. By the involvement of running several "Tournaments" among a few individuals (or "chromosomes") chosen at random from the population. The individual with the best fitness will be selected for the next generation. In other words, the Tournament selection is used to select the best fittest candidate from the current cycle of generation in a Genetic Algorithm. Moreover, Wikipedia also describes how the Tournament algorithm works in steps:

- choose k (the tournament size) individuals from the population at random
- choose the best individual from the tournament with probability p
- choose the second best individual with probability p\*(1-p)
- 4. choose the third best individual with probability  $p*((1-p)^2)$  and so on

Concerning my Tournament Algorithm, k is regarded as 2, which means for each of N generations that I loop through, I will select 2 random parents from the individual's population and compare their fitness, the one with better fitness will be taken to the offspring population.

#### **Roulette Wheel selection:**

Noraini Mohd Razali, John Geraghty state that in a proportional roulette wheel, individuals are selected with a probability that is directly proportional to their fitness values i.e. an individual's selection corresponds to a portion of a roulette wheel. That means fitter individuals take more proportional slots and obviously reverse with those whose fitness is weaker, they take small slots. The N times the wheel spun, the N times the individuals are selected. This process is repeated until the desired number of individuals has been selected (Jadaan, Rajamani, & Rao, 2008).

Noraini Mohd Razali, John Geraghty also state about the selected probability formula as below:

$$p_i = \frac{f_i}{\sum_{i=1}^n f_i}$$

Figure 1.3 selection probability, Pi for individual i

Where n is the size of population and  $f_1, f_2, ..., f_n$  are the fitness of individual 1,2,...,n.

Following are the steps for Roulette Wheel selection (A. Shukla, H. M. Pandey and D. Mehrotra, 2015):

1. Calculate the sum of the fitness values of every individual in the population.

- Calculate the fitness value of each individual and their probability of selection by dividing individual chromosome's fitness by the sum of fitness values of whole population.
- Partition the roulette wheel into sectors according to the probabilities calculated in the second step.
- Spin the wheel 'n' number of times. When the roulette stops, the sector on which the pointer points corresponds to the individual being selected.

#### **Ethical Issues of AI in medical Applications**

One of the related GA applications that I find interested in is Artificial Intelligence via Neural Networks Applied to Medical Applications. Artificial Intelligence can improve society's overall health (Ternent, James Thompson, Maximilian 2020). For example, it is used in healthcare for diagnostic purposes such as places as clinical practice and translational research. Besides all the beneficial sides that AI in medical application bring about, there also raise several ethical issues.

Firstly, what we need to concern about is the impact of Expectations of ML in Medicine according to Ternent, James Thompson, Maximilian. They state that There are unrealistically high hopes for machine learning in medicine, and there are just as many unrealistic fears to complement them. They also state about the statistic of 63% of the adult population [of the United Kingdom] is uncomfortable with allowing personal data to be used to improve healthcare and is unfavorable to artificial intelligence systems replacing doctors and nurses in tasks they usually perform. However, drawing from a German survey, they express that a large portion of medical students believe wholeheartedly that machine learning will improve medicine (Ternent, James Thompson, Maximilian 2020). Therefore, there might have a disconnect between an acceptable explanation for a machine learning expert and an acceptable explanation for a patient, which can cause distress and possibly even harm.

The next is Data and Privacy; they argue that the limitations of data sources (such as electronic health records) can introduce bias because they were only ever intended to be used (in their current state) for clinical care and billing. They also state that bills such as the General Data Protection Regulation (GDPR) bringing well-deserved attention to the storage and processing of personal data people are significantly more skeptical of what personal data is being collected and how it is being used. Therefore, it may create greater pressure on researchers to identify a concrete reason for including a data stream (Ternent, James Thompson, Maximilian 2020).

Lastly, they mention the Lack of Acceptable Explanation of Decision Making. They argue that exposing the facets of a problem considered by a neural network highlights an important ethical consideration: what potential aspects of a decision are suitable for an ethical explanation, and on what level should unethical aspects be removed or recontextualized? for instance, suppose skin tone was an emergent feature in a machine learning model; this would clearly be an unacceptable facet of a patient to consider. Therefore, there will be confusion in making decisions in medical diagnoses.

#### **3 EXPERIMENTATION**

From all the 3 worksheets, I have implemented a Genetic Algorithm containing Fitness calculation, Initialisation, Tournament selection, One-point crossover, and Bit-flipping mutation. All processes are in a form of function and are executed when I called those. And in order to compare with the Tournament selection, I also created a new function that illustrates the method of Roulette Wheel selection, so that when I execute 2 GAs with different selection methods within a program, I can evaluate and plot the performance between those via matplotlib.pyplot library and then the recorded results will be averages shown over 10 runs. Since we are working with not only maximization but also minimization, I have created 2 types of optimization programs, one for maximization using Counting One's function and two for minimization using respectively Rastrigin function and Ackley function to calculate fitness. From worksheet 3, we are required to change fitness calculation to work with real numbers instead of the binary representation (0 and 1).

This is my fitness calculation function with reals, wherein the fitness of an individual is equal to the number of '1's in its array of genes (genome) is easily extended to the sum of the real-valued genes:

Figure 1.4 Counting One's fitness calculation function

Two below are my Rastrigin and Ackley fitness calculation functions with real numbers:

```
# Calculate individual's fitness

def mini_function(ind):
    fitness = 0
    squared = 0
    cosin = 0
    for i in range(0, N):
        squared = ind.gene[i] * ind.gene[i] # x^2
        cosin = 10 * math.cos(ind.gene[i] * (2 * math.pi)) # 10.cos(2.pi.x)
        fitness += squared - cosin # x^2 - 10.cos(2.pi.x)
    fitness += 10 * N # 10.N + x^2 - 10.cos(2.pi.x)
    return fitness
```

```
# Calculate individual's fitness
# first minimisation function

def mini_function(ind):
    fitness = 0
    first_exp = 0
    second_exp = 0
    for i in range(0, N):
        first_exp += math.cos(2 * math.pi * ind.gene[i])
        second_exp += ind.gene[i] * ind.gene[i]
    first_exp = math.exp((1/N) * first_exp)
    second_exp = (-20) * math.exp((-0.2) * math.sqrt((1/N) * second_exp))
    fitness = second_exp - first_exp
    return fitness
```

Figure 1.5 1.6 Rastrigin fitness calculation function and Ackley fitness calculation function

And what I have done to my fitness calculation functions was that I passed the instance of the individual's population (ind) as a parameter, access each genome by looping from i to the size of individual's genes (ind.gene[i]), calculate and return its fitness.

Additionally, I also made changes to the Crossover algorithm to make it work correctly and better since the old crossover returned wrong individual's gene after swapping and I assume the reason could be the changes of temp when we assign back to offspring[i + 1]. I also tried to use deepcopy but it did not work in ways as I expected. (refer to code in the apendix)

And to even make the program more efficient, I have created an optimization function that illustrates the Elitism. Jadaan, Rajamani, & Rao (2008) state that Elitism involves replacing the worst chromosomes in the children population with the best members of the parent population. This operator has proved to increase the speed of convergence of the GA because it ensures that the best solution found in each generation is retained (Jadaan, Rajamani, & Rao, 2008). In the Maximization program, I replaced the two worst in the new population with the two best in the old population, the best fitness is the max fitness (best fitness). And the reverse in Minimization one, I replaced the two best in the new population with the two worst in the old population, the best fitness is the min fitness (worst fitness) at specific indices. (refer to code in the apendix).

