hw4_decision_tree_Appendix_2

October 29, 2020

```
[8]: import csv
      import numpy as np
      import copy
      import time
      import math
      from scipy import stats
      import random
 [9]: def split_train_label(data):
          train_x = []
          train_y = []
          for i in data:
              train_x.append(i[1:])
              train_y.append([i[0]])
          return train_x, train_y
[10]: with open('titanic_data.csv', 'r') as file:
          temp = csv.reader(file)
          data = list(temp)
      header = data[0]
      data = data[1:]
      for i in range(len(data)):
          row_len = len(data[0])
          for j in range(row_len):
              data[i][j] = float(data[i][j])
      train_x, train_y = split_train_label(data)
```

1 Convert all features into binary features

I used average as the criteria to change the data

```
[12]: #binary conversion
binary_avg = []
for i in range(len(header[1:])):
```

```
total = 0
avg = 0
for j in train_x:
    total += j[i]
avg = total/len(train_x)
binary_avg.append(avg)

for i in range(len(train_x)):
    for j in range(len(train_x[0])):
        if train_x[i][j] >= binary_avg[j]:
            train_x[i][j] = 1.0
    else:
        train_x[i][j] = 0.0

print(binary_avg)
```

[2.305524239007892, 0.35400225479143177, 29.471443066516347, 0.5253664036076663, 0.3833145434047351, 32.30542018038328]

2 Calculate mutual information (Problem 4.2)

```
[13]: def count_ones_Hx(featureNumber,data): # choice is 0 or 1, and data is the
       → training data that will be gone over
          x_prob = {}
          count = 0
          for i in range(len(data)):
              if 1 == data[i][featureNumber]:
                  count += 1
          x_prob[1] = count/len(data)
          x_{prob}[0] = 1-x_{prob}[1]
          return x_prob
      def count_ones_Hxy(featureNumber,dataX,dataY): # choice is 0 or 1, and data is_
       → the training data that will be gone over
          x_y_prob = \{(0,0):0,(0,1):0,(1,0):0,(1,1):0\}
          x_{cond_y} = \{(0,0):0,(0,1):0,(1,0):0,(1,1):0\}
          count_y = [0,0] ## condition when y = 0 or 1
          for i in range(len(dataX)):
              for j in range(2):
                  for k in range(2):
                      if dataX[i][featureNumber] == j and dataY[i][0] == k:
                           x_y_prob[(j,k)] += 1
          if (x_y_prob[(0,0)]+x_y_prob[(1,0)]) != 0:
              x_{cond_y[(0,0)]} = x_y_{prob[(0,0)]/(x_y_{prob[(0,0)]}+x_y_{prob[(1,0)]})
```

```
x_{cond}y[(1,0)] = x_{y_{prob}[(1,0)]/(x_{y_{prob}[(0,0)]}+x_{y_{prob}[(1,0)]})
    if (x_y_prob[(0,1)]+x_y_prob[(1,1)]) != 0:
        x_{cond}y[(0,1)] = x_{y_{prob}[(0,1)]/(x_{y_{prob}[(0,1)]}+x_{y_{prob}[(1,1)]})
        x_{cond_y[(1,1)]} = x_y_{prob[(1,1)]}/(x_y_{prob[(0,1)]}+x_y_{prob[(1,1)]})
    for i in x_y_prob.keys():
        x_y_prob[i] = x_y_prob[i]/len(dataX)
    return x_y_prob,x_cond_y
def MI_eval(train_x,train_y,feature_checked):
    MI array = []
    for i in range(len(train_x[0])): # i is the feature to calculate mutual_
\rightarrow information
        if feature_checked[i] == 1:
            MI_array.append(0)
            continue
        Hx = 0
        Hxy = 0
        x_prob = count_ones_Hx(i,train_x)
        x_y_prob,x_cond_y = count_ones_Hxy(i,train_x,train_y)
        for j in range(2):
            if x_prob[j] != 0:
                 Hx += x_{prob[j]}*math.log((1/x_{prob[j]}),2)
            for k in range(2):
                 if x_{cond_y[j,k]} == 0:
                     Hxy += 0
                 else:
                     if x_{ond}y[j,k] != 0:
                         Hxy += x_y_prob[j,k]*math.log((1/x_cond_y[j,k]),2)
        MI_array.append(Hx-Hxy)
    MI_y = 0
    prob_y = 0
    for i in train_y:
        MI_y += i[0]
    prob_y = MI_y/len(train_y)
    if prob_y == 0 or prob_y == 1:
        information_y = 0
    else:
        information_y = prob_y*math.log(1/prob_y,2) + (1-prob_y)*math.log(1/
 \hookrightarrow (1-prob_y),2)
    return MI_array, information_y
```

