Visualizing Dynamic Programming On Tree Decompositions

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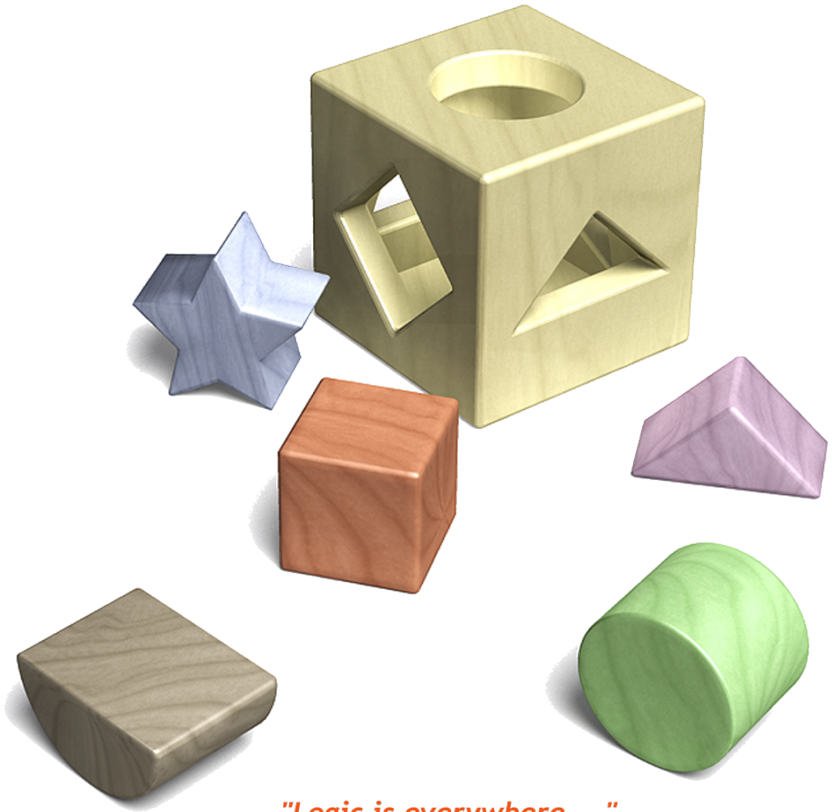
- WHAT **was the motivation**
- WHAT **could be used previously?**
- WHO **benefits from visualization?**
- CHALLENGES **and solutions**
- WHAT **could be developed next?**



"Logic is everywhere ..."

About me

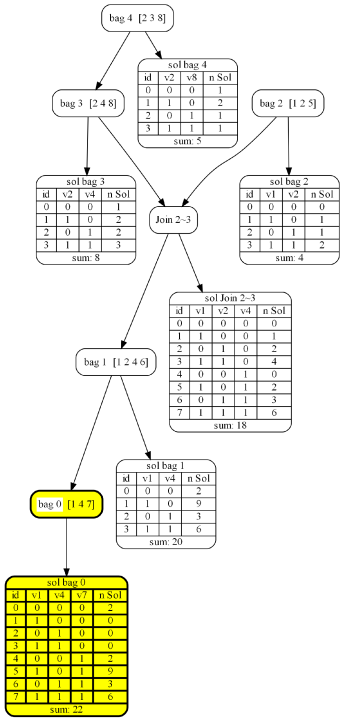
Martin Röbke
Johannes Fichte
Stefan Gumhold

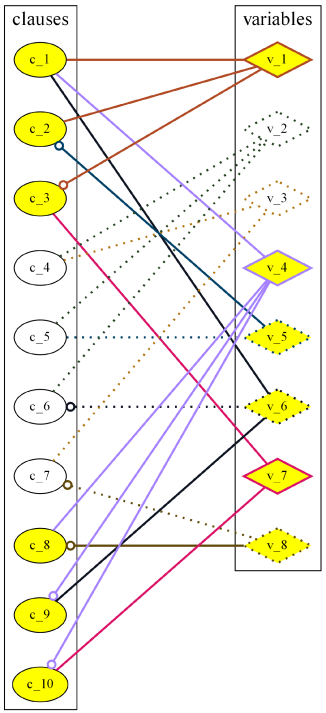
Motivation

Creating Visualization for:

Improving

- **examples for students**
- **debugging and improving interaction of complex data-structures**
- **hotspots**





Existing Visualization

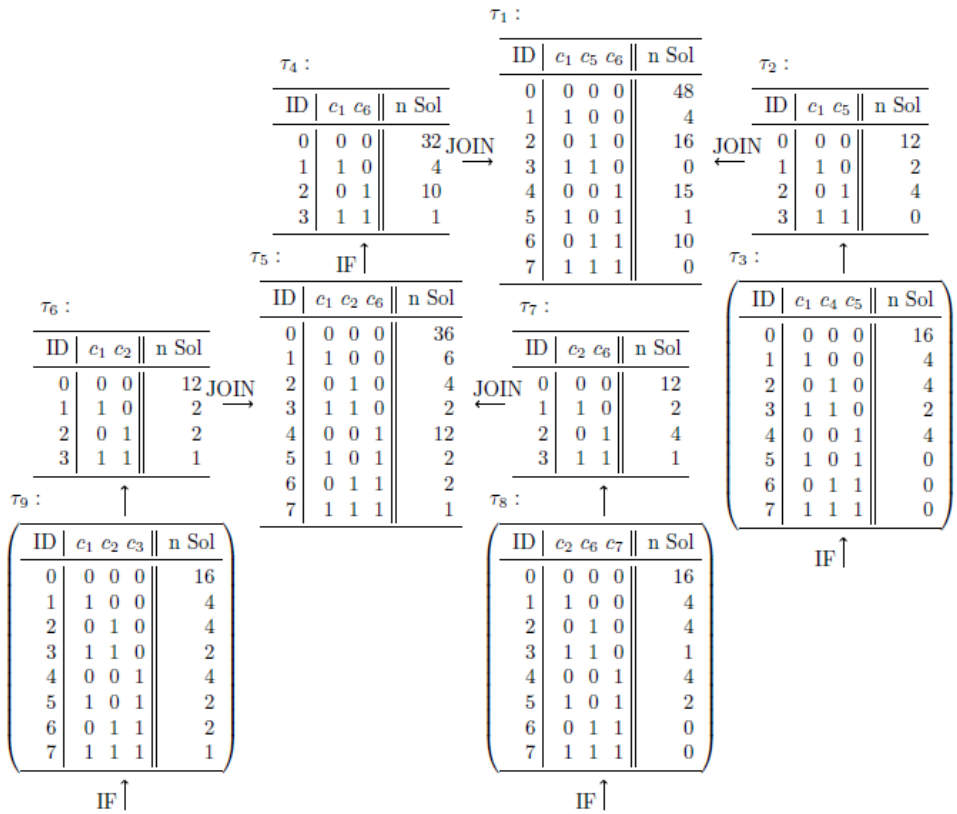


Figure: Handcrafted #SAT example-run from Markus Zisser[1]

[1] "Solving #SAT on the GPU with Dynamic Programming and OpenCL", Diploma Markus Zisser 2018 Technische Universitï¿½t Wien, p.33

