

# Real-Time Outlier Detection with Dynamic Process Limits

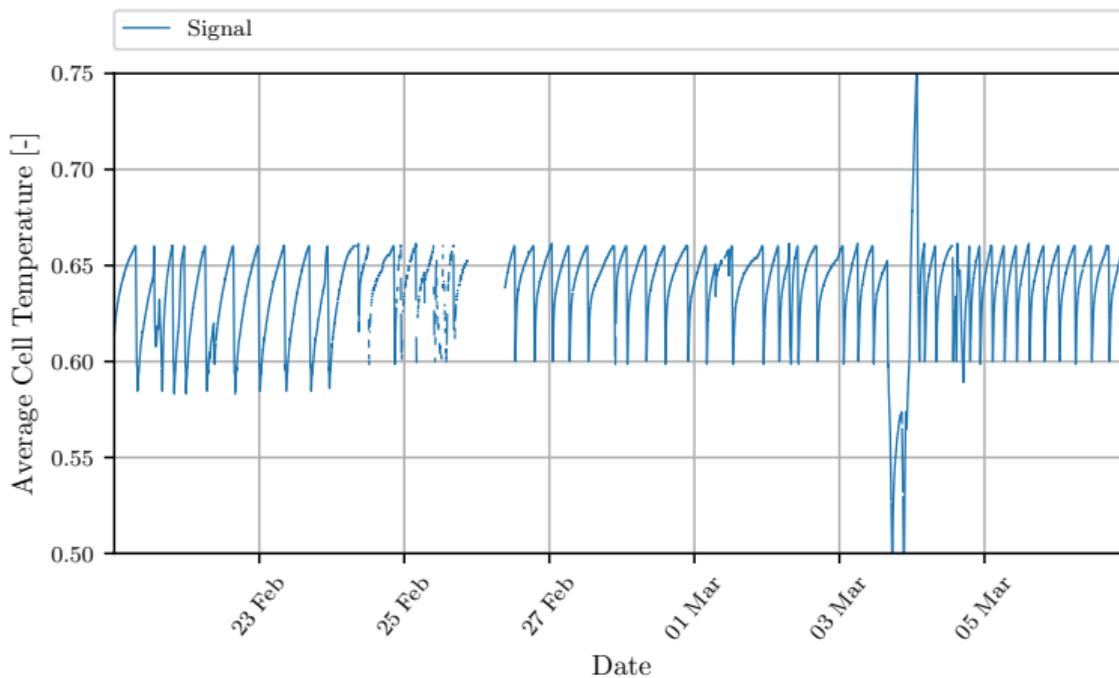
## Process Control 2023

**Marek Wadinger**, Michal Kvasnica

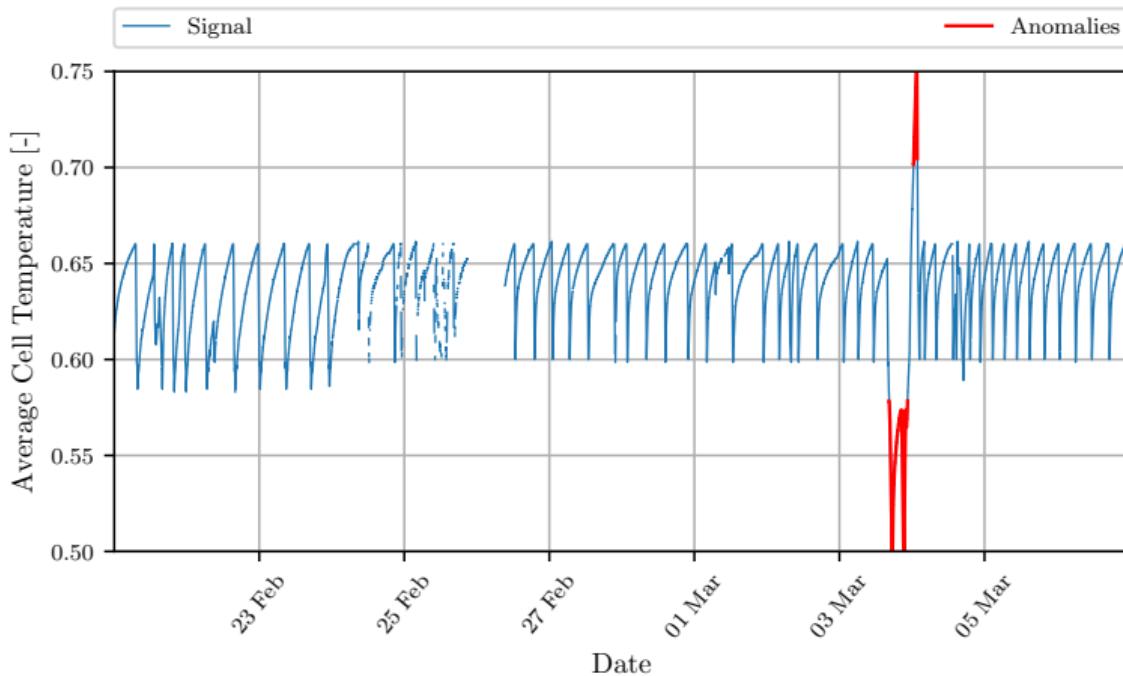
Institute of Information Engineering, Automation, and Mathematics  
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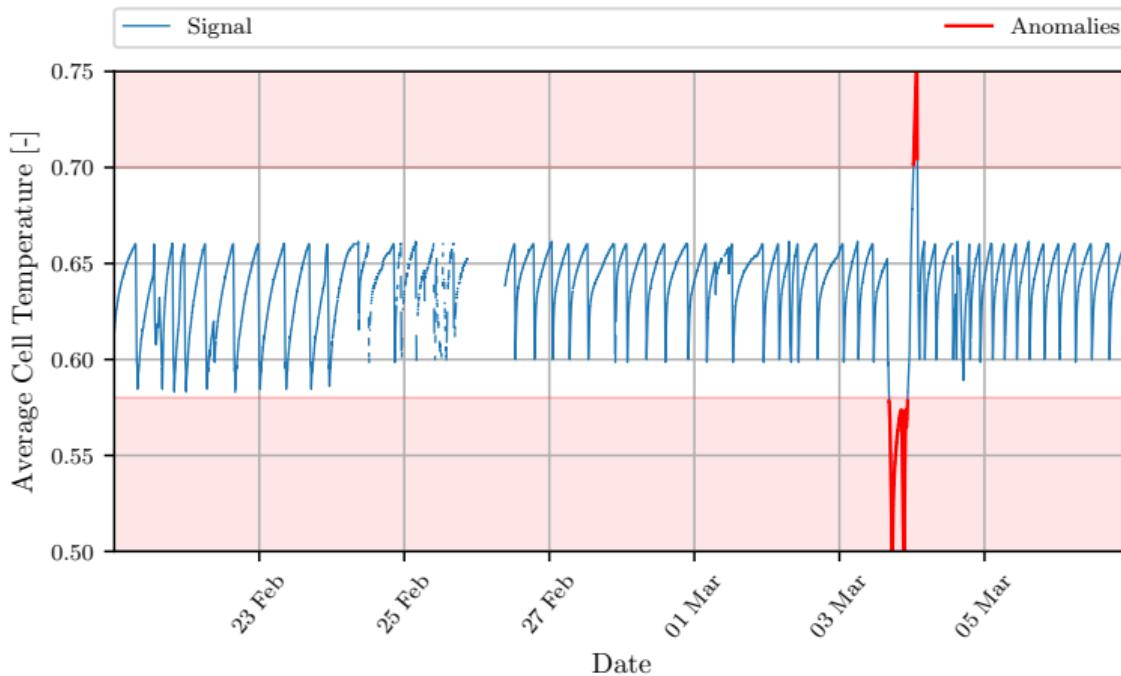
# Real World Data



