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Bachelor Thesis

Visualizing Dynamic Programming on Tree Decompositions

Author:

Martin Rübke

Supervisor:

Dr. Johannes Fichte

INTERNATIONAL CENTER FOR COMPUTATIONAL LOGIC

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Martin Röbbke
Matrikelnummer 3949819
Geburtsdatum 04.03.1995

TU Dresden E-Mail-Adresse:
Martin.Roebke@tu-dresden.de

Dresden,

.....

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Abstract

Answering questions that be expressed using graph theory is increasingly interesting in scientific work. Many problems such as Boolean satisfiability or problems related to traffic can be translated to and solved on a graph. We think that utilizing the graph structure of problems and the connection between data points can help to improve algorithms concerning problems for different areas of interest.

The algorithms we visualize in this thesis use dynamic programming on tree decompositions of such graphs. We preprocess the input graph into a customized tree-decomposition of small tree-width. This gives us a description of the processing sequence for the algorithm, and allows with right hindsight for good parallelization and allows for faster solving times on larger instances.

To help for further refinement and visualization of the dynamic programming, we specified a JSON-form to communicate between solvers and the newly created visualization tool TDVisu.

As two reference implementations of dynamic programming on tree decompositions we selected the existing solvers GPUSAT and dpdb.

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1. Introduction

Graphs are increasingly interesting in scientific work, as the applications of interconnected datasets grow. Some use cases for example outlined here do include fields of interest like

- Network and Database Infrastructure
- Recommendation Engines
- Artificial Intelligence and Analytics

It defines a JSON-format specification for portability and customization of the visualization combined in one human-readable file and two reference implementations in actual solvers. The implementation currently does not support hyper-graphs and assumes that each node in the tree decomposition has either one or two children. The visualization output consists by default of scalable-vector-graphics SVG, a very flexible text-based that can be compressed and modified very easily without loss of quality. The images are split up into different views on the current state of the tree decomposition for consecutive user-defined time steps showing the progress of the dynamic programming. As illustrations of the possibilities for an application smaller examples from the problem-types "#SAT" and "minimal vertex cover" are presented, as well as an example of a faulty tree-decomposition that occurred during development. Intended audience:

- Developer of dynamic programming on tree decompositions for debugging.
- Researcher of such algorithms for comparisons and visualizations.
- Teachers or students looking for automatic visualization of their examples and the dynamic programming.

The idea for this project comes from my supervisor Dr. Johannes Fichte, who works with many projects such as dpdb on solving monadic second order logic (MSOL[CE12]) problems using highly parallelized architectures like graphics processing units or state of the art databases. One early implementation is published in [Lan+12] where for different real world examples the results looked promising. These projects are very competitive for solving even large instances of those problems. The source code for TDVisu is available under GPL3 license.

Graphviz is open source graph visualization software that provides customizable visualization for directed and undirected graphs. The information processed by graphviz intro. mit motivation und related work, state of the art, advancements.

Visualization Pipeline

Stand Umsetzung, Tools: Slack, Trello, GitHub, Presentations

2. Background

This chapter provides the reader with a brief background for this work.

We begin with a description on SAT and #SAT as examples for a very general problem that can be described with monadic second order logic (MSOL). Furthermore the general case of MSOL will be described, as well as the *DIMACS*-file-format used in the projects. The following section describes Tree Decompositions (TDs) which are the basis for our visualization. Finally we shortly discuss Courcelle's Theorem [CE12] as a related method of solving these problems.

2.1. Boolean satisfiability problem

https://en.wikipedia.org/wiki/Boolean_satisfiability_problem

SAT was the first known NP-complete problem, shown by Stephen Cook at the University of Toronto in 1971 [Coo71]

literal \equiv boolean variable v or its negation

clause \equiv finite set of literals, interpreted as the disjunction

unit \equiv clause with $|c|=1$

CNF formula \equiv set of clauses, interpreted as their conjunction

var \equiv set of variables contained in the clause or clause set C

assignment $\equiv \alpha: \text{var}(C) \rightarrow \{0,1\}$

satisfiedclause \equiv if $\exists v \in \text{var}(c), v \in c$ and $\alpha(v)=1$ or $\neg v \in c$ and $\alpha(v)=0$. Otherwise falsified

satisfiedform \equiv each clause in the formula is satisfied by assignment

Connection to graphs with [Zis18]

SAT Handbook: Even finding a single solution can be a challenge for such problems; counting the number of solutions is much harder. Not surprisingly, the largest formulas we can solve for the model counting problem with state-of-the-art model counters are orders of magnitude smaller than the formulas we can solve with the best SAT solvers. Generally speaking, current exact counting methods can tackle problems with a couple of hundred variables, while approximate counting methods push this to around 1,000 variables.

2.2. Monadic Second Order Logic

See also figure 9.

Explain graphs? Node, Edge

MSO graph properties are "fixed-parameter-tractable" with respect to clique-width and tree-width. <https://www.youtube.com/watch?v=hZI-wANH01w> 5th workshop on Graph Classes, Optimization, and Width Parameters (GROW 2011) 2011-10-28. MSO

counting (k-colorings)and optimizing (distance between two vertices...) functions. Interested in MSO logic over graphs.

Two types of MSO formulas *or logical graph representations*.

- MSO formulas
- MSO_2 formulas with edge quantification \equiv MSO formulas over incidence graphs
- $G=(\text{vertices}, \text{edges as binary relation})$
- $\text{INC}(G) = (\text{vertices and edges}, \text{Inc})$ for G undirected: $\text{Inc}(e,v)$ \iff v is a vertex of edge e
- FPT for clique width
- FPT for tree-width

This can also be done for directed graphs!

Typical MSO_2 graph properties:

has a perfect matching has a Hamiltonian circuit spanning tree of degree ≤ 3

The expressions have the form: "There exists a **set of edges** that is..." can not be transferred into "set of vertices"

<https://youtu.be/Wyn3djrYg7c?t=1385> Bruno Courcelle: Recognizable sets of graphs: algebraic and logical aspects <https://library.cirm-math.fr/Record.htm?idlist=2&record=19276851124910940339> Recording during the thematic meeting: "Frontiers of reconnaissability" the April 29, 2014 at the Centre International de Rencontres Mathématiques (Marseille, France)

FPT for model checking: An algorithm is FPT if it takes time $f(k) \cdot n^c$ for some fixed function f and constant c . The size of the input is n . The value k is a parameter of the input. This algorithm is then usable for small values of k . usually tree-width and clique width.

2.3. DIMACS Format

Developed in 1993 at Rutgers University. DIMACS (the Center for Discrete Mathematics and Theoretical Computer Science)

Wolfram Language fully supports the DIMACS format for storing a single undirected graph. <https://reference.wolfram.com/language/ref/format/DIMACS.html>

DIMACS CNF: This format is used to define a Boolean expression, written in conjunctive normal form. <https://people.sc.fsu.edu/~jburkardt/data/cnf/cnf.html>

Other formats for WMC, different graphs...

Supported also in Maple <https://www.maplesoft.com/support/help/maple/view.aspx?path=Formats/CNF>

Examples in appendix

2.4. Tree Decomposition

[Zis18]chapter 2.2 Tree decompositions were originally introduced by Robertson and Seymour [RS84] in 1984. A *tree decomposition* (TD) of a graph G is a pair (T, χ) . T is a tree and χ is a mapping which assigns each node $n \in V(T)$ a set $\chi(n) \subseteq V(G)$ called a *bag*. Then (T, χ) . T is a TD if the following conditions hold:

1. for each vertex $v(n) \in V(G)$ there is a node $n \in V(T)$ such that $v \in \chi(n)$
2. for each edge $(x, y) \in E(G)$ there is a node $n \in V(T)$ such that $x, y \in \chi(n)$
3. if $x, y, z \in V(T)$ and y lies on the path from x to z then $\chi(x) \cap \chi(z) \subseteq \chi(y)$.

The width $width(T)$ of a tree decomposition T is $\max_{n \in V(T)} (|\chi(n)|) - 1$. The tree width of a graph is the *minimal width* over all tree decompositions of the graph.

!!!Example (can take one from the visualizations) also in [Fic19] page 169

2.5. Courcelle's Theorem

Every graph property definable in monadic second-order logic (MSO) is decidable in linear time on graphs of bounded tree-width.

Courcelle, Bruno (1990)¹

For all $k \in \mathbb{N}$ and MSO-sentences F is the decision problem for a given graph G , whether $G \models F$ is true, in time $2^{p(tw(G))} \cdot |G|$ with a polynom p decidable.

