

# K-Nearest Neighbors Classification

Taught by: Bedoor AlShebli

Based on Kevyn Collins-Thompson's Applied Machine Learning Course

# K-NN Classifier

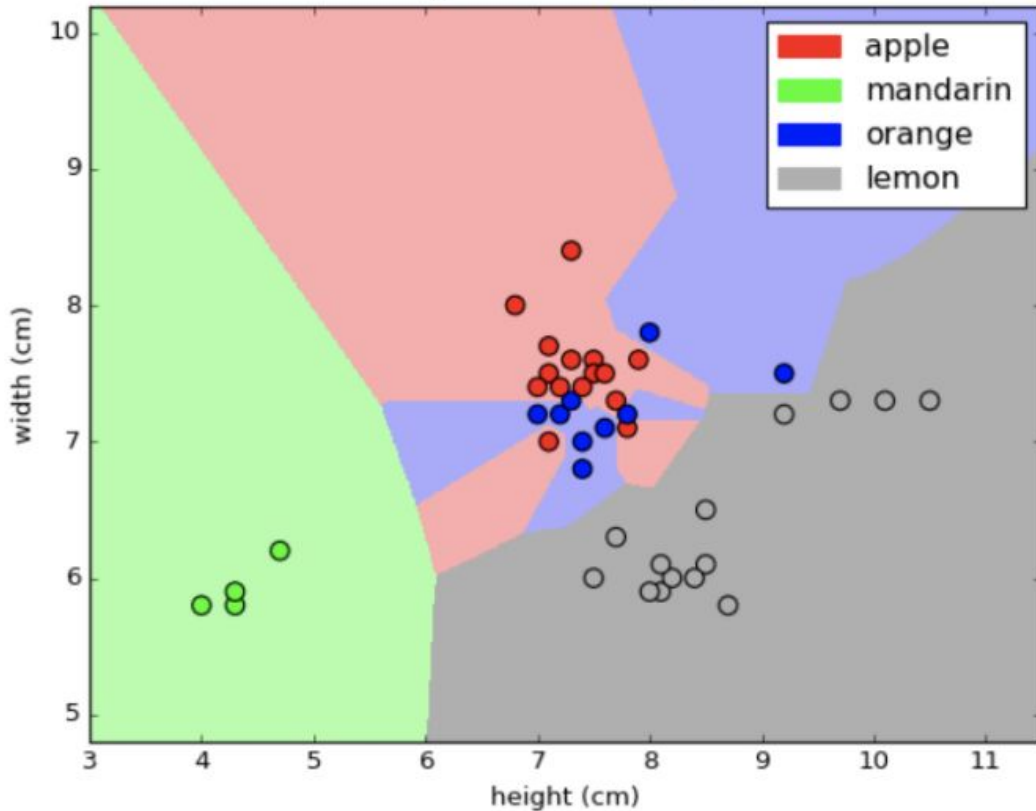
- An example of **instance or memory based supervised learning**
  - i.e. it works by memorizing the labeled examples in the training set
- The **k** refers to the **number of nearest neighbors** the classifier will retrieve and use in order to make its prediction

# K-NN Classifier: The Algorithm

Given a training set  $X_{\text{train}}$  with labels  $y_{\text{train}}$ , and given a new instance  $x_{\text{test}}$  to be classified:

1. Find the most similar instances (let's call them  $X_{\text{NN}}$ ) to  $x_{\text{test}}$  that are in  $X_{\text{train}}$ .
2. Get the labels  $y_{\text{NN}}$  for the instances in  $X_{\text{NN}}$
3. Predict the label for  $x_{\text{test}}$  by combining the labels  $y_{\text{NN}}$ . Eg) simple majority vote

