Problem type 1:

Provide the upper-asymptotic bound (*O*-notation) of the following recurrence:

(See variants below)

a. BYB

$$T(n) = 2T(n-1) + 1$$
 and $T(1) = 1$

Solution: $O(2^n)$

b. BYE

$$T(n) = T(\frac{n}{2}) + 1$$
 and $T(1) = 1$

Solution: $O(\log(n))$

c. BYA

$$T(n) = n \cdot T(n-1) + 1$$
 and $T(1) = 1$

Solution: O(n!)

d. BYF

$$T(n) = T(n-1) + n$$
 and $T(1) = 1$

Solution: $O(n^2)$

e. BYH

$$T(n) = 2T\left(\frac{n}{4}\right) + \sqrt{n}$$
 and $T(1) = 1$

Solution: $O(\sqrt{n}\log(n))$

f. BYD

$$T(n) = T\left(\frac{n}{4}\right) + \sqrt{n}$$
 and $T(1) = 1$

Solution: $O(\sqrt{n})$

g. BYC

$$T(n) = 4T(\frac{n}{2}) + n^2 \text{ and } T(1) = 1$$

Solution: $O(n^2 \log(n))$

h. BYG

$$T(n) = 2T\left(\frac{n}{2}\right) + n^2$$
 and $T(1) = 1$

Solution: $O(n^2)$