

# Determining Personalized Head Related Transfer Functions using Auralization

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**Abstract** - *This project aims to explore the basis of an enhanced way to deliver spatial audio in an observer's horizon using acoustic modeling in place of low-pass filtering, interaural time differences, and simple attenuation functions. The approach described in this paper determines two interpolating functions, used as head related transfer functions ("HRTFs") which provide the illusion of spatial audio. The HRTF is obtained by solving the wave and Helmholtz partial differential equations. The parameters for the aforementioned equations can be adjusted to account for any source and observer orientation in any anechoic space. In addition, the shape of the observer's head can be modeled to create a personalized HRTF tailored to the specific observer instead of a standard one. The model was able to successfully attenuate different frequency intervals and phase shift the audio signal for each channel to provide sufficient binaural cues to localize sound. Results from this implementation, although obtained through computationally intensive processes, could potentially be extended to virtual reality-based systems which would, in theory, provide for a more realistic audio experience.*

**Key Words** – Acoustics, Spatial Audio, Sound Localization, HRTFs.

## INTRODUCTION

Neuroscientists have been able to pinpoint the binaural and monaural cues that enable the human brain to accurately localize sound (determining its azimuth and elevation relative to the observer).

### I. Horizon Localization

Specifically, they found that the brain determines interaural time differences ("ITDs") and interaural intensity differences ("IIDs") [1], as illustrated in Figure 1, to establish the azimuth of a sound source relative to the observer. ITDs describe the variation in sound arrival time for each ear and exist as a result of the difference in distance between the observer and source. IIDs describe the variation in amplitude and exist as a result of a sound wave attenuating after reaching a boundary such as an observer's head or traversing long distances.

### II. Elevation Localization

The elevation of sound relative to the observer is determined by more complex monaural cues, specifically, spectral notches [2], which are closely related to head related impulse responses ("HRIRs"). These responses are dependent on a number of attributes including head diffraction, reflections from various body parts, and other refractions/diffractions due to the pinna. This phenomenon will not be covered in the scope of this paper, as the focus is to deliver spatial audio in the observer's two-dimensional horizon. However, a three-dimensional rendering of the user's head could in theory be used in the simulation domain, effectively allowing for the HRTF to accept elevation data as a parameter. This would require including the third spatial dimension, namely elevation, into the models which may influence the overall performance.

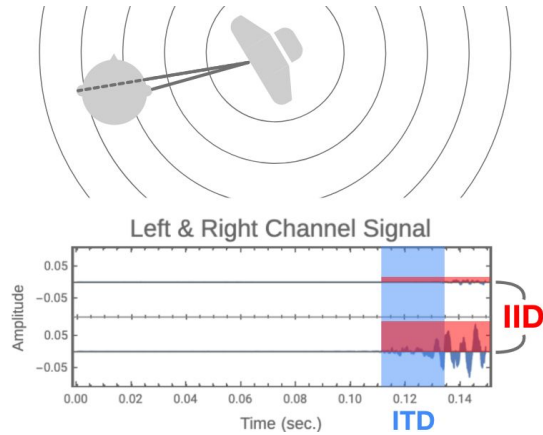


FIGURE 1: Certain arrangements of a sound source and observer yield subtle differences in the sound wave arrival time and amplitude for each ear. Note that the signal for the left ear is described by the graph above and the signal for the right ear is described by the graph below. The areas shaded in blue and red on the graph highlight the ITD and IID respectively. Notice the delayed start and lower amplitude for the left ear signal relative to the right ear signal.

However, it's worth noting that these cues may not be completely unique for every source and observer arrangement, yielding the same signal produced for both ears despite the orientation being different. This results in a phenomenon known as the cone of confusion [3]. One can easily circumvent this problem by simply moving their head and take note of changes that may occur in the channel for each ear.

### III. Related Work

Since the brain relies on relatively simple parameters to localize sound, there has been significant progress over recent years to create standard HRTFs for spatial audio [4]. These HRTFs alter the signal of an incoming sound wave to provide the illusion of spatial sound by processing two parameters, namely, the frequency of sound and the location of the source relative to the observer. However, many of the studies required investment in expensive resources including state-of-the-art anechoic chambers, high-quality speakers, and microphones to collect readings experimentally.

Additionally, this approach uses standard dummy heads to generalize the geometry of a human head, which yields a “one size fits all” HRTF. Hence, it fails to address the subtle details that typically vary depending on the shape of an individual's head and ears. Although one investigation has shown that one can adapt to a new hearing profile, it doesn't make for the most realistic experience [5].

### IV. Motivation

The process of creating personalized HRTFs for every single individual experimentally is infeasible. It would require the use of expensive acoustic equipment and computational resources which are generally inaccessible to the average consumer. Hence, the proposed method utilizes acoustic modeling to simulate the traditional measurement-based process. Ideally, the only equipment required would be a modern smartphone camera to recreate a three-dimensional rendering of a user's head. LIDAR mapping is another option that could be used, especially since there is an increasing number of handheld devices that integrate it in their optical systems. By simulating the experiment with a deterministic system, the costs and infrastructure associated with creating a custom HRTF would effectively be bypassed.

