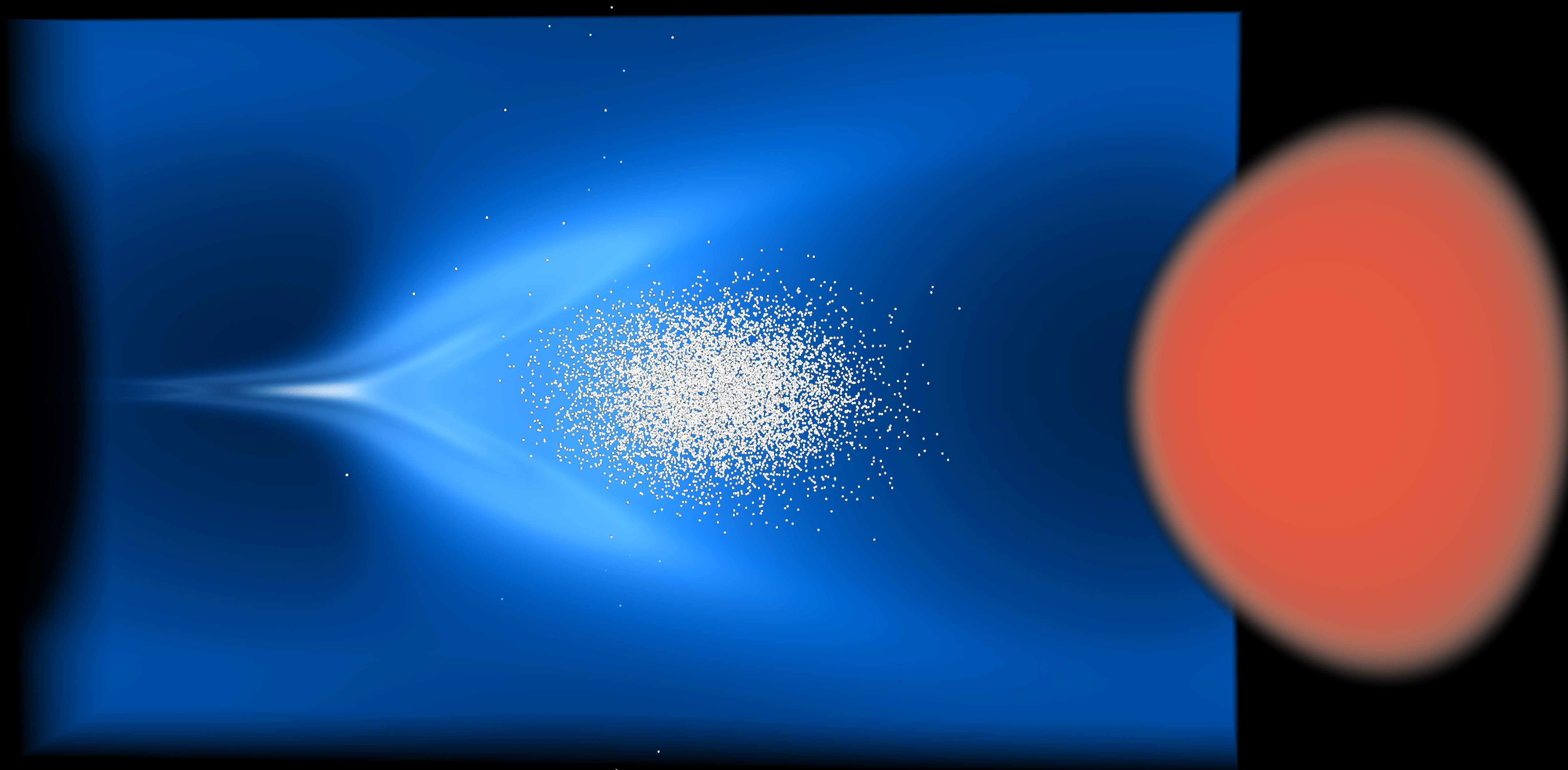
Simulation of Laser Wakefield Acceleration



Francesco Massimo, LPGP

1-4 Dec 2023

Outline

- Why plasma accelerators?
- Basics of plasma acceleration
- Numerical simulation of plasma acceleration: PIC codes
- The PIC code Smilei
- Introduction to the case study and the practical

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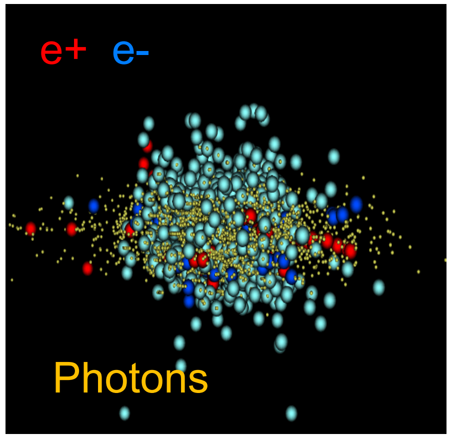
Applications of high energy electrons (just a few)

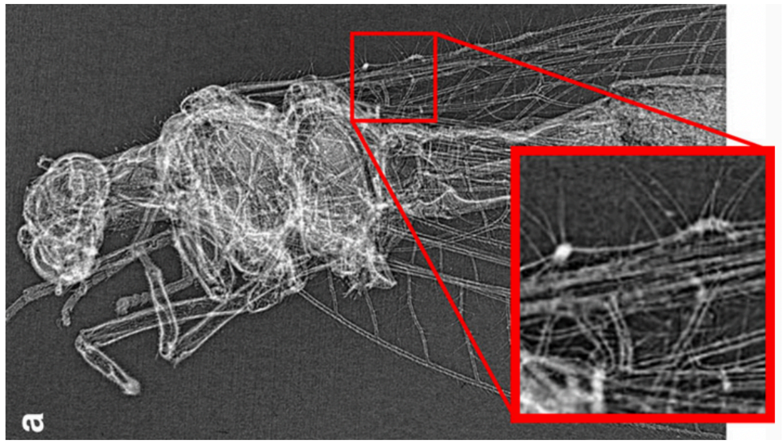
Fundamental Research:

- QED, Particle physics
- Matter Physics
- Biology

Smilei Simulation of QED e+e- pairs creation from photons

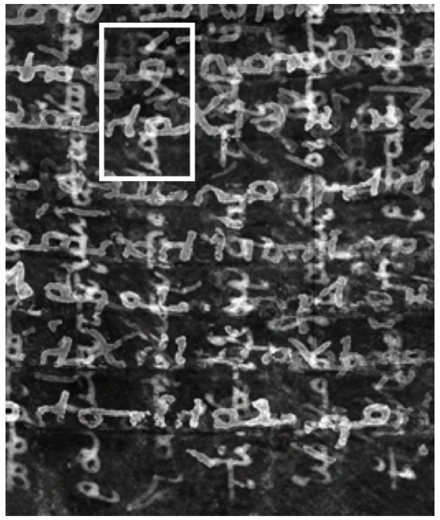


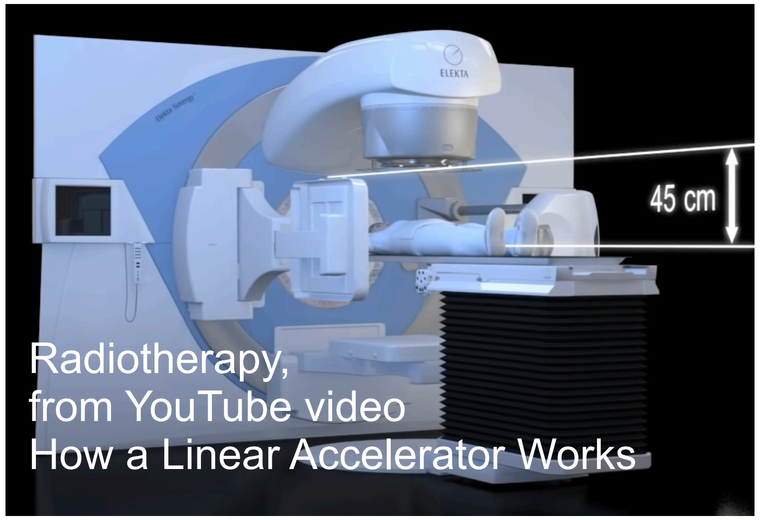
J. Wenz et al., Nat Comm 2014
Imaging through Betatron radiation



Medicine, Industry, Heritage, …:

- Cancer treatment,
- Medical imaging
- Electronic industry
- Study of materials
- Authentication of artwork
- …





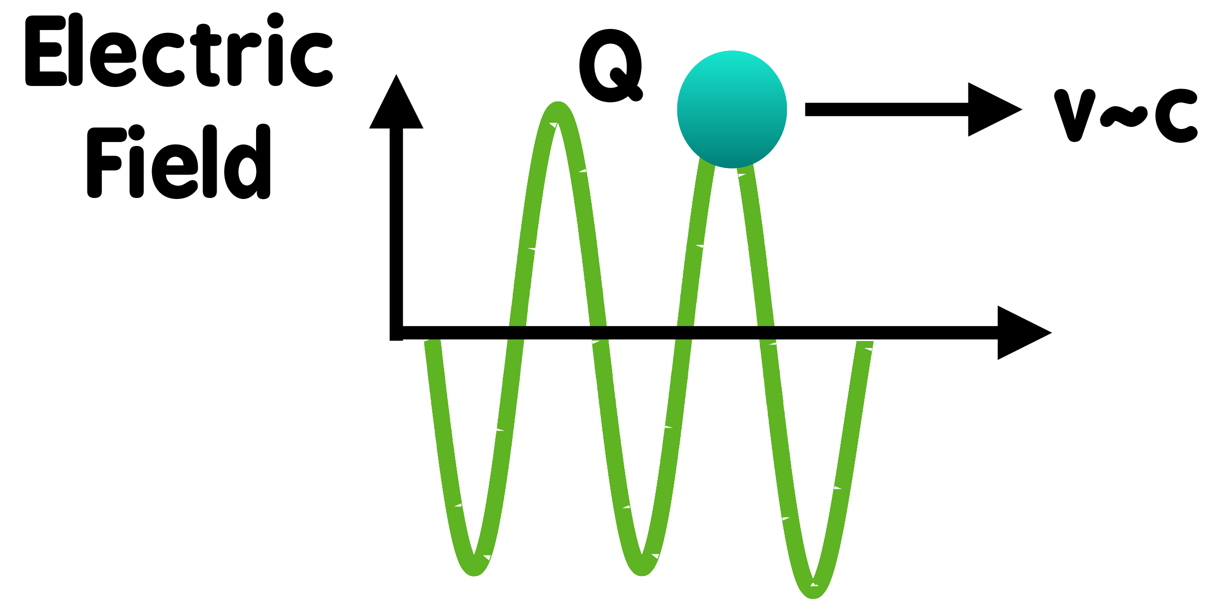
Hidden Archimede's Palimpsest, revealed by SLAC's synchrotron radiation in 2005 (U. Bergmann)

Particle accelerators size and cost

Relativistic charge **Q**

In an accelerating cavity of length **L**

With peak accelerating field **E**



Maximum energy gain = Q E L

Given a target energy,

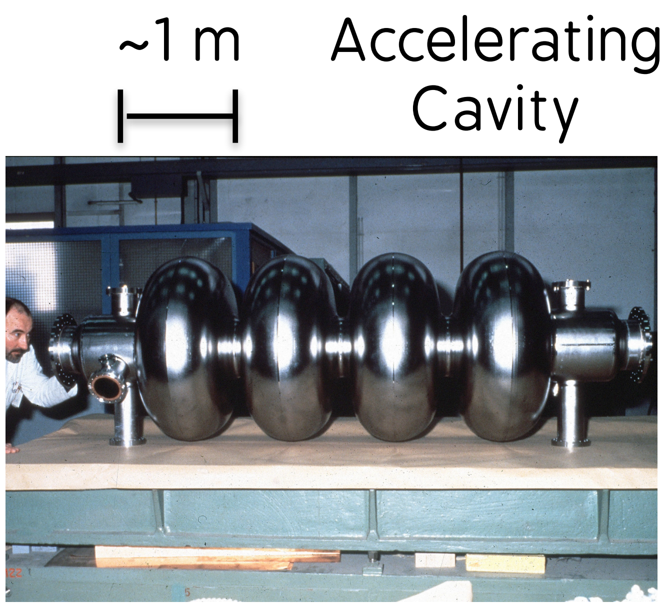
if **E** is limited by technology, **L** increases

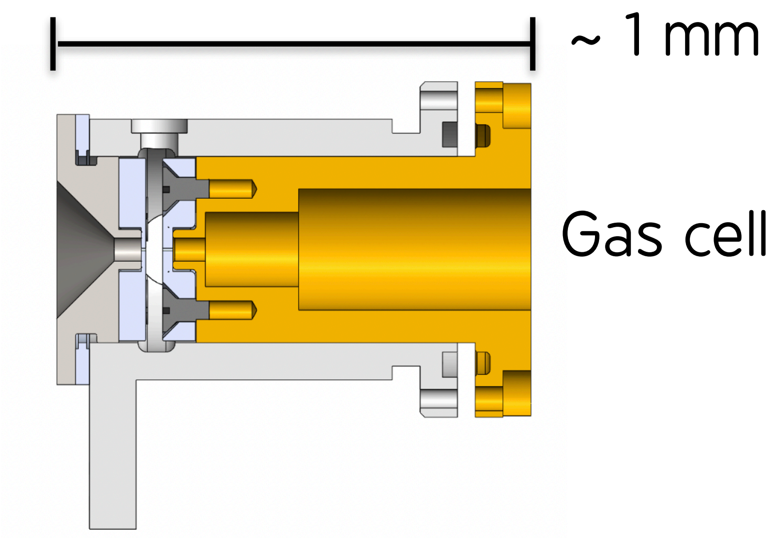
→ need more metallic cavities

→ the accelerator size and cost increase

Particle accelerators size and cost

Accelerator technology	Peak Accelerating Field	Acceleration length to gain 100 MeV
Radiofrequency metallic cavities	~10^2 MV/m	1 m
Laser Wakefield Acceleration (LWFA)*	~10^4 MV/m	0.01 mm





***Open challenge: improve performances of Laser Wakefield Acceleration. Numerical modeling is necessary!**

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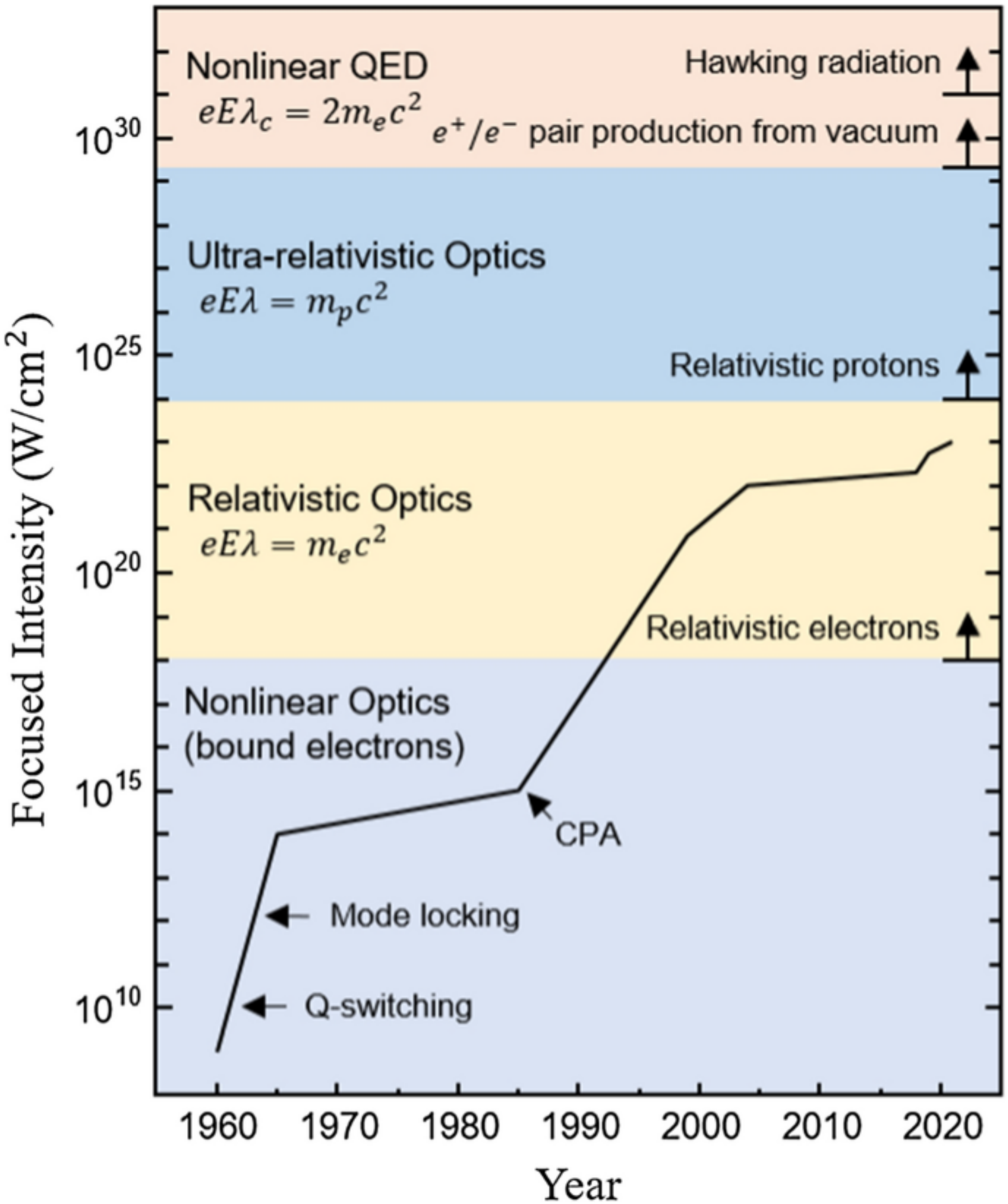
High Intensity Lasers and their interaction with matter



W. Bang et al, Journal of the Korean Physical Society 80,698–716 (2022)

Techniques:

- **Chirped Pulse Amplification**
- **Femtosecond Lasers**
- **Nonlinear Optics**
- …

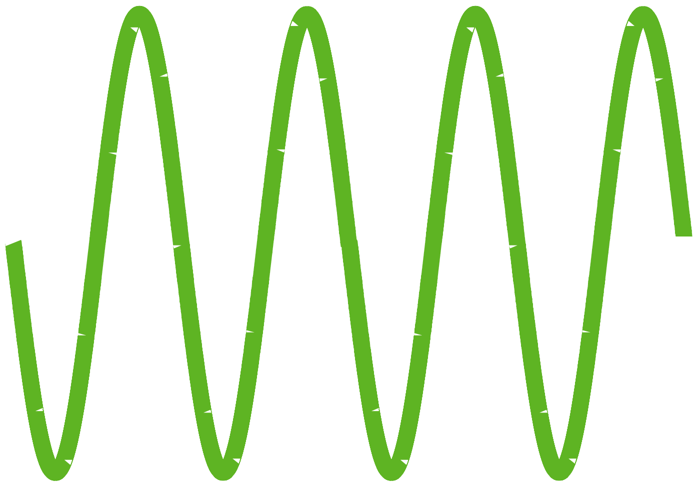
Physics Domains:

- Relativistic Fluids
- Physics of Relativistic Plasmas
- Relativistic Optics
- Laboratory Astrophysics

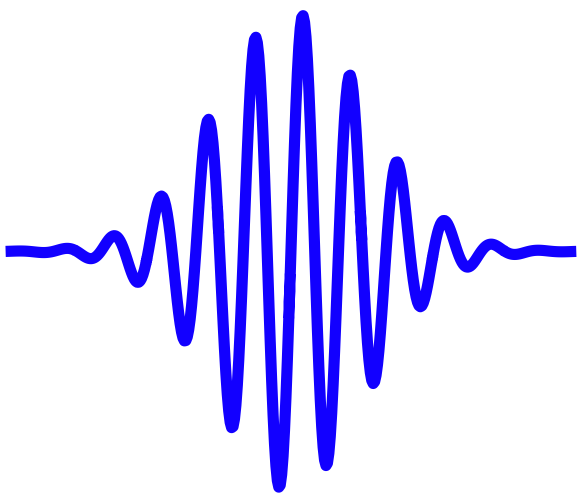
Applications:

- Electron and ion sources
- Acceleration of particles
- Radiation sources (UV, X, γ)
- Novel, high resolution diagnostics
- Pump-probe measurements

