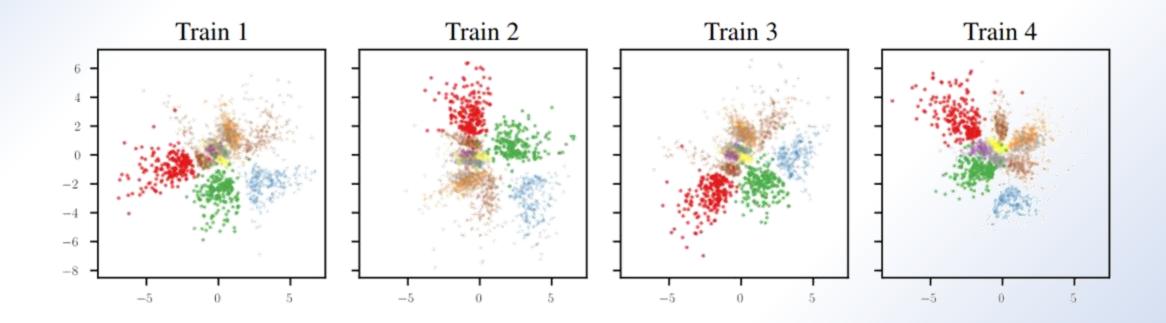
# RELATIVE REPRESENTATION EVALUATIONS AND COMPARISONS OF AUTOENCODERS AND VISUAL TRANSFORMERS

A further look into the paper "Relative representations enable zeroshot latent space communication." by Moschella, Luca, et al. Models, like Autoencoders and Transformers, transform high dimensional data into a meaningful representation they can use to solve tasks. These learned representations depend on the initial state and hyperparameters of the given model.

- Is there a meaningful way of comparing different learned representations?
- If there is, to what extent and to what architectures can this representation be used for?

## **AUTOENCODERS**

- Autoencoders' representations of a particular dataset reconstruction are intrinsically similar.
- They are extrinsically the same after an isometric correction.



## **COSINE SIMILARITY REPRESENTATION**

$$r_{x^{(i)}} = (S_c(e_{x^{(i)}}, e_{a^{(1)}}), S_c(e_{x^{(i)}}, e_{a^{(2)}}), \dots, S_c(e_{x^{(i)}}, e_{a^{(|A|)}}))$$

#### ...where:

- $\mathbb A$  is a set of pre-defined anchor points from the dataset, used to build the representation.  $a^{(n)} \in \mathbb A \ \, \forall n$
- $e_{\chi^{(i)},e_{a^{(n)}}}$  are the input and n-th anchor representations in latent space respectively.
- $S_c(a, b) = \frac{ab}{||a||*||b||} = \cos \theta$ , where  $\theta$  is the angle between the two vectors.

Invariant representation to relative rotations!

#### **EVALUATION METRICS**

The following metrics have been used to compare the representations:

Cosine Similarity Index:

Cosine(s) = 
$$\frac{f_{\mathbb{X}}(s) \cdot f_{\mathbb{Y}}(s)}{\|f_{\mathbb{X}}(s)\| \|f_{\mathbb{Y}}(s)\|}$$

Jaccard Index:

$$\mathbf{Jaccard}(\mathbf{s}) = \frac{|\operatorname{KNN}_{k}^{\mathbb{X}}(f_{\mathbb{X}}(s)) \cap \operatorname{KNN}_{k}^{\mathbb{Y}}(f_{\mathbb{X}}(s))|}{|\operatorname{KNN}_{k}^{\mathbb{X}}(f_{\mathbb{X}}(s)) \cup \operatorname{KNN}_{k}^{\mathbb{Y}}(f_{\mathbb{X}}(s))|}$$

Where X, Y are source and target space respectively, and  $f_X : S \to X$ ,  $f_Y : S \to Y$  are the encoding functions.

#### **ARCHITECTURES AND DATASETS**

The type of models used in this project are the following:

- Convolutional Autoencoder (with variable bottleneck size)
- Visual Transformer

The architectures are then trained on one of 4 datasets as reconstruction models:

- MNIST
- kMNIST
- FashionMNIST
- CIFAR-10

#### **HYPERPARAMETERS**

**Optimizer:** Adam

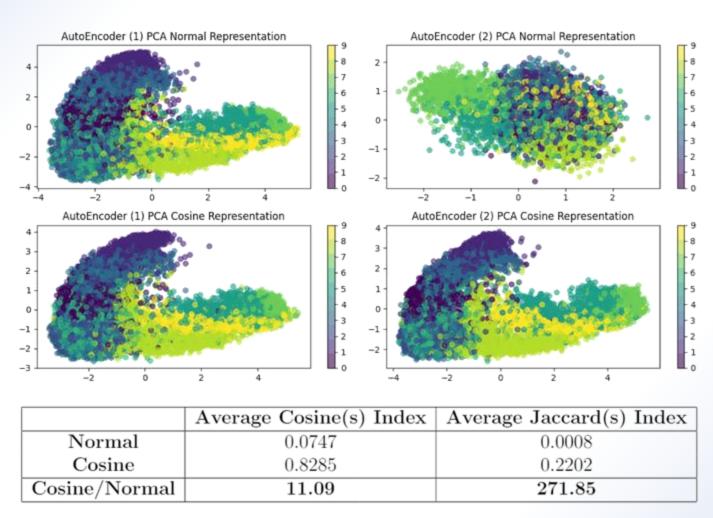
**Loss function:** Mean Square Error (MSE)

