

# Deep Learning - MAI

## Theory - Transformers

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## **Disclaimer:**

Many of the works this lesson is based on have not been thoroughly replicated yet. Conclusions and interpretations may be unreliable.

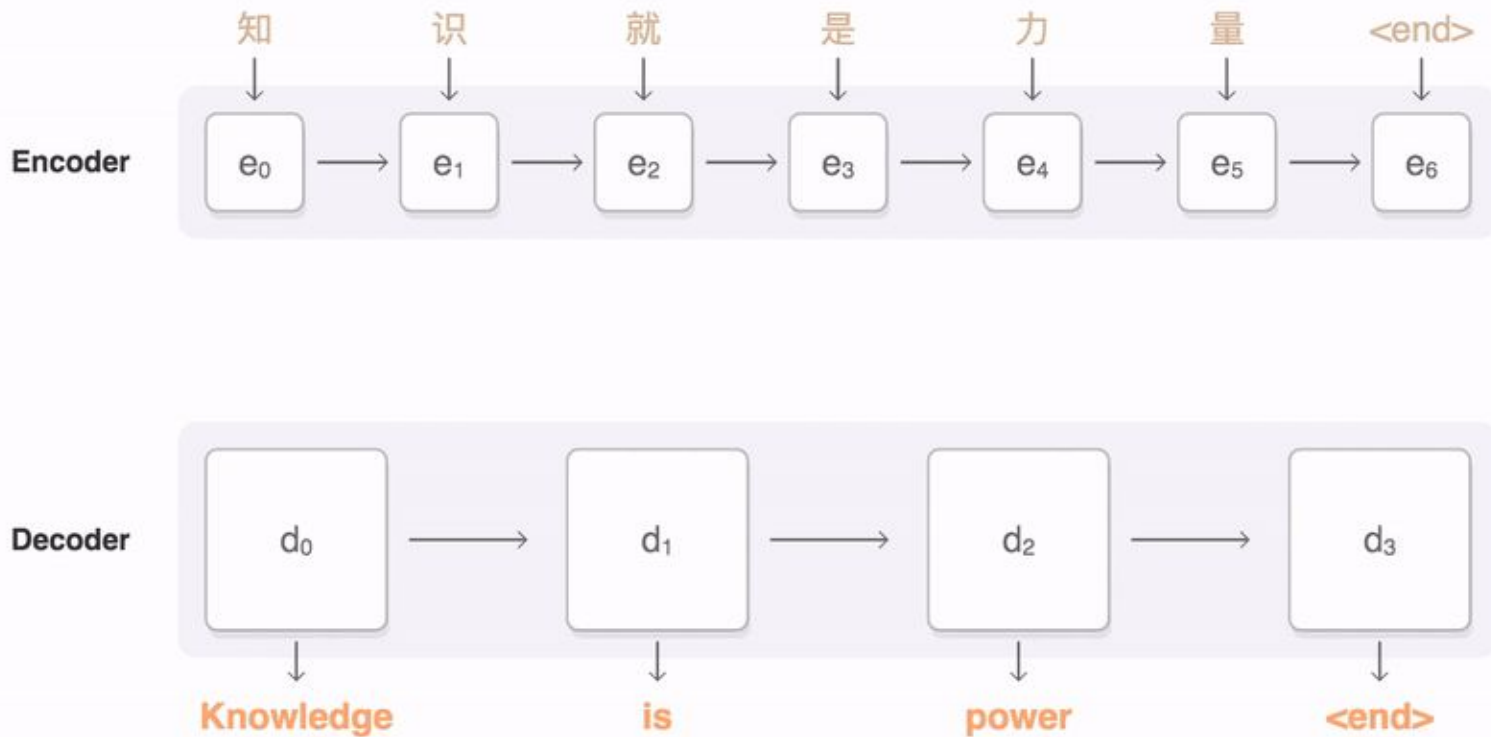
# Context

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# From Encoder-Decoder to Attention

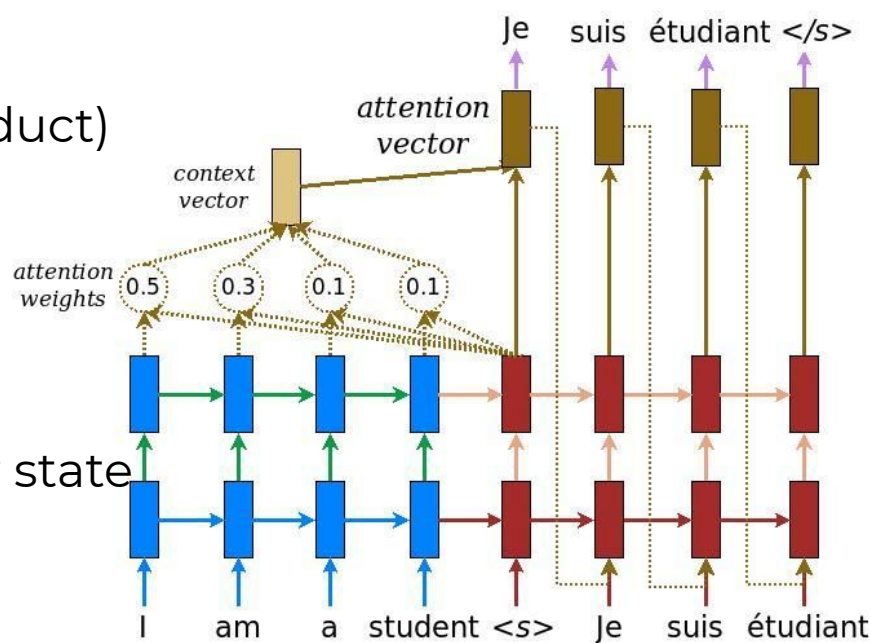
- ❖ seq2seq limitations
  - Full sentence into a fixed-sized, unique embedding (bottleneck)
  - Different parts of the decoder focus on different parts of the input
- ❖ Solution: Attention
  - Let each decoder step decide which part of the input use

