An invitation for transdisciplinary collaboration

The OSE team

May 18, 2021



Computational modeling in economics

Motivation

- Facilitate academic rigor
- Study mechanisms
- Predict public policies

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- Predict public policies

Transdisciplinary in nature

- Economic model
- Mathematical framework
- Computational implementation

Understanding individual decisions

- Human capital investment
- Consumption—savings decision

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Predicting effects of policies

- Welfare programs
- Tax schedules

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- Finite-horizon discrete Markov decision problem
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- ⇒ Transdisciplinary research on their **economics**, data, and computation

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Partners













Roadmap

- Economic model
- Mathematical formulation
- Calibration

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- · Mathematical formulation
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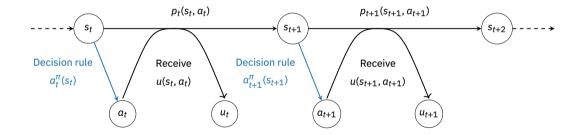
- Example
- Pipeline
- Projects

Economic model

Decision problem

$t = 1, \ldots, T$	decision period
$s_t \in S$	state
$a_t \in \mathcal{A}$	action
$p_t(s_t, a_t)$	conditional distribution
$a_t(s_t)$	decision rule
$\pi=(\alpha_1^\pi(s_1),\ldots,\alpha_T^\pi(s_T))$	policy
$u_t(s_t, \alpha_t)$	immediate utility
δ	discount factor

Timing of events



Individual's objective

$$\max_{\pi \in \Pi} \mathsf{E}_{\mathsf{s}_1}^{\pi} \left[\sum_{t=1}^{T} \delta^{t-1} u_t(\mathsf{s}_t, \alpha_t^{\pi}(\mathsf{s}_t)) \right]$$

Core economics

- Rational expectations
- Exponential discounting
- Time-separability

Mathematical formulation

Dynamic programming

Policy evaluation

$$v_t^{\pi}(s_t) = \mathsf{E}_{s_t}^{\pi} \left[\sum_{j=0}^{T-t} \delta^j \, u_{t+j}(s_{t+j}, \alpha_{t+j}^{\pi}(s_{t+j})) \right]$$

Optimality equations

$$v_t^{\pi^*}(s_t) = \max_{a_t \in A} \left\{ u_t(s_t, a_t) + \delta E_{s_t}^{\pi^*} \left[v_{t+1}^{\pi^*}(s_{t+1}) \right] \right\}$$

Backward induction algorithm

```
for t = T, \dots, 1 do
       ift = T then
             v_T^{\pi^*}(s_T) = \max_{\alpha_T \in A} \left\{ u_T(s_T, \alpha_T) \right\} \quad \forall s_T \in S
       else
              Compute v_t^{\pi^*}(s_t) for each s_t \in S by
                      v_t^{\pi^*}(s_t) = \max_{\alpha_t \in \Delta} \left\{ u_t(s_t, \alpha_t) + \delta E_{s_t}^{\pi} \left[ v_{t+1}^{\pi^*}(s_{t+1}) \right] \right\}
              and set
                       a_t^{\pi^*}(s_t) = \arg\max_{s,t} \left\{ u_t(s_t, a_t) + \delta E_{s_t}^{\pi} \left[ v_{t+1}^{\pi^*}(s_{t+1}) \right] \right\}
       end if
end for
```

Calibration procedure

Data

Dataset

$$\mathcal{D} = \{a_{it}, \bar{s}_{it}, \bar{u}_{it} : i = 1, ..., N; t = 1, ..., T_i\}$$

State variables

- $s_t = (\bar{s}_t, \varepsilon_t)$
 - \bar{s}_t observed
 - ε_t unobserved

Procedures

Likelihood-based

$$\hat{\theta} = \arg \max_{\theta \in \Theta} \prod_{i=1}^{N} \prod_{t=1}^{T_i} p_{it}(a_{it}, \bar{u}_{it} \mid \bar{s}_{it}, \theta)$$

Simulation-based

$$\hat{\theta} = \arg\min_{\theta \in \Theta} \left(M_D - M_S(\theta) \right)' W \left(M_D - M_S(\theta) \right)$$

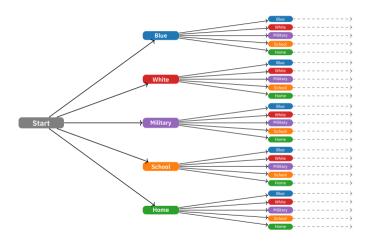
Example

Seminal paper

Michael P. Keane and Kenneth I. Wolpin. 1997. "The career decisions of young men." *Journal of Political Economy* 105 (3): 473–522.

