

CS 760 Homework 4 by Cheng-Wei Lu

Problem 4.1

For each non-binary feature, I use its average as a standard to decide the binary transformation of each data. I use average because in reality, we often divide data in two parts with average. Therefore, I think it would also be reasonable if I use average here. If the original feature is greater than the average, it will be converted to 1. If not, it will be converted to 0. The average for passenger class is 2.3, age is 29.4, siblings/spouses aboard is 0.5, parents/children aboard is 0.4 and fare is 32.3.

Problem 4.2

Please see the appendix notebook cell of title, "Calculate mutual information (Problem 4.2)."

Problem 4.3

Please see the appendix notebook cell of title, "Build Decision Tree (Problem 4.3)." I stop the tree from growing more nodes when the entropy of y is less than 0.2 or when all the features are tested.

Problem 4.4

Please see the appendix notebook cell of title, "Tree Displayed (Problem 4.4)." There you can see the structure of my tree.

Problem 4.5

Please see the appendix notebook cell of title, "10 fold cross validation (Problem 4.5)." The accuracy of my prediction is 0.813.

Problem 4.6

My original data is

$$\begin{pmatrix} 2(\text{class}) \\ 0(\text{sex}) \\ 25(\text{age}) \\ 0(\text{siblings/spouses aboard}) \\ 0(\text{parents/children aboard}) \\ 50(\text{fare}) \end{pmatrix}$$

According to the conversion rule, my data input to the decision tree will be,

$$\begin{pmatrix} 0(\text{class}) \\ 0(\text{sex}) \\ 0(\text{age}) \\ 0(\text{siblings/spouses aboard}) \\ 0(\text{parents/children aboard}) \\ 1(\text{fare}) \end{pmatrix}$$

According to my decision tree, I wouldn't have survived.

Problem 4.7

(a)

Please see the appendix notebook cell of title, "Random Forest on Sampling - Trees Displayed (Problem 4.7(a))." There you can see the structure of my trees.

(b)

The accuracy is 0.831

(c)

According to my random forest, I wouldn't have survived.

Problem 4.8

(a)

Please see the appendix notebook cell of title, "Random Forest on Feature Dropping - Trees Displayed (Problem 4.8(a))." There you can see the structure of my trees.

(b)

The accuracy is 0.825

(c)

According to my random forest, I wouldn't have survived.

Problem 4.9

Yes, my predictions all agree with each other. I would like to use logistic regression more, because with logistic regression, we analyze more detailedly on the relationship between the coefficient of a feature with the prediction result.

hw4_decision_tree_Appendix_2

October 29, 2020

```
[8]: import csv
import numpy as np
import copy
import time
import math
from scipy import stats
import random
```

```
[9]: def split_train_label(data):
    train_x = []
    train_y = []
    for i in data:
        train_x.append(i[1:])
        train_y.append([i[0]])

    return train_x, train_y
```

```
[10]: with open('titanic_data.csv', 'r') as file:
    temp = csv.reader(file)
    data = list(temp)

    header = data[0]
    data = data[1:]
    for i in range(len(data)):
        row_len = len(data[0])
        for j in range(row_len):
            data[i][j] = float(data[i][j])

    train_x, train_y = split_train_label(data)
```

1 Convert all features into binary features

I used average as the criteria to change the data

```
[12]: #binary conversion
binary_avg = []
for i in range(len(header[1:])):
```

```

total = 0
avg = 0
for j in train_x:
    total += j[i]
avg = total/len(train_x)
binary_avg.append(avg)

for i in range(len(train_x)):
    for j in range(len(train_x[0])):
        if train_x[i][j] >= binary_avg[j]:
            train_x[i][j] = 1.0
        else:
            train_x[i][j] = 0.0

print(binary_avg)

```

[2.305524239007892, 0.35400225479143177, 29.471443066516347, 0.5253664036076663, 0.3833145434047351, 32.30542018038328]

