

Face Recognition

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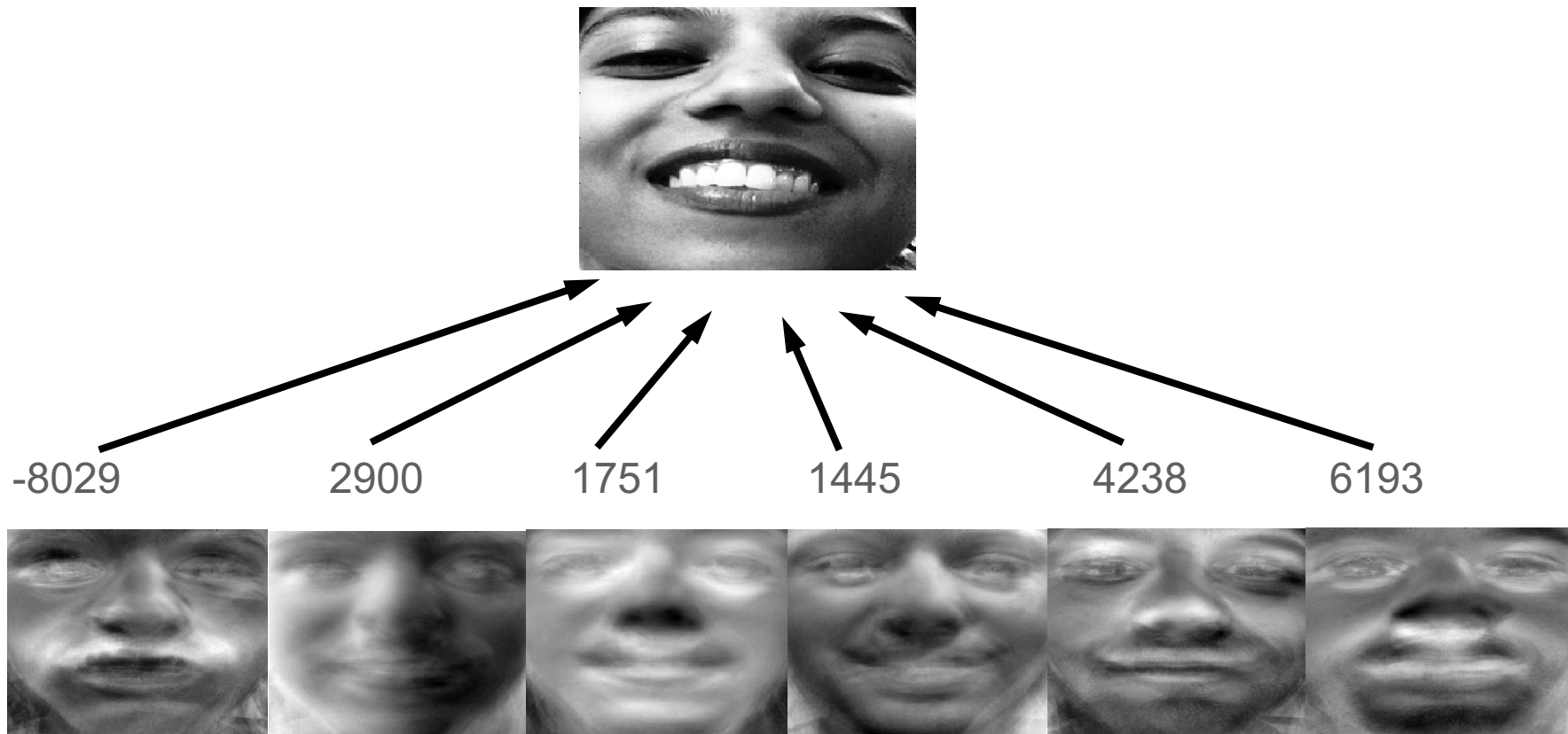


Plan

- Eigenfaces: the idea
- Eigenvectors and Eigenvalues
- Co-variance
- Learning Eigenfaces from training sets of faces
- Recognition and reconstruction