#### 1. MAXIMIZATION RESULTS:

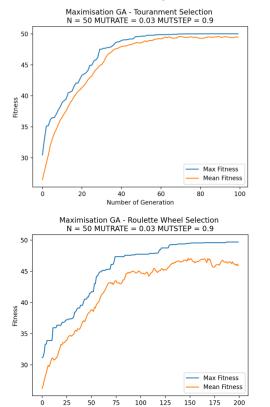
Two figures below are Tournament selection and Roulette Wheel selection that I have implemented to my maximization program using Counting One's function:

```
# Roulette Wheel Selection Process
def RW_selection(population):
    # total fitness of initial pop
    initial_fits = total_fitness(population)

    offspring = copy.deepcopy(population)
    # Roulette Wheel Selection Process
    # Select two parents and recombine pairs of parents
    for i in range(0, P):
        selection_point = random.uniform(0.0, initial_fits)
        running_total = 0
        j = 0
        while running_total <= selection_point:
            running_total += population[j].fitness
        j += 1
        if(j == P):
            break
        offspring[i] = population[j-1]</pre>
```

return offspring

Figure 1.7 1.8 Tournament selection Maximization and Roulette Wheel selection Maximization



Number of Generation

Figure 1.9 2.0 a single run of Maximization GA. – Tournament selection

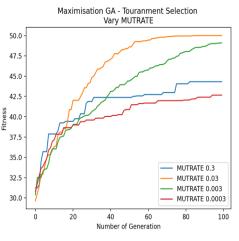
and Roulette Wheel selection

Gene length: N=50, Individual popultion: P=50, Mutation rate: MUTRATE = 0.03, Mutation step: MUTSTEP = 0.9, Number of Generation: GENERATIONS = 100/200.

Over 10 runs of my maximization GA with Tournament selection, I found that the max fitness increased and converged into a horizontal line at 50.0, while the mean fitness only reached 49.46629078875493. This plot was conducted over 100 cycles of generations. I plotted the same statistics with my Maximization GA with Roulette Wheel selection over 10 runs, and even though we could see that both Max and Mean fitness increased, but it took over 200 generations to converge. The max fitness only reached 49.68134975149576 while the mean one was even

lower, about 45.90391924550532.

After altering the Mutation rate and for both maximization GA with Tournament and Roulette Wheel over 4 different mutation rates, I noticed that the fitness reached max when MUTRATE = 0.03 and MUTSTEP = 0.9, which can be explained in the plot below:



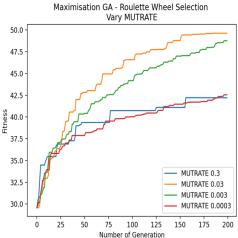
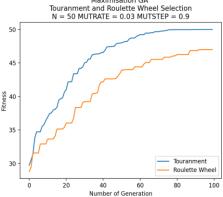


Figure 2.1 Max fitness at 50.0 - MUTRATE 0.03 Figure 2.2 Max fitness at 49.62520845180895 –MUTRATE 0.03

I also made 2 plots to show a clear competitive performance between two selection methods as below:



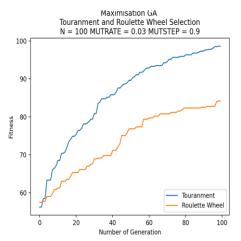


Figure 2.3 2.4 comparisons between Tournament selection and Roulette Wheel selection

The first plot with the gene length of 50 and the second one with the gene length of 100. As you can see, for both gene lengths, the fitness of Tournament selection always reaches its max first compared to those of Roulette Wheel selection. Tournament's fitness reached 50.0 in the first plot and 98.61599778697504 in the second one but never reaches 100.0 as I expect, so I think the problem might depend on the number of Generations, maybe when we increase the cycle, the fitness with 100 genes length hopefully be able to flatten. In regard to the Roulette Wheel's fitness, it reached max at 46.9937534034408 for the first plot and 84.18984529423331 for the second one.

#### 2. MINIMIZATION RESULTS:

As we are working with minimization program, then the best fitness that we get should be the smallest one and we as well should select the individuals with lower fitness in the population. Therefore, there are going to be some changes in the Selection process while implementing GA.

#### 2.1 Rastrigin minimization function

From the equation in figure 1.0 – Rastrigin minimization function, I have made some changes in Tournament selection and Roulette Wheel selection compared against those in figure 1.7 and 1.8.

Figure 2.5 Minimization Tournament - Rastrigin function

In this minimization Tournament selection, I changed the if condition so that the individual with smaller fitness will be selected for the offspring population.

```
Roulette Wheel Selection Process

of RW_selection(population):

# total fitness of initial pop
total = 0
for ind in population:

total += 1/ind.fitness

offspring = []

# Roulette Wheel Selection Process

# Select two parents and recombine pairs of parents
for i in range(0, P):

selection_point = random.uniform(0.0, total)

running_total = 0
j = 0

while running_total <= selection_point:

running_total += 1 / (population[j].fitness)

j += 1

if(j == P):

break

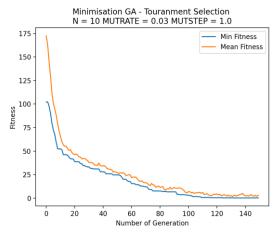
# print(running_total)

# print(j)
offspring.append(copy.deepcopy(population[j-1]))

return offspring
```

Figure 2.6 Minimization Roulette Wheel - Rastrigin function

In this minimization Roulette Wheel selection, we wanted to make sure the individuals with small fitness will get more chance to be selected, so what I did was to inverse the fitness of the individuals and took the sum of it, and that will make the algorithm pick up the weaker individuals.



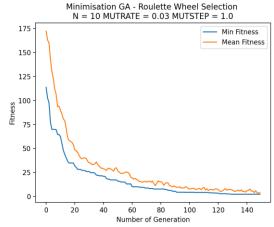
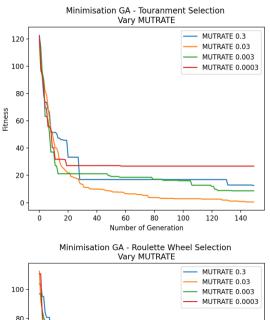


Figure 2.7 2.8 a single run of Minimization GA. – Tournament selection and Roulette Wheel selection

Gene length: N = 10, Individual popultion: P = 50, Mutation rate: MUTRATE = 0.03, Mutation step: MUTSTEP = 1.0, Number of Generation: GENERATIONS = 150

Over 10 runs of my minimization GA with Tournament selection, I found that the min fitness decreased sharply and converged into a horizontal line at 0.2762741152367312 which is the best fitness that I can get over 10 different runs, however, I expect to see it drops to 0.0 but the more cycles of generations I increased, it still stayed at nearly 0.0 and I think it will make the algorithm more realistic to have some approximate error, while the mean fitness only reduced to 3.217860610617649. This plot was conducted over 150 cycles of generations. With the same statistics, I also plotted a minimization GA using Roulette Wheel Selection and the lowest possible fitness achieved over 10 runs was 2.347698494062243 and the mean fitness was 3.9497076377781446.

I also made a variation of Mutation rate and Mutation step, and after altering and changing the Mutation step from 0.3 to 0.7 to 1.0, the best one that made the fitness decreased that much is 1.0 and the best possible mutation rate is 0.03 as always.



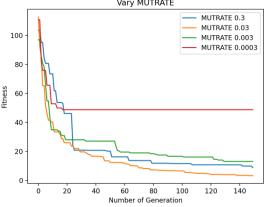


Figure 2.9 Max fitness at 0.4921120534116028 - MUTRATE 0.03 Figure 3.0 Max fitness at 3.3014290163064572 - MUTRATE 0.03

The next plots would be the comparison between two selection

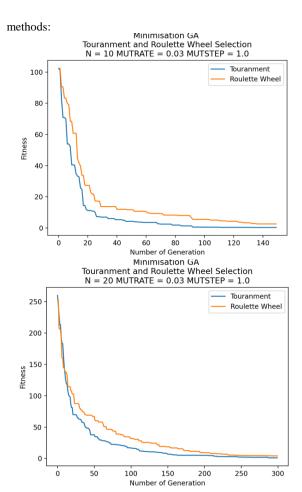


Figure 3.1 3.2 comparisons between Tournament selection and Roulette
Wheel selection

As we can see that both selection methods work well for minimization GA (Rastrigin function), but Tournament selection seems likely to be better. The min fitness of Tournament is 0.35614317207772217, while the one of Roulette Wheel is 2.646551764532333. Since I wanted to challenge my GA over a larger gene length which is 20, I noticed that it took a bit longer to process and conducted more numbers of generations (300 generations) to converge horizontal line.