- *drawback*: still expensive ($2^{p(tw(G))}$, $2^{2^{(\#Q)}}$, large constants)

The workflow then looks like we see in figure 1.

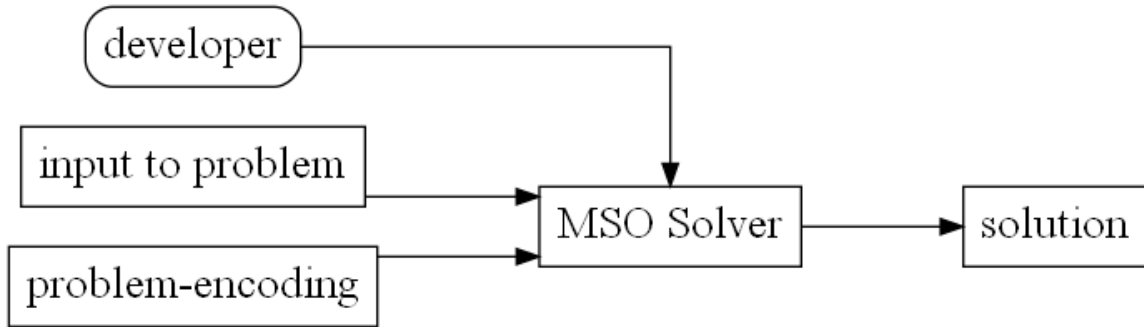


Figure 1: Implementation of the theorem

¹Courcelle, Bruno "The monadic second-order logic of graphs. I. Recognizable sets of finite graphs", Information and Computation, 85 (1990) no. 1: 12-75

3. Concept

We did setup a board with <https://trello.com> to track the progress and gather information connected to the project. Discussion and problems were mostly discussed with a dedicated <https://slack.com/intl/en-de/> in the *Collaborations Parameterized Algorithms and Complexity* team.

Research: language (python - explain) graph-construction (graphviz vs networkX), examples (diploma at first).

My previous experience connected to this work mainly stemmed from these two very good courses:

- Visualization with python from the lecture "Computational Physics" by Prof. Dr. A. Bäcker, chair of computational physics, TU Dresden 2016
- algorithms and various manipulations on graphs from the lecture "Graph Data Management and Analytics" by Hannes Voigt. [VK19]

The nodes in the dot-language are *labeled*, so creating a node takes one string identifier and can additionally be provided a string label. Valid examples for IDs include: a, b, A1, node1. The complete abstract grammar for DOT can be viewed at the DOT language.

It supports directed (*digraph* with edges indicated by '*-i*') an undirected (*graph* with edges indicated by '*--*') graphs. The visualizations presented here are constructed as undirected graphs, but would be easily extendable to directed representations since almost all operations keep the order of edge-endpoints given as input.

Another concept utilized were the sub-graphs and clusters available in DOT. To get a well structured (bipartite) incidence graph, each partition is placed in an individual cluster and sorted by node-label to easier find single nodes in potentially large clusters.

4. My Visualization Project

Python because: Rich dependency environment. Fast prototyping. Simple tooling for debugging (pdb), static analysis (mypy), code-style (pylint, autopep8), packaging (pip, pypi).

Python 3.8 because: Python 3.8 was the newest python version at the beginning of the project, released on October 14th 2019. The change applied most times in this project would be f-string support for shorter and easier to read string-building - for a longer list see summary of release highlights.

The development process was for most parts of the final software driven by evolutionary prototyping with the help of small and well understood examples such as 10. It helped to understand the possibilities of visualization in this domain and gather user input and requirements early [Ove91]. Some artifacts of the early prototypes with different graph-description languages can be still seen in the class *Graphoutput* in 5.0.1.

The first steps were in <https://github.com/VaeterchenFrost/gpusat-VISU> and the first releases of the source code outsourced to <https://github.com/VaeterchenFrost/tdvisu>

The objective of this project was/is to support the visualization mainly to document and improve the development efforts of dynamic programming on tree decompositions.

The tree decompositions in every tested application were provided by the utility <https://github.com/mabseher/htd> (small but efficient C++ library for computing (customized) tree and hypertree decompositions).

4.1. Commandline and Configuration

The *tdvisu.visualization* expects the command line parameters in a format described by table 1.

Table 1: Usage visualization.py

[-h] [--version] [--loglevel LOGLEVEL] [infile] outfolder	
infile=stdin	Input file for the visualization must conform with the JsonAPI.md
outfolder	Foldername to output the visualization results to
--loglevel	set the minimal loglevel for the root logger
--version	show program's version number and exit
-h, --help	show the help message and exit

We see that this input is very simple, and that the heavy lifting is done with the input file given in *infile*.

One extra possibility for configuration comes with the method **logging_cfg** from *tdvisu.utilities*. There are two example configurations provided with our project, one in the .yml, one in the .ini format. The implementation is very flexible in detecting which parser has to be applied - either via a dictionary-like or a configuration-like function.

Both possibilities are documented in python's logging configuration.

Our default configuration in `tdvisu/logging.yml` and `tdvisu/logging.ini` provides one handler, two formatters and six loggers.

The **handler** is a stream handler to `sys.stdout` with level *WARNING* and the the 'full'-formatter to format messages.

The **full-formatter** includes the full date and time up to milliseconds. After that we can expect the logging-level, filename and line where it was generated, and the message itself.

The **loggers** we use in our project are located in

- root, level: *WARNING*
- `visualization.py`, *NOTSET*
- `svgjoin.py`, *NOTSET*
- `reader.py`, *NOTSET*
- `construct_dpdb_visu.py`, *NOTSET*
- `utilities.py`, *NOTSET*

and can be individually customized using one configuration file. With the command line parameter *--loglevel* we can modify the level of *root* and it's associated handlers.

4.2. Initialization and Tree Decomposition

After the configuration we instantiate a Visualization object as shown in listing 1 , which parses the VisualizationData with the help from our `inspect_json` method.

The main purpose of the initialization is parsing the input file containing visualization information. This is encapsulated in *read_json*.

Next we want to extract information into two places:

- the instance variables
 - *timeline*, describing the time steps on the tree decomposition
 - *tree_dec*, describing the TD itself
 - *bagpre*, *joinpre*, *solpre* and *soljoinpre* as names for different nodes in the produced visualization
- *VisualizationData* containing the data for
 - IncidenceGraphData in listing 3
 - GeneralGraphData in 4
 - SvgJoinData in 9
 - adjustable parameters affecting the visuals of the visualization

Listing 1: Initializing a Visualization object

```

1 def __init__(self, infile, outfolder) -> None:
2     """Copy needed fields from arguments and create VisualizationData."""
3
4     self.data: VisualizationData = self.inspect_json(infile)
5     self.outfolder = outfolder
6
7     self.tree_dec_digraph = None
8
9 def inspect_json(self, infile) -> VisualizationData:
10    """Read and preprocess the needed data from the infile into VisualizationData."""
11
12    LOGGER.debug("Reading from: %s", infile)
13    visudata = read_json(infile)
14    LOGGER.debug("Found keys: %s", visudata.keys())
15
16    try:
17        _incid = visudata['incidenceGraph']
18        _general_graph = visudata['generalGraph']
19        _svg_join = visudata.get('svg_join', None)
20
21        incid_data: IncidenceGraphData = None
22        if _incid:
23            _incid['edges'] = [[x['id'], x['list']]]
24            for x in _incid['edges']:
25                incid_data = IncidenceGraphData(**_incid)
26            visudata.pop('incidenceGraph')
27        general_graph_data: GeneralGraphData = None
28        if _general_graph:
29            general_graph_data = GeneralGraphData(**_general_graph)
30            visudata.pop('generalGraph')
31        svg_join_data: SvgJoinData = None
32        if _svg_join:
33            svg_join_data = SvgJoinData(**_svg_join)
34            if 'svg_join' in visudata:
35                visudata.pop('svg_join')
36
37        self.timeline = visudata['tdTimeline']
38        visudata.pop('tdTimeline')
39        self.tree_dec = visudata['treeDecJson']
40        self.bagpre = self.tree_dec['bagpre']
41        self.joinpre = self.tree_dec.get('joinpre', 'Join%d~%d')
42        self.solpre = self.tree_dec.get('solpre', 'sol%d')
43        self.soljoinpre = self.tree_dec.get('soljoinpre', 'solJoin%d~%d')
44        visudata.pop('treeDecJson')

