

Let $X_i \in [0, 36]$ be the current state, or position of the traveler. The traveler always starts at position $X_0 = 0$. The final state must be $X_N \in [19, 36]$.

§3.2 Transition Matrix

Now that we've defined some notation, we can write the transition matrix P . Because a 37×37 matrix is cumbersome, we combine the states $[19, 36]$ into a

$$P = \begin{pmatrix} p_{0,0} = 0 & p_{0,1} = \frac{1}{6} & p_{0,2} = \frac{1}{6} & p_{0,3} = \frac{1}{6} & p_{0,4} = \frac{1}{6} & p_{0,5} = \frac{1}{6} & p_{0,6} = \frac{1}{6} & p_{0,7} = 0 & p_{0,8} = 0 & p_{0,9} = 0 & p_{0,10} = 0 & p_{0,11} = 0 & p_{0,12} = 0 & p_{0,13} = 0 & p_{0,14} = 0 & p_{0,15} = 0 & p_{0,16} = 0 & p_{0,17} = 0 & p_{0,18} = 0 & p_{0,19} = 0 \\ p_{1,0} = \frac{1}{6} & p_{1,1} = 0 & p_{1,2} = \frac{1}{6} & p_{1,3} = 0 & p_{1,4} = 0 & p_{1,5} = 0 & p_{1,6} = \frac{1}{6} & p_{1,7} = \frac{1}{6} & p_{1,8} = \frac{1}{6} & p_{1,9} = \frac{1}{6} & p_{1,10} = 0 & p_{1,11} = 0 & p_{1,12} = 0 & p_{1,13} = 0 & p_{1,14} = 0 & p_{1,15} = 0 & p_{1,16} = 0 & p_{1,17} = 0 & p_{1,18} = 0 & p_{1,19} = 0 \\ p_{2,0} = 0 & p_{2,1} = \frac{1}{6} & p_{2,2} = 0 & p_{2,3} = \frac{1}{6} & p_{2,4} = 0 & p_{2,5} = 0 & p_{2,6} = 0 & p_{2,7} = 0 & p_{2,8} = 0 & p_{2,9} = \frac{1}{6} & p_{2,10} = \frac{1}{6} & p_{2,11} = \frac{1}{6} & p_{2,12} = 0 & p_{2,13} = 0 & p_{2,14} = 0 & p_{2,15} = 0 & p_{2,16} = 0 & p_{2,17} = 0 & p_{2,18} = 0 & p_{2,19} = 0 \\ p_{3,0} = \frac{1}{6} & p_{3,1} = 0 & p_{3,2} = \frac{1}{6} & p_{3,3} = 0 & p_{3,4} = \frac{1}{6} & p_{3,5} = 0 & p_{3,6} = 0 & p_{3,7} = 0 & p_{3,8} = 0 & p_{3,9} = 0 & p_{3,10} = 0 & p_{3,11} = \frac{1}{6} & p_{3,12} = \frac{1}{6} & p_{3,13} = \frac{1}{6} & p_{3,14} = 0 & p_{3,15} = 0 & p_{3,16} = 0 & p_{3,17} = 0 & p_{3,18} = 0 & p_{3,19} = 0 \\ p_{4,0} = 0 & p_{4,1} = 0 & p_{4,2} = 0 & p_{4,3} = \frac{1}{6} & p_{4,4} = 0 & p_{4,5} = \frac{1}{6} & p_{4,6} = 0 & p_{4,7} = 0 & p_{4,8} = 0 & p_{4,9} = 0 & p_{4,10} = 0 & p_{4,11} = 0 & p_{4,12} = 0 & p_{4,13} = \frac{1}{6} & p_{4,14} = \frac{1}{6} & p_{4,15} = \frac{1}{6} & p_{4,16} = 0 & p_{4,17} = 0 & p_{4,18} = 0 & p_{4,19} = 0 \\ p_{5,0} = \frac{1}{6} & p_{5,1} = 0 & p_{5,2} = 0 & p_{5,3} = 0 & p_{5,4} = \frac{1}{6} & p_{5,5} = 0 & p_{5,6} = \frac{1}{6} & p_{5,7} = 0 & p_{5,8} = 0 & p_{5,9} = 