Existing Visualization

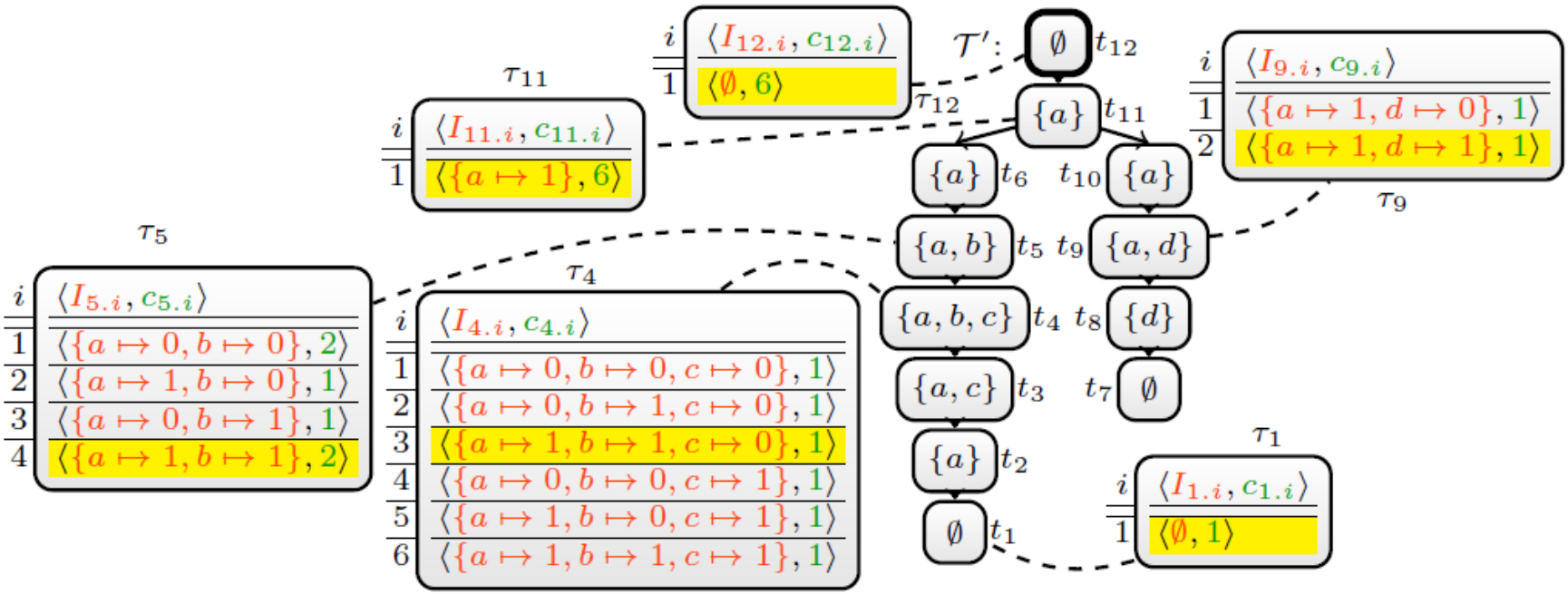


Figure: Handcrafted #SAT example-run from dpdb[2]

[2] "Exploiting Database Management Systems and Treewidth for Counting", Fichte, Hecher, Thier, Woltran

Background

(Weighted) Model-Counting

Graphs for Boolean Formulas

- **Example set of CNF-clauses:**

$\{c1 = \{v1, v3, \neg v4\}, c2 = \{\neg v1, v6\}, c3 = \{\neg v2, \neg v3, \neg v4\}, c4 = \{\neg v2, v6\}, c5 = \{\neg v3, \neg v4\}, c6 = \{\neg v3, v5\}, c7 = \{\neg v5, \neg v6\}, c8 = \{v5, v7\}\}$

