

# Battery Modelling

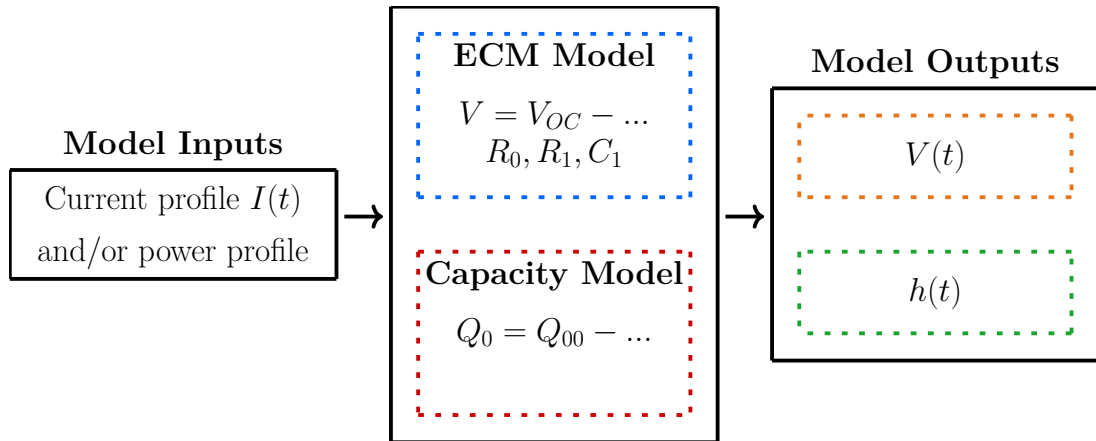
An MMSC Case Study on **MATHEMATICAL MODELLING**

Candidate Number: 1072462

## Abstract

This work will attempt to

The model was implemented in Python and there is a graphical user interface available with live insight into the model (cf. Figure 7).



**Figure 1:** Schematic overview of the battery model introduced in this report. A current input  $I(t)$  is converted into an output voltage  $V(t)$  and corresponding state of health  $h(t)$  due to battery degradation (aging). The core part of the model is an equivalent circuit model (ECM), while aging is modelled by the capacity model.

# 1 Introduction

Clearly, electric batteries are largely important for various industries today and demand for them is ever-growing. This includes, especially, the renewable energy sector due to the unpredictability of energy supplies such as wind and solar power where short-term storage is a necessary evil. Similar relevance may be found in the car industry where one aims for highly (space-)efficient mobile storage of energy. In many countries and/or regions, Electric Vehicles (EVs) still lack a well-enlarged network of charging stations, for various reasons including incompatibilities between charging station suppliers. Using methods introduced in the present report, we aim to optimise the customer experience of an electric vehicle owner through a routing application that takes electric battery peculiarities and battery life-time into account.

In this report, we will consider how to model a Lithium-Ion battery, more specifically the Panasonic 18650PF for which there is some characteristic data available in the public domain ([Kollmeyer 2018](#)). To do this, we will consider an Equivalent Circuit Model (ECM), namely the Thevenin ECM, which may be found in Figure 3. The key idea here is to model the voltage output  $V(t)$  given a current profile  $I(t)$ . This model not only depends on current and time, but also keeps track of internal quantities like the state of charge (SOC,  $s \in [0, 1]$ ) and state of health (SOH,  $h \in [0, 1]$ ). It can be reduced to a system of ordinary differential equations, for which, using given profiles, we find parameters  $R_0$ ,  $R_1$ ,  $C_1$  and more by a fitting procedure. Later on, we also considered aging effects of the battery through usage over time, which resulted in an additional differential equation in the ODE system.

Based on the model we obtained, verified and validated on new pulse test data, the next step was to apply the model to a real-world application, namely that of electric vehicle routing. For this purpose, we obtain graph data of the road network of choice (users may enter new localities as a text input) from OpenStreetMap ([OpenStreetMap contributors 2023](#)). In order to find the best route from A to B, the algorithm then performs a classical routing algorithm called *A-Star* to find the (geometrically) shortest path between A and B, which may not yet be a feasible or optimal path to the destination but a good start. A good initial condition is all that the remaining algorithm requires, which is a Monte-Carlo iterative method that repeatedly applies small, well-defined, perturbations to the graph route and then obtains a time or cost estimate of the modified trip using the battery (and car) model we introduced. If the

modified route yields an improvement in the metric of choice, it is accepted as the new state and the process repeats until a satisfactory route was found.

This report will focus on explicit formulation of the problem and model, numerical simulation of an electric car on a given real-world route and path optimisation through the Metropolis-Hastings method.

