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~~Settlers of Catan~~ A board game is played on a hexagonal grid of 19 tiles. A 'traveler' token starts on the center tile. Each turn a die is rolled to determine what neighboring tile the traveler moves to (all six directions equally likely). The turn that the traveler leaves the board, the game ends. What is the expected number of turns of the game?

A hexagonal lattice graph with 36 nodes and 60 edges. The nodes are arranged in a honeycomb pattern. Nodes 0 through 29 are labeled with black numbers and have a red dot. Nodes 30 through 35 are labeled with green numbers and have a green dot. The nodes are arranged in a roughly circular shape with 6 nodes on each side.

$$\mathbb{E}(N) = \sum N \mathbb{P}(N)$$

Page 1 of 4

$N =$	$P_{0,0} = \frac{45}{16}$		$P_{0,1} = \frac{16}{16}$		$P_{0,2} = \frac{16}{16}$		$P_{0,3} = \frac{16}{16}$		$P_{0,4} = \frac{16}{16}$		$P_{0,5} = \frac{16}{16}$		$P_{0,6} = \frac{16}{16}$		$P_{0,7} = \frac{16}{16}$		$P_{0,8} = \frac{16}{16}$		$P_{0,9} = \frac{16}{16}$		$P_{0,10} = \frac{16}{16}$		$P_{0,11} = \frac{16}{16}$		$P_{0,12} = \frac{16}{16}$		$P_{0,13} = \frac{16}{16}$		$P_{0,14} = \frac{16}{16}$		$P_{0,15} = \frac{16}{16}$		$P_{0,16} = \frac{16}{16}$		$P_{0,17} = \frac{16}{16}$		$P_{0,18} = \frac{16}{16}$		$P_{0,19} = \frac{16}{16}$		$P_{0,20} = \frac{16}{16}$		$P_{0,21} = \frac{16}{16}$		$P_{0,22} = \frac{16}{16}$		$P_{0,23} = \frac{16}{16}$		$P_{0,24} = \frac{16}{16}$		$P_{0,25} = \frac{16}{16}$		$P_{0,26} = \frac{16}{16}$		$P_{0,27} = \frac{16}{16}$		$P_{0,28} = \frac{16}{16}$		$P_{0,29} = \frac{16}{16}$		$P_{0,30} = \frac{16}{16}$		$P_{0,31} = \frac{16}{16}$		$P_{0,32} = \frac{16}{16}$		$P_{0,33} = \frac{16}{16}$		$P_{0,34} = \frac{16}{16}$		$P_{0,35} = \frac{16}{16}$		$P_{0,36} = \frac{16}{16}$		$P_{0,37} = \frac{16}{16}$		$P_{0,38} = \frac{16}{16}$		$P_{0,39} = \frac{16}{16}$		$P_{0,40} = \frac{16}{16}$		$P_{0,41} = \frac{16}{16}$		$P_{0,42} = \frac{16}{16}$		$P_{0,43} = \frac{16}{16}$		$P_{0,44} = \frac{16}{16}$		$P_{0,45} = \frac{16}{16}$		$P_{0,46} = \frac{16}{16}$		$P_{0,47} = \frac{16}{16}$		$P_{0,48} = \frac{16}{16}$		$P_{0,49} = \frac{16}{16}$		$P_{0,50} = \frac{16}{16}$		$P_{0,51} = \frac{16}{16}$		$P_{0,52} = \frac{16}{16}$		$P_{0,53} = \frac{16}{16}$		$P_{0,54} = \frac{16}{16}$		$P_{0,55} = \frac{16}{16}$		$P_{0,56} = \frac{16}{16}$		$P_{0,57} = \frac{16}{16}$		$P_{0,58} = \frac{16}{16}$		$P_{0,59} = \frac{16}{16}$		$P_{0,60} = \frac{16}{16}$		$P_{0,61} = \frac{16}{16}$		$P_{0,62} = \frac{16}{16}$		$P_{0,63} = \frac{16}{16}$		$P_{0,64} = \frac{16}{16}$		$P_{0,65} = \frac{16}{16}$		$P_{0,66} = \frac{16}{16}$		$P_{0,67} = \frac{16}{16}$		$P_{0,68} = \frac{16}{16}$		$P_{0,69} = \frac{16}{16}$		$P_{0,70} = \frac{16}{16}$		$P_{0,71} = \frac{16}{16}$		$P_{0,72} = \frac{16}{16}$		$P_{0,73} = \frac{16}{16}$		$P_{0,74} = \frac{16}{16}$		$P_{0,75} = \frac{16}{16}$		$P_{0,76} = \frac{16}{16}$		$P_{0,77} = \frac{16}{16}$		$P_{0,78} = \frac{16}{16}$		$P_{0,79} = \frac{16}{16}$		$P_{0,80} = \frac{16}{16}$		$P_{0,81} = \frac{16}{16}$		$P_{0,82} = \frac{16}{16}$		$P_{0,83} = \frac{16}{16}$		$P_{0,84} = \frac{16}{16}$		$P_{0,85} = \frac{16}{16}$		$P_{0,86} = \frac{16}{16}$		$P_{0,87} = \frac{16}{16}$		$P_{0,88} = \frac{16}{16}$		$P_{0,89} = \frac{16}{16}$		$P_{0,90} = \frac{16}{16}$		$P_{0,91} = \frac{16}{16}$		$P_{0,92} = \frac{16}{16}$		$P_{0,93} = \frac{16}{16}$		$P_{0,94} = \frac{16}{16}$		$P_{0,95} = \frac{16}{16}$		$P_{0,96}$
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$$t = N\mathbf{1}$$
[illegible]

Finally, we see that $t_0 = \boxed{\frac{213}{29} \approx 7.345}$