#### 2.2 Ackley minimization function

Another minimization function that I need to show the experimental results is the Ackley function from figure 1.1. The only change that I needed to make is the Roulette Wheel selection.

```
# Roulette Wheel Selection Process
def RW selection(population):
    # total fitness of initial pop
    total = 0
    for ind in population:
        total += abs(ind.fitness)
    offspring = []
     Roulette Wheel Selection Process
    # Select two parents and recombine pairs of parents
    for i in range(0, P):
        selection_point = random.uniform(0.0, total)
        running_total = 0
        while running total <= selection point:
            running_total += abs(population[j].fitness)
            if(j == P):
        # print(running_total)
        offspring.append(copy.deepcopy(population[j-1]))
   return offspring
```

Figure 3.3 Minimization Roulette Wheel selection Ackley function

since Ackley function returns negative fitness always so that I used the abs() in math library to convert all negative numbers into positive ones. As a result, the largest negative number will become the smallest positive one and reverse. The algorithm will look like the Roulette Wheel selection for maximization program.

The next plot would be the comparison between Tournament and Roulette Wheel selection over the minimization GA of Ackley function.

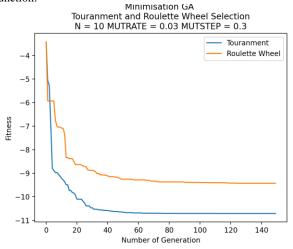


Figure 3.4 comparison between Tournament selection and Roulette Wheel selection

Gene length: N = 10, Individual popultion: P = 50, Mutation rate: MUTRATE = 0.03, Mutation step: MUTSTEP = 0.3, Number of Generation: GENERATIONS = 150

In this plot, each selection method converged at its own line. The finesses of using Tournament selection and Roulette Wheel selection converged horizontally respectively at -10.708492338435587 and -9.426192516643226 over 150 numbers of generations. Both functions used mutation rate of 0.03 and mutation step of 0.3. I also found that it took a bit longer for Roulette Wheel selection to print out result than

Tournament selection.

#### 4 CONCLUSIONS

From all the comparisons between Tournament and Roulette Wheel selection in Figure 2.8 2.9 3.6 3.7, I noticed that the performance of Tournament always reached the optimum fitness better than those of Roulette Wheel regardless of the same statistics. In the maximization program, with the same statistics (mutation rate of 0.03, mutation step of 0.9, 100 numbers of generations) the Tournament selection works better and reaches its max fitness while the Roulette wheel does not. I also found that with 0.03 MUTRATE and 0.9 MUTSTEP that work both for the two selections, however, I believe that their performances might change if we set the statistics not equally, which is not fair to either of the selection methods. In minimization programs, the mutation rate stays the same for both minimization functions which is 0.03, while the mutation step altered 1.0 for Rastrigin function and 0.3 for Ackley function. The change of mutation for each minimization program did not affect the whole GAs, especially the selection methods since I both compared Tournament and Roulette Wheel selection for each minimization program. And once again, the convergence of Tournament looks better than that of Roulette Wheel in all optimization function, which could be explained that the Roulette Wheel selection is based on the probability, the fitter individuals get more chance to be selected, but there is a possibility that the weaker individuals get chosen as well, so the algorithm cannot always optimize the highest fitness as it can, however, the Tournament selection is possible to do that since it always requires and compares two random individuals in the population, and the one with higher fitness will be selected in the offspring, therefore, the algorithm will be able to optimize the best fitness over numbers of generations. From all those facts, I finally can make a conclusion that Tournament selection is a better algorithm to work within GAs.

#### REFERENCES

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## Source code as an appendix

### Github link: https://github.com/Liam1809/Bio Computation

Old crossover

```
temp = individual()
for i in range(0, P, 2):
    temp = coopy.deepcopy(offspring[i])
    crosspoint = random.randint(0, N - 1)
    for j in range(crosspoint, N):
        offspring[i].gene[j] = offspring[i + 1].gene[j].copy()
        offspring[i + 1].gene[j] = temp.gene[j].copy()
```

#### New crossover

```
# Single-point Crossover process
                                                                                                  for j in range(0, crosspoint):
                                                                                                      head1.append(offspring[i].gene[i])
def crossover(offspring):
                                                                                                      head2.append(offspring[i + 1].gene[j])
   # Recombine pairs of parents from offspring
                                                                                                  # crosspoint to N adding gene to each tail
                                                                                                   for j in range(crosspoint, N):
   crossover_offspring = []
                                                                                                      tail2.append(offspring[i + 1].gene[j])
   for i in range(0, P, 2):
                                                                                                      tail1.append(offspring[i].gene[j])
        crosspoint = random.randint(0, N - 1) #pick up one random point in the gene length
                                                                                                  # print("head1 + tail2")
        # 2 new temporary instances
                                                                                                  # print(head1, tail2)
                                                                                                  # print("head2 + tail1")
        temp1 = individual()
                                                                                                  # print(head2, tail1)
       temp2 = individual()
                                                                                                   temp1.gene = head1 + tail2 # add first gene after crossover to temp1
                                                                                                  temp2.gene = head2 + tail1 # add second gene after crossover to temp2
       # 2 heads and 2 tails
                                                                                                  temp1.fitness = counting_ones(temp1) # call counting_ones to add fitness to temporary indv
        head1 = []
                                                                                                  temp2.fitness = counting_ones(temp2)
       tail1 = []
                                                                                                  # append temp1, temp2 respectively to crosover_offspring_offspring
       head2 = []
                                                                                                  crossover_offspring.append(temp1)
                                                                                                  crossover_offspring.append(temp2)
        tail2 = []
                                                                                                  # print(crosover_offspring_offspring[i].gene, crosover_offspring_offspring[i+1].gene)
        # print(offspring[i].gene, offspring[i+1].gene, crosspoint)
        # 0 to crosspoint adding gene to each head
                                                                                              return crossover offspring
```

#### Elitism

```
# Minimisation Optimisation
# Optimisation
                                                                                                                            def optimising(population, new_population):
def optimising(population, new_population):
                                                                                                                               # more optimising
    # more optimising
    # sorting instance with descending fitness
                                                                                                                               # sorting instance with descending fitness
                                                                                                                                population = sorting(population)
    population = sorting(population)
    # take two instances with the best fitness in the old population at index 0 and index 1
                                                                                                                               \# take the two instance with the worst fitness in the old population at index -1 and index -2
    bestFit_old_1 = population[0]
                                                                                                                                worstFit_old_1 = population[-1]
    bestFit_old_2 = population[1]
                                                                                                                                worstFit_old_2 = population[-2]
    # overwrite the old population with mutate_offspring
                                                                                                                                # overwrite the old population with mutate offspring
    population = copy.deepcopy(new_population)
                                                                                                                                population = copy.deepcopy(new_population)
    # sorting instance with descending fitness
                                                                                                                                # sorting instance with descending fitness
    population = sorting(population)
                                                                                                                                population = sorting(population)
    # after deepcopy new pop to old pop
                                                                                                                                # after deepcopy new pop to old pop
    # take the two instance with the worst fitness in the new population at index -1 and index -2
    worstFit_new_1 = population[-1]
                                                                                                                                \# take two instances with the best fitness in the new population at index \theta and index 1
    worstFit new 2 = population[-2]
                                                                                                                                bestFit new 1 = population[8]
                                                                                                                                bestFit_new_2 = population[1]
    # compare the fitness btw the ones in the old pop and the ones in the new pop
    # replace the two worst fitness/gene by the two best fitness/gene at specific index in the new population
                                                                                                                                # compare the fitness btw the ones in the old pop and the ones in the new pop
    if(bestFit_old_1.fitness > worstFit_new_1.fitness):
                                                                                                                                # replace the two best fitness/gene by the two worst fitness/gene at specific index in the new population
        population[-1].fitness = bestFit_old_1.fitness
                                                                                                                                if(worstFit old 1.fitness < bestFit new 1.fitness):</pre>
        population[-1].gene = bestFit_old_1.gene
                                                                                                                                   population[0].gene = worstFit_old_1.gene
    if(bestFit_old_2.fitness > worstFit_new_2.fitness):
                                                                                                                                   population[0].fitness = worstFit_old_1.fitness
        population[-2].fitness = bestFit old 2.fitness
                                                                                                                                if(worstFit_old_2.fitness < bestFit_new_2.fitness):</pre>
        population[-2].gene = bestFit_old_2.gene
                                                                                                                                   population[1].gene = worstFit_old_2.gene
                                                                                                                                   population[1].fitness = worstFit_old_2.fitness
    return population
```

