

WebAssembly Specification

Release 2.1 + function references (Draft 2022-08-02)

WebAssembly Community Group

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Contents

1	1 Introduction		1
	1.1 Introduction		1
	1.2 Overview		3
			_
2			5
	2.1 Conventions		5
	2.2 Values		7
	2.3 Types		9
	2.4 Instructions		12
	2.5 Modules	· · · · · · · · · · · · · · · · · · ·	20
3	3 Validation		25
	3.1 Conventions		25
	3.2 Types		28
	3.3 Matching		33
	3.4 Instructions		36
	3.5 Modules		53
4			63
	4.1 Conventions		63
	4.2 Runtime Structure		65 53
	4.3 Numerics		72
	4.4 Instructions		95
	4.5 Modules	1	30
5	5 Binary Format	1	41
	5.1 Conventions	1	41
	5.2 Values	1	43
	5.3 Types	1	44
	5.4 Instructions	1	46
	5.5 Modules	1	58
6	6 Text Format	1	65
•	6.1 Conventions	-	-
	6.2 Lexical Format		
	6.3 Values		
	6.4 Types		
	6.5 Instructions		
	6.6 Modules		80
7	7 Appendix	1	93

Index		223
7.6	Change History	219
	Soundness	
7.4	Custom Sections	208
7.3	Validation Algorithm	202
7.2	Implementation Limitations	200
/.1	Embedding	193

CHAPTER 1

Introduction

1.1 Introduction

WebAssembly (abbreviated Wasm²) is a *safe*, *portable*, *low-level code format* designed for efficient execution and compact representation. Its main goal is to enable high performance applications on the Web, but it does not make any Web-specific assumptions or provide Web-specific features, so it can be employed in other environments as well.

WebAssembly is an open standard developed by a W3C Community Group¹.

This document describes version 2.1 + function references (Draft 2022-08-02) of the *core* WebAssembly standard. It is intended that it will be superseded by new incremental releases with additional features in the future.

1.1.1 Design Goals

The design goals of WebAssembly are the following:

- Fast, safe, and portable *semantics*:
 - **Fast**: executes with near native code performance, taking advantage of capabilities common to all contemporary hardware.
 - Safe: code is validated and executes in a memory-safe³, sandboxed environment preventing data corruption or security breaches.
 - **Well-defined**: fully and precisely defines valid programs and their behavior in a way that is easy to reason about informally and formally.
 - Hardware-independent: can be compiled on all modern architectures, desktop or mobile devices and embedded systems alike.
 - Language-independent: does not privilege any particular language, programming model, or object model.
 - **Platform-independent**: can be embedded in browsers, run as a stand-alone VM, or integrated in other environments.

² A contraction of "WebAssembly", not an acronym, hence not using all-caps.

¹ https://www.w3.org/community/webassembly/

³ No program can break WebAssembly's memory model. Of course, it cannot guarantee that an unsafe language compiling to WebAssembly does not corrupt its own memory layout, e.g. inside WebAssembly's linear memory.

- Open: programs can interoperate with their environment in a simple and universal manner.
- Efficient and portable representation:
 - Compact: has a binary format that is fast to transmit by being smaller than typical text or native code formats.
 - Modular: programs can be split up in smaller parts that can be transmitted, cached, and consumed separately.
 - **Efficient**: can be decoded, validated, and compiled in a fast single pass, equally with either just-in-time (JIT) or ahead-of-time (AOT) compilation.
 - Streamable: allows decoding, validation, and compilation to begin as soon as possible, before all data has been seen.
 - **Parallelizable**: allows decoding, validation, and compilation to be split into many independent parallel tasks.
 - **Portable**: makes no architectural assumptions that are not broadly supported across modern hardware.

WebAssembly code is also intended to be easy to inspect and debug, especially in environments like web browsers, but such features are beyond the scope of this specification.

1.1.2 **Scope**

At its core, WebAssembly is a *virtual instruction set architecture* (*virtual ISA*). As such, it has many use cases and can be embedded in many different environments. To encompass their variety and enable maximum reuse, the WebAssembly specification is split and layered into several documents.

This document is concerned with the core ISA layer of WebAssembly. It defines the instruction set, binary encoding, validation, and execution semantics, as well as a textual representation. It does not, however, define how WebAssembly programs can interact with a specific environment they execute in, nor how they are invoked from such an environment.

Instead, this specification is complemented by additional documents defining interfaces to specific embedding environments such as the Web. These will each define a WebAssembly *application programming interface (API)* suitable for a given environment.

1.1.3 Security Considerations

WebAssembly provides no ambient access to the computing environment in which code is executed. Any interaction with the environment, such as I/O, access to resources, or operating system calls, can only be performed by invoking *functions* provided by the *embedder* and imported into a WebAssembly *module*. An embedder can establish security policies suitable for a respective environment by controlling or limiting which functional capabilities it makes available for import. Such considerations are an embedder's responsibility and the subject of *API definitions* for a specific environment.

Because WebAssembly is designed to be translated into machine code running directly on the host's hardware, it is potentially vulnerable to side channel attacks on the hardware level. In environments where this is a concern, an embedder may have to put suitable mitigations into place to isolate WebAssembly computations.

1.1.4 Dependencies

WebAssembly depends on two existing standards:

- IEEE 754-2019⁴, for the representation of *floating-point data* and the semantics of respective *numeric operations*.
- Unicode⁵, for the representation of import/export *names* and the *text format*.

However, to make this specification self-contained, relevant aspects of the aforementioned standards are defined and formalized as part of this specification, such as the *binary representation* and *rounding* of floating-point values, and the *value range* and *UTF-8 encoding* of Unicode characters.

Note: The aforementioned standards are the authoritative source of all respective definitions. Formalizations given in this specification are intended to match these definitions. Any discrepancy in the syntax or semantics described is to be considered an error.

1.2 Overview

1.2.1 Concepts

WebAssembly encodes a low-level, assembly-like programming language. This language is structured around the following concepts.

Values WebAssembly provides only four basic *number types*. These are integers and IEEE 754-2019⁶ numbers, each in 32 and 64 bit width. 32 bit integers also serve as Booleans and as memory addresses. The usual operations on these types are available, including the full matrix of conversions between them. There is no distinction between signed and unsigned integer types. Instead, integers are interpreted by respective operations as either unsigned or signed in two's complement representation.