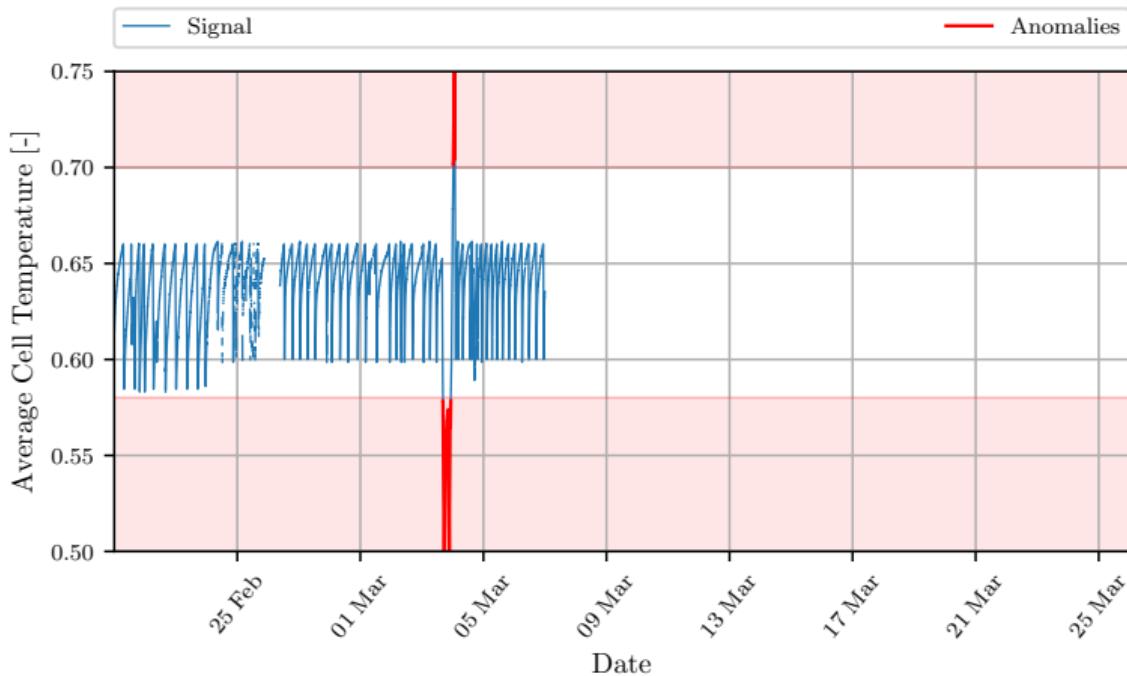
## Data with Outliers



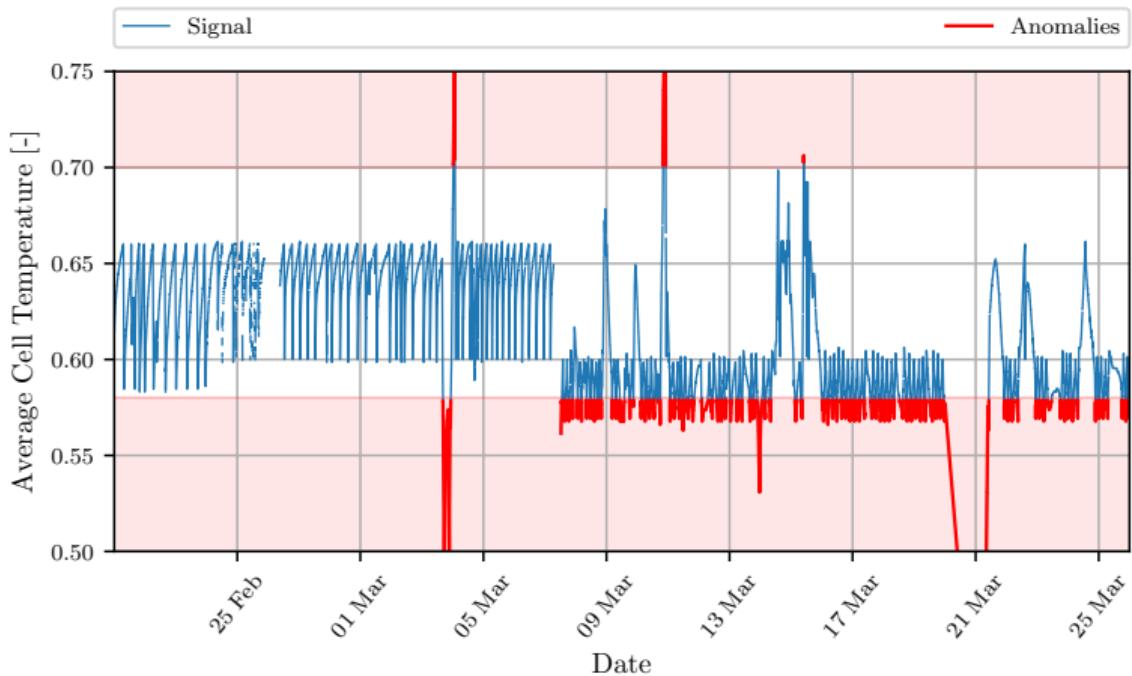
# Static Threshold Limits



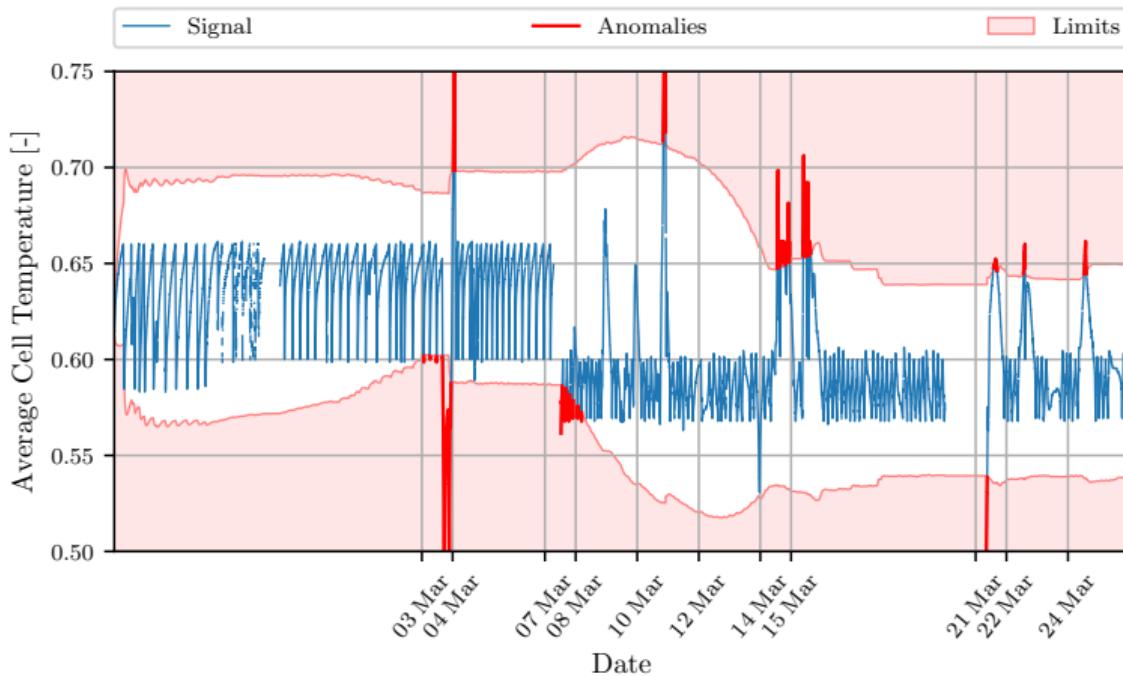
# Static Threshold Limits



# Comming Problem



# Control Engineering Meets Artificial Intelligence



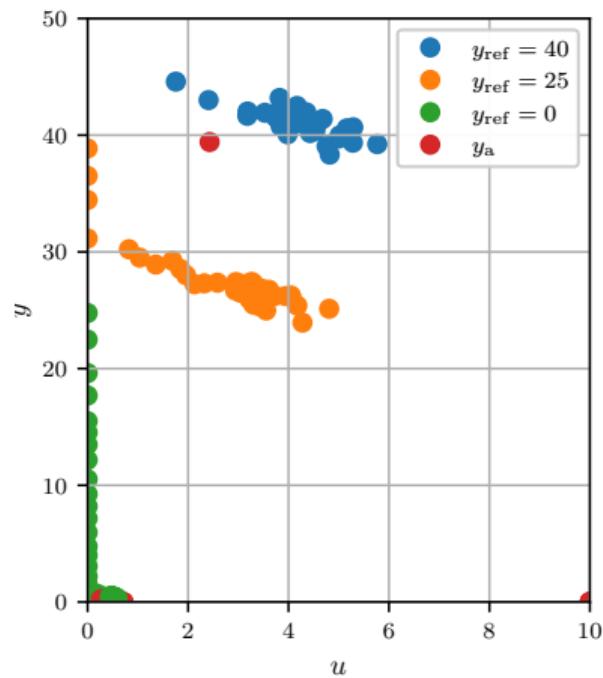
# Goals

We need to design a data-driven outlier detector that:

- adapts to unseen operation regime
- provides conservative dynamic process limits
- operates with existing infrastructure

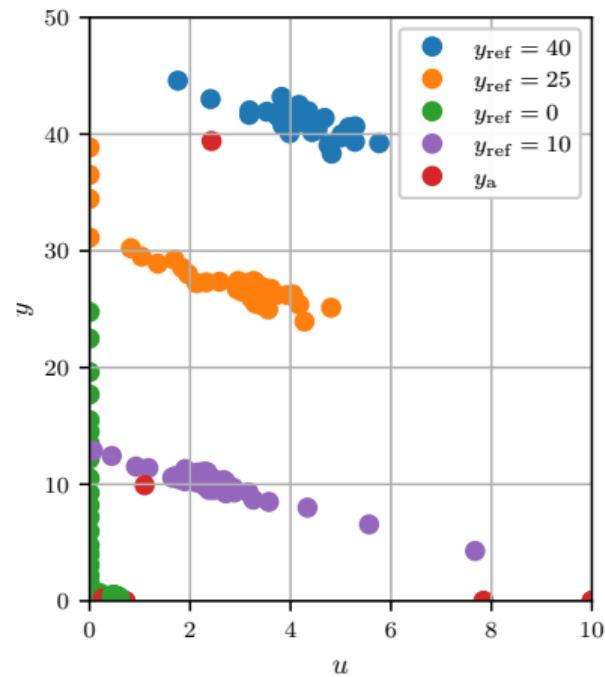
# Limitations of Data-driven Outlier Detection

- need for training data



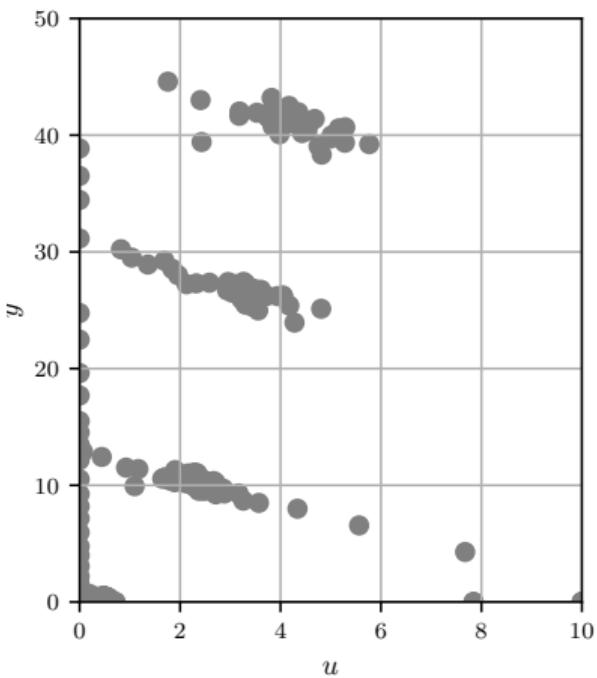
# Limitations of Data-driven Outlier Detection