## 2 Problem and Model Formulation

### 2.1 The Isolated Battery

In order to model a Lithium-Ion battery in and of itself, we consider the following (physical) quantities: Let  $s \in [0, 1]$  denote the *state of charge* (SOC) of the battery,  $h \in [0, 1]$  the *state of health* (SOH),  $Q \in \mathbb{R}^+$  the charge,  $Q_{00} \in \mathbb{R}^+$  the maximum possible charge at the time of production (in Coulombs),  $V \in \mathbb{R}$  the voltage across the battery (in Volts) with  $I \in \mathbb{R}$  the corresponding current (in Amperes) where  $I > 0$  corresponds to discharging the battery. Then, per common definition,  $s := \frac{Q}{Q_0}$  is the amount of charge currently present in the battery as compared to  $Q_0 \in \mathbb{R}^+$  the current maximum capacity, which itself is dependent on the state of health, as given by  $Q_0 := hQ_{00}$ . Further let  $T \in [-273.15, \infty)$  denote the temperature of the battery (in degrees Celsius) and let  $t \in \mathbb{R}$  represent time (in seconds). Let  $c \in \mathbb{R}^+$  denote the cycle, so the number of full discharges of the battery.

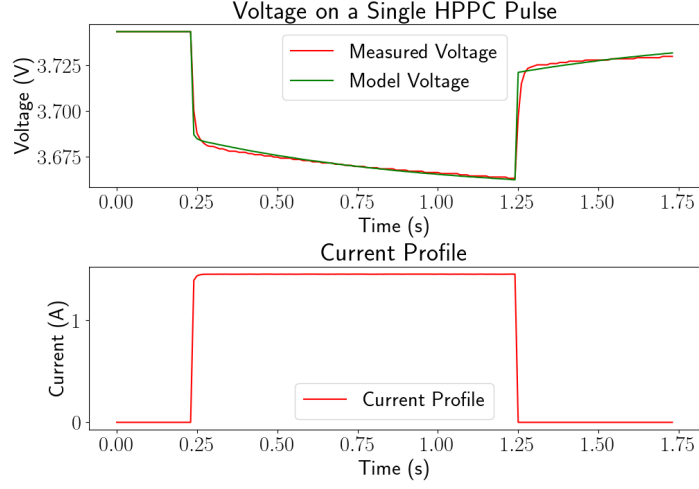
From the definition of current  $I := \frac{dQ}{dt}$ , we further have that for a single cycle,

$$s = \frac{Q}{Q_0} = 1 - \frac{1}{Q_0} \int_0^t I(\tau) d\tau,$$

under the assumption that  $Q_0$ , and therefore  $h$ , stays constant during that cycle.

### 2.2 The Equivalent Circuit Model

As mentioned earlier, we want to model the battery as an electrical component which exerts specific behaviour in an electrical circuit. In electrical engineering, such models of more complicated components are frequently represented by equivalent circuits which only consist of basic components, mostly resistors, diodes, transistors, capacitors and inductors.

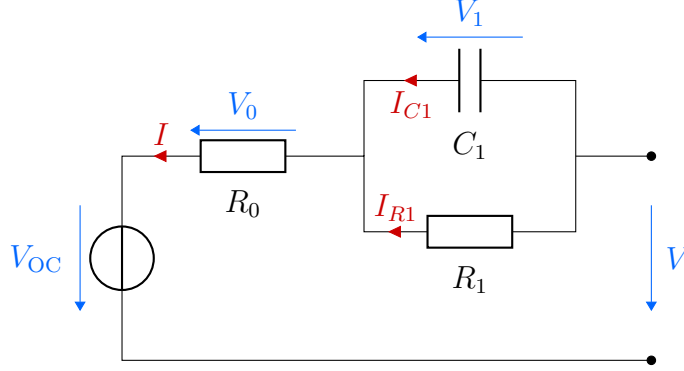


**Figure 2:** One of the sample HPPC (Hybrid Pulse Power Characterization) pulses we used for parameter finding. We want to model the output voltage  $V(t)$  given a current input profile  $I(t)$ . Each sample is characterised at a specific state of charge  $s$ , state of health  $h$  and temperature  $T$ , this one was taken at  $s \approx 1$ ,  $h \approx 1$  and  $T = 10^\circ\text{C}$ .

Empirically, we know that a battery’s voltage output looks roughly as given in Figure 2, which is part of a standardised cycle characterisation procedure taking the battery from “fully charged” ( $s = 1$ ) to “completely empty” ( $s = 0$ ). Data is due to [Kollmeyer 2018](#). As one can see from the voltage curve, the battery exerts a “time-relaxation” behaviour on high-frequency changes in the current. One way of modelling this is through an RC circuit, confer Figure 3: the parallel circuit of  $R_1$  and  $C_1$  is responsible for an exponential-looking behaviour in the voltage curve given (near-)jumps in the current. Normally, RC circuits also model additional ohmic impedance through  $R_0$ . The “heart” of the equivalent circuit model is the open-circuit voltage  $V_{OC}$  which behaves like a voltage source but strongly depends on parameters  $s$ ,  $h$  and  $T$ . We modelled it accordingly, using a polynomial ansatz including cross-terms