2 Calculate mutual information (Problem 4.2)

```

[13]: def count_ones_Hx(featureNumber,data): # choice is 0 or 1, and data is the
    ↪training data that will be gone over
    x_prob = {}
    count = 0
    for i in range(len(data)):
        if 1 == data[i][featureNumber]:
            count += 1
    x_prob[1] = count/len(data)
    x_prob[0] = 1-x_prob[1]
    return x_prob

def count_ones_Hxy(featureNumber,dataX,dataY): # choice is 0 or 1, and data is
    ↪the training data that will be gone over
    x_y_prob = {(0,0):0,(0,1):0,(1,0):0,(1,1):0}
    x_cond_y = {(0,0):0,(0,1):0,(1,0):0,(1,1):0}
    count_y = [0,0] ## condition when y = 0 or 1

    for i in range(len(dataX)):
        for j in range(2):
            for k in range(2):
                if dataX[i][featureNumber] == j and dataY[i][0] == k:
                    x_y_prob[(j,k)] += 1

    if (x_y_prob[(0,0)]+x_y_prob[(1,0)]) != 0:
        x_cond_y[(0,0)] = x_y_prob[(0,0)]/(x_y_prob[(0,0)]+x_y_prob[(1,0)])

```

```

        x_cond_y[(1,0)] = x_y_prob[(1,0)]/(x_y_prob[(0,0)]+x_y_prob[(1,0)])
    if (x_y_prob[(0,1)]+x_y_prob[(1,1)]) != 0:
        x_cond_y[(0,1)] = x_y_prob[(0,1)]/(x_y_prob[(0,1)]+x_y_prob[(1,1)])
        x_cond_y[(1,1)] = x_y_prob[(1,1)]/(x_y_prob[(0,1)]+x_y_prob[(1,1)])
    for i in x_y_prob.keys():
        x_y_prob[i] = x_y_prob[i]/len(dataX)

    return x_y_prob,x_cond_y

def MI_eval(train_x,train_y,feature_checked):
    MI_array = []
    for i in range(len(train_x[0])): # i is the feature to calculate mutual
        ↪ information
        if feature_checked[i] == 1:
            MI_array.append(0)
            continue
        Hx = 0
        Hxy = 0
        x_prob = count_ones_Hx(i,train_x)
        x_y_prob,x_cond_y = count_ones_Hxy(i,train_x,train_y)
        for j in range(2):
            if x_prob[j] != 0:
                Hx += x_prob[j]*math.log((1/x_prob[j]),2)
            for k in range(2):
                if x_cond_y[j,k] == 0:
                    Hxy += 0
                else:
                    if x_cond_y[j,k] != 0:
                        Hxy += x_y_prob[j,k]*math.log((1/x_cond_y[j,k]),2)
            MI_array.append(Hx-Hxy)

    MI_y = 0
    prob_y = 0
    for i in train_y:
        MI_y += i[0]
    prob_y = MI_y/len(train_y)

    if prob_y == 0 or prob_y == 1:
        information_y = 0
    else:
        information_y = prob_y*math.log(1/prob_y,2) + (1-prob_y)*math.log(1/
        ↪ (1-prob_y),2)
    return MI_array, information_y

```

3 Build Decision Tree (Problem 4.3)

```
[26]: class decision_tree_node:
    def __init__(self, train_x, train_y, feature_checked = [0,0,0,0,0,0], order_
    ↪= [], depth = 0, print_tree = False):
        self.train_x = train_x
        self.train_y = train_y
        self.feature_checked = feature_checked
        self.isleaf = 0
        self.leftNode = None
        self.rightNode = None
        self.feature_choice = None
        self.order = copy.deepcopy(order)
        self.depth = depth
        self.print_tree = print_tree
        self.build_tree()

    def build_tree(self):
        MI, Hy = MI_eval(self.train_x, self.train_y, self.feature_checked)
        left_x = []
        left_y = []
        right_x = []
        right_y = []

        if Hy <= 0.2 or sum(self.feature_checked) == len(self.train_x[0]):
            self.isleaf = 1
            #print(self.order)

        else:
            max_idx = 0
            for i in range(len(MI)):
                if MI[i] > MI[max_idx]:
                    max_idx = i
            self.feature_choice = max_idx

            for i in range(len(self.train_x)):
                if self.train_x[i][max_idx] == 0:
                    left_x.append(self.train_x[i])
                    left_y.append(self.train_y[i])
                else:
                    right_x.append(self.train_x[i])
                    right_y.append(self.train_y[i])

            if len(left_x) and len(right_x) > 0:
                new_feature_checked = copy.deepcopy(self.feature_checked)
                new_feature_checked[self.feature_choice] = 1
                self.order.append(str(self.feature_choice) + " L ")
```

```

        if self.print_tree == True:
            print('|---'*self.depth,'feature ',self.feature_choice+1, ": =_",
↪0")

            self.leftNode =_
↪decision_tree_node(left_x,left_y,new_feature_checked,self.order,depth = self.
↪depth+1,print_tree=self.print_tree)
            self.order[-1] = str(self.feature_choice) + " R "
            if self.print_tree == True:
                print('|---'*self.depth,'feature ',self.feature_choice+1, ": =_",
↪1")

            self.rightNode =_
↪decision_tree_node(right_x,right_y,new_feature_checked,self.order,depth =_
↪self.depth+1,print_tree=self.print_tree)
        else:
            self.isleaf = 1
        def predict(self,train_x):
            if self.isleaf == 1:
                count_1 = 0
                count_0 = 0
                for i in range(len(self.train_y)):
                    if self.train_y[i][0] == 1:
                        count_1 += 1
                    else:
                        count_0 += 1
                prob_1 = count_1/(count_1+count_0)
                prob_0 = count_0/(count_1+count_0)
                if prob_1 > prob_0:
                    return 1
                else:
                    return 0

            elif train_x[self.feature_choice] == 0:
                #print('feature:',self.feature_choice, ' go left')
                return(self.leftNode.predict(train_x))
            elif train_x[self.feature_choice] == 1:
                #print('feature:',self.feature_choice, ' go right')
                return(self.rightNode.predict(train_x))