- need for training data
- changes in operation regime



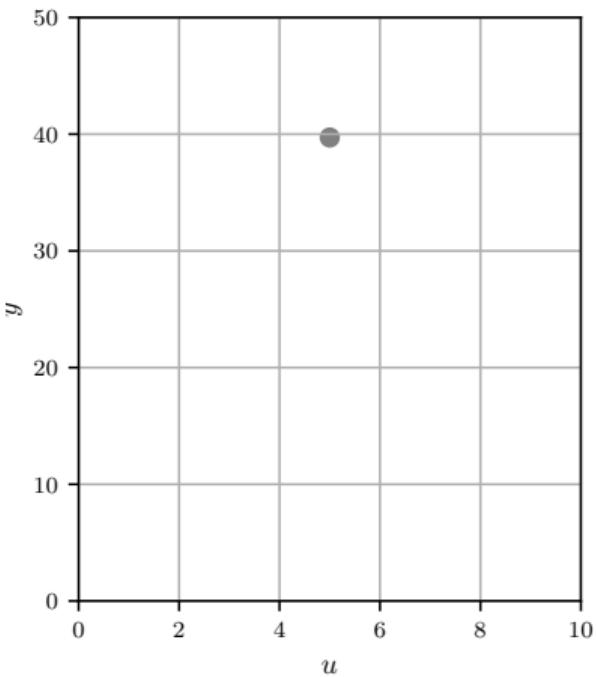
# Limitations of Data-driven Outlier Detection

- need for training data
- changes in operation regime
- unavailability of labels



# Limitations of Data-driven Outlier Detection

- need for training data
- changes in operation regime
- unavailability of labels
- no storage of historical data

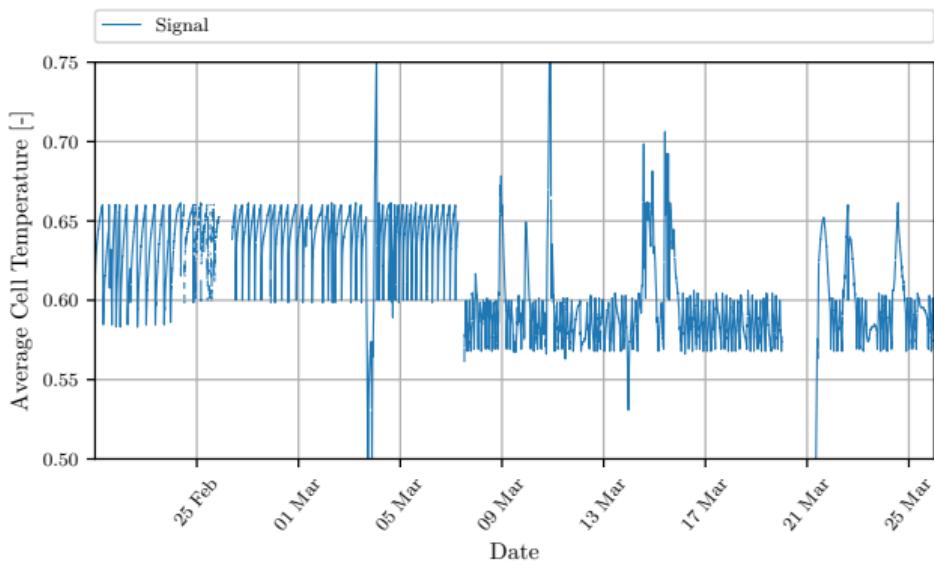


# Proposed Solution

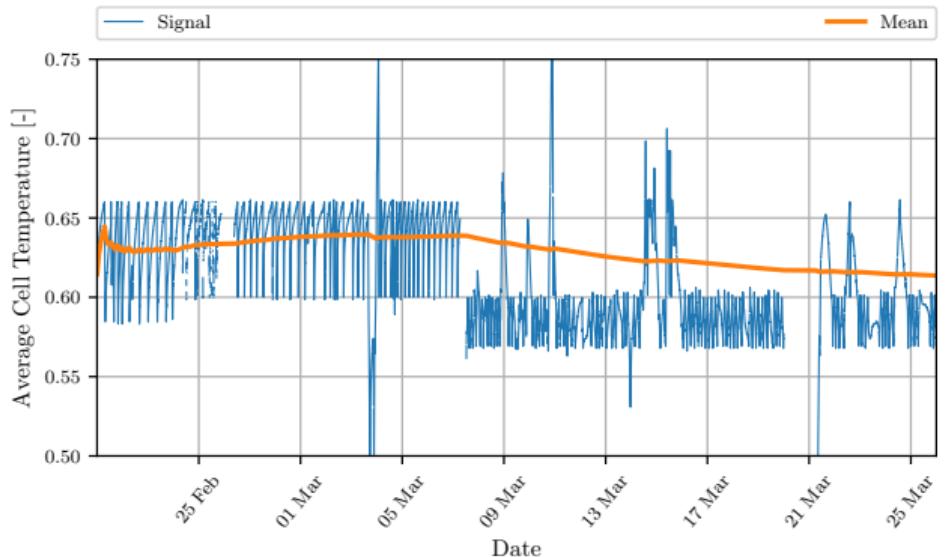
Real-Time Outlier Detection with Dynamic Process Limits combining:

- online learning
- invertible probabilistic model
- outlier detection
- self-supervised learning

# Real Operation Data

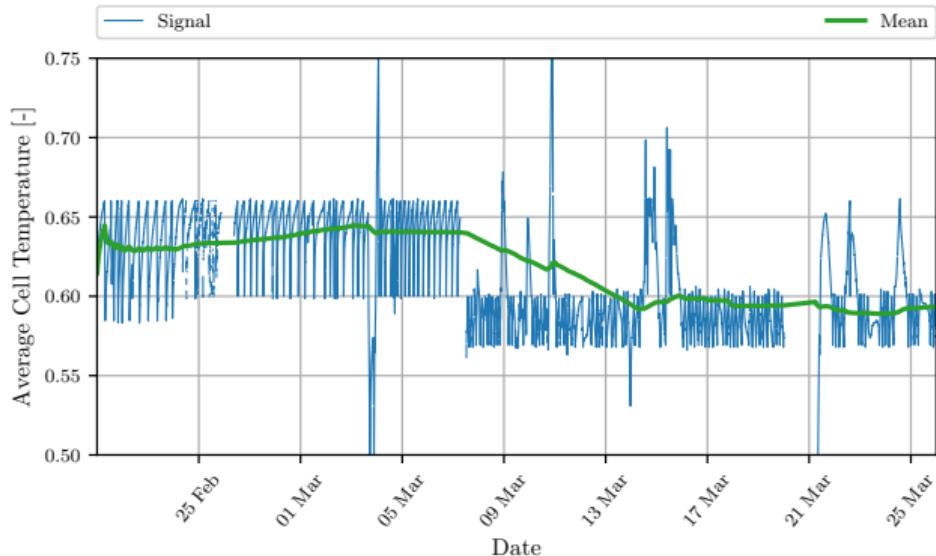


# Online Learning via Welford Algorithm



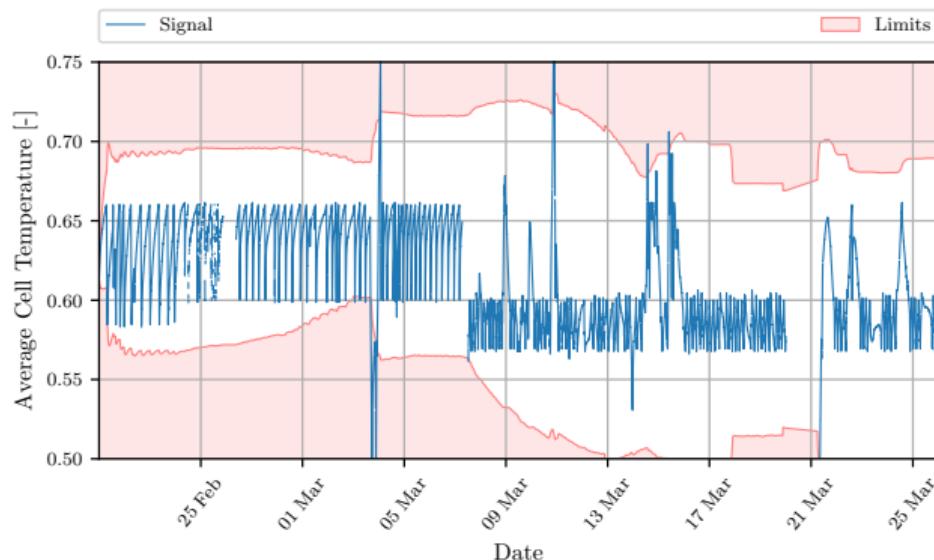
+ One-Pass Algorithm | - Adaptation Slows Down

