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~~Settlers of Catan~~ A board game is played on a hexagonal grid of 19 tiles. A 'traveler' token starts on the center tile. Each turn a die is rolled to determine what neighboring tile the traveler moves to (all six directions equally likely). The turn that the traveler leaves the board, the game ends. What is the expected number of turns of the game?

A diagram showing a central cluster of 19 hexagonal cells, numbered 0 to 18, arranged in a hexagonal pattern. The cells are surrounded by 21 green dots, numbered 19 to 39, which are arranged in a larger hexagonal pattern around the central cluster. The central cell is labeled 0. The cells are numbered 1 through 18 in a hexagonal arrangement around the center. The green dots are numbered 19 through 39, with 19 at the top and 39 at the bottom.

The dice is truly random, so there is no upper bound on N . We note that this game is really akin to a Markov chain, in that it doesn't matter what the past states are.

[illegible]

$$t = N\mathbf{1}$$
[illegible]

Finally, we see that $t_0 = \boxed{\frac{213}{29} \approx 7.345}$