

Rajeev Atla

~~Settlers of Catan~~ A board game is played on a hexagonal grid of 19 tiles. A 'traveler' token starts on the center tile. Each turn a die is rolled to determine what neighboring tile the traveler moves to (all six directions equally likely). The turn that the traveler leaves the board, the game ends. What is the expected number of turns of the game?

The diagram shows a hexagonal lattice structure. The central cell is labeled 0. It is surrounded by six cells labeled 1 through 6. These are further surrounded by a second ring of cells labeled 7 through 12, and a third ring of cells labeled 13 through 18. The vertices of the lattice are labeled with numbers 1 through 19, corresponding to the vertices of the cells. The vertices are labeled 1 through 19, and the cells are labeled 0 through 18.

$$\mathbb{E}(N) = \sum N \mathbb{P}(N)$$

Page 1 of 4

[illegible]

$$t = N\mathbf{1}$$
[illegible]

Finally, we see that $t_0 = \boxed{\frac{213}{29} \approx 7.345}$