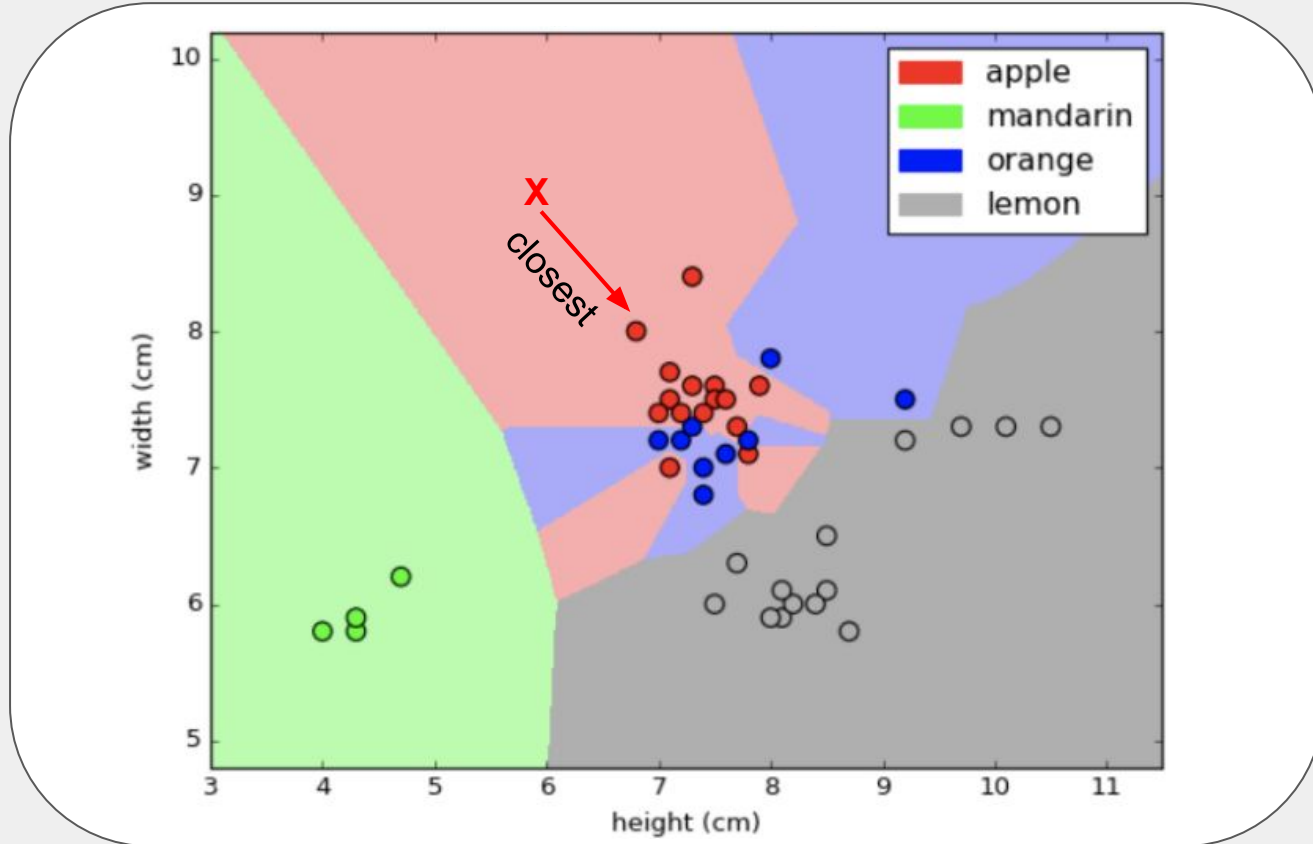
# A visual explanation of k-NN classifiers ( $k=1$ )



