

```
In [ ]: '''
Name: Om Kadam
Class: EXTC-A
Batch: TA-3
Roll No: 45
Semester: V
Date: 05-10-2023
Time: 15:00
'''
```

Design of IIR Butterworth Filter using ChebyShev

Problem Statement: Design Digital Butterworth Filter for following specifications using ChebyShev. Assume $T = 1\text{sec}$

Specifications:

$$0.8 \leq |H(e^{jw})| \leq 1 \quad 0 \leq w \leq 0.2\pi$$

$$|H(e^{jw})| \leq 0.2 \quad 0.5 \leq w \leq \pi$$

```
In [16]: # Importing in-built Libraries
import numpy as np
import matplotlib.pyplot as plt
import control.matlab as control
import scipy.signal as signal
```

```
In [17]: # Given data
T = 1
d1 = 0.8
d2 = 0.2
wp = 0.2 * np.pi
ws = 0.5 * np.pi
print(wp)
print(ws)
```

```
0.6283185307179586
1.5707963267948966
```

```
In [18]: d1db = -20 * np.log10(d1)
d2db = -20 * np.log10(d2)
```

```
In [19]: # Frequency Mapping
omegap = (2/T) * np.tan(wp/2)
omegas = (2/T) * np.tan(ws/2)
print(omegap)
print(omegas)
```

```
0.6498393924658126
1.9999999999999998
```

```
In [20]: # Determining Order of the Filter
N,wc = signal.cheb1ord(omegap, omegas, d1db, d2db, analog=True)
print('Order of Filter = ', N)
print(wc)
```

Order of Filter = 2
0.6498393924658126

```
In [21]: # Determining Analog T.F H(s)
num,den = signal.cheby1(N, 5, wc, btype = 'lowpass', analog = True)
trans1 = control.tf(num,den)
print('Analog Transfer Function of Butterworth filter H(s) = ', trans1)
```

Analog Transfer Function of Butterworth filter H(s) =
0.1436

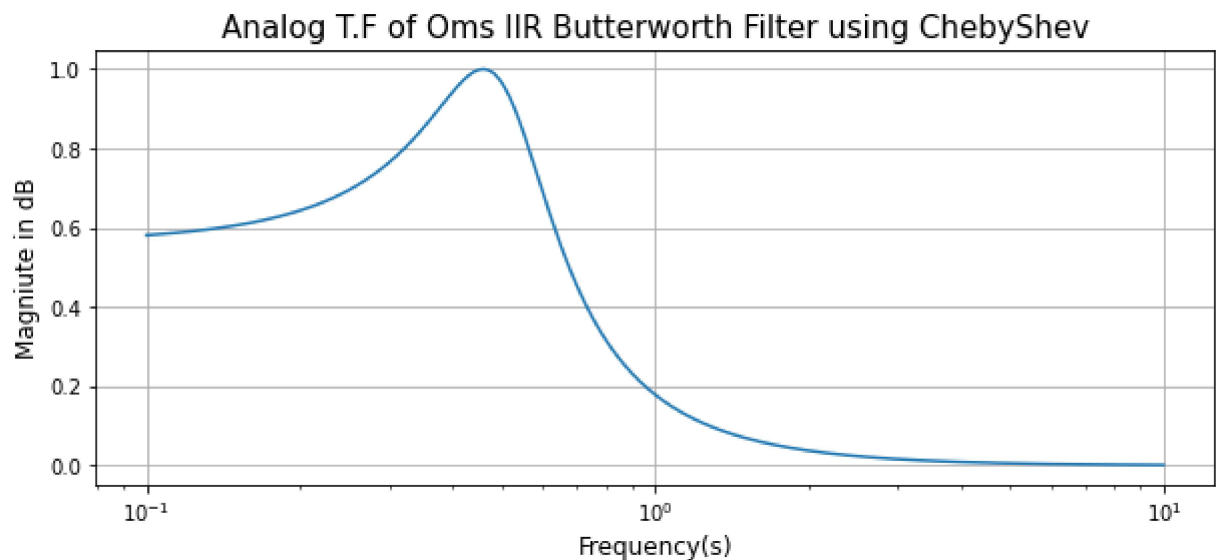
 $s^2 + 0.2973 s + 0.2553$

```
In [22]: # Transforming Analog Filter to Digital Filter using BLT
num1, den1 = signal.bilinear(num, den, T)
trans2 = control.tf(num1, den1)
print('Digital Transfer Function of Butterworth filter H(z) = ', trans2)
```

Digital Transfer Function of Butterworth filter H(z) =
0.02961 $s^2 + 0.05921 s + 0.02961$

 $s^2 - 1.544 s + 0.7548$

```
In [25]: # Plotting Analog T.F
w, h = signal.freqs(num, den)
h_db = np.abs(h)
plt.figure(figsize = (10,4))
plt.grid()
plt.xlabel('Frequency(s)', fontsize=12)
plt.ylabel('Magniute in dB', fontsize=12)
plt.title('Analog T.F of Oms IIR Butterworth Filter using ChebyShev', fontsize=15)
plt.semilogx(w, h_db)
plt.show()
```



```
In [26]: # Plotting Digital T.F
w1, h1 = signal.freqs(num1, den1)
h1_db = np.abs(h1)
plt.figure(figsize = (10,4))
plt.grid()
plt.xlabel('Frequency(z)', fontsize=12)
```

```
plt.ylabel('Magniute in dB', fontsize=12)  
plt.title('Digital T.F of Oms IIR Butterworth Filter using ChebyShev', fontsize=15)  
plt.semilogx(w1, h1_db)  
plt.show()
```

