



Let  $X_i \in [0, 36]$  be the current state, or position of the traveler. The traveler always starts at position  $X_0 = 0$ . The final state must be  $X_N \in [19, 36]$ .

Now that we've defined some notation, we can write the transition matrix  $P$ . Because a  $37 \times 37$  matrix is cumbersome, we combine the states  $[19, 36]$  into a

$$P = \begin{pmatrix} p_{0,0} = 0 & p_{0,1} = \frac{1}{6} & p_{0,2} = \frac{1}{6} & p_{0,3} = \frac{1}{6} & p_{0,4} = \frac{1}{6} & p_{0,5} = \frac{1}{6} & p_{0,6} = \frac{1}{6} & p_{0,7} = 0 & p_{0,8} = 0 & p_{0,9} = 0 & p_{0,10} = 0 & p_{0,11} = 0 & p_{0,12} = 0 & p_{0,13} = 0 & p_{0,14} = 0 & p_{0,15} = 0 & p_{0,16} = 0 & p_{0,17} = 0 & p_{0,18} = 0 & p_{0,19} = 0 \\ p_{1,0} = \frac{1}{6} & p_{1,1} = 0 & p_{1,2} = \frac{1}{6} & p_{1,3} = 0 & p_{1,4} = 0 & p_{1,5} = \frac{1}{6} & p_{1,6} = \frac{1}{6} & p_{1,7} = \frac{1}{6} & p_{1,8} = \frac{1}{6} & p_{1,9} = \frac{1}{6} & p_{1,10} = 0 & p_{1,11} = 0 & p_{1,12} = 0 & p_{1,13} = 0 & p_{1,14} = 0 & p_{1,15} = 0 & p_{1,16} = 0 & p_{1,17} = 0 & p_{1,18} = 0 & p_{1,19} = 0 \\ p_{2,0} = 0 & p_{2,1} = \frac{1}{6} & p_{2,2} = 0 & p_{2,3} = \frac{1}{6} & p_{2,4} = 0 & p_{2,5} = 0 & p_{2,6} = 0 & p_{2,7} = 0 & p_{2,8} = 0 & p_{2,9} = \frac{1}{6} & p_{2,10} = \frac{1}{6} & p_{2,11} = \frac{1}{6} & p_{2,12} = 0 & p_{2,13} = 0 & p_{2,14} = 0 & p_{2,15} = 0 & p_{2,16} = 0 & p_{2,17} = 0 & p_{2,18} = 0 & p_{2,19} = 0 \\ p_{3,0} = \frac{1}{6} & p_{3,1} = 0 & p_{3,2} = \frac{1}{6} & p_{3,3} = 0 & p_{3,4} = \frac{1}{6} & p_{3,5} = 0 & p_{3,6} = 0 & p_{3,7} = 0 & p_{3,8} = 0 & p_{3,9} = 0 & p_{3,10} = 0 & p_{3,11} = \frac{1}{6} & p_{3,12} = \frac{1}{6} & p_{3,13} = \frac{1}{6} & p_{3,14} = 0 & p_{3,15} = 0 & p_{3,16} = 0 & p_{3,17} = 0 & p_{3,18} = 0 & p_{3,19} = 0 \\ p_{4,0} = 0 & p_{4,1} = 0 & p_{4,2} = 0 & p_{4,3} = \frac{1}{6} & p_{4,4} = 0 & p_{4,5} = \frac{1}{6} & p_{4,6} = 0 & p_{4,7} = 0 & p_{4,8} = 0 & p_{4,9} = 0 & p_{4,10} = 0 & p_{4,11} = 0 & p_{4,12} = 0 & p_{4,13} = \frac{1}{6} & p_{4,14} = \frac{1}{6} & p_{4,15} = \frac{1}{6} & p_{4,16} = 0 & p_{4,17} = 0 & p_{4,18} = 