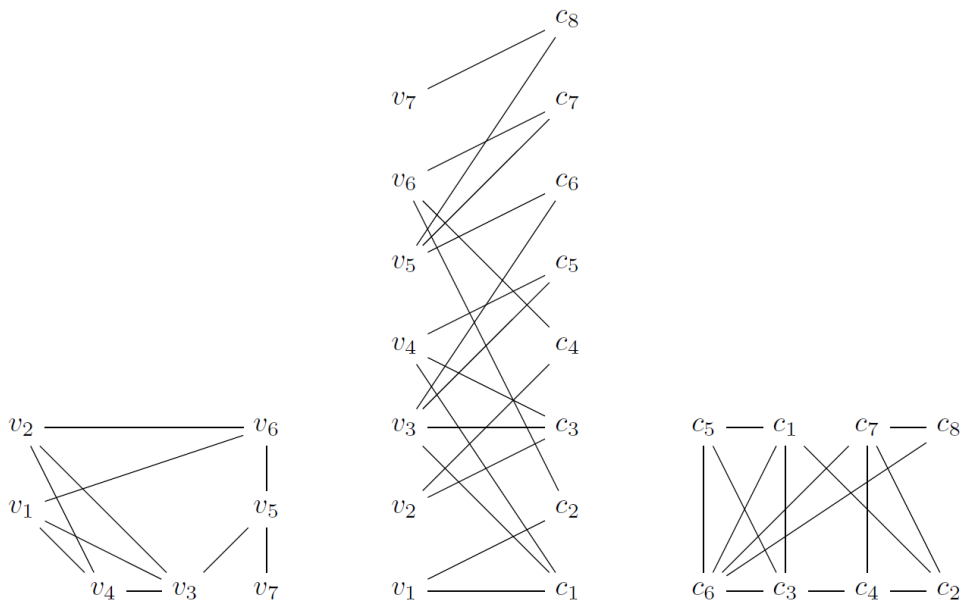


Figure: The primal (left), incidence (middle) and dual (right) graph

Tree Decompositions

Parameterized Complexity and its Applications in Practice
From Foundations to Implementations
Johannes K. Fichte
TU Dresden, Germany
Jakarta, Indonesia
Summer 2019 (May 6th - May 16th) pages 162-174

Backup: VC tree vs graph - example p69, 128

Example: Vertex-Cover problem

Courcelle's theorem

For all $k \in \mathbb{N}$ and MSO-sentences F is the decision problem for a given graph G, whether $G \models F$ is true, in time $2^{p(tw(G))} \cdot |G|$ with a polynom p decidable.

- **drawback: still expensive ($2^{p(twG)}$, $2^{2^{(\#Q)}}$, large constants)**
- **usage:**

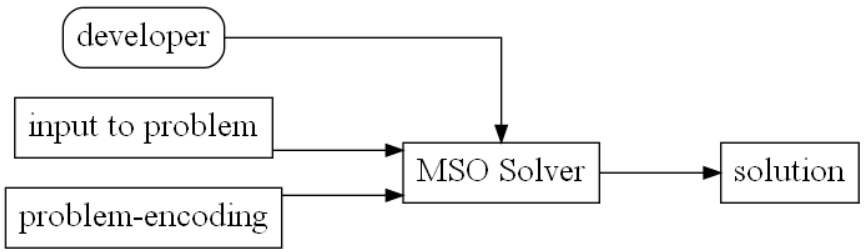


Figure: Implementation of the theorem

Existing Visualization

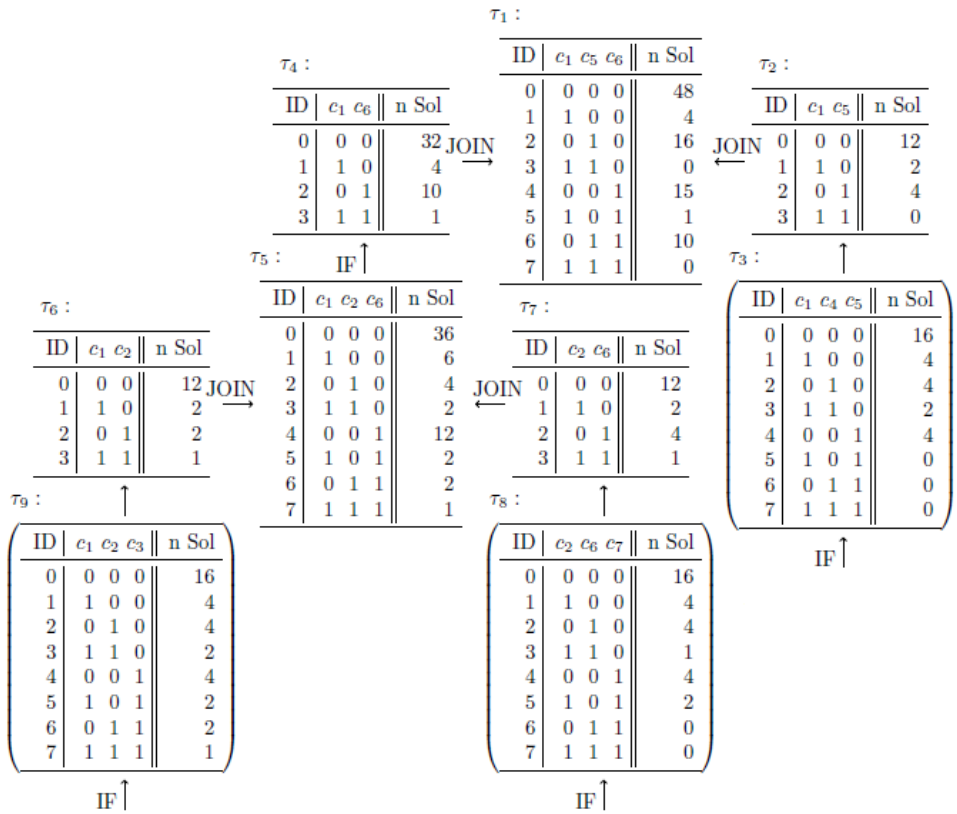


Figure: Handcrafted #SAT example-run from Markus Zisser[3]