```

```

46 except KeyError as err:
47     raise KeyError(f"Key_{err}_not_found_in_the_input_json.")
48 return VisualizationData(incidence_graph=incid_data,
49                           general_graph=general_graph_data,
50                           svg_join=svg_join_data,
51                           **visudata)

```

Listing 2: SvgJoinData

```

1 @dataclass
2 class SvgJoinData:
3     """Class holding different parameters to join the results."""
4     base_names: Union[str, Iterable[str]]
5     folder: Optional[str] = None
6     outname: str = 'combined'
7     suffix: str = '%d.svg'
8     preserve_aspectratio: str = 'xMinYMin'
9     num_images: int = 1
10    padding: Union[int, Iterable[int]] = 0
11    scale2: Union[float, Iterable[float]] = 1.0
12    v_top: Union[None, float, str,
13                Iterable[Union[None, float, str]]] = 'top'
14    v_bottom: Union[None, float, str,
15                   Iterable[Union[None, float, str]]] = None

```

Listing 3: IncidenceGraphData

```

1 @dataclass
2 class IncidenceGraphData:
3     """Class holding different parameters for the incidence graph."""
4     edges: list
5     subgraph_name_one: str = 'clauses'
6     subgraph_name_two: str = 'variables'
7     var_name_one: str = ''
8     var_name_two: str = ''
9     infer_primal: bool = False
10    infer_dual: bool = False
11    primal_file: str = 'PrimalGraphStep'
12    inc_file: str = 'IncidenceGraphStep'
13    dual_file: str = 'DualGraphStep'
14    fontsize: int = 16
15    penwidth: Union[float, str] = 2.2
16    second_shape: str = 'diamond'
17    column_distance: float = 0.5

```

Listing 4: GeneralGraphData

```

1 @dataclass

```

```

2 class GeneralGraphData:
3     """Class holding different parameters for the general graph."""
4     edges: list
5     extra_nodes: Optional[list] = None
6     graph_name: str = 'graph'
7     file_basename: str = 'graph'
8     var_name: str = ''
9     sort_nodes: bool = False
10    need_adj_nodes: bool = False
11    fontsize: int = 20
12    first_color: str = 'yellow'
13    first_style: str = 'filled'
14    second_color: str = 'green'
15    second_style: str = 'dotted,filled'

```

Next we call the method *Visualization.tree_dec_timeline* that will start the visualization. First it does a quick setup for a directed graph that

- is *strict*, meaning a simple graph where equal edges are merged into one
- has an orientation where it grows with each "rank" of the nodes
- has a shape and a fill-color for it's nodes
- has a margin around it's bounding box.

Secondly it creates the basic bag-structure adding nodes and edges for all bags of the provided tree decomposition.

Now comes the heavy lifting when it iterates over the timeline, adding provided solutions and edges connecting those to the existing bags. We do this in two cycles, one to layout all nodes into their final position, and another one to create the final time-step images. A special case occurs when joining two solved bags into a new one. In this case we basically remove old connections between the children and the parent node, insert the join-result into the graph and add connections from children to the join-result and from the join-result to the parent. Details for this function can be viewed in listing 7.

!!! Example !!!

The second run iterates backwards over all timesteps to hide later timesteps and emphasize the current node. When rendering the graphs there is an added option to automatically *view* the result (disabled by default). Details for this function can be viewed in listing 8.

4.3. Create time steps for the underlying graph

To get a more comprehensive insight into the solving process we decided to also highlight the parts of graphs that best describe the problem instance the solver worked on.

Because the data in the API does not directly include details about highlights in those graphs, we will construct this information on the fly.



Figure 2: Disconnected (dual) graph

First we select only bag ids from the timeline provided that represent an IF-operation. With additional data from *IncidenceGraphData* we are able to reconstruct the

- incidence graph,
- primal graph,
- dual graph

for Boolean formulas. With input from *GeneralGraphData* we can construct a simple graph that should include the nodes we find in the bags of the TD.

Because graph representations of Boolean formulas are not necessarily connected, we make sure to include potentially isolated nodes into the graph as well. For example the formula $(\neg a \vee \neg b \vee \neg c \vee \neg d) \wedge (b \vee c \vee d) \wedge g$ with its set of clauses $\{c_1 = \{-a, -b, -c, -d\}, c_2 = \{b, c, d\}, c_3 = \{g\}\}$ will create the dual graph 2. This happens with no pre-processing and if the variable g is only included in the unit c_3 .

4.4. Incidence Graph

The incidence graph is a bipartite graph that we present in a way that creates a one to one correspondence with the Boolean formula it does represent. For an example of an incidence graph visualization see 11

This bipartite graph is prepared with good default values, but is customizable in many parameters. Those values are:

1. *colors*, an iterable of colors that is used to color different nodes
2. *inc_file*, basis for the file created that gets appended with the step number
3. *view*, could automatically open the generated files with the default program
4. *fontsize*, the size of all text in this graph
5. *penwidth*, width of the lines around nodes
6. *basefill*, filling of the background for nodes
7. *shdshape*, shape of the nodes with variables

8. *neg_tail*, the shape of the edge-tail indicating a negated variable
9. *var_name_one(/two)*, prefix for nodes in the left (right) partition
10. *column_distance*, the distance between both partitions

We create the graph, add the necessary arguments and two sub-graphs. The first subgraph is called *cluster_clause* with it's label *clauses*. We add the clauses with their clause-ids starting at one sorted in ascending order from top to bottom.

The second sub-graph we call *cluster_ivar* labeled *variables* gets all variables added to it, starting from variable-id one. This sub-graph does get the different provided *colors* applied to its nodes and their adjacent edges.

The last step in this method is the highlighting of "active" parts in each time step beeing processed during it's dynamic programming. To accomplish this with as small overhead as possible, we apply and remove additional lines to the body of its graph source code. For highlighting there are two main cases:

- There is no active clause in this step: we only reset highlighting
- Else: we also create new highlighting for clauses, variables and edges

In each case we create one image after the step to provide the inside generated.

4.5. General Graph

The so called "general graph" can represent the underlying graph for different problems, as well as primal and dual graph for Boolean formulas. Because of its larger area of application the general graph was not as easy to layout as the incidence graph. We did prepare two different layouts that should cover most cases and are toggled by the parameter *do_sort_nodes*. For smaller and dense graphs of up to 20 vertices it might be helpful to sort the nodes on a circle, while for larger or sparse graphs an organic layout may be more appropriate.

To layout these two options we chose the engine

- *do_sort_nodes* true: circo (see [ST99])
- *do_sort_nodes* false: sfdp (see [Hu05]) with the spring constant 'K' in virtual physical model set to 2.

Additional parameters used in both layouts are set to: not overlap nodes to easily identify each node, and draw the edges first. This should provide a minimally cluttered layout compared to the defaults, but could make edges ambiguous in some cases. Of course these layouts could use even more configuration than what was set for this version, a complete overview is provided in the graphviz-doc.

Only if the option to sort the nodes was chosen with *do_sort_nodes* the method

1. saves the current graph source

2. sets the layout engine to *circo*
3. adds edges between successive node-ids to form a closed circle
4. runs the layout and reads back the output in plain dot-format
5. reads the calculated positions for each node in the graph
6. resets the source to step one, removing all temporary additions
7. writes the calculated positions into each node
8. sets the layout engine to an engine that uses those calculated positions later.

We add the edges, and eventually the isolated nodes also, to the graph. Then the highlighting for each time-step is done basically like in the incidence graph 4.4. We allow one additional option that would depend on the concrete algorithm being visualized, and that is *do_adj_nodes*. In case the algorithm uses adjacent nodes they can be visualized with this flag using a third color.

EXAMPLES

In each case we create one image after the time step to provide the inside generated.

4.6. Joining SVG

Joining each time step into one image Once all user defined images for one timeline are created, it would be nice to have only one file for every step. To support this functionality and some basic scaling and adjusting, there is a special key in the API for joining the svg-graphs. The functionality is placed in the file *svgjoin.py* and will be called with the specifications given in the optional dictionary **svgjoin** within the JsonAPI.

We transform this information into the python *dataclass* **SvgJoinData** 9. The internally used method *svgjoin.append_svg* joins two images horizontally in each step. With default settings it will align the top of both images and apply no scaling to either of them. The possible parameters (in [unit])

- centerpad: float = 0, [image coordinates], just "padding" in the JSON API
- v_bottom: float = None, [size of the *first* image]
- v_top: float = None, [size of the *first* image]
- scale2: float = 1, [size of the *second* image]

allow flexible and easy to use vertical, horizontal and scaling transformations. Note that the images are placed in a Cartesian coordinate system and its origin is the top left corner of its bounding box. All images fill a rectangle in this coordinate system with height and width respectively.

