Accurate autocorrelation modeling substantially improves fMRI reliability

A journal club about "sphericity" when the word appears nowhere in the whole article.

Article:

https://www.nature.com/articles/s41467-019-09230-w

Supplementary:

https://static-content.springer.com/esm/art%3A10.1038%2Fs41467-019-09230-w/MediaObjects/41467_2019_9230_MOESM1_ESM.pdf

Code:

https://github.com/wiktorolszowy/fMRI_temporal_autocorrelation

Peer-review:

https://static-content.springer.com/esm/art%3A10.1038%2Fs41467-019-09230-w/MediaObjects/41467_2019_9230_MOESM3_ESM.pdf

My code about it:

https://github.com/Remi-Gau/talk_sphericity_correction

Why talk about this?

- NARPS fMRI data
 - low repetition time ("high temporal resolution").
- For me (and you?)
 - better understand sphericity-correction.
- Peek under the hood
 - make SPM less of a black box.

- What is sphericity?

 How does SPM deal with non-sphericity when it runs a GLM?

The part where I talk about the paper

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30-Apr-2019 07:55:34 - Running job #1
30-Apr-2019 07:55:34 - Running 'fMRI model specification'
SPM12: spm fMRI design (v7210)
Saving fMRI design
SPM12: spm fmri spm ui (v7018)
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30-Apr-2019 07:55:38 - Done
30-Apr-2019 07:55:38 - Running 'Model estimation'
SPM12: spm est non sphericity (v6913)
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Chunk 1/1
Temporal non-sphericity (9162 voxels)
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  ReML Iteration 2
SPM12: spm spm (v7120)
Chunk 1/1
Spatial non-sphericity (over scans)
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                             'Model estimation'
30-Apr-2019 07:55:42 - Done
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```

Sphericity, Sphericity... If you say sphericity one more time...



What in the name of sanity is sphericity anyway?

General linear model:

$$Y = X \beta + \varepsilon$$

$$\varepsilon \sim N(0, \sigma^2 I)$$

Ordinary least square estimators (OLS) are the best* linear **unbiased** estimator (BLUE) IF errors are **uncorrelated** with **mean zero** and **homoscedastic** with finite variance.

* "best" means giving the lowest variance of the estimate, as compared to other unbiased, linear estimators.

General linear model: $Y = X \beta + \epsilon$

What do we want? We want the best model!

Why? Unmodelled things hurt our t-value! #PoorTValue.

beta =
$$(X' X)^{-1} X y$$
;

$$sigma^2 = e e' / (N - p)$$

$$t = c (X'X)^{-1} X' y / sigma (c(X'X)^{-1} c')^{.5}$$

$$t = c beta / sigma (c(X'X)^{-1} c')^{.5}$$

$$t=rac{Z}{s}=rac{ar{X}-\mu}{\widehat{\sigma}/\sqrt{n}}$$

General linear model: $Y = X \beta + \epsilon$

We want the best model!

- Block design (using data from auditory regions of SPM auditory data set)
- Convolve with HRF
- Convolve with HRF at higher resolution
- Model out other effects ("noise"):
 - linear drift low frequencies
 - High pass filtering: linear regressor
 - HPF à la SPM: Discrete cosine transform (SPM.xX.K.X0)
 - Motion regressors (or other data: physiological).

DEMO

General linear model: $Y = X \beta + \epsilon$

What else do we want? $\varepsilon \sim N(0, \sigma^2 I)$

"errors are uncorrelated with mean zero and homoscedastic with finite variance".

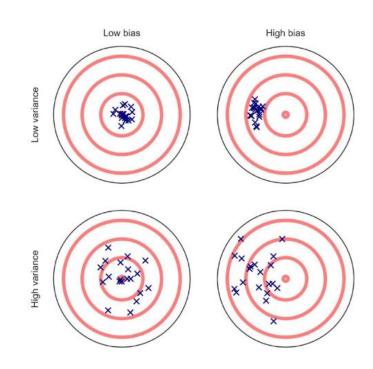
When the assumptions about ε breakdown

Errors with mean not equal to 0:

- bias

If unequal variance or correlation:

- increased variance

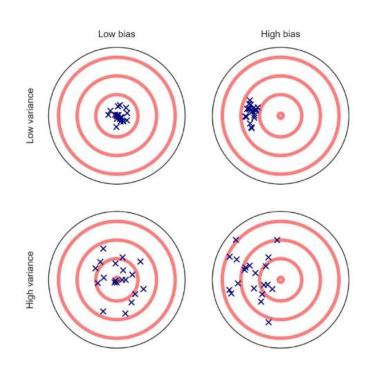


General linear model: $Y = X \beta + \epsilon$

What else do we want? $\varepsilon \sim N(0, \sigma^2 I)$

"errors are uncorrelated with mean zero and homoscedastic with finite variance".