# Attention overview



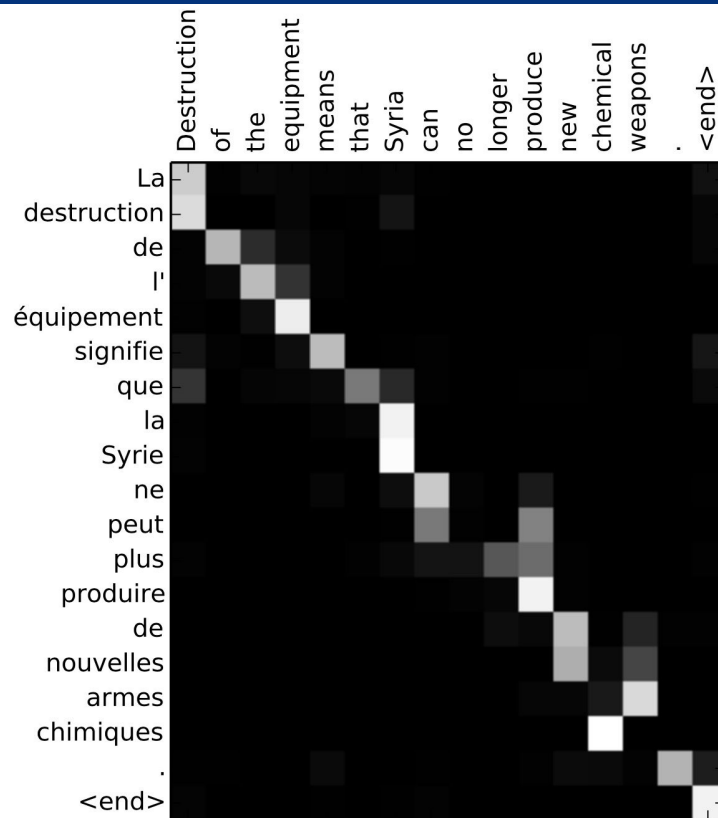
# Seq2seq with attention

- ❖ All encoder hidden states as decoder input
- ❖ Decoder states...
  - Score prev. hidden states (dot product)
  - Weight by their own probabilities (multiply by softmax value)
  - Sum to make the **context vec.**
  - Concatenate with hidden decoder state
  - Output and fed to next step



# Why seq2seq with attention

- ❖ Enables one different context for each decoding step
  - No fix-sized bottleneck
- ❖ Provides shortcuts (better gradient flows)
- ❖ More fine-grained -> better interpretability



# Attention to Transformers

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# The limits of RNNs

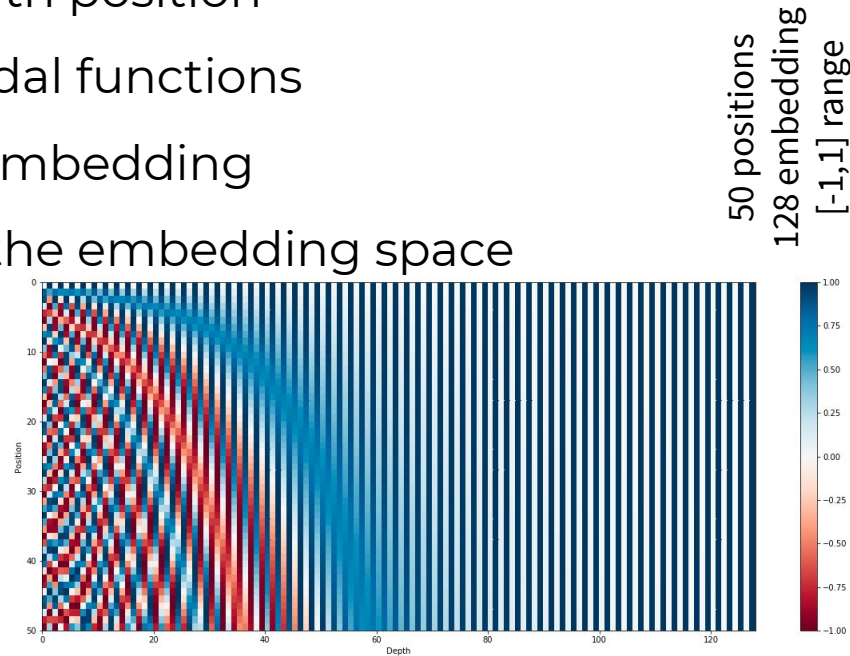
- ❖ The main challenges of RNNs
  - Distances (long, short or both?)
  - Directionality (data accessibility)
  - Lack of focus specificity (all look the same)
  - Poor parallelization
- ❖ How can we solve that?
  - As long as we work with **sequences**, is tough
    - Memory is hard to implement
    - Computational dependencies by sequential design

# The Attention revolution

- ❖ What if we *get rid of the sequence*? What if attention is enough?
  - No more sequences, no more memory, no more dependencies
  - Meet the Transformers
- ❖ Closer to *fully connected* than RNNs.
- ❖ All tokens processed concurrently (instead of recurrently)
  - Inputs are sets instead of sequences
  - Self-attention for focus