Since the order of the parameters v_bottom and v_top could be confused due to the coordinate system, we make sure to correctly set v_top to the smaller and v_bottom to the larger one if this is possible.

One special case is achieved by setting both these parameters to the same number. Then they are interpreted as the position of the vertical centerline for the second image in units of the first. So setting both parameters to $\frac{1}{2}$ would result in centering both images vertically.

Possibilities for joining images with these four parameters include:

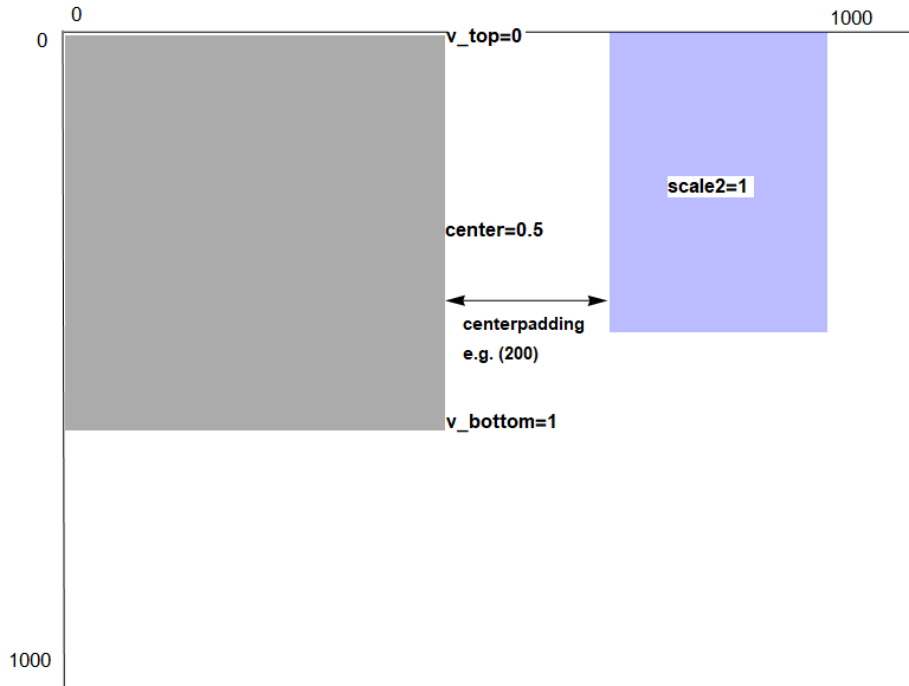


Figure 3: Joining the blue (right side) image to the left gray image with only one parameter $centerpad$ set to 200. We see the default vertical position $v_top=0$, and the implied coordinate system with an origin in the top left corner.

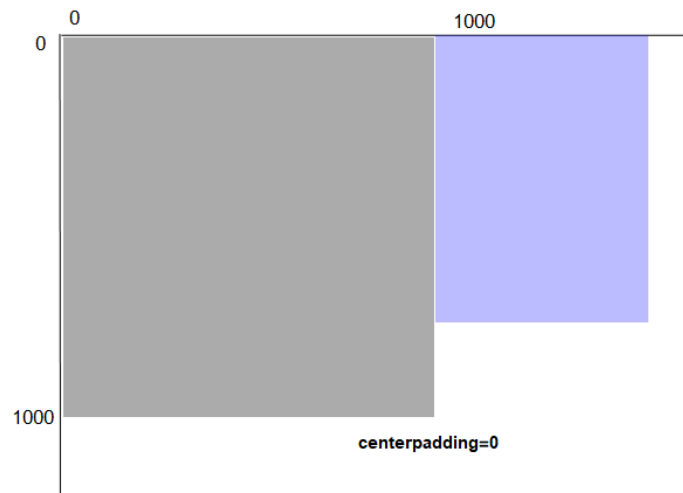


Figure 4: Example for joining with no *centerpad*.

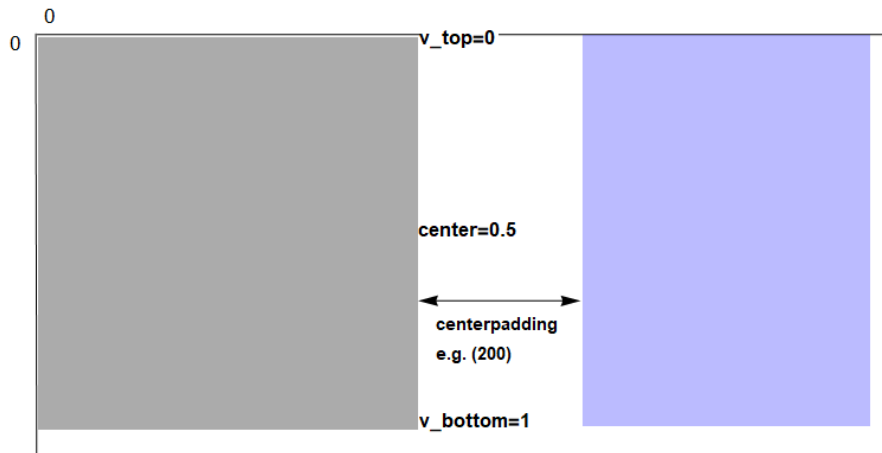


Figure 5: The second image gets scaled to the same size as the first image. This can be conveniently achieved by setting *v_top* to 0 and *v_bottom* to 1. Parameter *centerpad* is 200 as hinted.

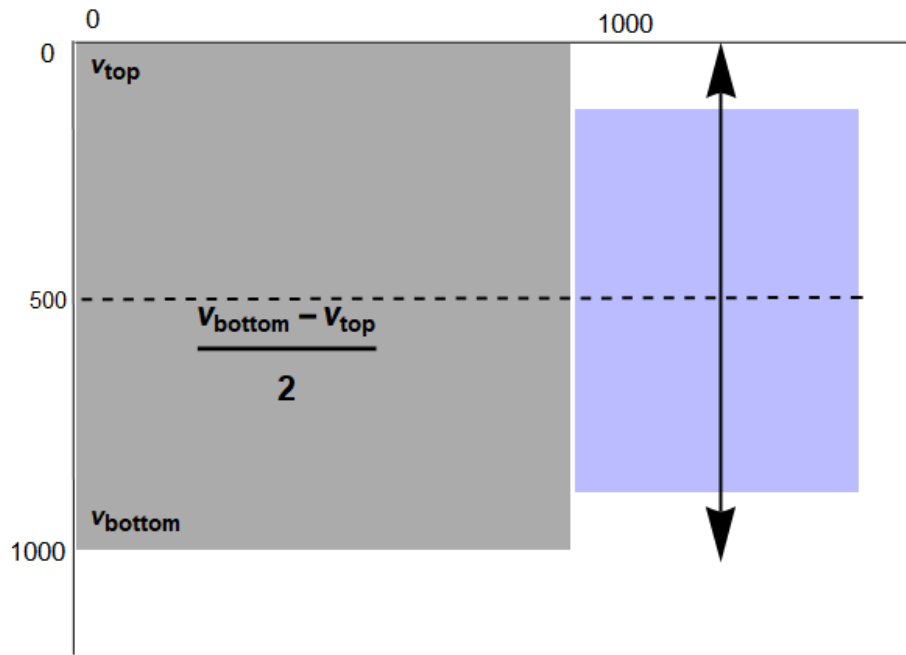


Figure 6: Aligning both images to be vertically centered.
This can be achieved by setting $v_{\text{bottom}} = v_{\text{top}} = 0.5$.