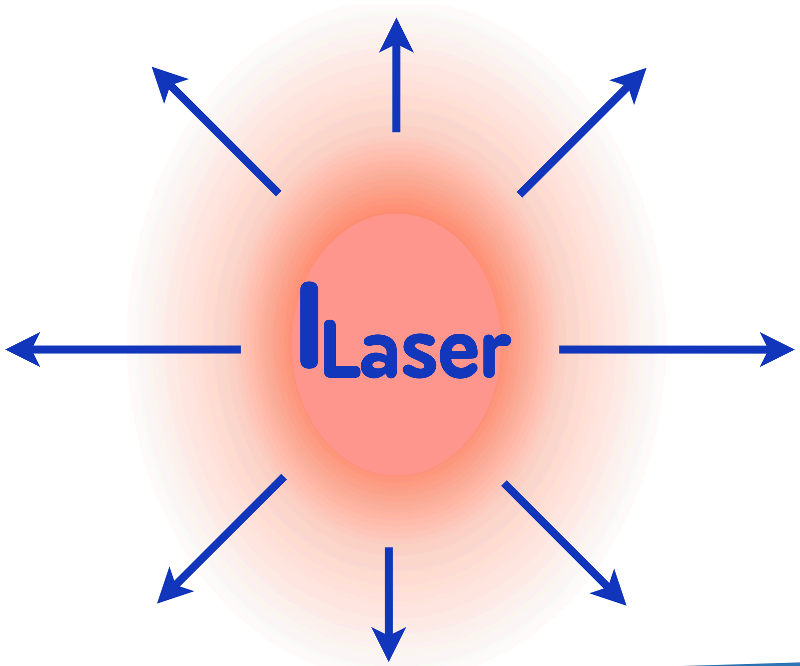
Ponderomotive Force:
the trigger for laser wakefield excitation in plasmas



Electron in infinite plane wave:
Oscillating Force



Electron in finite laser pulse:
Oscillating Force + Ponderomotive Force



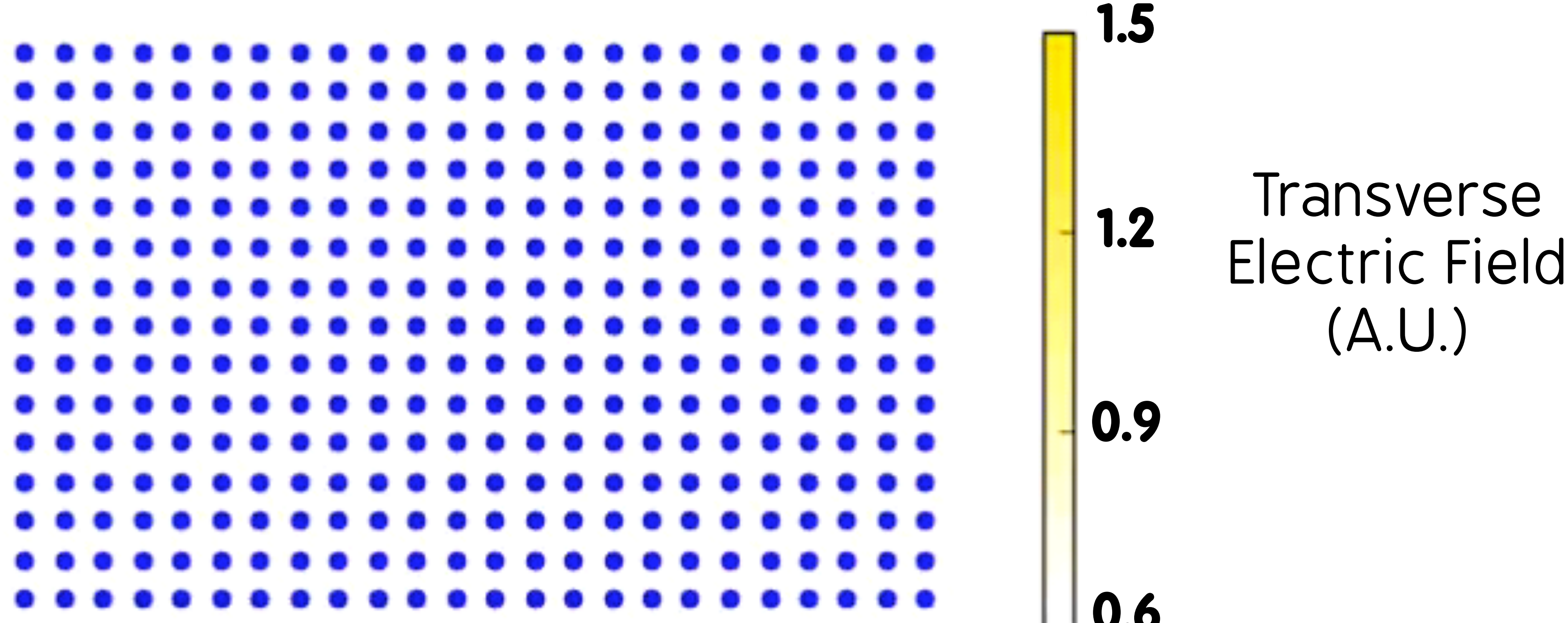
$F_{pond} \propto -\nabla I_{Laser}$ (a.k.a. radiation pressure)

Laser Wakefield Acceleration (LWFA):
plasma wave excitation by the laser ponderomotive force

Laser Beam Duration: 28 fs

Ponderomotive Force:

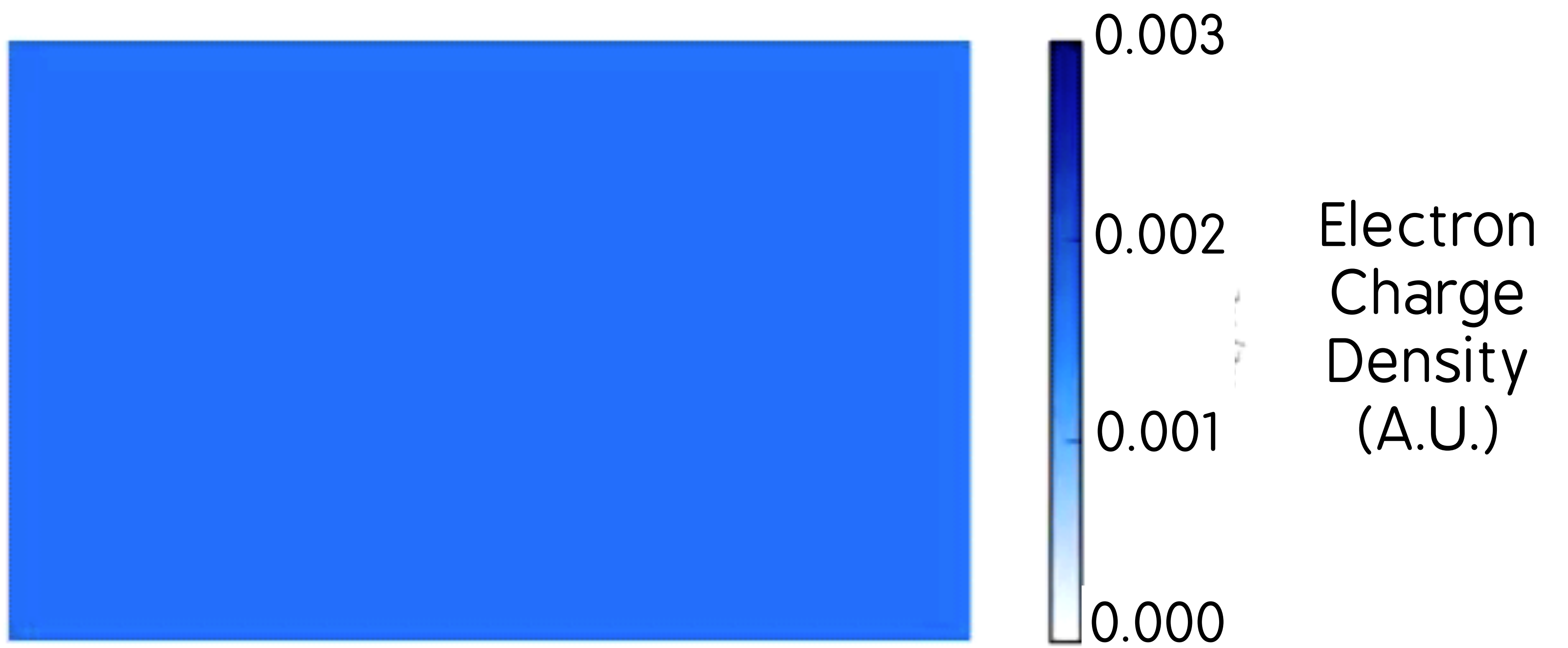
$F = -\nabla I_{Laser}$



Electrons • Immobile Ions ● $M_i >> m_e$

Plasma density: $3 \cdot 10^{18}$ cm^{-3}

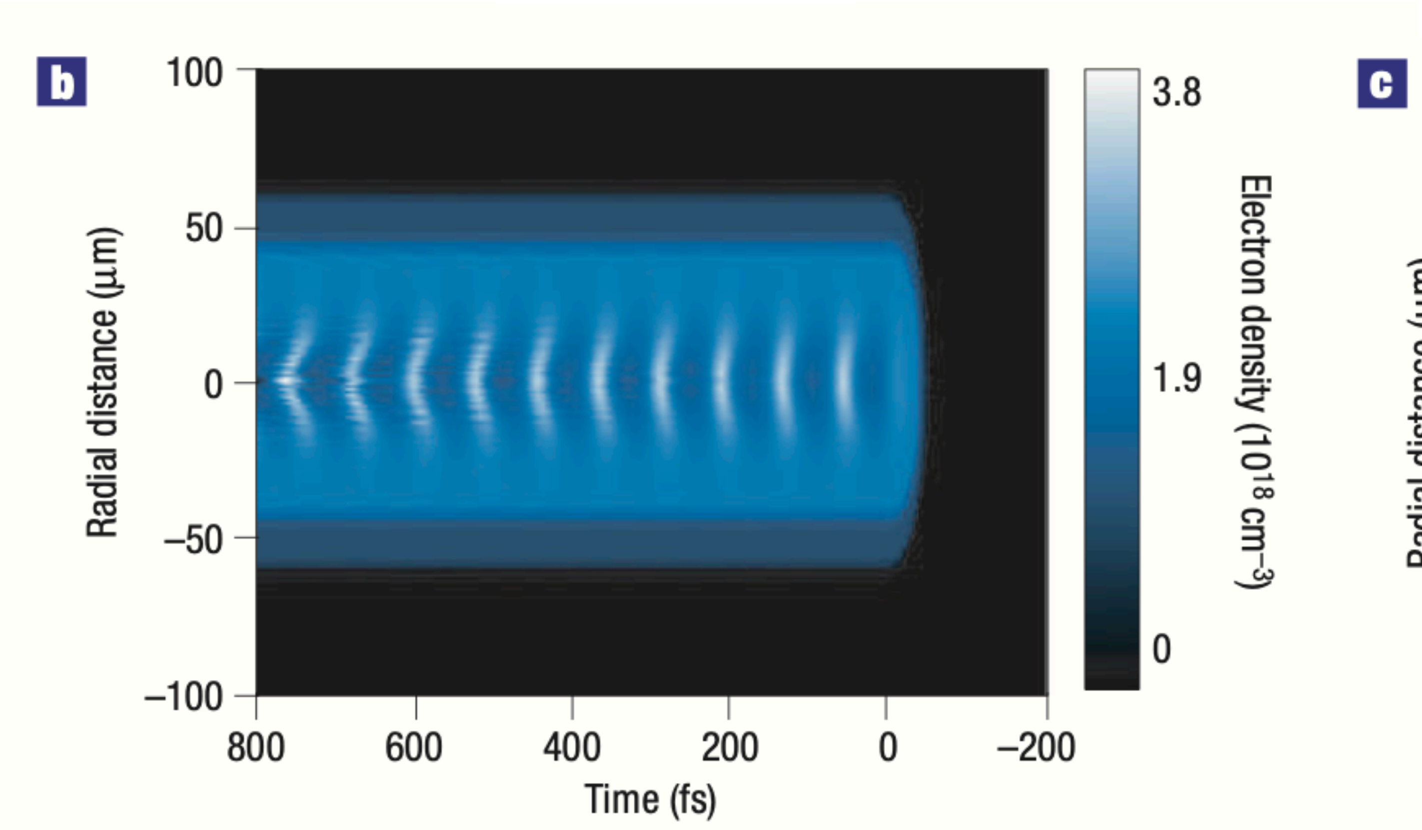
Plasma wavelength: ~20 µm

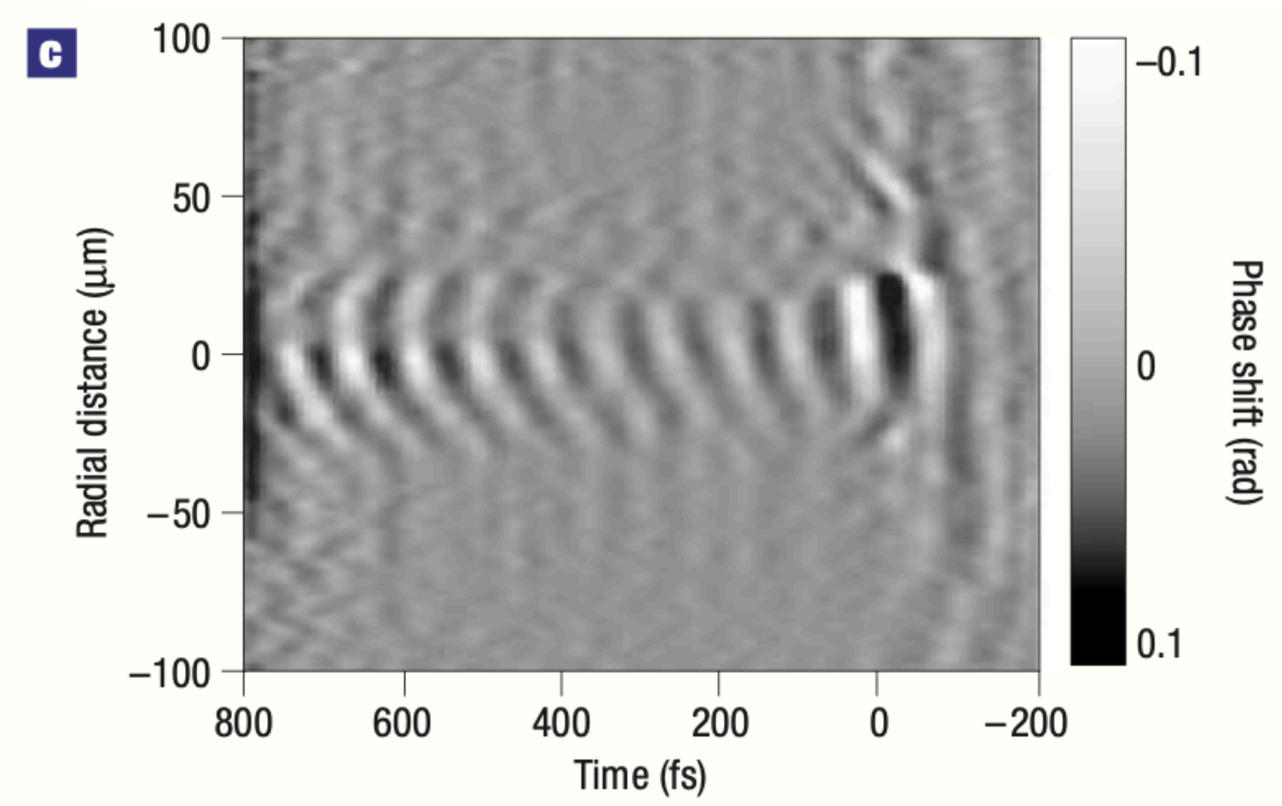


Laser Wakefield Acceleration (LWFA): visualising the plasma waves

Simulation

Experiment



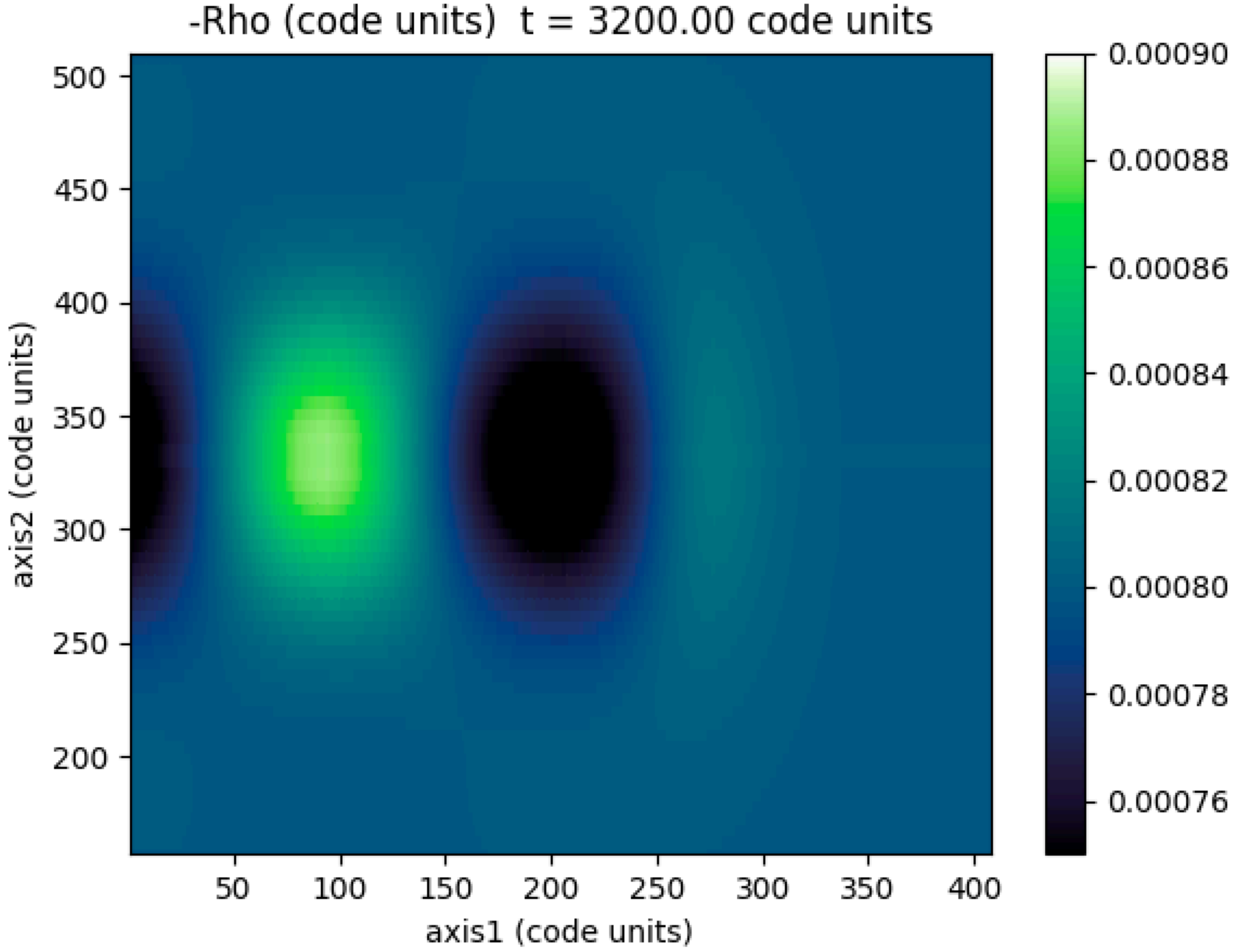


N. Matlis et al., Snapshots of laser wakefields, Nature Physics (2006)

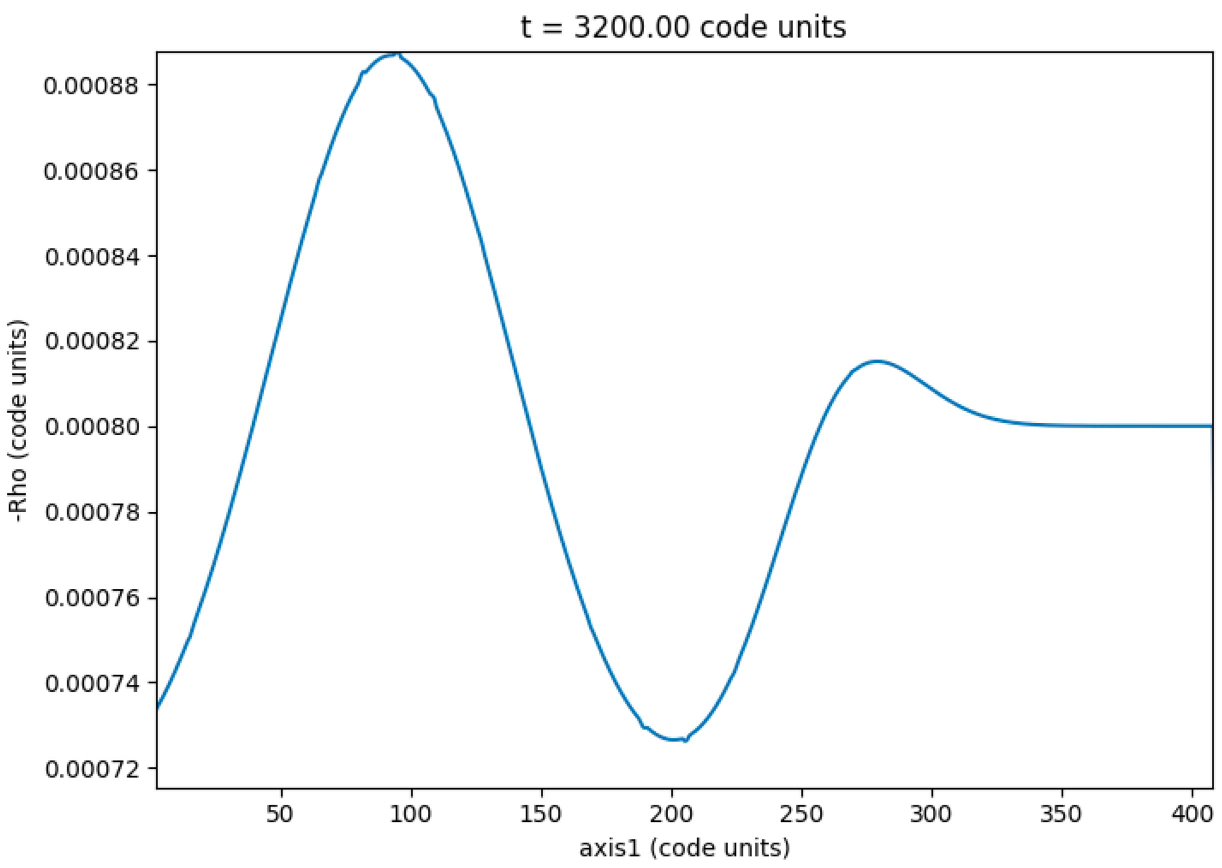
Laser wakefield excitation: linear regime

a_0 = normalized laser peak field = $0.86\ \lambda_0[\mu m]\ (I\ [10^{18}\ W/cm^2])^{1/2}$

