

# Real-Time Outlier Detection with Dynamic Process Limits

## Process Control 2023

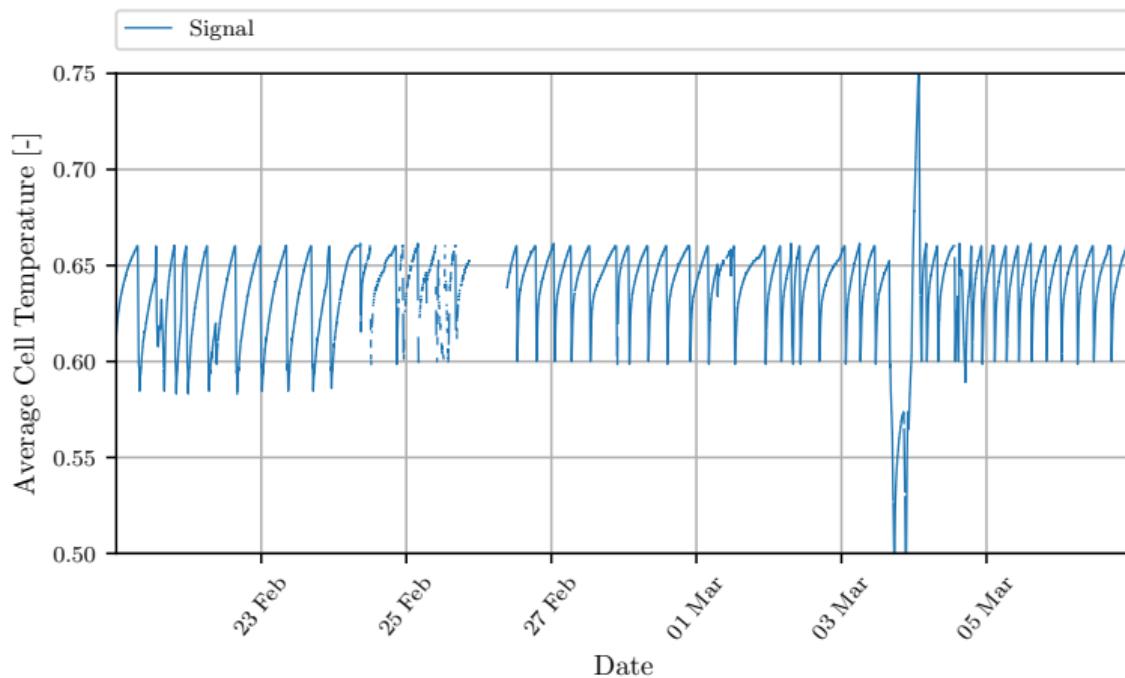
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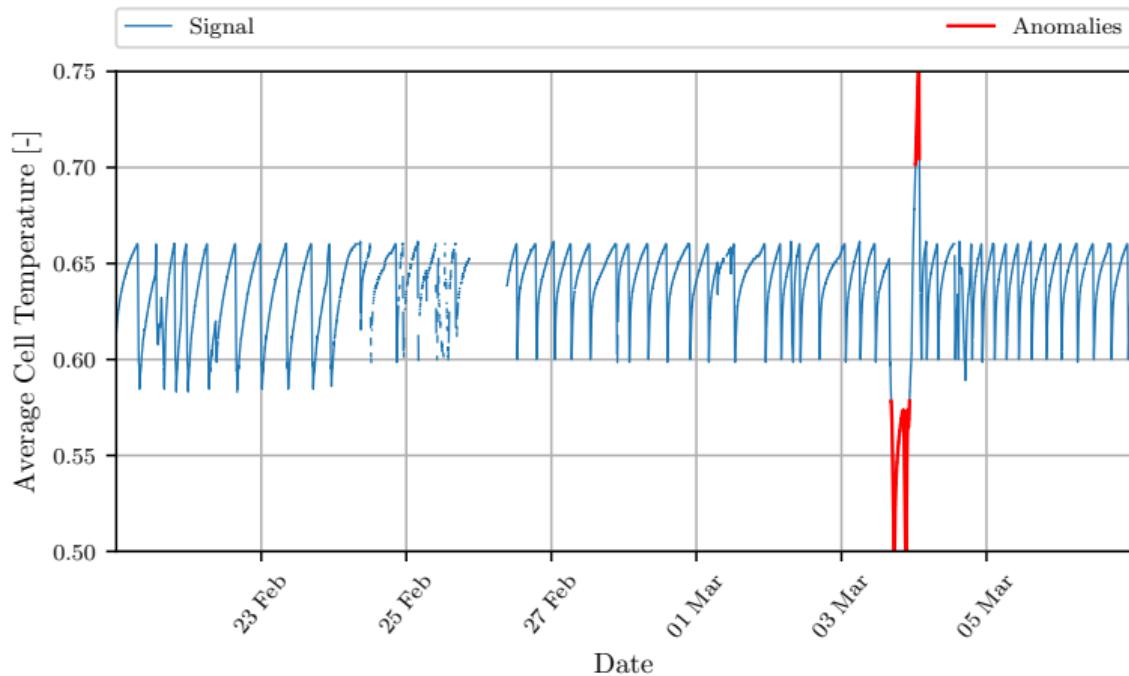


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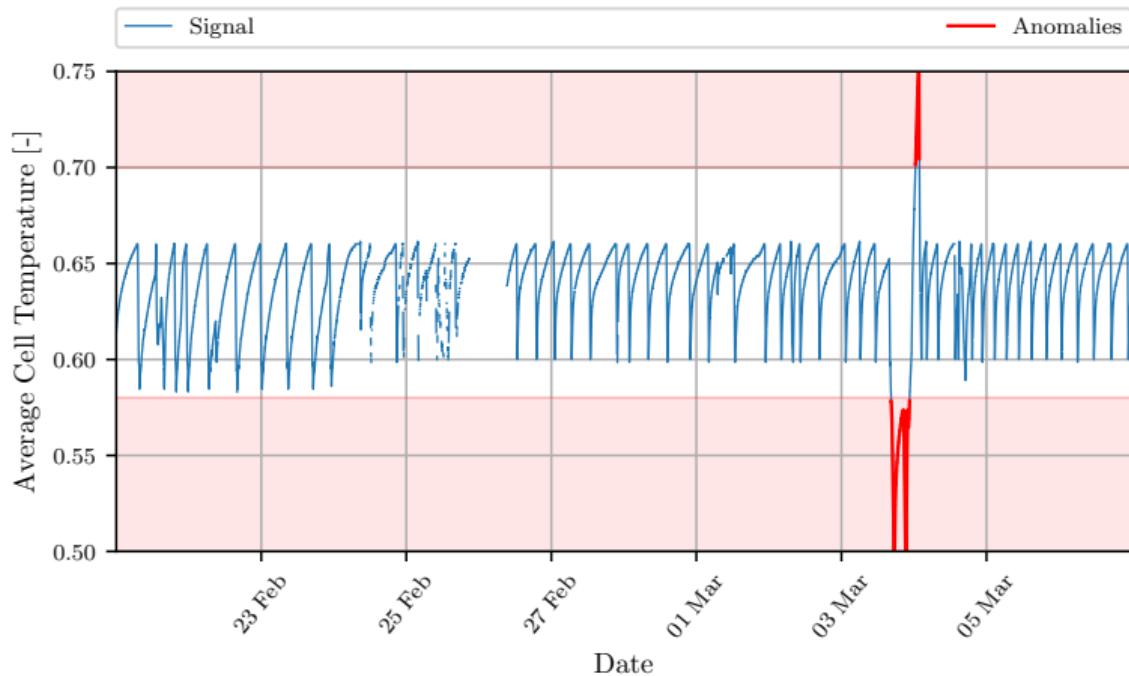
## Real World Data