## ACOUSTIC MODELING

Pressure changes in a medium, caused by wave propagation, are typically described using the wave equation in the time domain and the Helmholtz equation in the frequency domain. These differential equations enable us to probe pressure data at any spatial location and at any point in time or at any frequency, effectively returning attenuation coefficients. Typically HRTFs accept a spatial location and frequency as a parameter, but examining wave propagation in the time domain helps visualize some of the behaviors that aren't immediately clear when visualized in the frequency domain. Moreover, the data visualizations in the time domain helped fine-tune some of the inconsistencies observed in the simulations and results.

## I. Approach Overview

By setting a sound source to emit the original audio signal or a relevant frequency, and the head of an observer in the region as depicted in Figure 2, the pressure at the location of each ear can be probed to define the attenuation coefficients. Additionally, the phase shift can also be determined through a similar process, either through the model or a simple delay, based on the difference in distance from both ears.

## II. Defining Equations

Variable symbols, definitions, and units are used as described in Table 1.

TABLE 1: Nomenclature as used in the following equations and expressions.		
Symbol	Definition	Units
$\mathbf{X}$	Position vector	$[m]$
$t$	Time	$[s]$
$\rho$	Density of a medium	$[kg/m^3]$
$c$	Speed of sound in a medium	$[m/s]$
$p$	Sound pressure	$[Pa]$
$\Omega$	Simulation domain	$[m]$
$\omega$	Sound wave angular frequency	$[rad/s]$
$Z$	Specific Impedance	$[Pa * s/m]$
$Z_b$	Boundary Impedance	$[Pa * s/m]$
$F$	Dipole Source	$[1/s^2]$
$Q$	Monopole Source	$[1/s^2]$

The partial differential equations (“PDEs”) used to model sound propagation and pressure distribution inside the space are the wave equation and the time-independent variant of the wave equation, the Helmholtz equation [6, 7]. The equations are defined as follows:

$$\nabla \cdot \left( -\frac{1}{\rho} (\nabla p(\mathbf{X}) + F) \right) - \frac{\omega^2}{\rho c^2} p(\mathbf{X}) = Q$$

$$\frac{1}{\rho c^2} \frac{\partial^2 p(t, \mathbf{X})}{\partial t^2} + \nabla \cdot \left( -\frac{1}{\rho} (\nabla p(t, \mathbf{X}) + F) \right) = Q$$

Neumann boundary conditions,  $\Gamma_{abc}$  and  $\Gamma_{rbc}$ , were used to dictate how sound waves interacted with walls and the observer’s head. The head used an impedance boundary condition and the walls used an absorption boundary condition.

## III. Solving the PDEs

The PDEs were solved using discretization using the finite element method for easy implementation on digital computers. The results returned were in the form of interpolating functions. The Helmholtz PDE was also parametric, with the parameter being frequency.

## IV. Visualizing and Interpreting Results

By plotting the interpolating functions, many of the expected behaviors become apparent, as shown in Figure 2. Sound propagation in the time domain occurs as anticipated and effects such as head shadowing are visible in the pressure distribution plots. By solving the PDEs with discretization, the data is no longer continuous and hence yields certain anomalies in the data; however, these anomalies aren’t too noticeable when it is applied to the audio.

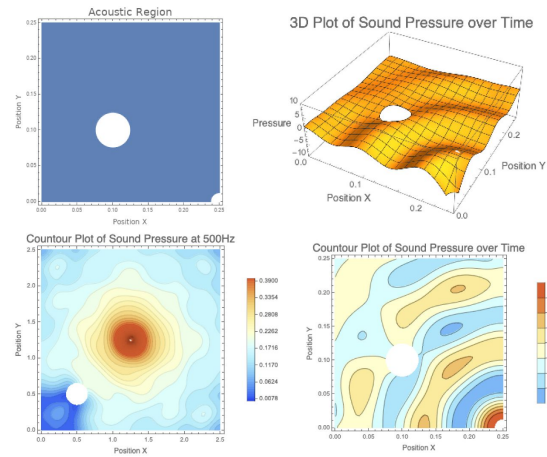


FIGURE 2: Graphs are identified one through four starting at the top left clockwise. Graph one shows the anechoic region with the large white circle representing the observer's head and the small white quarter circle at the bottom right representing the sound source, defined by a Neumann radiation boundary. Graph two and three display the pressure distribution at a single point in time as a contour and three-dimensional plot respectively. Graph four shows the pressure distribution when a monopole source emits a 500Hz frequency.

## AUDIO PROCESSING

Having determined an HRTF that accepts a frequency and a spatial location as parameters, the next step would be applying the functions to an audio input. The most effective way to do so is by using a Fast Fourier Transform and an Inverse Fast Fourier Transform pair along with a window function to fill in any discontinuities that appear while processing.

### I. Fourier Transform

Decomposing the original audio into a sum of sinusoids using a Discrete Fourier Transform gives access to frequency intervals which can be attenuated using the parametric function obtained by solving the Helmholtz equation. Additionally, applying the Fourier Transform allows for informative visualizations using the spectrogram. The spectrogram helps visualize the changes in the

amplitude for each frequency interval and the quality of the generated audio.

