

Distributions in Reliability sub-system

Birnbaum-Saunders

x ~ dbs(alpha, beta)
$$\frac{1}{\sqrt{2\pi x^3}} \frac{(x+\beta)}{2\alpha\sqrt{\beta}} \exp\left\{-\frac{1}{2\alpha^2} \left(\frac{x}{\beta} + \frac{\beta}{x} - 2\right)\right\}; \ x > 0$$

Burr X (Generalized Rayleigh)

x ~ dburrX(alpha, lambda)
$$2 \alpha \lambda^2 x e^{-(\lambda x)^2} \left\{ 1 - e^{-(\lambda x)^2} \right\}^{\alpha - 1}; \quad x > 0$$

Burr XII Distribution

$$x \sim \text{dburrXII(alpha, beta)}$$
 $\alpha \beta x^{\beta-1} \left\{ 1 + x^{\beta} \right\}^{-(\alpha+1)}$; $x > 0$.

Exponential Power (Smith & Bain)

$$\text{x ~- dexp.power(alpha, lambda)} \quad \alpha \, \lambda^{\alpha} \, \, x^{\alpha-1} \, e^{\left(\lambda \, x\right)^{\alpha}} \, exp \left\{ 1 - e^{\left(\lambda \, x\right)^{\alpha}} \, \right\} \quad \text{; } x \geq 0$$

Exponentiated Weibull

$$x \sim \text{dexp.weib(alpha, theta)}$$
 $\alpha \theta x^{\alpha-1} e^{-x^{\alpha}} \left\{ 1 - \exp(-x^{\alpha}) \right\}^{\theta-1}$; $x > 0$

Extended Exponential (Marshall-Olkin)

$$x \sim \text{dext.exp(alpha, lambda)} \qquad \frac{\alpha \, \lambda \, e^{-\lambda x}}{\left\{1 - (1 - \alpha) \, e^{-\lambda x}\right\}^2} \; ; \qquad x > 0$$

Extended Weibull(Marshall-Olkin)

$$x \sim \text{dext.weib(alpha, lambda)} \qquad \frac{\lambda \alpha \, x^{\alpha-1} \exp\left(-x^{\alpha}\right)}{\left\{1 - (1 - \lambda) \exp\left(-x^{\alpha}\right)\right\}^2} \; ; \qquad x > 0$$

Flexible Weibull

$$x \sim \text{dflex.weib(alpha, beta)} \qquad \left(\alpha + \frac{\beta}{x^2}\right) \ exp \left(\alpha \ x - \frac{\beta}{x}\right) \ exp \left\{-exp \left(\alpha \ x - \frac{\beta}{x}\right)\right\} \quad ; x \geq 0$$

Generalized Exponential

x ~ dgen.exp(alpha, lambda)
$$\alpha \lambda e^{-\lambda x} \left\{ 1 - e^{-\lambda x} \right\}^{\alpha - 1}; x > 0$$

Generalized Power Weibull

$$\text{x ~-dgp.weibull(alpha, theta)} \qquad \alpha \, \theta \, \, x^{\alpha - 1} \Big(1 + x^{\alpha} \Big)^{\theta - 1} \, \exp \left\{ 1 - \Big(1 + x^{\alpha} \Big)^{\theta} \right\} \quad ; x \geq 0$$

Gompertz

x ~dgpz(alpha, theta)
$$\theta \ e^{\alpha x} \exp \left\{ \frac{\theta}{\alpha} \left(1 - e^{\alpha x} \right) \right\} \quad ; x \ge 0$$

Gumbel

x ~dgumbel(mu, sigma)
$$\frac{1}{\sigma} exp \left\{ -\left(\frac{x-\mu}{\sigma}\right) \right\} exp \left[-exp \left\{ -\left(\frac{x-\mu}{\sigma}\right) \right\} \right]; \quad -\infty < x < \infty$$

Inverse Gaussian

x ~ dinv.gauss(mu, lambda)
$$\sqrt{\left(\frac{\lambda}{2\pi}\right)} \quad x^{-3/2} exp\left\{-\frac{\lambda(x-\mu)^2}{2\mu^2 x}\right\} \; ; \; x>0$$

Inverse Weibull

x ~dinv.weib(beta, lambda)
$$\beta \ \lambda^{\beta} \ x^{-(\beta+1)} \exp \left\{ -\left(\frac{\lambda}{x}\right)^{\beta} \right\} \quad ; x > 0$$

Linear Failure Rate

x ~dlin.fr(alpha, beta)
$$(\alpha + \beta x) \exp \left\{ -\left(\alpha x + \frac{\beta x^2}{2}\right) \right\} ; x \ge 0$$

Logistic-exponential

$$\text{x \simdlogis.exp(alpha, lambda)} \qquad \frac{\lambda \ \alpha \ e^{\lambda x} \left(e^{\lambda x} - 1\right)^{\alpha - 1}}{\left\{1 + \left(e^{\lambda x} - 1\right)^{\alpha}\right\}^2} \quad ; x \ge 0$$

Log-logistic Distribution

x ~dlog.logis(beta, theta)
$$\frac{\beta (x/\theta)^{\beta}}{x \{1 + (x/\theta)^{\beta}\}^2} \quad ; \quad x > 0.$$

Log-Weibull

x ~dlog.weib(mu, sigma)
$$\frac{1}{\sigma} exp\left(\frac{x-\mu}{\sigma}\right) \cdot exp\left\{-exp\left(\frac{x-\mu}{\sigma}\right)\right\} \quad ; \quad -\infty < x < \infty$$

Modified Weibull

$$\text{x ~- dweib.modified(alpha, beta, lambda)} \quad \alpha \left(\ \beta + \lambda x \ \right) x^{\beta - 1} \ e^{\lambda x} \ exp \left\{ -\alpha \ x^{\beta} e^{\lambda x} \right\} \quad ; x > 0$$