# **Expression Trees**

#### Postfix to Expression Tree Rules

Terms: Append x to y means add child x to node y.

Rule1: Operators can have children but operands can't.

Rule2: Nodes can only have 2 children.

Rule3: When appending nodes, always append to right first. If right is occupied, then append to left.

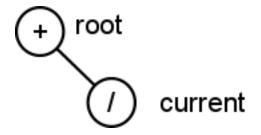
#### Postfix to Expr Tree Algorithm

- 1. Get the last symbol (rightmost) of postfix notation, create a node for it and designate the new node as the root.
- 2. Set the root node as current node.
- 3. For each element from right to left (excluding the last):
  - 3.1 Create a node for it.
- 3.2 If current node cannot have more children, search for the first parent/grandparent that can have more children and set it as the current node.
- 3.3 Append the new node to the current node.
- 3.4 Set new node as current node.

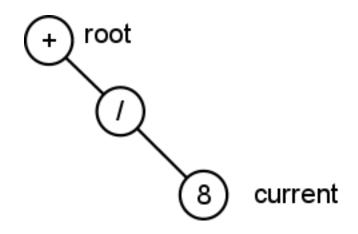
Postfix: 2, 6, \*, 3, 8, /, + Step 1 & 2

+ root & current

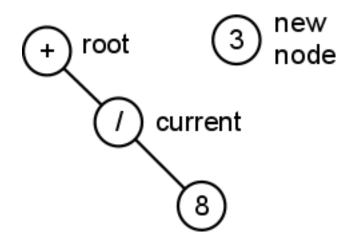
Postfix: 2, 6, \*, 3, 8, /, + Step 3.1, 3.3 & 3.4



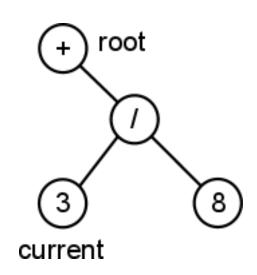
Postfix: 2, 6, \*, 3, 8, /, + Step 3.1, 3.3 & 3.4



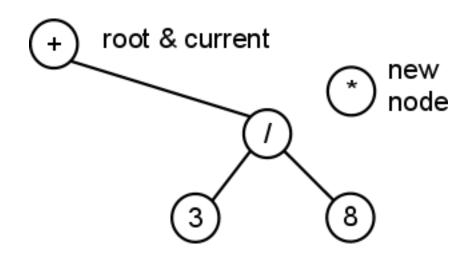
Postfix: 2, 6, \*, 3, 8, /, + Step 3.1 & 3.2



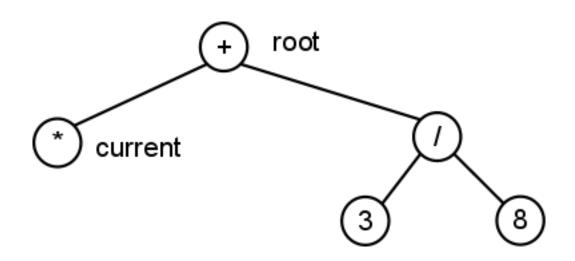
Postfix: 2, 6, \*, 3, 8, /, + Step 3.3 & 3.4



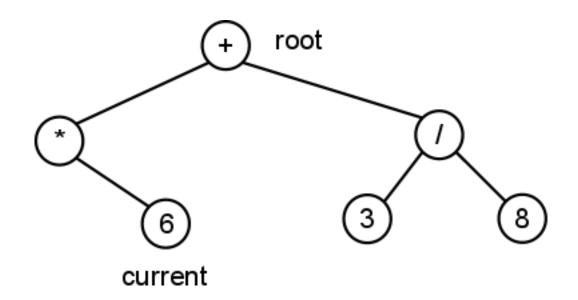
Postfix: 2, 6, \*, 3, 8, /, + Step 3.1 & 3.2