3 Build Decision Tree (Problem 4.3)

```
[26]: class decision_tree_node:
          def __init__(self, train_x, train_y, feature_checked = [0,0,0,0,0,0], order_u
       →= [],depth = 0,print_tree = False):
              self.train_x = train_x
              self.train_y = train_y
              self.feature_checked = feature_checked
              self.isleaf = 0
              self.leftNode = None
              self.rightNode = None
              self.feature_choice = None
              self.order = copy.deepcopy(order)
              self.depth = depth
              self.print_tree = print_tree
              self.build_tree()
          def build tree(self):
              MI, Hy = MI_eval(self.train_x, self.train_y, self.feature_checked)
              left_x = []
              left_y = []
              right_x = []
              right_y = []
              if Hy <= 0.2 or sum(self.feature_checked) == len(self.train_x[0]):
                  self.isleaf = 1
                  #print(self.order)
              else:
                  max_idx = 0
                  for i in range(len(MI)):
                      if MI[i] > MI[max_idx]:
                          \max idx = i
                  self.feature_choice = max_idx
                  for i in range(len(self.train_x)):
                      if self.train_x[i][max_idx] == 0:
                          left_x.append(self.train_x[i])
                          left_y.append(self.train_y[i])
                      else:
                          right_x.append(self.train_x[i])
                          right_y.append(self.train_y[i])
              if len(left_x) and len(right_x) > 0:
                  new_feature_checked = copy.deepcopy(self.feature_checked)
                  new_feature_checked[self.feature_choice] = 1
                  self.order.append(str(self.feature_choice) + " L ")
```

```
if self.print_tree == True:
               print('|---'*self.depth,'feature ',self.feature_choice+1, ": =__
→0")
           self.leftNode =
→decision_tree_node(left_x,left_y,new_feature_checked,self.order,depth = self.
⇒depth+1,print tree=self.print tree)
           self.order[-1] = str(self.feature_choice) + " R "
           if self.print_tree == True:
               print('|---'*self.depth, 'feature ', self.feature_choice+1, ": =_
→1")
           self.rightNode =
→decision_tree_node(right_x,right_y,new_feature_checked,self.order,depth = __
→self.depth+1,print_tree=self.print_tree)
       else:
           self.isleaf = 1
   def predict(self,train_x):
           if self.isleaf == 1:
               count 1 = 0
               count_0 = 0
               for i in range(len(self.train y)):
                   if self.train_y[i][0] == 1:
                       count 1 += 1
                   else:
                       count_0 += 1
               prob_1 = count_1/(count_1+count_0)
               prob_0 = count_0/(count_1+count_0)
               if prob_1 > prob_0:
                   return 1
               else:
                   return 0
           elif train_x[self.feature_choice] == 0:
               #print('feature:' ,self.feature_choice, ' go left')
               return(self.leftNode.predict(train_x))
           elif train x[self.feature choice] == 1:
               #print('feature:' ,self.feature_choice, ' go right')
               return(self.rightNode.predict(train_x))
```

4 Tree Displayed (Problem 4.4)

```
[27]: a = decision_tree_node(train_x, train_y,print_tree = True)

feature 2 := 0
|--- feature 1 := 0
|---|--- feature 5 := 0
|---|--- feature 6 := 0
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|---|---| feature 4 : = 0
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feature 2 : = 1
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```

5 10 fold cross validation (Problem 4.5)

```
[48]: interval = math.ceil(len(train_x)/10)
    global_accuracy = []
    for i in range(10):
        local_accuracy = 0
        count = 0
        tr_x = []
        tr_y = []
        te_x = []
        te_y = []
        te_y += train_x[i*interval : (i+1)*interval]
        te_y += train_y[i*interval : (i+1)*interval]
        tr_x += train_x[0:i*interval]
        tr_y += train_x[0:i*interval]
        tr_y += train_y[0:i*interval]
```

```
tr_y += train_y[(i+1)*interval:]
tree = decision_tree_node(tr_x, tr_y)

for j in range(len(te_x)):
    if tree.predict(te_x[j]) == te_y[j][0]:
        count += 1
    global_accuracy.append(count/len(te_x))
print('average accuracy = ', sum(global_accuracy)/len(global_accuracy))
```

average accuracy = 0.8130128037627383

6 Will I survived?