# Transformers and Order Position

- ❖ We need to keep some notion of position
  - Add order information on the input token embedding
  - Token representation changes with position
- ❖ *Positional encoding* through Sinusoidal functions
  - Add the position vector to each embedding
  - Provides consistent distances in the embedding space
    - Regardless of sequence length
    - Bounded range of values
    - Deterministic



# How basic attention works

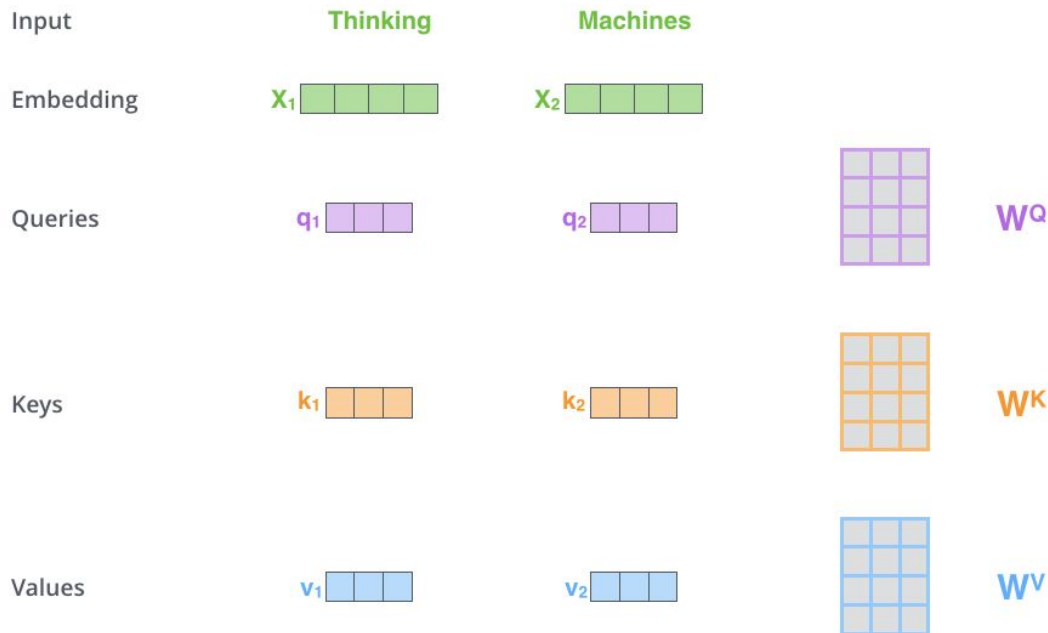
- ❖ Pseudo-limited connectivity (learnt sparsity, dense computation)
- ❖ Every input token has its own embedding
- ❖ All tokens stacked (e.g., word embeddings ) are the input
- ❖ Length of token is arbitrary (e.g., 512)
- ❖ Number of tokens defined by dataset

# Why attention works

- ❖ What should be computed together with input X?
- ❖ Learn and use a 'mask'
  - **Query** for what you want to match (current token)
  - **Keys** to match the query with (other tokens)
  - **Value** to be returned (relevance between both)
- ❖ Let's do it weighted, through matrix multiply
  - No dependencies. Parallelism!

# Basic attention

- ❖ Three weight matrices ( $\mathbf{Q}, \mathbf{K}, \mathbf{V}$ ) learnt
- ❖ Dot product from input embedding of token  $X$  and  $\mathbf{Q}, \mathbf{K}, \mathbf{V}$  matrices
  - $\mathbf{Q}, \mathbf{K}, \mathbf{V}$  vectors for token  $X$
  - Typically smaller dimensionality than token



# Basic attention

- ❖ Attention of token  $X$  on token  $Y$  (all with all):
  - Dot product between  $\mathbf{Q}$  vector of  $X$  and  $\mathbf{K}$  vector of  $Y$
  - Stabilize gradients (square root of vector length)
  - Normalize (apply softmax)
  - Multiply by  $\mathbf{V}$  vector of  $Y$  (weighting  $Y$  by relevance of  $Y$  w.r.t  $X$ )
  - Sum over all  $Y \rightarrow$  output for  $X$

$$\text{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}}\right)\mathbf{V}$$

# Multiple Embedding Spaces

- ❖ Multi-headed attention
- ❖ Learn different sets of Q,K,V matrices
- ❖ Each provides a different view on the data (enforceable on att. weights)
- ❖ On output
  - Concat all output embeddings in feature dim.
  - Multiply by another learnt matrix to fit dim.
- ❖ Attention heads can be computed in parallel



# Computing in Parallel

- ❖ Attention relates inputs at arbitrary distance within **constant** num. ops
  - Close or far away, it's the same
  - Fully-connected style
- ❖ ByteNet does so within a **logarithmic** num. ops (dilated convolutions)
- ❖ Convs s2s does so within a **linear** num. ops
- ❖ Retaining memory is more complicated as this grows

1) This is our  
input sentence\*

2) We embed  
each word\*

3) Split into 8 heads.  
We multiply  $X$  or  
 $R$  with weight matrices

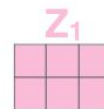
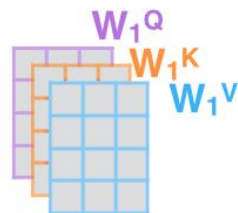
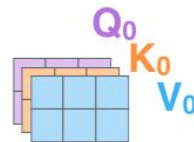
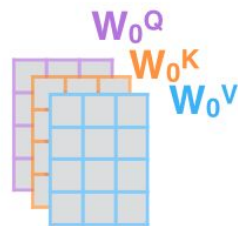
4) Calculate attention  
using the resulting  
 $Q/K/V$  matrices

5) Concatenate the resulting  $Z$  matrices,  
then multiply with weight matrix  $W^O$  to  
produce the output of the layer

Thinking  
Machines



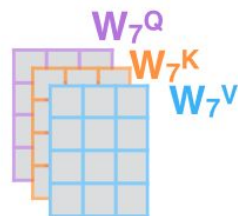
\* In all encoders other than #0,  
we don't need embedding.  
We start directly with the output  
of the encoder right below this one



...