Sphericity is about to the uncorrelated bit.



Sphericity violations occur when $\varepsilon \sim N(0, \sigma^2 V)$ instead of $\varepsilon \sim N(0, \sigma^2 I)$

- $N(0, \sigma^2 I)$ and $N(0, \sigma^2 V)$. What does this look like? DEMO
- White residuals means this $N(0,\sigma^2 I)$. What does it look like? DEMO

How do we typically deal with this? (e.g repeated measure ANOVAs)

- Greenhouse-Geiser correction
- Huynh and Feldt correction

Estimate how far V is from I and reduce the degrees of freedom.

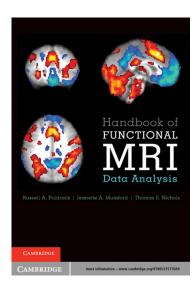
References for non-sphericity correction / pre-whitening in neuroimaging

What the "bible" has to say about it. Page 90 and 195

Jeanette Mumford

- Youtube
- Course
- <u>Slide</u>

SPM course (minute 32) SPM slides



Andy Field's book "discovering statistices" is awesome: <u>His bluffer's guide to sphericity</u>

$$\varepsilon \sim N(0, \sigma^2 V)$$
 but we want $\varepsilon \sim N(0, \sigma^2 I)$

$$W V W' = I$$

W is a whitening matrix.

$$WY = WX\beta + W\epsilon$$

Premultiply data and design matrix by W.

$$var(WY) = var(W\varepsilon) = \sigma^2 W V W' = \sigma^2 I$$

Woohoo!

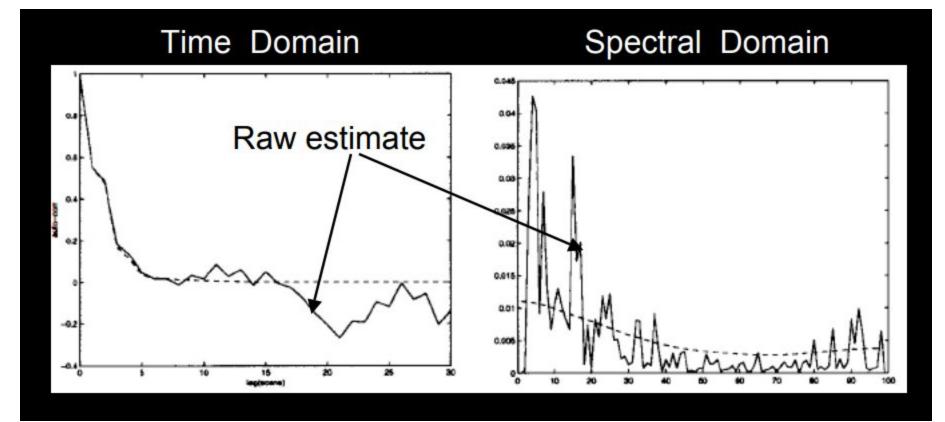
In practice: We need to estimate W. Need to be done from data.

- Run GLM without worrying about autocorrelation (OLS)
- Get residuals from this to estimate W (that's the crux)
- Create whitened model.

Bias / variance trade off: hard to estimate W in an unbiased way.

Different ways to to go around it.

- Voxel wise: More variance. Less bias.
 - FSL: Tukey taper is used to smooth the spectral density estimates. These smoothed estimates are then additionally smoothed within tissue type.
- Voxel wise but fewer things (hyperparameters) to estimate: Less variance.
 Less bias.
 - AFNI: an autoregressive-moving-average ARMA(1,1) model is estimated



Bias / variance trade off: hard to estimate W in an unbiased way.

Different ways to to go around it.

- Global approach: Less variance. More bias.
 - SPM: Same W for the whole brain, but get more stable estimate because we can pool over voxels
 - autoregressive (AR) + white noise model.
 - FAST.
 - I tried to understand the paper but it was written in Fristonian.