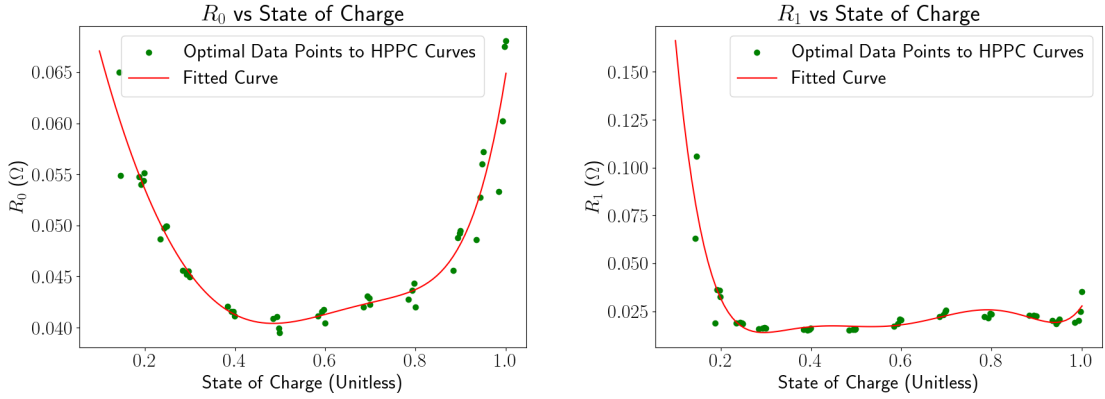
$$V_{OC}(s, h, T) = c_1 s + c_2 h + c_3 T + c_4 sh + c_5 sT + c_6 hT + c_7 shT + \mathcal{O}(s^2, h^2, T^2, \dots),$$

and similar polynomials are chosen for  $R_0$ ,  $R_1$  and  $C_1$ , completing the model. Using the abovementioned dataset ([Kollmeyer 2018](#)), these fits were obtained numerically using a least-squares fitting procedure. An example of the dependency on the state of charge  $s$  can be found in Figure 4.



**Figure 3:** The Thevenin equivalent circuit model (ECM) with parameters  $R_0 \in \mathbb{R}^+$ ,  $R_1 \in \mathbb{R}^+$  and  $C_1 \in \mathbb{R}^+$  and  $V_{OC} \in \mathbb{R}^+$  the *open circuit voltage* which behaves according to a function  $V_{OC}(s, h, T)$  dependent on  $s$ ,  $h$  and  $T$ .

Kirchhoff's law then tells us that the currents  $I_{R1} \in \mathbb{R}$  and  $I_{C1} \in \mathbb{R}$  add up to the total current  $I = I_{R1} + I_{C1}$ , and that the voltages  $V_0 \in \mathbb{R}$ ,  $V_1 \in \mathbb{R}$  and  $V_{OC}$  sum up to  $V = V_0 + V_1 + V_{OC}$ . The capacitor behaves according to  $I_{C1} = C_1 \frac{dV_1}{dt}$ , while the resistors follow Ohm's law  $V_0 = R_0 I$  and  $V_1 = R_1 I_{R1}$ . The resulting circuit then behaves approximately as a real Lithium-Ion battery would in many relevant situations.



(a) Fit of  $R_0$  as a function of the SOC ( $s$ ).

(b) Fit of  $R_1$  as a function of the SOC ( $s$ ).

**Figure 4:** Dependencies of the Thevenin equivalent circuit (Figure 3) model's parameters  $R_0$  and  $R_1$  on the state of charge with a polynomial fit through the data points. Data is again due to [Kollmeyer 2018](#).

Let us consider an application of this model in an electric vehicle next.

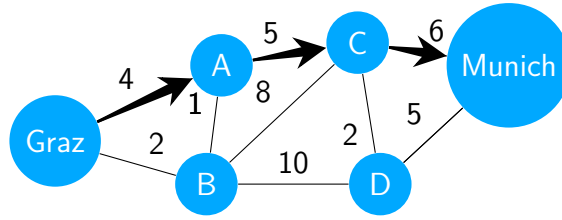
### 2.3 Battery in an Electric Vehicle (EV)

In order to model a road network, let us first consider the definition of an undirected graph  $G = (V_G, E)$ . We take an undirected graph for simplicity, assuming that cars may go in arbitrary direction along each edge.

#### 2.1 Definition: Undirected Graph

A graph  $G = (V_G, E)$  with vertices  $V_G$  and edges  $E \subseteq V_G \times V_G$  is undirected if and only if  $(v_i, v_j) \in E \Rightarrow (v_j, v_i) \in E \quad \forall v_i, v_j \in V_G$ .