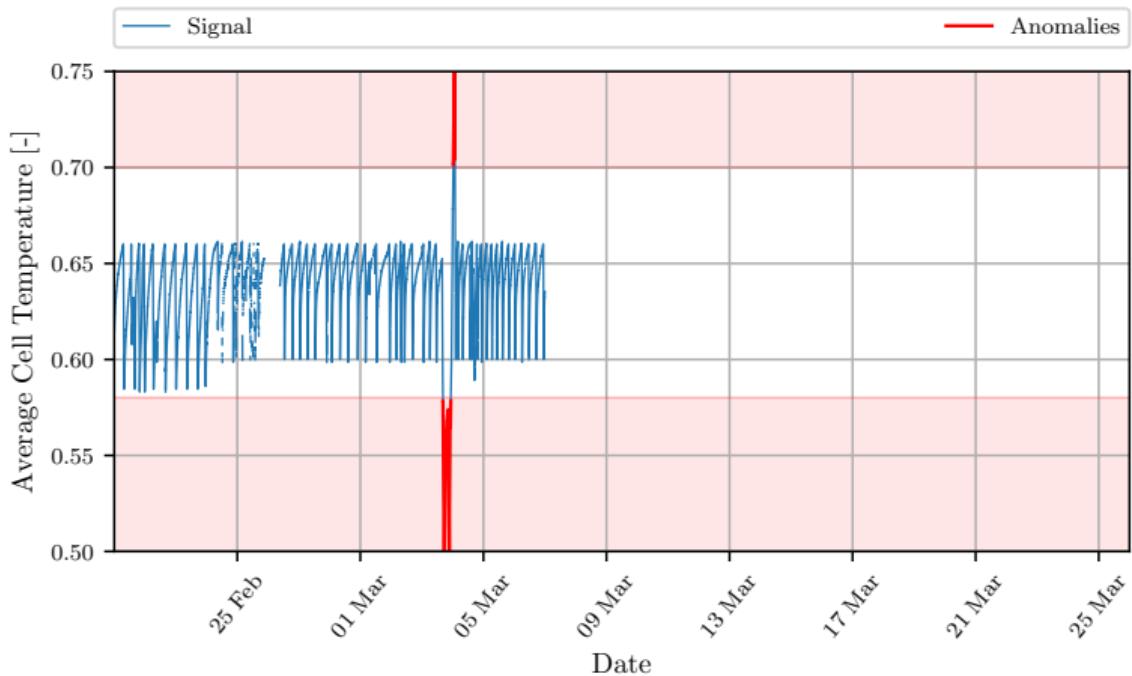
## Data with Outliers



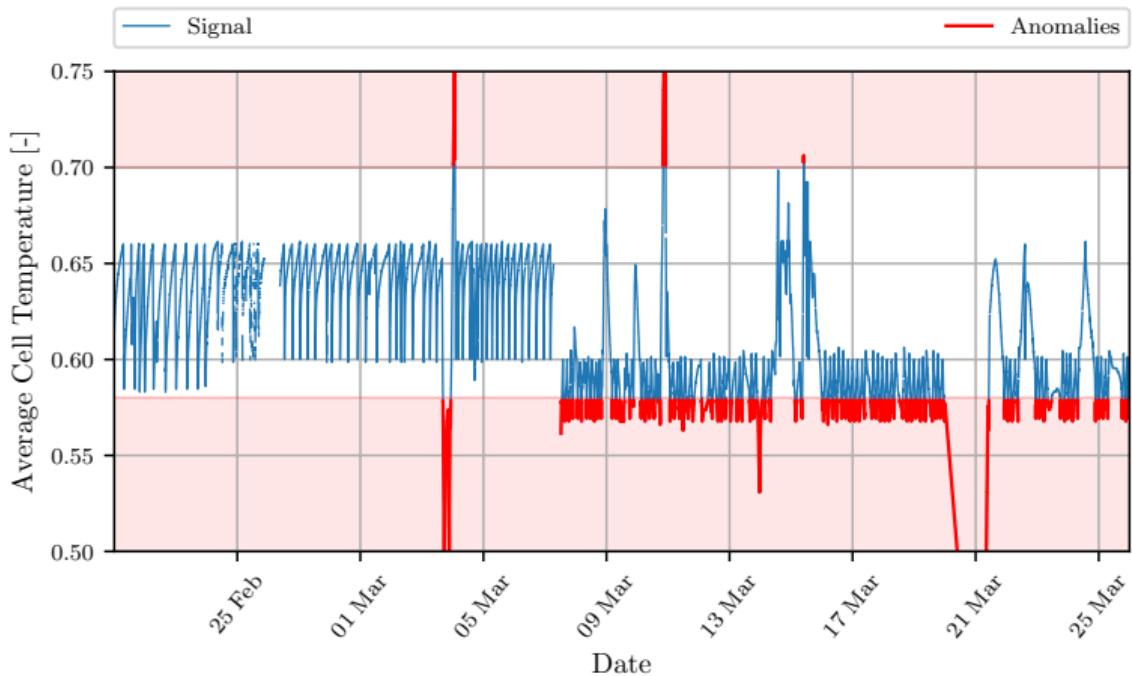
## Static Threshold Limits



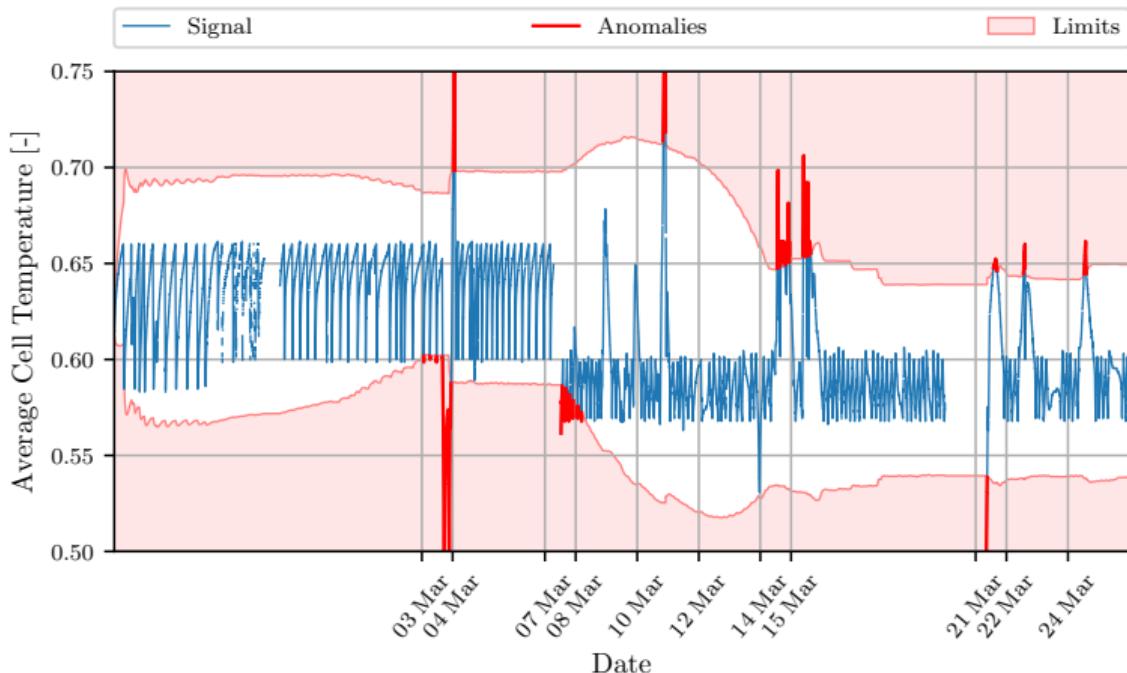
## Static Threshold Limits



# Comming Problem



# Control Engineering Meets Artificial Intelligence



# Goals

We need to design a detector that:

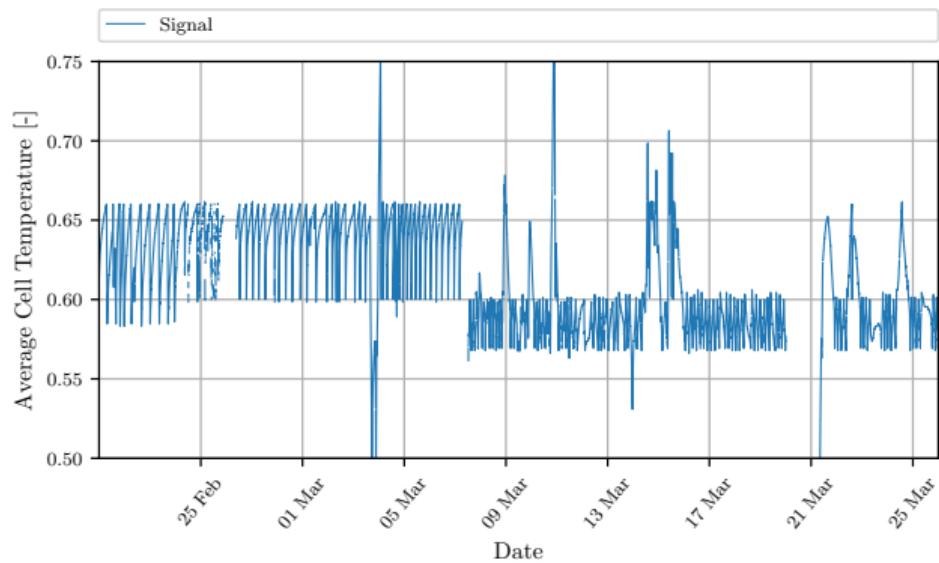
- does not require huge amount of data
- adapts to unseen operation
- provides conservative process limits
- operates with existing infrastructure

# Proposed Solution

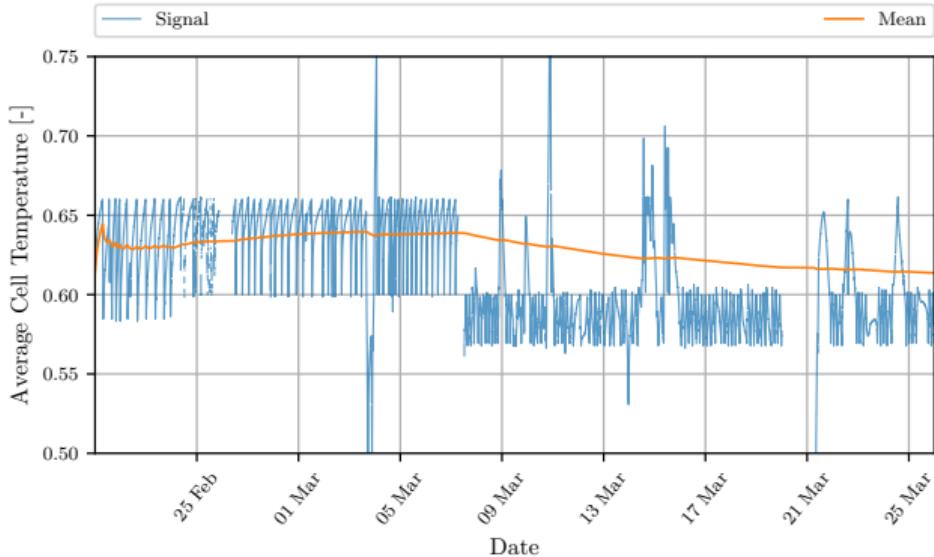
Real-Time Outlier Detection with Dynamic Process Limits combining:

- online learning
- invertible probabilistic model
- outlier detection
- self-supervised learning

## Real Operation Data

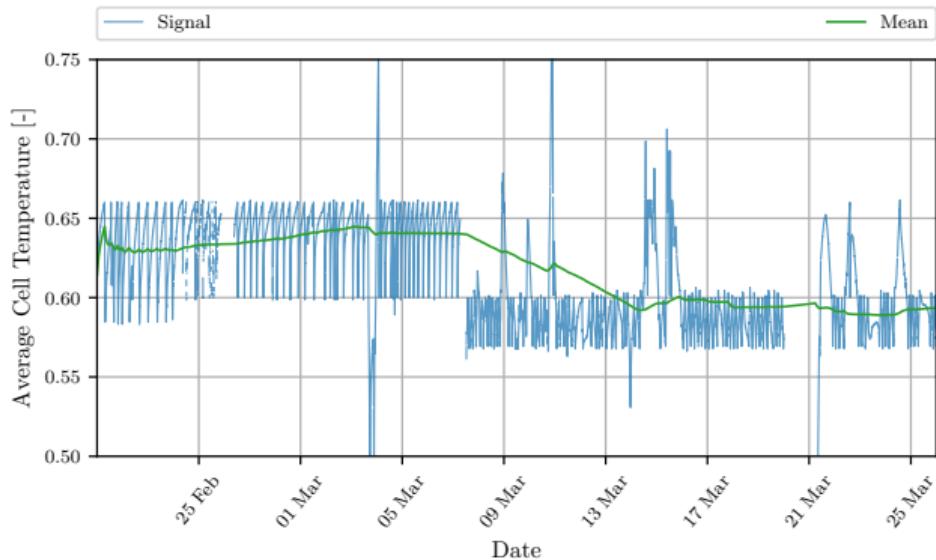


# Online Learning via Welford Algorithm



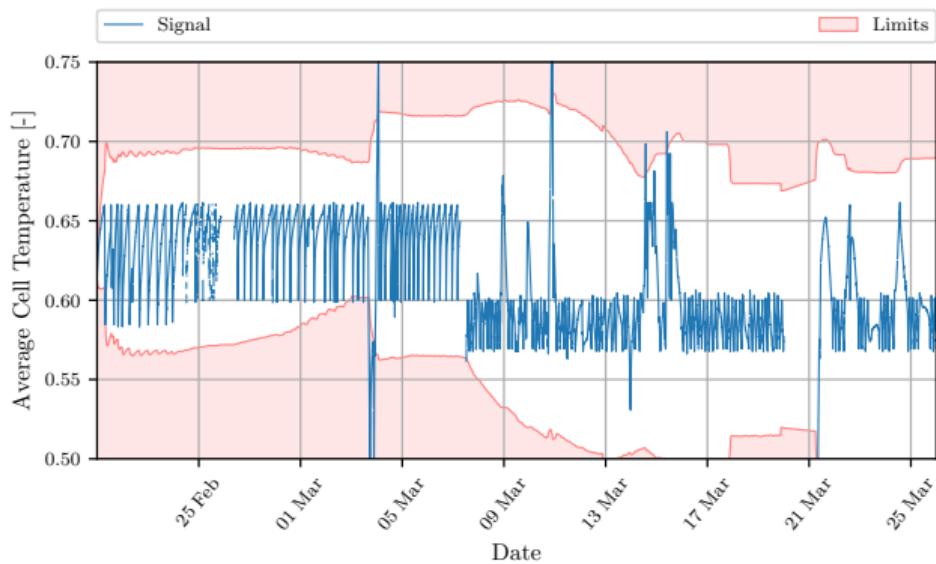
+ One-Pass Algorithm | - Adaptation Slows Down