...

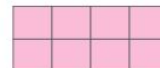
...



$W^O$

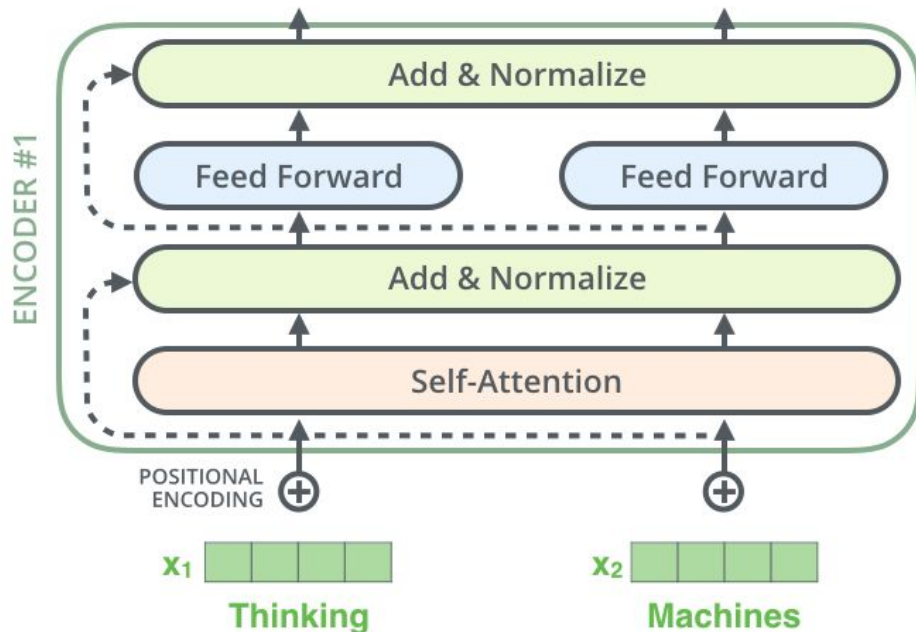


$Z$



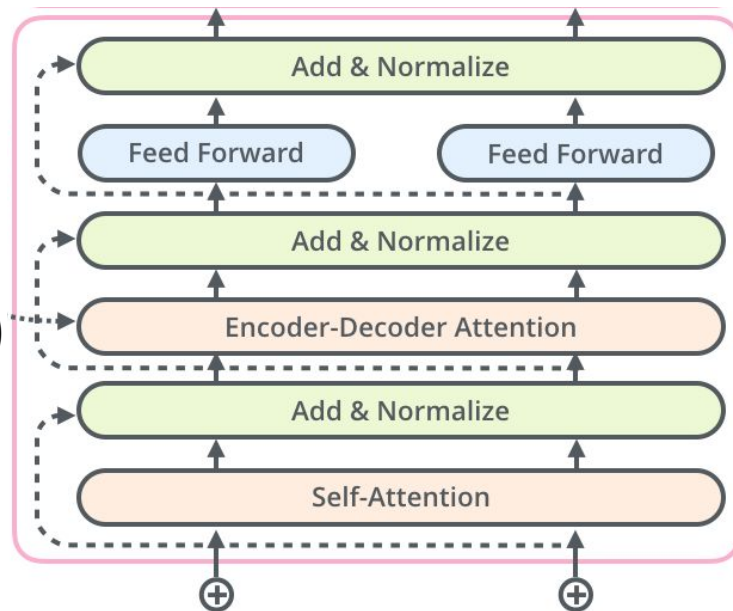
# The Encoder block

- ❖ Self-Attention + Feed Forward
  - Each token follows its own path
- ❖ Both with
  - Residual connection
    - To self-attend or not
  - Layer normalization
    - Sample-wise layer-wide mean and var.
- ❖ Stack several of these blocks