$a_0 \ll 1$: Linear regime
Sinusoidal plasma waves at the plasma frequency



2D charge density

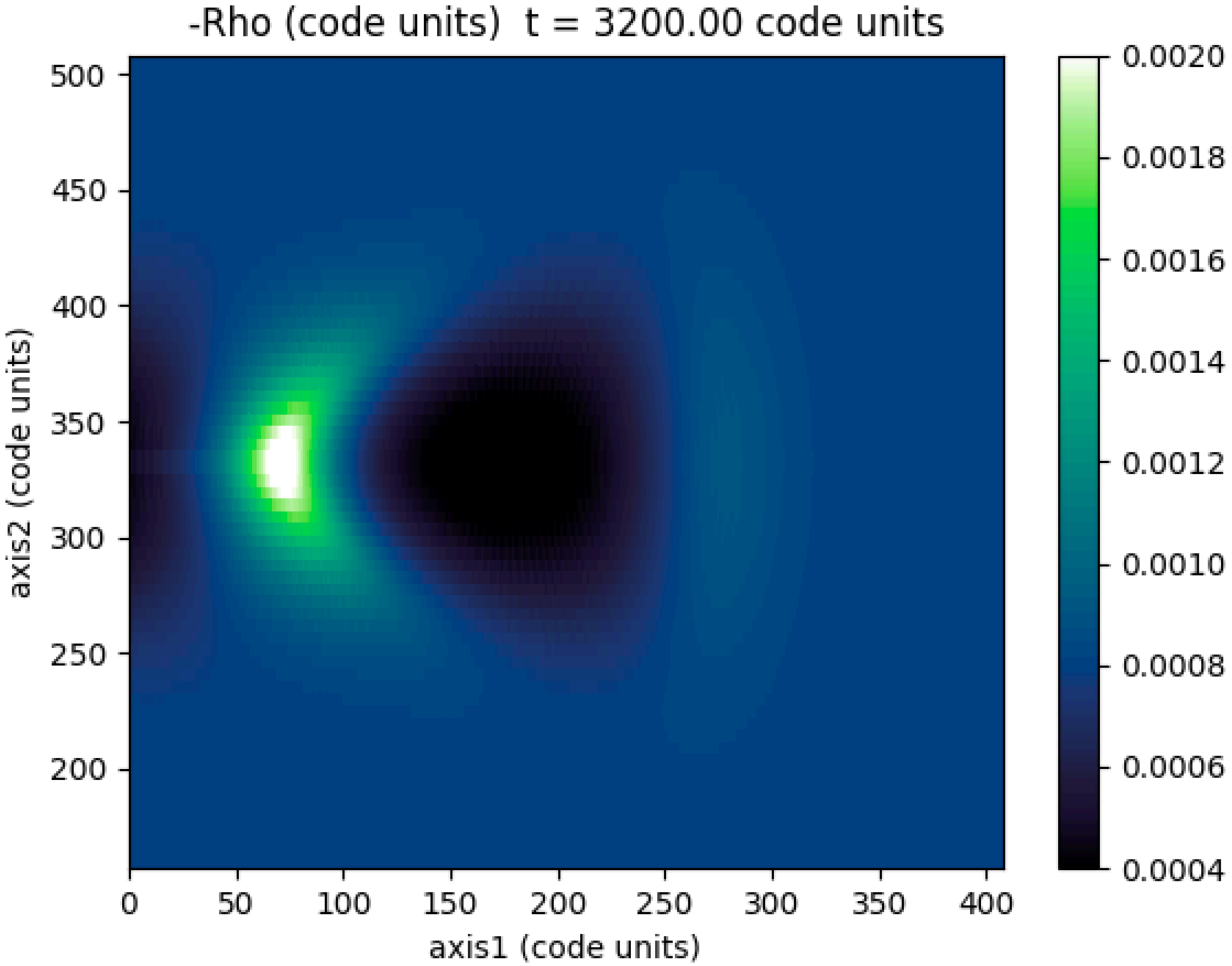


1D charge density
on propagation axis

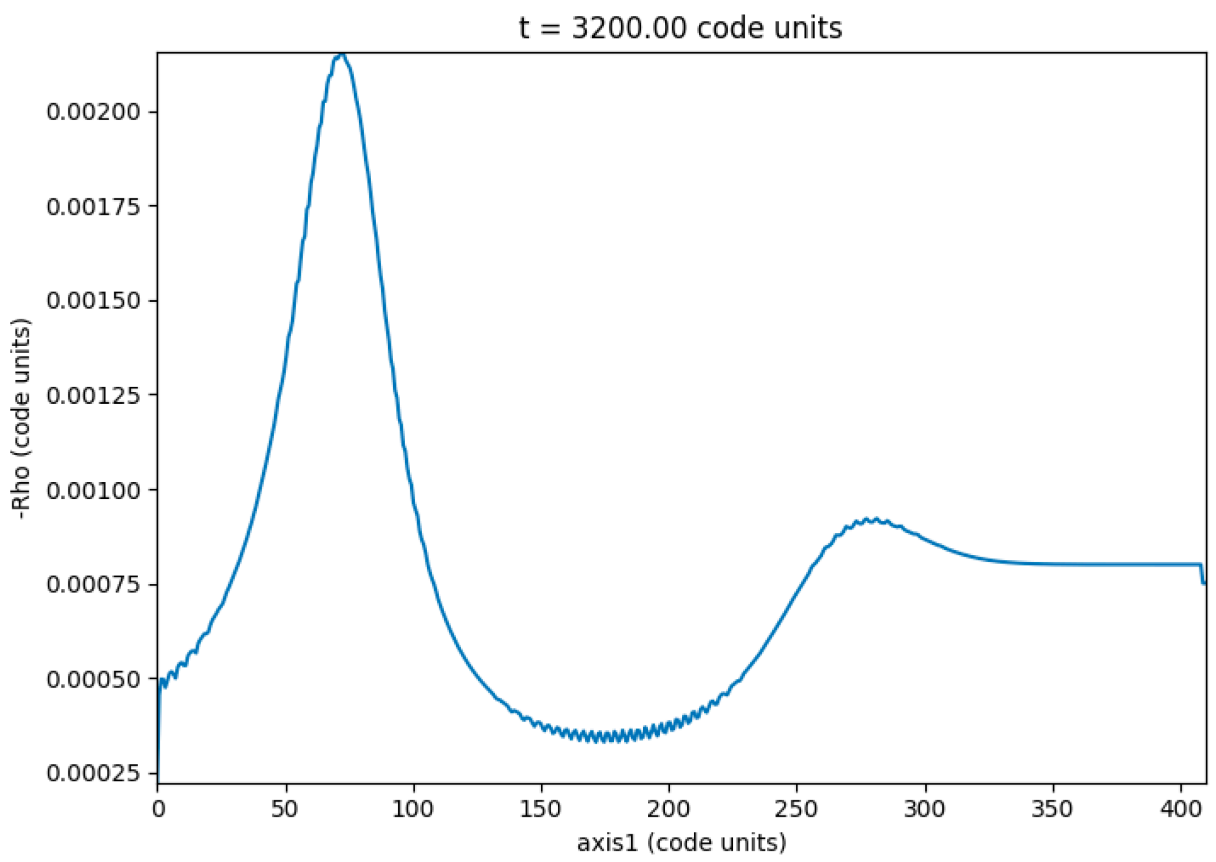
Laser wakefield excitation: weakly linear regime

a_0 = normalized laser peak field = $0.86\ \lambda_0[\mu m]\ (I\ [10^{18}\ W/cm^2])^{1/2}$

$a_0 \lesssim 1$: Weakly nonlinear regime



2D charge density

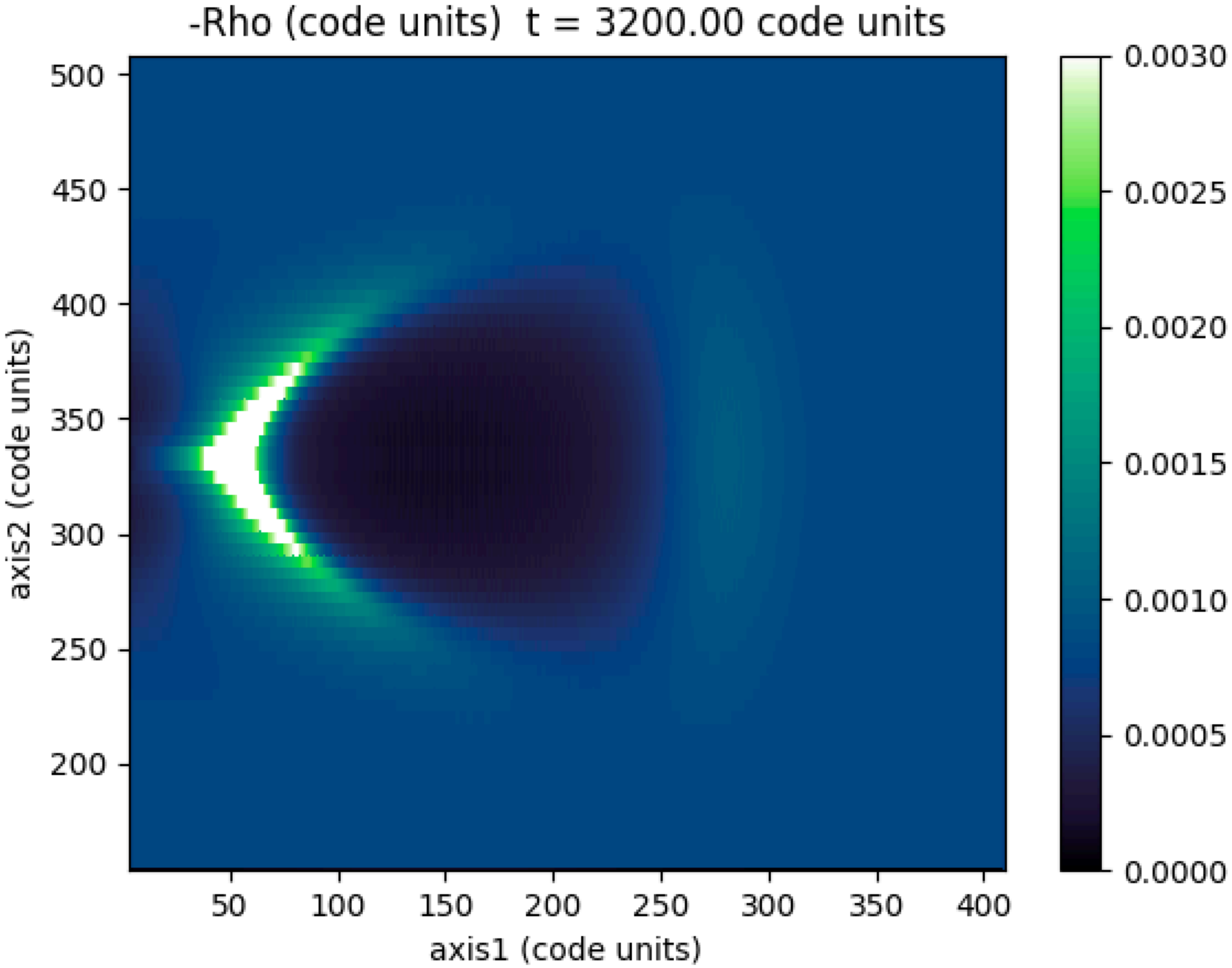


1D charge density
on propagation axis

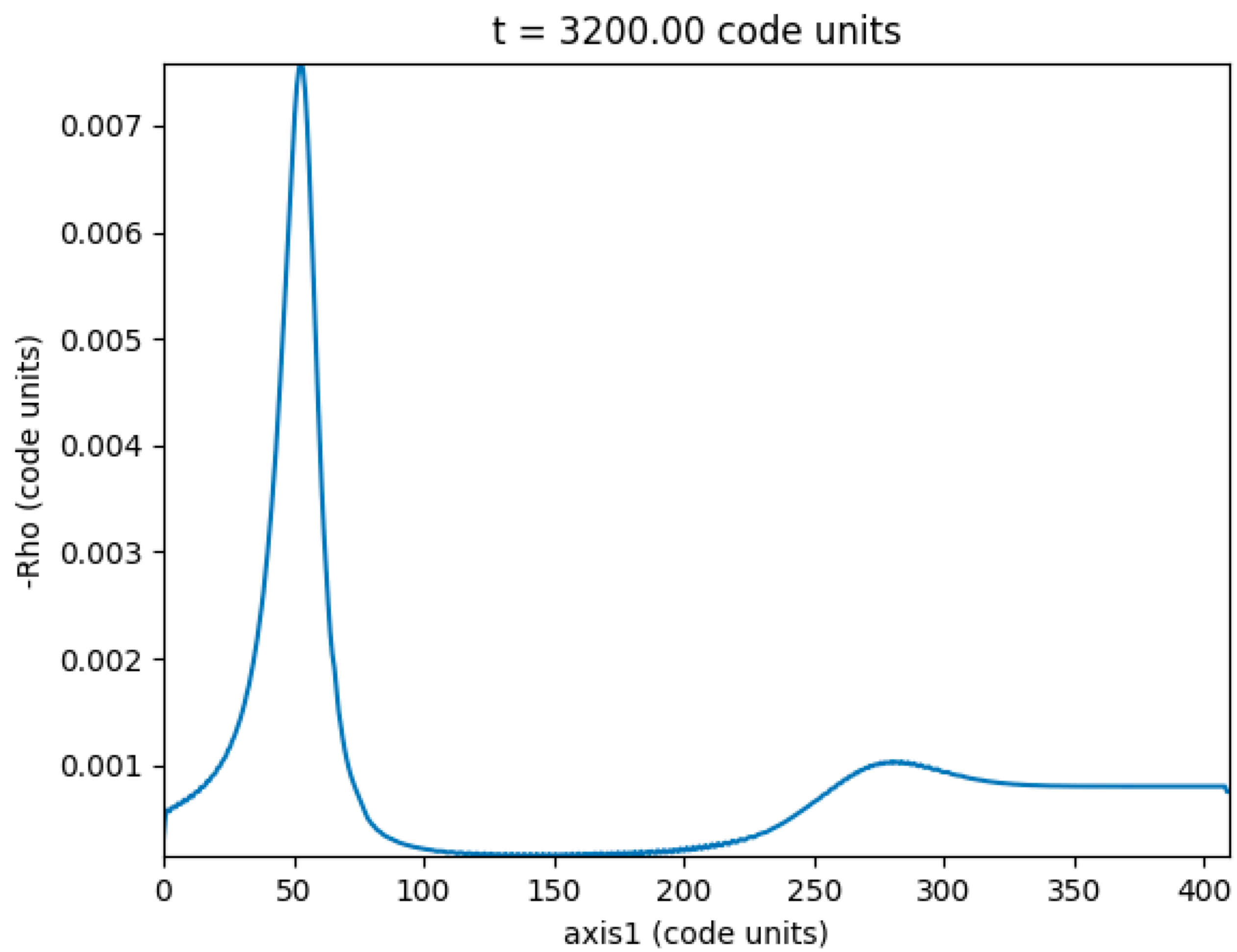
Laser wakefield excitation: nonlinear regime

a_0 = normalized laser peak field = $0.86\ \lambda_0[\mu m]\ (I\ [10^{18}\ W/cm^2])^{1/2}$