0 & p_{5,10} = 0 & p_{5,11} = 0 & p_{5,12} = 0 & p_{5,13} = 0 & p_{5,14} = 0 & p_{5,15} = \frac{1}{6} & p_{5,16} = \frac{1}{6} & p_{5,17} = \frac{1}{6} & p_{5,18} = 0 & p_{5,19} = 0 \\ p_{6,0} = \frac{1}{6} & p_{6,1} = \frac{1}{6} & p_{6,2} = 0 & p_{6,3} = 0 & p_{6,4} = 0 & p_{6,5} = \frac{1}{6} & p_{6,6} = 0 & p_{6,7} = 0 & p_{6,8} = 0 & p_{6,9} = 0 & p_{6,10} = 0 & p_{6,11} = 0 & p_{6,12} = 0 & p_{6,13} = 0 & p_{6,14} = 0 & p_{6,15} = 0 & p_{6,16} = 0 & p_{6,17} = \frac{1}{6} & p_{6,18} = \frac{1}{6} & p_{6,19} = 0 \\ p_{7,0} = 0 & p_{7,1} = 0 & p_{7,2} = 0 & p_{7,3} = 0 & p_{7,4} = 0 & p_{7,5} = 0 & p_{7,6} = \frac{1}{6} & p_{7,7} = 0 & p_{7,8} = \frac{1}{6} & p_{7,9} = 0 & p_{7,10} = 0 & p_{7,11} = 0 & p_{7,12} = 0 & p_{7,13} = 0 & p_{7,14} = 0 & p_{7,15} = 0 & p_{7,16} = 0 & p_{7,17} = 0 & p_{7,18} = \frac{1}{6} & p_{7,19} = \frac{1}{6} \\ p_{8,0} = 0 & p_{8,1} = \frac{1}{6} & p_{8,2} = 0 & p_{8,3} = 0 & p_{8,4} = 0 & p_{8,5} = 0 & p_{8,6} = 0 & p_{8,7} = \frac{1}{6} & p_{8,8} = 0 & p_{8,9} = \frac{1}{6} & p_{8,10} = 0 & p_{8,11} = 0 & p_{8,12} = 0 & p_{8,13} = 0 & p_{8,14} = 0 & p_{8,15} = 0 & p_{8,16} = 0 & p_{8,17} = 0 & p_{8,18} = 0 & p_{8,19} = 0 \\ p_{9,0} = 0 & p_{9,1} = 0 & p_{9,2} = \frac{1}{6} & p_{9,3} = 0 & p_{9,4} = 0 & p_{9,5} = 0 & p_{9,6} = 0 & p_{9,7} = 0 & p_{9,8} = \frac{1}{6} & p_{9,9} = 0 & p_{9,10} = \frac{1}{6} & p_{9,11} = 0 & p_{9,12} = 0 & p_{9,13} = 0 & p_{9,14} = 0 & p_{9,15} = 0 & p_{9,16} = 0 & p_{9,17} = 0 & p_{9,18} = 0 & p_{9,19} = 0 \\ p_{10,0} = 0 & p_{10,1} = 0 & p_{10,2} = \frac{1}{6} & p_{10,3} = 0 & p_{10,4} = 0 & p_{10,5} = 0 & p_{10,6} = 0 & p_{10,7} = 0 & p_{10,8} = 0 & p_{10,9} = \frac{1}{6} & p_{10,10} = \frac{1}{6} & p_{10,11} = \frac{1}{6} & p_{10,12} = 0 & p_{10,13} = 0 & p_{10,14} = 0 & p_{10,15} = 0 & p_{10,16} = 0 & p_{10,17} = 0 & p_{10,18} = 0 & p_{10,19} = 0 \\ p_{11,0} = 0 & p_{11,1} = 0 & p_{11,2} = \frac{1}{6} & p_{11,3} = \frac{1}{6} & p_{11,4} = 0 & p_{11,5} = 0 & p_{11,6} = 0 & p_{11,7} = 0 & p_{11,8} = 0 & p_{11,9} = 0 & p_{11,10} = 0 & p_{11,11} = 0 & p_{11,12} = 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p_{14,11} = 0 & p_{14,12} = 0 & p_{14,13} = \frac{1}{6} & p_{14,14} = 0 & p_{14,$$

We also write the matrix Q , which doesn't have any absorbing states.