```

4 Tree Displayed (Problem 4.4)

```
[27]: a = decision_tree_node(train_x, train_y,print_tree = True)
```

```

feature 2 : = 0
|--- feature 1 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 6 : = 0

```

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|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
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|---|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 1
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feature 2 : = 1
|--- feature 1 : = 0
|---|--- feature 6 : = 0

```



```

|---|---|--- feature 5 := 0
|---|---|---|--- feature 3 := 0
|---|---|---|---|--- feature 4 := 0
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|--- feature 1 := 1
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|---|---|--- feature 4 := 0
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|---|---|---|--- feature 5 := 1
|---|---|---|---|--- feature 3 := 0
|---|---|---|---|--- feature 3 := 1
|---|--- feature 6 := 1

```

5 10 fold cross validation (Problem 4.5)

```

[48]: interval = math.ceil(len(train_x)/10)
global_accuracy = []
for i in range(10):
    local_accuracy = 0
    count = 0
    tr_x = []
    tr_y = []
    te_x = []
    te_y = []
    te_x += train_x[i*interval : (i+1)*interval]
    te_y += train_y[i*interval : (i+1)*interval]
    tr_x += train_x[0:i*interval]
    tr_x += train_x[(i+1)*interval:]
    tr_y += train_y[0:i*interval]

```

```

tr_y += train_y[(i+1)*interval:]
tree = decision_tree_node(tr_x, tr_y)

for j in range(len(te_x)):
    if tree.predict(te_x[j]) == te_y[j][0]:
        count += 1
global_accuracy.append(count/len(te_x))
print('average accuracy = ', sum(global_accuracy)/len(global_accuracy))

```

average accuracy = 0.8130128037627383

6 Will I survived?

```

[45]: my_data = [0,0,0,0,0,1]
      tree.predict(my_data )

```

[45]: 0

7 Random Forest on Sampling - Trees Displayed (Problem 4.7(a))

```

[39]: interval = math.ceil(len(train_x)/10)
      forest = []
      global_accuracy = []
      for i in range(5):
          tr_x = []
          tr_y = []
          te_x = []
          te_y = []
          for j in range(len(train_x)):
              if random.random() <= 0.8:
                  tr_x.append(train_x[j])
                  tr_y.append(train_y[j])
              else:
                  te_x.append(train_x[j])
                  te_y.append(train_y[j])
          print('-----tree {}-----'.
→format(i+1))
          tree = decision_tree_node(tr_x, tr_y, print_tree = True)

          forest.append(tree)

```

```

-----tree 1-----
feature 2 : = 0
|--- feature 1 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 6 : = 0

```

```

|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
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|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
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feature 2 : = 1
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|---|---|---|--- feature 4 : = 1
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-----tree 2-----
feature 2 : = 0
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|---|---|---|---|--- feature 4 : = 0
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feature 2 : = 0
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|---|---|---|---|--- feature 4 : = 0
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-----tree 4-----
feature 2 : = 0
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|---|---|---|---|--- feature 3 : = 0
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|---|--- feature 6 : = 0

```

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|---|---|--- feature 3 := 0
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|---|---|--- feature 5 := 0
|---|---|---|--- feature 4 := 0
|---|---|---|---|--- feature 3 := 0
|---|---|---|---|--- feature 3 := 1
|---|---|---|--- feature 4 := 1
|---|---|---|---|--- feature 3 := 0
|---|---|---|---|--- feature 3 := 1
|---|---|--- feature 5 := 1
|---|---|---|--- feature 3 := 0
|---|---|---|---|--- feature 4 := 0
|---|---|---|---|--- feature 4 := 1
|---|---|---|--- feature 3 := 1
|---|---|---|--- feature 4 := 0