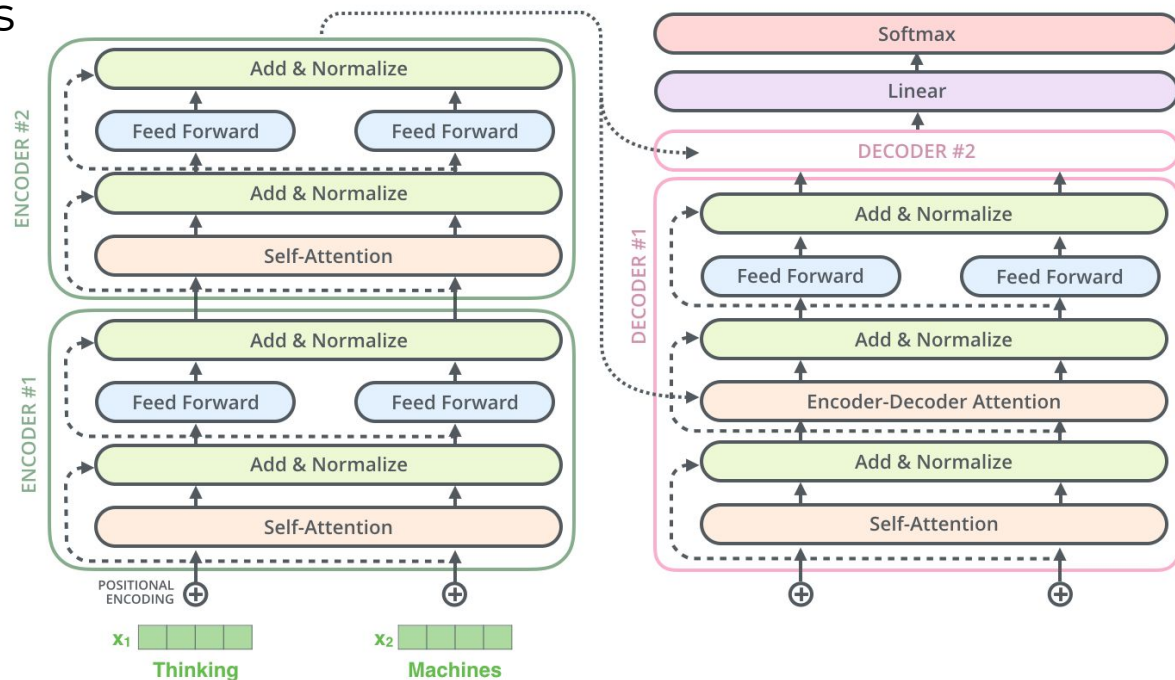
# The Decoder block

- ❖ Same components as encoder
  - Self-Attention in the past only (mask out previous tokens)
  - Encoder-Decoder attention (**K** & **V** from encoder, **Q** from prev dec.)
  - Feed Forward, Residual & Norm
- ❖ Input: Special token, then previous token (also with pos. encoding)



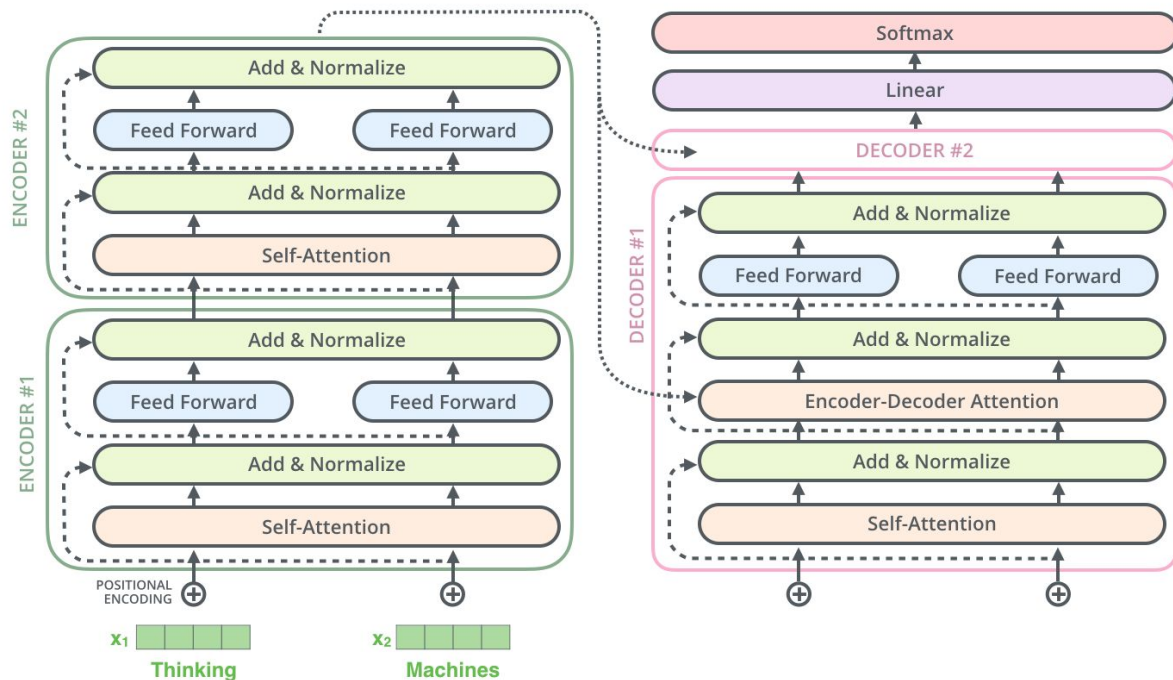
# From input to output

- ❖ Linear layer for logits (dictionary length!)
- ❖ Softmax for probabilities



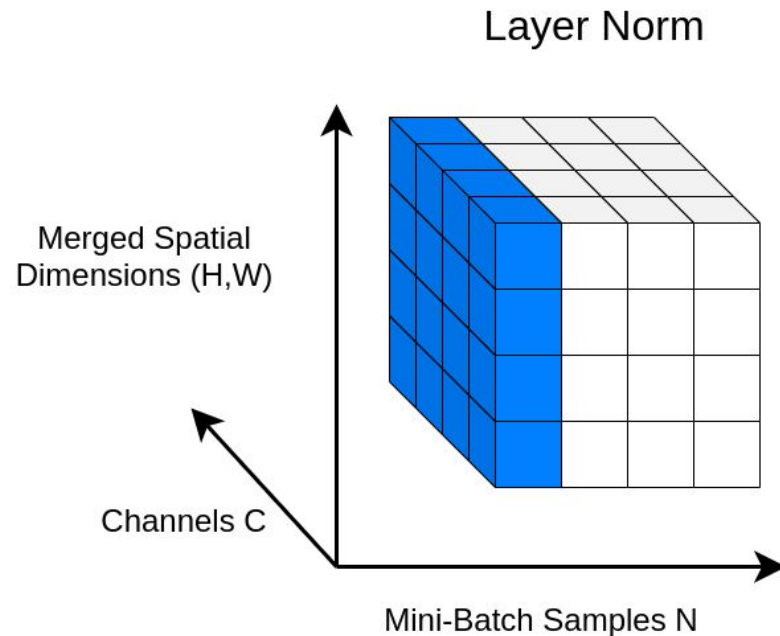
# General Transformers

- ❖ Without positional encoding, a transformer is a fully connected NN with focus