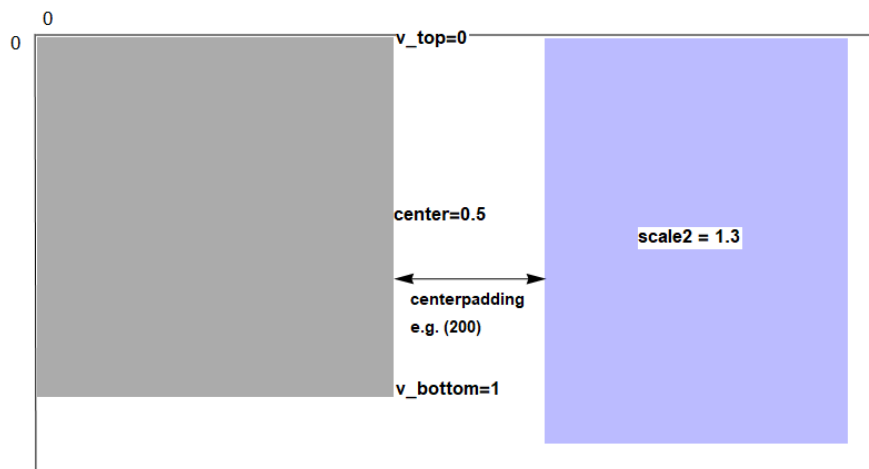


Figure 7: Setting scale2 to 1.3 to scale the blue (right) image uniformly. Parameter centerpad is 200 as hinted.

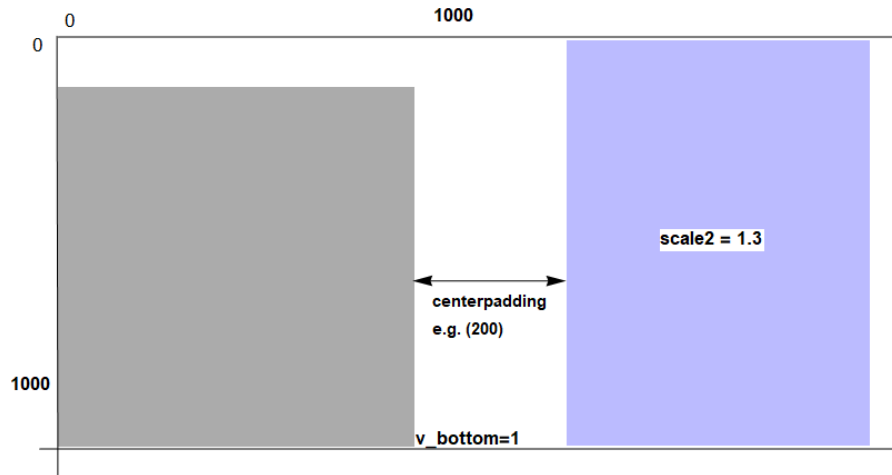


Figure 8: As in figure 7 we use *scale2* to scale the blue rectangle. To align both images at the bottom edge, we use the value $v_bottom = 1$.

5. Integration in GPUSAT

To study and improve the handling of the C++ program was chronologically the first task I experimented with. Getting the program up and running proved to be more difficult than we envisioned due to a probable bug in the driver when running OpenCL Drivers from CUDA on the Windows OS.

Impact on performance: Utilizing small classes and streams we tried to keep the impact on performance during the solving process low. However running on the same thread especially for larger problem instances

Some non-functional changes made to the source were

- a) some adjustments to satisfy the local compiler (shortening kernel string, replacing *'and'* with *'&&'*)
- b) some explicit casts
- c) fixed documentation of command line arguments

The functional changes were:

1. allow tabs instead of spaces in input files
2. output more information about the hardware used (*device_query*)
3. add verbose output globally toggled by a flag
4. decide on https://en.wikipedia.org/wiki/DOT_%28graph_description_language%29 as the intermediate format for storing graphs.
5. start collecting information that might be needed for a visualization *graphfile* for saving the decomposition graph
6. add *graphout* to solver flow to get automated insight into the structure of a run.
7. add function *solutiontable* to extract tables of variable assignments as a string
8. add labels to each node (bags and solutions at this point)
9. encapsulating the previous functions into *gpusat::Graphoutput* class and instantiate it in main.
10. using the class functionality in the Solver
11. changing enum to the scoped enum class for better encapsulation and strongly typed.
12. with inlining *gpusatutils* the current functionality of creating raw dot was completed.

13. Experimented with Neo4j, but found the visualization in particular not that presentable. The functionality to create cypher-queries for the SAT formula with primal, incidence and dual graph is still present in the class.
14. The functionality to create the cypher-query for the graph of the tree-decomposition was added.
15. Rename *visualisierung* into *visualization*
16. Using JsonCPP for processing and formatting json objects in C++
17. Setting format to BasedOnStyle: LLVM, UseTab: Never, IndentWidth: 4, TabWidth: 4, ColumnLimit: 0
18. Creating a *Grid* class for efficiently storing unsigned integer values in a two-dimensional structure based on ideas from this thread
19. create guide for remote development with *Visual Code*
20. Converted intermediate string operations to string-streams instead of files
21. Updated README.md
22. Added Doxygen for docbook, html, latex

Programm <https://github.com/VaeterchenFrost/GPUSAT>

Differences: <https://github.com/daajoe/GPUSAT/compare/master...VaeterchenFrost:master> Commits 142 Files changed 94 Nagoya talk: Graphs for performance are Ordered by used time per algorithm - gpusat quite good

Working with cmake remotly. ssh @(sg1.)dbai.tuwien.ac.at CPU branch wasn't working. Only AMD/Nvidia graphics with respective flags.

Manual configuration with the include options from cmake in CMakeLists.txt or with help from <https://marketplace.visualstudio.com/items?itemName=ms-vscode.cmake-tools> to set up for the (potentially remote) environment.

-
- Options:

Table 2: Usage: ./gpusat [OPTIONS]

-s, --seed INT	number used to initialize the pseudorandom number generator
-f, --formula TEXT	path to the file containing the sat formula
-d, --decomposition TEXT	path to the file containing the tree decomposition
--CPU	run the solver on a cpu

<code>--NVIDIA</code>	run the solver on an NVIDIA device
<code>--AMD</code>	run the solver on an AMD device
<code>--weighted</code>	use weighted model count
<code>--noExp</code>	don't use extended exponents
<code>-v, --verbose</code>	print additional program information
<code>-p, --nopreprocess</code>	skips the preprocessing step for debugging and visualization-purposes
<code>-w, --combineWidth INT=20</code>	maximum width to combine bags of the decomposition
<code>-g, --graph TEXT</code>	filename for saving the decomposition graph
<code>--visufile TEXT</code>	filename for saving the visualization file

An example call with `./gpusat -f ../examples/test_da4_1.cnf -v -p -d ../examples/td4p1.txt -g ../examples/graphfileda41.txt --visufile ../examples/visufileda41.json` enabled verbose output, disabled pre-processing to prevent the creation of bags with too many variables at once to be visualized, and creates full visualization output. The console output produced by this example call is listed in 14.

5.0.1. Class Graphoutput

First steps to automatically visualize the tree decomposition of the solving process with its solutions. Outputs a graph specified in gml[Him10] (Graph Modeling Language). For our example for #SAT 13 with the bags and respective solutions as nodes connected to the bag they solve.

Two additional functions generate a Neo4j Cypher query with:

- one graph representing the SAT formula and queries to construct incidence, dual and primal representations. output as `satFile = "cypherSatFormula.txt"`
- one graph representing the tree decomposition of the primal graph with it's bags containing variables. output as `tdFile = "cypherTreedec.txt"`

5.0.2. Class SolverVisualization

To include the extraction of all necessary visualization information into the solver I created a separate fork. To simplify the creation of valid json I selected the actively developed c++ library JsonCpp <https://github.com/open-source-parsers/jsoncpp> version 1.9.2 from the open-source-parsers repository.

6. Integration in dpdb

The integration of the API with dpdb was easier to implement after the solving process instead of hooking into the solving, provided that all necessary information got persisted in the database. The integration is included in the TDVisu project as a separate python file. A complete workflow can be accomplished using the arguments

- `--store-formula` as a problem specific option for Sat and SharpSat
- `--gr-file GR_FILE` for problems like VertexCover with graph input

when calling `dpdb.py`

The integration for SharpSat was the first implemented in the file `construct_dpdb_visu.py` with the main parameters

- **problemnumber** the problem-id to select in the database
- **--twfile** TWFILE tw-file containing the edges of the graph
- **--outfile** OUTFILE file to write the output to, default `'dbjson%d.json'`
- **--loglevel** LOGLEVEL set the minimal loglevel for the root logger
- **--pretty** pretty-print the JSON
- **--inter-nodes** Calculate and animate the shortest path between successive bags in the order of evaluation. To accomplish this task, an efficient implementation of the bidirectional Dijkstra's algorithm [Gol+06] based on the implementation by NetworkX [HSS08] in `bidirectional_dijkstra`. in our case the weight function is always one, as the edges have no weight associated with them.

After the arguments are parsed by python's `argparse` it is possible to adjust logging output by either providing a configuration file (template provided) or giving a minimal logging level per program argument.