```

```
|---|---|---|---|--- feature 4 : = 1  
|---|--- feature 6 : = 1
```

```
[46]: for i in forest:  
       print(i.predict(my_data))
```

```
0  
0  
0  
0  
0
```

8 random forest + cross validation

```
[51]: interval = math.ceil(len(train_x)/10)  
global_accuracy = []  
for cros_val in range(10):  
    forest = []  
    train_x2 = []  
    train_y2 = []  
    test_x2 = []  
    test_y2 = []  
    test_x2 += train_x[cros_val*interval : (cros_val+1)*interval]  
    test_y2 += train_y[cros_val*interval : (cros_val+1)*interval]  
    train_x2 += train_x[0:cros_val*interval]  
    train_x2 += train_x[(cros_val+1)*interval:]  
    train_y2 += train_y[0:cros_val*interval]  
    train_y2 += train_y[(cros_val+1)*interval:]  
  
    for i in range(5):  
        tr_x = []  
        tr_y = []  
        te_x = []  
        te_y = []  
        for j in range(len(train_x2)):  
            if random.random() <= 0.8:  
                tr_x.append(train_x2[j])  
                tr_y.append(train_y2[j])  
            else:  
                te_x.append(train_x2[j])  
                te_y.append(train_y2[j])  
  
        tree = decision_tree_node(tr_x, tr_y)  
        forest.append(tree)  
    temp_accuracy = []  
    for k in range(len(te_x)):  
        temp = []
```

```

    answer = None
    for j in forest:
        temp.append(j.predict(te_x[k]))
    if sum(temp) > len(temp)/2 :
        answer = 1
    else :
        answer = 0

    if answer == te_y[k][0]:
        temp_accuracy.append(1)
    else:
        temp_accuracy.append(0)
    global_accuracy.append(sum(temp_accuracy)/len(temp_accuracy))

print('average accuracy = ',sum(global_accuracy)/len(global_accuracy))

```

average accuracy = 0.8316802629711637

9 Random Forest on Feature Dropping - Trees Displayed (Problem 4.8(a))

```

[53]: forest = []

for k in range(len(train_x[0])):

    #drop features
    tr_x_drop = []
    for row in train_x:
        tr_x_drop.append(row[0:k] + row[k+1:])
    print('-----tree {}-----'.
    ↪format(k+1))
    forest.append(decision_tree_node(tr_x_drop, train_y, print_tree = True))

```

```

-----tree 1-----
feature 1 := 0
|--- feature 5 := 0
|---|--- feature 4 := 0
|---|---|--- feature 3 := 0
|---|---|---|--- feature 2 := 0
|---|---|---|--- feature 2 := 1
|---|---|--- feature 3 := 1
|---|---|---|--- feature 2 := 0
|---|---|---|--- feature 2 := 1
|---|--- feature 4 := 1
|---|---|--- feature 2 := 0
|---|---|---|--- feature 3 := 0

```

```

|---|---|---|--- feature 3 : = 1
|---|---|--- feature 2 : = 1
|--- feature 5 : = 1
|---|--- feature 4 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
feature 1 : = 1
|--- feature 5 : = 0
|---|--- feature 3 : = 0
|---|---|--- feature 2 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 2 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|--- feature 5 : = 1
|---|--- feature 4 : = 0
|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
-----tree 2-----
feature 1 : = 0
|--- feature 4 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 2 : = 0

```

```

|---|---|---|--- feature 2 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 2 : = 0
|---|---|---|--- feature 2 : = 1
|--- feature 4 : = 1
|---|--- feature 2 : = 0
|---|---|--- feature 5 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 5 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|--- feature 2 : = 1
|---|---|--- feature 5 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 5 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
feature 1 : = 1
|--- feature 2 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 0
|---|---|--- feature 3 : = 1
|--- feature 2 : = 1
|---|--- feature 5 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 4 : = 0

```

```

|---|---|--- feature 4 : = 1
-----tree 3-----
feature 2 : = 0
|--- feature 1 : = 0
|---|--- feature 4 : = 0
|---|---|--- feature 5 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 5 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|--- feature 1 : = 1
|---|--- feature 4 : = 0
|---|---|--- feature 5 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 5 : = 1
|---|--- feature 4 : = 1
|---|---|--- feature 5 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 5 : = 1
feature 2 : = 1
|--- feature 1 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|--- feature 5 : = 1
|--- feature 1 : = 1
|---|--- feature 5 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|--- feature 5 : = 1