## MAXIMIZATION PROGRAM (COUNTING ONE'S):

```
import random
import copy
import matplotlib.pyplot as plt
# Each individual should be represented by a data structure,
# consisting of an array of binary genes and a fitness value
class individual:
  gene = []
   fitness = 0
  def __repr__(self):
     return "Gene string " + "".join(str(x) for x in self.gene) + " - fitness: " + str(self.fitness)
# The initial population array of such individuals,
# and random gene length number of 50 and population of 50
N = 50
GENERATIONS = 100 # initialise 100 generations
# random mutation rate and mutation step
MUTRATE = 0.03
MUTSTEP = 0.9
# Calculate individual's fitness
# the individual's fitness is equal to the number of '1's in its array of genes (genome)
# instance parameter
def counting_ones(ind):
  fitness = 0
   for i in range(0, N):
     # if(ind.gene[i] == 1): # if gene of an individual at index i equals to 1
       fitness = fitness + ind.gene[i]
  return fitness
# Calculate population's fitness
# list parameter
def total_fitness(population):
   totalfit = 0
   for ind in population:
    totalfit += ind.fitness
   return totalfit
# Initialise original population
def initialise_population():
  population = []
   # Initialise population with random candidate solutions
  # Generate random genes and append to a temporary gene list
   # Assign fitness and gene to individual and append one to population
  for x in range(0, P):
    tempgene = []
     for x in range(0, N):
       tempgene.append(random.uniform(0.0, 1.0)) # a random gene between 0.0 and 1.0(inclusive)
     # print(tempgene)
     newindi = individual() # initialise new instance
     newindi.gene = tempgene.copy() # copy the gene from tempgene and assign to gene of individual
     newindi.fitness = counting_ones(newindi) # initialise instance's fitness
     population.append(newindi)
   return population
# Tourament Selection Process
def touranment_selection(population):
  offspring = []
   # Select two parents and recombine pairs of parents
  for i in range(0, P):
```

```
parent1 = random.randint(0, P - 1)
    off1 = population[parent1]
    parent2 = random.randint(0, P - 1)
     off2 = population[parent2]
    if (off1.fitness > off2.fitness): # if one's fitness higher then add to temp offsptring
       offspring.append(off1)
     else:
       offspring.append(off2)
  return offspring
# Roulette Wheel Selection Process
def RW_selection(population):
  # total fitness of initial pop
  initial_fits = total_fitness(population)
  offspring = copy.deepcopy(population) \\
  # Roulette Wheel Selection Process
  # Select two parents and recombine pairs of parents
  for i in range(0, P):
     selection_point = random.uniform(0.0, initial_fits)
    running\_total = 0
    while running_total <= selection_point:
       running_total += population[j].fitness
       j += 1
       if(j == P):
         break
     offspring[i] = population[j-1]
  return offspring
# Single-point Crossover process
def crossover(offspring):
  # Recombine pairs of parents from offspring
  crossover_offspring = []
  for i in range(0, P, 2):
    crosspoint = random.randint(0, N - 1) #pick up one random point in the gene length
    # 2 new temporary instances
    temp1 = individual()
    temp2 = individual()
     # 2 heads and 2 tails
    head1 = []
    tail1 = []
    head2 = []
    tail2 = []
     # print(offspring[i].gene, offspring[i+1].gene, crosspoint)
     # 0 to crosspoint adding gene to each head
    for j in range(0, crosspoint):
       head1.append(offspring[i].gene[j])
       head2.append(offspring[i + 1].gene[j])
     # crosspoint to N adding gene to each tail
     for j in range(crosspoint, N):
       tail2.append(offspring[i + 1].gene[j])
       tail1.append(offspring[i].gene[j])
     # print("head1 + tail2")
     # print(head1, tail2)
     # print("head2 + tail1")
     # print(head2, tail1)
    temp1.gene = head1 + tail2 # add first gene after crossover to temp1
     temp2.gene = head2 + tail1 # add second gene after crossover to temp2
     temp1.fitness = counting_ones(temp1) # call counting_ones to add fitness to temporary indv
    temp2.fitness = counting_ones(temp2)
     # append temp1, temp2 respectively to crosover_offspring_offspring
    crossover_offspring.append(temp1)
    crossover_offspring.append(temp2)
    # print(crosover_offspring_offspring[i].gene, crosover_offspring_offspring[i+1].gene)
  return crossover_offspring
```

```
#Bit-wise Mutation
def mutation(crosover_offspring, MUTRATE, MUTSTEP):
  # Mutate the result of new_offspring
  mutate_offspring = []
  for i in range(0, P):
    new_indi = individual()
    new_indi.gene = []
     for j in range(0, N):
       gene = crosover_offspring[i].gene[j]
       ALTER = random.uniform(0.0, MUTSTEP)
       MUTPROB = random.uniform(0.0, 100.0)
       if (MUTPROB < (100*MUTRATE)):
         if(random.randint(0, 1) == 1): # if random num is 1, add ALTER
            gene += ALTER
          else: # if random num is 0, minus ALTER
            gene -= ALTER
          if(gene > 1.0): # if gene value is larger than 1.0, reset it to 1.0
            gene = 1.0
          if(gene < 0.0): # if gene value is smaller than 0.0, reset it to 0.0
            gene = 0.0
       new_indi.gene.append(gene) # add gene to instance
     new_indi.fitness = counting_ones(new_indi) # add fitness to instance by calling counting_ones
    mutate_offspring.append(new_indi)
  return mutate_offspring
# Descending sorting
def sorting(population):
  # descending sorting based on individual's fitness
  population.sort(key=lambda individual:individual.fitness, reverse=True)
  return population
# Optimisation
def optimising(population, new_population):
  # more optimising
  # sorting instance with descending fitness
  population = sorting(population)
  # take two instances with the best fitness in the old population at index 0 and index 1
  bestFit_old_1 = population[0]
  bestFit_old_2 = population[1]
  # overwrite the old population with mutate_offspring
  population = copy.deepcopy(new_population)
  # sorting instance with descending fitness
  population = sorting(population)
  # after deepcopy new pop to old pop
  # take the two instance with the worst fitness in the new population at index -1 and index -2
  worstFit_new_1 = population[-1]
  worstFit_new_2 = population[-2]
  # compare the fitness btw the ones in the old pop and the ones in the new pop
  # replace the two worst fitness/gene by the two best fitness/gene at specific index in the new population
  if(bestFit_old_1.fitness > worstFit_new_1.fitness):
     population[-1].fitness = bestFit_old_1.fitness
population[-1].gene = bestFit_old_1.gene
  if(bestFit_old_2.fitness > worstFit_new_2.fitness):
    population[-2].fitness = bestFit_old_2.fitness
    population[-2].gene = bestFit\_old\_2.gene
  return population
def GA(population, Selection, MUTRATE, MUTSTEP):
  # storing data to plot
  meanFit_values = []
```

```
maxFit_values = []
  # ======GENETIC ALGORITHM======
  for gen in range(0, GENERATIONS):
     ## touranment/ RW selection process
    offspring = Selection(population)
    # crossover process
    crossover_offspring = crossover(offspring)
    # mutation process
    mutate_offspring = mutation(crossover_offspring, MUTRATE, MUTSTEP)
    # optimising
    population = optimising(population, mutate_offspring)
    # calculate Max and Mean Fitness
     # storing fitness in a list
    Fit = []
     for ind in population:
       Fit.append(counting_ones(ind))
     # print(Fit)
    maxFit = max(Fit) # take out the max fitness among fitnesses in Fit
    meanFit = sum(Fit)/ P # sum all the fitness and divide by Population size
    # append maxFit and meanFit respectively to MaxFit_values and MeanFit_values
     maxFit_values.append(maxFit)
    meanFit_values.append(meanFit)
     # display
    # print("GENERATION " + str(gen + 1))
    # print("Mean Fitness: " + str(meanFit))
# print("Max Fitness: " + str(maxFit) + "\n")
  print("Max Fitness: " + str(maxFit) + "\n")
  print("Mean Fitness: " + str(meanFit) + "\n")
  return maxFit_values, meanFit_values
# plotting
plt.ylabel("Fitness")
plt.xlabel("Number of Generation")
# Storing
maxFit_data1 = []
maxFit_data2 = []
maxFit_data3 = []
maxFit\_data4 = []
meanFit_data1 = []
meanFit_data2 = []
meanFit\_data3 = []
meanFit_data4 = []
# EXPERIMENT
# TOURANMENT vs ROULETTE WHEEL SELECTION COMPARISON
# [------ UNCOMMENT THIS AND ALTER N TO TEST ------]
plt.title("Maximisation GA \n Touranment and Roulette Wheel Selection \n"
       + "N = " + str(N) + "MUTRATE = " + str(MUTRATE) + "MUTSTEP = " + str(MUTSTEP)) \\
# initialise original population
population = initialise_population()
maxFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.03, 0.9)
maxFit_data2, meanFit_data2 = GA(population, RW_selection, 0.03, 0.9)
```

```
plt.plot(maxFit_data1, label="Touranment")
plt.plot(maxFit_data2, label="Roulette Wheel")
# [------ UNCOMMENT THIS AND ALTER N TO TEST ------]
# N = 50
#MUTRATE = 0.03
# MUTSTEP = 0.9
# Max Fitness: 50.0 - TS
# Max Fitness: 46.9937534034408 - RW
#N = 100
# MUTRATE = 0.03
# MUTSTEP = 0.9
# Max Fitness: 98.61599778697504 - TS
# Max Fitness: 84.18984529423331 - RW
# TOURANMENT SELECTION
# Best Fitness and Mean Fitness of TS
# [------ UNCOMMENT THIS TO TEST -----]
# plt.title("Maximisation GA - Touranment Selection \n"

# "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
## initialise original population
# population = initialise_population()
# maxFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.03, 0.9)
# plt.plot(maxFit_data1, label="Max Fitness")
# plt.plot(meanFit_data1, label="Mean Fitness")
      ------ UNCOMMENT THIS TO TEST ------]
# N = 50
#MUTRATE = 0.03
# MUTSTEP = 0.9
# Max Fitness: 50.0
# Mean Fitness: 49.46629078875493
# Vary MUTRATE
# [------ UNCOMMENT THIS TO TEST ------
# plt.title("Maximisation GA - Touranment Selection \n"
        + "Vary MUTRATE")
## initialise original population
# population = initialise_population()
# maxFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.3, 0.9)
# maxFit_data2, meanFit_data2 = GA(population, touranment_selection, 0.03, 0.9)
\# \ maxFit\_data3, \ meanFit\_data3 = GA(population, touranment\_selection, 0.003, 0.9)
# maxFit_data4, meanFit_data4 = GA(population, touranment_selection, 0.0003, 0.9)
# plt.plot(maxFit_data1, label="MUTRATE 0.3")
# plt.plot(maxFit_data2, label="MUTRATE 0.03")
# plt.plot(maxFit_data3, label="MUTRATE 0.003")
# plt.plot(maxFit_data4, label="MUTRATE 0.0003")
       ------UNCOMMENT THIS TO TEST -------
#N = 50
# MUTSTEP = 0.9
# Max Fitness: 44.322739025242676 - MUTRATE 0.3
# Max Fitness: 50.0 - MUTRATE 0.3
# Max Fitness: 49.10608786326543 - MUTRATE 0.3
```

```
# ROULETTE WHEEL SELECTION
# Best Fitness and Mean Fitness of RW
# [----- UNCOMMENT THIS TO TEST -----]
# GENERATIONS = 200
# plt.title("Maximisation GA - Roulette Wheel Selection \n"
        + "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
## initialise original population
# population = initialise_population()
# maxFit_data1, meanFit_data1 = GA(population, RW_selection, 0.03, 0.9)
# plt.plot(maxFit_data1, label="Max Fitness")
# plt.plot(meanFit_data1, label="Mean Fitness")
# [------ UNCOMMENT THIS TO TEST ------]
\# N = 50
# MUTRATE = 0.03
# MUTSTEP = 0.9
# Max Fitness: 49.68134975149576
# Mean Fitness: 45.90391924550532
# Vary MUTRATE
     ------ UNCOMMENT THIS TO TEST ------]
# GENERATIONS = 200
# plt.title("Maximisation GA - Roulette Wheel Selection \n"
        + "Vary MUTRATE")
## initialise original population
# population = initialise_population()
# maxFit_data1, meanFit_data1 = GA(population, RW_selection, 0.3, 0.9)
# maxFit_data2, meanFit_data2 = GA(population, RW_selection, 0.03, 0.9)
# maxFit_data3, meanFit_data3 = GA(population, RW_selection, 0.003, 0.9)
# maxFit_data4, meanFit_data4 = GA(population, RW_selection, 0.0003, 0.9)
# plt.plot(maxFit_data1, label="MUTRATE 0.3")
# plt.plot(maxFit_data2, label="MUTRATE 0.03")
# plt.plot(maxFit_data3, label="MUTRATE 0.003")
# plt.plot(maxFit_data4, label="MUTRATE 0.0003")
# [------ UNCOMMENT THIS TO TEST ------]
\# N = 50
#MUTSTEP = 0.9
# Max Fitness: 42.21149205376807 - MUTRATE 0.3
# Max Fitness: 49.62520845180895 - MUTRATE 0.03
# Max Fitness: 48.75858687274626 - MUTRATE 0.003
# Max Fitness: 42.5484988452875 - MUTRATE 0.0003
# DISPLAY PLOT
plt.legend(loc = "lower right")
plt.show()
```