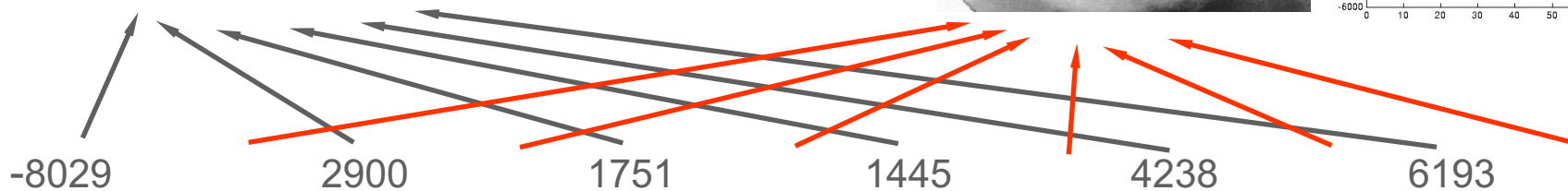
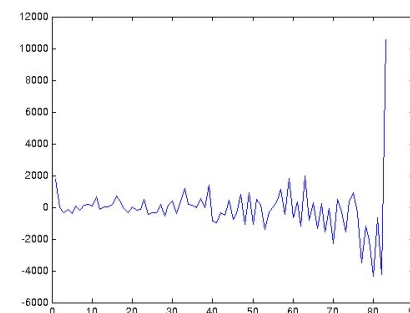
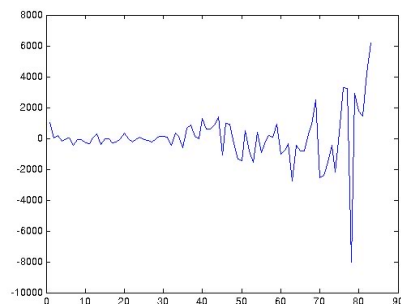
Eigenfaces: the idea

- Think of a face as being a weighted combination of some “component” or “basis” faces
- These basis faces are called eigenfaces



Eigenfaces: representing faces

- These basis faces can be differentially weighted to represent any face
- So we can use different vectors of weights to represent different faces



Learning Eigenfaces

Q: How do we pick the set of basis faces?

A: We take a set of real training faces



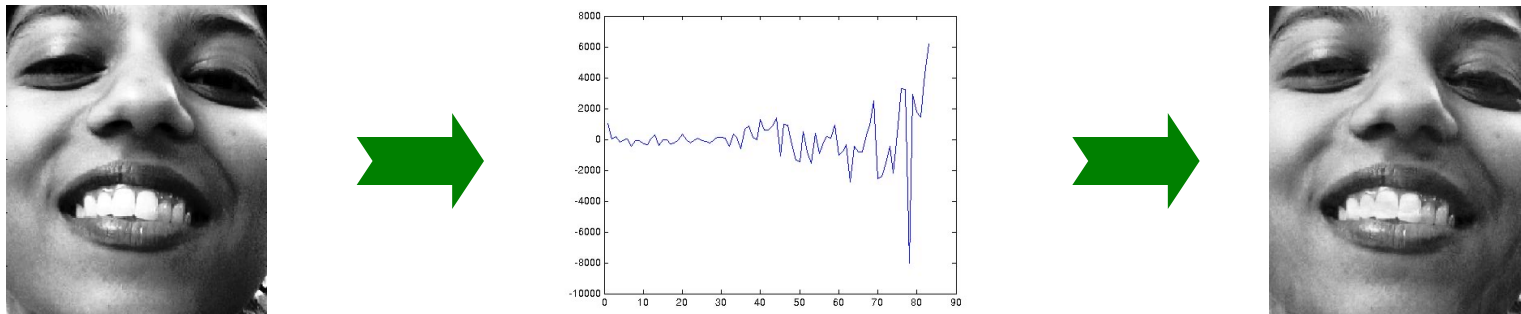
Then we find (learn) a set of basis faces which best represent the differences between them

We'll use a statistical criterion for measuring this notion of “best representation of the differences between the training faces”

We can then store each face as a set of weights for those basis faces

Using Eigenfaces: recognition & reconstruction

- We can use the eigenfaces in two ways
- 1: we can store and then reconstruct a face from a set of weights



- 2: we can recognise a new picture of a familiar face



Learning Eigenfaces

- How do we learn them?
- We use a method called Principle Components Analysis (PCA)
- To understand this we will need to understand
 - What an eigenvector is
 - What covariance is
 - what is happening in PCA qualitatively

Eigenfaces

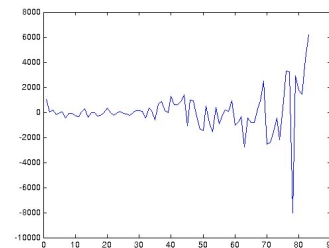
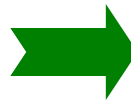
- All we are doing in the face case is treating the face as a point in a high-dimensional space, and then treating the training set of face pictures as our set of points
- To train:
 - Take your images, and re-arrange as a 2Dmatrix
 - Rows: Each image
 - Columns: Each pixel value
 - We calculate the covariance matrix of the faces
 - We then find the eigenvectors of that covariance matrix
- These eigenvectors are the eigenfaces or basis faces
- Eigenfaces with bigger eigenvalues will explain more of the variation in the set of faces, i.e. will be more distinguishing

