An invitation for transdisciplinary collaboration

The OSE team

March 10, 2021



# **Computational modeling in economics**

#### **Motivation**

- Facilitate academic rigor
- Study mechanisms
- Predict public policies

# Computational modeling in economics

#### **Motivation**

- Facilitate academic rigor
- Study mechanisms
- Predict public policies

## Transdisciplinary in nature

- Economic model
- Mathematical framework
- Computational implementation

## **Understanding individual decisions**

- Human capital investment
- Consumption—savings decision

# **Understanding individual decisions**

- Human capital investment
- Consumption—savings decision

## **Predicting effects of policies**

- Welfare programs
- Tax schedules

#### **Understanding individual decisions**

- Human capital investment
- Consumption—savings decision

## **Predicting effects of policies**

- Welfare programs
- Tax schedules

- Finite-horizon discrete Markov decision problem
- Backward induction algorithm

#### **Understanding individual decisions**

- Human capital investment
- Consumption—savings decision

## **Predicting effects of policies**

- Welfare programs
- Tax schedules

- Finite-horizon discrete Markov decision problem
- Backward induction algorithm
- ⇒ Transdisciplinary research on their **economics**, data, and computation

#### **Understanding individual decisions**

- Human capital investment
- Consumption—savings decision

# **Predicting effects of policies**

- Welfare programs
- Tax schedules

- Finite-horizon discrete Markov decision problem
- Backward induction algorithm
- $\Rightarrow$  Transdisciplinary research on their economics, data, and computation

#### **Understanding individual decisions**

- Human capital investment
- Consumption—savings decision

## **Predicting effects of policies**

- Welfare programs
- Tax schedules

- Finite-horizon discrete Markov decision problem
- Backward induction algorithm
- $\Rightarrow$  Transdisciplinary research on their economics, data, and computation

#### **Partners**



Institute for **Numerical Simulation** 





UNIL | Université de Lausanne

# **Roadmap**

- Economic model
- Mathematical formulation
- Calibration

# Roadmap

- Economic model
- · Mathematical formulation
- Calibration

- Example
- Pipeline
- Projects

# **Economic model**

# **Decision Problem**

t = 1, ..., T decision period

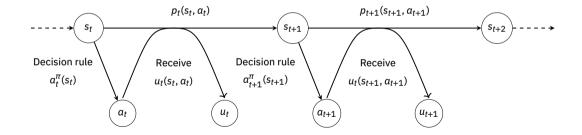
 $s_t \in S$  state

 $a_t \in A$  action

 $a_t(s_t)$  decision rule

 $u_t(s_t, a_t)$  immediate utility

# **Timing of events**



$$\pi = (\alpha_1^{\pi}(s_1), \dots, \alpha_T^{\pi}(s_T))$$
 policy  $\delta$  discount factor  $\rho_t(s_t, \alpha_t)$  conditional distribution

# Individual's objective

$$\max_{\pi \in \Pi} \mathsf{E}_{\mathsf{s}_1}^{\pi} \left[ \sum_{t=1}^{T} \delta^{t-1} u_t(\mathsf{s}_t, a_t^{\pi}(\mathsf{s}_t)) \right]$$

#### **Core economics**

- Rational expectations
- Exponential discounting
- Time-separability

# **Mathematical formulation**

# **Dynamic programming**

## **Policy evaluation**

$$v_t^{\pi}(s_t) = \mathsf{E}_{s_t}^{\pi} \left[ \sum_{j=0}^{T-t} \delta^j \, u_{t+j}(s_{t+j}, \alpha_{t+j}^{\pi}(s_{t+j})) \right]$$

# **Optimality equations**

$$v_t^{\pi^*}(s_t) = \max_{a_t \in A} \left\{ u_t(s_t, a_t) + \delta E_{s_t}^{\pi^*} \left[ v_{t+1}^{\pi^*}(s_{t+1}) \right] \right\}$$