# Online Learning via Invertible Welford Algorithm



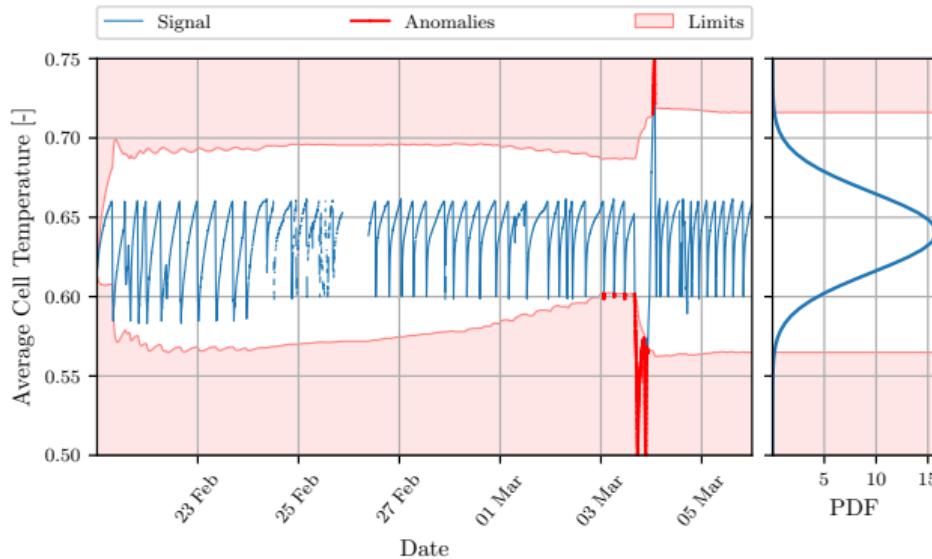
+ Constant Adaptation | - Memorizes Data Window

# Dynamic Threshold Limits via Inversion



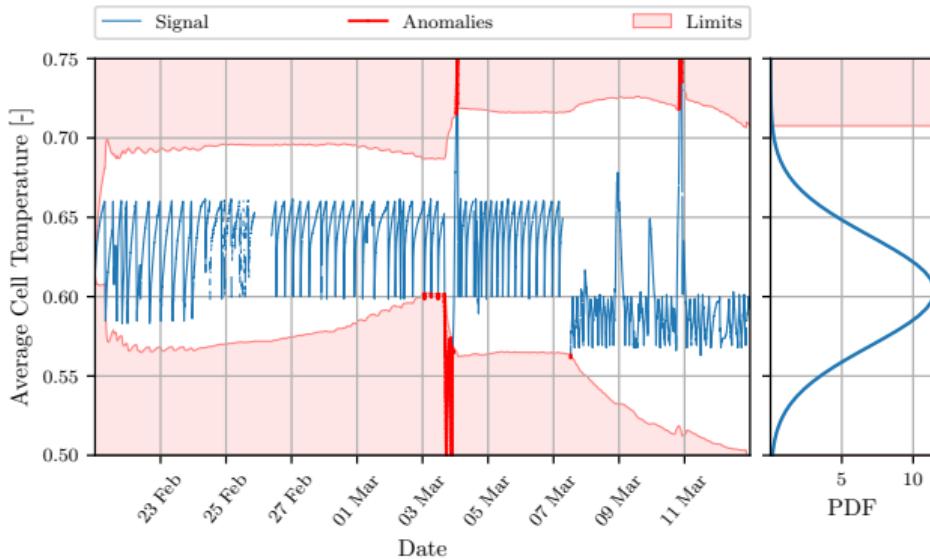
$$\begin{aligned}x_u &= F_X(q; \bar{x}_n, s_n)^{-1} \\x_l &= F_X(1 - q; \bar{x}_n, s_n)^{-1}\end{aligned}$$

# Distance-based Outlier Detection



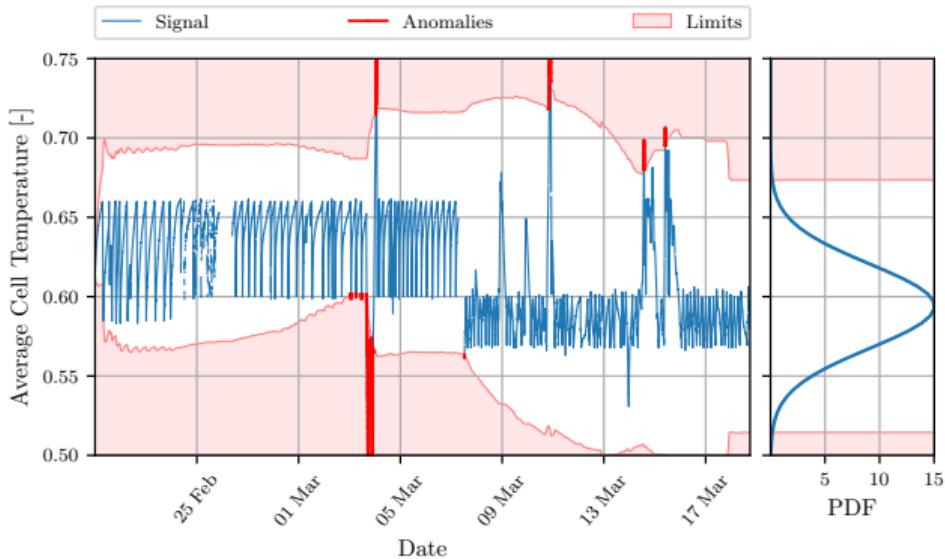
$$y_i = \begin{cases} 0 & \text{if } q \leq F_X(x_i; \bar{x}_n, s_n) \\ 1 & \text{if } q > F_X(x_i; \bar{x}_n, s_n) \end{cases}$$

# Distance-based Outlier Detection



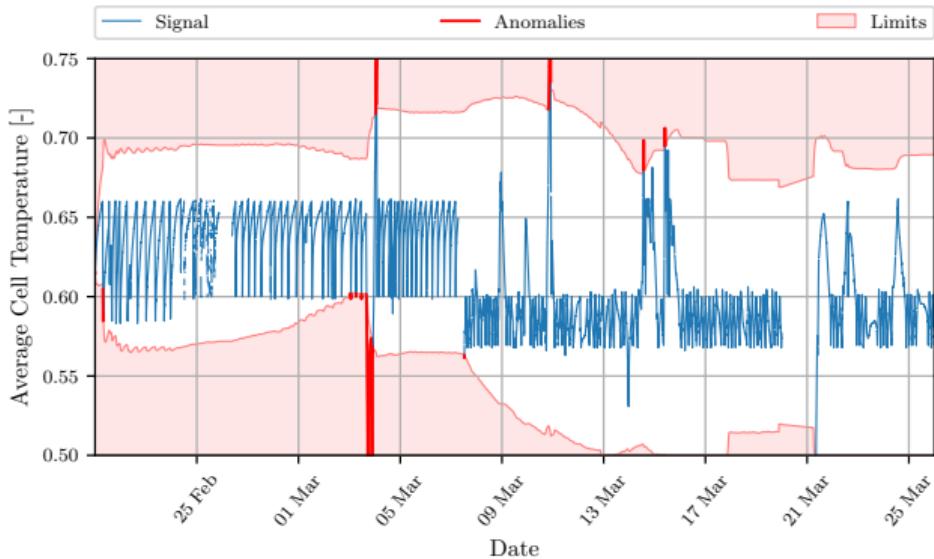
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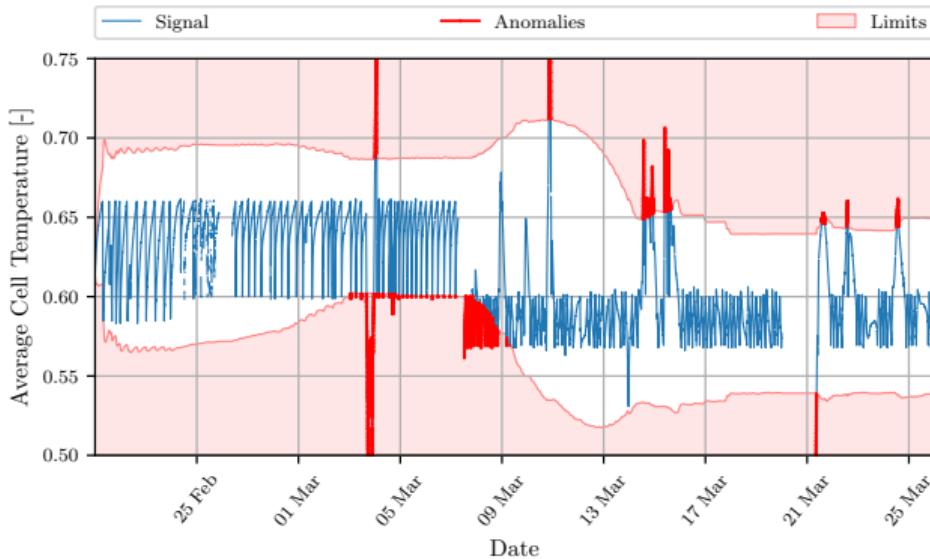
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# Distance-based Outlier Detection