In addition to these basic number types, there is a single 128 bit wide vector type representing different types of packed data. The supported representations are 4 32-bit, or 2 64-bit IEEE 754-2019⁷ numbers, or different widths of packed integer values, specifically 2 64-bit integers, 4 32-bit integers, 8 16-bit integers, or 16 8-bit integers.

Finally, values can consist of opaque *references* that represent pointers towards different sorts of entities. Unlike with other types, their size or representation is not observable.

Instructions The computational model of WebAssembly is based on a *stack machine*. Code consists of sequences of *instructions* that are executed in order. Instructions manipulate values on an implicit *operand stack*⁸ and fall into two main categories. *Simple* instructions perform basic operations on data. They pop arguments from the operand stack and push results back to it. *Control* instructions alter control flow. Control flow is *structured*, meaning it is expressed with well-nested constructs such as blocks, loops, and conditionals. Branches can only target such constructs.

Traps Under some conditions, certain instructions may produce a *trap*, which immediately aborts execution. Traps cannot be handled by WebAssembly code, but are reported to the outside environment, where they typically can be caught.

Functions Code is organized into separate *functions*. Each function takes a sequence of values as parameters and returns a sequence of values as results. Functions can call each other, including recursively, resulting in an implicit call stack that cannot be accessed directly. Functions may also declare mutable *local variables* that are usable as virtual registers.

1.2. Overview 3

⁴ https://ieeexplore.ieee.org/document/8766229

⁵ https://www.unicode.org/versions/latest/

⁶ https://ieeexplore.ieee.org/document/8766229

⁷ https://ieeexplore.ieee.org/document/8766229

⁸ In practice, implementations need not maintain an actual operand stack. Instead, the stack can be viewed as a set of anonymous registers that are implicitly referenced by instructions. The *type system* ensures that the stack height, and thus any referenced register, is always known statically.

- **Tables** A *table* is an array of opaque values of a particular *element type*. It allows programs to select such values indirectly through a dynamic index operand. Currently, the only available element type is an untyped function reference. Thereby, a program can call functions indirectly through a dynamic index into a table. For example, this allows emulating function pointers by way of table indices.
- **Linear Memory** A *linear memory* is a contiguous, mutable array of raw bytes. Such a memory is created with an initial size but can be grown dynamically. A program can load and store values from/to a linear memory at any byte address (including unaligned). Integer loads and stores can specify a *storage size* which is smaller than the size of the respective value type. A trap occurs if an access is not within the bounds of the current memory size.
- **Modules** A WebAssembly binary takes the form of a *module* that contains definitions for functions, tables, and linear memories, as well as mutable or immutable *global variables*. Definitions can also be *imported*, specifying a module/name pair and a suitable type. Each definition can optionally be *exported* under one or more names. In addition to definitions, modules can define initialization data for their memories or tables that takes the form of *segments* copied to given offsets. They can also define a *start function* that is automatically executed.
- **Embedder** A WebAssembly implementation will typically be *embedded* into a *host* environment. This environment defines how loading of modules is initiated, how imports are provided (including host-side definitions), and how exports can be accessed. However, the details of any particular embedding are beyond the scope of this specification, and will instead be provided by complementary, environment-specific API definitions.

1.2.2 Semantic Phases

Conceptually, the semantics of WebAssembly is divided into three phases. For each part of the language, the specification specifies each of them.

- **Decoding** WebAssembly modules are distributed in a *binary format*. *Decoding* processes that format and converts it into an internal representation of a module. In this specification, this representation is modelled by *abstract syntax*, but a real implementation could compile directly to machine code instead.
- **Validation** A decoded module has to be *valid*. Validation checks a number of well-formedness conditions to guarantee that the module is meaningful and safe. In particular, it performs *type checking* of functions and the instruction sequences in their bodies, ensuring for example that the operand stack is used consistently.
- **Execution** Finally, a valid module can be *executed*. Execution can be further divided into two phases:

Instantiation. A module *instance* is the dynamic representation of a module, complete with its own state and execution stack. Instantiation executes the module body itself, given definitions for all its imports. It initializes globals, memories and tables and invokes the module's start function if defined. It returns the instances of the module's exports.

Invocation. Once instantiated, further WebAssembly computations can be initiated by *invoking* an exported function on a module instance. Given the required arguments, that executes the respective function and returns its results.

Instantiation and invocation are operations within the embedding environment.

Structure

2.1 Conventions

WebAssembly is a programming language that has multiple concrete representations (its *binary format* and the *text format*). Both map to a common structure. For conciseness, this structure is described in the form of an *abstract syntax*. All parts of this specification are defined in terms of this abstract syntax.

2.1.1 Grammar Notation

The following conventions are adopted in defining grammar rules for abstract syntax.

- Terminal symbols (atoms) are written in sans-serif font: i32, end.
- Nonterminal symbols are written in italic font: valtype, instr.
- A^n is a sequence of $n \ge 0$ iterations of A.
- A^* is a possibly empty sequence of iterations of A. (This is a shorthand for A^n used where n is not relevant.)
- A^+ is a non-empty sequence of iterations of A. (This is a shorthand for A^n where $n \ge 1$.)
- $A^{?}$ is an optional occurrence of A. (This is a shorthand for A^{n} where $n \leq 1$.)
- Productions are written $sym := A_1 \mid \ldots \mid A_n$.
- Large productions may be split into multiple definitions, indicated by ending the first one with explicit ellipses, $sym ::= A_1 \mid \ldots$, and starting continuations with ellipses, $sym ::= \ldots \mid A_2$.
- Some productions are augmented with side conditions in parentheses, "(if *condition*)", that provide a shorthand for a combinatorial expansion of the production into many separate cases.
- If the same meta variable or non-terminal symbol appears multiple times in a production, then all those occurrences must have the same instantiation. (This is a shorthand for a side condition requiring multiple different variables to be equal.)