$a_0 > 1$: Nonlinear regime
"Bubble"-like waves



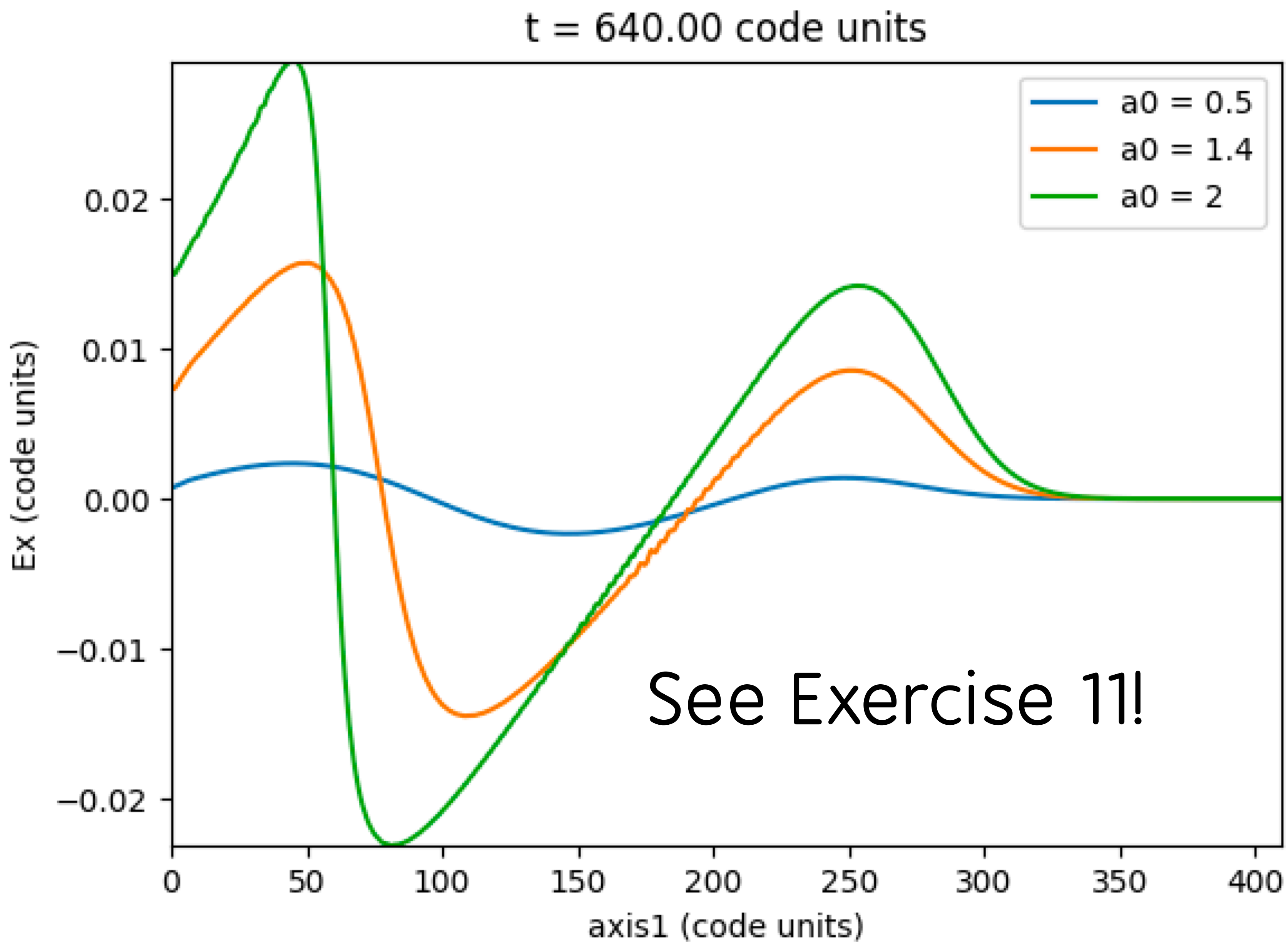
2D charge density



1D charge density
on propagation axis

Laser wakefield excitation regimes: Ex on axis

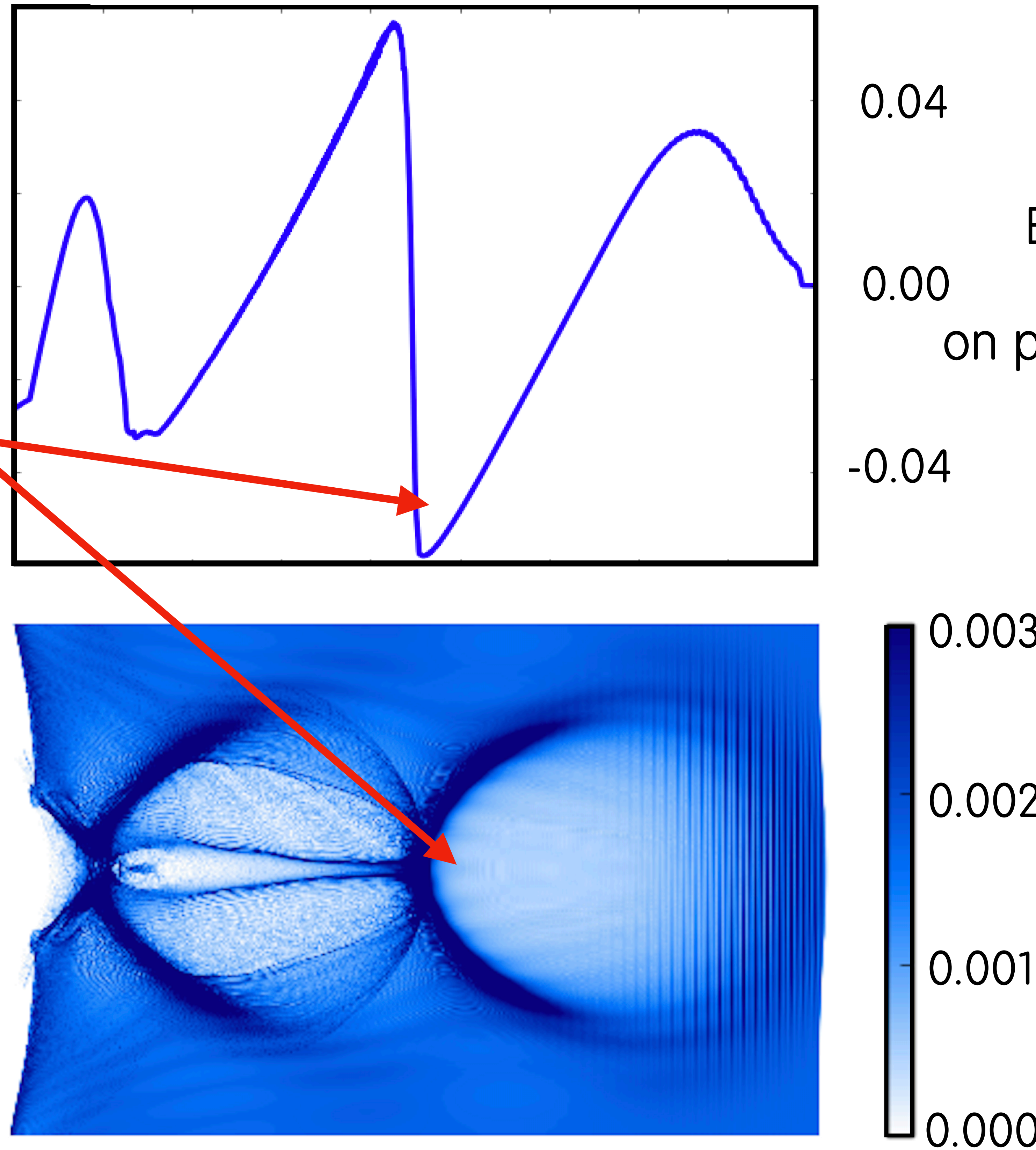
```
import happi
S1 = happi.Open("path/to/sim1"); Ex1 = S1.Probe.Probe0("Ex",timesteps=1000)
S2 = happi.Open("path/to/sim2"); Ex2 = S2.Probe.Probe0("Ex",timesteps=1000)
S3 = happi.Open("path/to/sim3"); Ex3 = S3.Probe.Probe0("Ex",timesteps=1000)
happi.multiPlot(Ex1,Ex2,Ex3,figure=3)
```



Laser Wakefield Acceleration (LWFA): accelerating electric field

E > 100 GV/m

Relativistic electrons injected here are accelerated towards the right



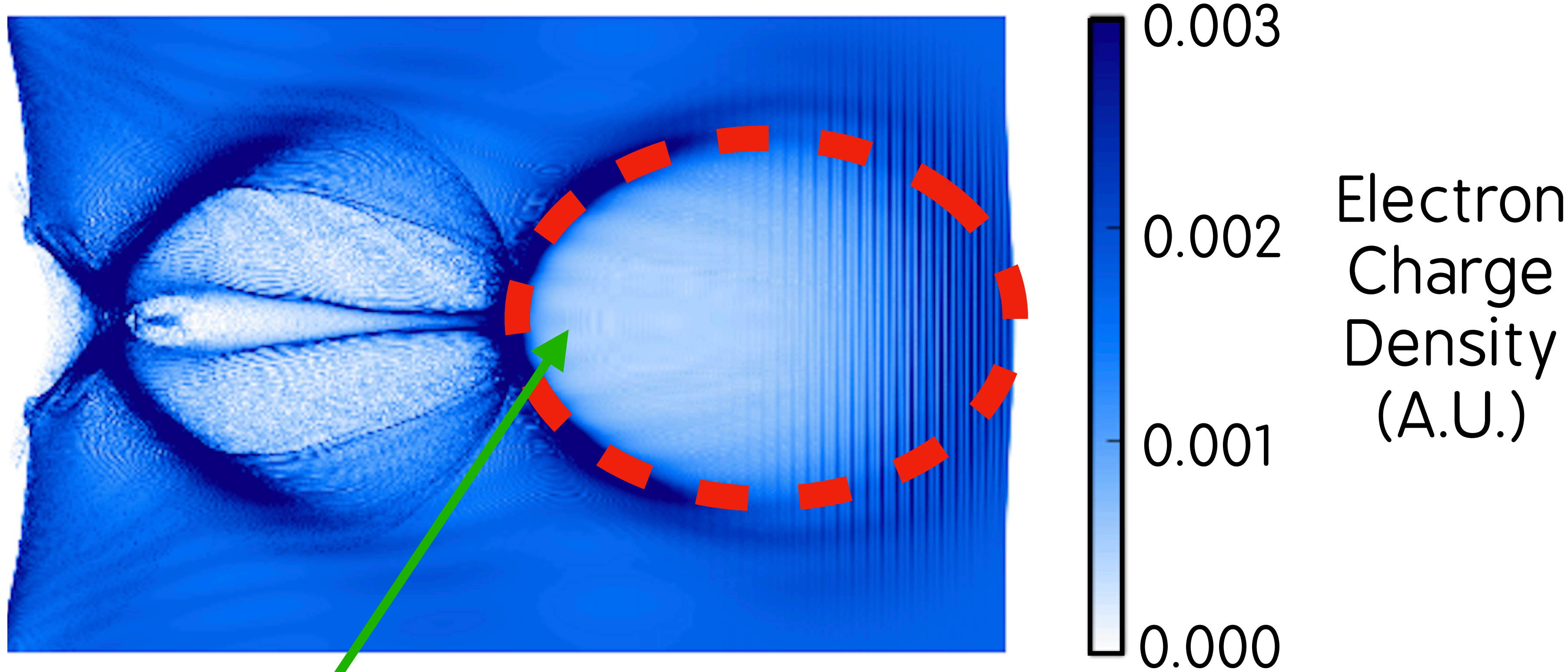
Longitudinal Electric Field (A.U.) on propagation axis

Electron Charge Density (A.U.)

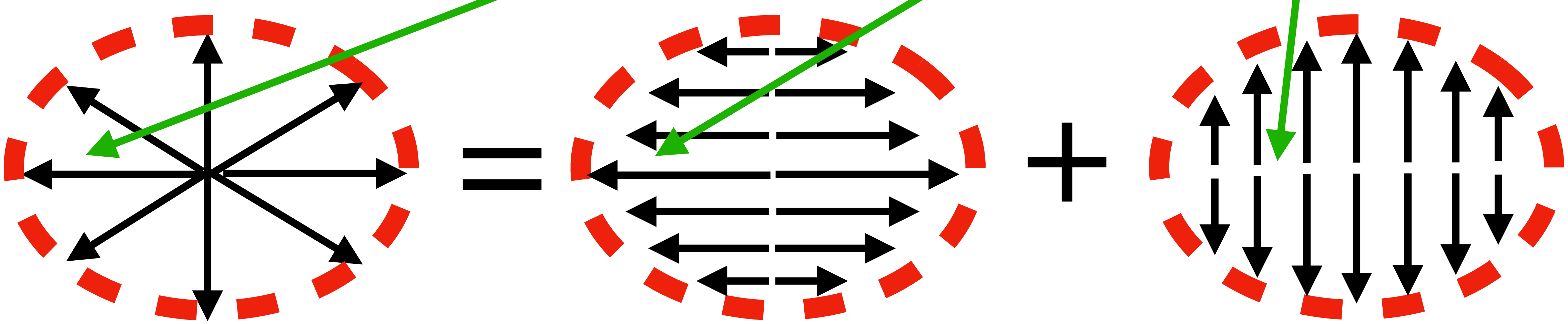
Nonlinear regime here

LWFA: Electric fields inside the “bubble”

Plasma wavelength: ~20 μm



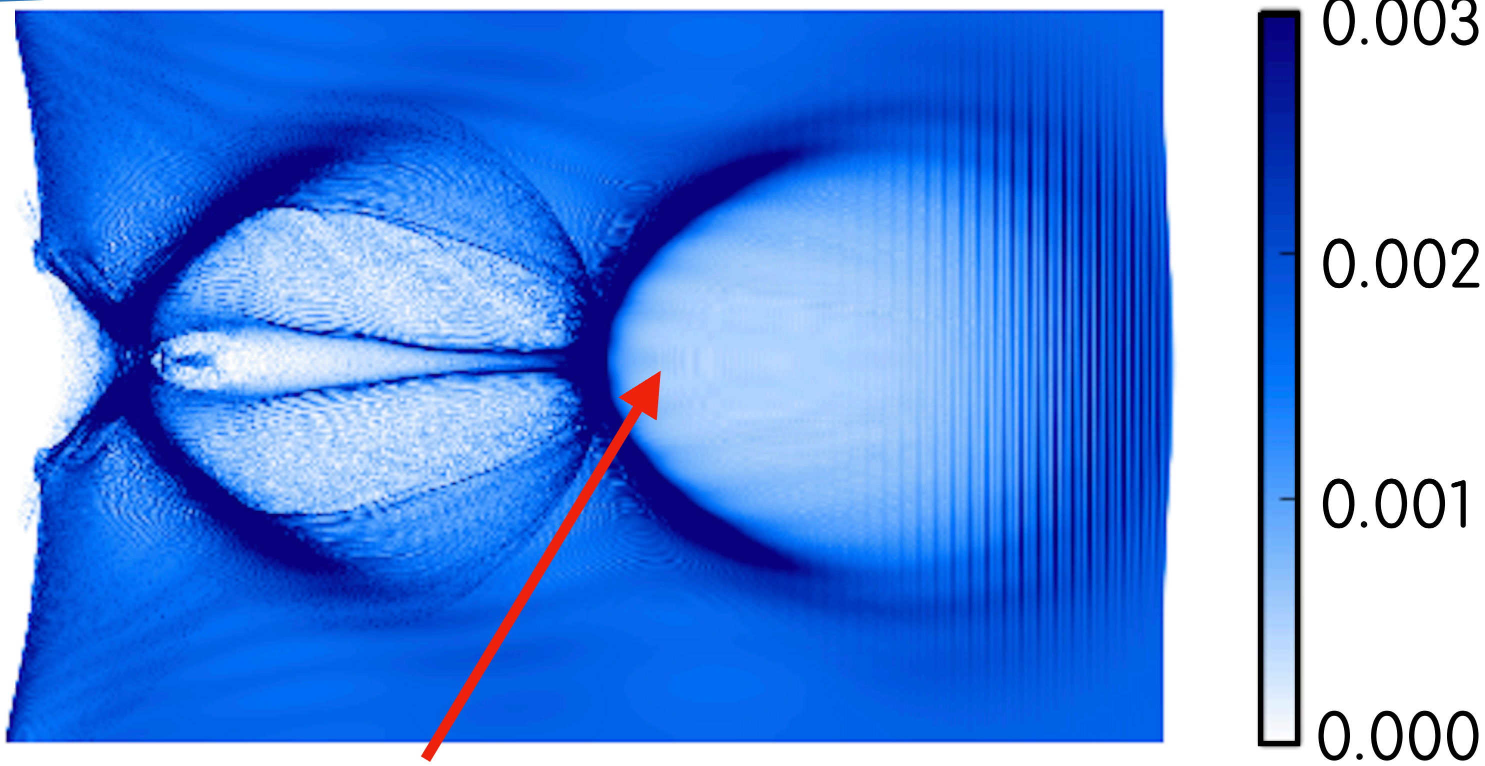
Relativistic electrons injected here are both accelerated and focused



$$\vec{E} = E_{\text{longitudinal}} + E_{\text{perpendicular}}$$

Fields inside the "bubble": effects on an electron beam

Plasma wavelength: ~20 μm



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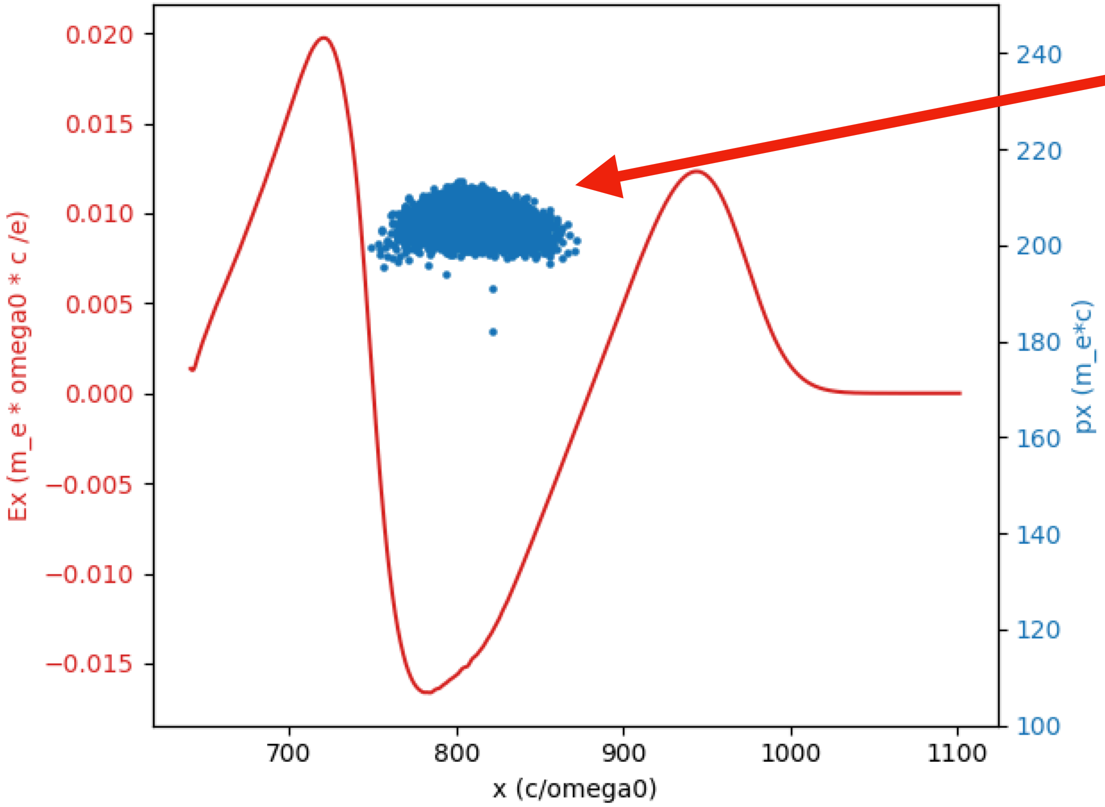
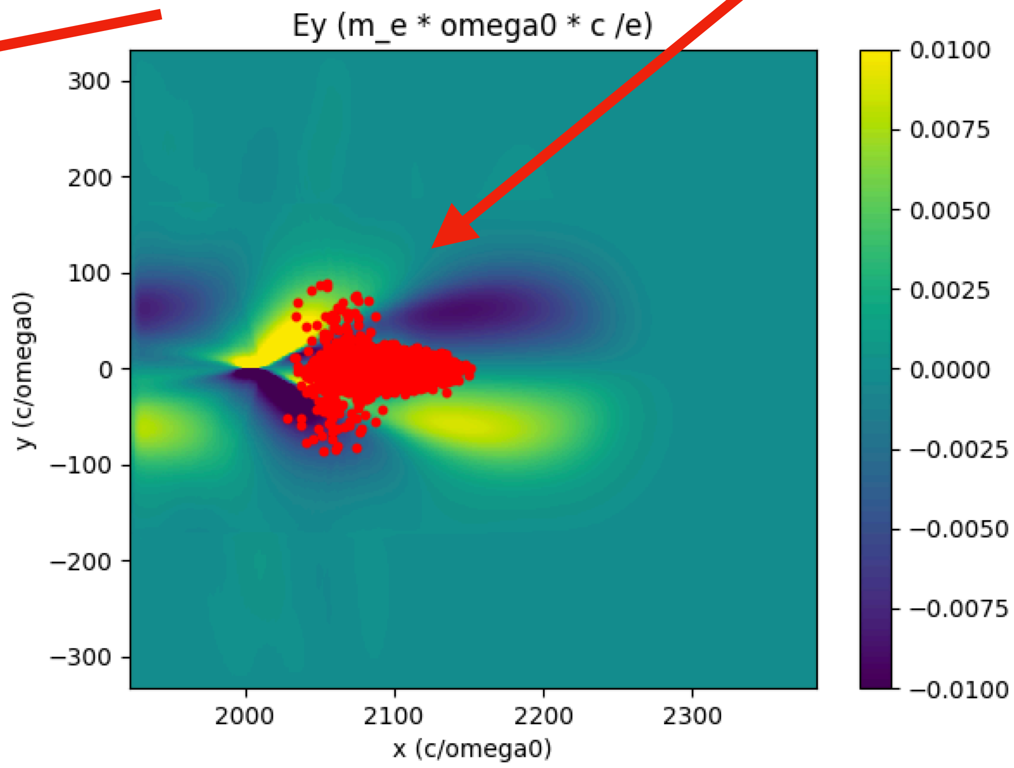
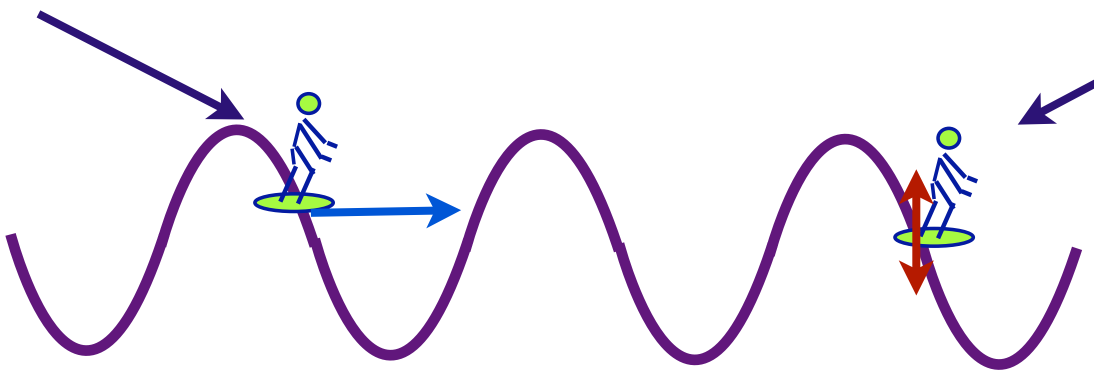