# Online Learning via Invertible Welford Algorithm



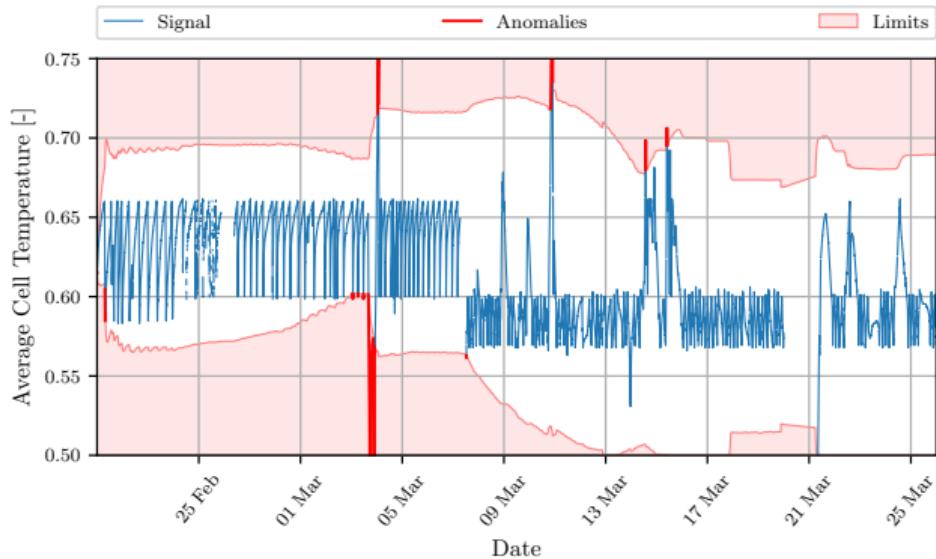
+ Constant Adaptation | - Memorizes Data Window

# Dynamic Threshold Limits via Inversion



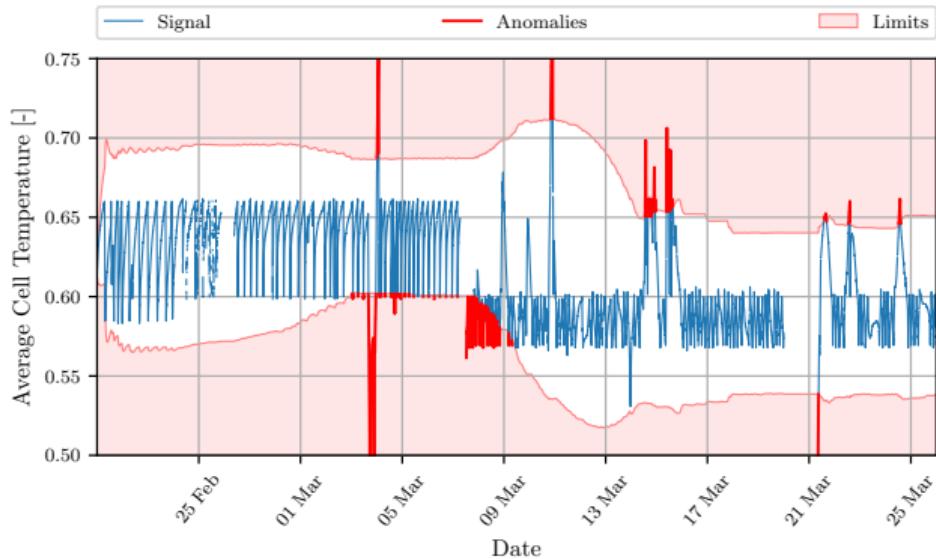
$$x_1 = F_X(1 - q; \bar{x}_n, s_n)^{-1}$$
$$x_u = F_X(q; \bar{x}_n, s_n)^{-1}$$

# Distance-based Outlier Detection



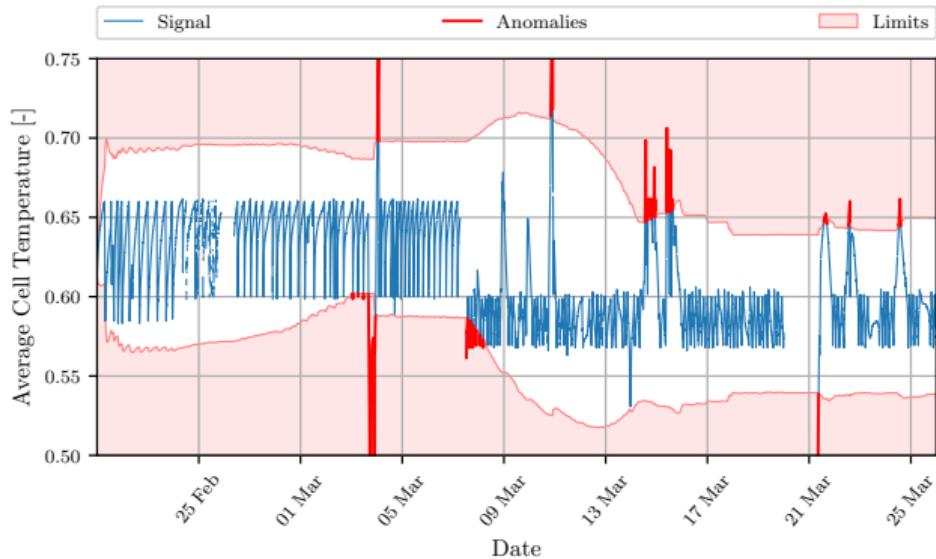
$$y_i = \begin{cases} 0 & \text{if } q \leq F_X(x_i; \bar{x}_n, s_n) \\ 1 & \text{if } q > F_X(x_i; \bar{x}_n, s_n) \end{cases}$$

# Self-Supervised Learning



$$y_i = \begin{cases} 0 & \text{if } q \leq F_X(x_i; \bar{x}_n, s_n) \\ 1 & \text{if } q > F_X(x_i; \bar{x}_n, s_n) \end{cases}$$

