

$$(d) \lim_{x \rightarrow \pi} \frac{\sin x}{x - \pi} = -1$$

Note que  $\frac{\sin \pi}{\pi - \pi} = \frac{0}{0}$  gera uma indeterminação

mas, note que  $\sin(x - \pi) = -\sin x$

$$\text{De fato, } \sin(x - \pi) = \sin x \cdot \underbrace{\cos \pi}_{-1} - \underbrace{\sin \pi}_0 \cdot \cos x = -\sin x$$

$$\text{Logo, } \frac{\sin x}{x - \pi} = \frac{-\sin(x - \pi)}{x - \pi} = -\frac{\sin u}{u} \text{ se } u = x - \pi$$

$$\text{Assim, } \lim_{x \rightarrow \pi} \frac{\sin x}{x - \pi} = -\lim_{u \rightarrow 0} \frac{\sin u}{u} = -1$$

