

Problem type 1:

Let's say we have the following known problem and an unknown problem X . Assume you were able to prove the reduction below. Does that mean X **may** be decidable or undecidable or both? (no explanation necessary, just write decidable, undecidable, or both).

(See variants below)

a. BYD/BYG

Problem: $A_{TM}(\langle M, w \rangle)$ - the problem of determining if a turing machine M will accept string w .

Reduction: $A_{TM} \implies X$

b. BYA/BYE

Problem: $A_{TM}(\langle M, w \rangle)$ - the problem of determining if a turing machine M will accept string w .

Reduction: $X \implies A_{TM}$

c. BYB/BYH

SAT: ($\text{SAT}(\phi)$)

- **INPUT:** A conjunctive normal formula ϕ
- **OUTPUT:** True if there exists a truth assignment that let's ϕ evaluate to True, False otherwise

Reduction: $X \implies SAT$

d. BYC/BYF

SAT: ($\text{SAT}(\phi)$)

- **INPUT:** A conjunctive normal formula ϕ
- **OUTPUT:** True if there exists a truth assignment that let's ϕ evaluate to True, False otherwise

Reduction: $SAT \implies X$