**The KNN algorithm assumed that similar things exist in close proximity.**

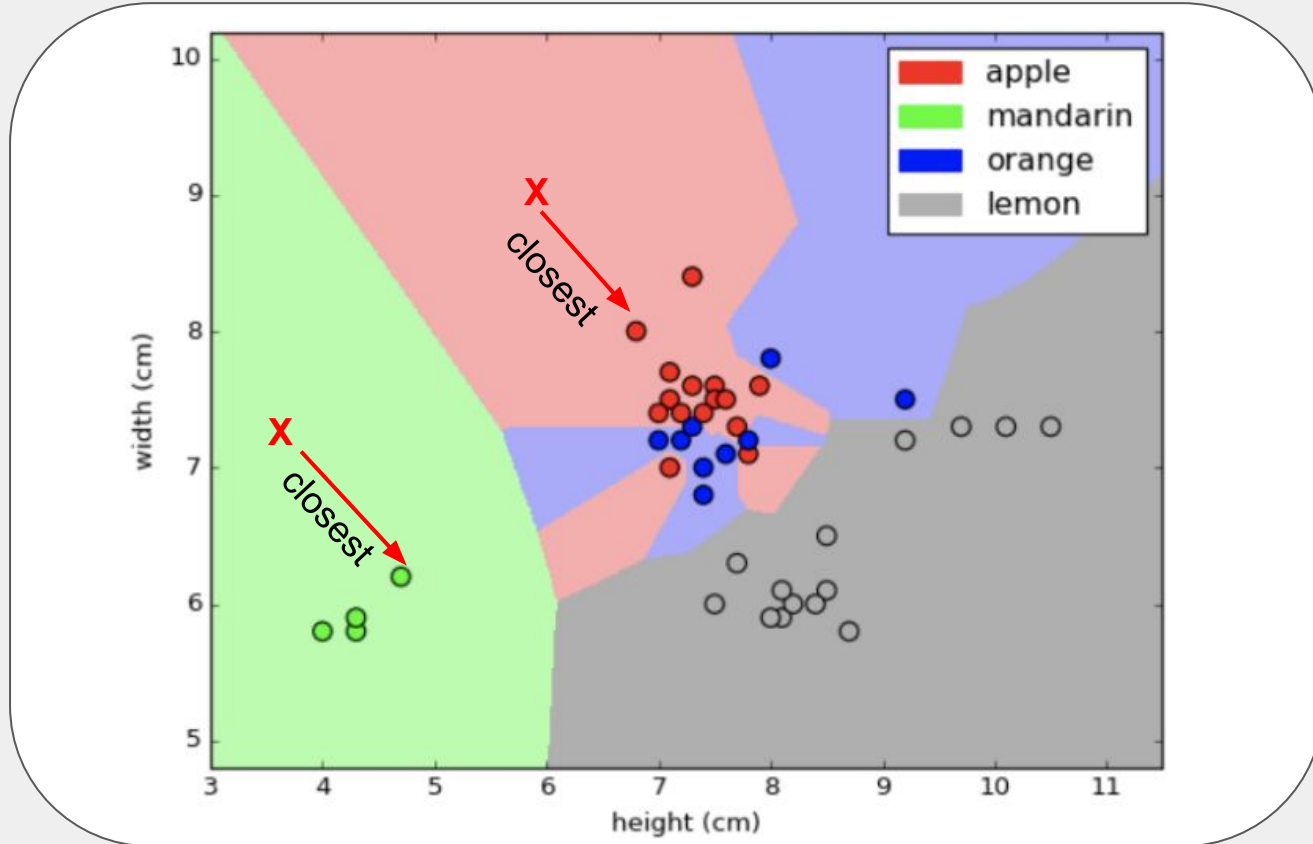
**“Birds of a feature, flock together”**