Modelling a vehicle on a road network requires a few more definitions. On a graph  $(V_G, E)$  with edges  $E = \{AB, AC, \dots\} \subseteq V_G \times V_G$  and vertices  $V_G = \{A, B, \dots\}$ , let  $d_{AB} \in \mathbb{R}^+$  denote the distance between two vertices  $A \in V_G$  and  $B \in V_G$  (in meters),  $x = x_{AB} \in [0, d_{AB}]$  the progress (current location) on the route from vertex  $A$  to  $B$  (in meters),  $v := \frac{dx}{dt}$  denote the current velocity with  $v_{\max, AB} \in \mathbb{R}^+$  the maximum allowed velocity on  $AB$  (in meters per second). Then let  $T_{\text{env}}(x) \in [-273.15, \infty)$  denote the temperature of the environment (in degrees Celsius) at location  $x$ . Note that this graph-based approach to the problem does not require any more geometric information about the network than edge lengths  $\{d_{ij}\}_{i,j}$ , while it may of course be motivated by spherical coordinates on the earth. Consider for example Figure 5 or Figure 9 for an actual route in Ireland.



**Figure 5:** Exemplary route from Graz to Munich on a road network  $(V_G, E)$ , where edge weights correspond to distances in between the physical places represented by nodes.

The model of our car still lacks a component realising electrical into mechanical power (a motor), which we model very in a very ordinary fashion. Let  $P \in \mathbb{R}$ ,  $P := I \cdot V$  denote the (electrical) power the car draws from the battery (in Watts) so  $P > 0$  corresponds to discharging the battery. This power is to be realised into a mechanical component  $P_{\text{motor}} \in \mathbb{R}^+$  driving the car forwards, heating for the battery  $P_{\text{heat}} \in \mathbb{R}^+$ ,  $P_{\text{heat}} = c(T - T_{\text{env}})$ , with  $c \in \mathbb{R}^+$  the heat conduction constant describing the relation

between the heater and battery, and power dissipation  $P_{\text{diss}} \in \mathbb{R}^+$ . While driving,  $P = P_{\text{motor}} + P_{\text{heat}} + P_{\text{diss}}$ . The acceleration of the car  $a \in \mathbb{R}$  (in meters per second squared), where  $a := \frac{dv}{dt} = \frac{d^2x}{dt^2}$  is decomposed into  $a_m \in \mathbb{R}$ , which directly impacts  $P_{\text{motor}}(a_m)$ , and the deceleration due to friction (air, etc.)  $a_f(v) \in \mathbb{R}^-$ , so that in total  $a = a_m + a_f$ .

Most electric cars have a range from approximately 160 up to 650 km (*EV Database, Range of electric vehicles 2023*), making route changes through charging stations a necessity for longer trips. The resulting routing problem we want to solve then inspires the following definitions of charging stations. On the graph  $(V_G, E)$  there exists a set of EV charging stations  $V_{\text{charge}} \subseteq V_G$  where  $P_{C, \text{charge}}$  denotes the possible charging power (in Watts) at the charging station vertex  $C \in V_{\text{charge}}$  with  $K_C \in \mathbb{R}^+$  the occurring costs per energy unit (in Euros per Watt second) and  $t_C \in \mathbb{R}^+$  the charging time per charging station  $B$  (in seconds)<sup>1</sup>.

## 2.4 Battery Aging

A central aspect considered in our project was to study the effects of battery degradation, or aging. One possible model for this would be to express  $Q_0$  in terms of the original capacity at the time of production  $Q_{00}$  along with multiple degradation effects that we consider:

$$Q_0(t, c, s, I) = Q_{00} - \frac{F_{\text{acycle}}(c)}{F_{\text{current}}(I)} - F_{\text{cal}} \in [0, Q_{00}]. \quad (1)$$

By  $F_{\text{acycle}}(c) \in \mathbb{R}$  we denote the **Current Agnostic Cycle Degradation Factor** which models cycle aging at a single current. It models the aging effects resulting only from discharge usage of the battery, at an idealised single current.  $F_{\text{current}}(I) \in \mathbb{R}$  represents the **Current Scaling Factor**, a value  $0 < F_{\text{current}} \leq 1$  that incorporates behaviour where higher currents are worse for cycle aging (Perez et al. 2018). This term is highly relevant for scenarios where one can choose the amount of current drawn from the battery and then optimise accordingly if this behaviour is well-known. Finally,  $F_{\text{cal}}(s, t) \in \mathbb{R}$ , the **Calendar Degradation Factor**, ages the battery over time and accounts for suboptimal storage in terms of the state of charge. Storage at the right state of charge and environment is one of the most crucial aspects for battery lifetime.

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<sup>1</sup>Charging station & street data was obtained from [OpenStreetMap](https://nominatim.openstreetmap.org/) and subsequently invoking `osmfilter england-latest.o5m keep="amenity=charging_station"`. Daily dumps of OSM's public map data were obtained from <https://download.geofabrik.de/>.