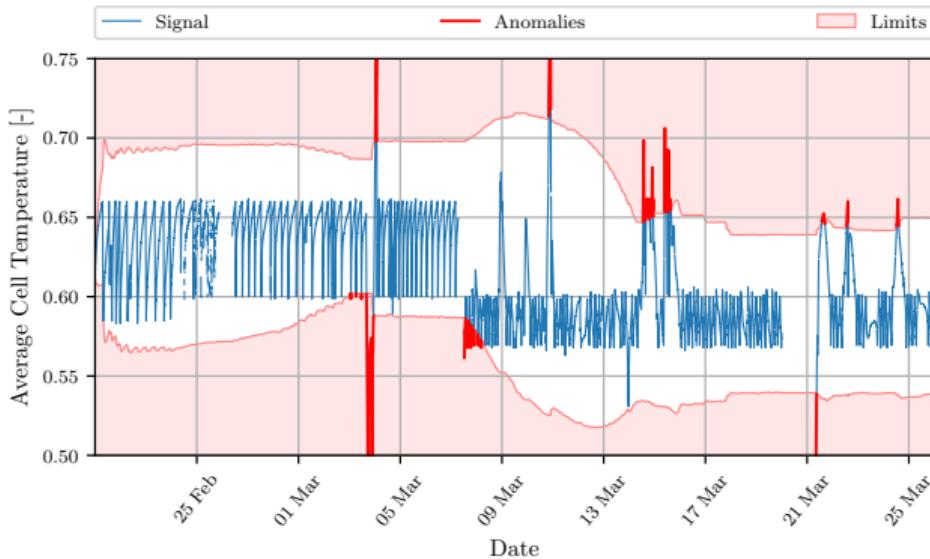
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# Self-Supervised Learning



$$y_i = \begin{cases} 0 & \text{if } q \leq F_X(x_i; \bar{x}_n, s_n) \\ 1 & \text{if } q > F_X(x_i; \bar{x}_n, s_n) \end{cases}$$