# Self-Supervised Learning

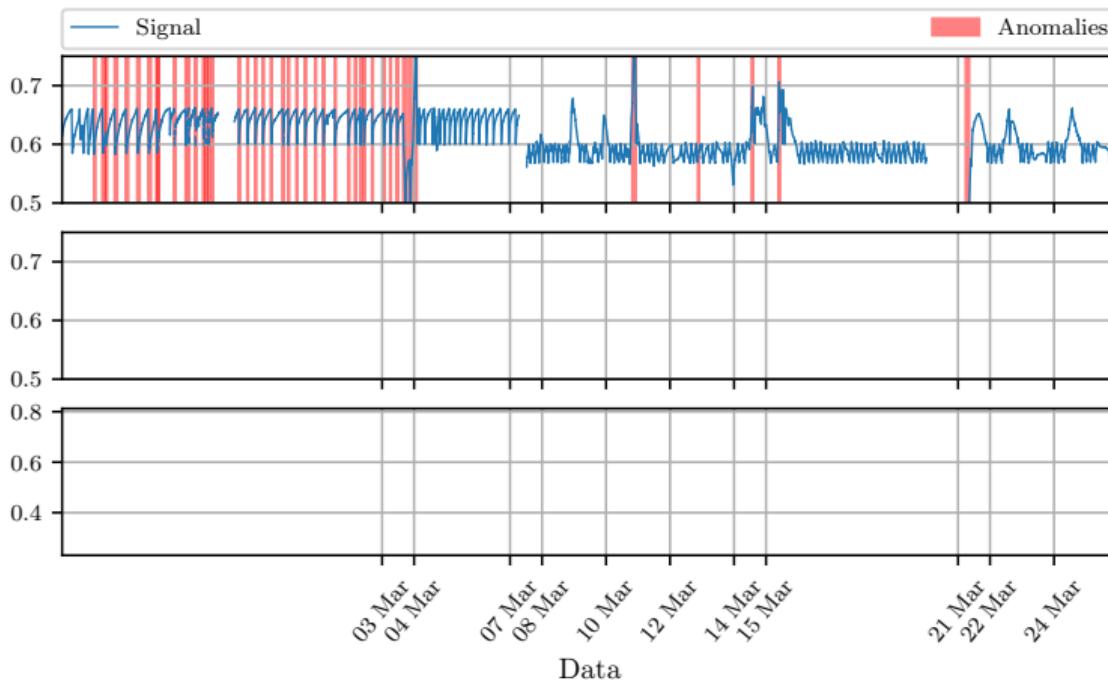


$$\frac{\sum_{y \in Y} y}{|Y|} > q$$

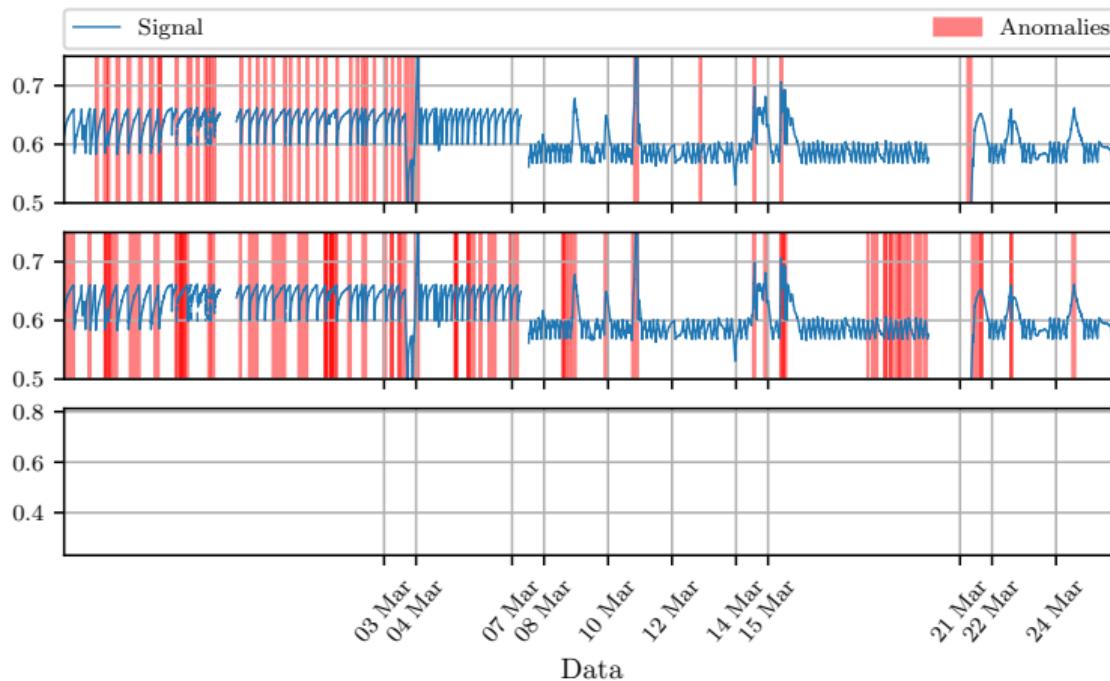
# Battery Energy Storage System - BESS



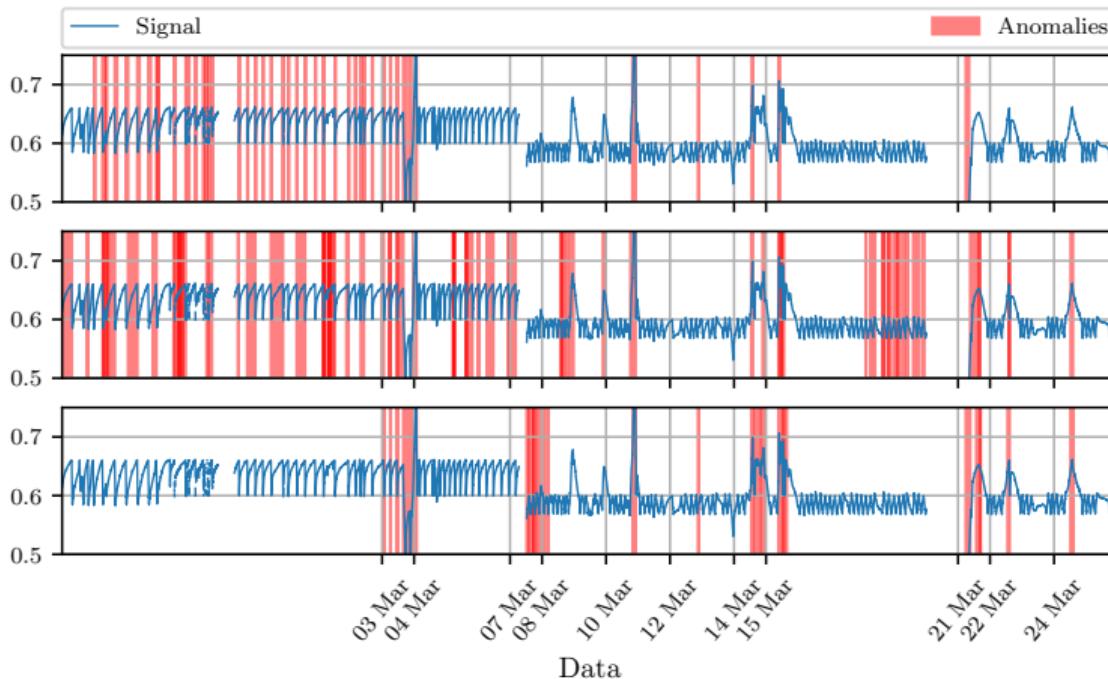
## Case Study - BESS



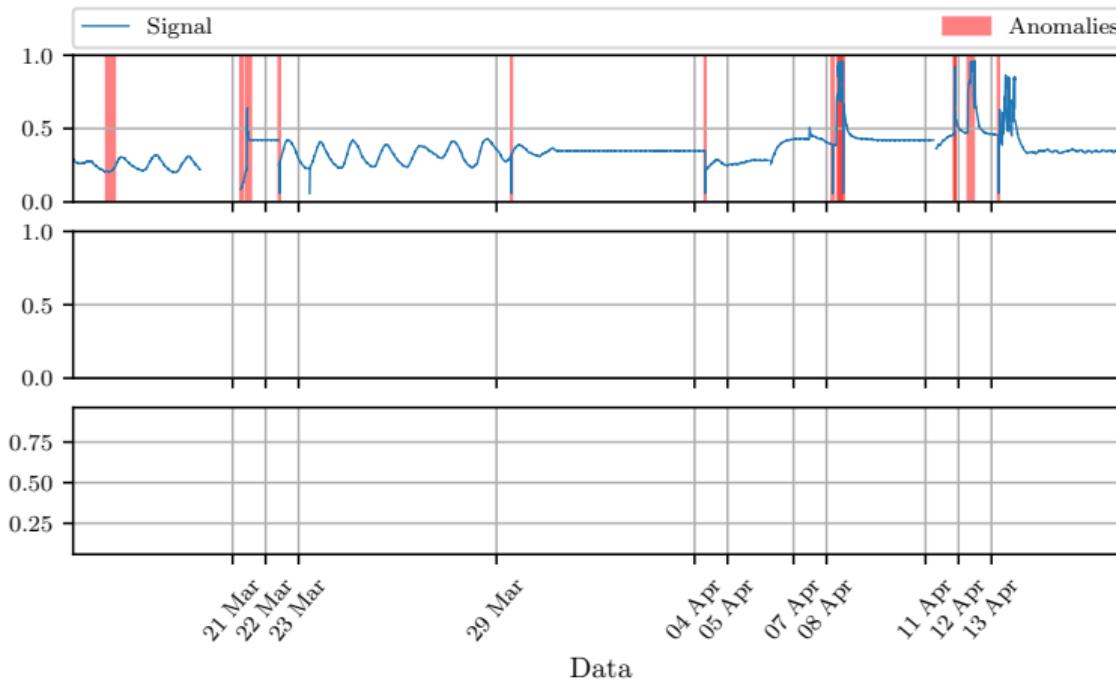
## Case Study - BESS



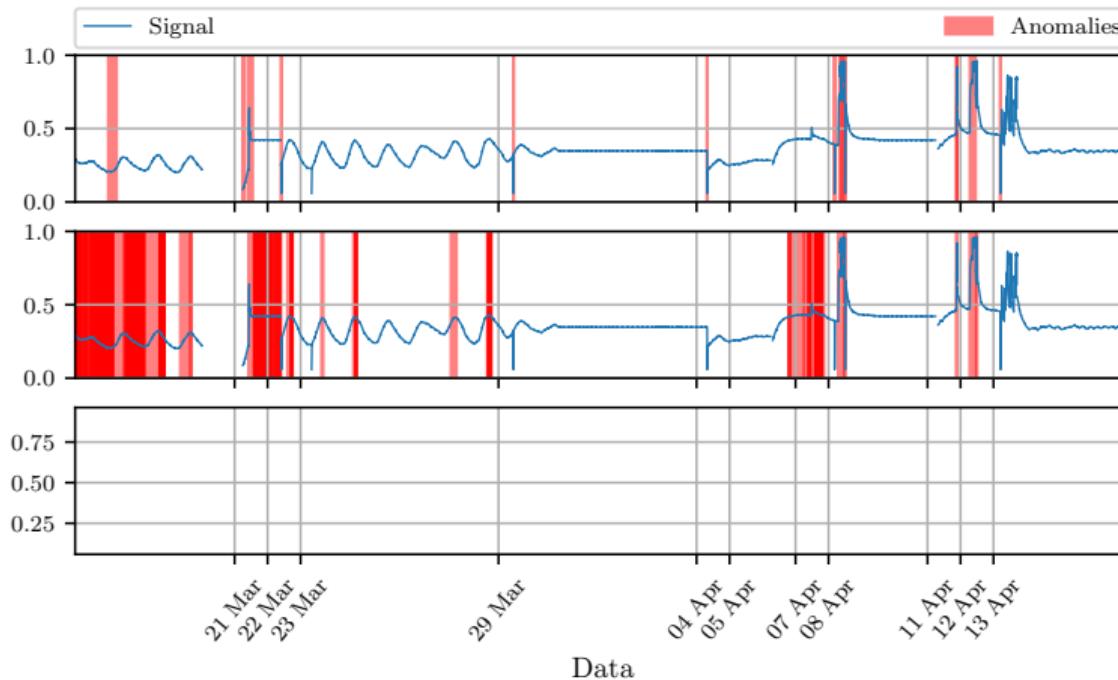
## Case Study - BESS



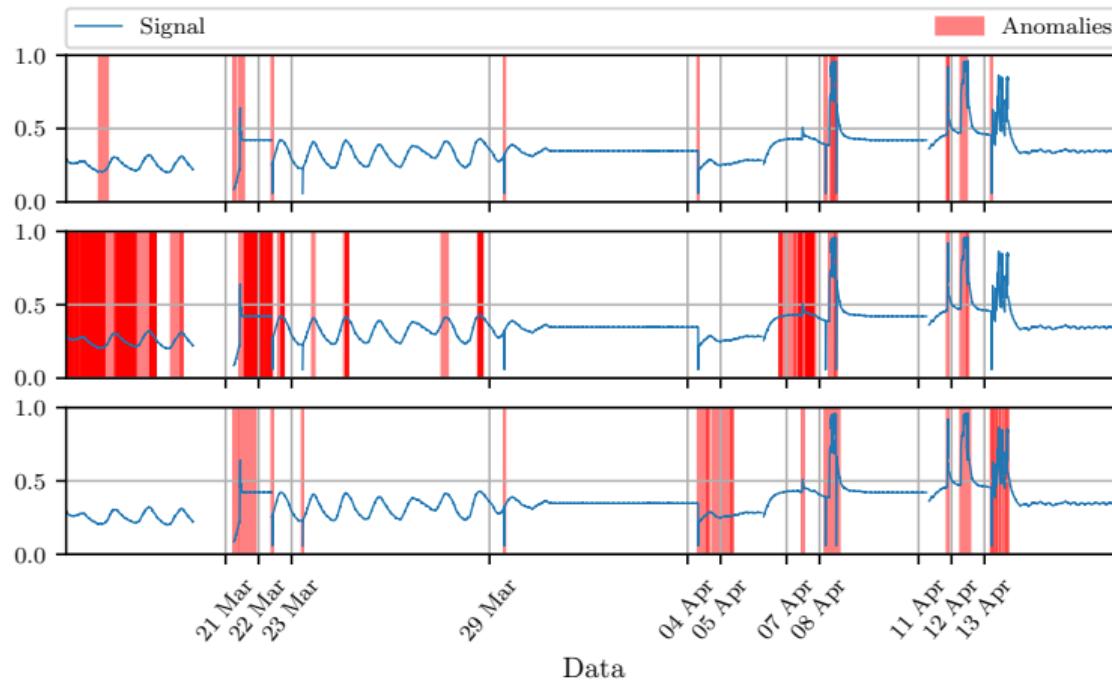
# Case Study - Inverter



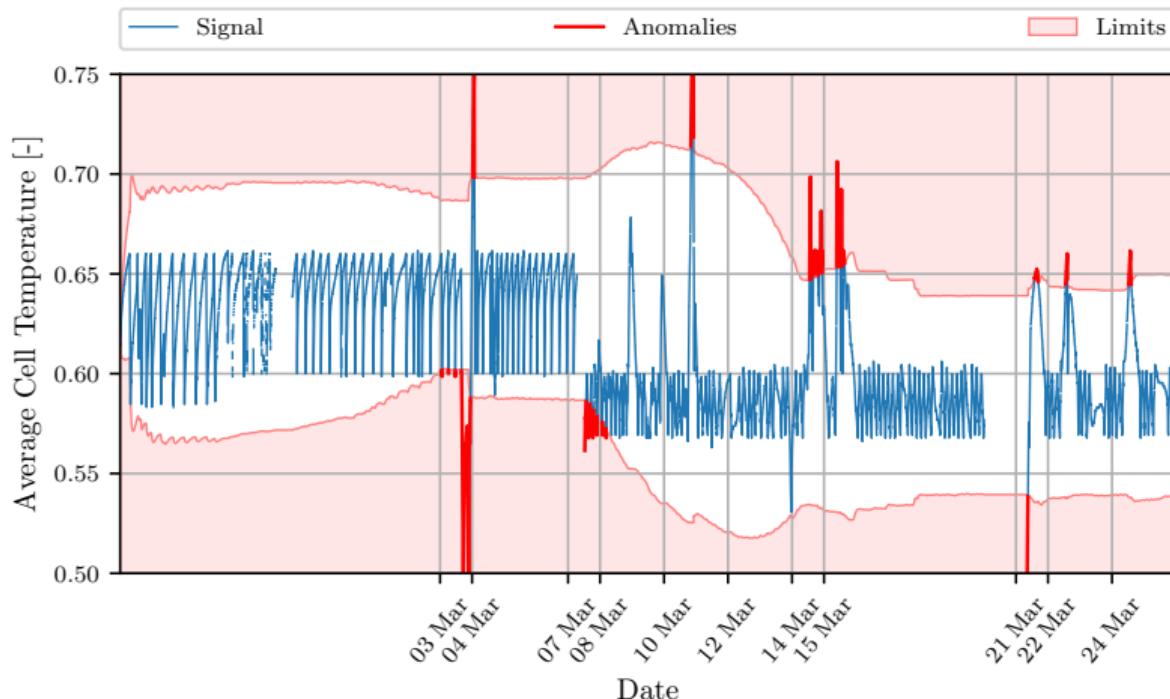
# Case Study - Inverter



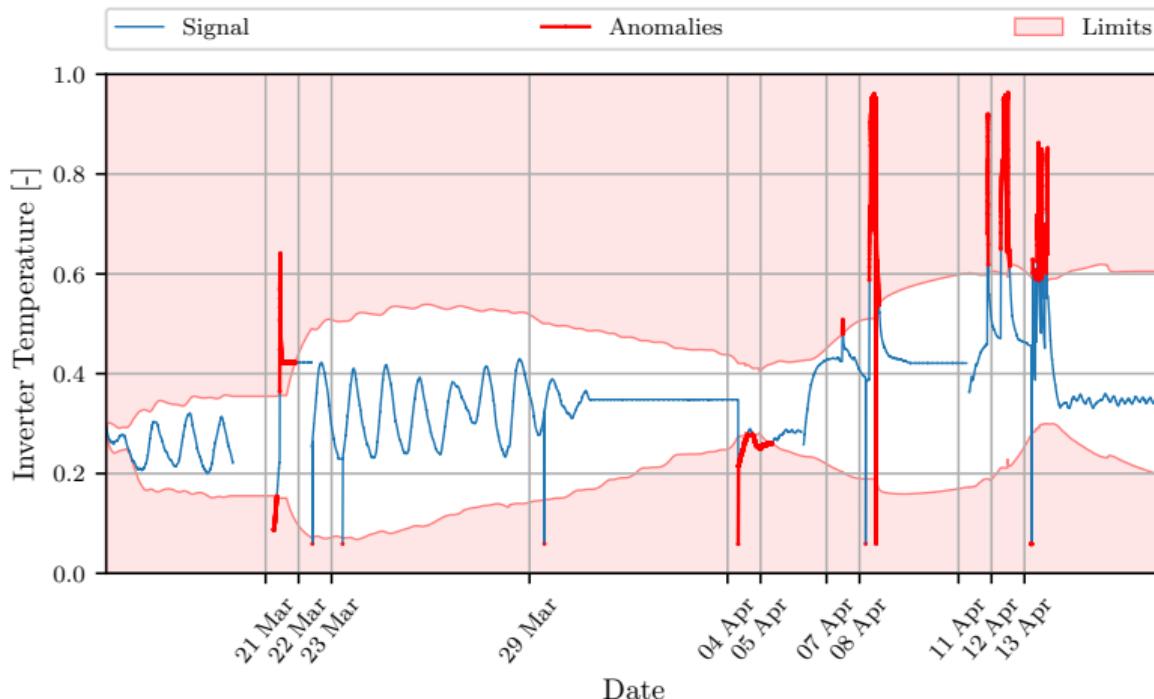
# Case Study - Inverter



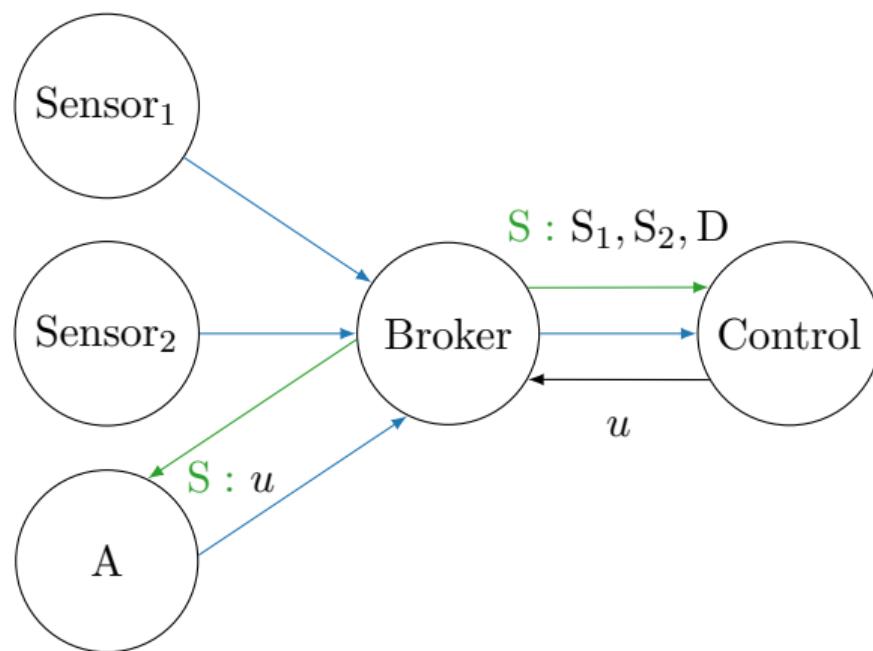