```
[45]: my_data = [0,0,0,0,0,1]
tree.predict(my_data )
[45]: 0
```

7 Random Forest on Sampling - Trees Displayed (Problem 4.7(a))

```
[39]: interval = math.ceil(len(train_x)/10)
     forest = []
     global_accuracy = []
     for i in range(5):
         tr_x = []
         tr_y = []
         te_x = []
         te_y = []
         for j in range(len(train_x)):
             if random.random() <= 0.8:</pre>
                tr_x.append(train_x[j])
                tr_y.append(train_y[j])
             else:
                te_x.append(train_x[j])
                te_y.append(train_y[j])
         print('-----'.
      \rightarrowformat(i+1))
         tree = decision_tree_node(tr_x, tr_y,print_tree = True)
         forest.append(tree)
```

feature 2 : = 0 |--- feature 1 : = 0 |---|-- feature 5 : = 0 |---|-- feature 6 : = 0

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|---|---| feature 4 : = 0
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-----tree 2-----
feature 2 := 0
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-----tree 3-----
feature 2 := 0
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-----tree 4-----
feature 2 := 0
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feature 2 := 1
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-----tree 5-----
feature 2 := 0
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|---|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
|---|---|---| feature 4 : = 0
```

8 random forest + cross validation

```
[51]: interval = math.ceil(len(train_x)/10)
      global_accuracy = []
      for cros_val in range(10):
          forest = []
          train_x2 = []
          train y2 = []
          test x2 = []
          test_y2 = []
          test_x2 += train_x[cros_val*interval : (cros_val+1)*interval]
          test_y2 += train_y[cros_val*interval : (cros_val+1)*interval]
          train x2 += train x[0:cros val*interval]
          train_x2 += train_x[(cros_val+1)*interval:]
          train_y2 += train_y[0:cros_val*interval]
          train_y2 += train_y[(cros_val+1)*interval:]
          for i in range(5):
              tr_x = []
              tr_y = []
              te_x = []
              te_y = []
              for j in range(len(train_x2)):
                  if random.random() <= 0.8:</pre>
                      tr_x.append(train_x2[j])
                      tr_y.append(train_y2[j])
                  else:
                      te_x.append(train_x2[j])
                      te_y.append(train_y2[j])
              tree = decision_tree_node(tr_x, tr_y)
              forest.append(tree)
          temp_accuracy = []
          for k in range(len(te_x)):
              temp = []
```

```
answer = None
for j in forest:
    temp.append(j.predict(te_x[k]))
if sum(temp) > len(temp)/2 :
    answer = 1
else :
    answer = 0

if answer == te_y[k][0]:
    temp_accuracy.append(1)
else:
    temp_accuracy.append(0)
global_accuracy.append(sum(temp_accuracy)/len(temp_accuracy))

print('average accuracy = ',sum(global_accuracy)/len(global_accuracy))
```