- The study follows individuals over their working life from young adulthood at age 16 to retirement at age 65 where the decision period $t = 16, \ldots, 65$ is a school year.
- Individuals decide $a \in \mathcal{A}$ whether to work in a blue-collar or white-collar occupation (a = 1, 2), to serve in the military (a = 3), to attend school (a = 4), or to stay at home (a = 5).

Decision tree



Immediate utility

$$u_{\alpha}(s_t) = \begin{cases} \zeta_{\alpha}(s_t) + w_{\alpha}(s_t) & \text{if } \alpha \in \{1, 2, 3\} \\ \zeta_{\alpha}(s_t) & \text{if } \alpha \in \{4, 5\} \end{cases}$$

Informed by reduced-form evidence

- Mincer equation
- Sheepskin effects
- Skill depreciation
- Mobility and search costs
- Monetary and psychic cost of schooling

Transitions

• Work experience k_t and years of completed schooling h_t evolve deterministically.

$$k_{a,t+1} = k_{a,t} + 1[a_t = a]$$
 if $a \in \{1, 2, 3\}$
 $h_{t+1} = h_t + 1[a_t = 4]$

- Productivity shocks ε_t are uncorrelated across time and follow a multivariate normal distribution with mean **0** and covariance matrix Σ .
- Given the structure of the utility functions and the distribution of the shocks, the state at time t is $s_t = \{k_t, h_t, t, \alpha_{t-1}, e, \varepsilon_t\}$.

Utility of blue-collar occupation

Non-pecuniary

$$\begin{aligned} \zeta_1(\cdot) &= \alpha_1 + c_{1,1} \cdot \mathbf{1}[a_{t-1} \neq 1] + c_{1,2} \cdot \mathbf{1}[k_{1,t} = 0] \\ &+ \vartheta_1 \cdot \mathbf{1}[h_t \geq 12] + \vartheta_2 \cdot \mathbf{1}[h_t \geq 16] + \vartheta_3 \cdot \mathbf{1}[k_{3,t} = 1] \end{aligned}$$

Wage component

$$w_1(\cdot)=r_1\,x_1(\cdot),$$

where $x_1(\cdot)$ is the occupation-specific skill level.

Skill production for blue-collar occupation

$$x_1(\cdot) = \left(\Gamma_1(\mathbf{k}_t, h_t, t, a_{t-1}, e_{j,1}) \cdot \varepsilon_{1,t}\right)$$

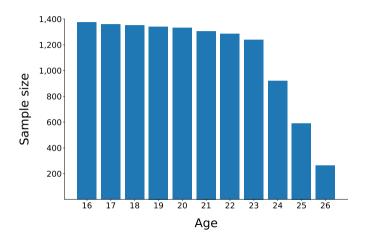
• Parameterization of the deterministic component of the skill production function:

$$\begin{split} \Gamma_{1}(\cdot) &= e_{j,1} + \beta_{1,1} \cdot h_{t} + \beta_{1,2} \cdot \mathbf{1}[h_{t} \geq 12] + \beta_{1,3} \cdot \mathbf{1}[h_{t} \geq 16] \\ &+ \gamma_{1,1} \cdot k_{1,t} + \gamma_{1,2} \cdot (k_{1,t})^{2} + \gamma_{1,3} \cdot \mathbf{1}[k_{1,t} > 0] \\ &+ \gamma_{1,4} \cdot t + \gamma_{1,5} \cdot \mathbf{1}[t < 18] \\ &+ \gamma_{1,6} \cdot \mathbf{1}[\alpha_{t-1} = 1] + \gamma_{1,7} \cdot k_{2,t} + \gamma_{1,8} \cdot k_{3,t} \end{split}$$

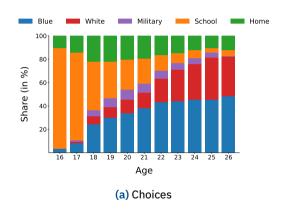
National Longitudinal Survey of Youth 1979