# Dynamic Process Limits - BESS



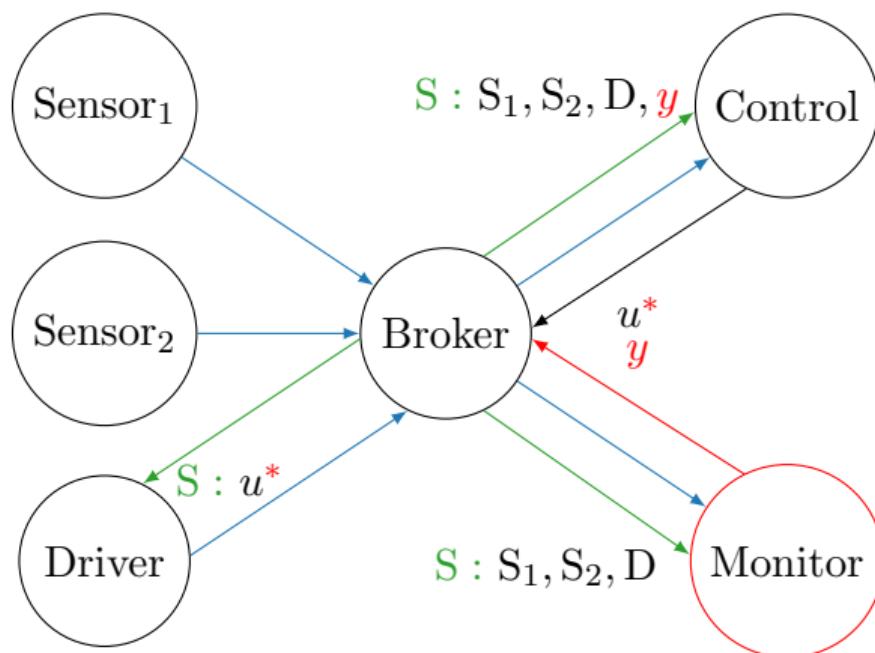
# Dynamic Process Limits - Inverter



# Utilize Existing Infrastructure

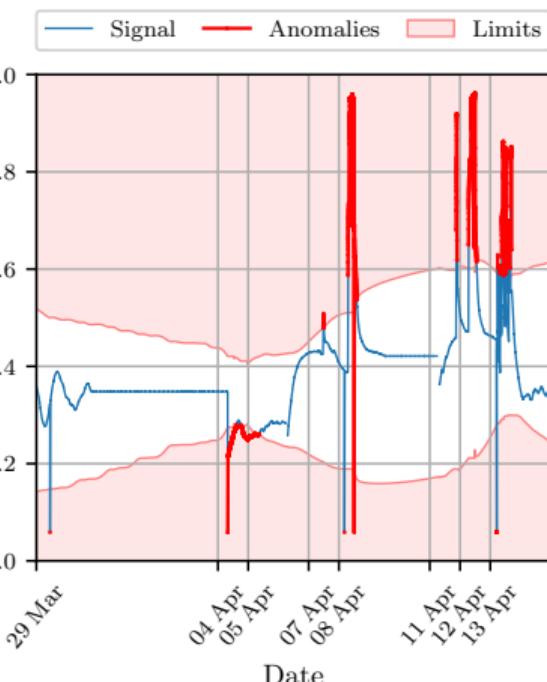


# Utilize Existing Infrastructure



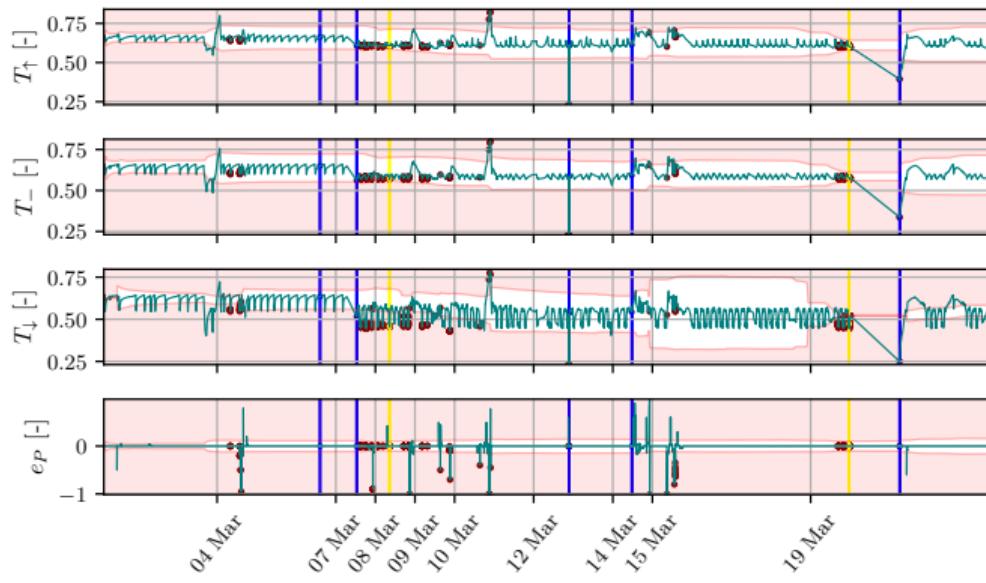
# Summary

- outlier detection on streamed data
- adaptation to external conditions
- online self-learning approach
- dynamic process limits for individual signals
- integration with existing IT infrastructure



Acknowledgements: APVV-20-0261. VEGA 1/0490/23. Horizon Europe under the grant no. 101079342.

# Follow-up research



1