# **Backward induction algorithm**

```
for t = T, \dots, 1 do
      ift = Tthen
             v_T^{\pi^*}(s_T) = \max_{\alpha_T \in A} \left\{ u_T(s_T, \alpha_T) \right\} \quad \forall s_T \in S
      else
             Compute v_t^{\pi^*}(s_t) for each s_t \in S by
                      v_t^{\pi^*}(s_t) = \max_{\alpha_t \in \Delta} \left\{ u_t(s_t, \alpha_t) + \delta E_{s_t}^{\pi} \left[ v_{t+1}^{\pi^*}(s_{t+1}) \right] \right\}
             and set
                       a_t^{\pi^*}(s_t) = \arg\max_{s,t} \left\{ u_t(s_t, a_t) + \delta E_{s_t}^{\pi} \left[ v_{t+1}^{\pi^*}(s_{t+1}) \right] \right\}
      end if
end for
```

# Calibration procedure

## **Data**

#### **Dataset**

$$\mathcal{D} = \{a_{it}, \bar{s}_{it}, \bar{u}_{it} : i = 1, ..., N; t = 1, ..., T_i\}$$

#### State variables

- $s_t = (\bar{s}_t, \varepsilon_t)$ 
  - $\bar{s}_t$  observed
  - $\varepsilon_t$  unobserved

#### **Procedures**

#### Likelihood-based

$$\hat{\theta} = \arg \max_{\theta \in \Theta} \prod_{i=1}^{N} \prod_{t=1}^{r_i} p_{it}(\alpha_{it}, \bar{u}_{it} \mid \bar{s}_{it}, \theta)$$

#### Simulation-based

$$\hat{\vartheta} = \arg\min_{\vartheta \in \Theta} \left( M_D - M_S(\vartheta) \right)' W \left( M_D - M_S(\vartheta) \right)$$

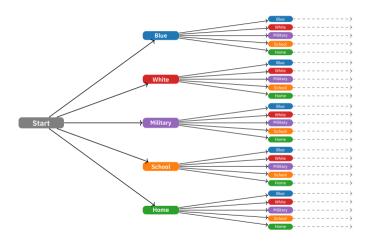
# Example

# Seminal paper

Michael P Keane and Kenneth I Wolpin. 1997. "The Career Decisions of Young Men." *Journal of Political Economy* 105 (3): 473–522.

- The study follows individuals over their working life from young adulthood at age 16 to retirement at age 65 where the decision period t = 16, ..., 65 is a school year.
- Individuals decide  $\alpha \in \mathcal{A}$  whether to work in a blue-collar or white-collar occupation  $(\alpha = 1, 2)$ , to serve in the military  $(\alpha = 3)$ , to attend school  $(\alpha = 4)$ , or to stay at home  $(\alpha = 5)$ .

# **Decision tree**



# **Immediate utility**

$$u_t(s_t) = \begin{cases} \zeta_a(s_t) + w_a(s_t) & \text{if } a \in \{1, 2, 3\} \\ \zeta_a(s_t) & \text{if } a \in \{4, 5\} \end{cases}$$

# Informed by reduced-form evidence

- Mincer equation
- Sheepskin effects
- Skill depreciation
- Mobility and search costs
- Monetary and psychic cost of schooling

#### **Transitions**

• Work experience  $k_t$  and years of completed schooling  $h_t$  evolve deterministically.

$$k_{a,t+1} = k_{a,t} + 1[a_t = a]$$
 if  $a \in \{1, 2, 3\}$   
 $h_{t+1} = h_t + 1[a_t = 4]$ 

- Productivity shocks  $\varepsilon_t$  are uncorrelated across time and follow a multivariate normal distribution with mean **0** and covariance matrix  $\Sigma$ .
- Given the structure of the utility functions and the distribution of the shocks, the state at time t is  $s_t = \{k_t, h_t, t, \alpha_{t-1}, e, \varepsilon_t\}$ .