0 & p_{4,19} = 0 \\ p_{5,0} = 0 & p_{5,1} = 0 & p_{5,2} = 0 & p_{5,3} = 0 & p_{5,4} = \frac{1}{6} & p_{5,5} = 0 & p_{5,6} = \frac{1}{6} & p_{5,7} = 0 & p_{5,8} = 0 & p_{5,9} = 0 & p_{5,10} = 0 & p_{5,11} = 0 & p_{5,12} = 0 & p_{5,13} = 0 & p_{5,14} = 0 & p_{5,15} = \frac{1}{6} & p_{5,16} = \frac{1}{6} & p_{5,17} = \frac{1}{6} & p_{5,18} = 0 & p_{5,19} = 0 \\ p_{6,0} = \frac{1}{6} & p_{6,1} = \frac{1}{6} & p_{6,2} = 0 & p_{6,3} = 0 & p_{6,4} = 0 & p_{6,5} = \frac{1}{6} & p_{6,6} = 0 & p_{6,7} = \frac{1}{6} & p_{6,8} = 0 & p_{6,9} = 0 & p_{6,10} = 0 & p_{6,11} = 0 & p_{6,12} = 0 & p_{6,13} = 0 & p_{6,14} = 0 & p_{6,15} = 0 & p_{6,16} = 0 & p_{6,17} = \frac{1}{6} & p_{6,18} = \frac{1}{6} & p_{6,19} = 0 \\ p_{7,0} = 0 & p_{7,1} = \frac{1}{6} & p_{7,2} = 0 & p_{7,3} = 0 & p_{7,4} = 0 & p_{7,5} = 0 & p_{7,6} = \frac{1}{6} & p_{7,7} = 0 & p_{7,8} = \frac{1}{6} & p_{7,9} = 0 & p_{7,10} = 0 & p_{7,11} = 0 & p_{7,12} = 0 & p_{7,13} = 0 & p_{7,14} = 0 & p_{7,15} = 0 & p_{7,16} = 0 & p_{7,17} = 0 & p_{7,18} = \frac{1}{6} & p_{7,19} = \frac{1}{6} \\ p_{8,0} = 0 & p_{8,1} = \frac{1}{6} & p_{8,2} = 0 & p_{8,3} = 0 & p_{8,4} = 0 & p_{8,5} = 0 & p_{8,6} = 0 & p_{8,7} = \frac{1}{6} & p_{8,8} = 0 & p_{8,9} = \frac{1}{6} & p_{8,10} = 0 & p_{8,11} = 0 & 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$$Q = \begin{pmatrix} P_{0,0} = 0 & P_{0,1} = \frac{1}{6} & P_{0,2} = \frac{1}{6} & P_{0,3} = \frac{1}{6} & P_{0,4} = \frac{1}{6} & P_{0,5} = \frac{1}{6} & P_{0,6} = \frac{1}{6} & P_{0,7} = 0 & P_{0,8} = 0 & P_{0,9} = 0 & P_{0,10} = 0 & P_{0,11} = 0 & P_{0,12} = 0 & P_{0,13} = 0 & P_{0,14} = 0 & P_{0,15} = 0 & P_{0,16} = 0 & P_{0,17} = 0 & P_{0,18} = 0 \\ P_{1,0} = \frac{1}{6} & P_{1,1} = 0 & P_{1,2} = 0 & P_{1,3} = 0 & P_{1,4} = 0 & P_{1,5} = 0 & P_{1,6} = 0 & P_{1,7} = \frac{1}{6} & P_{1,8} = \frac{1}{6} & P_{1,9} = \frac{1}{6} & P_{1,10} = 0 & P_{1,11} = 0 & P_{1,12} = 0 & P_{1,13} = 0 & P_{1,14} = 0 & P_{1,15} = 0 & P_{1,16} = 0 & P_{1,17} = 0 & P_{1,18} = 0 \\ P_{2,0} = \frac{1}{6} & P_{2,1} = \frac{1}{6} & P_{2,2} = 0 & P_{2,3} = \frac{1}{6} & P_{2,4} = 0 & P_{2,5} = 