<sup>1</sup> M. Wadinger and M. Kvasnica. Adaptable and interpretable framework for novelty detection in real-time iot systems. In Proceedings of the 62nd IEEE CDC, Singapore, 2023. under review.

## Process Time Evaluation

Evaluation Time [ $\mu$ s]	BESS		Inverter	
	average	max	average	max
Half-Space Trees	218±198	10129	216±196	11281
One-Class SVM	8± 7	1233	9± 9	1711
Proposed	57± 55	9431	60± 75	12330

# Online Anomaly Detection Workflow

**Input:** expiration period  $t_e$ , time constant  $t_c$

**Output:** score  $y_i$ , threshold  $x_{q,i}$

*Initialisation :*

- 1:  $i \leftarrow 1; n \leftarrow 1; q \leftarrow 0.9973; \bar{x} \leftarrow x_0; s^2 \leftarrow 1;$
- 2: compute  $F_X(x_0)$  ;

*LOOP Process*

3: **loop**

4:    $x_i \leftarrow \text{RECEIVE}();$

5:    $y_i \leftarrow \text{PREDICT}(x_i) ;$

6:    $x_{q,i} \leftarrow \text{GET}(q, \bar{x}, s^2);$

7:   **if** (1a) **or** (3) **then**

8:      $\bar{x}, s^2 \leftarrow \text{UPDATE}(x_i, \bar{x}, s^2, n);$

9:      $n \leftarrow n + 1;$

10:    **for**  $x_{i-t_e}$  **do**

11:       $\bar{x}, s^2 \leftarrow \text{REVERT}(x_{i-t_e}, \bar{x}, s^2, n);$

12:       $n \leftarrow n - 1;$

13:    **end for**

14:   **end if**

15:    $i \leftarrow i + 1;$

16: **end loop**