## MINIMIZATION PROGRAM (RASTRIGIN FUNCTION):

```
import random
import copy
import math
import matplotlib.pyplot as plt
# Each individual should be represented by a data structure,
# consisting of an array of binary genes and a fitness value
class individual:
  gene = []
  fitness = 0
  def __repr__(self):
    return "Gene string" + "".join(str(x) for x in self.gene) + " - fitness: " + str(self.fitness)
# The initial population array of such individuals,
# and random gene length number of 10 and population of 50
N = 10
GENERATIONS = 150 # initialise 150 generations
# random mutation rate and mutation step
MUTRATE = 0.03
MUTSTEP = 1.0
# Calculate individual's fitness
def mini_function(ind):
  fitness = 0
  squared = 0
  cosin = 0
  for i in range(0, N):
     squared = ind.gene[i] * ind.gene[i] # x^2
    cosin = 10 * math.cos(ind.gene[i] * (2 * math.pi)) # 10.cos(2.pi.x) fitness += squared - cosin # x^2 - 10.cos(2.pi.x)
  fitness += 10 * N # 10.N + x^2 - 10.\cos(2.pi.x)
  return fitness
# Calculate population's fitness
# list parameter
def total_fitness(population):
  totalfit = 0
  for ind in population:
    totalfit += ind.fitness
  return totalfit
# Initialise original population
def initialise_population():
  population = []
  # Initialise population with random candidate solutions
  # Generate random genes and append to a temporary gene list
  # Assign fitness and gene to individual and append one to population
  for x in range(0, P):
    tempgene = []
     for x in range(0, N):
       tempgene.append(random.uniform(-5.12, 5.12)) # a random gene between -5.12 and 5.12(inclusive)
     newindi = individual() # initialise new instance
    newindi.gene = tempgene.copy() # copy the gene from tempgene and assign to gene of individual
     newindi.fitness = mini_function(newindi) # initialise instance's fitness
     population.append(newindi)
```

```
return population
```

```
# Tourament Selection Process
def touranment_selection(population):
  offspring = []
  # Select two parents and recombine pairs of parents
  for i in range(0, P):
    parent1 = random.randint(0, P - 1)
     off1 = population[parent1]
    parent2 = random.randint(0, P - 1)
     off2 = population[parent2]
     if (off1.fitness > off2.fitness): # if one's fitness higher then add the smaller one to temp offsptring
       offspring.append(off2)
     else:
       offspring.append(off1)
  return offspring
# Roulette Wheel Selection Process
def RW_selection(population):
  # total fitness of initial pop
  total = 0
  for ind in population:
    total += 1/ind.fitness
  offspring = []
  # Roulette Wheel Selection Process
  # Select two parents and recombine pairs of parents
  for i in range(0, P):
     selection_point = random.uniform(0.0, total)
     running\_total = 0
     while running_total <= selection_point:
       running_total += 1 / (population[j].fitness)
       i += 1
       if(j == P):
          break
     # print(running_total)
     offspring.append(copy.deepcopy(population[j-1]))
  return offspring
# Single-point Crossover process
def crossover(offspring):
  # Recombine pairs of parents from offspring
  crossover_offspring = []
  for i in range(0, P, 2):
     crosspoint = random.randint(1, N - 1) #pick up one random point in the gene length
     # 2 new temporary instances
    temp1 = individual()
     temp2 = individual()
     #2 heads and 2 tails
    head1 = []
    tail1 = []
head2 = []
    tail2 = []
     # print(offspring[i].gene, offspring[i+1].gene, crosspoint)
     # 0 to crosspoint adding gene to each head
     for j in range(0, crosspoint):
       head1.append(offspring[i].gene[j])
       head 2.append (offspring [i+1].gene[j]) \\
     # crosspoint to N adding gene to each tail
     for j in range(crosspoint, N):
       tail2.append(offspring[i + 1].gene[j])
       tail1.append(offspring[i].gene[j])
     # print("head1 + tail2")
     # print(head1, tail2)
```

```
# print("head2 + tail1")
     # print(head2, tail1)
     temp1.gene = head1 + tail2 # add first gene after crossover to temp1
     temp2.gene = head2 + tail1 # add second gene after crossover to temp2
     temp1.fitness = mini_function(temp1) # call counting_ones to add fitness to temporary indv
     temp2.fitness = mini\_function(temp2)
     # append temp1, temp2 respectively to crosover_offspring_offspring
    crossover_offspring.append(temp1)
    crossover_offspring.append(temp2)
     # print(crosover_offspring_offspring[i].gene, crosover_offspring_offspring[i+1].gene)
  return crossover_offspring
#Bit-wise Mutation
def mutation(crossover_offspring, MUTRATE, MUTSTEP):
  # Mutate the result of new_offspring
  #Bit-wise Mutation
  mutate\_offspring = []
  for i in range(0, P):
    new_indi = individual()
     new_indi.gene = []
     for j in range(0, N):
       gene = crossover_offspring[i].gene[i]
       ALTER = random.uniform(0.0, MUTSTEP)
       MUTPROB = random.uniform(0.0, 100.0)
       if (MUTPROB < (100*MUTRATE)):
         if(random.randint(0, 1) == 1): # if random num is 1, add ALTER
            gene += ALTER
         else: # if random num is 0, minus ALTER
            gene -= ALTER
         if(gene > 5.12): # if gene value is larger than 5.12, reset it to 5.12
            gene = 5.12
         if(gene < -5.12): # if gene value is smaller than -5.12, reset it to -5.12
            gene = -5.12^{\circ}
       new_indi.gene.append(gene)
     new_indi.fitness = mini_function(new_indi) # add fitness to instance by calling mini_function
     mutate_offspring.append(new_indi)
  return mutate_offspring
# Descending sorting
def sorting(population):
  # descending sorting based on individual's fitness
  population.sort(key=lambda individual:individual.fitness, reverse=True)
  return population
# Minimisation Optimisation
def\ optimising (population,\ new\_population):
  # more optimising
  # sorting instance with descending fitness
  population = sorting(population)
  # take the two instance with the worst fitness in the old population at index -1 and index -2
  worstFit\_old\_1 = population[-1]
  worstFit_old_2 = population[-2]
  # overwrite the old population with mutate_offspring
  population = copy.deepcopy(new_population)
  # sorting instance with descending fitness
  population = sorting(population)
  # after deepcopy new pop to old pop
  # take two instances with the best fitness in the new population at index 0 and index 1
  bestFit_new_1 = population[0]
  bestFit_new_2 = population[1]
  # compare the fitness btw the ones in the old pop and the ones in the new pop
```

```
# replace the two best fitness/gene by the two worst fitness/gene at specific index in the new population
  if(worstFit_old_1.fitness < bestFit_new_1.fitness):</pre>
     population[0].gene = worstFit_old_1.gene
     population[0].fitness = worstFit_old_1.fitness
  if(worstFit_old_2.fitness < bestFit_new_2.fitness):
     population[1].gene = worstFit_old_2.gene
     population [1]. fitness = worstFit\_old\_2. fitness
  return population
def GA(population, Selection, MUTRATE, MUTSTEP):
             ====GENETIC ALGORITHM=
  # storing data to plot
  meanFit_values = []
  minFit_values = []
   for gen in range(0, GENERATIONS):
     # touranment selection process / RW selection process
     offspring = Selection(population) \\
     # crossover process
     crossover_offspring = crossover(offspring)
     # mutation process
     mutate_offspring = mutation(crossover_offspring, MUTRATE, MUTSTEP)
     population = optimising(population, mutate_offspring)
     # calculate Max and Mean Fitness
     # storing fitness in a list
     Fit = []
     for ind in population:
       Fit.append(mini_function(ind))
     # print(Fit)
     minFit = min(Fit) # take out the min fitness among fitnesses in Fit
     meanFit = sum(Fit)/ P # sum all the fitness and divide by P size
     # append minFit and meanFit respectively to MinFit_values and MeanFit_values
     minFit_values.append(minFit)
     meanFit_values.append(meanFit)
     # display
     # print("GENERATION " + str(gen + 1))
  print("Min Fitness: " + str(minFit) + "\n")
print("Mean Fitness: " + str(meanFit) + "\n")
  return minFit_values, meanFit_values
# plotting
plt.ylabel("Fitness")
plt.xlabel("Number of Generation")
# Storing
minFit_data1 = []
minFit_data2 = []
minFit_data3 = []
minFit_data4 = []
meanFit_data1 = []
meanFit_data2 = []
meanFit_data3 = []
meanFit_data4 = []
# EXPERIMENT
```