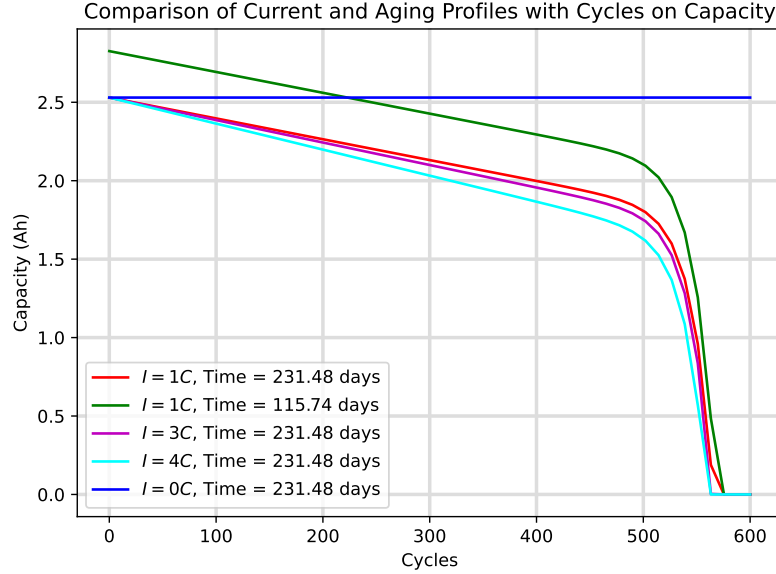
The state of health  $h$ , the ratio between  $Q_0$  and  $Q_{00}$  is then given by

$$h = \frac{Q_0}{Q_{00}} = 1 - \frac{F_{\text{acycle}}(c) + F_{\text{cal}}F_{\text{current}}(I)}{F_{\text{current}}(I)Q_{00}} \in [0, 1],$$

directly following from Equation 1 and yielding a simple, yet effective approximation for aging of the battery. In our model, we used

$$\begin{aligned} F_{\text{acycle}} &= c (\alpha_1 + \alpha_2 \exp\{\alpha_3 c - \alpha_4\}) , \\ F_{\text{current}} &= \alpha_5 - \alpha_6 \exp\{\alpha_7 I - \alpha_8\} , \\ F_{\text{cal}} &= \int \left( \alpha_9(T) \left\{ \cosh(\alpha_{10}s - \alpha_{11}) + \alpha_{10}t |\sinh(\alpha_{10}s - \alpha_{11})| \left| \frac{ds}{dt} \right| \right\} \right) dt , \end{aligned}$$

largely following [Perez et al. 2018](#) with  $\alpha_{1,\dots,11} \in \mathbb{R}$  various parameters obtained through fitting procedures. A plot of the degradation function is given in Figure 6, using the given expressions for  $F_{\text{acycle}}$ ,  $F_{\text{current}}$  and  $F_{\text{cal}}$ .



**Figure 6:** Capacity over discharging cycles behaviour according to the degradation model of the battery, according to Equation 1 with  $Q_{00} = 2.9$  A h. Each line corresponds to different discharge currents  $I$ , as multiples of the capacity, and a different battery aging time.

Using the car and road network models introduced above, in general terms the problem may be stated as follows:



## 2.5 A Variational Optimisation Problem

Given source and destination vertices  $A, Z \in V_G$  on the graph  $(V_G, E)$ , **which connected set of edges**  $E_R \subseteq E$  connecting  $A$  to  $Z$ , set of visited **charging stations**  $V_C \subseteq V_{\text{charge}}$  along  $E_R$  and **charging times**  $\{t_C\}_{C \in V_C}$  visited on the route  $E_R$ , and **driving behaviour**  $a_m(x, v, t, s, h, T_{\text{env}}, \dots)$ ,  $a_m \in \mathcal{C}^1(\mathbb{P})$  with  $\mathbb{P}$  the parameter space, **minimises**

1. the total travel time  $t_{\text{total}} := \int_{V_R} \frac{1}{v} dx + \sum_{C \in V_C} t_C$ ,
2. the total cost of travel  $K := \sum_{C \in V_C} P_{C, \text{charge}} t_C K_C$ ,
3. or  $-N$  where  $N$  is the highest possible number of repetitions (commutes from  $A$  to  $Z$ ) with the same battery (requiring  $h > 0$ ).

In other words, we aim to minimise the functional  $F \in \mathcal{C}(\mathbb{P})^*$ , so  $F : \mathcal{C}(\mathbb{P}) \mapsto \mathbb{R}$  where either  $F[a_m, E_R, V_C, t_C] = t_{\text{total}}$ ,  $F[a_m, E_R, V_C, t_C] = K$  or  $F[a_m, E_R, V_C, t_C] = -N$ .

Obviously, solving the stated problem in its full form and with all the given details is a task exceeding the scope of this project, although we were able to make some progress in the direction of it. The intention here is to state the model in high generality and be clear about the simplifications that were made within the scope of this report in order to be able to move ahead.

