

3.

a> sphere of radius  $R$  at  $C=(C_x, C_y, C_z)$

$$\text{obs} = \left\{ \begin{bmatrix} x \\ y \\ z \end{bmatrix} \mid (x-C_x)^2 + (y-C_y)^2 + (z-C_z)^2 \leq R^2 \right\}$$

$$b(o_i) = \begin{cases} \frac{R}{\|o_i - C\|} \begin{bmatrix} o_x - C_x \\ o_y - C_y \\ o_z - C_z \end{bmatrix}, & \text{if } \|o_i\| \geq R \\ \begin{bmatrix} o_x - C_x \\ o_y - C_y \\ o_z - C_z \end{bmatrix}, & \text{if } \|o_i\| < R \end{cases}$$

use above for  $\|o_i(q_j) - b\|$  &  $o_i(q_j) - b$ .

b> cylinder with infinite height:

$$\text{obs} = \left\{ \begin{bmatrix} x \\ y \\ z \end{bmatrix} \mid \underbrace{x^2 + y^2}_{\vec{v}} \leq R^2 \right\}$$

$$b(o_i) = \begin{cases} \frac{R}{\|\vec{v}\|} \begin{bmatrix} o_x \\ o_y \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ o_z \end{bmatrix}, & \text{if } \sqrt{o_x^2 + o_y^2} \geq R \\ \begin{bmatrix} o_x \\ o_y \\ o_z \end{bmatrix}, & \text{if } \sqrt{o_x^2 + o_y^2} < R \end{cases}$$

use above for  $\|o_i(q_j) - b\|$  &  $o_i(q_j) - b$ .