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```
# TOURANMENT vs ROULETTE WHEEL SELECTION COMPARISON
# [------ UNCOMMENT THIS AND ALTER N TO TEST ------]
plt.title("Minimisation GA \setminus n \ Touranment \ and \ Roulette \ Wheel \ Selection \setminus n" \\ + "N = " + str(N) + " \ MUTRATE = " + str(MUTRATE) + " \ MUTSTEP = " + str(MUTSTEP))
# initialise original population
population = initialise_population()
minFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.03, 1.0)
minFit_data2, meanFit_data2 = GA(population, RW_selection, 0.03, 1.0)
plt.plot(minFit_data1, label="Touranment")
plt.plot(minFit_data2, label="Roulette Wheel")
# [------ UNCOMMENT THIS AND ALTER N TO TEST ------]
#N = 10
#MUTRATE = 0.03
# MUTSTEP = 1.0
# Min Fitness: 0.35614317207772217 - TS
# Min Fitness: 2.646551764532333 - RW
#N = 20
# MUTRATE = 0.03
# MUTSTEP = 1.0
# Min Fitness: 0.9973430696900323 - TS
# Min Fitness: 4.102001421670991 - RW
# TOURANMENT SELECTION
# Best Fitness and Mean Fitness of TS
# [------ UNCOMMENT THIS TO TEST -----]
# plt.title("Minimisation GA - Touranment Selection \n" 
# "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
## initialise original population
# population = initialise_population()
# minFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.03, 1.0)
# plt.plot(minFit_data1, label="Min Fitness")
# plt.plot(meanFit_data1, label="Mean Fitness")
# [------ UNCOMMENT THIS TO TEST ------]
#N = 10
# MUTRATE = 0.03
# MUTSTEP = 1.0
# Min Fitness: 0.2762741152367312
# Mean Fitness: 3.217860610617649
# Vary MUTRATE
# [------ UNCOMMENT THIS TO TEST -----]
# plt.title("Minimisation GA - Touranment Selection \n"
         + "Vary MUTRATE")
## initialise original population
# population = initialise_population()
# minFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.3, 1.0)
# minFit_data2, meanFit_data2 = GA(population, touranment_selection, 0.03, 1.0)
```