Eigenfaces: image space to face space

- When we see an image of a face we can transform it to face space

$$\mathbf{w}_k = \mathbf{x}^i \cdot \mathbf{v}_k$$

- There are $k=1\dots n$ eigenfaces \mathbf{v}_k
- The i^{th} face in image space is a vector \mathbf{x}^i
- The corresponding weight is w_k
- We calculate the corresponding weight for every eigenface

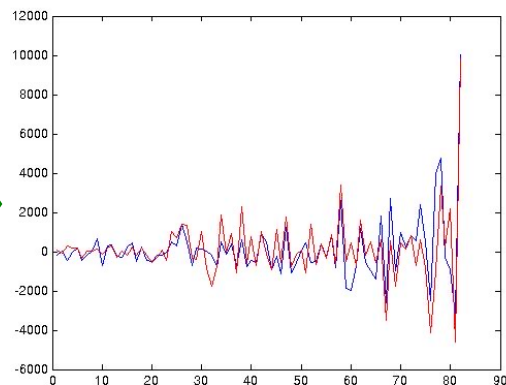


Recognition in face space

- Recognition is now simple. We find the euclidean distance d between our face and all the other stored faces in face space:

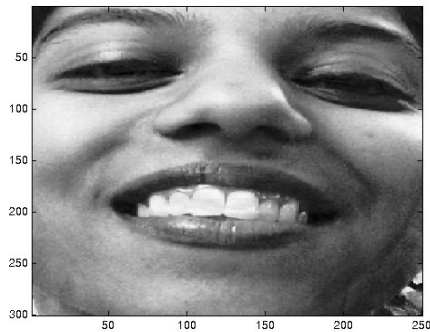
$$d(w^1, w^2) = \sqrt{\sum_{i=1}^n (w_i^1 - w_i^2)^2}$$

- The closest face in face space is the chosen match

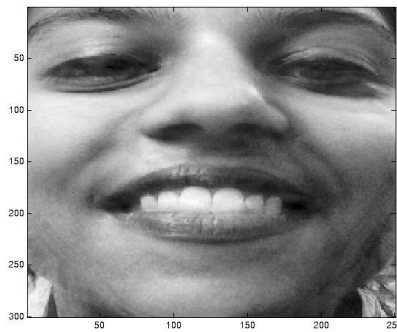


Reconstruction

- The more eigenfaces you have the better the reconstruction, but you can have high quality reconstruction even with a small number of eigenfaces



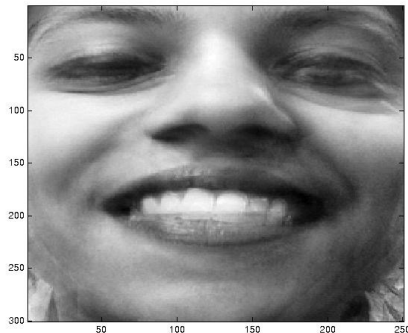
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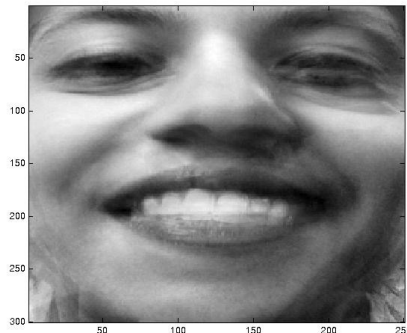
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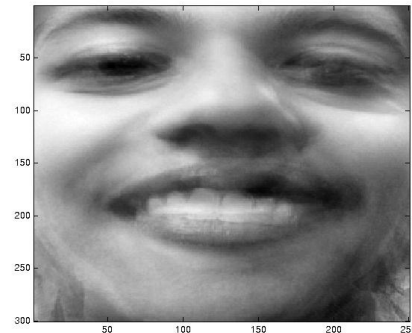
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Summary

- Statistical approach to visual recognition
- Also used for object recognition
- Problems
- Reference: M. Turk and A. Pentland (1991). Eigenfaces for recognition, *Journal of Cognitive Neuroscience*, 3(1): 71–86.