Laser Wakefield Acceleration (LWFA) challenges: injection

Surfer with
- sufficient initial speed,
- injected in the proper phase

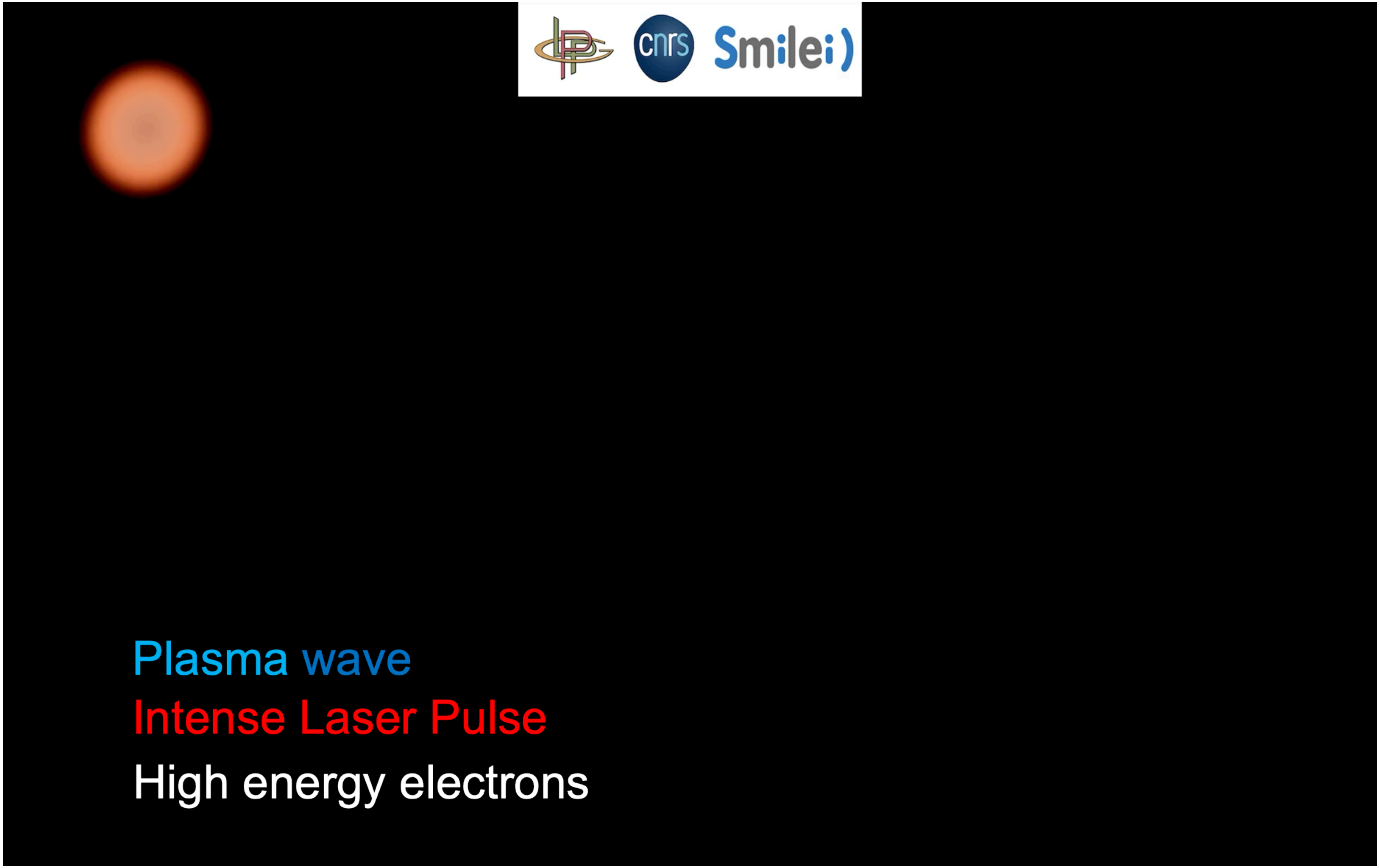
Surfer with
Zero initial speed



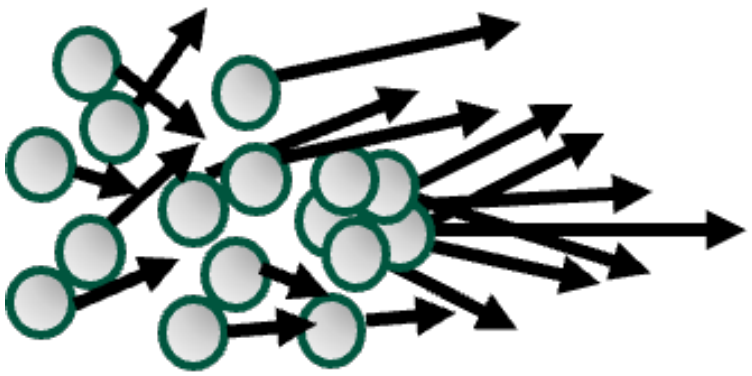
Surfer: electron
wave: electric field of the plasma wave in the wake of the laser

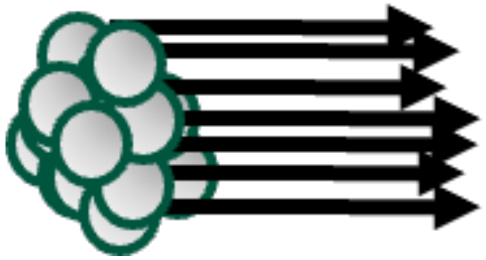
Plasma wavelength < 100 μm, Duration of the electron beam < 10 fs ~3 μm

Laser Wakefield Acceleration with ionization injection



LWFA objective (not the only one): realize compact electron accelerators for applications

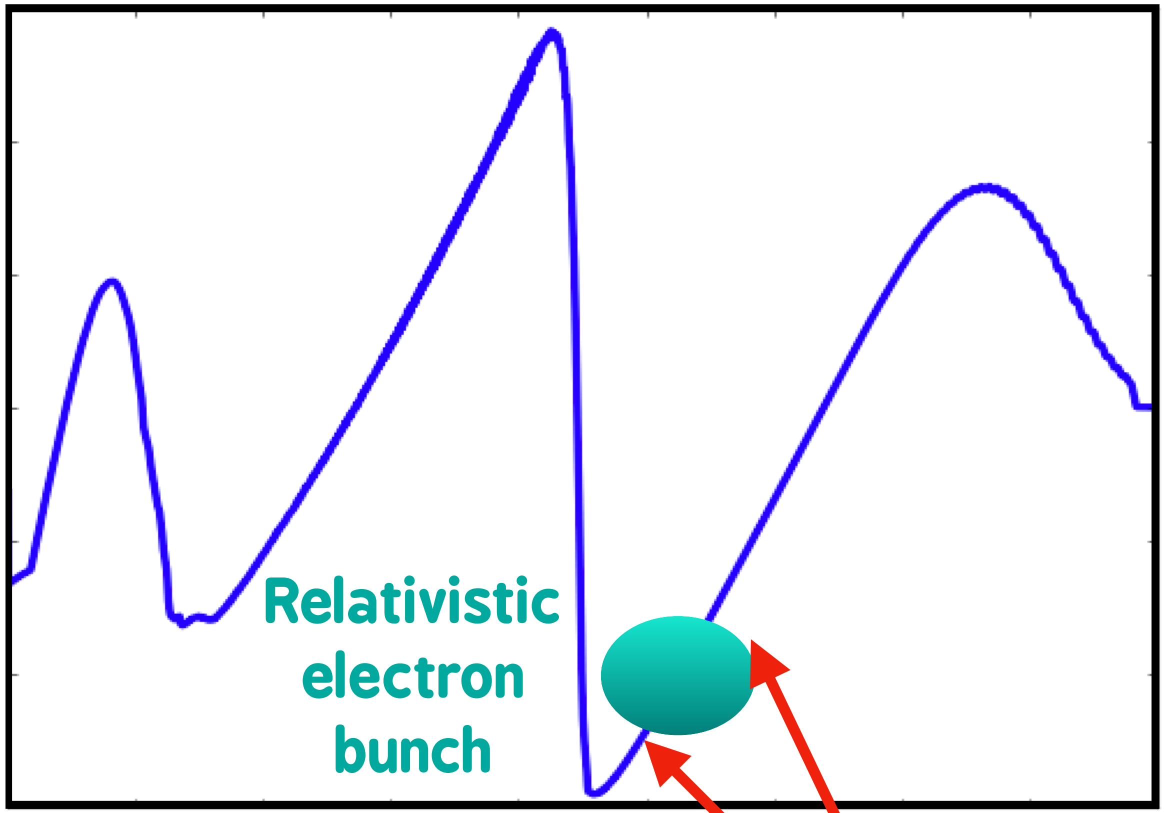




- Few electrons or many dispersed in space
- High divergence
- Different Energies (high energy spread)

- Many electrons in a small volume
- Low divergence
- Similar Energies (low energy spread)

LWFA challenges: reduce the energy spread

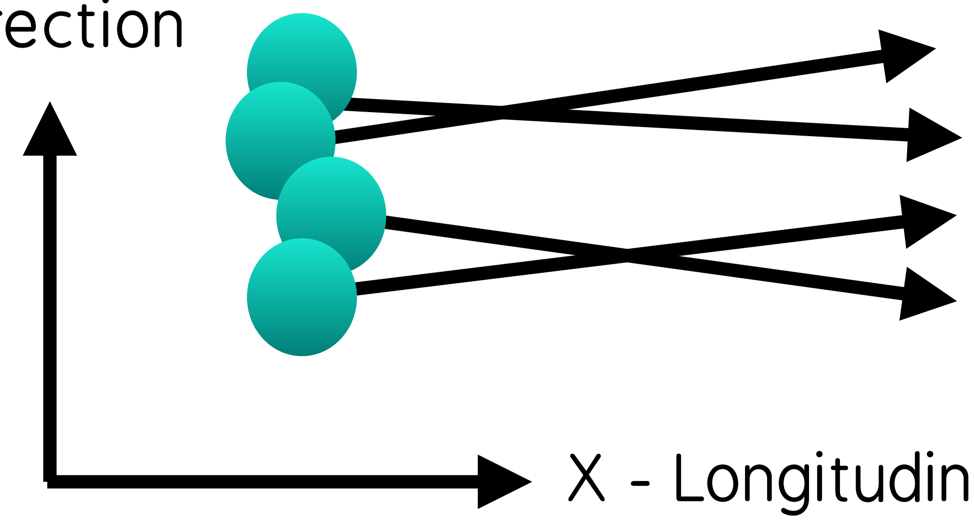


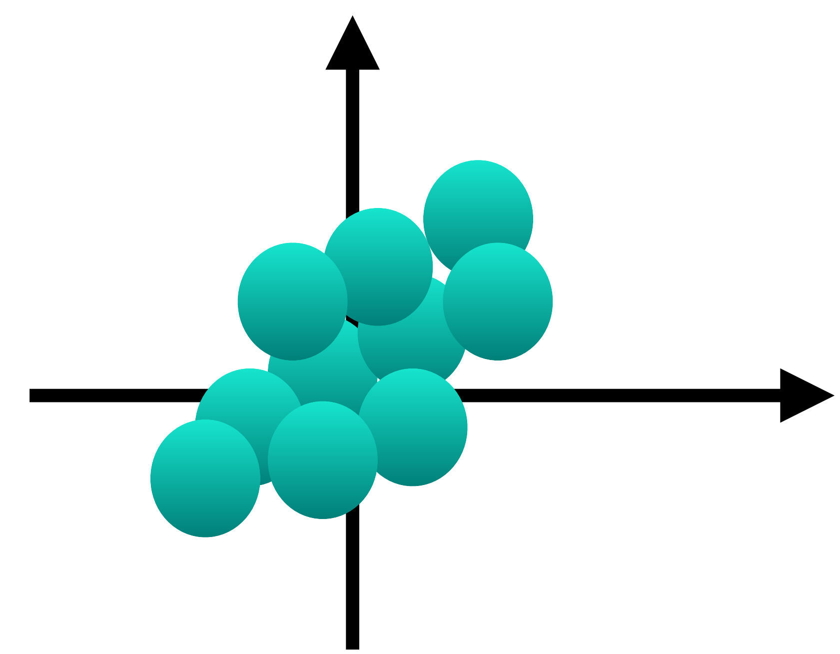
Longitudinal
Electric Field
(A.U.)
on propagation axis

Electrons injected
in different phases of the wave
will experience a different accelerating field

Energy spread increase

LWFA challenges: lowering the emittance





Most applications of accelerated beams require:
- Small transverse size (i.e. small σ_y)
- Small divergence (i.e. small σ_{p_y}/Energy)

→ **Minimize Transverse Emittance**

Transverse Normalized Emittance

$$\varepsilon_{ny} = \frac{1}{m_e c^2}\sqrt{\sigma^2_y\,\sigma^2_{p_y} - \sigma^2_{yp_y}}$$

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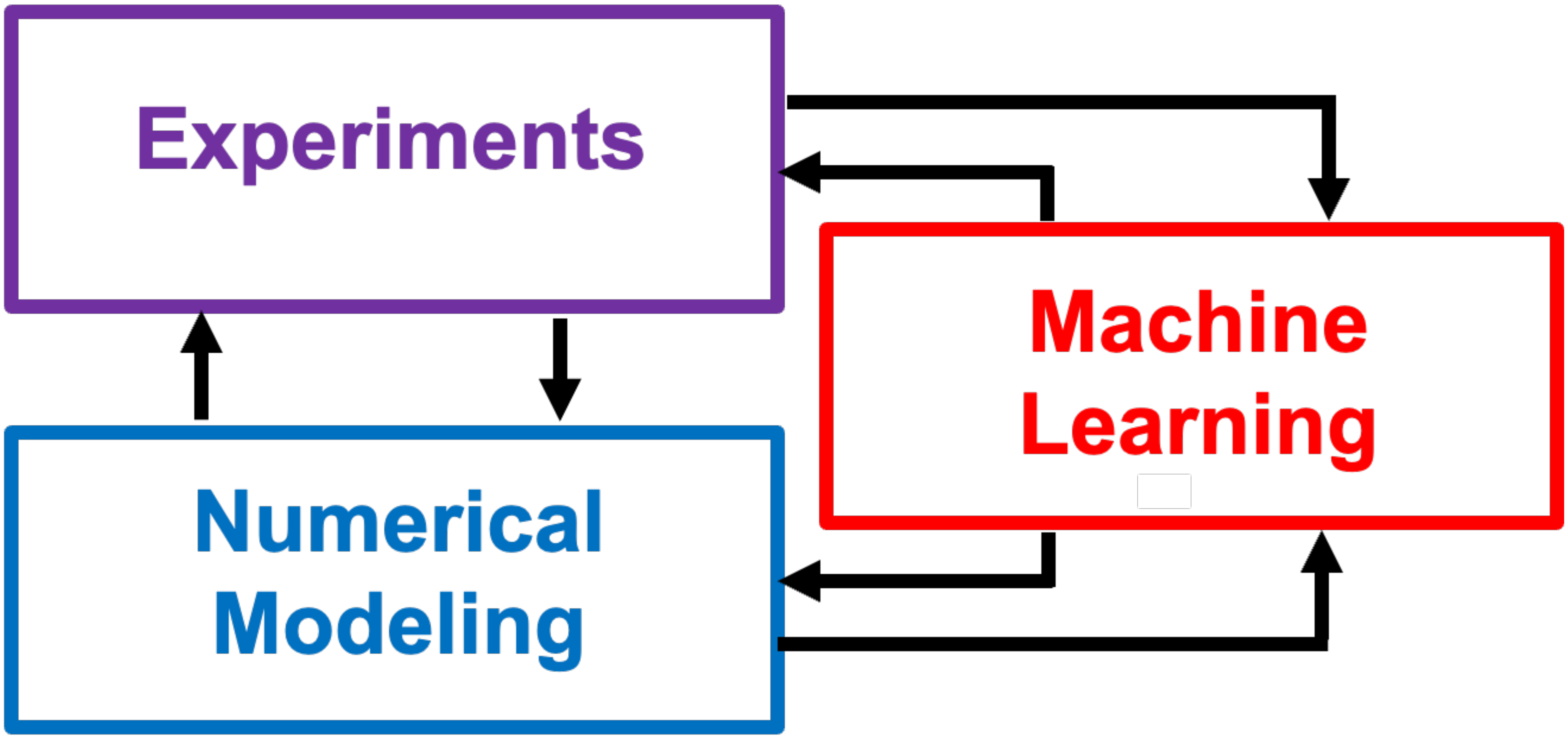
LWFA investigation techniques



Why numerical simulation is necessary for LWFA?

- **No general analytical solutions are available**
- **You cannot measure everything simultaneously**
- **Before the experiment:**
  - Study new physical phenomena
  - Conceive new kind of experiments
  - Design experiments (also using Machine Learning)
- **After the experiment:**
  - Analyze the data (also using Machine Learning)
  - Understand the physics

Model for Laser-Plasma Interaction in LWFA

Complete Maxwell-Vlasov system

Plasma distribution function

f(x, y, z, p_x, p_y, p_z, t) ⟶ **6 dimensions + time!**

Coupled to the electromagnetic fields ⟶ **Non-linearity**

$$\frac{\partial f}{\partial t} + \boldsymbol{\beta}\, c \cdot \nabla_{\boldsymbol{x}} f - e\,(\boldsymbol{E} + \boldsymbol{\beta}\, c \times \boldsymbol{B}) \cdot \nabla_{\boldsymbol{p}} f = 0$$ ⟵ **Collisions neglected**

$$\nabla \times \boldsymbol{E} = -\frac{\partial \boldsymbol{B}}{\partial t}$$

Current density J of the plasma

$$\nabla \times \boldsymbol{B} = -\mu_0 e c \left(\int \boldsymbol{\beta} f d^3 p \right) + \frac{1}{c^2} \frac{\partial \boldsymbol{E}}{\partial t}$$

Explorable Physics:

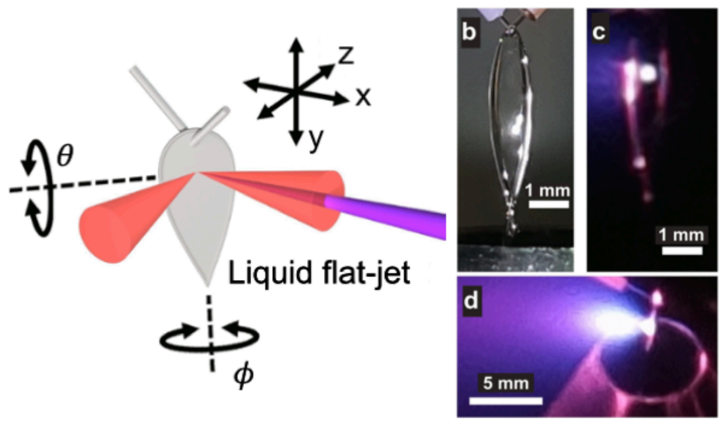
- Relativistic optics (laser self-focusing, …)
- Nonlinear phenomena
- Wave-breaking
- Injection and acceleration of particles

Approximate solution: Particle in Cell method

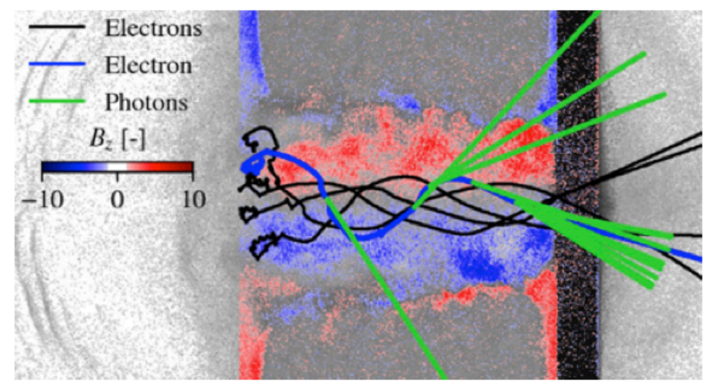
Particle in Cell (PIC) method : essential kinetic plasma investigation technique

Applications From Laboratory plasmas to Space and Astrophysical plasmas

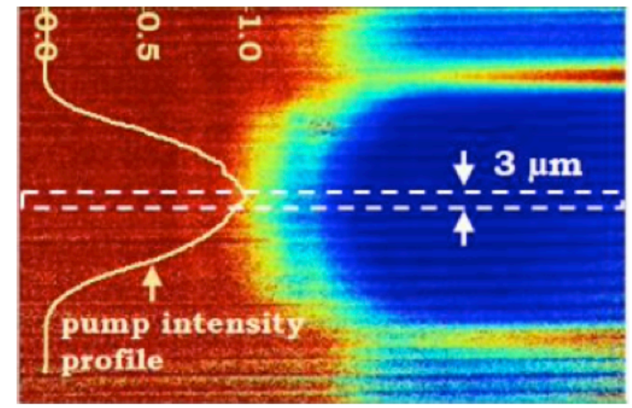
High-Harmonic Generation



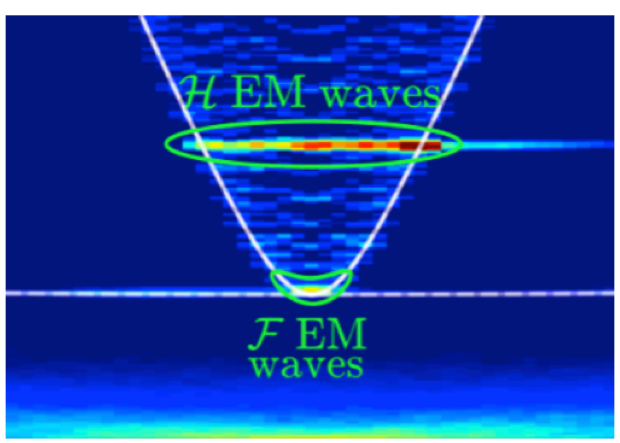
Radiation sources from DLT



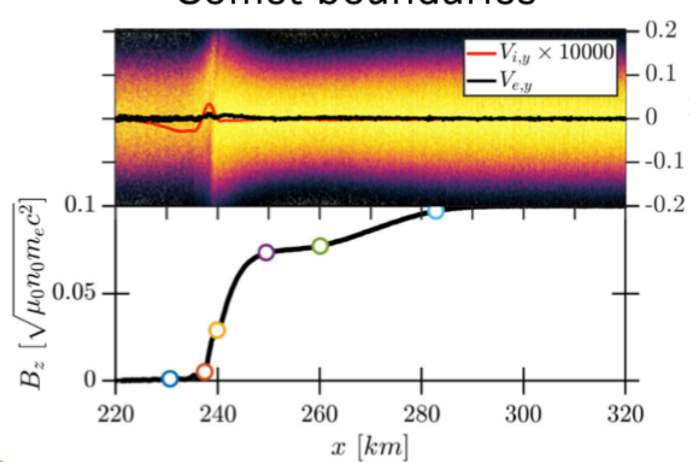
Solid to plasma transition



Solar radio-burst



Comet boundaries



Collisionless shocks & Dark Matter

Some studies performed with Smilei

- Wide range of physics applications
- Conceptually simple
- Efficiently implemented on small or massively parallel supercomputers