$$Q = \begin{pmatrix} P_{0,0} = 0 & P_{0,1} = \frac{1}{6} & P_{0,2} = \frac{1}{6} & P_{0,3} = \frac{1}{6} & P_{0,4} = \frac{1}{6} & P_{0,5} = \frac{1}{6} & P_{0,6} = \frac{1}{6} & P_{0,7} = 0 & P_{0,8} = 0 & P_{0,9} = 0 & P_{0,10} = 0 & P_{0,11} = 0 & P_{0,12} = 0 & P_{0,13} = 0 & P_{0,14} = 0 & P_{0,15} = 0 & P_{0,16} = 0 & P_{0,17} = 0 & P_{0,18} = 0 \\ P_{1,0} = \frac{1}{6} & P_{1,1} = 0 & P_{1,2} = \frac{1}{6} & P_{1,3} = 0 & P_{1,4} = 0 & P_{1,5} = 0 & P_{1,6} = \frac{1}{6} & P_{1,7} = \frac{1}{6} & P_{1,8} = \frac{1}{6} & P_{1,9} = \frac{1}{6} & P_{1,10} = 0 & P_{1,11} = 0 & P_{1,12} = 0 & P_{1,13} = 0 & P_{1,14} = 0 & P_{1,15} = 0 & P_{1,16} = 0 & P_{1,17} = 0 & P_{1,18} = 0 \\ P_{2,0} = \frac{1}{6} & P_{2,1} = \frac{1}{6} & P_{2,2} = 0 & P_{2,3} = \frac{1}{6} & P_{2,4} = 0 & P_{2,5} = 0 & P_{2,6} = 0 & P_{2,7} = 0 & P_{2,8} = 0 & P_{2,9} = \frac{1}{6} & P_{2,10} = \frac{1}{6} & P_{2,11} = \frac{1}{6} & P_{2,12} = 0 & P_{2,13} = 0 & P_{2,14} = 0 & P_{2,15} = 0 & P_{2,16} = 0 & P_{2,17} = 0 & P_{2,18} = 0 \\ P_{3,0} = \frac{1}{6} & P_{3,1} = 0 & P_{3,2} = \frac{1}{6} & P_{3,3} = 0 & P_{3,4} = \frac{1}{6} & P_{3,5} = 0 & P_{3,6} = 0 & P_{3,7} = 0 & P_{3,8} = 0 & P_{3,9} = 0 & P_{3,10} = 0 & P_{3,11} = \frac{1}{6} & P_{3,12} = \frac{1}{6} & P_{3,13} = \frac{1}{6} & P_{3,14} = 0 & P_{3,15} = 0 & P_{3,16} = 0 & P_{3,17} = 0 & P_{3,18} = 0 \\ P_{4,0} = \frac{1}{6} & P_{4,1} = 0 & P_{4,2} = 0 & P_{4,3} = \frac{1}{6} & P_{4,4} = 0 & P_{4,5} = \frac{1}{6} & P_{4,6} = 0 & P_{4,7} = 0 & P_{4,8} = 0 & P_{4,9} = 0 & P_{4,10} = 0 & P_{4,11} = 0 & P_{4,12} = 0 & P_{4,13} = \frac{1}{6} & P_{4,14} = \frac{1}{6} & P_{4,15} = \frac{1}{6} & P_{4,16} = 0 & P_{4,17} = 0 & P_{4,18} = 0 \\ P_{5,0} = \frac{1}{6} & P_{5,1} = 0 & P_{5,2} = 0 & P_{5,3} = 0 & P_{5,4} = \frac{1}{6} & P_{5,5} = 0 & P_{5,6} = \frac{1}{6} & P_{5,7} = 0 & P_{5,8} = 0 & P_{5,9} = 0 & P_{5,10} = 0 & P_{5,11} = 0 & P_{5,12} = 0 & P_{5,13} = 0 & P_{5,14} = 0 & P_{5,15} = \frac{1}{6} & P_{5,16} = \frac{1}{6} & P_{5,17} = \frac{1}{6} & P_{5,18} = 0 \\ P_{6,0} = 0 & P_{6,1} = \frac{1}{6} & P_{6,2} = 0 & P_{6,3} = 0 & P_{6,4} = 0 & P_{6,5} = \frac{1}{6} & P_{6,6} = 0 & P_{6,7} = \frac{1}{6} & P_{6,8} = 0 & P_{6,9} = 0 & P_{6,10} = 0 & P_{6,11} = 0 & P_{6,12} = 0 & P_{6,13} = 0 & P_{6,14} = 0 & P_{6,15} = 0 & P_{6,16} = 0 & P_{6,17} = 0 & P_{6,18} = \frac{1}{6} \\ P_{7,0} = 0 & P_{7,1} = \frac{1}{6} & P_{7,2} = 0 & P_{7,3} = 0 & P_{7,4} = 0 & P_{7,5} = 0 & P_{7,6} = \frac{1}{6} & P_{7,7} = 0 & P_{7,8} = \frac{1}{6} & P_{7,9} = \frac{1}{6} & P_{7,10} = 0 & P_{7,11} = 0 & P_{7,12} = 0 & P_{7,13} = 0 & P_{7,14} = 0 & P_{7,15} = 0 & P_{7,16} = 0 & P_{7,17} = 0 & P_{7,18} = \frac{1}{6} \\ P_{8,0} = 0 & P_{8,1} = 0 & P_{8,2} = 0 & P_{8,3} = 0 & P_{8,4} = 0 & P_{8,5} = 0 & P_{8,6} = 0 & P_{8,7} = \frac{1}{6} & P_{8,8} = 0 & P_{8,9} = \frac{1}{6} & P_{8,10} = 0 & P_{8,11} = 0 & P_{8,12} = 0 & P_{8,13} = 0 & P_{8,14} = 0 & P_{8,15} = 0 & P_{8,16} = 0 & P_{8,17} = 0 & P_{8,18} = 0 \\ P_{9,0} = 0 & P_{9,1} = \frac{1}{6} & P_{9,2} = \frac{1}{6} & P_{9,3} = 0 & P_{9,4} = 0 & P_{9,5} = 0 & P_{9,6} = 0 & P_{9,7} = 0 & P_{9,8} = \frac{1}{6} & P_{9,9} = 0 & P_{9,10} = \frac{1}{6} & P_{9,11} = 0 & P_{9,12} = 0 & P_{9,13} = 0 & P_{9,14} = 0 & P_{9,15} = 0 & P_{9,16} = 0 & P_{9,17} = 0 & P_{9,18} = 0 \\ P_{10,0} = 0 & P_{10,1} = 0 & P_{10,2} = 0 & P_{10,3} = 0 & P_{10,4} = 0 & P_{10,5} = 0 & P_{10,6} = 0 & P_{10,7} = 0 & P_{10,8} = 0 & P_{10,9} = \frac{1}{6} & P_{10,10} = \frac{1}{6} & P_{10,11} = \frac{1}{6} & P_{10,12} = 0 & P_{10,13} = 0 & P_{10,14} = 0 & P_{10,15} = 0 & P_{10,16} = 0 & P_{10,17} = 0 & P_{10,18} = 0 \\ P_{11,0} = 0 & P_{11,1} = 0 & P_{11,2} = \frac{1}{6} & P_{11,3} = \frac{1}{6} & P_{11,4} = 0 & P_{11,5} = 0 & P_{11,6} = 0 & P_{11,7} = 0 & P_{11,8} = 0 & P_{11,9} = 0 & P_{11,10} = \frac{1}{6} & P_{11,11} = 0 & P_{11,12} = \frac{1}{6} & P_{11,13} = 0 & P_{11,14} = 0 & P_{11,15} = 0 & P_{11,16} = 0 & P_{11,17} = 0 & P_{11,18} = 0 \\ P_{12,0} = 0 & P_{12,1} = 0 & P_{12,2} = 0 & P_{12,3} = \frac{1}{6} & P_{12,4} = 0 & P_{12,5} = 0 & P_{12,6} = 0 & P_{12,7} = 0 & P_{12,8} = 0 & P_{12,9} = 0 & P_{12,10} = 0 & P_{12,11} = \frac{1}{6} & P_{12,12} = 0 & P_{12,13} = \frac{1}{6} & P_{12,14} = 0 & P_{12,15} = 0 & P_{12,16} = 0 & P_{12,17} = 0 & P_{12,18} = 0 \\ P_{13,0} = 0 & P_{13,1} = 0 & P_{13,2} = 0 & P_{13,3} = \frac{1}{6} & P_{13,4} = \frac{1}{6} & P_{13,5} = 0 & P_{13,6} = 0 & P_{13,7} = 0 & P_{13,8} = 0 & P_{13,9} = 0 & P_{13,10} = 0 & P_{13,11} = 0 & P_{13,12} = \frac{1}{6} & P_{13,13} = 0 & P_{13,14} = \frac{1}{6} & P_{13,15} = 0 & P_{13,16} = 0 & P_{13,17} = 0 & P_{13,18} = 0 \\ P_{14,0} = 0 & P_{14,1} = 0 & P_{14,2} = 0 & P_{14,3} = 0 & P_{14,4} = \frac{1}{6} & P_{14,5} = 0 & P_{14,6} = 0 & P_{14,7} = 0 & P_{14,8} = 0 & P_{14,9} = 0 & P_{14,10} = 0 & P_{14,11} = 0 & P_{14,12} = 0 & P_{14,13} = \frac{1}{6} & P_{14,14} = \frac{1}{6} & P_{14,15} = \frac{1}{6} & P_{14,16} = 0 & P_{14,17} = 0 & P_{14,18} = 0 \\ P_{15,0} = 0 & P_{15,1} = 0 & P_{15,2} = 0 & P_{15,3} = 0 & P_{15,4} = \frac{1}{6} & P_{15,5} = \frac{1}{6} &$$

$N = (I - Q)^{-1}$ is known as the fundamental matrix of P .