0 & P_{2,6} = 0 & P_{2,7} = 0 & P_{2,8} = 0 & P_{2,9} = \frac{1}{6} & P_{2,10} = \frac{1}{6} & P_{2,11} = \frac{1}{6} & P_{2,12} = 0 & P_{2,13} = 0 & P_{2,14} = 0 & P_{2,15} = 0 & P_{2,16} = 0 & P_{2,17} = 0 & 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\frac{1}{6} & P_{15,5} = \frac{1}{6} & P_{15,6} = 0 & P_{15,7} = 0 & P_{15,8} = 0 & P_{15,9} = 0$$

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|-------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
| $N =$ | $P_{0,0} = .45$ | $P_{0,1} = .16$ | $P_{0,2} = .16$ | $P_{0,3} = .16$ | $P_{0,4} = .16$ | $P_{0,5} = .16$ | $P_{0,6} = .16$ | $P_{0,7} = .16$ | $P_{0,8} = .16$ | $P_{0,9} = .16$ | $P_{0,10} = .16$ | $P_{0,11} = .16$ | $P_{0,12} = .16$ | $P_{0,13} = .16$ | $P_{0,14} = .16$ | $P_{0,15} = .16$ | $P_{0,16} = .16$ | $P_{0,17} = .16$ | $P_{0,18} = .16$ |
|       | $P_{1,0} = .16$ | $P_{1,1} = .16$ | $P_{1,2} = .16$ | $P_{1,3} = .16$ | $P_{1,4} = .16$ | $P_{1,5} = .16$ | $P_{1,6} = .16$ | $P_{1,7} = .16$ | $P_{1,8} = .16$ | $P_{1,9} = .16$ | $P_{1,10} = .16$ | $P_{1,11} = .16$ | $P_{1,12} = .16$ | $P_{1,13} = .16$ | $P_{1,14} = .16$ | $P_{1,15} = .16$ | $P_{1,16} = .16$ | $P_{1,17} = .16$ | $P_{1,18} = .16$ |
|       | $P_{2,0} = .16$ | $P_{2,1} = .16$ | $P_{2,2} = .16$ | $P_{2,3} = .16$ | $P_{2,4} = .16$ | $P_{2,5} = .16$ | $P_{2,6} = .16$ | $P_{2,7} = .16$ | $P_{2,8} = .16$ | $P_{2,9} = .16$ | $P_{2,10} = .16$ | $P_{2,11} = .16$ | $P_{2,12} = .16$ | $P_{2,13} = .16$ | $P_{2,14} = .16$ | $P_{2,15} = .16$ | $P_{2,16} = .16$ | $P_{2,17} = .16$ | $P_{2,18} = .16$ |
|       | $P_{3,0} = .16$ | $P_{3,1} = .16$ | $P_{3,2} = .16$ | $P_{3,3} = .16$ | $P_{3,4} = .16$ | $P_{3,5} = .16$ | $P_{3,6} = .16$ | $P_{3,7} = .16$ | $P_{3,8} = .16$ | $P_{3,9} = .16$ | $P_{3,10} = .16$ | $P_{3,11} = .16$ | $P_{3,12} = .16$ | $P_{3,13} = .16$ | $P_{3,14} = .16$ | $P_{3,15} = .16$ | $P_{3,16} = .16$ | $P_{3,17} = .16$ | $P_{3,18} = .16$ |