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30-Apr-2019 07:55:38 - Running 'Model estimation'
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'Model estimation'

...3.329980e-03 [+4.50]

07:55:39 - 30/04/2019

07:55:41 - 30/04/2019

...done

...done

ReML Iteration 1
ReML Iteration 2

SPM12: spm spm (v7120)

Spatial non-sphericity (over scans)

30-Apr-2019 07:55:42 - Done

30-Apr-2019 07:55:42 - Done

Chunk 1/1

Completed

Done

Saving SPM.mat

What's in SPM.mat? Check here

Calculating globals with spm_global.

Will be used to create the inclusive mask where the GLM will be run.

See also threshold used to define inclusive mask.

matlabbatch.spm.stats.fmri_spec.mthresh = 0.8;

Default is 0.8 and it can be changed.

Create a spm_my_defaults based on spm_defaults defaults.mask.thresh = 0.8;

```
30-Apr-2019 07:55:34 - Running job #1
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SPM12: spm fMRI design (v7210)
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30-Apr-2019 07:55:42 - Done
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```

spm_spm is the heart of the SPM package.

```
%-Get non-sphericity (xVi), otherwise assume i.i.d.
if isfield(SPM,'xVi')
         = SPM.xVi:
  xVi
else
  хVі
          = struct('form', 'i.i.d.',...
              'V', speye(nScan,nScan));
end
%-Evoke ReML for hyperparameter estimation
if ~isfield(xVi,'V')
  SPM.xY.VY = VY;
  SPM.xM = xM:
  SPM.xX.K = xX.K;
  [xVi, am] = spm_est_non_sphericity(SPM);
  mask = mask & am;
  spm('FnBanner',mfilename,SVNid);
end
```

```
30-Apr-2019 07:55:34 - Running job #1
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Spatial non-sphericity (over scans)
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Done
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30-Apr-2019 07:55:42 - Done
30-Apr-2019 07:55:42 - Done
```

spm_est_non_sphericity

% In a first pass, voxels over which non-sphericity will be estimated are % selected using an 'effects of interest' F-contrast (can be specified in % SPM.xVi.Fcontrast) and critical threshold taken from SPM defaults % stats.<modality>.UFp.

Check hyperparameters in "Review design"

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SPM12: spm_spm (v7120)		07:55:38 - 30/04/2019
		07:55:38 - 30/04/2019 07:55:38 - 30/04/2019
SPM12: spm_est_non_sphericity (v6913)		
SPM12: spm_est_non_sphericity (v6913)	:	07:55:38 - 30/04/2019
SPM12: spm_est_non_sphericity (v6913)	: : :	07:55:38 - 30/04/2019 done
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Spatial non-sphericity.

For MVPA check RSA toolbox

function

[u_hat, resMS, Sw_hat, beta_hat, shrinkage, trRR] = noiseNormalizeB
eta(Y, SPM, varargin)

- % function
- [u_hat, Sw_hat, resMS, beta_hat] = rsa_noiseNormalizeBeta(Y, SPM, v
 arargin)
- % Estimates beta coefficiencts beta_hat and residuals from raw time series Y
- $\mbox{\%}$ Estimates the true activity patterns u_hat by applying noise normalization to beta ha