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Existing Visualization

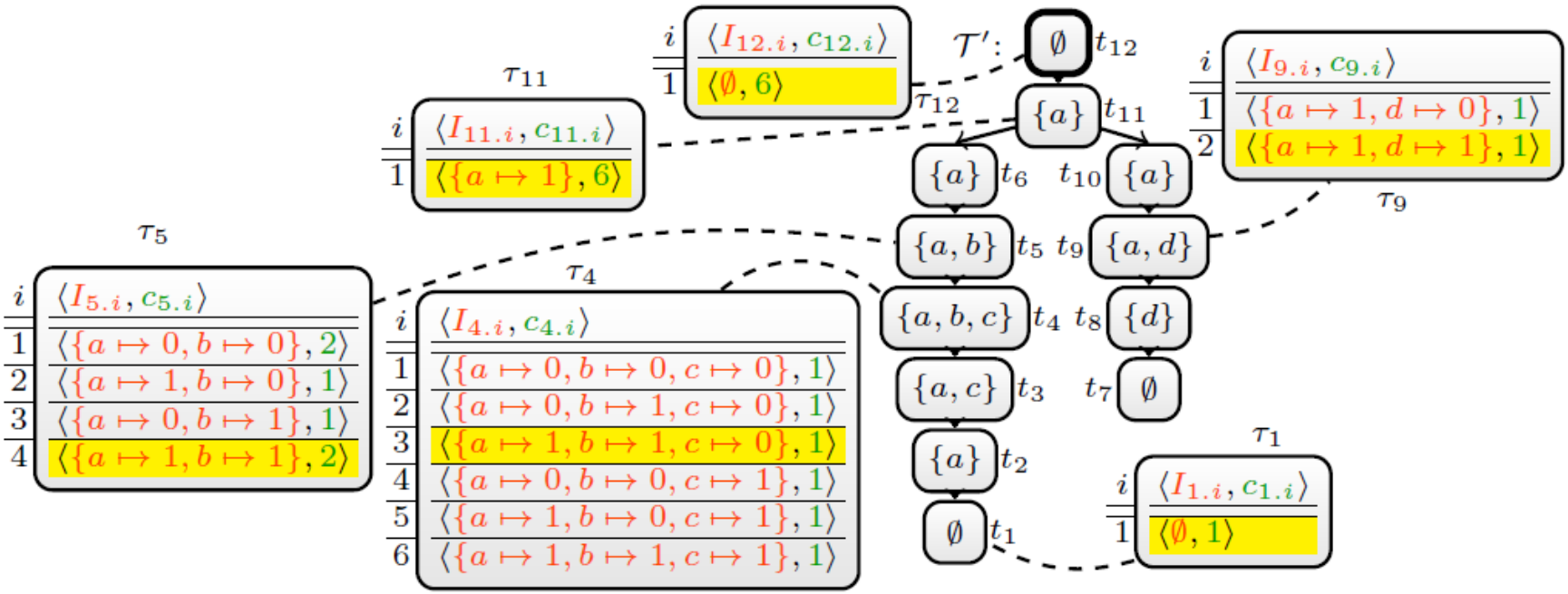


Figure: Handcrafted #SAT example-run from dpdb[4]