# A visual explanation of k-NN classifiers ( $k=1$ )



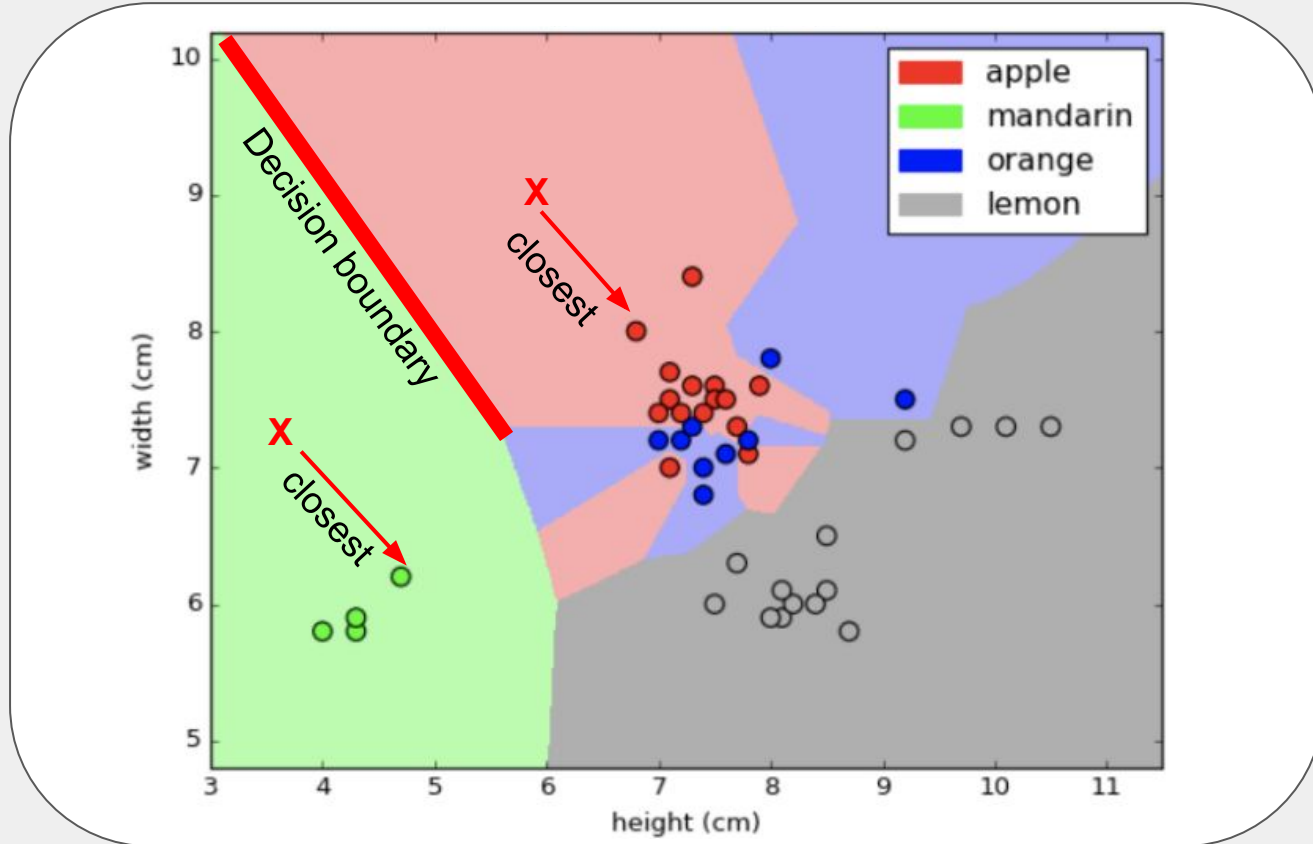
**What is x with  
height = 6 and  
width = 9?**