Postfix: 2, 6, \*, 3, 8, /, + Step 3.3 & 3.4

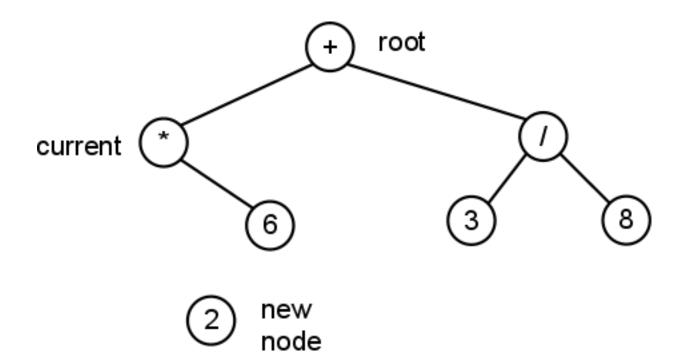


Postfix: 2, 6, \*, 3, 8, /, + Step 3.1, 3.3 & 3.4

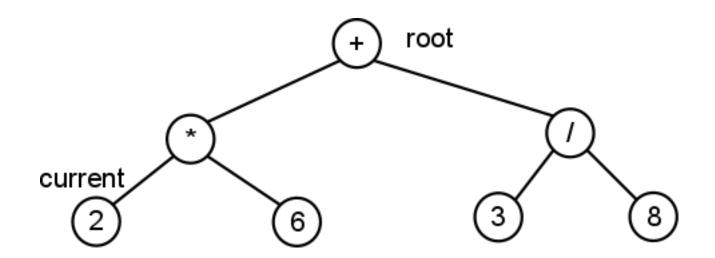


Postfix: 2, 6, \*, 3, 8, /, +

Step 3.1 & 3.2



Postfix: 2, 6, \*, 3, 8, /, + Step 3.3 & 3.4



#### Prefix from Expression Tree

Rule1: Start at the root node.

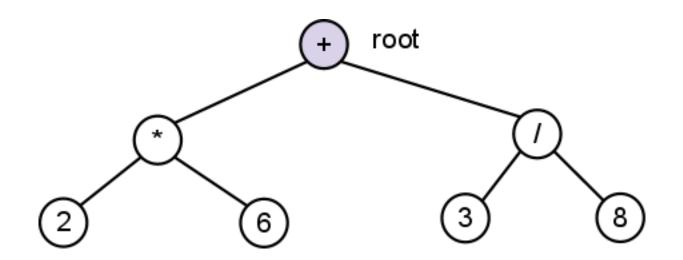
Rule2: When node is visited for the first time, output value of node.

Rule3: Go from left to right when visiting children.

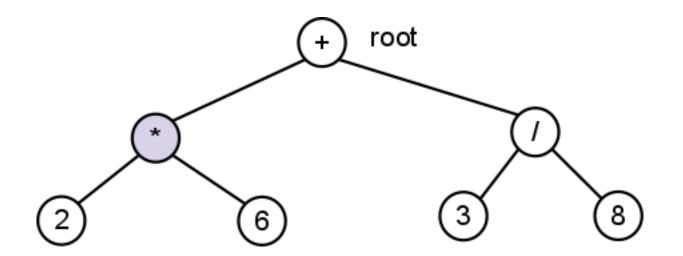
Rule4: If left child has children, visit their children first before going to right child.

Rule5: Prefix notation is complete when every node is visited.

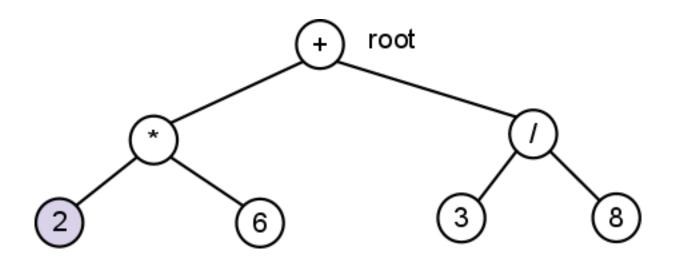
Output: +



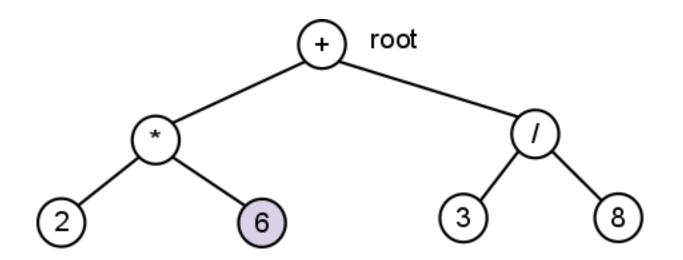
Output: +, \*



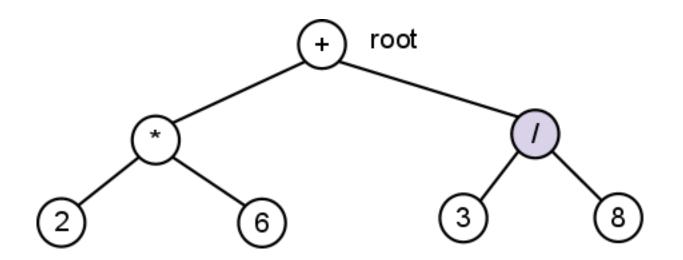
Output: +, \*, 2



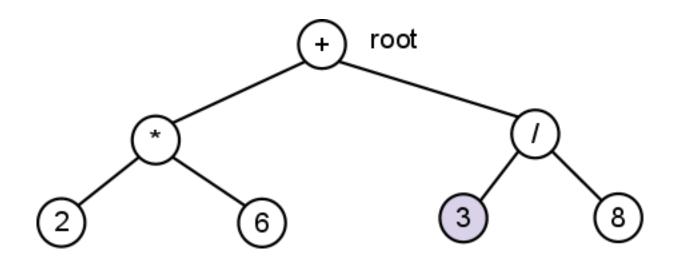
Output: +, \*, 2, 6



Output: +, \*, 2, 6, /



Output: +, \*, 2, 6, /, 3



Output: +, \*, 2, 6, /, 3, 8