```
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SPM12: spm spm (v7120)
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Spatial non-sphericity (over scans)
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Completed
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Done
                               'Model estimation'
30-Apr-2019 07:55:42 - Done
30-Apr-2019 07:55:42 - Done
```

Wanna speed things up?

Reduce the number of chunks by changing memory usage defaults.

defaults.stats.maxmem = 2^2 ;

30-Apr-2019 07:55:34 - Running job #1		
30-Apr-2019 07:55:34 - Running 'fMRI	model specifi	.cation'
SPM12: spm_fMRI_design (v7210)		07:55:37 - 30/04/2019
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SPM12: spm_fmri_spm_ui (v7018)		07:55:37 - 30/04/2019
Mapping files	:	done
Calculating globals	:	done
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SPM12: spm_spm (v7120)	========	07:55:38 - 30/04/2019
SPM12: spm_est_non_sphericity (v6913)		07:55:38 - 30/04/2019
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Temporal non-sphericity (9162 voxels) ReML Block 1	:	ReML estimation
ReML Iteration 1	:	1.695290e+00 [+4.25]
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SPM12: spm_spm (v7120)		07:55:39 - 30/04/2019
Chunk 1/1	:	done
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30-Apr-2019 07:55:42 - Done 'Model 30-Apr-2019 07:55:42 - Done	estimation'	

The part where I talk about the paper...

About time if you ask me.

Note:

- Glaring absence of p-values in the whole paper
- Statistical test: IOTT (IntraOcular Trauma Test)

"Plot the data. If the result hits you between the eyes, then it's significant."

Data

Table 1 Overview of the employed datasets

Study	Experiment	Place	Design	No. subjects	Field [T]	TR [s]	Voxel size [mm]	No. voxels	Time point
FCP	Resting state	Beiiing	N/A	198	3	2	3.1 × 3.1 × 3.6	64 × 64 × 33	225

Study	Experiment	Place	Design	No. subjects	Field [T]	TR [s]	Voxel size [mm]	No. voxels	Time points
FCP	Resting state	Beijing	N/A	198	3	2	$3.1 \times 3.1 \times 3.6$	64 × 64 × 33	225
	Resting state	Cambridge, US	N/A	198	3	3	$3 \times 3 \times 3$	$72 \times 72 \times 47$	119
NKI	Resting state	Orangeburg, US	N/A	30	3	1.4	$2 \times 2 \times 2$	$112 \times 112 \times 64$	404
	Resting state	Orangeburg, US	N/A	30	3	0.645	$3 \times 3 \times 3$	$74 \times 74 \times 40$	900
CRIC	Resting state	Cambridge, UK	N/A	73	3	2	$3 \times 3 \times 3.8$	$64 \times 64 \times 32$	300
neuRosim	Resting state	(Simulated)	N/A	100	NA	2	$3.1 \times 3.1 \times 3.6$	$64 \times 64 \times 33$	225
NKI	Checkerboard	Orangeburg, US	20 s off + 20 s on	30	3	1.4	$2 \times 2 \times 2$	$112 \times 112 \times 64$	98