|       | $P_{4,0} = .16$ | $P_{4,1} = .16$ | $P_{4,2} = .16$ | $P_{4,3} = .16$ | $P_{4,4} = .16$ | $P_{4,5} = .16$ | $P_{4,6} = .16$ | $P_{4,7} = .16$ | $P_{4,8} = .16$ | $P_{4,9} = .16$ | $P_{4,10} = .16$ | $P_{4,11} = .16$ | $P_{4,12} = .16$ | $P_{4,13} = .16$ | $P_{4,14} = .16$ | $P_{4,15} = .16$ | $P_{4,16} = .16$ | $P_{4,17} = .16$ | $P_{4,18} = .16$ |
|       | $P_{5,0} = .16$ | $P_{5,1} = .16$ | $P_{5,2} = .16$ | $P_{5,3} = .16$ | $P_{5,4} = .16$ | $P_{5,5} = .16$ | $P_{5,6} = .16$ | $P_{5,7} = .16$ | $P_{5,8} = .16$ | $P_{5,9} = .16$ | $P_{5,10} = .16$ | $P_{5,11} = .16$ | $P_{5,12} = .16$ | $P_{5,13} = .16$ | $P_{5,14} = .16$ | $P_{5,15} = .16$ | $P_{5,16} = .16$ | $P_{5,17} = .16$ | $P_{5,18} = .16$ |
|       | $P_{6,0} = .16$ | $P_{6,1} = .16$ | $P_{6,2} = .16$ | $P_{6,3} = .16$ | $P_{6,4} = .16$ | $P_{6,5} = .16$ | $P_{6,6} = .16$ | $P_{6,7} = .16$ | $P_{6,8} = .16$ | $P_{6,9} = .16$ | $P_{6,10} = .16$ | $P_{6,11} = .16$ | $P_{6,12} = .16$ | $P_{6,13} = .16$ | $P_{6,14} = .16$ | $P_{6,15} = .16$ | $P_{6,16} = .16$ | $P_{6,17} = .16$ | $P_{6,18} = .16$ |
|       | $P_{7,0} = .16$ | $P_{7,1} = .16$ | $P_{7,2} = .16$ | $P_{7,3} = .16$ | $P_{7,4} = .16$ | $P_{7,5} = .16$ | $P_{7,6} = .16$ | $P_{7,7} = .16$ | $P_{7,8} = .16$ | $P_{7,9} = .16$ | $P_{7,10} = .16$ | $P_{7,11} = .16$ | $P_{7,12} = .16$ | $P_{7,13} = .16$ | $P_{7,14} = .16$ | $P_{7,15} = .16$ | $P_{7,16} = .16$ | $P_{7,17} = .16$ | $P_{7,18} = .16$ |
|       | $P_{8,0} = .16$ | $P_{8,1} = .16$ | $P_{8,2} = .16$ | $P_{8,3} = .16$ | $P_{8,4} = .16$ | $P_{8,5} = .16$ | $P_{8,6} = .16$ | $P_{8,7} = .16$ | $P_{8,8} = .16$ | $P_{8,9} = .16$ | $P_{8,10} = .16$ | $P_{8,11} = .16$ | $P_{8,12} = .16$ | $P_{8,13} = .16$ | $P_{8,14} = .16$ | $P_{8,15} = .16$ | $P_{8,16} = .16$ | $P_{8,17} = .16$ | $P_{8,18} = .16$ |
|       | $P_{9,0} = .16$ | $P_{9,1} = .16$ | $P_{9,2} = .16$ | $P_{9,3} = .16$ | $P_{9,4} = .16$ | $P_{9,5} = .16$ | $P_{9,6} = .16$ | $P_{9,7} = .16$ | $P_{9,8} = .16$ | $P_{9,9} = .16$ | $P_{9,10} = .16$ | $P_{9,11} = .16$ | $P_{9,12} = .16$ | $P_{9,13} = .16$ | $P_{9,14} = .16$ | $P_{9,15} = .16$ | $P_{9,16} = .16$ | $P_{9,17} = .16$ | $P_{9,18} = .16$ |

$$t = N\mathbf{1}$$
[illegible]

Finally, we see that  $t_0 = \boxed{\frac{213}{29} \approx 7.345}$