!!! Database Config!!!

Next the `create_json` function connects to the database driver with the number of the stored problem. The "problem type" is available as a string in table `public.problem`, and the appropriate class to prepare the json will be instantiated. At this time the solver handles the problems of *satisfiability* (Sat), *count solutions to a Boolean formula* (SharpSat) as well as *minimum vertex cover* (VertexCover).

Beispiel

7. Application and Images

8. Summary and Outline

What is achieved?

What worked good, what bad?

A. Images

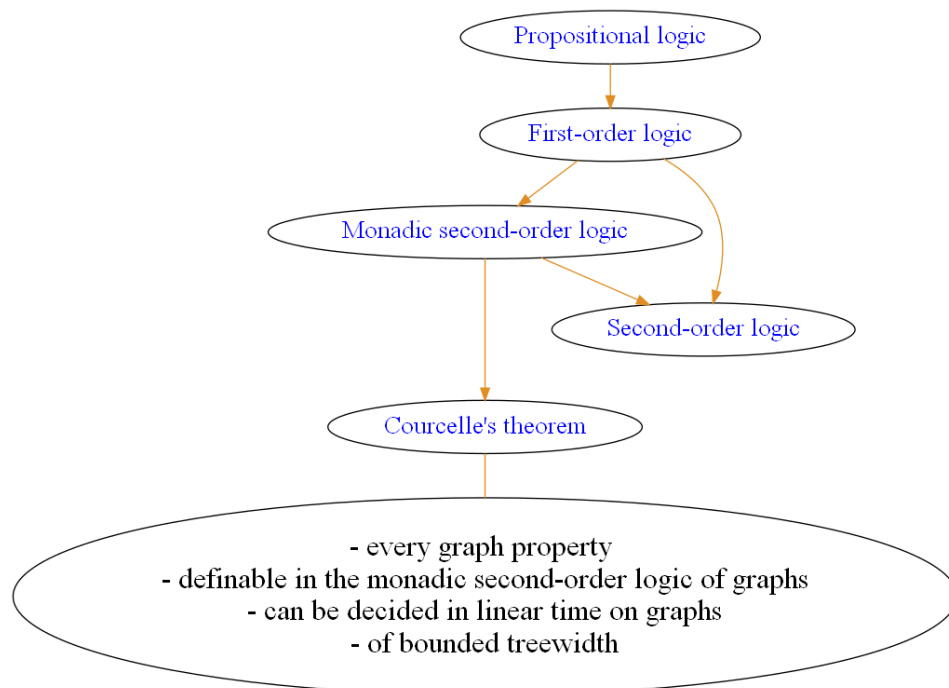


Figure 9: From propositional logic to monadic second order logic and Courcelle's Theorem

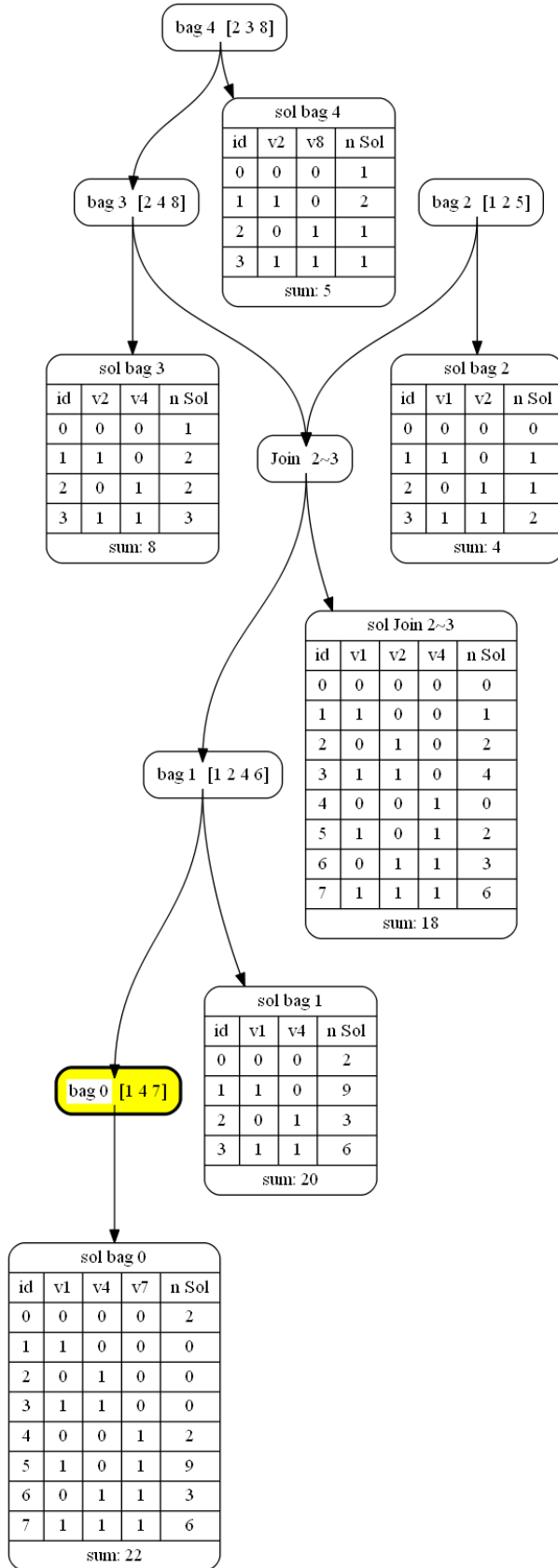


Figure 10: Created scalable-vector-graphic directly from 13

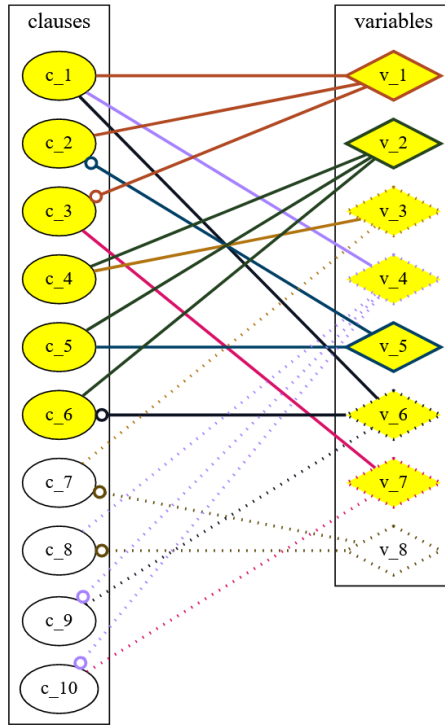


Figure 11: Example for an incidence graph from example 4.1

B. Code Snippets

Listing 5: The JSON format used to describe MSOL visualization on tree decompositions

```
1 {
2   "incidenceGraph" : false or
3   {
4     Optional("subgraph_name_one" : STR, default='clauses'),
5     Optional("subgraph_name_two" : STR, default='variables'),
6
7     Optional("var_name_one" : STR, default=''),
8     Optional("var_name_two" : STR, default=''),
9
10    Optional("infer_primal" : BOOLEAN, default=false),
11    Optional("infer_dual" : BOOLEAN, default=false),
12    Optional("fontsize" : INT, default=16),
13    Optional("second_shape" : STR, default='diamond'),
14    Optional("column_distance" : FLOAT, default=0.5),
15
16    "edges" : [
17      {"id" : INT (subgraphOneId),
18       "list" : [INT...]}
19    ]
20  },
21
22  "generalGraph" : false or
23  {
24    Optional("graph_name" : STR, default='graph'),
25    Optional("var_name" : STR, default=''),
26    Optional("sort_nodes" : BOOLEAN, default=false),
27    Optional("need_adj_nodes" : BOOLEAN, default=false),
28    Optional("extra_nodes" : LIST, default=[]),
29    Optional("fontsize" : INT, default=20),
30    Optional("first_color" : STR/COLOR, default='yellow'),
31    Optional("first_style" : STR, default='filled'),
32    Optional("second_color" : STR/COLOR, default='green'),
33    Optional("second_style" : STR, default='dotted,filled'),
34
35    "edges" : [
36      [INT, INT],
37      ...
38    ]
39  },
40
41  "tdTimeline" :
```

```

44  [
45      [INT (bagId)] or
46      [INT (bagId) or [INT(bagId), INT(bagId)],
47          [[
48              [Any],
49              [Any],
50              ...
51          ]
52          ,STR (header)
53          ,STR (footer)
54          ,BOOL (transpose)
55      ]
56  ]
57  ...
58 ],
59
60 "treeDecJson" :
61 {
62     "bagpre" : STR,
63     "num_vars" : INT,
64     Optional("joinpre" : STR, default= 'Join %d~%d'),
65     Optional("solpre" : STR, default= 'sol%d'),
66     Optional("soljoinpre" : STR, default= 'solJoin%d~%d'),
67
68     "edgearray" :
69         [[INT, INT]...],
70     "labeldict" :
71         [
72             {
73                 "id" : INT (bagId),
74                 "items" : [ INT... ],
75                 "labels" : [ STR... ]
76             }
77             ...
78         ],
79 },
80
81 Optional("orientation" : Any['BT', 'TB', 'LR', 'RL'] , default='BT'),
82 Optional("linesmax" : INT, default=100),
83 Optional("columnsmax" : INT, default=20),
84 Optional("bagcolor" : STR, default='white'),
85 Optional("fontsize" : INT, default=20),
86 Optional("penwidth" : FLOAT, default=2.2),
87 Optional("fontcolor" : STR, default='black'),
88
89 Optional("emphasis" : DICT, default=