$N =$	$P_{0,0} = \frac{45}{16}$		$P_{0,1} = \frac{16}{16}$		$P_{0,2} = \frac{16}{16}$		$P_{0,3} = \frac{16}{16}$		$P_{0,4} = \frac{16}{16}$		$P_{0,5} = \frac{16}{16}$		$P_{0,6} = \frac{16}{16}$		$P_{0,7} = \frac{16}{16}$		$P_{0,8} = \frac{16}{16}$		$P_{0,9} = \frac{16}{16}$		$P_{0,10} = \frac{16}{16}$		$P_{0,11} = \frac{16}{16}$		$P_{0,12} = \frac{16}{16}$		$P_{0,13} = \frac{16}{16}$		$P_{0,14} = \frac{16}{16}$		$P_{0,15} = \frac{16}{16}$		$P_{0,16} = \frac{16}{16}$		$P_{0,17} = \frac{16}{16}$		$P_{0,18} = \frac{16}{16}$		$P_{0,19} = \frac{16}{16}$		$P_{0,20} = \frac{16}{16}$		$P_{0,21} = \frac{16}{16}$		$P_{0,22} = \frac{16}{16}$		$P_{0,23} = \frac{16}{16}$		$P_{0,24} = \frac{16}{16}$		$P_{0,25} = \frac{16}{16}$		$P_{0,26} = \frac{16}{16}$		$P_{0,27} = \frac{16}{16}$		$P_{0,28} = \frac{16}{16}$		$P_{0,29} = \frac{16}{16}$		$P_{0,30} = \frac{16}{16}$		$P_{0,31} = \frac{16}{16}$		$P_{0,32} = \frac{16}{16}$		$P_{0,33} = \frac{16}{16}$		$P_{0,34} = \frac{16}{16}$		$P_{0,35} = \frac{16}{16}$		$P_{0,36} = \frac{16}{16}$		$P_{0,37} = \frac{16}{16}$		$P_{0,38} = \frac{16}{16}$		$P_{0,39} = \frac{16}{16}$		$P_{0,40} = \frac{16}{16}$		$P_{0,41} = \frac{16}{16}$		$P_{0,42} = \frac{16}{16}$		$P_{0,43} = \frac{16}{16}$		$P_{0,44} = \frac{16}{16}$		$P_{0,45} = \frac{16}{16}$		$P_{0,46} = \frac{16}{16}$		$P_{0,47} = \frac{16}{16}$		$P_{0,48} = \frac{16}{16}$		$P_{0,49} = \frac{16}{16}$		$P_{0,50} = \frac{16}{16}$		$P_{0,51} = \frac{16}{16}$		$P_{0,52} = \frac{16}{16}$		$P_{0,53} = \frac{16}{16}$		$P_{0,54} = \frac{16}{16}$		$P_{0,55} = \frac{16}{16}$		$P_{0,56} = \frac{16}{16}$		$P_{0,57} = \frac{16}{16}$		$P_{0,58} = \frac{16}{16}$		$P_{0,59} = \frac{16}{16}$		$P_{0,60} = \frac{16}{16}$		$P_{0,61} = \frac{16}{16}$		$P_{0,62} = \frac{16}{16}$		$P_{0,63} = \frac{16}{16}$		$P_{0,64} = \frac{16}{16}$		$P_{0,65} = \frac{16}{16}$		$P_{0,66} = \frac{16}{16}$		$P_{0,67} = \frac{16}{16}$		$P_{0,68} = \frac{16}{16}$		$P_{0,69} = \frac{16}{16}$		$P_{0,70} = \frac{16}{16}$		$P_{0,71} = \frac{16}{16}$		$P_{0,72} = \frac{16}{16}$		$P_{0,73} = \frac{16}{16}$		$P_{0,74} = \frac{16}{16}$		$P_{0,75} = \frac{16}{16}$		$P_{0,76} = \frac{16}{16}$		$P_{0,77} = \frac{16}{16}$		$P_{0,78} = \frac{16}{16}$		$P_{0,79} = \frac{16}{16}$		$P_{0,80} = \frac{16}{16}$		$P_{0,81} = \frac{16}{16}$		$P_{0,82} = \frac{16}{16}$		$P_{0,83} = \frac{16}{16}$		$P_{0,84} = \frac{16}{16}$		$P_{0,85} = \frac{16}{16}$		$P_{0,86} = \frac{16}{16}$		$P_{0,87} = \frac{16}{16}$		$P_{0,88} = \frac{16}{16}$		$P_{0,89} = \frac{16}{16}$		$P_{0,90} = \frac{16}{16}$		$P_{0,91} = \frac{16}{16}$		$P_{0,92} = \frac{16}{16}$		$P_{0,93} = \frac{16}{16}$		$P_{0,94} = \frac{16}{16}$		$P_{0,95} = \frac{16}{16}$		$P_{0,96}$
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$$t = N\mathbf{1}$$
[illegible]

Finally, we see that $t_0 = \boxed{\frac{213}{29} \approx 7.345}$