2.1.2 Auxiliary Notation

When dealing with syntactic constructs the following notation is also used:

- ϵ denotes the empty sequence.
- |s| denotes the length of a sequence s.
- s[i] denotes the *i*-th element of a sequence s, starting from 0.
- s[i:n] denotes the sub-sequence $s[i] \ldots s[i+n-1]$ of a sequence s.
- s with [i] = A denotes the same sequence as s, except that the i-th element is replaced with A.
- s with $[i:n] = A^n$ denotes the same sequence as s, except that the sub-sequence s[i:n] is replaced with A^n .
- $\operatorname{concat}(s^*)$ denotes the flat sequence formed by concatenating all sequences s_i in s^* .

Moreover, the following conventions are employed:

- The notation x^n , where x is a non-terminal symbol, is treated as a meta variable ranging over respective sequences of x (similarly for x^* , x^+ , x^2).
- When given a sequence x^n , then the occurrences of x in a sequence written $(A_1 \ x \ A_2)^n$ are assumed to be in point-wise correspondence with x^n (similarly for x^* , x^+ , x^7). This implicitly expresses a form of mapping syntactic constructions over a sequence.

Productions of the following form are interpreted as *records* that map a fixed set of fields field_i to "values" A_i , respectively:

$$r ::= \{ \mathsf{field}_1 \ A_1, \mathsf{field}_2 \ A_2, \dots \}$$

The following notation is adopted for manipulating such records:

- r.field denotes the contents of the field component of r.
- r with field = A denotes the same record as r, except that the contents of the field component is replaced with A.
- $r_1 \oplus r_2$ denotes the composition of two records with the same fields of sequences by appending each sequence point-wise:

$$\{ \text{field}_1 A_1^*, \text{field}_2 A_2^*, \dots \} \oplus \{ \text{field}_1 B_1^*, \text{field}_2 B_2^*, \dots \} = \{ \text{field}_1 A_1^* B_1^*, \text{field}_2 A_2^* B_2^*, \dots \}$$

• $\bigoplus r^*$ denotes the composition of a sequence of records, respectively; if the sequence is empty, then all fields of the resulting record are empty.

The update notation for sequences and records generalizes recursively to nested components accessed by "paths" $pth ::= ([...] | .field)^+$:

- s with [i] pth = A is short for s with [i] = (s[i] with pth = A),
- r with field pth = A is short for r with field = (r.field with pth = A),

where r with .field = A is shortened to r with field = A.

2.1.3 Vectors

Vectors are bounded sequences of the form A^n (or A^*), where the A can either be values or complex constructions. A vector can have at most $2^{32} - 1$ elements.

$$vec(A) ::= A^n \text{ (if } n < 2^{32})$$

2.2 Values

WebAssembly programs operate on primitive numeric *values*. Moreover, in the definition of programs, immutable sequences of values occur to represent more complex data, such as text strings or other vectors.

2.2.1 Bytes

The simplest form of value are raw uninterpreted *bytes*. In the abstract syntax they are represented as hexadecimal literals.

$$byte ::= 0x00 | \dots | 0xFF$$

Conventions

- The meta variable b ranges over bytes.
- Bytes are sometimes interpreted as natural numbers n < 256.

2.2.2 Integers

Different classes of *integers* with different value ranges are distinguished by their bit width N and by whether they are unsigned or signed.

$$\begin{array}{lll} uN & ::= & 0 \mid 1 \mid \dots \mid 2^{N} - 1 \\ sN & ::= & -2^{N-1} \mid \dots \mid -1 \mid 0 \mid 1 \mid \dots \mid 2^{N-1} - 1 \\ iN & ::= & uN \end{array}$$

The class iN defines uninterpreted integers, whose signedness interpretation can vary depending on context. In the abstract syntax, they are represented as unsigned values. However, some operations *convert* them to signed based on a two's complement interpretation.

Note: The main integer types occurring in this specification are u32, u64, s32, s64, i8, i16, i32, i64. However, other sizes occur as auxiliary constructions, e.g., in the definition of *floating-point* numbers.

Conventions

- The meta variables m, n, i range over integers.
- Numbers may be denoted by simple arithmetics, as in the grammar above. In order to distinguish arithmetics like 2^N from sequences like $(1)^N$, the latter is distinguished with parentheses.

2.2.3 Floating-Point

Floating-point data represents 32 or 64 bit values that correspond to the respective binary formats of the IEEE 754-2019⁹ standard (Section 3.3).

Every value has a sign and a magnitude. Magnitudes can either be expressed as normal numbers of the form $m_0.m_1m_2...m_M\cdot 2^e$, where e is the exponent and m is the significand whose most significant bit m_0 is 1, or as a subnormal number where the exponent is fixed to the smallest possible value and m_0 is 0; among the subnormals are positive and negative zero values. Since the significands are binary values, normals are represented in the form $(1+m\cdot 2^{-M})\cdot 2^e$, where M is the bit width of m; similarly for subnormals.

2.2. Values 7

⁹ https://ieeexplore.ieee.org/document/8766229

Possible magnitudes also include the special values ∞ (infinity) and nan (NaN, not a number). NaN values have a payload that describes the mantissa bits in the underlying binary representation. No distinction is made between signalling and quiet NaNs.

$$\begin{array}{lll} fN & ::= & +fNmag \mid -fNmag \\ fNmag & ::= & (1+uM\cdot 2^{-M})\cdot 2^e & (\text{if } -2^{E-1}+2 \leq e \leq 2^{E-1}-1) \\ & \mid & (0+uM\cdot 2^{-M})\cdot 2^e & (\text{if } e=-2^{E-1}+2) \\ & \mid & \infty \\ & \mid & \mathsf{nan}(n) & (\text{if } 1 \leq n < 2^M) \end{array}$$

where $M = \operatorname{signif}(N)$ and $E = \operatorname{expon}(N)$ with

$$signif(32) = 23$$
 $expon(32) = 8$
 $signif(64) = 52$ $expon(64) = 11$

A canonical NaN is a floating-point value $\pm nan(canon_N)$ where $canon_N$ is a payload whose most significant bit is 1 while all others are 0:

$$\operatorname{canon}_N = 2^{\operatorname{signif}(N) - 1}$$

An arithmetic NaN is a floating-point value $\pm nan(n)$ with $n \ge canon_N$, such that the most significant bit is 1 while all others are arbitrary.

