HOMEWORK

- (1) Write out all elements of the set $\mathcal{P}(\{0,1,2\})$.
- (2) Prove the following identity:

$$(X \cup Y) \cap Z = (X \cap Z) \cup (Y \cap Z)$$

(3) Prove the following identity:

$$(X \cup Y)^c = X^c \cap Y^c$$

(4) A set is called *finite* if it only has a finite number of elements. For a finite set X, we denote by |X| the number of the elements in X. It is called the *order* of X. Establish the following theorem: if X is a finite set and $Y \subseteq X$ then

$$|Y| \le |X|$$

Note that you should show that Y is also finite so be able to use |Y|.

The contrapositive of this result says that if |Y| > |X| then $Y \nsubseteq X$.

- (5) Decide (with proof) if the following are true always, sometimes, or never.
 - (a) Let X and Y be sets such that $X \setminus Y = \emptyset$. Then X = Y.
 - (b) Let X, Y, and Z be sets such that $X \setminus Y = Z$ and $Y \subseteq Z$. Then $X = Y \cup Z$.
 - (c) Let X be a set. Then $\{\emptyset\} \in \mathcal{P}(X)$.