### II. Attenuating Frequency Intervals

The spatial location of each ear is passed into the parametric function in addition to a frequency parameter. To expedite processing time, frequencies were inputted at intervals of 500Hz yielding a total of ten interpolating functions. While this didn't produce the most accurate results, it was the most computationally reasonable process. Obtaining an interpolating function from the parametric was a rather time-consuming operation.

Each interpolating function returns an attenuation coefficient for its specific frequency interval and is multiplied by the corresponding frequency in the original audio data. Once each frequency interval has been attenuated successfully, the generated audio is recreated using an Inverse Fast Fourier Transform.

### III. Hann Smoothing Window

Through this process, several artifacts are introduced into the generated audio and there is substantial data loss. To alleviate this problem, a Hanning (Hann) window was used to smooth discontinuities in the audio, preserve frequency resolution and reduce spectral leakage. Upon close examination of the spectrogram plots of the audio before and after applying the function, it is revealed that each frequency interval has been attenuated as expected, shown in Figure 3.

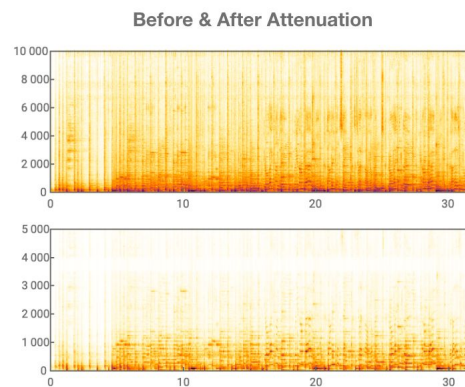


FIGURE 3: Spectrogram plots of the audio before and after attenuation in a single channel. Since the top end of the spectrogram became lighter, it is suggested that the higher frequencies are attenuated at a higher magnitude in comparison to the lower frequencies, as predicted. Notice the change in scale along the frequency axis for both graphs, the generated audio has no data for frequencies above 5000Hz. This is most likely attributed to a loss in quality after processing since experimentally measured HRTFs possessed data for those frequencies.

Other window functions including Blackman, Gaussian, and Poisson were used to experiment with different audio files. However, the Hann window was able to generalize to all tested audio inputs the best and outperformed the others in terms of quality.

### RESULTS

As seen in Figure 3, attenuation appeared to have been performed accurately. When compared to spectrograms of experimentally determined HRTFs, such as MIT KEMAR, performance is similar, but there are a few notable shortcomings. The most prominent was the low-quality audio output after processing.

One reason could be the significant data loss even after applying a Hann window. While some discontinuities were eradicated, the overall audio still experienced a noticeable loss in quality. Additionally, the introduction of artifacts in certain frequency intervals still persisted. The investigation presented in this paper was conducted in its entirety using the Wolfram Language in Mathematica [8], which is known for being a high-level language and may have been the cause of quality loss. The aforementioned issues would likely be resolved if the entire process was translated to a lower level language with proprietary algorithm implementations. Not only would this make the entire process run at a reduced time complexity, but it would also enable more

flexible experimentation since there would be no restriction to exclusively use the built-in functions offered by the Wolfram Function Repository.

Additionally, frequency interval ranges could have also been decreased to provide for a more immersive experience but would have come at the expense of processing time. This tweak would have required solving for more than the ten interpolating functions from the parametric function obtained from the Helmholtz equation. Hence, it wasn't feasible with the Wolfram Language. However, as mentioned earlier, lower language implementation may alleviate this problem. Note that all code from this project is stored in Github [9] and the preliminary work is documented in the Wolfram Community [10].

### FUTURE WORK

This project, although far from perfect, serves as a strong underlying foundation for future improvement. The proposed method produced reassuring results and provided a clear path for future work. As suggested in the results, one of the next steps would include transcribing the Wolfram Language code into a slightly lower level language like Python that would still offer built-in methods and frameworks that would streamline the development process, while still allowing for flexibility in experimentation and customizability.

Additionally, introducing the third spatial dimension into the model and comparing the monaural spectral cues it produces with experimentally measured cues could be interesting. Another possible extension would be to create three-dimensional renderings of an actual head to truly produce a custom HRTF. Most importantly, however, there is a need for a concrete metric to quantify the performance and quality of results. As of now, the comparison consisted of looking at the phase shift for each channel and the amplitude differences. If the project is implemented to simulate a three-dimensional space, the current form of analyzing results won't be as effective since it would

be difficult to closely examine the monaural cues through a spectrogram.

It may also be informative to investigate some of the behaviors of the model in an environment with obstacles and different types of boundaries. This may help gauge the accuracy and performance of the model. Another extension could include utilizing an accelerometer on the user's headset to determine their position relative to other objects in the simulated room and make changes to the audio in real-time. These ideas are indeed far-fetched but may be possible to implement if the quality of the audio is improved and the third spatial dimension is incorporated into the existing model.

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