Note: In the abstract syntax, subnormals are distinguished by the leading 0 of the significand. The exponent of subnormals has the same value as the smallest possible exponent of a normal number. Only in the *binary representation* the exponent of a subnormal is encoded differently than the exponent of any normal number.

Conventions

• The meta variable z ranges over floating-point values where clear from context.

2.2.4 Vectors

Numeric vectors are 128-bit values that are processed by vector instructions (also known as *SIMD* instructions, single instruction multiple data). They are represented in the abstract syntax using *i128*. The interpretation of lane types (*integer* or *floating-point* numbers) and lane sizes are determined by the specific instruction operating on them.

2.2.5 Names

Names are sequences of characters, which are scalar values as defined by Unicode¹⁰ (Section 2.4).

```
\begin{array}{lll} \textit{name} & ::= & \textit{char*} & (\text{if } | \text{utf8}(\textit{char*})| < 2^{32}) \\ \textit{char} & ::= & \text{U} + 00 \mid \ldots \mid \text{U} + \text{D7FF} \mid \text{U} + \text{E000} \mid \ldots \mid \text{U} + 10\text{FFFF} \end{array}
```

Due to the limitations of the binary format, the length of a name is bounded by the length of its UTF-8 encoding.

¹⁰ https://www.unicode.org/versions/latest/

Convention

• Characters (Unicode scalar values) are sometimes used interchangeably with natural numbers n < 1114112.

2.3 Types

Various entities in WebAssembly are classified by types. Types are checked during *validation*, *instantiation*, and possibly *execution*.

2.3.1 Number Types

Number types classify numeric values.

$$numtype ::= i32 | i64 | f32 | f64$$

The types i32 and i64 classify 32 and 64 bit integers, respectively. Integers are not inherently signed or unsigned, their interpretation is determined by individual operations.

The types f32 and f64 classify 32 and 64 bit floating-point data, respectively. They correspond to the respective binary floating-point representations, also known as *single* and *double* precision, as defined by the IEEE 754-2019¹¹ standard (Section 3.3).

Number types are *transparent*, meaning that their bit patterns can be observed. Values of number type can be stored in *memories*.

Conventions

• The notation |t| denotes the *bit width* of a number type t. That is, |i32| = |f32| = 32 and |i64| = |f64| = 64.

2.3.2 Vector Types

Vector types classify vectors of *numeric* values processed by vector instructions (also known as *SIMD* instructions, single instruction multiple data).

$$vectype ::= v128$$

The type v128 corresponds to a 128 bit vector of packed integer or floating-point data. The packed data can be interpreted as signed or unsigned integers, single or double precision floating-point values, or a single 128 bit type. The interpretation is determined by individual operations.

Vector types, like *number types* are *transparent*, meaning that their bit patterns can be observed. Values of vector type can be stored in *memories*.

Conventions

• The notation |t| for *bit width* extends to vector types as well, that is, |v128| = 128.

2.3. Types 9

¹¹ https://ieeexplore.ieee.org/document/8766229

2.3.3 Heap Types

Heap types classify objects in the runtime store.

```
heaptype ::= func | extern | typeidx
```

The type func denotes the infinite union of all types of functions, regardless of their concrete function types.

The type extern denotes the infinite union of all objects owned by the *embedder* and that can be passed into WebAssembly under this type.

A concrete heap type consists of a type index and classifies an object of the respective type defined in the module.

2.3.4 Reference Types

Reference types classify values that are first-class references to objects in the runtime store.

A reference type is characterised by the *heap type* it points to.

In addition, a reference type of the form refnullht is nullable, meaning that it can either be a proper reference to ht or null. Other references are non-null.

Reference types are *opaque*, meaning that neither their size nor their bit pattern can be observed. Values of reference type can be stored in *tables*.

2.3.5 Value Types

Value types classify the individual values that WebAssembly code can compute with and the values that a variable accepts. They are either *number types*, *vector types*, *reference types*, or the unique *bottom type*, written bot.

The type bot is a *subtype* of all other types. By virtue of being representable in neither the *binary format* nor the *text format*, it cannot be used in a program; it only occurs during *validation*, as a possible operand type for instructions.

$$valtype ::= numtype \mid vectype \mid reftype \mid bot$$

Conventions

• The meta variable t ranges over value types or subclasses thereof where clear from context.

2.3.6 Result Types

Result types classify the result of executing instructions or functions, which is a sequence of values, written with brackets.

```
result type ::= [vec(valtype)]
```

2.3.7 Instruction Types

Instruction types classify the behaviour of *instructions* or instruction sequences, by describing how they manipulate the *operand stack* and the initialization status of *locals*:

```
instrtype ::= resulttype \rightarrow localidx* resulttype
```

An instruction type $[t_1^*] \to {}_{x^*}[t_2^*]$ describes the required input stack with argument values of types t_1^* that an instruction pops off and the provided output stack with result values of types t_2^* that it pushes back. Moreover, it enumerates the *indices* x^* of locals that have been set by the instruction or sequence.

Note: Instruction types are only used for *validation*, they do not occur in programs.

2.3.8 Local Types

Local types classify locals, by describing their value type as well as their initialization status:

```
init ::= set | unset local type ::= init val type
```

Note: Local types are only used for *validation*, they do not occur in programs.

2.3.9 Function Types

Function types classify the signature of *functions*, mapping a vector of parameters to a vector of results. They are also used to classify the inputs and outputs of *instructions*.

```
functype ::= resulttype \rightarrow resulttype
```

2.3.10 Limits

Limits classify the size range of resizeable storage associated with memory types and table types.

```
limits ::= \{\min u32, \max u32^?\}
```

If no maximum is given, the respective storage can grow to any size.

2.3.11 Memory Types

Memory types classify linear *memories* and their size range.

```
memtype ::= limits
```

The limits constrain the minimum and optionally the maximum size of a memory. The limits are given in units of *page size*.

2.3. Types 11

2.3.12 Table Types

Table types classify tables over elements of reference type within a size range.

```
table type ::= limits \ reftype
```

Like memories, tables are constrained by limits for their minimum and optionally maximum size. The limits are given in numbers of entries.

Note: In future versions of WebAssembly, additional element types may be introduced.