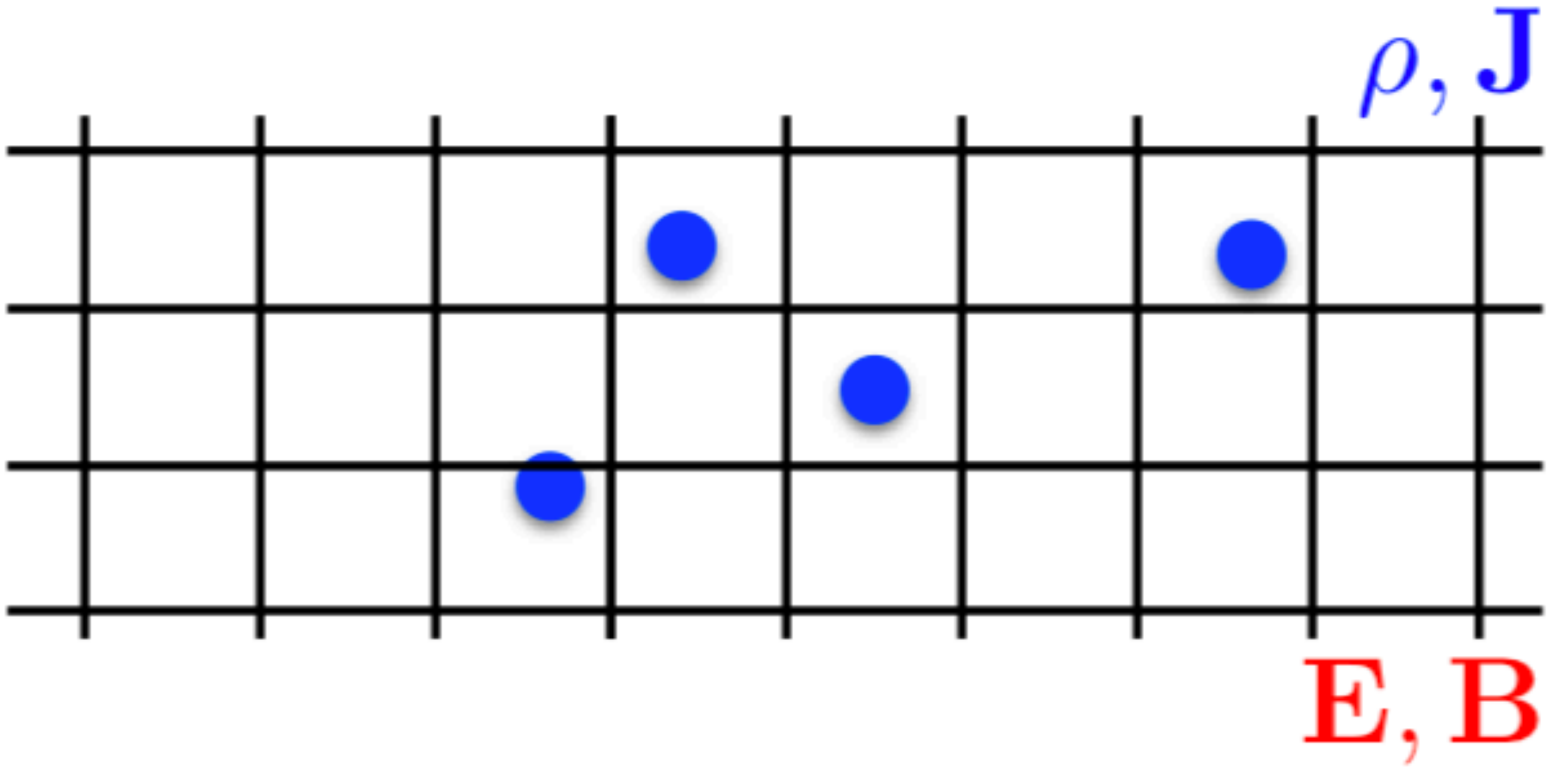
Particle in Cell concept

Sample Plasma with Macro-Particles
(1 Macroparticle = position, momentum, charge, …)

+

Discretize space with computational grid

Define E, B, ρ, J on the grid cells

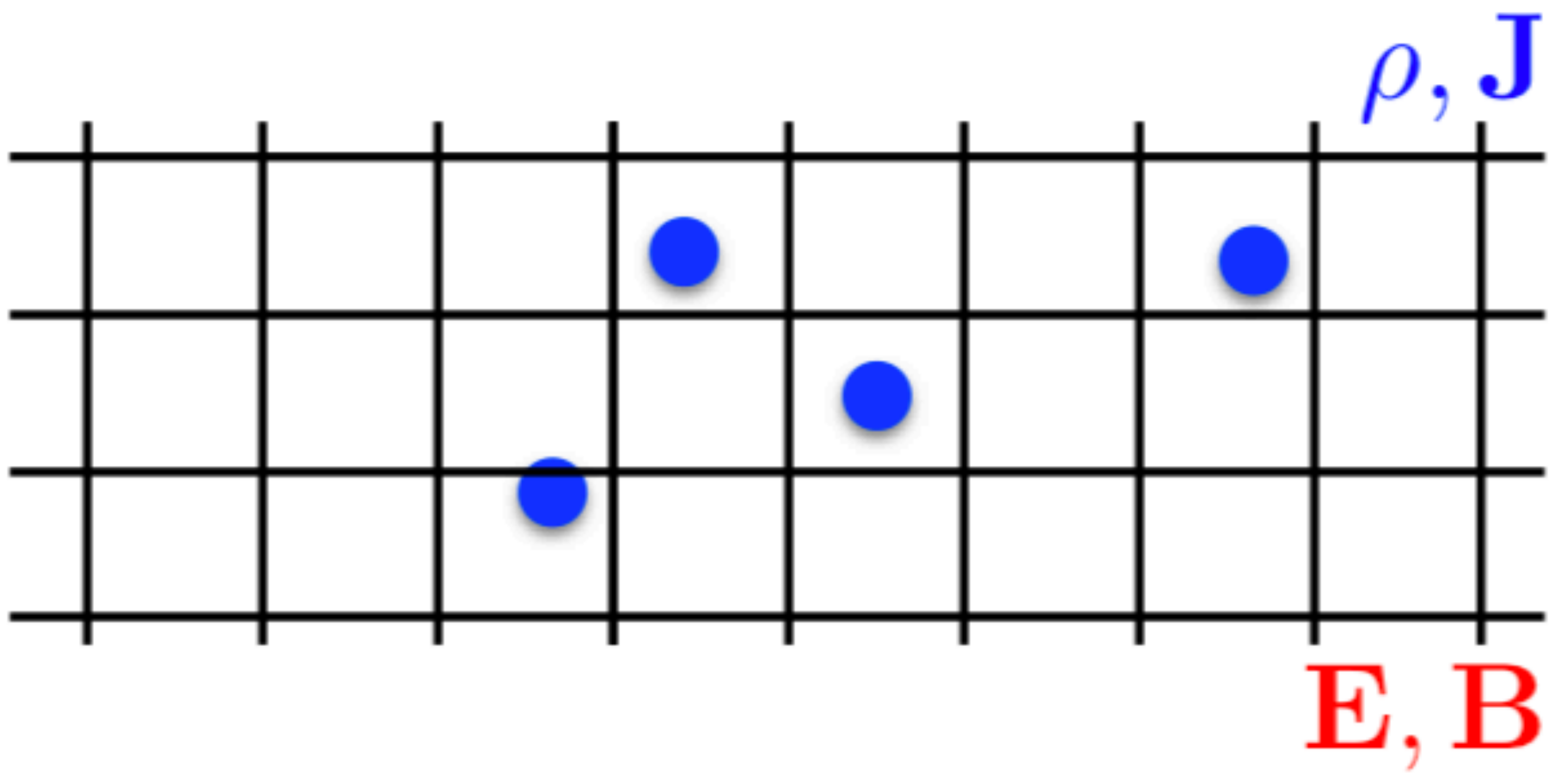


Particle in Cell concept

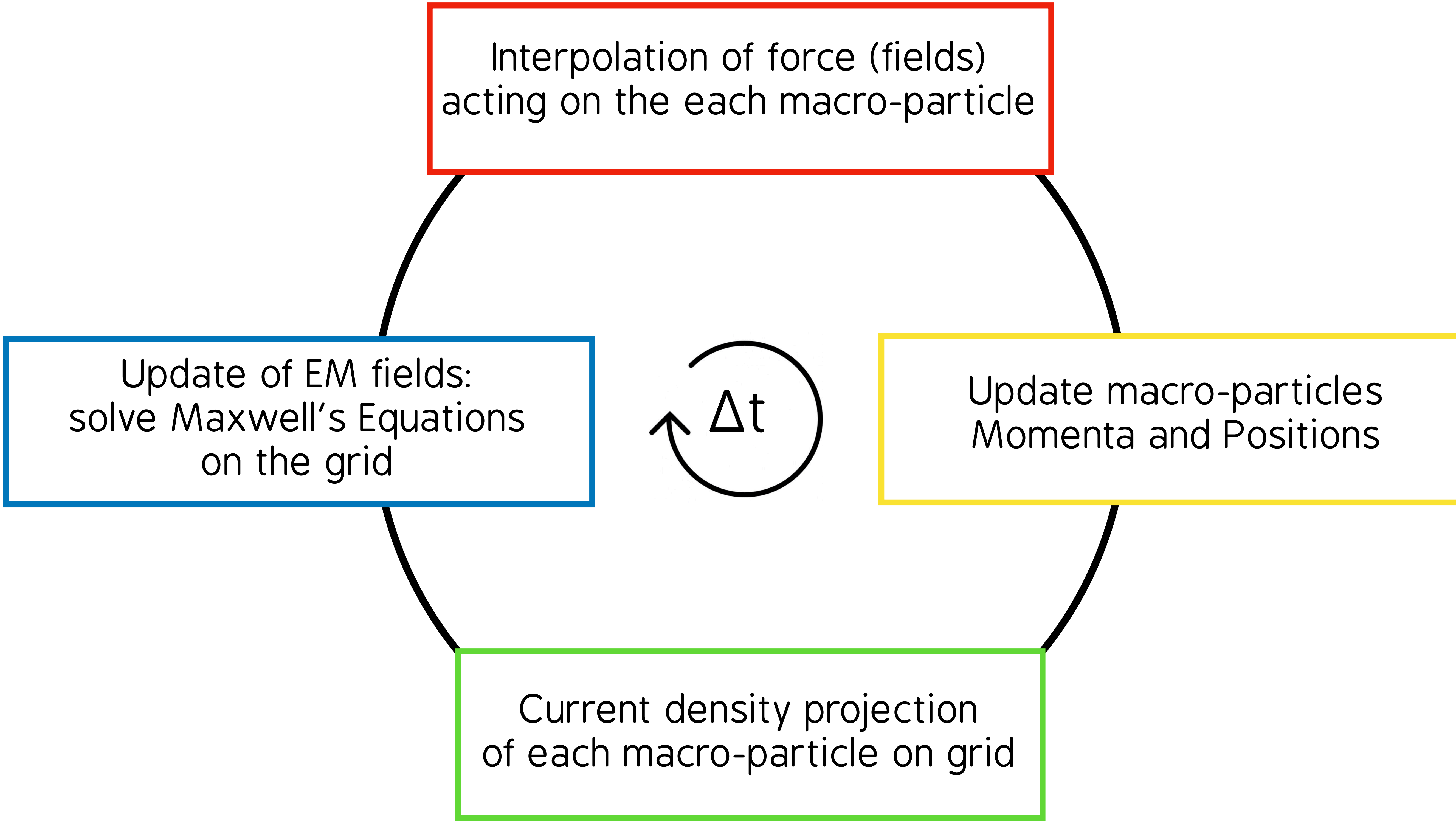
Macro-Particles:
evolve following the characteristics of Vlasov Equation
(In the PIC method they look like equations of motion)

+

Electromagnetic Fields: evolve following Maxwell's Equations



Particle in Cell modelling is self-consistent



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Smilei)

A collaborative, open source multi-purpose Particle in Cell code

https://smileipic.github.io/Smilei/index.html

User-friendly

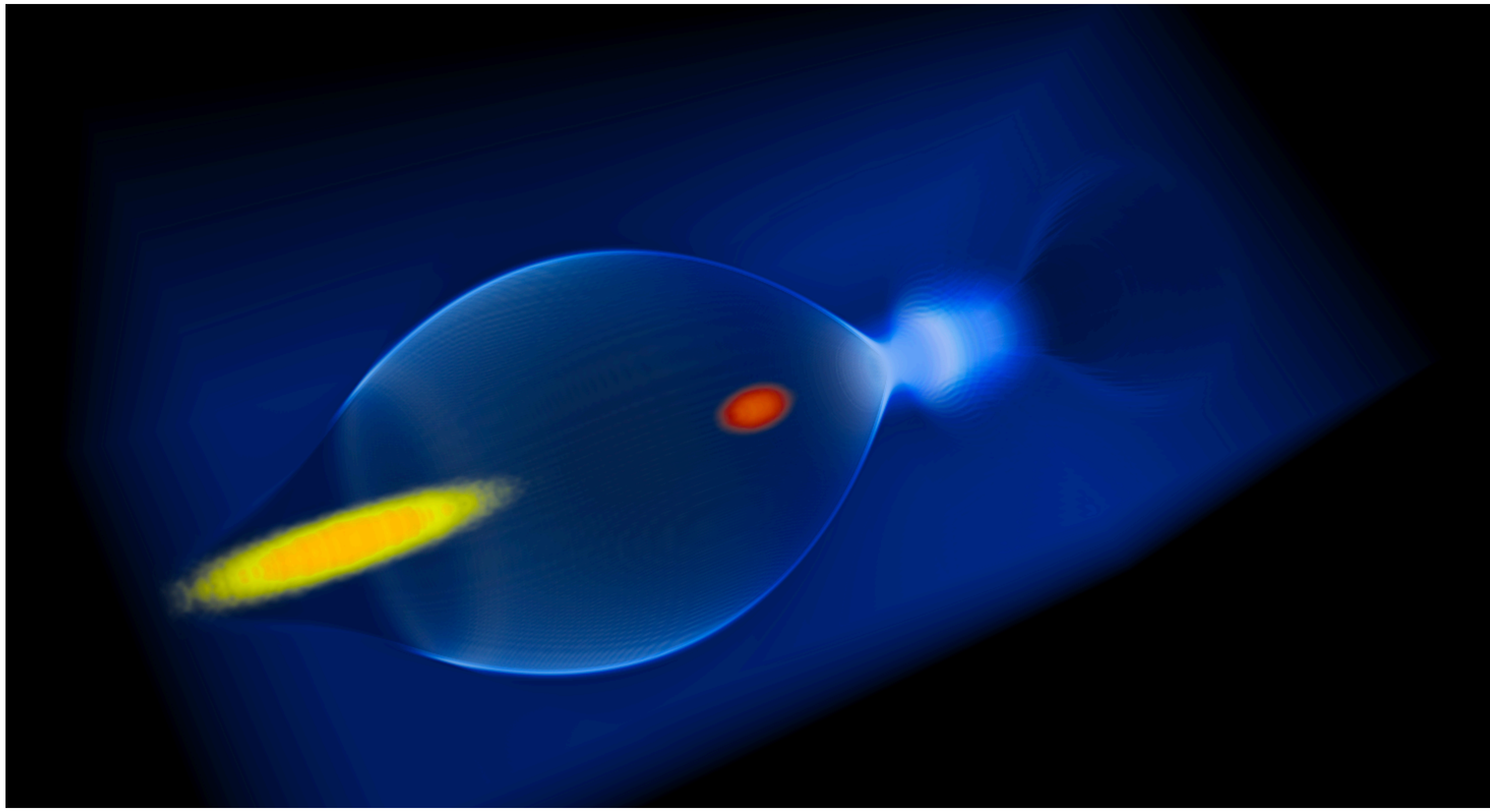
- online: documentation, tutorials
- Python input/output
- quick visualisation library
- teaching platform
- bi-annual training workshop
- Element chat with the developers

High Performance

- MPI + OpenMP parallelization
- dynamic load balancing
- adaptive vectorization
- GPU computing on both NVIDIA and AMD architectures

Multi-physics

- 1D, 2D, 3D, quasi-3D geometries
- ionization, collisions, strong-field QED
- laser envelope model
- relativistic beam field initialization



MAISON DE LA SIMULATION

High quality

- developers: experts of physics and HPC
- continuously benchmarked
- GitHub bug reporting
- OpenPMD standard
- >130 publications using the code up to 2023

Additional material

Extensive Documentation
(Installation, Use, Postprocessing, ...)

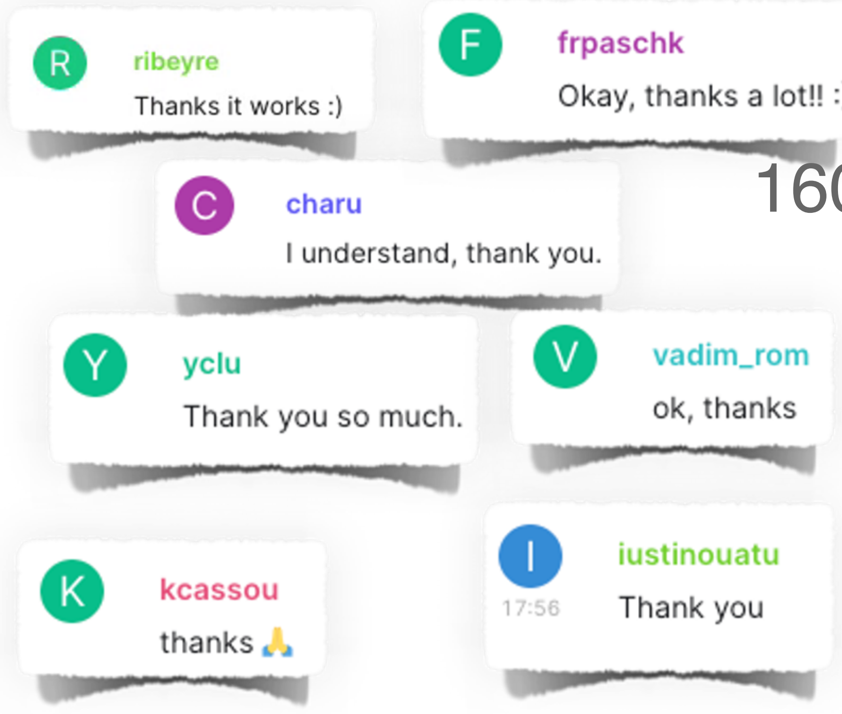
https://smileipic.github.io/Smilei/index.html

https://smileipic.github.io/tutorials/

Presentations from the
4th User & Training Workshop at ELI-Beamlines

https://indico.math.cnrs.fr/event/9577/

Questions?
We answer on the Element chat



1600 messages
in 2021

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Example of input file

```
Main(
    geometry           = "1Dcartesian",
    timestep           = 0.009,
    cell_length        = [0.01],
    ...
)

x_center_plasma        = 200.

def my_density_profile(x):
    return exp(-(x-x_center_plasma)**2)

Species(
    name               = "electron",
    charge             = -1.,
    mass               = 1.,
    particles_per_cell = 100,
    number_density     = my_density_profile
    ...

)
```