	Checkerboard	Orangeburg, US	20 s off + 20 s on	30	3	0.645	$3 \times 3 \times 3$	$74 \times 74 \times 40$	240
BMMR	Checkerboard	Magdeburg	12 s off + 12 s on	21	7	3	$1 \times 1 \times 1$	$182 \times 140 \times 45$	80
CRIC	Checkerboard	Cambridge, UK	16 s off + 16 s on	70	3	2	$3 \times 3 \times 3.8$	$64 \times 64 \times 32$	160
CamCAN	Sensorimotor	Cambridge, UK	Event-related	200	3	1.97	$3 \times 3 \times 4.44$	$64 \times 64 \times 32$	261

For the enhanced NKI data, only scans from release 3 were used. Out of the 46 subjects in release 3, scans of 30 subjects were taken. For the rest, at least 1 scan was missing. For the BMMR data, there were 7 subjects at 3 sessions, resulting in 21 scans. For the CamCAN data, 200 subjects were considered only

FCP Functional Connectomes Project, NKI Nathan Kline Institute, BMMR Biomedical Magnetic Resonance, CRIC Cambridge Research into Impaired Consciousness, CamCAN Cambridge Centre for Ageing and Neuroscience

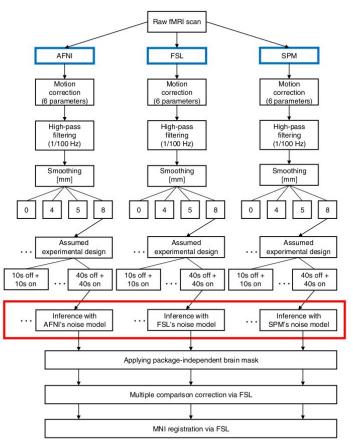


Fig. 4 The employed analyses pipelines. For SPM, we investigated both the default noise model and the alternative noise model: FAST. The noise models used by AFNI, FSL, and SPM were the only relevant difference (marked in a red box)

Dummy design approach:

take resting state MRI data and fit a GLM on it as if it were task fMRI

H0:

any activation you see is a false positive

Advantage:

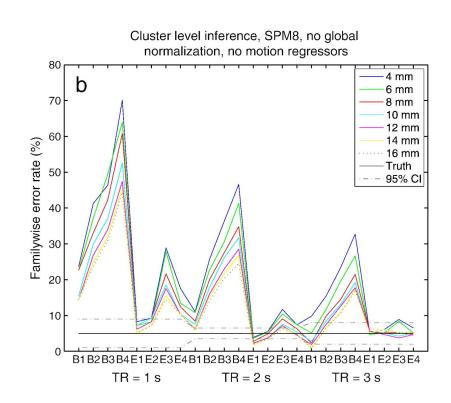
using real data with real underlying noise structure

See Eklund's papers

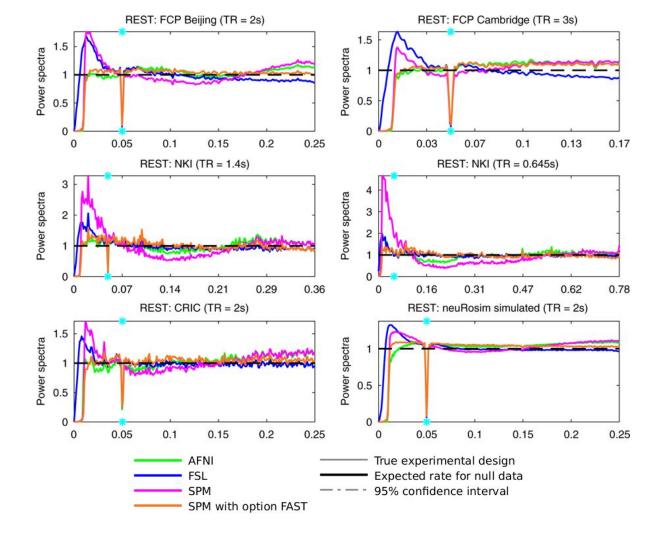
- SPM
- SPM, AFNI, FSL subject level
- Cluster F...

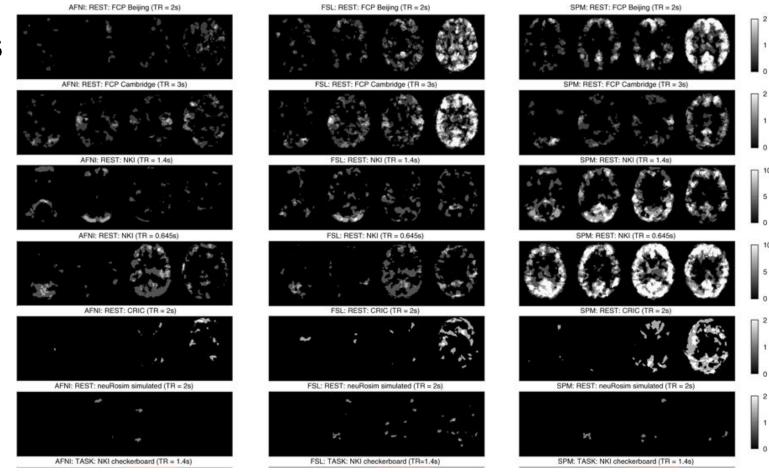
TLDR: Neuroskeptics posts about it

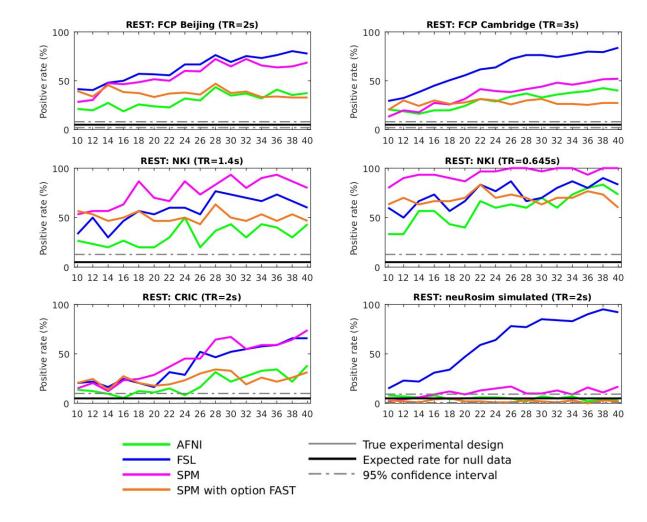
- Post 1
- <u>Post 2</u>
- <u>Post 3</u>
- <u>Post 4</u>



- (1) the power spectra of the GLM residuals: should be flat
- (2) the spatial distribution of significant clusters
- (3) the average percentage of significant voxels within the brain mask
- (4) the positive rate: proportion of subjects with at least one significant cluster







Do problem at the first level spread at the group level?

Results at group level compared summary statistics approach and mixed effect.

"FWER for the mixed effects analyses was almost twice higher than FWER for the summary statistic analyses.

The use of AFNI's pre-whitening led to highest FWER (????), while FAST led to lower FWER than the SPM's default approach."

Conclusion

When using SPM go FAST... Or go home.

Check your residuals: authors provide function on github repo (sort of works)

Check model fit and compare models: MACS toolbox