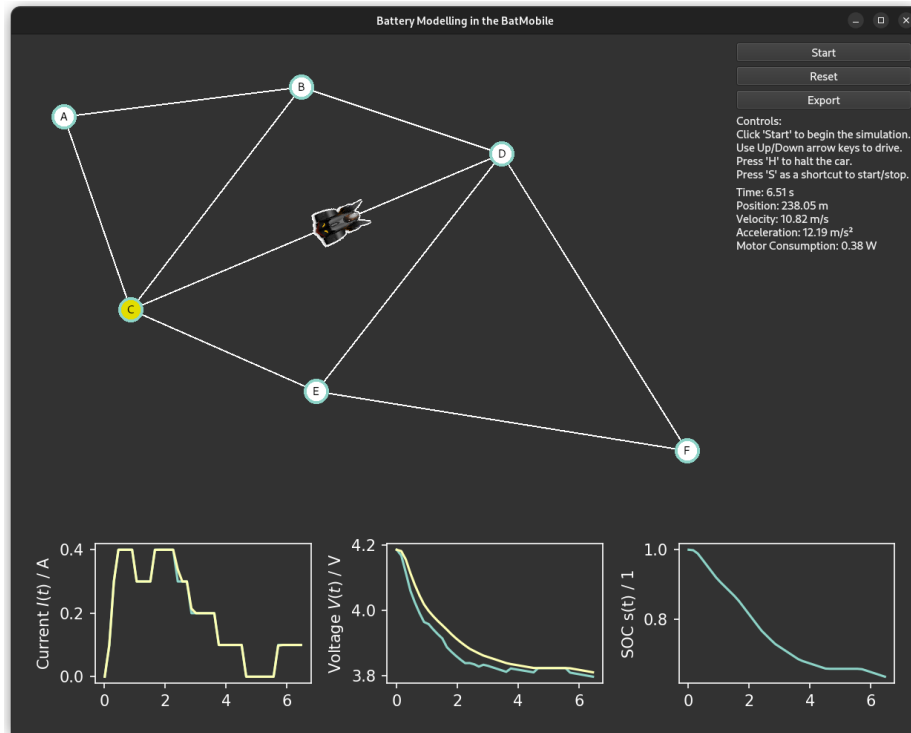
There are endless possibilities to simplify, for example one could take  $V_G = \{A, B\}$  and  $E = \{AB\}$  with some  $d_{AB}$ ,  $v_{\text{max}, AB} = \infty$  and  $V_C = \{\}$ , so only looking at the minimisation of  $t_{\text{total}}$ . This is equivalent to ignoring the graph-algorithmic component of the problem, as it is only a single line without a charger. Another potential simplification would be to take  $h = 1$  to ignore battery aging / degradation effects. Or even more radically,  $s = \text{const}$  to only model very short-term (on the order of seconds) effects of this model.



In the remaining sections of the report, we will assume the following:

- $T = T_{\text{env}} = \text{const.}$  and therefore  $P_{\text{heat}} = 0$  to ignore the motor heating component. We neglected temperature changes in the environment and a respective battery heating strategy  $P_{\text{heat}}(x, v, t, s, h, T_{\text{env}}, \dots)$ ,  $P_{\text{heat}} \in \mathcal{C}(\mathbb{P})$ .
- $P_{\text{diss}} = 0$  as this is an easily implementable extension to the existing model.
- $a_f = 0$  to ignore friction terms in the acceleration. Then  $a = a_m$  is the first argument of the functional  $F[a, E_R, V_C, t_C]$  we are trying to minimise.
- $v_{\text{max}, ij} = \infty \forall i, j$  so there is no speed limit.

### 3 Numerical Simulation of a Car

#### 3.1 Forward Euler Simulation



**Figure 7:** Screenshot of the Qt6 user interface of the car simulation software accompanying this report (confer Appendix A) running on the graph depicted in Figure 5. Using the arrow keys, one can control the battery mobile (*batmobile*) along edges of the road network. Pressing  accelerates the car and the resulting battery model changes can be observed in real-time using the charts at the bottom.  decelerates (in this scenario, we used current-control, so  $I(t)$  is decreased).

## 4 Metropolis-Hastings and A-Star

### 4.1 Shortest Path Finding

The graph data was retrieved using OSMnx (Boeing 2017) which itself is built on NetworkX (Hagberg, Schult and Swart 2008). The edges retrieved from the OpenStreetMap API also contain data on the highest allowed velocity  $v_{\max}$ , but we did not use it in our solver as this would need to be a carefully considered constraint to the optimisation routine.

## 4.2 Monte-Carlo Optimisation

Metropolis et al. 1953; Hastings 1970.

