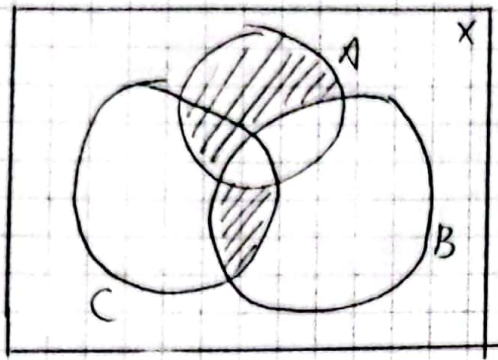


Q1

(a) (i)



$$(A \setminus B) \cup ((B \setminus C) \setminus A)$$

$$(ii) (A \cap \bar{B}) \cup (B \cap C \cap \bar{A})$$

$$(iii) D = \{-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6\}$$

$$D \cap E = \{-6, -3, 0, 3, 6\}$$

(b) (i)

| X | 0 | 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 2 | 3 | 4 | 5 |
| 2 | 0 | 2 | 4 | 0 | 2 | 4 |
| 3 | 0 | 3 | 0 | 3 | 0 | 3 |
| 4 | 0 | 4 | 2 | 0 | 4 | 2 |
| 5 | 0 | 5 | 4 | 3 | 2 | 1 |

not satisfy

$$(ii) x \leftarrow 0$$

$$s \leftarrow 0$$

while ($x < 0$) {

$$x \leftarrow x + 1$$

$$s \leftarrow s + 2 \times x - 1$$

return s

$$S = 0 + 2 \times 1 - 1 + 2 \times 2 - 1 + 2 \times 3 - 1 \dots + 2 \times x - 1$$

$$S = 2(1 + \dots + x) - 1 \times x$$

$$S = 2 \times \frac{(1+x) \times x}{2} - x$$

$$S = x + x^2 - x = x^2$$

(c) countable

as the length of array is specified as an int variable

Q2

(a) $(\neg A \vee \neg B) \rightarrow ((\neg A \wedge B) \rightarrow \neg C)$

$$\begin{array}{c}
 \frac{\frac{\frac{\overline{C \rightarrow A \wedge B}}{A \wedge B} \quad C}{A \wedge B} [E] \quad \frac{\frac{\overline{\neg A \vee \neg B}}{\neg(A \wedge B)} [VE]}{\neg(A \wedge B)} [E]}{\perp} \\
 \frac{\perp}{\neg C} [\neg I] \\
 \frac{\neg C}{(C \rightarrow A \wedge B) \rightarrow \neg C} [\rightarrow I] \\
 \frac{(C \rightarrow A \wedge B) \rightarrow \neg C}{(\neg A \vee \neg B) \rightarrow ((\neg A \wedge B) \rightarrow \neg C)} [\rightarrow I]
 \end{array}$$

(b) (i) $\neg \neg \neg A \rightarrow \neg A$

$$\begin{array}{c}
 \frac{\frac{\overline{\neg \neg \neg A}}{\neg A} [DNE]}{\neg A} [E]}{\perp} \\
 \frac{\perp}{\neg A} [\neg I] \\
 \frac{\neg A}{\neg \neg \neg A \rightarrow \neg A} [\rightarrow I]
 \end{array}$$

(ii) $\neg \neg \neg A \rightarrow \neg A$

$$\begin{array}{c}
 \frac{\neg A \vdash \neg A}{} [Id]}{\vdash \neg A, \neg A} [\neg R]}{\vdash \neg \neg A \vdash \neg A} [\neg L]}{\vdash \neg \neg \neg A \rightarrow \neg A} [\rightarrow R]
 \end{array}$$

(c) $(\neg P \rightarrow Q \wedge R) \rightarrow P \vee R$

$$\begin{array}{c}
 \frac{}{\neg P \vdash \neg P, R} \text{[Id]} \quad \frac{\frac{}{\neg P, Q, R \vdash R} \text{[Id]} \quad \neg P, Q \wedge R \vdash R}{\neg P, Q \wedge R \vdash R} \text{[}\wedge R\text{]} \\
 \hline
 \frac{\neg P \rightarrow Q \wedge R, \neg P \vdash R}{\neg P \rightarrow Q \wedge R \vdash \neg P, R} \text{[}\rightarrow R\text{]} \\
 \frac{\neg P \rightarrow Q \wedge R \vdash \neg P, R}{\neg P \rightarrow Q \wedge R \vdash P \vee R} \text{[}\vee I\text{]} \\
 \hline
 \vdash (\neg P \rightarrow Q \wedge R) \rightarrow P \vee R \text{[}\rightarrow I\text{]}
 \end{array}$$