```



```

90     {
91         "firstcolor" : STR/COLOR, default='yellow',
92         "secondcolor" : STR/COLOR, default='green',
93         "firststyle" : STR, default='filled',
94         "secondstyle" : STR, default='dotted,filled'
95     }
96 )
97
98 Optional("svgjoin" :
99     {
100         "base_names" : [STR],
101         Optional("folder" : STR/NULL, default=null),
102         Optional("outname" : STR, default='combined'),
103         Optional("suffix" : STR, default='%d.svg'),
104         Optional("preserve_aspectratio" : STR, default='xMinYMin'),
105         Optional("num_images" : INT, default=1),
106         Optional("padding" : [INT], default=0),
107         Optional("scale2" : [FLOAT], default=1),
108         Optional("v_top" : [FLOAT/STR], default='top'),
109         Optional("v_bottom" : [FLOAT/STR]/NULL, default=null),
110     }
111 )
112 }

```

Listing 6: Construct_dpdb_visu.py

```

1 def create_json(problem: int, tw_file=None, intermed_nodes=False):
2     """Create the JSON for the specified problem instance."""
3     with connect() as connection:
4         # get type of problem
5         with connection.cursor() as cur:
6             query = """SELECT name,type,num_bags
7             FROM public.problem WHERE id=%s"""
8             cur.execute(query, (problem,))
9             (name, ptype, num_bags) = cur.fetchone()
10
11         constructor: IDpdbVisuConstruct
12         if ptype == 'SharpSat':
13             constructor = DpdbSharpSatVisu(
14                 connection, problem, intermed_nodes)
15         elif ptype == 'VertexCover':
16             constructor = DpdbMinVcVisu(
17                 connection, problem, intermed_nodes, tw_file)
18         return constructor.construct()
19     return {}

```

Listing 7: forward_iterate_tdg

```

1 def forward_iterate_tdg(self, joinpre, solpre, soljoinpre) -> None:
2     """Create the final positions of all nodes with solutions."""
3     tdg = self.tree_dec_digraph # shorten name
4
5     for i, node in enumerate(self.timeline): # Create the positions
6         if len(node) > 1:
7             # solution to be displayed
8             id_inv_bags = node[0]
9             if isinstance(id_inv_bags, int):
10                 last_sol = solpre % id_inv_bags
11                 tdg.node(last_sol, solution_node(
12                     *(node[1])), shape='record')
13                 tdg.edge(self.bagpre % id_inv_bags, last_sol)
14
15             else: # joined node with 2 bags
16                 suc = self.timeline[i + 1][0] # get the joined bags
17
18                 LOGGER.debug('joining %s to %s', node[0], suc)
19
20                 id_inv_bags = tuple(id_inv_bags)
21                 last_sol = soljoinpre % id_inv_bags
22                 tdg.node(last_sol, solution_node(
23                     *(node[1])), shape='record')
24
25                 tdg.edge(joinpre % id_inv_bags, last_sol)
26                 # edges
27                 for child in id_inv_bags: # basically "remove" current
28                     tdg.edge(
29                         self.bagpre % child
30                         if isinstance(child, int) else joinpre % child,
31                         self.bagpre % suc
32                         if isinstance(suc, int) else joinpre % suc,
33                         style='invis',
34                         constraint='false')
35                 tdg.edge(self.bagpre % child if isinstance(child, int)
36                         else joinpre % child,
37                         joinpre % id_inv_bags)
38                 tdg.edge(joinpre % id_inv_bags, self.bagpre % suc
39                         if isinstance(suc, int) else joinpre % suc)

```

Listing 8: backwards_iterate_tdg

```

1 def backwards_iterate_tdg(self, joinpre, solpre, soljoinpre,
2     view=False) -> None:
3     """Cut the single steps back and update emphasis accordingly."""
4     tdg = self.tree_dec_digraph # shorten name

```

```

5  last_sol = ""
6
7  for i, node in enumerate(reversed(self.timeline)):
8      id_inv_bags = node[0]
9      LOGGER.debug("%s: Reverse traversing on %s", i, id_inv_bags)
10
11     if i > 0:
12         # Delete previous emphasis
13         prevhead = self.timeline[len(self.timeline) - i][0]
14         bag = (
15             self.bagpre %
16             prevhead if isinstance(
17                 prevhead,
18                 int) else joinpre %
19                 tuple(prevhead))
20         base_style(tdg, bag)
21         if last_sol:
22             style_hide_node(tdg, last_sol)
23             style_hide_edge(tdg, bag, last_sol)
24             last_sol = ""
25
26     if len(node) > 1:
27         # solution to be displayed
28         if isinstance(id_inv_bags, int):
29             last_sol = solpre % id_inv_bags
30             emphasise_node(tdg, last_sol)
31             tdg.edge(self.bagpre % id_inv_bags, last_sol)
32         else: # joined node with 2 bags
33             id_inv_bags = tuple(id_inv_bags)
34             last_sol = soljoinpre % id_inv_bags
35             emphasise_node(tdg, last_sol)
36
37     emphasise_node(tdg,
38         self.bagpre %
39         id_inv_bags if isinstance(id_inv_bags, int) else
40         joinpre % id_inv_bags)
41     _filename = self.outfolder + self.data.td_file + '%d'
42     tdg.render(
43         view=view, format='svg', filename=_filename %
44         (len(self.timeline) - i))

```

Listing 9: SvgJoinData

```

1  @dataclass
2  class SvgJoinData:
3      """Class for holding different parameters to join the results."""
4      base_names: Union[str, Iterable[str]]

```

```

5  folder: Optional[str] = None
6  outname: str = 'combined'
7  suffix: str = '%d.svg'
8  preserve_aspectratio: str = 'xMinYMin'
9  num_images: int = 1
10 padding: Union[int, Iterable[int]] = 0
11 scale2: Union[float, Iterable[float]] = 1.0
12 v_top: Union[None, float, str,
13             Iterable[Union[None, float, str]]] = 'top'
14 v_bottom: Union[None, float, str,
15                Iterable[Union[None, float, str]]] = None

```

C. Input Examples

Listing 10: Edge encoding of example graph with 16 vertices

```

p tw 16 36
1 2
2 1
2 3
3 2
3 4
4 3
3 5
5 3
4 5
5 4
4 6
6 4
6 7
7 6
7 8
8 7
8 9
9 8
9 10
10 9
9 11
11 9
11 12
12 11
12 13
13 12
12 14
14 12

```

```

11 14
14 11
14 7
7 14
6 15
15 6
15 16
16 15

```

Listing 11: CNF clauses from example 4.1 on page 27 [Zis18]

```

p cnf 8 10
1 4 6 0
1 -5 0
-1 7 0
2 3 0
2 5 0
2 -6 0
3 -8 0
4 -8 0
-4 6 0
-4 7 0

```

Listing 12: CNF clauses from random example with 12 units

```

p cnf 18 24
-1 0
-2 0
-3 0
-4 0
-5 0
-6 0
-7 0
-8 0
-9 0
-10 0
-11 0
-12 0
-13 -14 -15 0
-13 -14 16 0
-13 -15 -16 -18 0
-13 -15 -17 0
13 14 16 -17 18 0
13 15 -16 -18 0
-14 -15 16 17 0
-14 15 -17 18 0
-14 15 17 -18 0
-15 -16 -17 18 0

