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~~Settlers of Catan~~ A board game is played on a hexagonal grid of 19 tiles. A 'traveler' token starts on the center tile. Each turn a die is rolled to determine what neighboring tile the traveler moves to (all six directions equally likely). The turn that the traveler leaves the board, the game ends. What is the expected number of turns of the game?

A hexagonal grid of 36 cells, numbered 0 to 35. Cell 0 is the central cell. Cells 1 through 6 are in the first ring around cell 0. Cells 7 through 12 are in the second ring. Cells 13 through 18 are in the third ring. Cells 19 through 24 are in the fourth ring. Cells 25 through 30 are in the fifth ring. Cells 31 through 36 are in the sixth ring. Each cell contains a red dot and is surrounded by green dots.

$$\mathbb{E}(N) = \sum N \mathbb{P}(N)$$

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[illegible]

$$t = N\mathbf{1}$$
[illegible]

Finally, we see that  $t_0 = \boxed{\frac{213}{29} \approx 7.345}$