# A visual explanation of k-NN classifiers ( $k=1$ )



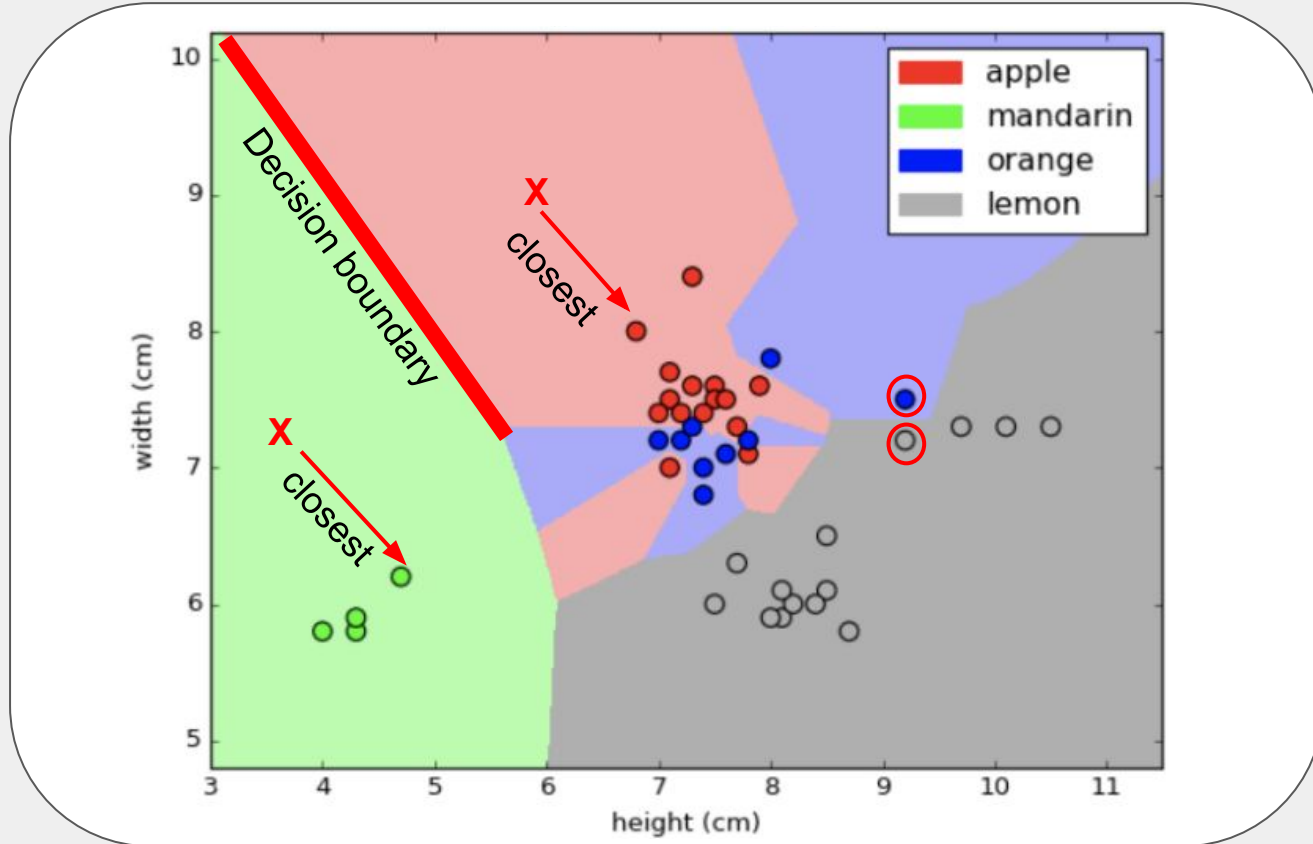
**What about this second x?**

# A visual explanation of k-NN classifiers ( $k=1$ )



**Decision Boundaries  
with  $k=1$**