# Layer Normalization

- ❖ Normalize sample-wise
- ❖ Compute mean and std-dev across spatial dimensions (1 for sequences) and channels



# Loss & Training

- ❖ A transformer outputs a vector of probabilities a number of times (?)
  - Cross entropy loss against golden probabilities\*
- ❖ Batch training requires padding
- ❖ As with RNNs, decoders use
  - Greedy search (explore one path only)
  - Beam search (explore  $n$  branches on each step)



# Transformer details

- ❖ In the original paper
  - Adam optimizer. Warm-up round and then decay
  - Dropout on residual connections, embeddings sums and pos. enc.
  - Label smoothing

# Limitations of Transformers

- ❖ Reduced resolution (averaging attention)
  - Multi-head to circumvent
- ❖ Sequence length
  - All tokens must be computed concurrently (for context)
- ❖ Computational cost / Complexity
  - All relations are learnt (quadratic self-attention complexity). No limited connectivity by design.

# A serious issue

- ❖ Transformers are efficient, but costly

- Worthy trade-off?
- Measuring efficiency

- ❖ Interpretability (too many heads)

- ❖ Google ethical crisis (Gebru, Bengio, ...)

- Stochastic parrots

- ❖ Interpretability (too many heads) & Bias (too many data)

## Common carbon footprint benchmarks

in lbs of CO2 equivalent

Roundtrip flight b/w NY and SF (1 passenger)	1,984
Human life (avg. 1 year)	11,023
American life (avg. 1 year)	36,156
US car including fuel (avg. 1 lifetime)	126,000
Transformer (213M parameters) w/ neural architecture search	626,155

Chart: MIT Technology Review • Source: Strubell et al. • Created with Datawrapper

# Fancy Transformers

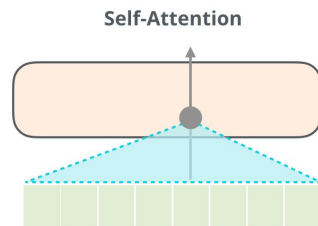
# Beyond Encoder-Decoder

- ❖ Encoder-Decoder was inherited from RNN times
- ❖ Transformers (aka self-attention) is beyond that
- ❖ What works:
  - Pre-train heavy (as in Google-level, Millions of \$)
  - Fine-tune for everything
- ❖ The story goes: GPT - BERT - GPT2 - GPT3 - ....
- ❖ Tell me how do you pre-train and...

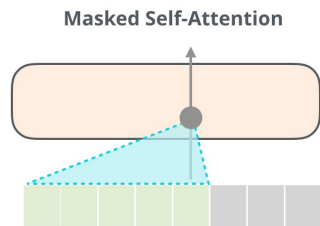
# The two (main) sides

- ❖ Encoder only (BERT)
  - Bidirectional Transformer
  - Gain context (classification↑)
- ❖ Decoder only (GPT family)
  - Left to Right Transformer
  - Gain auto-regression (generation↑)

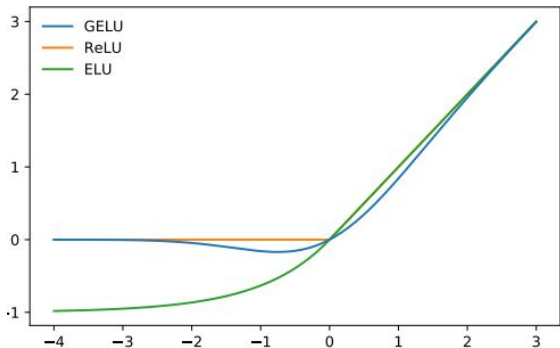
Denoising self-supervised  
(encoder)



Language modeling  
(decoder)

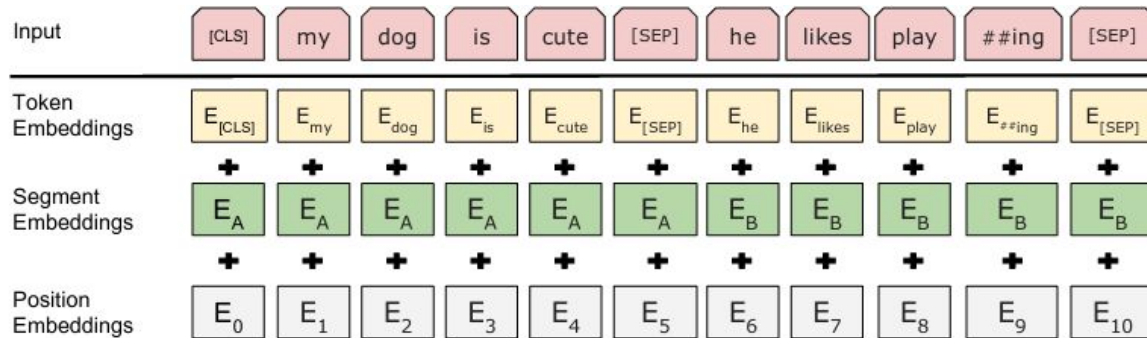


- ❖ GELU instead of ReLU
  - Gaussian Error Linear Unit



# Famous Transformers: BERT

- ❖ For text generation: Encoder only
- ❖ Special token to separate sentences, and embedded id (+pos. enc.)
- ❖ Train two tasks concurrently
  - Masked LM: Mask 15% of tokens, and try to predict them
  - NSP (Sentence prediction): Is the follow up sentence correct?