# **Utility of blue-collar occupation**

Non-pecuniary

$$\zeta_{1}(\cdot) = \alpha_{1} + c_{1,1} \cdot \mathbf{1}[a_{t-1} \neq 1] + c_{1,2} \cdot \mathbf{1}[k_{1,t} = 0]$$
  
+  $\vartheta_{1} \cdot \mathbf{1}[h_{t} \geq 12] + \vartheta_{2} \cdot \mathbf{1}[h_{t} \geq 16] + \vartheta_{3} \cdot \mathbf{1}[k_{3,t} = 1]$ 

Wage component

$$w_1(\cdot)=r_1\,x_1(\cdot),$$

where  $x_1(\cdot)$  is the occupation-specific skill level.

# Skill production for blue-collar occupation

$$x_1(\cdot) = \exp\left(\Gamma_1(\mathbf{k}_t, h_t, t, \alpha_{t-1}, e_{j,1}) \cdot \varepsilon_{1,t}\right)$$

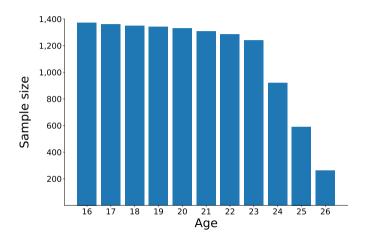
• Parameterization of the deterministic component of the skill production function:

$$\begin{split} \Gamma_{1}(\cdot) &= e_{j,1} + \beta_{1,1} \cdot h_{t} + \beta_{1,2} \cdot \mathbf{1}[h_{t} \geq 12] + \beta_{1,3} \cdot \mathbf{1}[h_{t} \geq 16] \\ &+ \gamma_{1,1} \cdot k_{1,t} + \gamma_{1,2} \cdot (k_{1,t})^{2} + \gamma_{1,3} \cdot \mathbf{1}[k_{1,t} > 0] \\ &+ \gamma_{1,4} \cdot t + \gamma_{1,5} \cdot \mathbf{1}[t < 18] \\ &+ \gamma_{1,6} \cdot \mathbf{1}[\alpha_{t-1} = 1] + \gamma_{1,7} \cdot k_{2,t} + \gamma_{1,8} \cdot k_{3,t} \end{split}$$

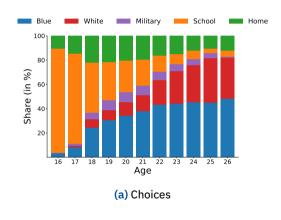
# **National Longitudinal Survey of Youth 1979**

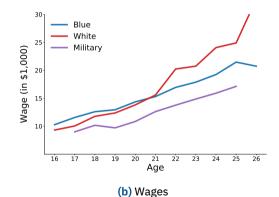
- 1,373 individuals starting at age 16
- Life cycle histories
  - School attendance
  - Occupation-specific work status
  - Wages

# Sample size

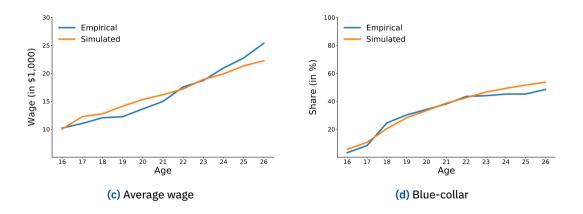


# **Data descriptives**

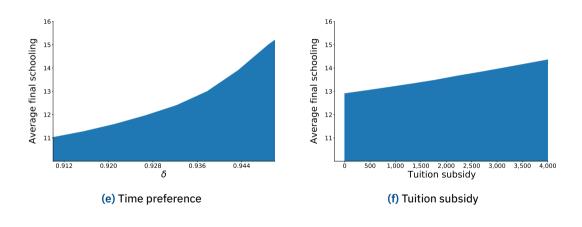




#### **Calibration results**



# **Economic insights**



# **Pipeline**

## **Tooling**

### respy

GitHub OpenSourceEconomics/respy

Docs respy.readthedocs.io

## estimagic

GitHub OpenSourceEconomics/estimagic

Docs estimagic.readthedocs.io

#### Workflow

```
import respy as rp
from estimagic import maximize
# obtain model input
params, options, df = rp.get example model("kw 97 extended respy")
# process model specification
log_like = rp.get_log_like_func(params, options, df)
simulate = rp.get simulate func(params, options)
# perform calibration
results, params rslt = maximize(log like, params, "nlopt bobyga")
# conduct analysis
df rslt = simulate(params rslt)
```