[4] "Exploiting Database Management Systems and Treewidth for Counting", Fichte, Hecher, Thier, Woltran

gpuSAT2 - Improving Upon Previous Ideas

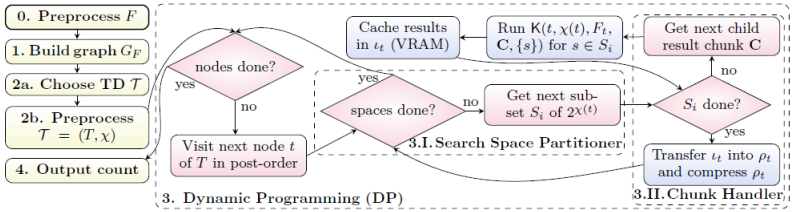
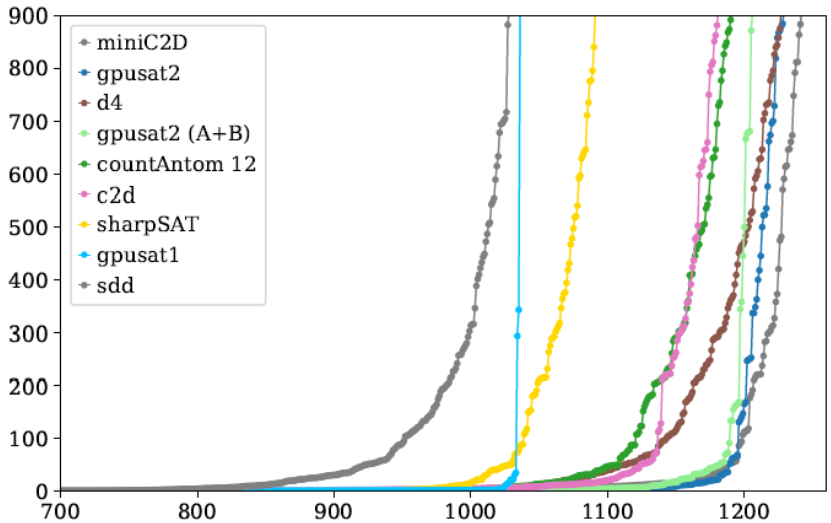


Figure 1: Architecture of our DP-based solver for parallel execution. Yellow colored boxes indicate tasks that are required as initial step for the DP-run or to finally read the model count from the computed results. The parts framed by a dashed box illustrate the DP-part. Boxes colored in red indicate computations that run on the CPU. Boxes colored in blue indicate computations that are executed on the GPU (with waiting CPU).

- **only primal graph (simpler solving DP)**
- **customized tree decompositions**
- **adapted memory-management**
- **improved precision handling**



dpdb

Using databases for intermediate results

- **SAT**
- **#SAT**
- **Vertex cover**

- #εTab#: `SELECT 1 AS cnt`
- #intrTab#: `SELECT 1 AS val UNION ALL 0`
- #localProbFilter#: $(l_{1,1}$ `OR ...` `OR` $l_{1,k_1})$ `AND ...` `AND` $(l_{n,1}$ `OR ...` `OR` $l_{n,k_n})$
- #aggrExp#: `SUM(cnt) AS cnt`
- #extProj#: τ_1`.cnt * ... *` τ_ℓ`.cnt AS cnt`

(a) Problem #SAT

- #εTab#: `SELECT 1 AS cnt`
- #intrTab#: `SELECT 1 AS val UNION ALL ... UNION ALL` o
- #localProbFilter#: `NOT` $([\![u_1]\!] = [\![v_1]\!])$ `AND ...` `AND NOT` $([\![u_n]\!] = [\![v_n]\!])$
- #aggrExp#: `SUM(cnt) AS cnt`
- #extProj#: τ_1`.cnt * ... *` τ_ℓ`.cnt AS cnt`

(b) Problem #o-Col

- #εTab#: `SELECT 0 AS card`
- #intrTab#: `SELECT 1 AS val UNION ALL 0`
- #localProbFilter#: $([\![u_1]\!]$ `OR` $[\![v_1]\!])$ `AND ...` `AND` $([\![u_n]\!]$ `OR` $[\![v_n]\!])$
- #aggrExp#: `MIN(card) AS card`
- #extProj#: τ_1`.card + ... +` τ_ℓ`.card -` $(\Sigma_{i=1}^{\ell}|\chi(t_i) \cap \{a_1\}|$ `- 1) *` $\tau_1.[\![a_1]\!]$ `- ... -` $(\Sigma_{i=1}^{\ell}|\chi(t_i) \cap \{a_k\}|$ `- 1) *` $\tau_1.[\![a_k]\!]$