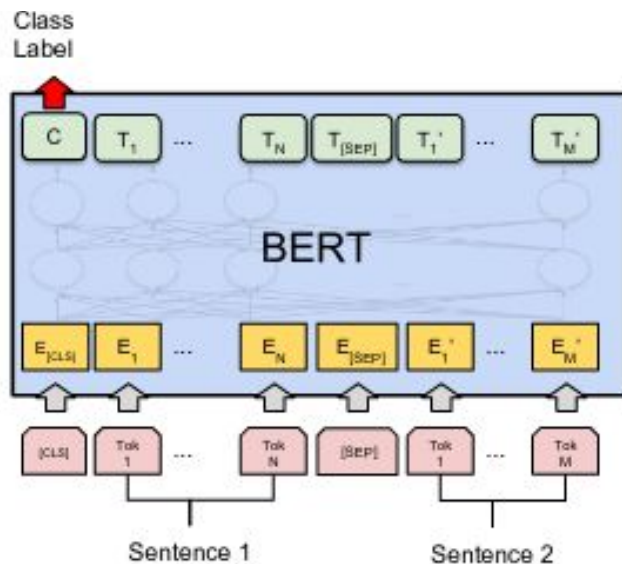
[65,66]

# Famous Transformers: BERT

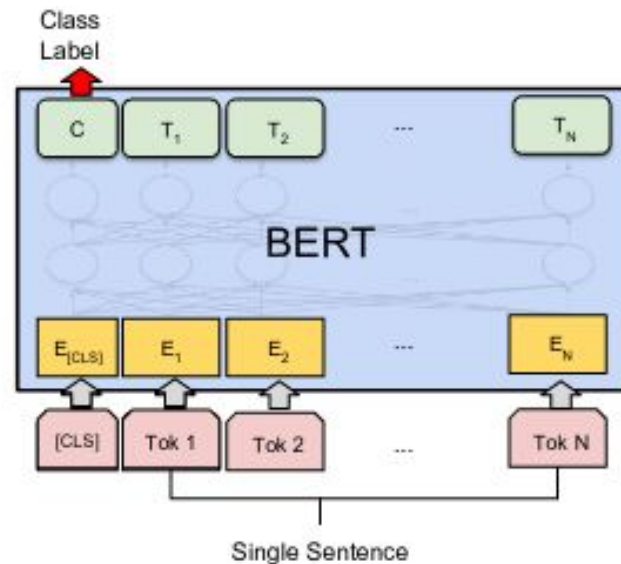
- ❖ Pre-train (bulk text) + fine-tuning (paraphrasing, QA, classification, ...)
- ❖ BERT-base:
  - 6 blocks, 12 attention heads, 110M params (4 TPUs 4 days)
- ❖ BERT-large
  - 12 blocks, 16 attention heads, 340M params (16 TPUs 4 days)
- ❖ Fine-tuning: 1 TPU 1 hour



# Famous Transformers: BERT

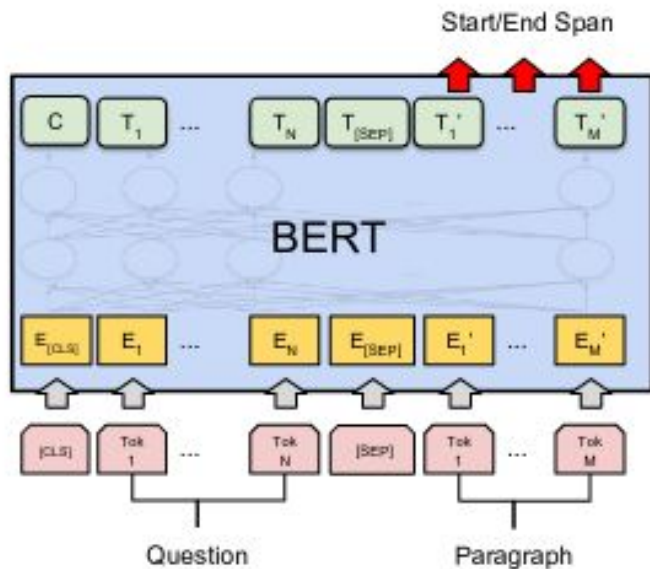


(a) Sentence Pair Classification Tasks:  
MNLI, QQP, QNLI, STS-B, MRPC,  
RTE, SWAG

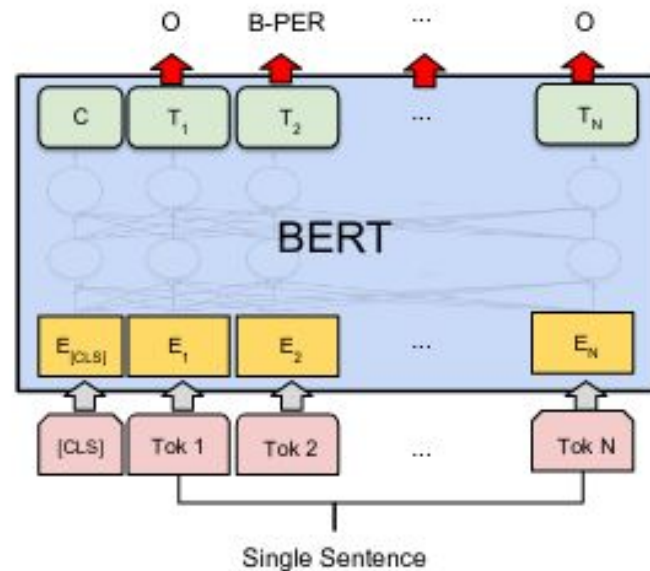


(b) Single Sentence Classification Tasks:  
SST-2, CoLA

# Famous Transformers: BERT



(c) Question Answering Tasks:  
SQuAD v1.1



(d) Single Sentence Tagging Tasks:  
CoNLL-2003 NER

# Famous Transformers: GPT

## ❖ GPT

- Pretrain + fine-tune (117 M params)