```
# minFit_data3, meanFit_data3 = GA(population, touranment_selection, 0.003, 1.0)
# minFit_data4, meanFit_data4 = GA(population, touranment_selection, 0.0003, 1.0)
# plt.plot(minFit_data1, label="MUTRATE 0.3")
# plt.plot(minFit_data2, label="MUTRATE 0.03")
# plt.plot(minFit_data3, label="MUTRATE 0.003")
# plt.plot(minFit_data4, label="MUTRATE 0.0003")
           ----- UNCOMMENT THIS TO TEST ------]
\#N = 10
# MUTSTEP = 1.0
# Min Fitness: 12.5460038868992 - MUTRATE 0.3
# Min Fitness: 0.4921120534116028 - MUTRATE 0.03
# Min Fitness: 8.66909400410961 - MUTRATE 0.003
# Min Fitness: 26.745458844423908 - MUTRATE 0.0003
# ROULETTE WHEEL SELECTION
# Best Fitness and Mean Fitness of RW
# [------ UNCOMMENT THIS TO TEST ------]
# plt.title("Minimisation GA - Roulette Wheel Selection \n" # + "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
## initialise original population
# population = initialise_population()
# minFit_data1, meanFit_data1 = GA(population, RW_selection, 0.03, 1.0)
# plt.plot(minFit_data1, label="Min Fitness")
# plt.plot(meanFit_data1, label="Mean Fitness")
# [------ UNCOMMENT THIS TO TEST ------
# N = 10
# MUTRATE = 0.03
# MUTSTEP = 1.0
# Min Fitness: 2.347698494062243
# Mean Fitness: 3.9497076377781446
# Vary MUTRATE
# [----- UNCOMMENT THIS TO TEST -----]
# plt.title("Minimisation GA - Roulette Wheel Selection \n"
        + "Vary MUTRATE")
## initialise original population
# population = initialise_population()
\# \ minFit\_data1, \ meanFit\_data1 = GA(population, \ RW\_selection, \ 0.3, \ 1.0)
# minFit_data2, meanFit_data2 = GA(population, RW_selection, 0.03, 1.0) # minFit_data3, meanFit_data3 = GA(population, RW_selection, 0.003, 1.0)
# minFit_data4, meanFit_data4 = GA(population, RW_selection, 0.0003, 1.0)
# plt.plot(minFit_data1, label="MUTRATE 0.3")
# plt.plot(minFit_data2, label="MUTRATE 0.03")
# plt.plot(minFit_data3, label="MUTRATE 0.003")
# plt.plot(minFit_data4, label="MUTRATE 0.0003")
        ------ UNCOMMENT THIS TO TEST ------]
# [---
\# N = 10
# MUTSTEP = 1.0
# Min Fitness: 8.848386018229803 - MUTRATE 0.3
# Min Fitness: 3.3014290163064572 - MUTRATE 0.03
# Min Fitness: 13.071407182572443 - MUTRATE 0.003
# Min Fitness: 48.747183334043555 - MUTRATE 0.0003
# DISPLAY PLOT
plt.legend(loc = "upper right")
plt.show()
```

## MINIMIZATION PROGRAM (ACKLEY FUNCTION):

```
import random
import copy
import math
import matplotlib.pyplot as plt
# Each individual should be represented by a data structure,
# consisting of an array of binary genes and a fitness value
class individual:
  gene = []
  fitness = 0
  def __repr__(self):
     return "Gene string " + "".join(str(x) for x in self.gene) + " - fitness: " + str(self.fitness)
# The initial population array of such individuals,
# and random gene length number of 10 and population of 50
P = 50
N = 10
GENERATIONS = 150 # initialise 150 generations
# random mutation rate and mutation step
MUTRATE = 0.03
MUTSTEP = 0.3
# Calculate individual's fitness
# first minimisation function
def mini function(ind):
  fitness = 0
  first_exp = 0
  second \exp = 0
  for i in range(0, N):
     first_exp += math.cos(2 * math.pi * ind.gene[i])
     second_exp += ind.gene[i] * ind.gene[i]
  first_exp = math.exp((1/N) * first_exp)
second_exp = (-20) * math.exp((-0.2) * math.sqrt((1/N) * second_exp))
  fitness = second_exp - first_exp
  return fitness
# Calculate population's fitness
# list parameter
def total_fitness(population):
  totalfit = 0
  for ind in population:
    totalfit += ind.fitness
  return totalfit
# Initialise original population
def initialise_population():
  population = []
  # Initialise population with random candidate solutions
  # Generate random genes and append to a temporary gene list
  # Assign fitness and gene to individual and append one to population
  for x in range(0, P):
     tempgene = []
     for x in range(0, N):
       tempgene.append(random.uniform(-32.0, 32.0)) # a random gene between -5.12 and 5.12(inclusive)
     # print(tempgene)
     newindi = individual() # initialise new instance
     newindi.gene = tempgene.copy() # copy the gene from tempgene and assign to gene of individual
    newindi.fitness = mini_function(newindi) # initialise instance's fitness
     population.append(newindi)
  return population
# Tourament Selection Process
def touranment selection(population):
  offspring = []
```

```
# Select two parents and recombine pairs of parents
  for i in range(0, P):
     parent1 = random.randint(0, P - 1)
     off1 = population[parent1]
    parent2 = random.randint(0, P - 1)
     off2 = population[parent2]
     if (off1.fitness > off2.fitness): # if one's fitness higher then add the smaller one to temp offsptring
       offspring.append(off2)
     else:
       offspring.append(off1)
  return offspring
# Roulette Wheel Selection Process
def RW selection(population):
  # total fitness of initial pop
  total = 0
  for ind in population:
     total += abs(ind.fitness)
  off spring = []
  # Roulette Wheel Selection Process
  # Select two parents and recombine pairs of parents
  for i in range(0, P):
     selection_point = random.uniform(0.0, total)
     running\_total = 0
     while running total <= selection point:
       running total += abs(population[j].fitness)
       j += 1
       if(j == P):
         break
     # print(running_total)
     # print(j)
     offspring.append(copy.deepcopy(population[j-1]))
  return offspring
# Single-point Crossover process
def crossover(offspring):
  # Recombine pairs of parents from offspring
  crossover_offspring = []
  for i in range(0, P, 2):
     crosspoint = random.randint(1, N - 1) #pick up one random point in the gene length
     # 2 new temporary instances
     temp1 = individual()
     temp2 = individual()
     # 2 heads and 2 tails
    head1 = []
tail1 = []
head2 = []
    tail2 = []
     # print(offspring[i].gene, offspring[i+1].gene, crosspoint)
     # 0 to crosspoint adding gene to each head
     for j in range(0, crosspoint):
       head1.append(offspring[i].gene[j])\\
       head2.append(offspring[i + 1].gene[j])
     # crosspoint to N adding gene to each tail for j in range(crosspoint, N):
        tail2.append(offspring[i + 1].gene[j])
        tail1.append(offspring[i].gene[j])
     # print("head1 + tail2")
     # print(head1, tail2)
     # print("head2 + tail1")
     # print(head2, tail1)
     temp1.gene = head1 + tail2 # add first gene after crossover to temp1
     temp2.gene = head2 + tail1 # add second gene after crossover to temp2
     temp1.fitness = mini_function(temp1) # call counting_ones to add fitness to temporary indv
```