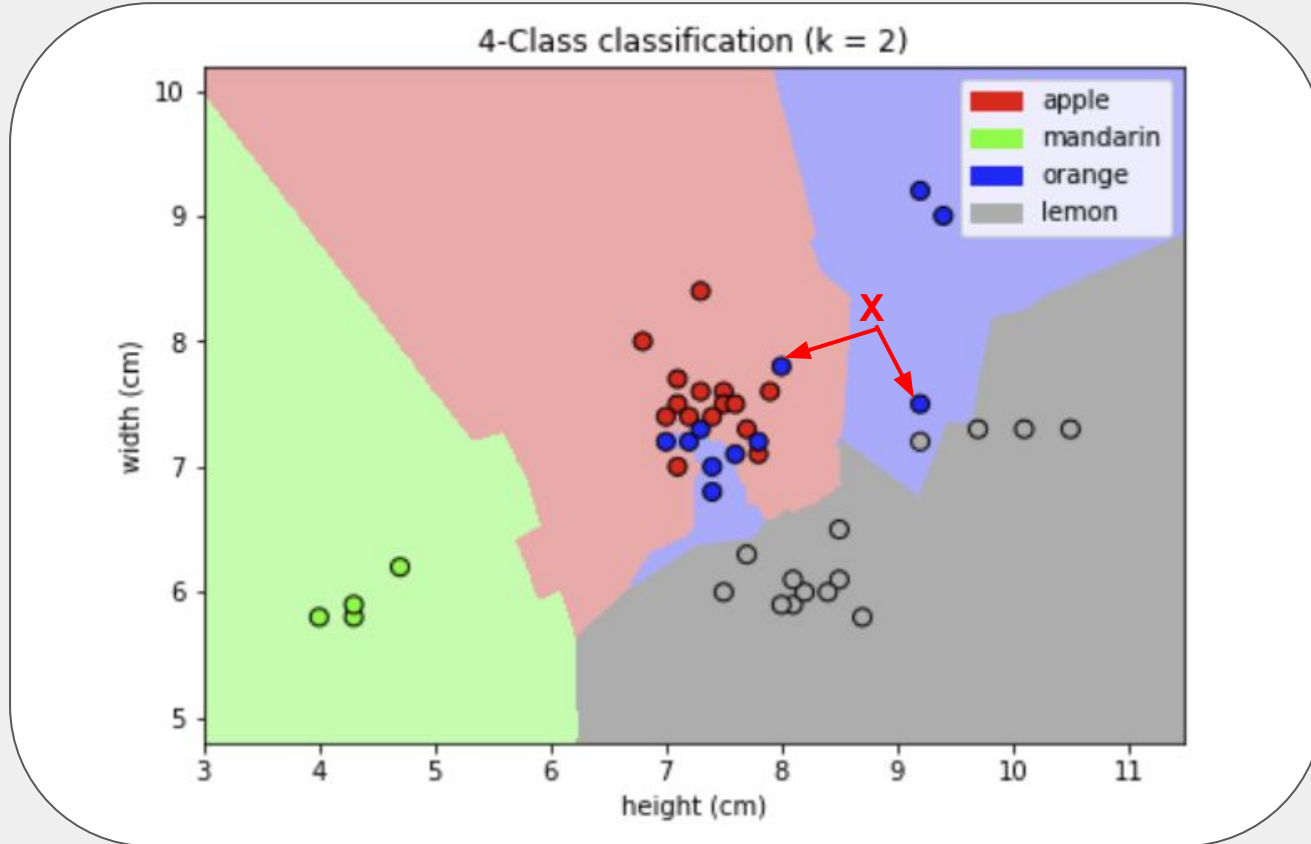
# A visual explanation of k-NN classifiers ( $k=1$ )



**Decision boundaries are constructed to be equidistant based on the euclidean distance between two different labeled instances.**