2.3.13 Global Types

Global types classify global variables, which hold a value and can either be mutable or immutable.

```
globaltype ::= mut \ valtype
mut ::= const | var
```

2.3.14 External Types

External types classify imports and external values with their respective types.

```
externtype ::= func functype | table tabletype | mem memtype | global globaltype
```

Conventions

The following auxiliary notation is defined for sequences of external types. It filters out entries of a specific kind in an order-preserving fashion:

```
• funcs(externtype^*) = [functype | (func functype) \in externtype^*]
```

- tables($externtype^*$) = $[tabletype \mid (table tabletype) \in externtype^*]$
- $mems(externtype^*) = [memtype \mid (mem memtype) \in externtype^*]$
- $globals(externtype^*) = [globaltype \mid (global globaltype) \in externtype^*]$

2.4 Instructions

12

WebAssembly code consists of sequences of *instructions*. Its computational model is based on a *stack machine* in that instructions manipulate values on an implicit *operand stack*, consuming (popping) argument values and producing or returning (pushing) result values.

In addition to dynamic operands from the stack, some instructions also have static *immediate* arguments, typically *indices* or type annotations, which are part of the instruction itself.

Some instructions are structured in that they bracket nested sequences of instructions.

The following sections group instructions into a number of different categories.

2.4.1 Numeric Instructions

Numeric instructions provide basic operations over numeric *values* of specific *type*. These operations closely match respective operations available in hardware.

```
nn, mm ::= 32 \mid 64
          ::= u \mid s
instr
          ::= inn.const inn | fnn.const fnn
               inn.iunop \mid fnn.funop
               inn.ibinop \mid fnn.fbinop
               inn.itestop
               inn.irelop | fnn.frelop
               inn.extend8_s | inn.extend16_s | i64.extend32_s
               i32.wrap_i64 | i64.extend_i32_sx | inn.trunc_fmm_sx
               inn.trunc sat fmm sx
               f32.demote_f64 | f64.promote_f32 | fnn.convert_imm_sx
               inn.reinterpret_fnn \mid fnn.reinterpret_inn
iunop
          ::= clz | ctz | popcnt
ibinop
          ::= add | sub | mul | div_sx | rem_sx
               and or xor shl shr_sx rotl rotr
          ::= abs | neg | sqrt | ceil | floor | trunc | nearest
funop
          ::= add | sub | mul | div | min | max | copysign
fbinop
itestop
          ::=
               eaz
irelop
               eq | ne | lt_sx | gt_sx | le_sx | ge_sx
          ::=
frelop
          ::= eq | ne | lt | gt | le | ge
```

Numeric instructions are divided by *number type*. For each type, several subcategories can be distinguished:

- Constants: return a static constant.
- *Unary Operations*: consume one operand and produce one result of the respective type.
- Binary Operations: consume two operands and produce one result of the respective type.
- Tests: consume one operand of the respective type and produce a Boolean integer result.
- Comparisons: consume two operands of the respective type and produce a Boolean integer result.
- *Conversions*: consume a value of one type and produce a result of another (the source type of the conversion is the one after the "_").

Some integer instructions come in two flavors, where a signedness annotation sx distinguishes whether the operands are to be *interpreted* as *unsigned* or *signed* integers. For the other integer instructions, the use of two's complement for the signed interpretation means that they behave the same regardless of signedness.

Conventions

Occasionally, it is convenient to group operators together according to the following grammar shorthands:

```
\begin{array}{llll} unop & ::= & iunop \mid funop \mid extend N\_s \\ binop & ::= & ibinop \mid fbinop \\ testop & ::= & itestop \\ relop & ::= & irelop \mid frelop \\ cvtop & ::= & wrap \mid extend \mid trunc \mid trunc\_sat \mid convert \mid demote \mid promote \mid reinterpret \\ \end{array}
```

2.4. Instructions



2.4.2 Vector Instructions

Vector instructions (also known as SIMD instructions, single data multiple value) provide basic operations over values of vector type.

```
ishape
                        i8x16 | i16x8 | i32x4 | i64x2
                  ::=
   fshape
                        f32x4 | f64x2
                  ::=
   shape
                        ishape | fshape
                  ::=
   half
                  ::=
                        low | high
   laneidx
                  ::=
                        u8
   instr
                  ::=
                        v128.const i128
                        v128.vvunop
                        v128.vvbinop
                        v128.vvternop
                        v128.vvtestop
                        i8x16.shuffle laneidx^{16}
                        i8x16.swizzle
                        shape.splat
                        i8x16.extract_lane_sx laneidx | i16x8.extract_lane_sx laneidx
                        i32x4.extract_lane\ laneidx\ |\ i64x2.extract_lane\ laneidx
                        fshape.extract lane laneidx
                        shape.replace_lane laneidx
                        i8x16.virelop | i16x8.virelop | i32x4.virelop
                        i64x2.eq | i64x2.ne | i64x2.lt_s | i64x2.gt_s | i64x2.le_s | i64x2.ge_s
                        fshape.vfrelop
                        ishape.viunop | i8x16.popcnt
                        i16x8.q15mulr_sat_s
                        i32x4.dot_i16x8_s
                        fshape.vfunop
                        is hape.vitestop\\
                        ishape.bitmask
                        i8x16.narrow_i16x8_sx | i16x8.narrow_i32x4_sx
                        i16x8.extend half i8x16 sx | i32x4.extend half i16x8 sx
                        i64x2.extend\_half\_i32x4\_sx
                        ishape.vishiftop
                        ishape.vibinop
                        i8x16.viminmaxop | i16x8.viminmaxop | i32x4.viminmaxop
                        i8x16.visatbinop \mid i16x8.visatbinop
                        i16x8.mul | i32x4.mul | i64x2.mul
                        i8x16.avgr u | i16x8.avgr u
                        i16x8.extmul\_half\_i8x16\_sx \mid i32x4.extmul\_half\_i16x8\_sx \mid i64x2.extmul\_half\_i32x4\_sx
                        i16x8.extadd_pairwise_i8x16_sx | i32x4.extadd_pairwise_i16x8_sx
                        fshape.vfbinop
                        i32x4.trunc sat f32x4 sx | i32x4.trunc sat f64x2 sx zero
                        f32x4.convert_i32x4_sx | f32x4.demote_f64x2 zero
                        f64x2.convert_low_i32x4_sx | f64x2.promote_low_f32x4
                        . . .
   vvunop
                        not
                  ::=
                        and | andnot | or | xor
   vvbinop
                  ::=
   vvternop
                  ::=
                        bitselect
   vvtestop
                  ::=
                        any_true
   vitestop
                  ::=
                        all true
   virelop
                  ::= eq | ne | lt_sx | gt_sx | le_sx | ge_sx
                  ::= eq | ne | It | gt | le | ge
   vfrelop
   viunop
                        abs | neg
                  ::=
                        add | sub
   vibinop
                  ::=
   vimin max op
                        min\_sx \mid max\_sx
                  ::=
                        add_sat_sx \mid sub_sat_sx
   visatbinop
                  ::=
   vishiftop
                        shl shr sx
                   ::=
    vfunop
                        abs | neg | sqrt | ceil | floor | trunc | nearest
2.4. Instructions
                                                                                                           15
                        add | sub | mul | div | min | max | pmin | pmax
```