## **Model parameterization**

		value	name
category	name		
delta	delta	9.370735e-01	delta_delta
wage_white_collar	constant	8.741888e+00	wage_white_collar_constant
	exp_school	6.548940e-02	wage_white_collar_exp_school
	exp_white_collar	1.763655e-02	wage_white_collar_exp_white_collar
	exp_white_collar_square	-4.215936e-02	wage_white_collar_exp_white_collar_square
	exp_blue_collar	3.431936e-02	wage_white_collar_exp_blue_collar
	exp_military	1.406945e-02	wage_white_collar_exp_military
	hs_graduate	-3.599855e-03	wage_white_collar_hs_graduate
	co_graduate	2.301313e-03	wage_white_collar_co_graduate
	period	9.577717e-03	wage_white_collar_period
	is_minor	-1.509984e-01	wage_white_collar_is_minor

## **Model options**

	value
estimation_draws	200
estimation_seed	500
estimation_tau	500
interpolation_points	-1
n_periods	50
simulation_agents	5000
simulation_seed	132
solution_draws	500
solution_seed	456
monte_carlo_sequence	random
covariates {'hs_graduate': 'exp_school >= 12', 'co_gradua	

# **Projects**

#### **Economics and data**

- Biased expectations
- Incorporate subjective expectations
  Collaboration with DIW for SOEP-IS data collection

- Robust decisions
- Option value

#### **Economics and data**

- Biased expectations
- Robust decisions

Account for ubiquitous uncertainties

Option value

Robust decision in light of model misspecification

#### **Economics and data**

- Biased expectations
- Robust decisions
- Option value

Schooling reform for identification and validation Collaboration with Statistics Norway

### Computation

- Uncertainty quantification Capture parametric uncertainty

  Assess competing policy implications
- · Global optimization
- HPC implementation

## Computation

Uncertainty quantification

Global optimization

Explore estimation uncertainty

HPC implementation

Acknowledge multiplicity of local minima

### Computation

- · Uncertainty quantification
- · Global optimization
- HPC implementation

Enable increased realism and auditing of economic models Exploit large-scale parallelism on supercomputers

# Conclusion

## Join us!



http://bit.ly/ose-github



http://bit.ly/ose-zulip



https://twitter.com/open\_econ



https://open-econ.org



Open Source Economics



respy



econsa

# References

#### References

- Aguirregabiria, Victor, and Pedro Mira. 2010. "Dynamic Discrete Choice Structural Models: A survey." *Journal of Econometrics* 156 (1): 38–67.
- Becker, Gary S. 1964. Human Capital. New York City, NY: Columbia University Press.
- **Bellman, Richard E.** 1954. "The theory of dynamic programming." *Bulletin of the American Mathematical Society* 60 (6): 503–15.
- Keane, Michael P, and Kenneth I Wolpin. 1997. "The Career Decisions of Young Men." *Journal of Political Economy* 105 (3): 473–522. [PDF p. 25]
- Keane, Micheal P, and Kenneth I Wolpin. 1994. "The Solution and Estimation of Discrete Choice Dynamic Programming Models by Simulation and Interpolation: Monte Carlo Evidence." Review of Economics and Statistics 76 (4): 648–72.
- Puterman, Martin L. 1994. Markov Decision Processes: Discrete Stochastic Dynamic Programming. New York City, NY: John Wiley & Sons.
- White, D. J. 1993. Markov Decision Processes. New York City, NY: John Wiley & Sons.
- Wolpin, Kenneth I. 2013. The Limits to Inference without Theory. Cambridge, MA: MIT University Press.