```

```
15 -16 -17 -18 0
15 16 17 -18 0
```

Listing 13: DOT source for visualization of example 4.1

```
strict digraph g41dot {
  node [fillcolor=white shape=box style="rounded,filled"]
  bag4 [label=<<TABLE BORDER="0" CELLBORDER="0" CELLSPACING="0">
    <TR><TD>bag 4</TD><TD PORT="anchor"></TD>
    <TD>[2 3 8]</TD></TR></TABLE>>]
  bag3 [label=<<TABLE BORDER="0" CELLBORDER="0" CELLSPACING="0">
    <TR><TD BGCOLOR="white">bag 3</TD><TD PORT="anchor"></TD>
    <TD>[2 4 8]</TD></TR></TABLE>>]
  join1 [label=<<TABLE BORDER="0" CELLBORDER="0" CELLSPACING="0">
    <TR><TD BGCOLOR="white">Join</TD><TD PORT="anchor"></TD>
    <TD>2~3</TD></TR></TABLE>>]
  bag2 [label=<<TABLE BORDER="0" CELLBORDER="0" CELLSPACING="0">
    <TR><TD BGCOLOR="white">bag 2</TD><TD PORT="anchor"></TD>
    <TD>[1 2 5]</TD></TR></TABLE>>]
  bag1 [label=<<TABLE BORDER="0" CELLBORDER="0" CELLSPACING="0">
    <TR><TD BGCOLOR="white">bag 1</TD><TD PORT="anchor"></TD>
    <TD>[1 2 4 6]</TD></TR></TABLE>>]
  bag0 [label=<<TABLE BORDER="0" CELLBORDER="0" CELLSPACING="0">
    <TR><TD BGCOLOR="white">bag 0</TD><TD PORT="anchor"></TD>
    <TD>[1 4 7]</TD></TR></TABLE>>]
  node [shape=record]
  sol2 [label="{sol bag 2|{{id|0|1|2|3}}|{v1|0|1|0|1}}|{v2|0|0|1|1}}
    |{n Sol|0|1|1|2}}|sum: 4}"]
  sol4 [label="{sol bag 4|{{id|0|1|2|3}}|{v2|0|1|0|1}}|{v8|0|0|1|1}}
    |{n Sol|1|2|1|1}}|sum: 5}"]
  sol3 [label="{sol bag 3|{{id|0|1|2|3}}|{v2|0|1|0|1}}|{v4|0|0|1|1}}
    |{n Sol|1|2|2|3}}|sum: 8}"]
  solJoin1 [label="{sol Join 2~3|{{id|0|1|2|3|4|5|6|7}}
    |{v1|0|1|0|1|0|1|0|1}}|{v2|0|0|1|1|0|0|1|1}}
    |{v4|0|0|0|0|1|1|1|1}}|{n Sol|0|1|2|4|0|2|3|6}}
    |sum: 18}"]
  sol1 [label="{sol bag 1|{{id|0|1|2|3}}|{v1|0|1|0|1}}|{v4|0|0|1|1}}
    |{n Sol|2|9|3|6}}|sum: 20}"]
  sol0 [label="{sol bag 0|{{id|0|1|2|3|4|5|6|7}}
    |{v1|0|1|0|1|0|1|0|1}}|{v4|0|0|1|1|0|0|1|1}}
    |{v7|0|0|0|0|1|1|1|1}}|{n Sol|2|0|0|0|2|9|3|6}}|sum: 22}"]
  bag4:anchor -> bag3:anchor
  bag2:anchor -> join1:anchor
  bag3:anchor -> join1:anchor
  join1:anchor -> bag1:anchor
  bag1:anchor -> bag0:anchor
  bag4:anchor -> sol4
```

```

bag3:anchor -> sol3
bag2:anchor -> sol2
bag1:anchor -> sol1
bag0:anchor -> sol0
join1:anchor -> solJoin1
bag0:anchor -> sol0
bag0 [fillcolor=yellow penwidth=2.5]
}

```

Listing 14: stdout of program gpusat with call `./gpusat -f ../examples/test_da4_1.cnf -v -p -d ../examples/td4p1.txt -g ../examples/graphfileda41.txt --visufile ../examples/visufileda41.json`

```

Seed: 1592417295
Platform - 1
  1.1 CL_PLATFORM_NAME: AMD Accelerated Parallel Processing
  1.2 CL_PLATFORM_VENDOR: Advanced Micro Devices, Inc.
  1.3 CL_PLATFORM_VERSION: OpenCL 2.1 AMD-APP (2671.3)
  1.4 CL_PLATFORM_PROFILE: FULL_PROFILE
  1.5 CL_PLATFORM_EXTENSIONS: cl_khr_icd cl_amd_event_callback
                             cl_amd_offline_devices
Device - 1:
  CL_DEVICE_NAME: Ellesmere
  CL_DEVICE_VENDOR: Advanced Micro Devices, Inc.
  CL_DRIVER_VERSION: 2671.3
  CL_DEVICE_VERSION: OpenCL 1.2 AMD-APP (2671.3)
  CL_DEVICE_MAX_COMPUTE_UNITS: 32
  CL_DEVICE_MAX_CONSTANT_BUFFER_SIZE : 3422266572
  CL_DEVICE_MAX_CONSTANT_ARGS : 8

-- treeDecomp Before --
bags: 5
0 : [1 4 7 ]-(1 )-
1 : [1 2 4 6 ]-(2 3 )-
2 : [1 2 5 ]()
3 : [2 4 8 ]-(4 )-
4 : [2 3 8 ]()

-- treeDecomp after preprocessFacts--
bags: 5
0 : [1 4 7 ]-(1 )-
1 : [1 2 4 6 ]-(2 3 )-
2 : [1 2 5 ]()
3 : [2 4 8 ]-(4 )-
4 : [2 3 8 ]()
---Determining datastructure---
input:

```

```

SOLUTIONTYPE : TREE
treeDecomp.width : 4
-----
Opened visualization with file ../examples/visufileda41.json true
-----
==> Entering solveProblem on id 0 <==
==> Entering solveProblem on id 1 <==
==> Entering solveProblem on id 2 <==
solveIF 1 + 0 => 2
    bag(2): bags= 0 , exp= 0 , correction= 0
    var= [1, 2, 5, ]
Solved IF-0 on node 2
    bag(2): bags= 1 , exp= 1 , correction= 0
    var= [1, 2, ]
==> Entering solveProblem on id 3 <==
==> Entering solveProblem on id 4 <==
solveIF 3 + 0 => 4
    bag(4): bags= 0 , exp= 0 , correction= 0
    var= [2, 3, 8, ]
Solved IF-0 on node 4
    bag(4): bags= 1 , exp= 1 , correction= 0
    var= [2, 8, ]
solveIF 1 + 4 => 3
    bag(3): bags= 0 , exp= 0 , correction= 0
    var= [2, 4, 8, ]
    edges to [4, ]
Solved IF-1 on node 3
    bag(3): bags= 1 , exp= 0 , correction= 1
    var= [2, 4, ]
    edges to [4, ]
Solved JOIN-1 on nodes 2~3
    bag(0): bags= 1 , exp= 0 , correction= 2
    var= [1, 2, 4, ]
solveIF 0 + 0 => 1
    bag(1): bags= 0 , exp= 0 , correction= 0
    var= [1, 2, 4, 6, ]
    edges to [0, 3, ]
Solved JOIN-IF on node 1
    bag(1): bags= 1 , exp= 1 , correction= 2
    var= [1, 4, ]
    edges to [0, 3, ]
solveIF 0 + 1 => 0
    bag(0): bags= 0 , exp= 0 , correction= 0
    var= [1, 4, 7, ]
    edges to [1, ]
Solved IF-1 on node 0

```



```

bag(0): bags= 1 , exp= 0 , correction= 3
var= [1, 4, 7, ]
edges to [1, ]

==== GRAPH END ====
Entering writeJsonFile, enabled 1

--- Solutions: ---
bag 0    (from 0 to 7)
id: 0 count: 0.25
id: 1 count: 0
id: 2 count: 0
id: 3 count: 0
id: 4 count: 0.25
id: 5 count: 1.125
id: 6 count: 0.375
id: 7 count: 0.75
...

{
  "Num Join": 1
  ,"Num Introduce Forget": 5
  ,"max Table Size": 13
  ,"Model Count": 22
  ,"Time":{
    "Decomposing": 0
    ,"Solving": 0.006
    ,"Total": 0.383
  }
}

```

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