## ❖ GPT2

- More data, 48 blocks, zero-shot task/transfer (1,500 M params)
- 1024 tokens

## ❖ GPT3 (& DALL-E)

- More data, 96 blocks, 96 heads, (175 B params)
- 2048 tokens

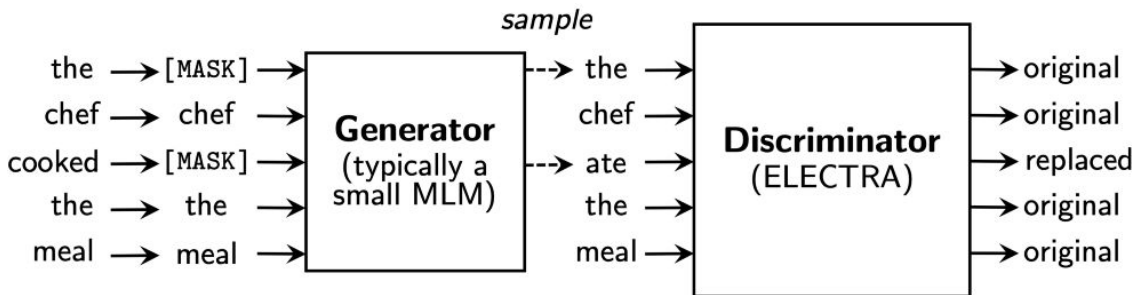
# Pre-training Transformers like GANs

## ❖ Masked Language Model (BERT)

- Limited token efficiency
- Differences between train/test

## ❖ Electra

- Generator / Discriminator scheme (keep the later)
- Validate each token
- Full token efficiency
- Faster (12x)

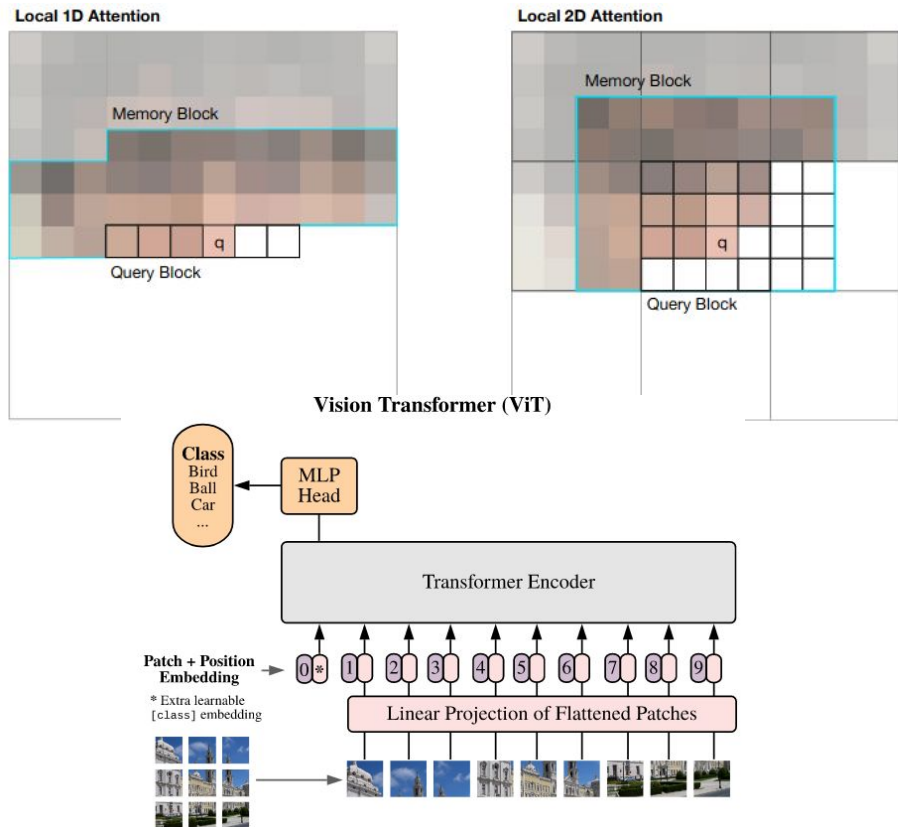


# Vision Transformers (ViTs)

- ❖ Lack inductive biases implicit in CNNs
  - Translation invariance (weight sharing)
  - Locality (limited connectivity)
- ❖ **These can be learnt from enough data** (14M - 300M samples)
  - Mitigable by knowledge distillation - soft labels - noisy student (?)
- ❖ Each pixel attending to each other pixel is unfeasible
  - Several local self-attention mechanisms are being proposed

# Vision Transformers (ViTs)

- ❖ Doing CNNs with Transformers
  - Self-attention limited spatially
  - Images flattened to 1D
  - Positional encodings
  - Attention bottlenecks
  - Autoencoders



# So what are Transformers?

- ❖ Great models for processing data which can be represented as a set of independent numerical features
  - More powerful and smarter version of FFN nets
  - If computation and data availability allows!
- ❖ Capable of including location info through Positional Encodings
- ❖ Can be good for sequences (the shorter the better). Not for streams, recursion and hierarchies.
- ❖ The biggest hammer out there right now

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