# Self-Supervised Learning – Faster Adaptation

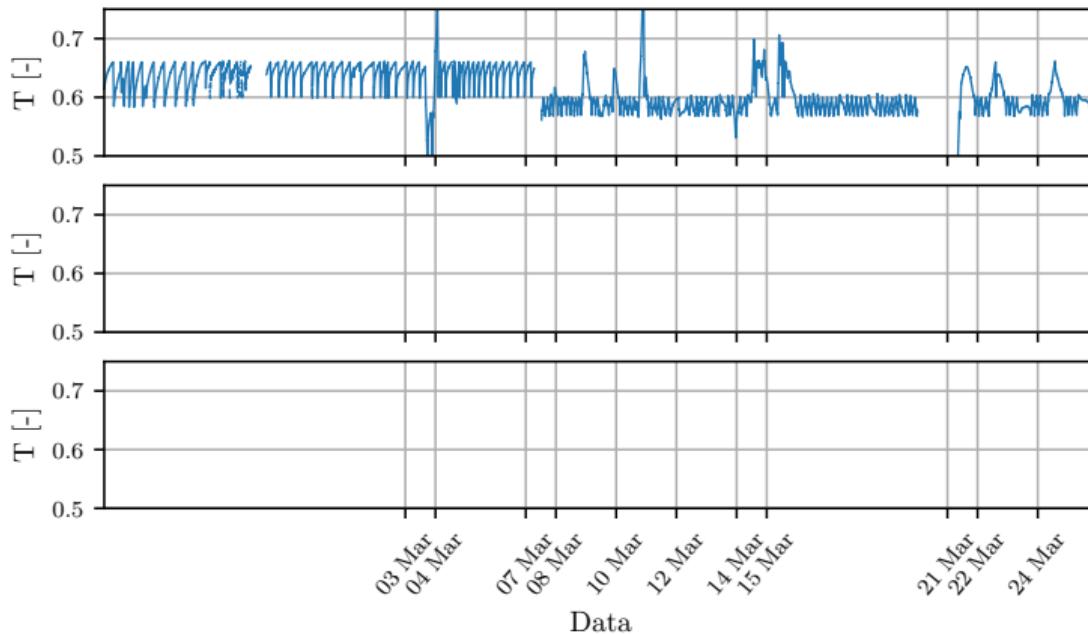


$$\frac{\sum_{y \in Y} y}{|Y|} > q$$

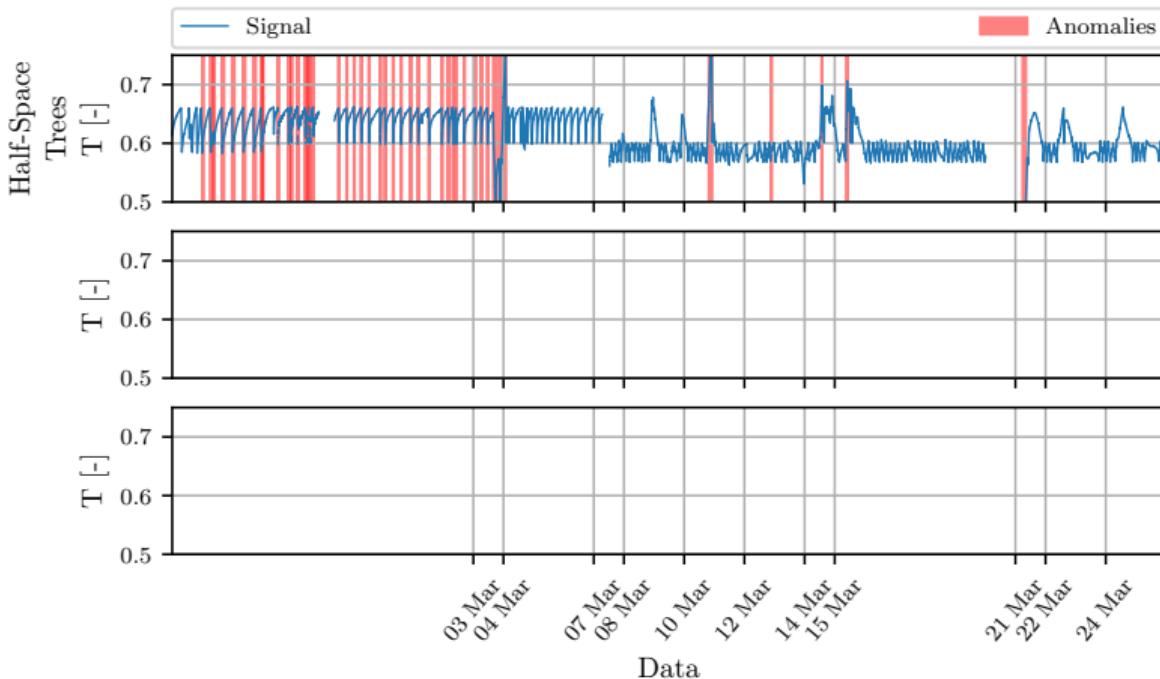
# Battery Energy Storage System – BESS



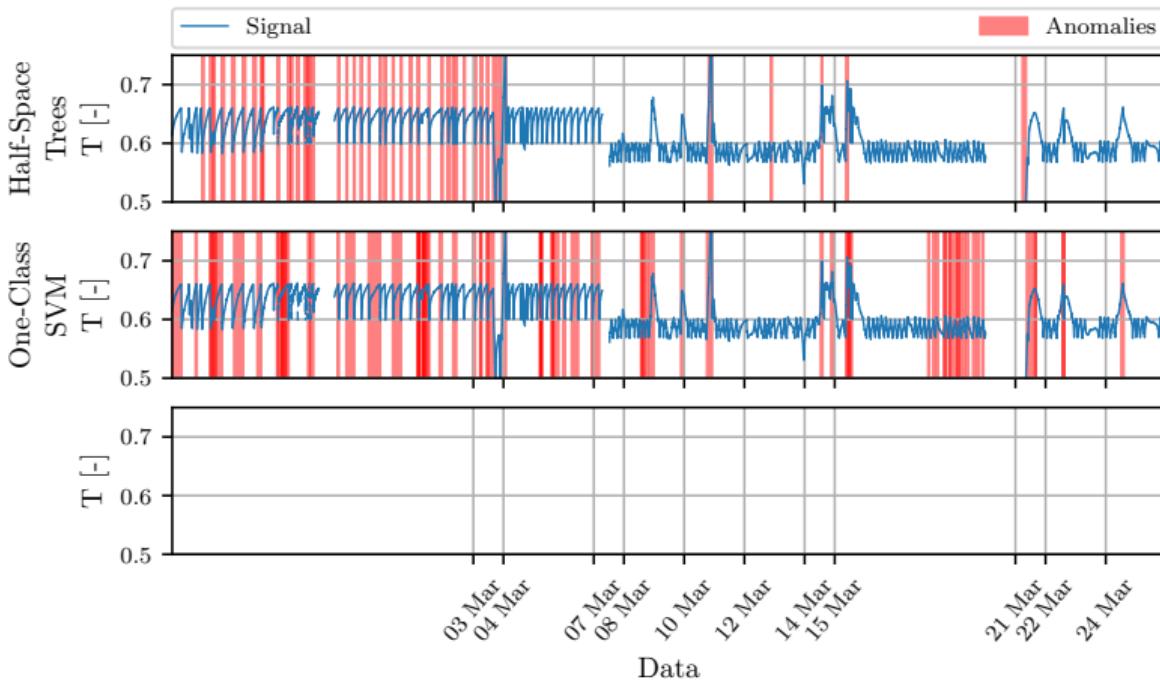
## Case Study – BESS



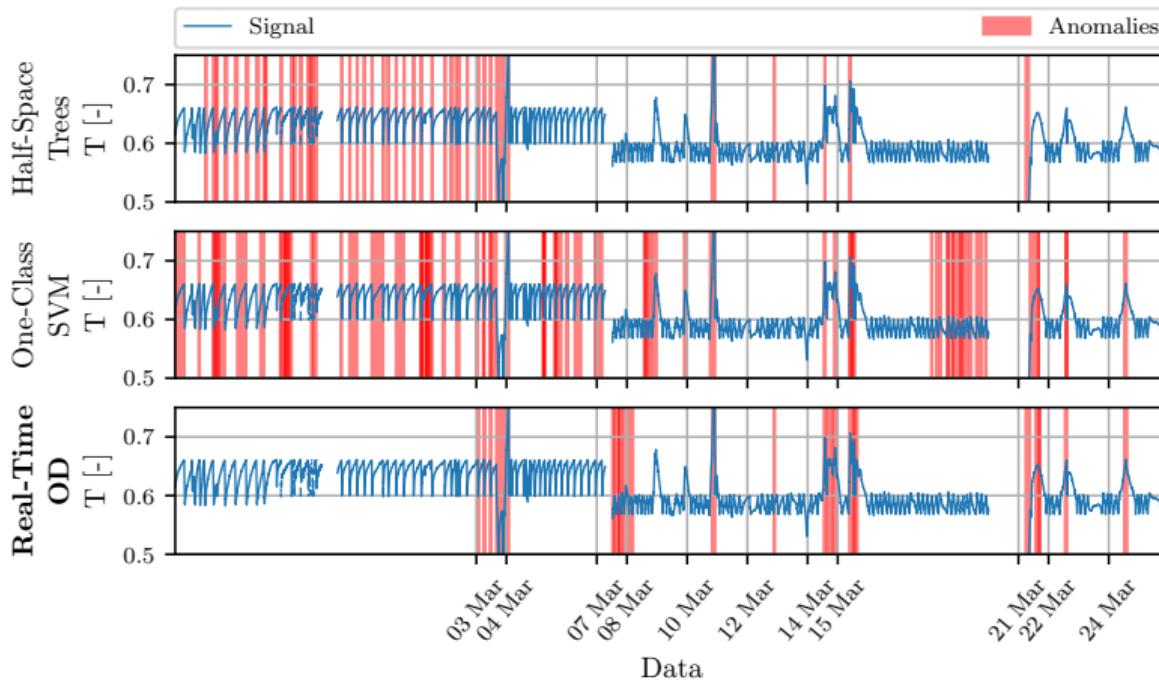
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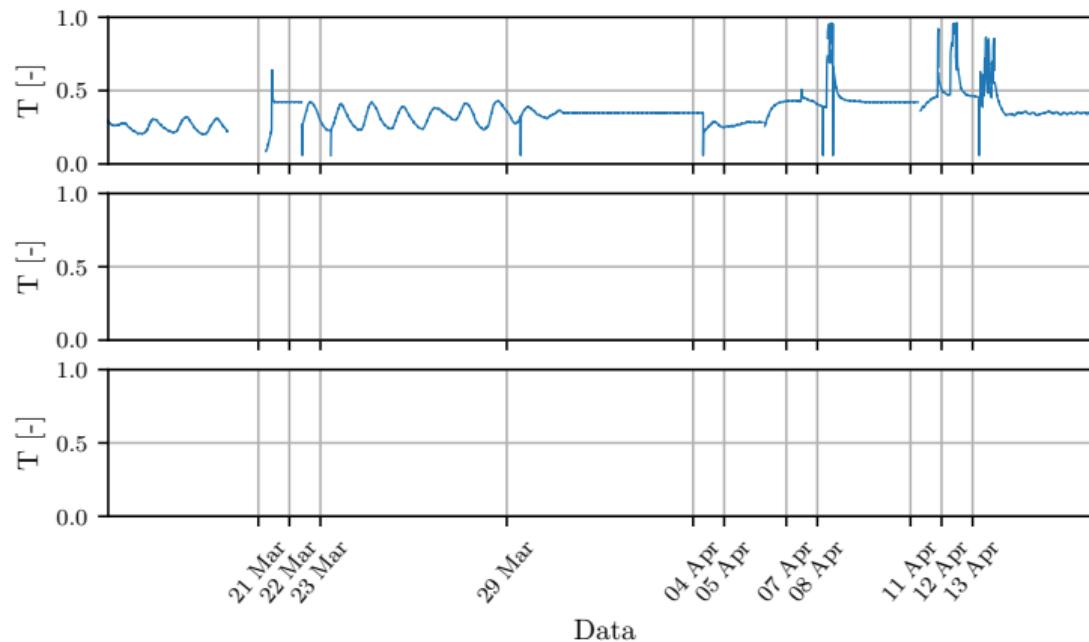
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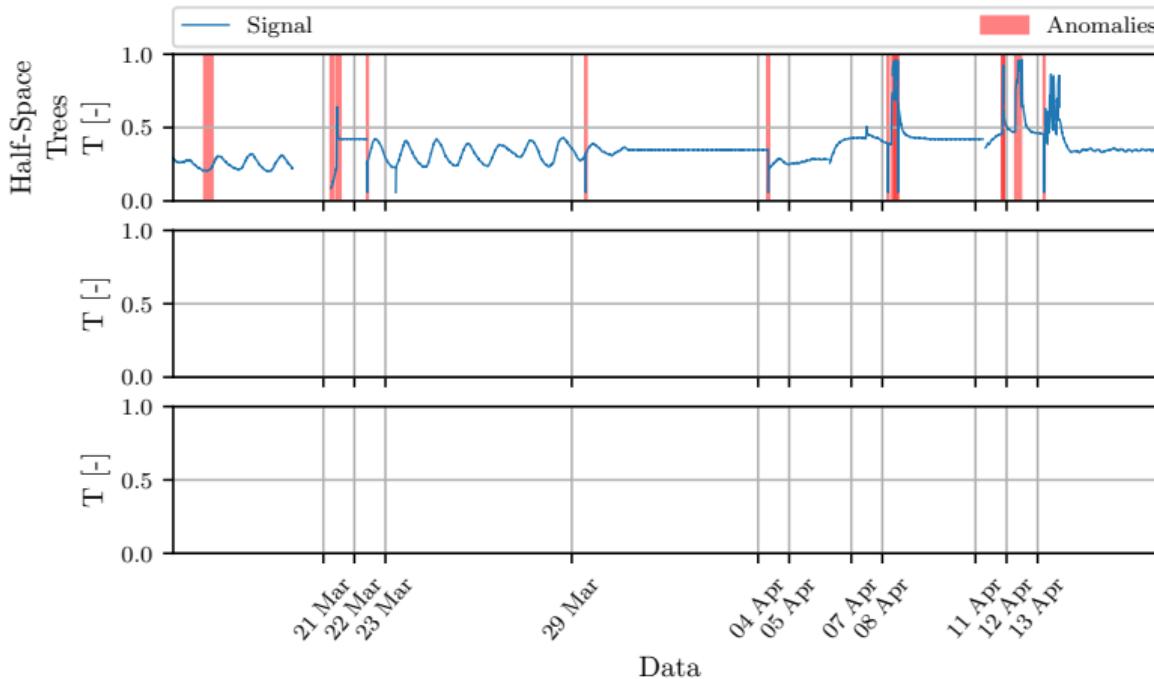
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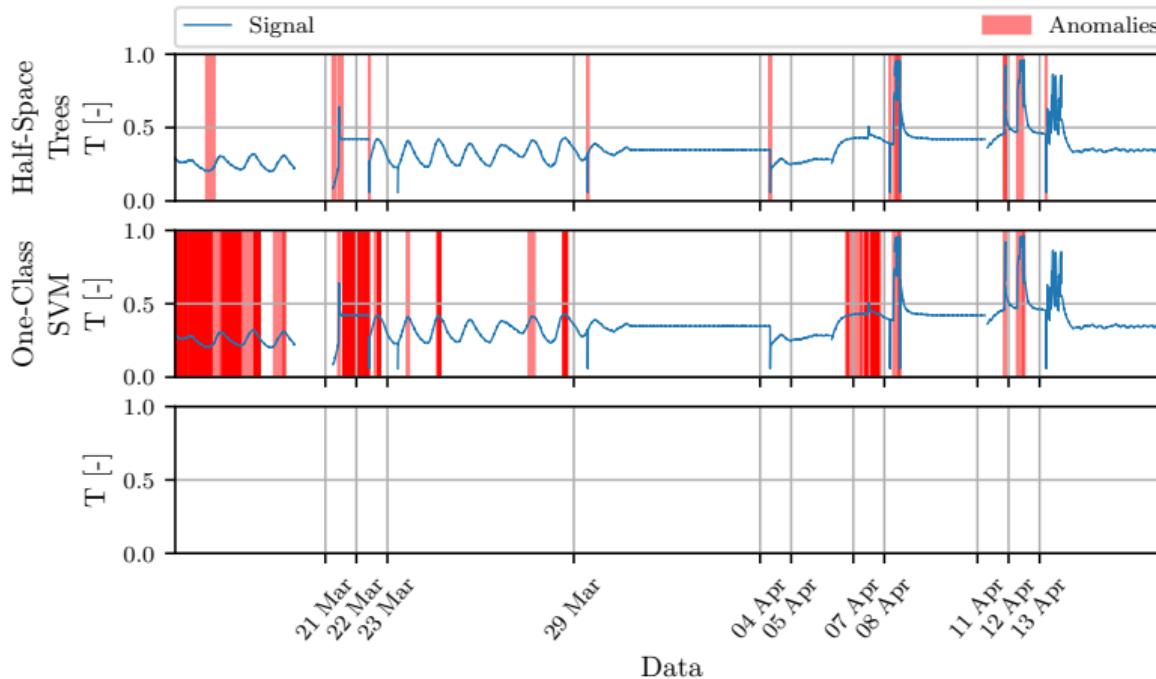
## Case Study – Inverter