Vector instructions have a naming convention involving a prefix that determines how their operands will be interpreted. This prefix describes the *shape* of the operand, written $t \times N$, and consisting of a packed *numeric type t* and the number of *lanes N* of that type. Operations are performed point-wise on the values of each lane.

Note: For example, the shape i32x4 interprets the operand as four i32 values, packed into an i128. The bitwidth of the numeric type t times N always is 128.

Instructions prefixed with v128 do not involve a specific interpretation, and treat the v128 as an i128 value or a vector of 128 individual bits.

Vector instructions can be grouped into several subcategories:

- Constants: return a static constant.
- Unary Operations: consume one v128 operand and produce one v128 result.
- Binary Operations: consume two v128 operands and produce one v128 result.
- Ternary Operations: consume three v128 operands and produce one v128 result.
- Tests: consume one v128 operand and produce a Boolean integer result.
- Shifts: consume a v128 operand and a i32 operand, producing one v128 result.
- Splats: consume a value of numeric type and produce a v128 result of a specified shape.
- Extract lanes: consume a v128 operand and return the numeric value in a given lane.
- Replace lanes: consume a v128 operand and a numeric value for a given lane, and produce a v128 result.

Some vector instructions have a signedness annotation sx which distinguishes whether the elements in the operands are to be *interpreted* as *unsigned* or *signed* integers. For the other vector instructions, the use of two's complement for the signed interpretation means that they behave the same regardless of signedness.

Conventions

Occasionally, it is convenient to group operators together according to the following grammar shorthands:

```
\begin{array}{llll} vunop & ::= & viunop \mid vfunop \mid \mathsf{popcnt} \\ vbinop & ::= & vibinop \mid vfbinop \\ & \mid & viminmaxop \mid visatbinop \\ & \mid & \mathsf{mul} \mid \mathsf{avgr\_u} \mid \mathsf{q15mulr\_sat\_s} \\ vtestop & ::= & vitestop \\ vrelop & ::= & virelop \mid vfrelop \\ vcvtop & ::= & \mathsf{extend} \mid \mathsf{trunc\_sat} \mid \mathsf{convert} \mid \mathsf{demote} \mid \mathsf{promote} \end{array}
```

2.4.3 Reference Instructions

Instructions in this group are concerned with accessing references.

The first three of these instruction produce a *null* value, produce a reference to a given function, or check for a null value, respectively. The ref.as_non_null casts a *nullable* to a non-null one, and *traps* if it encounters null.

2.4.4 Parametric Instructions

Instructions in this group can operate on operands of any value type.

```
instr ::= \dots
| drop
| select (valtype^*)^?
```

The drop instruction simply throws away a single operand.

The select instruction selects one of its first two operands based on whether its third operand is zero or not. It may include a *value type* determining the type of these operands. If missing, the operands must be of *numeric type*.

Note: In future versions of WebAssembly, the type annotation on select may allow for more than a single value being selected at the same time.

2.4.5 Variable Instructions

Variable instructions are concerned with access to *local* or *global* variables.

These instructions get or set the values of variables, respectively. The local tee instruction is like local set but also returns its argument.

2.4.6 Table Instructions

Instructions in this group are concerned with tables table.

The table.get and table.set instructions load or store an element in a table, respectively.

The table.size instruction returns the current size of a table. The table.grow instruction grows table by a given delta and returns the previous size, or -1 if enough space cannot be allocated. It also takes an initialization value for the newly allocated entries.

The table.fill instruction sets all entries in a range to a given value.

The table.copy instruction copies elements from a source table region to a possibly overlapping destination region; the first index denotes the destination. The table.init instruction copies elements from a *passive element segment* into a table. The elem.drop instruction prevents further use of a passive element segment. This instruction is intended to be used as an optimization hint. After an element segment is dropped its elements can no longer be retrieved, so the memory used by this segment may be freed.

An additional instruction that accesses a table is the *control instruction* call indirect.

2.4. Instructions

2.4.7 Memory Instructions

Instructions in this group are concerned with linear memory.

```
{offset u32, align u32}
memarg
         ::=
              8 | 16 | 32 | 64
ww
          ::=
instr
               inn.load memarg | fnn.load memarg | v128.load memarg
               inn.store memarg | fnn.store memarg | v128.store memarg
               inn.load8_sx memarg | inn.load16_sx memarg | i64.load32_sx memarg
               inn.store8 memarg | inn.store16 memarg | i64.store32 memarg
               v128.load8x8_sx memarg | v128.load16x4_sx memarg | v128.load32x2_sx memarg
               v128.load32_zero memarg | v128.load64_zero memarg
              v128.load ww_splat memarg
              v128.load ww_lane memarg laneidx | v128.storeww_lane memarg laneidx
               memory.size
               memory.grow
               memory.fill
               memory.copy
               memory.init dataidx
               data.drop dataidx
```

Memory is accessed with load and store instructions for the different *number types*. They all take a *memory immediate memarg* that contains an address *offset* and the expected *alignment* (expressed as the exponent of a power of 2). Integer loads and stores can optionally specify a *storage size* that is smaller than the *bit width* of the respective value type. In the case of loads, a sign extension mode sx is then required to select appropriate behavior.