Optimise a large problem (huge state-space). Metric: Time! Could be anything.  $\Rightarrow$  Use Monte-Carlo Markov Chain Methods! Slightly perturb the route using a specific alteration technique. Metropolis-Hastings updates the state (route) based on

$$p_{\text{accept}} = \min \left( 1, e^{-\beta(T_{\text{next}} - T_{\text{current}})} \right), \quad \text{with } \beta \in \mathbb{R}^+ \text{ a transition factor.}$$

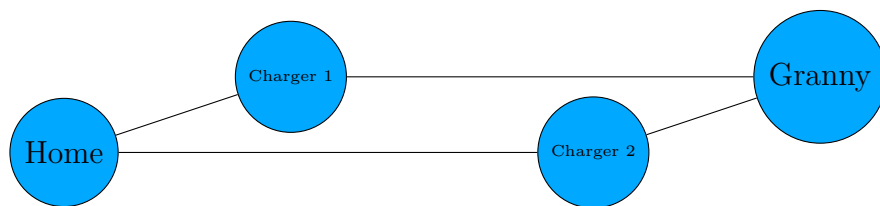
Does a full numerical simulation of the drive. Stop to charge? Explore the state-space to some extent, and return the best route! Larger scales / maps (e.g. England) are not a problem!

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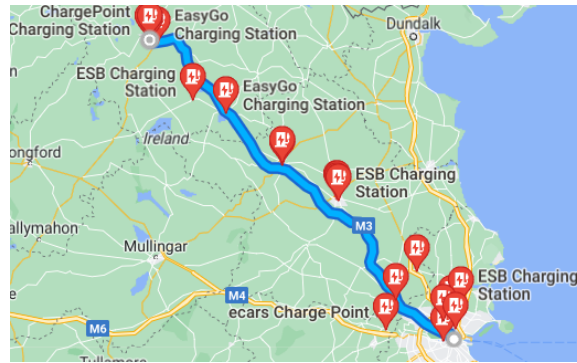
1 newEnergy = self.measureRoute(newRoute) if newRoute not in self.testedRoutes else
  ↪ self.testedRoutes[newRoute]
2 delta = newEnergy - self.testedRoutes[self.route]
3 acceptanceProbability = min(1, math.exp(-delta / self.temperature))
4 if random.random() < acceptanceProbability:
5     self.route = newRoute
6     print(f"Accepted new route {newRoute} with delta: {delta:.2f}. Total:
  ↪ {self.testedRoutes[newRoute]:.2f}.")
7 else:
8     print(f"Rejected route {newRoute} with delta: {delta:.2f}.")

```

## 4.3 Special Case: Granny's House



**Figure 8:** The graph of our exemplary problem “Granny’s House”, a simplified case of the problem described in subsection 2.5. The situation is that we want to visit our grandmother, who lives 115 km away from our home, in regular intervals. Along the route, there are two chargers. Our car only has a range of 200 km. Is it better to charge at the first or second charger, on the way there or on the way back?



**Figure 9:** The unperturbed route for the “Granny’s House” problem in Ireland, with charging stations depicted using red pins. Screenshot due to [Google 2023](#).

## 4.4 Routing in Jericho

The  $A^*$ -search algorithm ([Optimization 2021](#))

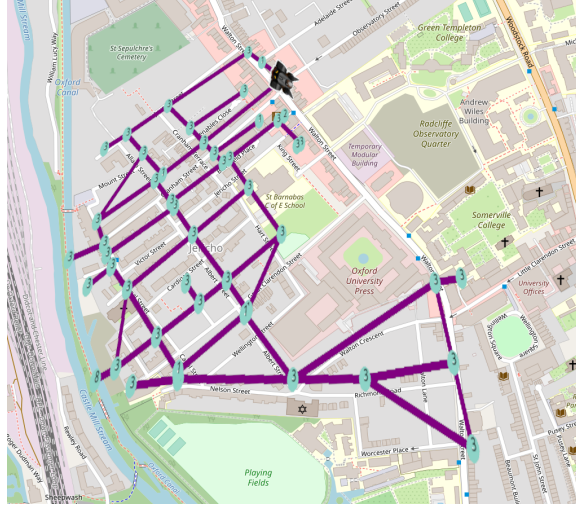
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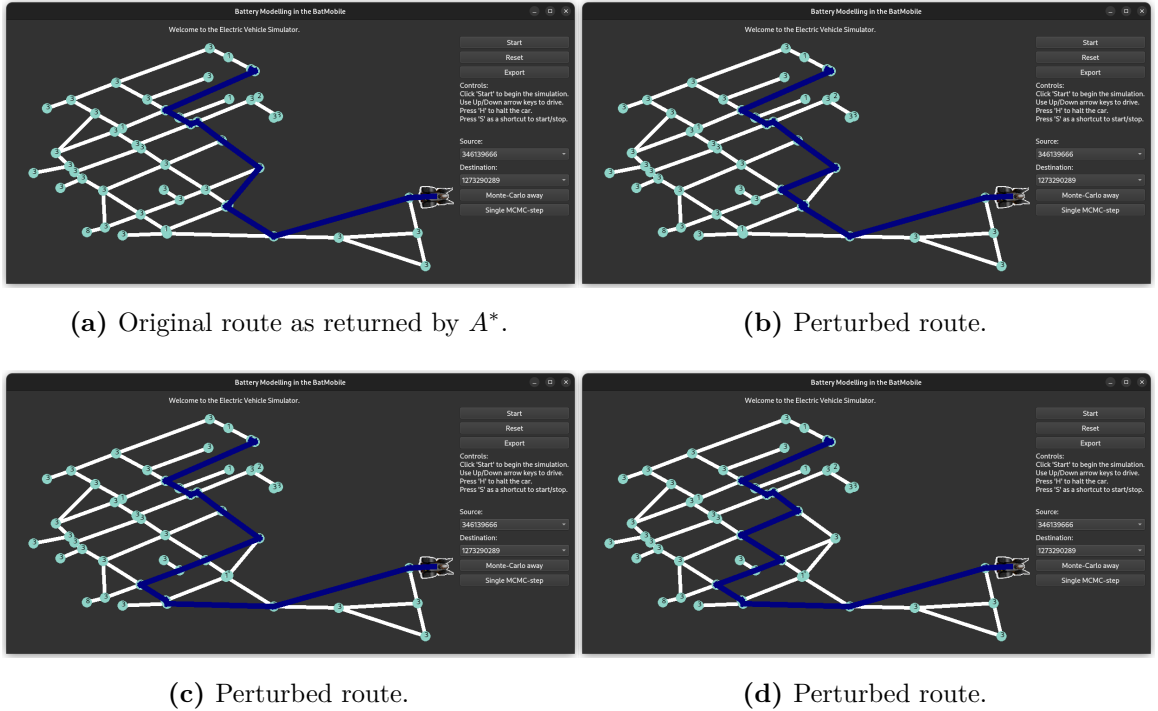
1 open_list, closed_list = empty list of possible positions
2 adjacent_val = 0
3 next_position = null
4 push start_position to open_list
5 while open_list is not empty, do
6     current_node = pop(open_list)
7     for each adjacent position of current_node (ap_current)
8         with value (av_current), do
9             if (adjacent_val < av_current) or (ap_current ∈ closed_list), do
10                 adjacent_val = av_current
11                 next_position = ap_current
12             push ap_current to closed_list
13             push next_position to open_list

