Übung 3

$$\begin{cases} \begin{pmatrix} \sigma(\sigma(x_1,\alpha),\sigma(\gamma(x_3),x_3)) \\ \sigma(\sigma(\gamma(x_2),\alpha),\sigma(x_2,x_3)) \end{pmatrix} \\ \overset{\text{Dek.}}{\Longrightarrow} \left\{ \begin{pmatrix} \sigma(x_1,\alpha) \\ \sigma(\gamma(x_2),\alpha) \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3),x_3) \\ \sigma(x_2,x_3) \end{pmatrix} \right\} \\ \overset{\text{Dek.}}{\Longrightarrow} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \sigma(\gamma(x_3),x_3) \\ \sigma(x_2,x_3) \end{pmatrix} \right\} \\ \overset{\text{Dek.}}{\Longrightarrow} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix}, \begin{pmatrix} x_3 \\ x_3 \end{pmatrix} \right\} \\ \overset{\text{El.}}{\Longrightarrow} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \alpha \\ \alpha \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \\ \overset{\text{Dek.}}{\Longrightarrow} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \end{cases}$$

Übung 3

$$\begin{split} &\left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} \gamma(x_3) \\ x_2 \end{pmatrix} \right\} \\ & \stackrel{\mathsf{Vert.}}{\Longrightarrow} \left\{ \begin{pmatrix} x_1 \\ \gamma(x_2) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \\ & \stackrel{\mathsf{Sub.}}{\Longrightarrow} \left\{ \begin{pmatrix} x_1 \\ \gamma(\gamma(x_3)) \end{pmatrix}, \begin{pmatrix} x_2 \\ \gamma(x_3) \end{pmatrix} \right\} \end{split}$$

allgemeinster Unifikator:

$$\begin{aligned} x_1 &\mapsto \gamma(\gamma(x_3)) \\ x_2 &\mapsto \gamma(x_3) \\ x_3 &\mapsto x_3 \end{aligned}$$

Übung 3

weitere Unifikatoren:

$$\begin{array}{ll} x_1 \mapsto \gamma(\gamma(\alpha)) & x_1 \mapsto \gamma(\gamma(\gamma(\alpha))) \\ x_2 \mapsto \gamma(\alpha) & x_2 \mapsto \gamma(\gamma(\alpha)) \\ x_3 \mapsto \alpha & x_3 \mapsto \gamma(\alpha) \end{array}$$

Occurs-Check schlägt fehl bei:

$$t_1 = x_1$$

$$t_2 = \gamma(x_1)$$