Vector loads can specify a shape that is half the *bit width* of v128. Each lane is half its usual size, and the sign extension mode sx then specifies how the smaller lane is extended to the larger lane. Alternatively, vector loads can perform a splat, such that only a single lane of the specified storage size is loaded, and the result is duplicated to all lanes.

The static address offset is added to the dynamic address operand, yielding a 33 bit *effective address* that is the zero-based index at which the memory is accessed. All values are read and written in little endian¹² byte order. A *trap* results if any of the accessed memory bytes lies outside the address range implied by the memory's current size.

Note: Future versions of WebAssembly might provide memory instructions with 64 bit address ranges.

The memory.size instruction returns the current size of a memory. The memory.grow instruction grows memory by a given delta and returns the previous size, or -1 if enough memory cannot be allocated. Both instructions operate in units of *page size*.

The memory.fill instruction sets all values in a region to a given byte. The memory.copy instruction copies data from a source memory region to a possibly overlapping destination region. The memory.init instruction copies data from a *passive data segment* into a memory. The data.drop instruction prevents further use of a passive data segment. This instruction is intended to be used as an optimization hint. After a data segment is dropped its data can no longer be retrieved, so the memory used by this segment may be freed.

Note: In the current version of WebAssembly, all memory instructions implicitly operate on *memory index* 0. This restriction may be lifted in future versions.

¹² https://en.wikipedia.org/wiki/Endianness#Little-endian

2.4.8 Control Instructions

Instructions in this group affect the flow of control.

```
blocktype ::= typeidx \mid valtype?
instr
            ::=
                 nop
                  unreachable
                  block blocktype\ instr^* end
                  loop blocktype instr* end
                  if blocktype instr* else instr* end
                  br labelidx
                  br_if\ labelidx
                  br_table vec(labelidx) labelidx
                  br on null labelidx
                  br_on_non_null\ labelidx
                  return
                  call funcidx
                  call ref
                  call indirect tableidx typeidx
```

The nop instruction does nothing.

The unreachable instruction causes an unconditional *trap*.

The block, loop and if instructions are *structured* instructions. They bracket nested sequences of instructions, called *blocks*, terminated with, or separated by, end or else pseudo-instructions. As the grammar prescribes, they must be well-nested.

A structured instruction can consume *input* and produce *output* on the operand stack according to its annotated *block type*. It is given either as a *type index* that refers to a suitable *function type*, or as an optional *value type* inline, which is a shorthand for the function type $[] \rightarrow [valtype^?]$.

Each structured control instruction introduces an implicit *label*. Labels are targets for branch instructions that reference them with *label indices*. Unlike with other *index spaces*, indexing of labels is relative by nesting depth, that is, label 0 refers to the innermost structured control instruction enclosing the referring branch instruction, while increasing indices refer to those farther out. Consequently, labels can only be referenced from *within* the associated structured control instruction. This also implies that branches can only be directed outwards, "breaking" from the block of the control construct they target. The exact effect depends on that control construct. In case of block or if it is a *forward jump*, resuming execution after the matching end. In case of loop it is a *backward jump* to the beginning of the loop.

Note: This enforces *structured control flow*. Intuitively, a branch targeting a block or if behaves like a break statement in most C-like languages, while a branch targeting a loop behaves like a continue statement.

Branch instructions come in several flavors: br performs an unconditional branch, br_if performs a conditional branch, and br_table performs an indirect branch through an operand indexing into the label vector that is an immediate to the instruction, or to a default target if the operand is out of bounds. The br_on_null and br_on_non_null instructions check whether a reference operand is *null* and branch if that is the case or not the case, respectively. The return instruction is a shortcut for an unconditional branch to the outermost block, which implicitly is the body of the current function. Taking a branch *unwinds* the operand stack up to the height where the targeted structured control instruction was entered. However, branches may additionally consume operands themselves, which they push back on the operand stack after unwinding. Forward branches require operands according to the output of the targeted block's type, i.e., represent the values produced by the terminated block. Backward branches require operands according to the input of the targeted block's type, i.e., represent the values consumed by the restarted block.

The call instruction invokes another *function*, consuming the necessary arguments from the stack and returning the result values of the call. The call_ref instruction invokes a function indirectly through a *function reference* operand. The call_indirect instruction calls a function indirectly through an operand indexing into a *table* that is denoted

2.4. Instructions

by a *table index* and must contain *function references*. Since it may contain functions of heterogeneous type, the callee is dynamically checked against the *function type* indexed by the instruction's second immediate, and the call is aborted with a *trap* if it does not match.

2.4.9 Expressions

Function bodies, initialization values for *globals*, and offsets of *element* or *data* segments are given as expressions, which are sequences of *instructions* terminated by an end marker.

```
expr ::= instr^* end
```

In some places, validation *restricts* expressions to be *constant*, which limits the set of allowable instructions.

2.5 Modules

WebAssembly programs are organized into *modules*, which are the unit of deployment, loading, and compilation. A module collects definitions for *types*, *functions*, *tables*, *memories*, and *globals*. In addition, it can declare *imports* and *exports* and provide initialization in the form of *data* and *element* segments, or a *start function*.

```
module ::= \{ types \ vec(functype), \\ funcs \ vec(func), \\ tables \ vec(table), \\ mems \ vec(mem), \\ globals \ vec(global), \\ elems \ vec(elem), \\ datas \ vec(data), \\ start \ start^2, \\ imports \ vec(import), \\ exports \ vec(export) \}
```

Each of the vectors – and thus the entire module – may be empty.

2.5.1 Indices

Definitions are referenced with zero-based *indices*. Each class of definition has its own *index space*, as distinguished by the following classes.

```
typeidx
        ::= u32
funcidx
       ::= u32
tableidx ::=
             u32
memidx
        ::= u32
globalidx ::= u32
elemidx ::= u32
dataidx
       ::= u32
localidx
       ::= u32
labelidx
            u32
        ::=
```

The index space for *functions*, *tables*, *memories* and *globals* includes respective *imports* declared in the same module. The indices of these imports precede the indices of other definitions in the same index space.

Element indices reference *element segments* and data indices reference *data segments*.

The index space for *locals* is only accessible inside a *function* and includes the parameters of that function, which precede the local variables.

Label indices reference structured control instructions inside an instruction sequence.