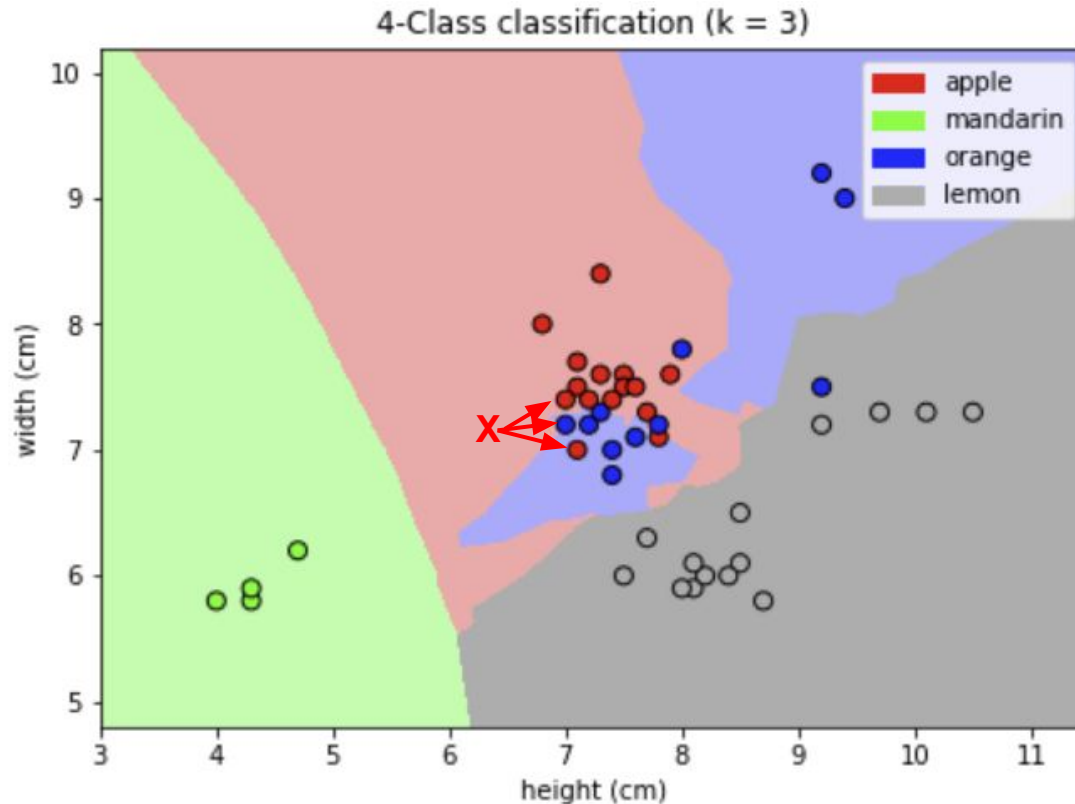
# A visual explanation of k-NN classifiers (k=2,3,4?)



**What if k = 2?**

**We look at the 2  
closest points and  
use a simple  
majority vote to  
decide**

# A visual explanation of k-NN classifiers (k=2,3,4?)



Typically  $k$  is odd, to avoid / resolve tie breaks.

X here would be an apple.

# Nearest Neighbor Algorithm Requirements

Generally, to use a nearest neighbor algorithm, we need to specify the following:

- 1. A distance metric**

- In our example, we used a simple straight line or euclidean distance

- 2. How many 'nearest' neighbors to look at, i.e.  $k$ ?**

- Must be at least 1

- 3. Optional weighting function on the neighbor points.**

- We may decide that neighbors closer to the new instance should have more influence or more votes. In our example, we chose to ignore this option, i.e. give “uniform” weighting.

- 4. Method for aggregating the classes of neighbor points**

- In our example, we used the default scikit-learn option, which is a simple majority vote.

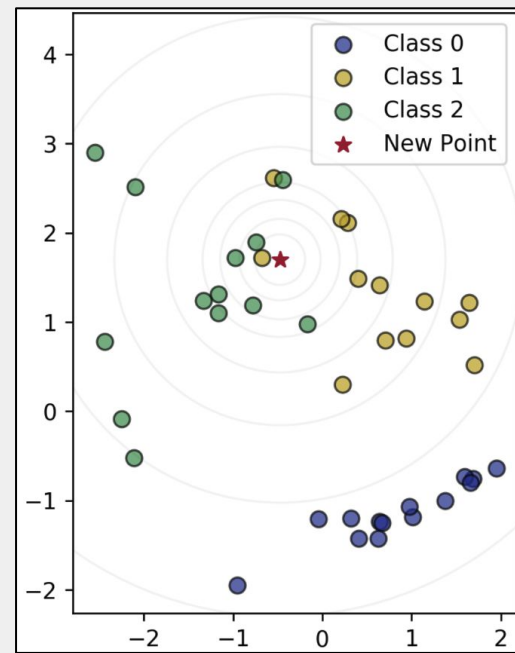
# Questions

1- Given the following data for Classes 0, 1 and 2, what class would the KNN Classifier classify the new point if :

- $k=1$ ?
- $k=3$ ?

2- Which of the following is true for KNN classifiers? *Select all that apply.*

- A higher value of  $k$  leads to a more complex decision boundary.
- KNN partitions observations into  $k$  clusters, where each new observation belongs to the cluster with the nearest mean.
- KNN memorizes the entire training set.
- Given a data instance to classify, computes the probability of each possible class using a statistical model of the input features.



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