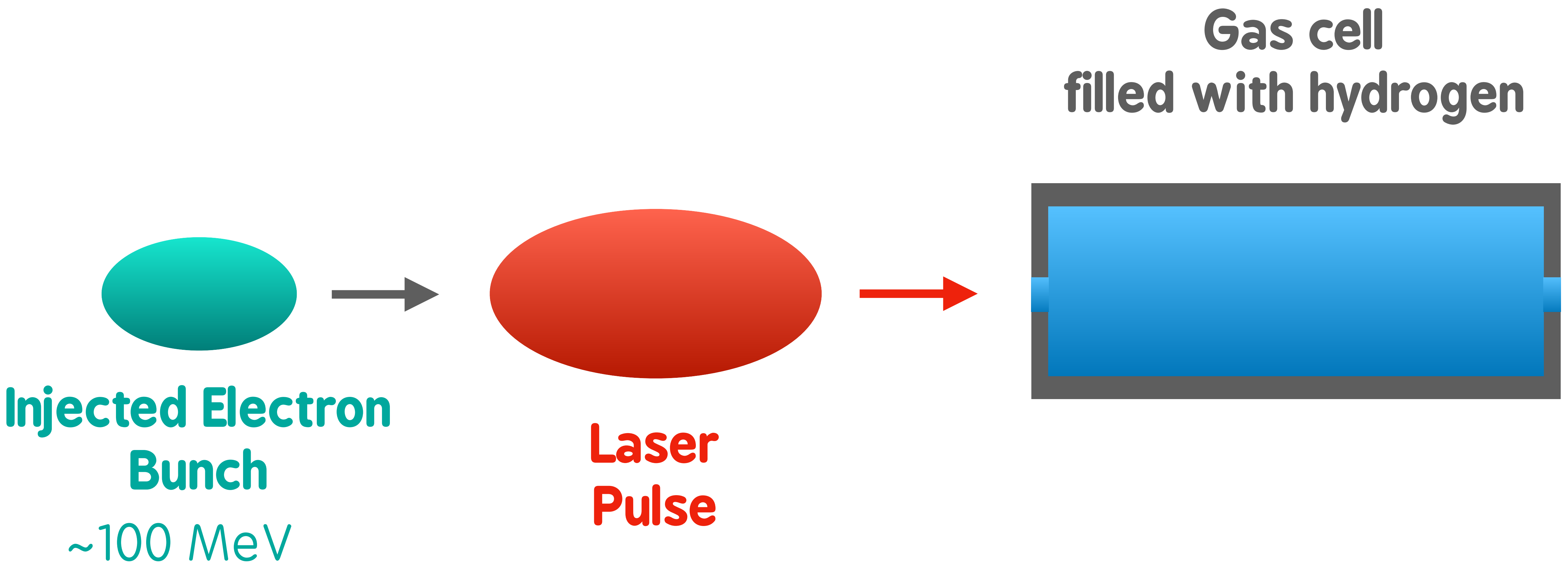
- Normalised units

- Quantities can be computed at runtime

Laser /Plasma profiles = Functions (also user-defined)

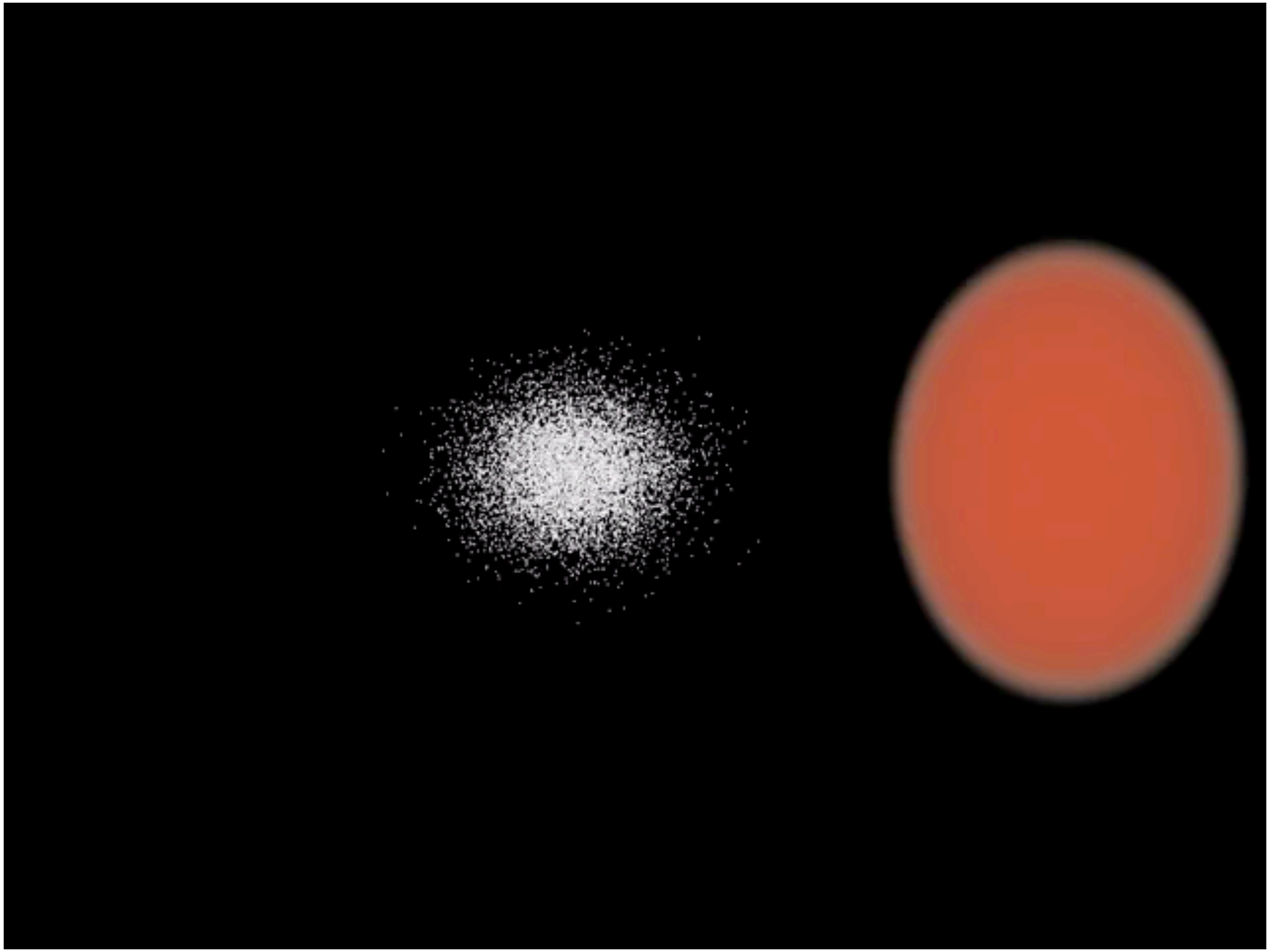
If Python can read it, SMILEI can read it

Case study: LWFA with external injection



Assumption: plasma already created in the gas cell
(the laser's repulse ionises the gas in its path)

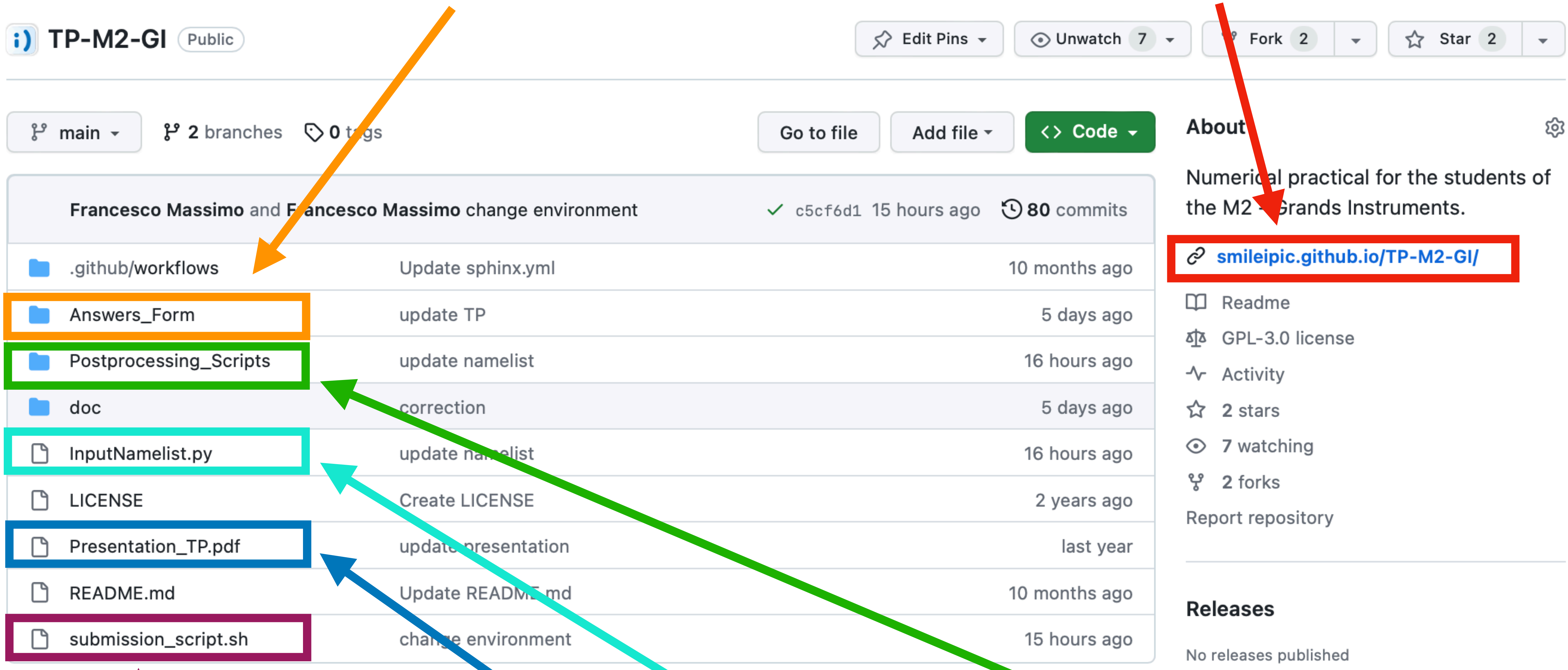
3D rendering of LWFA with external injection



Practical material

https://github.com/SmileiPIC/TP-M2-GI/tree/main

Answer Form for the Exercises **Link to TP documentation and Exercises**



These slides **Input Namelist file to run simulations** **Postprocessing Scripts**

Simulation submission file

Practical exercises

- Read **in detail** the **TP documentation**
  https://smileipic.github.io/TP-M2-GI/index.html
- Solve the exercises in the **TP documentation** progressively, e.g.

Exercise 1:

Assuming $\lambda_0 = 0.8\mu m$ (a Ti:Sa laser system), what is the value of the critical density n_c?

What is the value of the reference electric field $E_0 = (2\pi m_e c^2)/(e\lambda_0)$?

This choice of λ_0 will be used throughout all subsequent exercises.

Hint: Some lines at the start of the `InputNamelist.py` file can help you in the calculations.

Exercise 5:

In the next exercise we will check that the Gaussian laser pulse diffracts following the theory for a Gaussian beam [Siegman]: $w(x) = w_0\sqrt{1 + x^2/x_R^2}$, where w_0 is the laser waist size at the focal plane position, $w(x)$ the laser waist size at propagation distance x, x_R is the Rayleigh length $x_R = \pi w_0^2/\lambda_0$.

What is the theoretical Rayleigh length x_R?

Exercise 10:

Launch a new simulation with `a0=1.8`. This simulation will be in the nonlinear regime ($a_0 > 1$), so the plasma wave will not be sinusoidal. You can visualize both the normalized absolute value of the envelope of the laser field and the electron number density by defining a transparency for the parts where the latter field is lower than a threshold `vmin`:

```
Env_E  = S.Probe.Probe1("Env_E_abs",units=["um"],cmap="hot",vmin=0.8,transparent="unde
Rho    = S.Probe.Probe1("-Rho/e",units=["fs","um","1/cm^3"],cmap="Blues_r",vmin=0.,vma
happi.multiSlide(Rho,Env_E,xmin=0,figure=10, xlabel="x [um]",ylabel="y [um]")
```

Using `timestep=2500` in the definition of `Env_E` and `Rho`, and then using `multiPlot` instead of `multiSlide`, you should have a plot of the data at half of the propagation length.

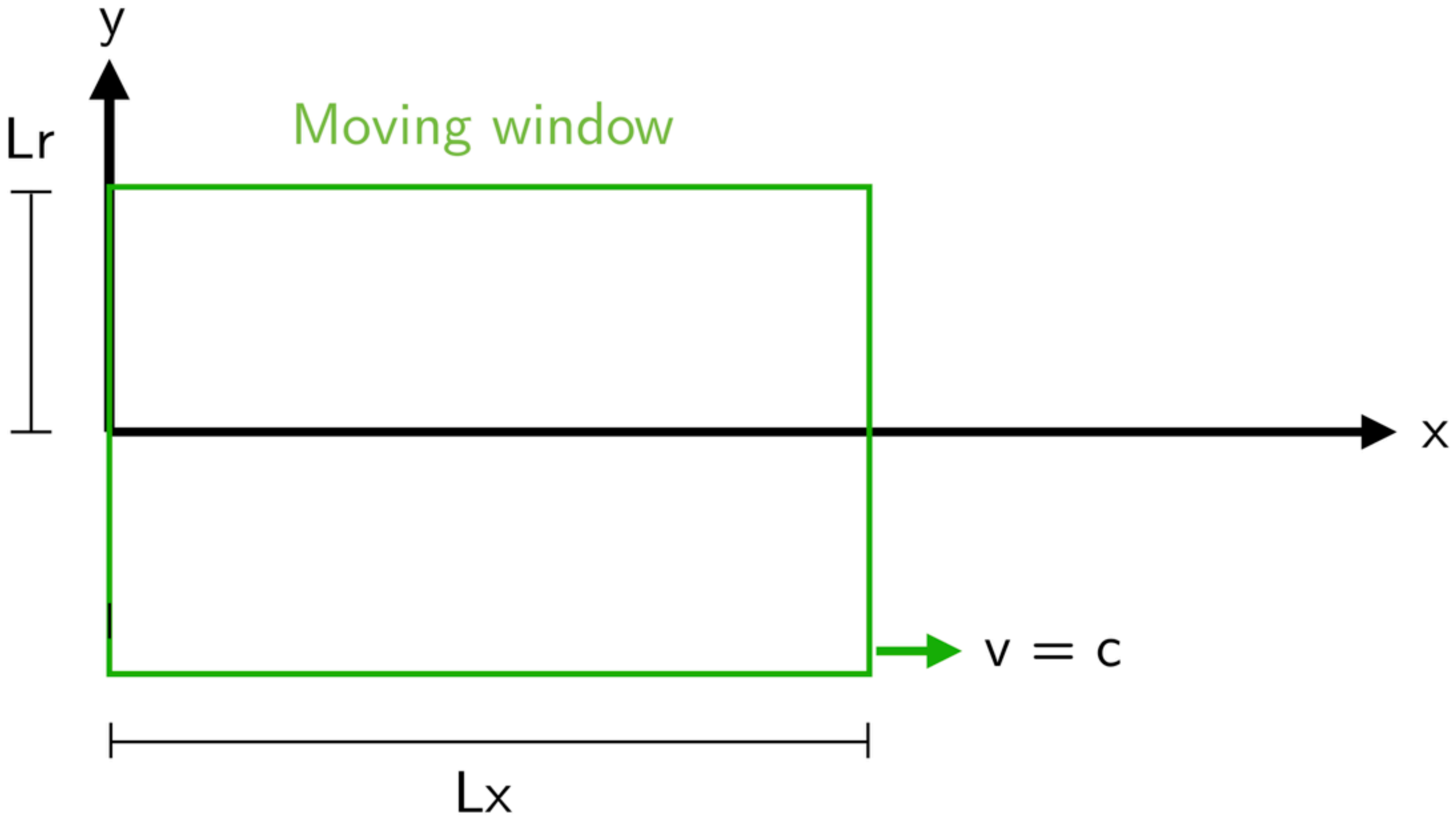
Include this image in your answers.

- Run simulations when necessary,
  following the instructions in the **TP documentation**
- Fill the answers report **Answers_Form.docx**
  (You can download it from GitHub
  https://github.com/SmileiPIC/TP-M2-GI/tree/main)

Suggestions

- Again read **in detail** the **TP documentation**
- **Understand** the physical set-up
- **Any doubts? Ask the instructor**
- Solve the exercises **progressively**
- Create one folder for each simulation asked by the exercises (to **avoid losing data**)
- Feel free to adapt the commands in the **TP documentation**
- When an image is asked for the report, save it or make a screenshot
- **Better do few exercises but understand them at 100%**

Part 1: Exploring the Input Namelist (Exercises 1-2)



Part 1: Exploring the Input Namelist (Exercises 1-2)

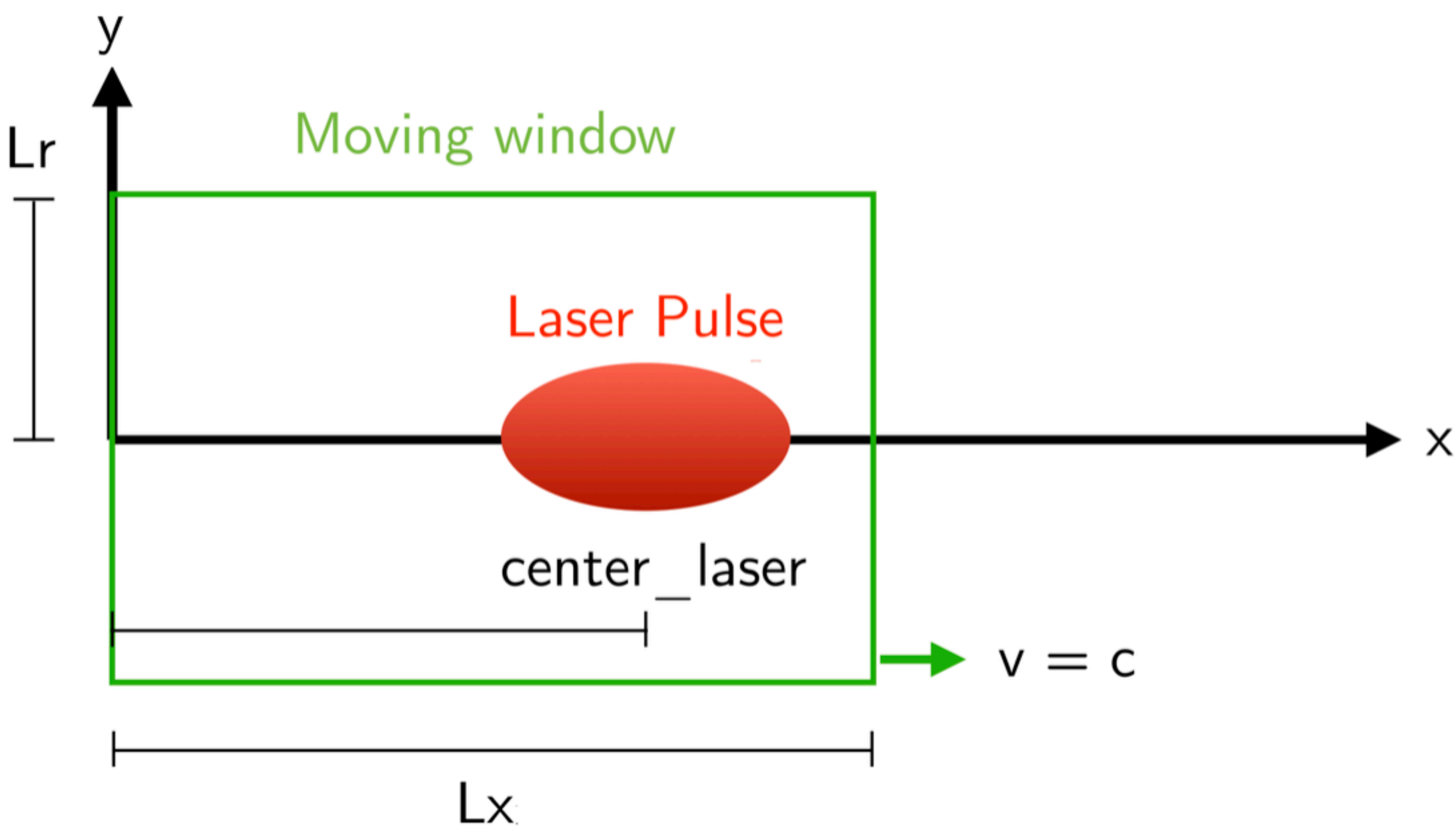
Input Namelist structure

- Main Block
- Moving Window Block
- Laser Envelope Block
- Species Block (for the plasma)
- Species Block (for the relativistic electron bunch)
- Diagnostic Blocks (for Postprocessing)

Blue: Active

Gray: Commented = Inactive

Part 2: Laser pulse in vacuum (Exercises 4-6)



Part 2: Laser pulse in vacuum (Exercises 4-6)