(c) Problem MinVC

github: `https://github.com/hmarkus/dp_on_dbs`

Challenge1

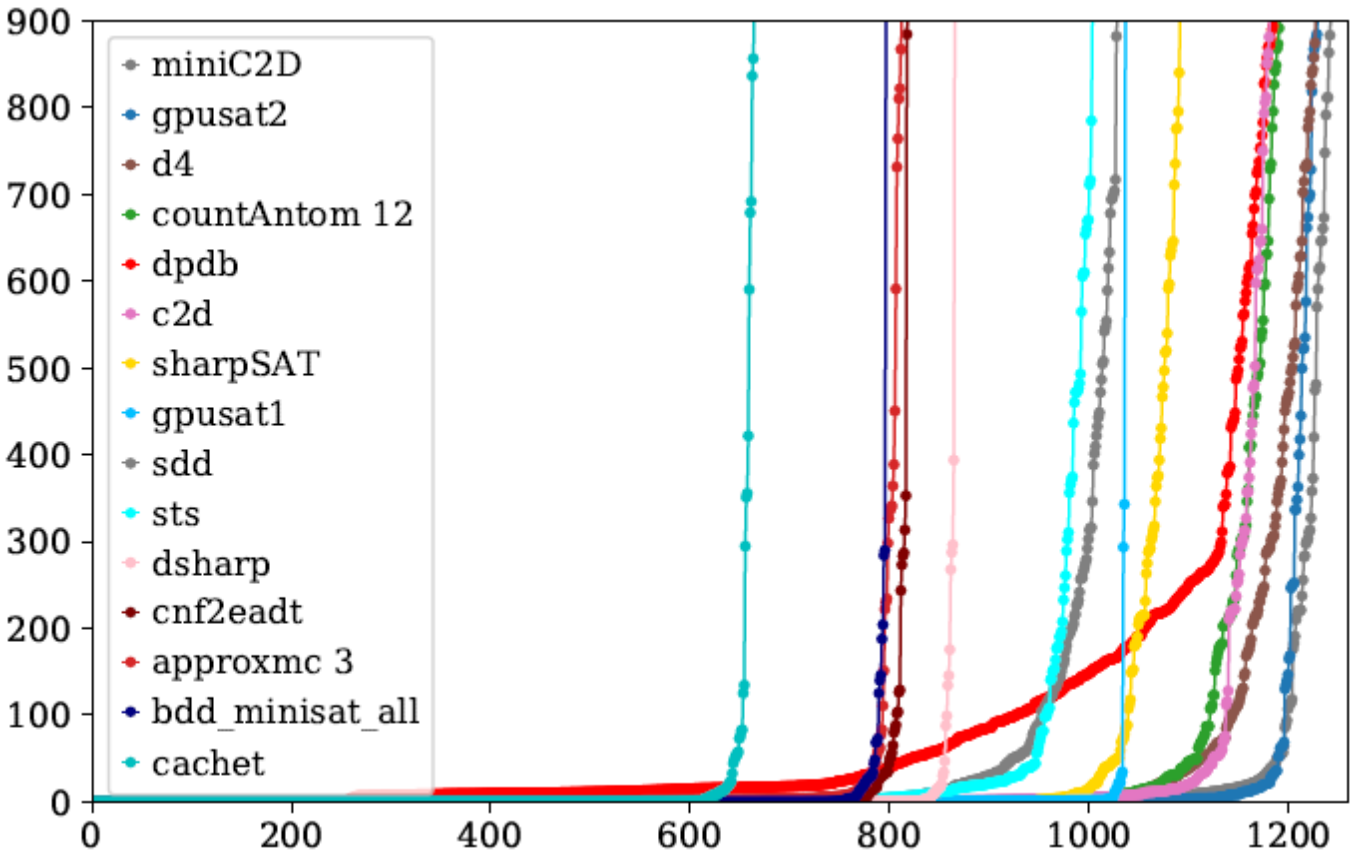
Challenge2

Challenge3

Outlook

Benchmark

Performance of all three programs on #SAT instances:



Bibliography