Problem type 1:

In lab 13, you saw the problem below and the recurrence that computes that problem. In plain English, describe what the call to that recurrence f(i, j, ...) means.

(See variants below)

a. BYD/BYE

Problem: You are give an integer value x and an array A[1..n] where each element of the array represents a coin denomination:

Recurrence:

$$CC(i,j) = \begin{cases} 1 & \text{if } j = 0\\ 0 & \text{if } j < 0 \text{ or } (j > 0 \text{ and } i = 0)\\ CC(i,j-A[i]) + CC(i-1,j) & \text{otherwise} \end{cases}$$

In plain english, what does CC(i, j) represent?

b. BYC/BYF

Problem: Find maximum value of items that can be fit into knapsack of the defined capacity. You are given: a array of values V where each element corresponds to item i with value V[i], an array of integer weights W where each elements corresponds to item i with weight W[i] and an integer X which corresponds to the capacity of the knapsack.

Recurrence:

$$Sack(i,j) = \begin{cases} 0 & i > n \\ Sack(i+1,j) & W[i] > j \\ \max\{V[i] + Sack(i+1,j-W[i]), Sack(i+1,j)\} & W[i] \le j \end{cases}$$
 (1)

In plain english, what does Sack(i, j) represent?

c. BYB/BYG

Problem: You are given a $n \times n$ binary array A and the goal is to find the set of elements within that array that form a square filled with only **1**'s.

Recurrence:

In plain english, what does LSq(i, j) represent?

d. BYA/BYH

Problem: You are given an integer x that represents the length of rod you have and an array A where i corresponds to a rod length and A[i] corresponds to the price a rod of that length would fetch. You need to determine the maximum value you can fetch from the rod assuming you cut it optimally.

Recurrence:

$$MV(n) = \max_{0 \le i < n} (A[i] + MV(n-i))$$

In plain english, what does MV(n) represent?