average accuracy = 0.8316802629711637

9 Random Forest on Feature Dropping - Trees Displayed (Problem 4.8(a))

-----tree 1------feature 1 : = 0

```
|--- feature 5 : = 0
|---|-- feature 4 : = 0
|---|--| feature 3 : = 0
|---|--|-- feature 2 : = 0
|---|--|-- feature 2 : = 1
|---|--|-- feature 3 : = 1
|---|--|-- feature 2 : = 0
|---|--|-- feature 2 : = 1
|---|-- feature 4 : = 1
|---|-- feature 2 : = 0
|---|--|-- feature 3 : = 0
```

```
|---|---| feature 3 : = 1
|---|---| feature 2 : = 1
|--- feature 5 : = 1
|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---|---| feature 3 : = 1
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---|---| feature 3 : = 1
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
feature 1 : = 1
|--- feature 5:=0
|---| feature 3 : = 0
|---|---| feature 2 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|--- feature 2 : = 1
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---| feature 3 : = 1
|---|---| feature 4 : = 0
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---|---| feature 4 : = 1
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|--- feature 5:=1
|---| feature 4 : = 0
|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---|---| feature 3 : = 1
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
-----tree 2-----
feature 1 := 0
|--- feature 4 := 0
|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 2 : = 0
```

```
|---|---| feature 2 : = 1
|---|---| feature 3 : = 1
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|---|---| feature 3 : = 1
|---|---| feature 2 : = 0
|---|---| feature 2 : = 1
|--- feature 4 : = 1
|---| feature 2 : = 0
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|--- feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 2 : = 1
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
feature 1 : = 1
|--- feature 2 := 0
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|--- feature 2 : = 1
|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---| feature 5 : = 1
|---|---| feature 4 : = 0
```

```
|---|---| feature 4 : = 1
-----tree 3-----
feature 2 := 0
|--- feature 1 := 0
|---| feature 4 : = 0
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|--- feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|---|---| feature 3 : = 1
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 4 : = 0
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|--- feature 5 : = 1
|---| feature 4 : = 1
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 5 : = 1
feature 2 : = 1
|---| feature 1 : = 0
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---| feature 5 : = 1
```

```
-----tree 4-----
feature 2 := 0
|---| feature 1 : = 0
|---| feature 4 : = 0
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|---|---| feature 3 : = 1
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 4 : = 0
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 4 : = 1
|---|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 5 : = 1
feature 2 : = 1
|--- feature 1 := 0
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
```

```
|---|-- feature 5 : = 1
-----tree 5-----
feature 2 := 0
|--- feature 1 := 0
|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|---|---| feature 3 : = 1
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|---|---| feature 3 : = 1
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
feature 2 : = 1
|---| feature 1 : = 0
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
```

```
|---|---| feature 3 : = 1
|---| feature 5 : = 1
-----tree 6-----
feature 2 := 0
|---| feature 1 : = 0
|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---|---| feature 4 : = 1
|---|---| feature 3 : = 0
|---|---| feature 3 : = 1
|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|--- feature 1 : = 1
|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---| feature 5 : = 1
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 3 : = 1
feature 2 : = 1
|--- feature 1 := 0
|---| feature 3 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 5 : = 0
|---|---| feature 5 : = 1
|---| feature 3 : = 1
|---|---| feature 5 : = 0
|---|---| feature 4 : = 0
|---|---| feature 4 : = 1
|---|---| feature 5 : = 1
|--- feature 1 : = 1
|---| feature 5 : = 0
|---|---| feature 3 : = 0
|---|---| feature 4 : = 0
```

```
|---|---|--- feature 4 : = 1
|---|---|--- feature 3 : = 1
|---|---|--- feature 4 : = 0
|---|---|--- feature 4 : = 1
|---|--- feature 5 : = 1
|---|---|--- feature 4 : = 0
|---|---|--- feature 3 : = 0
|---|---|--- feature 3 : = 1
|---|---|--- feature 3 : = 0
|---|---|---- feature 3 : = 0
|---|---|---- feature 3 : = 1
```

10 Will I survived?

11 Random forest + feature dropping(10 fold cross validation)

```
[57]: interval = math.ceil(len(train_x)/10)
      global_accuracy = []
      for i in range(len(train_x[0])):
          #drop features
          tr_x_drop = []
          for row in train_x:
              tr_x_drop.append(row[0:i] + row[i+1:])
          forest.append(decision_tree_node(tr_x_drop, train_y))
          for cros_val in range(10):
              forest = []
              train_x2 = []
              train_y2 = []
              test_x2 = []
              test_y2 = []
              test_x2 += tr_x_drop[cros_val*interval : (cros_val+1)*interval]
              test_y2 += train_y[cros_val*interval : (cros_val+1)*interval]
              train x2 += tr x drop[0:cros val*interval]
              train_x2 += tr_x_drop[(cros_val+1)*interval:]
```

```
train_y2 += train_y[0:cros_val*interval]
       train_y2 += train_y[(cros_val+1)*interval:]
       tree = decision_tree_node(train_x2, train_y2)
       forest.append(tree)
   temp_accuracy = []
   for k in range(len(test_x2)):
       temp = []
       answer = None
       for j in forest:
            temp.append(j.predict(test_x2[k]))
        if sum(temp) > len(temp)/2 :
            answer = 1
        else :
            answer = 0
        if answer == test_y2[k][0]:
           temp_accuracy.append(1)
        else:
            temp_accuracy.append(0)
   global_accuracy.append(sum(temp_accuracy)/len(temp_accuracy))
print('average accuracy = ',sum(global_accuracy)/len(global_accuracy))
```

average accuracy = 0.8255813953488372