```
temp2.fitness = mini function(temp2)
    # append temp1, temp2 respectively to crosover offspring offspring
     crossover_offspring.append(temp1)
     crossover_offspring.append(temp2)
     # print(crosover_offspring_offspring[i].gene, crosover_offspring_offspring[i+1].gene)
  return crossover_offspring
#Bit-wise Mutation
def mutation(crossover_offspring, MUTRATE, MUTSTEP):
  # Mutate the result of new_offspring
  #Bit-wise Mutation
  mutate_offspring = []
  for i in range(0, P):
    new indi = individual()
     new_indi.gene = []
     for j in range(0, N):
       gene = crossover_offspring[i].gene[j]
       ALTER = random.uniform(0.0, MUTSTEP)
       MUTPROB = random.uniform(0.0, 100.0)
       if (MUTPROB < (100*MUTRATE)):
         if(random.randint(0, 1) == 1): # if random num is 1, add ALTER
           gene += ALTER
         else: # if random num is 0, minus ALTER
            gene -= ALTER
         if(gene > 32.0): # if gene value is larger than 32.0, reset it to 32.0
           gene = 32.0
         if(gene < -32.0): # if gene value is smaller than -32.0, reset it to -32.0
            gene = -32.0
       new_indi.gene.append(gene)
     new_indi.fitness = mini_function(new_indi) # add fitness to instance by calling mini_function
    mutate offspring.append(new indi)
  return mutate_offspring
# Descending sorting
def sorting(population):
  # descending sorting based on individual's fitness
  population.sort(key=lambda individual:individual.fitness, reverse=True)
  return population
# Minimisation Optimisation
def optimising(population, new_population):
  # more optimising
  # sorting instance with descending fitness
  population = sorting(population)
  # take the two instance with the worst fitness in the old population at index -1 and index -2
  worstFit\_old\_1 = population[-1]
  worstFit_old_2 = population[-2]
  # overwrite the old population with mutate_offspring
  population = copy.deepcopy(new population)
  # sorting instance with descending fitness
  population = sorting(population)
  # after deepcopy new pop to old pop
  # take two instances with the best fitness in the new population at index 0 and index 1
  bestFit_new_1 = population[0]
  bestFit_new_2 = population[1]
  # compare the fitness btw the ones in the old pop and the ones in the new pop
  # replace the two best fitness/gene by the two worst fitness/gene at specific index in the new population
  if(worstFit old 1.fitness < bestFit new 1.fitness):
     population[0].gene = worstFit_old_1.gene
     population[0].fitness = worstFit_old_1.fitness
```

```
if(worstFit old 2.fitness < bestFit new 2.fitness):
     population[1].gene = worstFit_old_2.gene
     population[1].fitness = worstFit_old_2.fitness
  return population
def GA(population, Selection, MUTRATE, MUTSTEP):
                 GENETIC ALGORITHM
  # storing data to plot
  meanFit_values = []
  minFit_values = []
   for gen in range(0, GENERATIONS):
     # touranment selection process
     offspring = Selection(population)
     # crossover process
     crossover_offspring = crossover(offspring)
     # mutation process
     mutate offspring = mutation(crossover offspring, MUTRATE, MUTSTEP)
     population = optimising(population, mutate offspring)
     # calculate Max and Mean Fitness
     # storing fitness in a list
     Fit = []
     for ind in population:
       Fit.append(mini_function(ind))
     # print(Fit)
     minFit = min(Fit) # take out the min fitness among fitnesses in Fit
     meanFit = sum(Fit)/ P # sum all the fitness and divide by P size
     # append minFit and meanFit respectively to MinFit_values and MeanFit_values
     minFit_values.append(minFit)
     meanFit_values.append(meanFit)
     ## display
     # print("GENERATION " + str(gen + 1))
  print("Min Fitness: " + str(minFit) + "\n")
print("Mean Fitness: " + str(meanFit) + "\n")
  return minFit_values, meanFit_values
plt.ylabel("Fitness")
plt.xlabel("Number of Generation")
# Storing
minFit_data1 = []
minFit_data2 = []
minFit_data3 = []
minFit data4 = []
meanFit_data1 = []
meanFit_data2 = []
meanFit_data3 = []
meanFit_data4 = []
# EXPERIMENT
# TOURANMENT vs ROULETTE WHEEL SELECTION COMPARISON
# [------ UNCOMMENT THIS AND ALTER N TO TEST ------]
```

```
plt.title("Minimisation GA \n Touranment and Roulette Wheel Selection \n"
       + "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
N = 10
# initialise original population
population = initialise_population()
minFit data1, meanFit data1 = GA(population, touranment selection, 0.03, 0.3)
minFit_data2, meanFit_data2 = GA(population, RW_selection, 0.03, 0.3)
plt.plot(minFit_data1, label="Touranment")
plt.plot(minFit_data2, label="Roulette Wheel")
# [------ UNCOMMENT THIS AND ALTER N TO TEST ------]
#MUTRATE = 0.03
# MUTSTEP = 0.3
# Min Fitness: -10.708492338435587 - TS
# Min Fitness: -9.426192516643226 - RW
#N = 50
# MUTRATE = 0.03
# MUTSTEP = 0.3
# Min Fitness: -4.225967898881414 - TS
# Min Fitness: -4.0251242091551624 - RW
# TOURANMENT SELECTION
# Best Fitness and Mean Fitness of TS
# [------ UNCOMMENT THIS TO TEST -----]
# plt.title("Minimisation GA - Touranment Selection \n" 
# "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
## initialise original population
# population = initialise_population()
# minFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.03, 0.3)
# plt.plot(minFit_data1, label="Min Fitness")
# plt.plot(meanFit_data1, label="Mean Fitness")
# [------ UNCOMMENT THIS TO TEST ------]
\#N = 10
#MUTRATE = 0.03
# MUTSTEP = 0.3
# Min Fitness: -10.852278293354441
# Mean Fitness: -10.804764892978262
# Vary MUTRATE
# [------ UNCOMMENT THIS TO TEST ------]
# plt.title("Minimisation GA - Touranment Selection \n"
        + "Vary MUTRATE")
## initialise original population
# population = initialise_population()
# minFit_data1, meanFit_data1 = GA(population, touranment_selection, 0.3, 0.3)
# minFit_data2, meanFit_data2 = GA(population, touranment_selection, 0.03, 0.3)
# minFit_data3, meanFit_data3 = GA(population, touranment_selection, 0.003, 0.3)
```

```
# minFit data4, meanFit data4 = GA(population, touranment selection, 0.0003, 0.3)
# plt.plot(minFit_data1, label="MUTRATE 0.3")
# plt.plot(minFit_data2, label="MUTRATE 0.03")
# plt.plot(minFit data3, label="MUTRATE 0.003")
# plt.plot(minFit_data4, label="MUTRATE 0.0003")
          ------ UNCOMMENT THIS TO TEST ------]
\#N = 10
# MUTSTEP = 0.3
# Min Fitness: -8.610121679863145 - MUTRATE 0.3
# Min Fitness: -11.170587355807932 - MUTRATE 0.03
# Min Fitness: -9.524295765255925 - MUTRATE 0.003
# Min Fitness: -8.867615254560471 - MUTRATE 0.0003
# ROULETTE WHEEL SELECTION
# Best Fitness and Mean Fitness of RW
# [------ UNCOMMENT THIS TO TEST ------]
# plt.title("Minimisation GA - Roulette Wheel Selection \n"

# "N = " + str(N) + " MUTRATE = " + str(MUTRATE) + " MUTSTEP = " + str(MUTSTEP))
## initialise original population
# population = initialise_population()
# minFit data1, meanFit data1 = GA(population, RW selection, 0.03, 0.3)
# plt.plot(minFit_data1, label="Min Fitness")
# plt.plot(meanFit_data1, label="Mean Fitness")
# [------ ŪNCOMMENT THIS TO TEST ------]
\#N = 10
#MUTRATE = 0.03
# MUTSTEP = 0.3
# Min Fitness: -7.929936862642863
# Mean Fitness: -7.686559831777039
# Vary MUTRATE
# [----- UNCOMMENT THIS TO TEST -----]
# plt.title("Minimisation GA - Roulette Wheel Selection \n"
        + "Vary MUTRATE")
## initialise original population
# population = initialise_population()
# minFit_data1, meanFit_data1 = GA(population, RW_selection, 0.3, 0.3)
# minFit_data2, meanFit_data2 = GA(population, RW_selection, 0.03, 0.3)
# minFit_data3, meanFit_data3 = GA(population, RW_selection, 0.003, 0.3)
# minFit_data4, meanFit_data4 = GA(population, RW_selection, 0.0003, 0.3)
# plt.plot(minFit_data1, label="MUTRATE 0.3")
# plt.plot(minFit_data2, label="MUTRATE 0.03")
# plt.plot(minFit_data3, label="MUTRATE 0.003")
# plt.plot(minFit_data4, label="MUTRATE 0.0003")
# [------ UNCOMMENT THIS TO TEST ------]
\# N = 10
# MUTSTEP = 0.3
# Min Fitness: -14.254437249778938 - MUTRATE 0.3
# Min Fitness: -10.447878031888726 - MUTRATE 0.03
# Min Fitness: -9.727185493333165 - MUTRATE 0.003
# Min Fitness: -8.94342734801122 - MUTRATE 0.0003
# DISPLAY PLOT
plt.legend(loc = "upper right")
plt.show()
```