

$$m \sum x_i^2 + c \sum x_i = \sum x_i y_i$$

$$\times \sum x_i \left(m \sum x_i + n c = \sum y_i \right)$$

$$\times \sum x_i^2 \left(m \sum x_i \sum x_i^2 + c \left(\sum x_i \right)^2 = \sum x_i \sum x_i y_i \right)$$

$$\times \sum x_i^2 \left(m \sum x_i \sum x_i^2 + c n \sum x_i^2 = \sum y_i \sum x_i^2 \right)$$

$$c = \frac{\sum x_i \sum x_i y_i - \sum y_i \sum x_i^2}{\left(\sum x_i \right)^2 - n \sum x_i^2}$$

$$\bar{x} \sum x_i y_i - \bar{y} \sum x_i^2$$

$$n \frac{\left(\sum x_i \right)^2}{n^2} - \sum x_i^2$$

$$\bar{y} \sum x_i^2 - \bar{x} \sum x_i y_i$$

$$n \bar{x}^2 - \sum x_i^2$$

$$m n \sum x_i^2 + c n \sum x_i = n \sum x_i y_i$$

$$m (\sum x_i)^2 + c n \sum x_i = \sum x_i y_i$$

$$m [n \sum x_i^2 - (\sum x_i)^2] = n \sum x_i y_i - \sum x_i \sum y_i$$

$$m = \frac{n \sum x_i y_i - \sum x_i \sum y_i}{n \sum x_i^2 - (\sum x_i)^2}$$

$$= \frac{\sum x_i y_i - n \frac{\sum x_i}{n} \frac{\sum y_i}{n}}{\sum x_i^2 - n \left(\frac{\sum x_i}{n} \right)^2}$$

$$= \frac{\sum x_i y_i - n \bar{x} \bar{y}}{\sum x_i^2 - n \bar{x}^2}$$

$$m = \frac{n \bar{x} \bar{y} - \sum x_i y_i}{n \bar{x}^2 - \sum x_i^2}$$

$$\therefore m = \frac{n \bar{x} \bar{y} - \sum x_i y_i}{Z}$$

$$c = \frac{\bar{y} \sum x_i^2 - \bar{x} \sum x_i y_i}{Z}$$

$$\text{where, } Z = n \bar{x}^2 - \sum x_i^2$$