```

```

-----tree 4-----
feature 2 := 0
|--- feature 1 := 0
|---|--- feature 4 := 0
|---|---|--- feature 5 := 0
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|---|--- feature 5 := 1
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|--- feature 4 := 1
|---|---|--- feature 3 := 0
|---|---|---|--- feature 5 := 0
|---|---|---|--- feature 5 := 1
|---|---|--- feature 3 := 1
|---|---|---|--- feature 5 := 0
|---|---|---|--- feature 5 := 1
|--- feature 1 := 1
|---|--- feature 4 := 0
|---|---|--- feature 5 := 0
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|---|--- feature 5 := 1
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|--- feature 4 := 1
|---|---|--- feature 5 := 0
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|---|--- feature 5 := 1
feature 2 := 1
|--- feature 1 := 0
|---|--- feature 5 := 0
|---|---|--- feature 4 := 0
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|---|--- feature 4 := 1
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|--- feature 5 := 1
|--- feature 1 := 1
|---|--- feature 5 := 0
|---|---|--- feature 4 := 0
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1
|---|---|--- feature 4 := 1
|---|---|---|--- feature 3 := 0
|---|---|---|--- feature 3 := 1

```



```

|---|--- feature 5 : = 1
-----tree 5-----
feature 2 : = 0
|--- feature 1 : = 0
|---|--- feature 4 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|--- feature 1 : = 1
|---|--- feature 5 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
feature 2 : = 1
|--- feature 1 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|--- feature 5 : = 1
|--- feature 1 : = 1
|---|--- feature 5 : = 0
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 0

```

```

|---|---|---|--- feature 3 : = 1
|---|--- feature 5 : = 1
-----tree 6-----
feature 2 : = 0
|--- feature 1 : = 0
|---|--- feature 5 : = 0
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|--- feature 1 : = 1
|---|--- feature 5 : = 0
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 3 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
feature 2 : = 1
|--- feature 1 : = 0
|---|--- feature 3 : = 0
|---|---|--- feature 4 : = 0
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 5 : = 0
|---|---|---|--- feature 5 : = 1
|---|--- feature 3 : = 1
|---|---|--- feature 5 : = 0
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 5 : = 1
|--- feature 1 : = 1
|---|--- feature 5 : = 0
|---|---|--- feature 3 : = 0
|---|---|--- feature 4 : = 0

```

```
|---|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|---|--- feature 4 : = 0
|---|---|---|--- feature 4 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 4 : = 0
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 1
|---|---|---|--- feature 3 : = 0
|---|---|---|--- feature 3 : = 1
```

10 Will I survived?

```
[54]: for i in forest:
      print(i.predict(my_data))
```

```
0
0
0
0
0
0
0
```

11 Random forest + feature dropping(10 fold cross validation)

```
[57]: interval = math.ceil(len(train_x)/10)
      global_accuracy = []
      for i in range(len(train_x[0])):

          #drop features
          tr_x_drop = []
          for row in train_x:
              tr_x_drop.append(row[0:i] + row[i+1:])
          forest.append(decision_tree_node(tr_x_drop, train_y))

      for cros_val in range(10):
          forest = []
          train_x2 = []
          train_y2 = []
          test_x2 = []
          test_y2 = []
          test_x2 += tr_x_drop[cros_val*interval : (cros_val+1)*interval]
          test_y2 += train_y[cros_val*interval : (cros_val+1)*interval]
          train_x2 += tr_x_drop[0:cros_val*interval]
          train_x2 += tr_x_drop[(cros_val+1)*interval:]
```

```

train_y2 += train_y[0:cros_val*interval]
train_y2 += train_y[(cros_val+1)*interval:]

tree = decision_tree_node(train_x2, train_y2)
forest.append(tree)
temp_accuracy = []
for k in range(len(test_x2)):
    temp = []
    answer = None
    for j in forest:
        temp.append(j.predict(test_x2[k]))
    if sum(temp) > len(temp)/2 :
        answer = 1
    else :
        answer = 0

    if answer == test_y2[k][0]:
        temp_accuracy.append(1)
    else:
        temp_accuracy.append(0)
global_accuracy.append(sum(temp_accuracy)/len(temp_accuracy))

print('average accuracy = ',sum(global_accuracy)/len(global_accuracy))

```

average accuracy = 0.8255813953488372