Input Namelist structure

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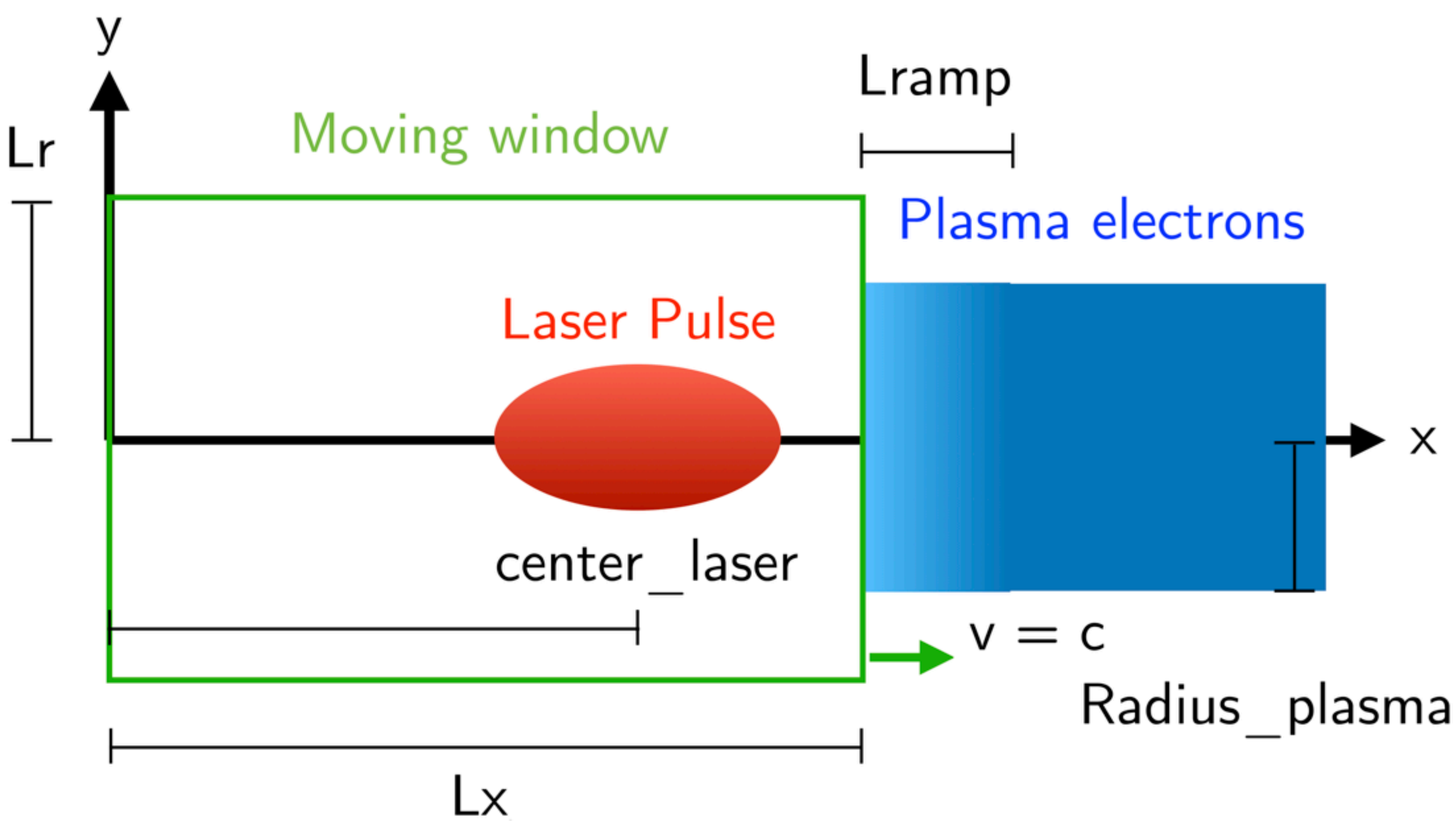
- Diagnostic Blocks (for Postprocessing)

Blue: Active

Gray: Commented = Inactive

Part 3: Laser Wakefield Excitation (Exercises 7-11)



Part 3: Laser Wakefield Excitation (Exercises 7-11)

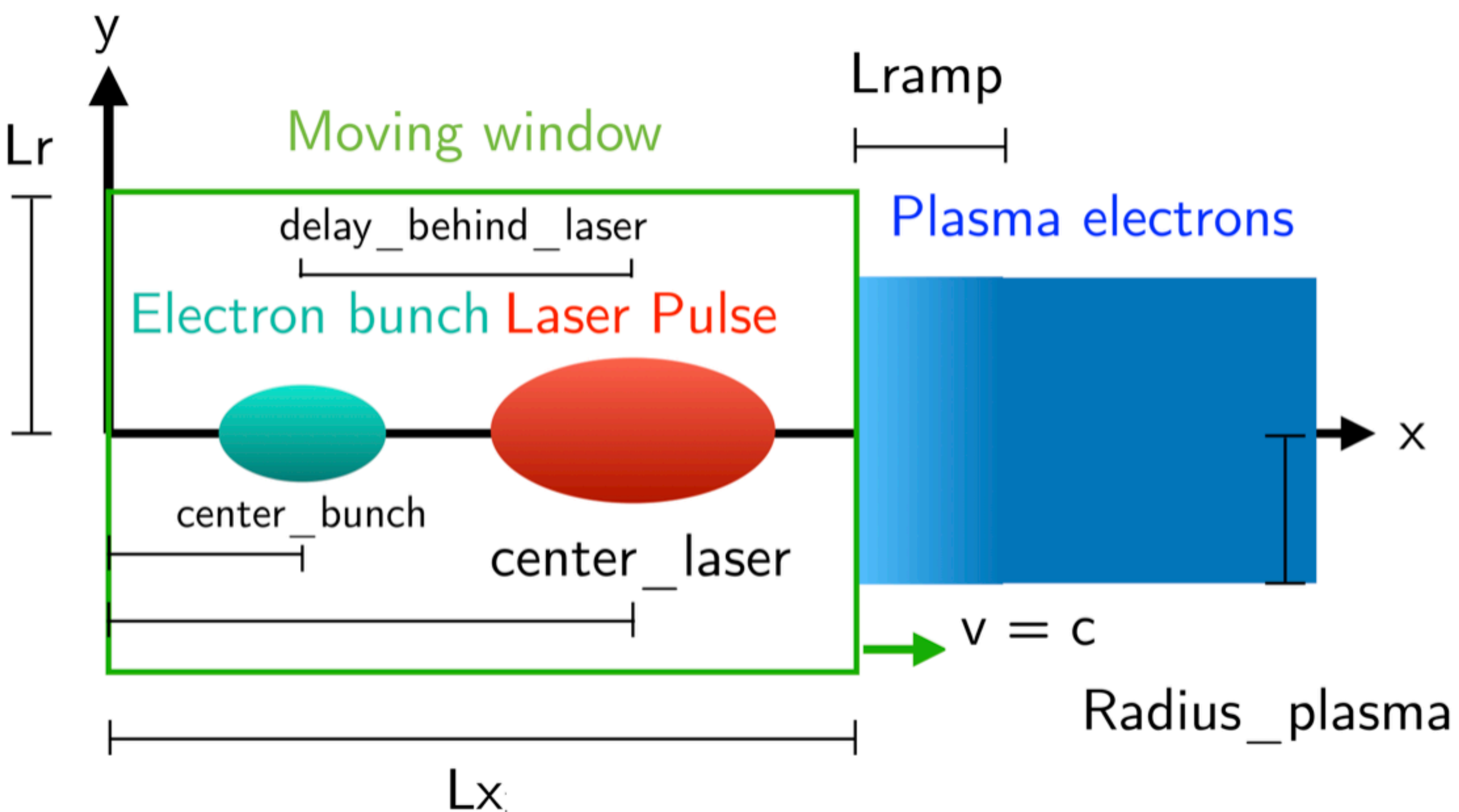
Input Namelist structure

- Main Block
- Moving Window Block
- Laser Envelope Block
- Species Block (for the plasma)
- Species Block (for the relativistic electron bunch)
- Diagnostic Blocks (for Postprocessing)

Blue: Active

Gray: Commented = Inactive

Part 4: Laser Wakefield Acceleration of an electron bunch (Exercises 12-20)



Input Namelist structure

- Main Block
- Moving Window Block
- Laser Envelope Block
- Species Block (for the plasma)
- Species Block (for the relativistic electron bunch)
- Diagnostic Blocks (for Postprocessing)

Blue: Active

Gray: Commented = Inactive

Postprocessing for the practical

Included in the code: the Python postprocessing library **happi**

```
$ ipython
In [1]: import happi
```

Diagnostics available for this practical:

- 1D Probe on the x axis (electromagnetic fields, density)
- 2D Probe on the xy plane (electromagnetic fields, density)
- DiagTrackParticles for the bunch electrons (phase space data)

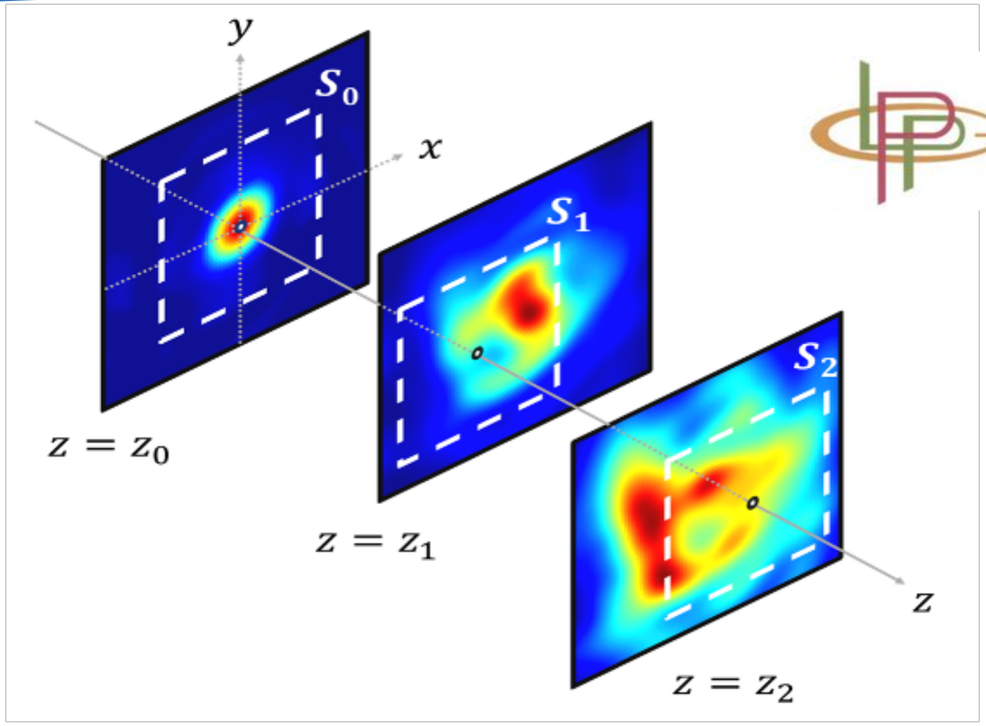
Tips:

- Open the **Ipython** interface (command **ipython** in the terminal)
- Copy and paste the happi commands from the handouts
- Adapt them for your purposes
- Use the post processing scripts available (see handouts)

Questions?

Additional Slides

Some current LWFA research themes (1)



Realistic laser pulses in PIC simulations yield

Accurate reconstructions of experimental data

I. Moulanier et al.,

Physics of Plasmas (2023)

I. Moulanier et al.,

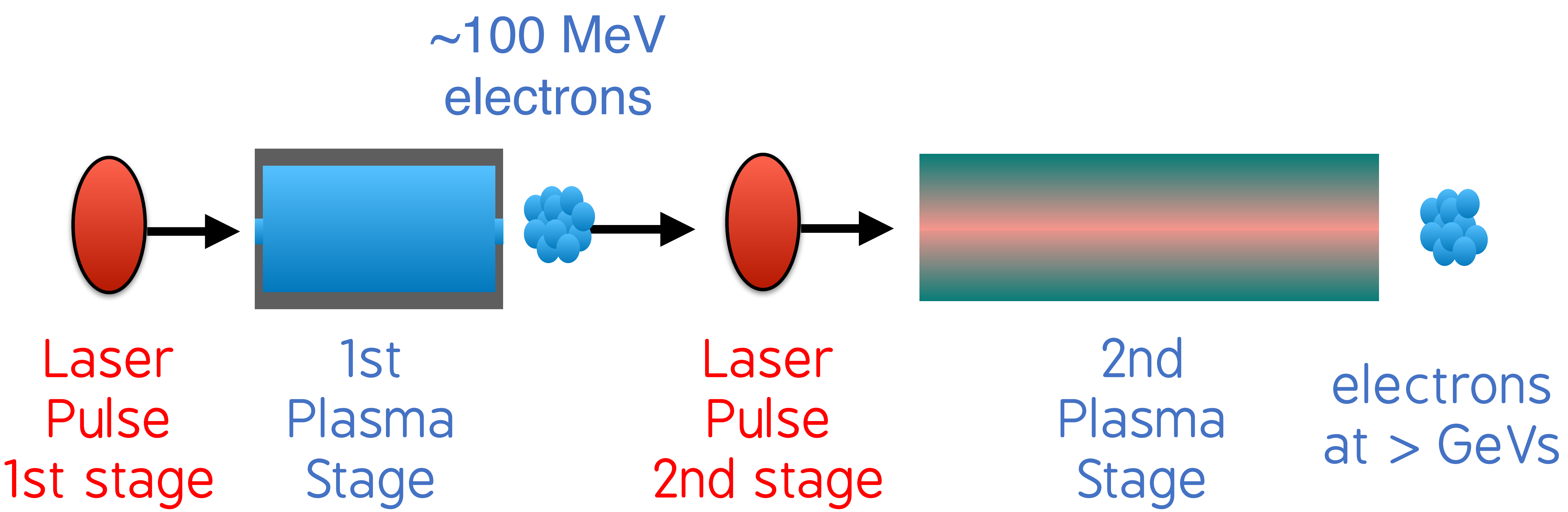
J. Opt. Soc. Am. B **40**(9), 2450-2461 (2023)

Internship at LPGP:
Advanced electric field reconstruction analysis

Use advanced phase reconstruction algorithm to reconstruct laser field

Some current LWFA research themes (2)

Making LWFA scalable: Multi-stage experiments



Some current LWFA research themes (3)

European Project EuPRAXIA

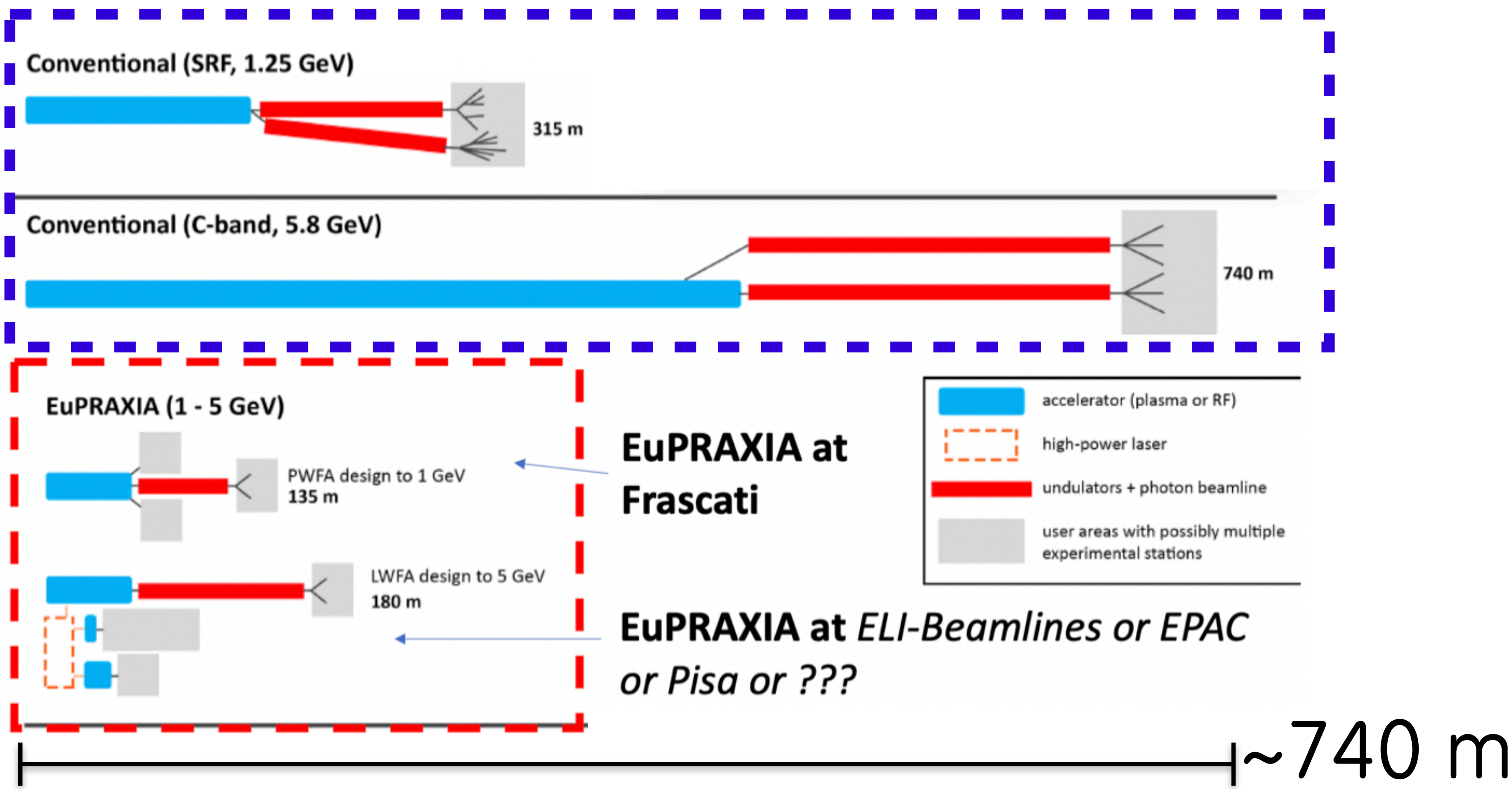
Objective: build a European, large scale, distributed plasma acceleration facility for users

R. Assmann, EuPRAXIA Preparatory Phase kick-off meeting (Nov 2022)

Conventional Acceleration (Max ~100 MV/m)

Plasma Acceleration (Max ~100 GV/m)

Scientific challenge: Obtain beam qualities suited for applications



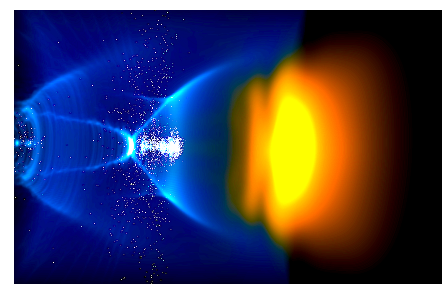
http://www.eupraxia-project.eu

Some current LWFA research themes (4)

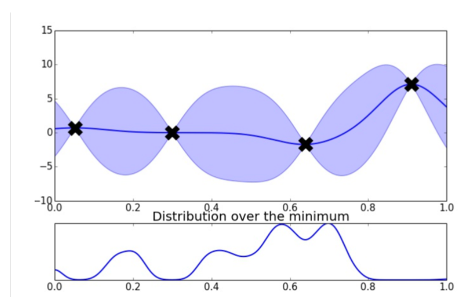
Machine Learning and AI for LWFA

~10²-10³ Quick Simulations

One (/or more)
Quick simulation(s)

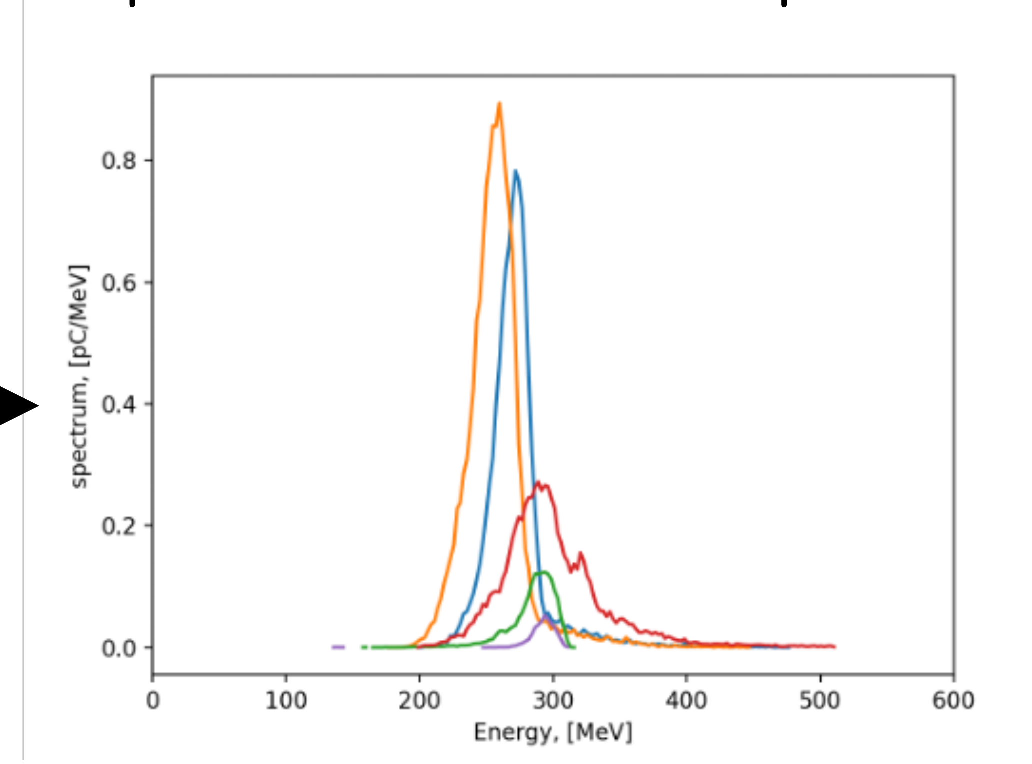


Analysis of the
simulation results



Optimization algorithm
(e.g. Random search, Bayesian Optimisation, CMA-ES, Particle Swarm Optimisation)

Optimized Electron Spectra



P. Drobniak and IJClab, 2021