```

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**Figure 10:** Overlay of the routing graph on a map of Jericho, Oxford, Oxfordshire (OpenStreetMap contributors 2023), without adjusting for the Merkator projection or non-linear roads, which leads to a slightly skewed appearance. The Oxford Mathematical Institute is adjacent to one of the shown edges.



**Figure 11:** Routes on the extended user interface including  $A^*$  route finding along with the Monte-Carlo route perturbation-based optimisation functionality. The user can select a source and target vertex on the road graph  $G = (V_G, E)$  loaded from OpenStreetMap and start the optimisation procedure. The displayed road network is that of Jericho, Oxford, Oxfordshire.

## 5 Conclusion

Potential improvements are, for instance, using more analytical methods to obtain solutions of the variational optimisation problem described in subsection 2.5.

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## A Code Structure and Setup

The code of this group project can be found on GitHub, namely in [this repository](#). To use and sustain a Python virtual environment, install [poetry](#), which works with the `pyproject.toml` file. After installing poetry (and subsequently after pulling, each time), run

```
poetry install
```

in the project folder. To install PyBamm as well (which has  $\mathcal{O}(\frac{1}{\epsilon})$  number of dependencies), run

```
poetry install --with=pybamm
```

instead or additionally. This sadly requires Python 3.8 based on a pybamm restriction. Without pybamm, 3.11 should be fine too.

Having all dependencies installed, the main interface may be launched up by executing

```
python3 main.py
```

which starts a graphical user interface (with looks depending on your operating system). Note that you may need to install some Qt6 dependencies.

The relevant code structure is:

- The folder `simulator/` is responsible for the (numerical) simulation itself, which may be invoked without any interface at all.
  - `simulation.py` features the `Simulation` class with an `iterate()` method that represents a numerical integration step in time by an amount of `dt`.
  - `batgraph.py` exports a class `BatGraph` that represents a graph (a tuple of sets of edges and vertices) that the car will drive on.
  - `batmobile.py` contains the `BatMobile` class that represents our battery mobile i.e. car. **Much of the simulation takes place in this file!**
  - `battery.py` is the central file for our battery modelling project, which exports a `Battery` class, also featuring an `iterate()` method. **Most of the battery simulation takes place in this file!**
  - `optimiser.py` takes care of the optimisation part of the routing problem. It implements the Metropolis-Hastings (Monte-Carlo Markov Chain) method and defines the graph perturbations.
- The interface code is contained within the `interface/` folder.
  - `mainwindow.py` defines the general layout and actions in the user interface.
  - `batmap.py` exports the central widget that renders / animates the `BatMobile` car on the `BatGraph`.



- `graphs.py` handles the connection of the interface and (live) plots. The plots are handled by `matplotlib` and are very intuitive to use, further almost all commands are the same as they are in MatLab.
- `main.py` creates a `MainWindow` and runs the simulator GUI.