Number of anchors: 30 per class

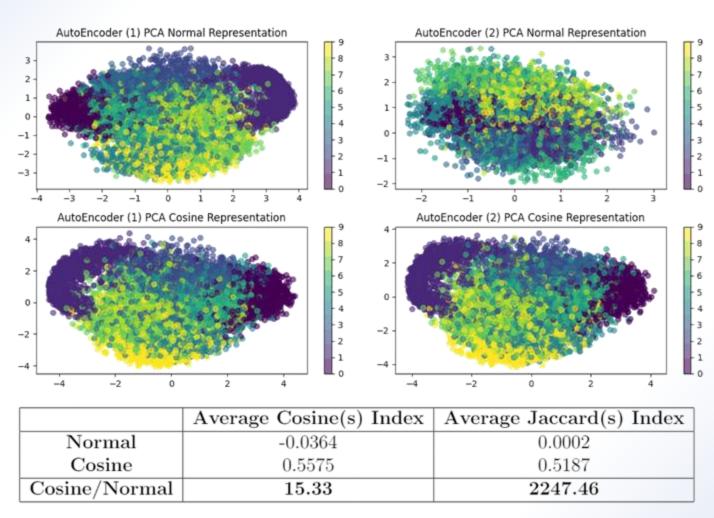
Number of k-neighbours for Jaccard index: 10

Regularization: Dropout (0.5), Batch Normalization, Early Stopping

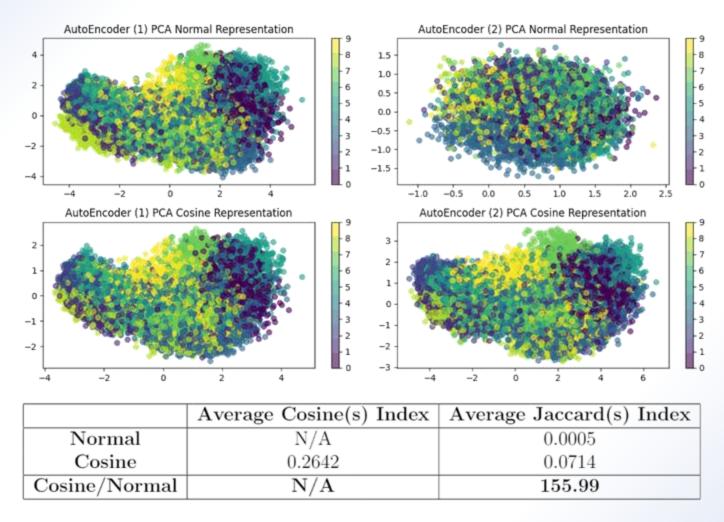
#### 2 Autoencoders – Bottleneck of size 48 - FashionMNIST



#### 2 Autoencoders – Bottleneck of size 24 - MNIST

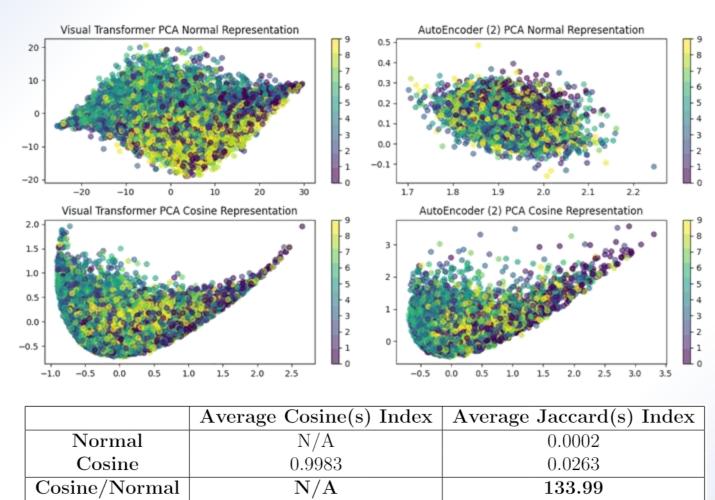


#### 2 Autoencoders – Bottleneck of sizes 48,24 – kMNIST

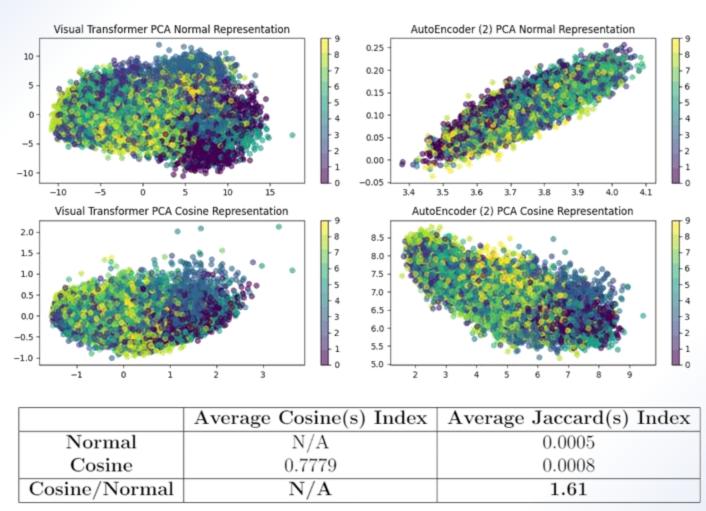


Different scales in Cosine representation when the bottlenecks have different dimensionalities!

#### Visual Transformer and Autoencoder – Bottleneck of size 72 – CIFAR10



#### Visual Transformer and Autoencoder – Bottleneck of size 48 – kMNIST



## **CONCLUSIONS**

- Autoencoders' latent spaces are comparable through a rotationally invariant representation.
- Autoencoders of different latent space dimensionalities scale with respect to the number of dimensions.
- Transformers and Autoencoders do share inconsistent similarities, further research is required in order to have a definitive answer regarding the possibility of alternative representations that might fit the models better.