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~~Settlers of Catan~~ A board game is played on a hexagonal grid of 19 tiles. A 'traveler' token starts on the center tile. Each turn a die is rolled to determine what neighboring tile the traveler moves to (all six directions equally likely). The turn that the traveler leaves the board, the game ends. What is the expected number of turns of the game?

A hexagonal grid of 19 cells, each containing a red dot and a number from 0 to 18. The grid is surrounded by 20 green dots, each labeled with a number from 19 to 38. The grid is arranged in a 4x4 pattern with the bottom-right cell missing.

Cell Index	Number	Color
0	0	Red
1	1	Red
2	2	Red
3	3	Red
4	4	Red
5	5	Red
6	6	Red
7	7	Red
8	8	Red
9	9	Red
10	10	Red
11	11	Red
12	12	Red
13	13	Red
14	14	Red
15	15	Red
16	16	Red
17	17	Red
18	18	Red

Cell Index	Number	Color
19	19	Green
20	20	Green
21	21	Green
22	22	Green
23	23	Green
24	24	Green
25	25	Green
26	26	Green
27	27	Green
28	28	Green
29	29	Green
30	30	Green
31	31	Green
32	32	Green
33	33	Green
34	34	Green
35	35	Green
36	36	Green

$$\mathbb{E}(N) = \sum N \mathbb{P}(N)$$

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[illegible]

$$\mathbf{t} = N\mathbf{1}$$
[illegible]

Finally, we see that $t_0 = \boxed{\frac{213}{29} \approx 7.345}$