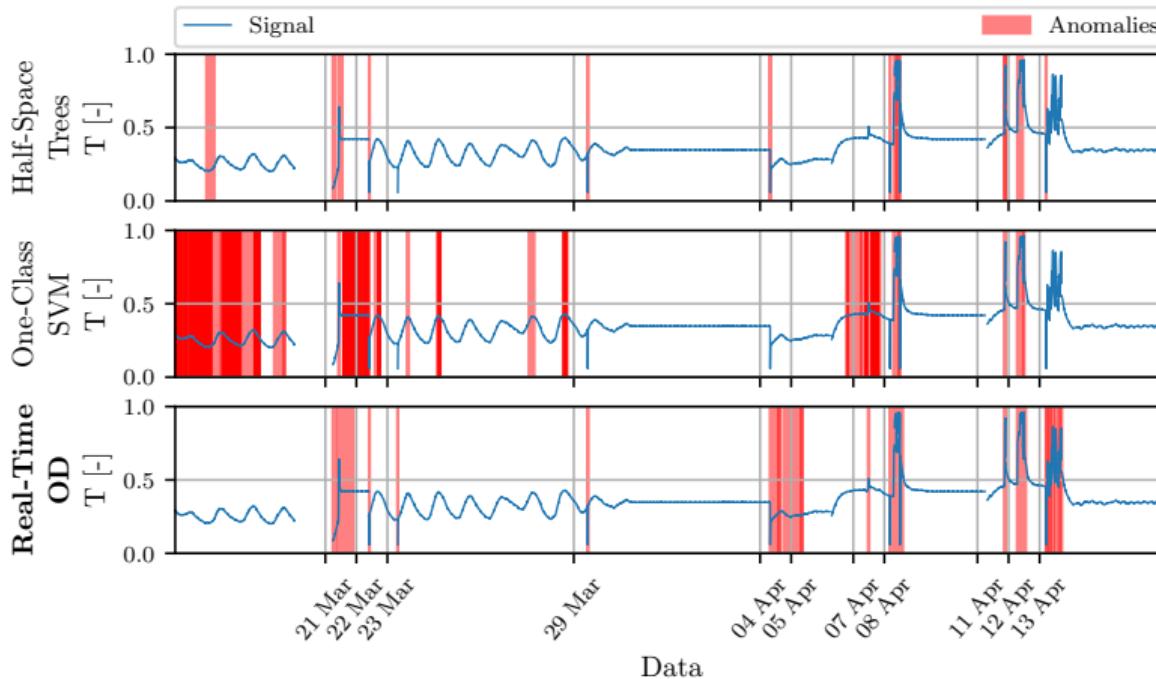
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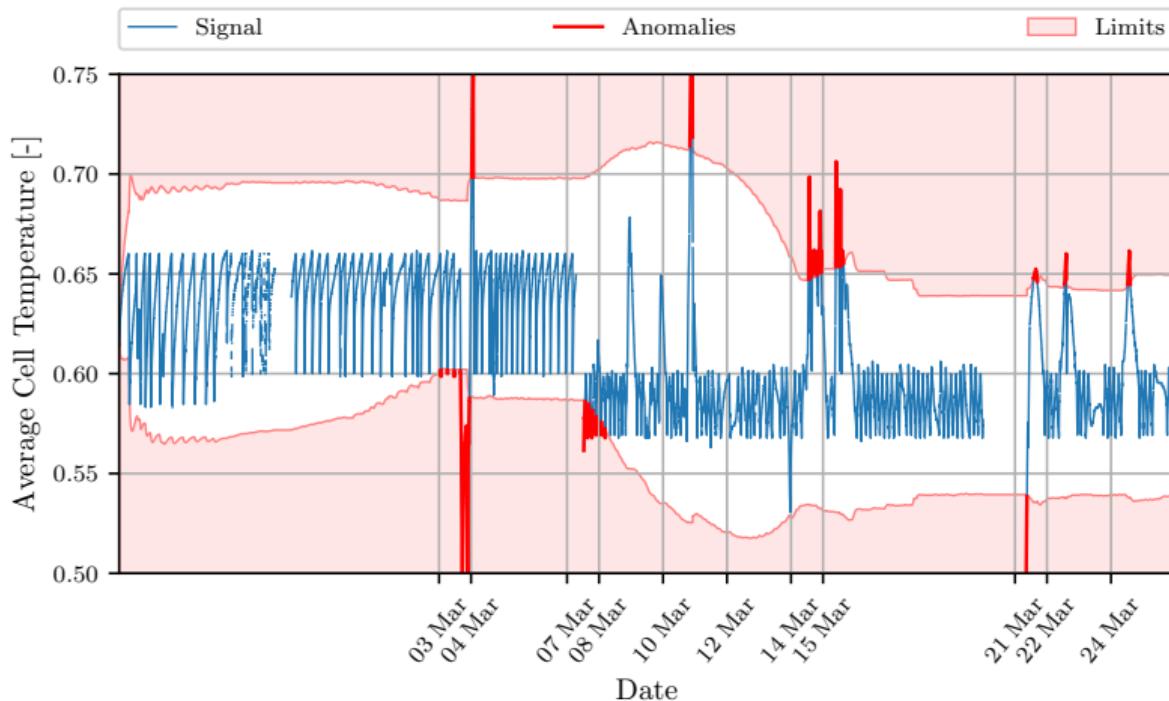
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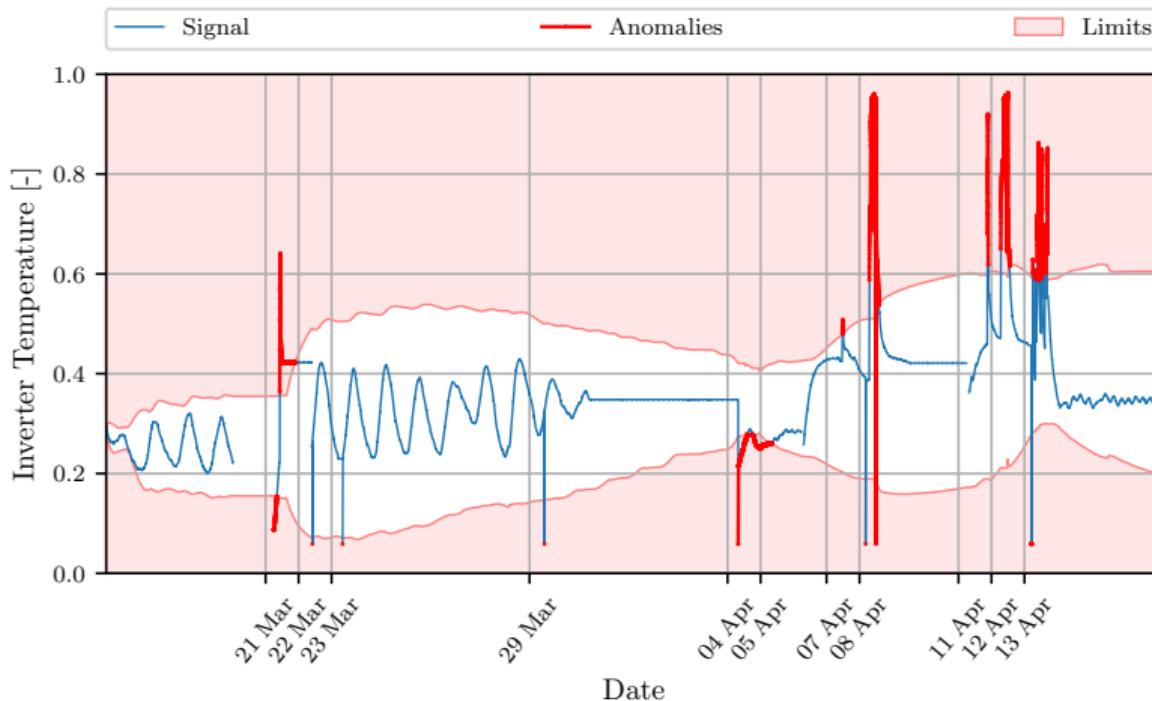
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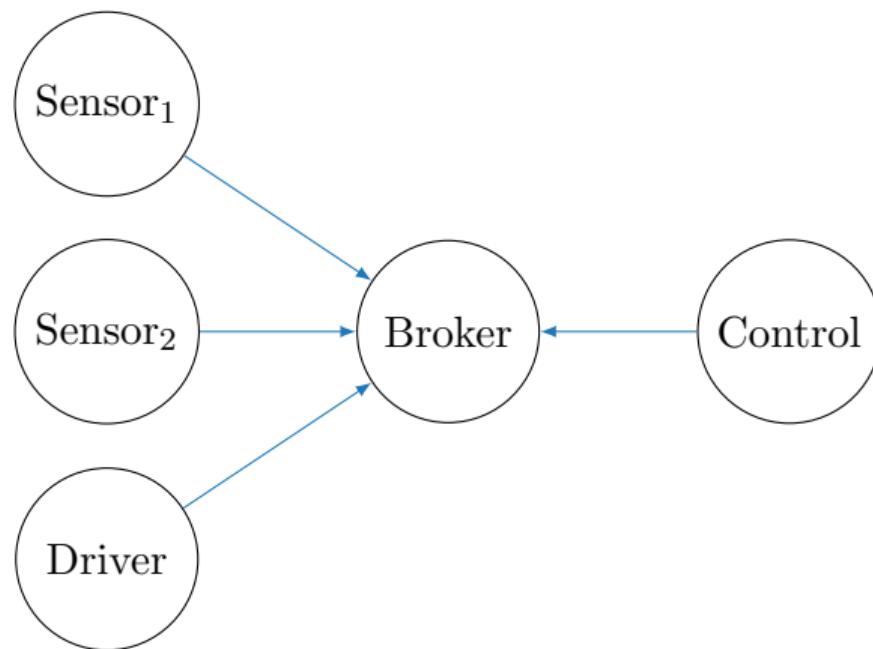
# Dynamic Process Limits – BESS