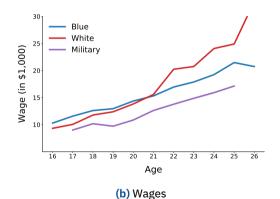
- 1,373 individuals starting at age 16
- Life cycle histories
 - School attendance
 - Occupation-specific work status
 - Wages

Sample size

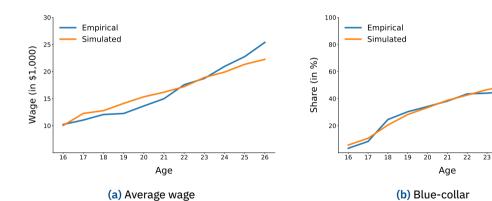


Data descriptives



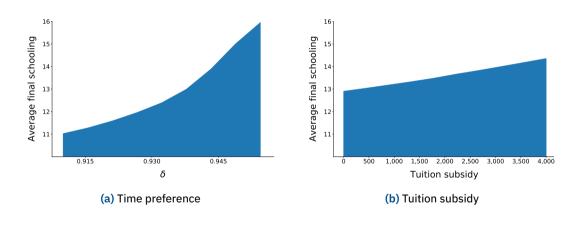


Calibration results



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Economic insights



Pipeline

Tooling

respy

GitHub OpenSourceEconomics/respy

Docs respy.readthedocs.io

estimagic

GitHub OpenSourceEconomics/estimagic

Docs estimagic.readthedocs.io

Workflow

```
import respy as rp
from estimagic import maximize
# obtain model input
params, options, df = rp.get example model("kw 97 extended respy")
# process model specification
log_like = rp.get_log_like_func(params, options, df)
simulate = rp.get simulate func(params, options)
# perform calibration
results, params rslt = maximize(log like, params, "nlopt bobyga")
# conduct analysis
df rslt = simulate(params rslt)
```

Model parameterization

		value	name
category	name		
delta	delta	9.370735e-01	delta_delta
wage_white_collar	constant	8.741888e+00	wage_white_collar_constant
	exp_school	6.548940e-02	wage_white_collar_exp_school
	exp_white_collar	1.763655e-02	wage_white_collar_exp_white_collar
	exp_white_collar_square	-4.215936e-02	wage_white_collar_exp_white_collar_square
	exp_blue_collar	3.431936e-02	wage_white_collar_exp_blue_collar
	exp_military	1.406945e-02	wage_white_collar_exp_military
	hs_graduate	-3.599855e-03	wage_white_collar_hs_graduate
	co_graduate	2.301313e-03	wage_white_collar_co_graduate
	period	9.577717e-03	wage_white_collar_period
	is_minor	-1.509984e-01	wage_white_collar_is_minor

Model options

	value	
estimation_draws	200	
estimation_seed	500	
estimation_tau	500	
interpolation_points	-1	
n_periods	50	
simulation_agents	5000	
simulation_seed	132	
solution_draws	500	
solution_seed	456	
monte_carlo_sequence	random	
covariates	{'hs_graduate': 'exp_school >= 12', 'co_gradua	

Projects

Economics and data

- Biased expectations
- Incorporate subjective expectations
 Collaboration with DIW for SOEP-IS data collection

- Robust decisions
- Option value

Economics and data

- Biased expectations
- Robust decisions

Account for ubiquitous uncertainties

Option value

Robust decision in light of model misspecification

Economics and data

- Biased expectations
- Robust decisions
- Option value

Schooling reform for identification and validation Collaboration with Statistics Norway

Computation

- Uncertainty quantification Capture parametric uncertainty

 Assess competing policy implications
- · Global optimization
- HPC implementation

Computation

- Uncertainty quantification
- Global optimization

Explore estimation uncertainty

HPC implementation

Acknowledge multiplicity of local minima

Computation

- · Uncertainty quantification
- · Global optimization
- HPC implementation

Enable increased realism and auditing of economic models Exploit large-scale parallelism on supercomputers

Conclusion

Join us!



http://bit.ly/ose-github



http://bit.ly/ose-zulip



https://twitter.com/open_econ



https://open-econ.org



Open Source Economics



respy



econsa

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