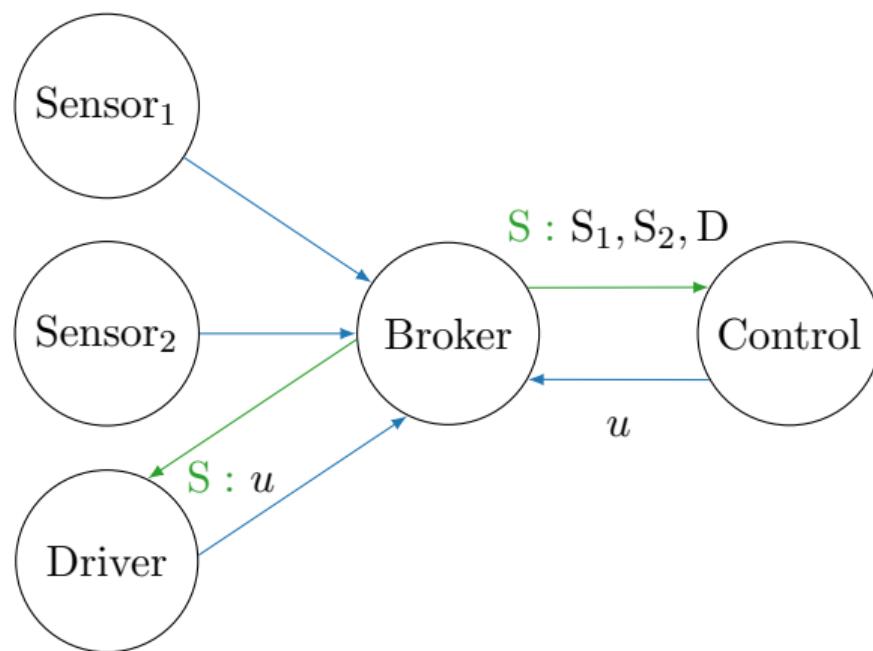
# Dynamic Process Limits – Inverter



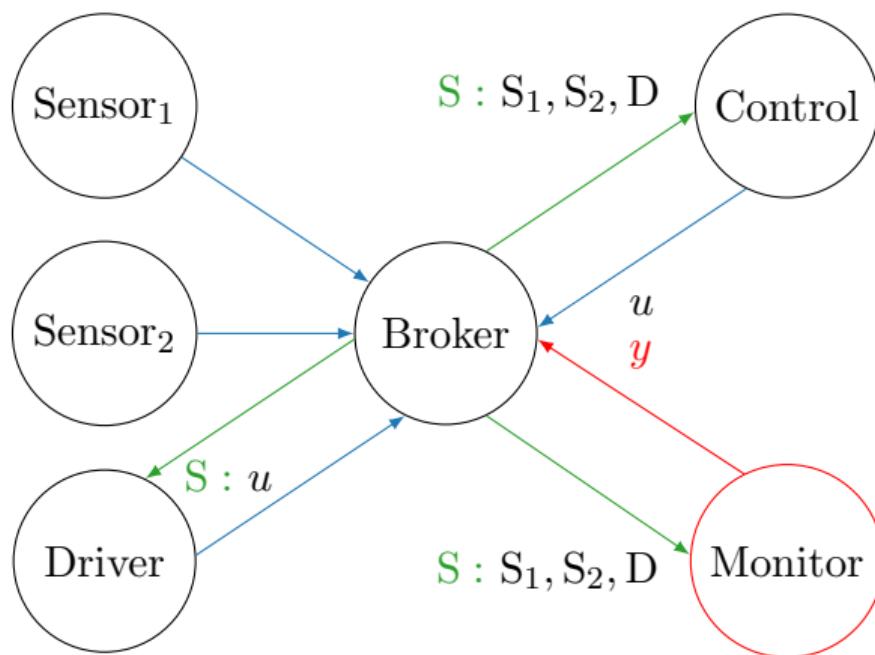
# Utilize Existing Infrastructure



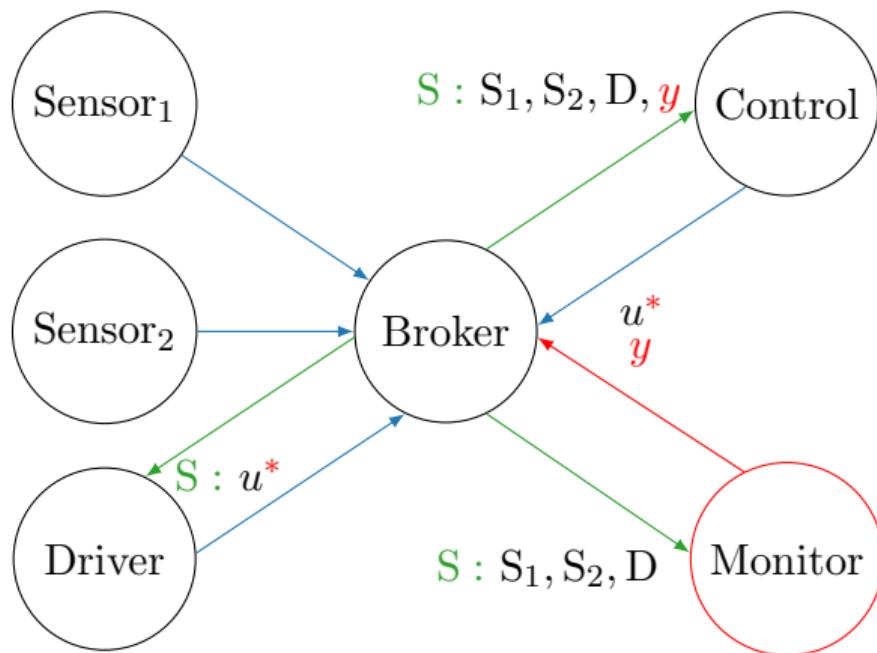
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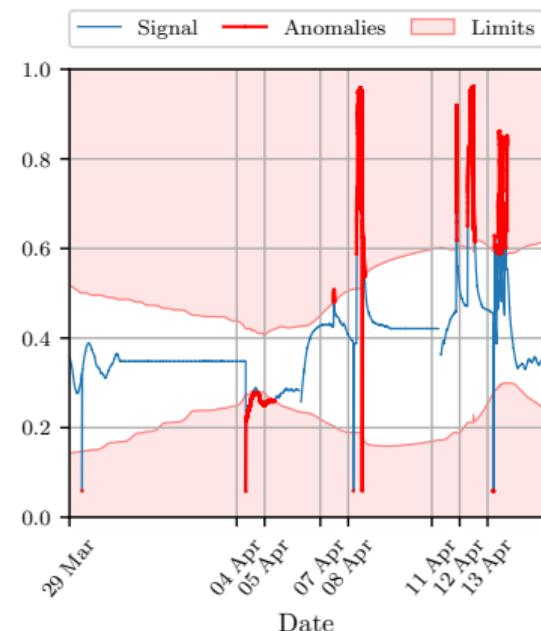


# Utilize Existing Infrastructure



# Summary

- outlier detection on streamed data
- adaptation to external conditions
- online self-learning approach
- dynamic process limits for individual signals
- integration with existing IT infrastructure



Acknowledgements: APVV-20-0261. VEGA 1/0490/23. Horizon Europe under grant no. 101079342 (FrontSeat).

## Process Time Evaluation

Comparison of latency on univariate data.

Algorithm	BESS		Inverter	
	average [ $\mu$ s $\pm$ $\mu$ s]	max [ms]	average [ $\mu$ s $\pm$ $\mu$ s]	max [ms]
Half-Space Trees	220 $\pm$ 200	10	220 $\pm$ 200	11
One-Class SVM	8 $\pm$ 7	1	9 $\pm$ 9	2
<b>Proposed</b>	57 $\pm$ 55	9	60 $\pm$ 75	12

# Online Anomaly Detection Workflow

**Input:** expiration period  $t_e$ , time constant  $t_c$

**Output:** score  $y_i$ , threshold  $x_{q,i}$

*Initialisation :*

```
1:  $i \leftarrow 1; n \leftarrow 1; q \leftarrow 0.9973; \bar{x} \leftarrow x_0; s^2 \leftarrow 1;$ 
2: compute  $F_X(x_0)$  ;
   LOOP Process
3: loop
4:    $x_i \leftarrow \text{RECEIVE}();$ 
5:    $y_i \leftarrow \text{PREDICT}(x_i) ;$ 
6:    $x_{q,i} \leftarrow \text{GET}(q, \bar{x}, s^2);$ 
7:   if (1a) or (3) then
8:      $\bar{x}, s^2 \leftarrow \text{UPDATE}(x_i, \bar{x}, s^2, n);$ 
9:      $n \leftarrow n + 1;$ 
10:    for  $x_{i-t_e}$  do
11:       $\bar{x}, s^2 \leftarrow \text{REVERT}(x_{i-t_e}, \bar{x}, s^2, n);$ 
12:       $n \leftarrow n - 1;$ 
13:    end for
14:  end if
15:   $i \leftarrow i + 1;$ 
16: end loop
```

# Far Less False Positive Alarms

Recall, precision, and F1 evaluation on multivariate benchmark dataset.

Algorithm	Recall [%]	Precision [%]	F1 [%]
Half-Space Trees	33	36	34
One-Class SVM	<b>57</b>	37	44
<b>Proposed</b>	50	<b>48</b>	<b>49</b>

## Follow-up research