Conventions

- The meta variable *l* ranges over label indices.
- The meta variables x, y range over indices in any of the other index spaces.
- The notation idx(A) denotes the set of indices from index space idx occurring free in A. We sometimes reinterpret this set as the *vector* of its elements.

Note: For example, if $instr^*$ is $(data.drop\ x)(memory.init\ y)$, then $dataidx(instr^*) = \{x,y\}$, or equivalently, the vector $x\ y$.

2.5.2 Types

The types component of a module defines a vector of function types.

All function types used in a module must be defined in this component. They are referenced by type indices.

Note: Future versions of WebAssembly may add additional forms of type definitions.

2.5.3 Functions

The funcs component of a module defines a vector of functions with the following structure:

```
func ::= \{ type \ typeidx, locals \ vec(local), body \ expr \} \ local ::= \{ type \ valtype \}
```

The type of a function declares its signature by reference to a *type* defined in the module. The parameters of the function are referenced through 0-based *local indices* in the function's body; they are mutable.

The locals declare a vector of mutable local variables and their types. These variables are referenced through *local indices* in the function's body. The index of the first local is the smallest index not referencing a parameter.

The body is an *instruction* sequence that upon termination must produce a stack matching the function type's *result type*.

Functions are referenced through *function indices*, starting with the smallest index not referencing a function *import*.

2.5.4 Tables

The tables component of a module defines a vector of tables described by their table type:

```
table ::= \{type \ table type\}
```

A table is a vector of opaque values of a particular *reference type*. The min size in the *limits* of the table type specifies the initial size of that table, while its max, if present, restricts the size to which it can grow later.

Tables can be initialized through element segments.

Tables are referenced through *table indices*, starting with the smallest index not referencing a table *import*. Most constructs implicitly reference table index 0.

2.5. Modules 21

2.5.5 Memories

The mems component of a module defines a vector of *linear memories* (or *memories* for short) as described by their *memory type*:

```
mem ::= \{type \ mem type\}
```

A memory is a vector of raw uninterpreted bytes. The min size in the *limits* of the memory type specifies the initial size of that memory, while its max, if present, restricts the size to which it can grow later. Both are in units of *page size*.

Memories can be initialized through data segments.

Memories are referenced through *memory indices*, starting with the smallest index not referencing a memory *import*. Most constructs implicitly reference memory index 0.

Note: In the current version of WebAssembly, at most one memory may be defined or imported in a single module, and *all* constructs implicitly reference this memory 0. This restriction may be lifted in future versions.

2.5.6 Globals

The globals component of a module defines a vector of global variables (or globals for short):

```
global ::= \{type \ global \ type, init \ expr\}
```

Each global stores a single value of the given *global type*. Its type also specifies whether a global is immutable or mutable. Moreover, each global is initialized with an init value given by a *constant* initializer *expression*.

Globals are referenced through global indices, starting with the smallest index not referencing a global import.

2.5.7 Element Segments

The initial contents of a table is uninitialized. *Element segments* can be used to initialize a subrange of a table from a static *vector* of elements.

The elems component of a module defines a vector of element segments. Each element segment defines a *reference type* and a corresponding list of *constant* element *expressions*.

Element segments have a mode that identifies them as either *passive*, *active*, or *declarative*. A passive element segment's elements can be copied to a table using the table.init instruction. An active element segment copies its elements into a table during *instantiation*, as specified by a *table index* and a *constant expression* defining an offset into that table. A declarative element segment is not available at runtime but merely serves to forward-declare references that are formed in code with instructions like ref.func.

```
\begin{array}{lll} elem & ::= & \{ \text{type } reftype, \text{init } vec(expr), \text{mode } elemmode \} \\ elemmode & ::= & \text{passive} \\ & | & \text{active } \{ \text{table } tableidx, \text{offset } expr \} \\ & | & \text{declarative} \end{array}
```

The offset is given by a *constant expression*.

Element segments are referenced through *element indices*.

Note: In the current version of WebAssembly, only tables whose elements are *function references* can be initialized with an element segment. This limitation may be lifted in the future.

2.5.8 Data Segments

The initial contents of a *memory* are zero bytes. *Data segments* can be used to initialize a range of memory from a static *vector* of *bytes*.

The datas component of a module defines a vector of data segments.

Like element segments, data segments have a mode that identifies them as either *passive* or *active*. A passive data segment's contents can be copied into a memory using the memory init instruction. An active data segment copies its contents into a memory during *instantiation*, as specified by a *memory index* and a *constant expression* defining an offset into that memory.

```
\begin{array}{ll} \textit{data} & ::= & \{ \text{init } \textit{vec(byte)}, \text{mode } \textit{datamode} \} \\ \textit{datamode} & ::= & \text{passive} \\ & | & \text{active } \{ \text{memory } \textit{memidx}, \text{ offset } \textit{expr} \} \end{array}
```

Data segments are referenced through data indices.

Note: In the current version of WebAssembly, at most one memory is allowed in a module. Consequently, the only valid *memidx* is 0.

2.5.9 Start Function

The start component of a module declares the *function index* of a *start function* that is automatically invoked when the module is *instantiated*, after *tables* and *memories* have been initialized.

```
start ::= \{func funcidx\}
```

Note: The start function is intended for initializing the state of a module. The module and its exports are not accessible before this initialization has completed.

2.5.10 Exports

The exports component of a module defines a set of *exports* that become accessible to the host environment once the module has been *instantiated*.

```
\begin{array}{lll} export & ::= & \{ name \ name, desc \ export desc \} \\ export desc & ::= & func \ funcidx \\ & | & table \ table idx \\ & | & mem \ mem idx \\ & | & global \ global idx \end{array}
```

Each export is labeled by a unique *name*. Exportable definitions are *functions*, *tables*, *memories*, and *globals*, which are referenced through a respective descriptor.

Conventions

The following auxiliary notation is defined for sequences of exports, filtering out indices of a specific kind in an order-preserving fashion:

```
funcs(export*) = [funcidx | func funcidx ∈ (export.desc)*]
tables(export*) = [tableidx | table tableidx ∈ (export.desc)*]
mems(export*) = [memidx | mem memidx ∈ (export.desc)*]
globals(export*) = [globalidx | global globalidx ∈ (export.desc)*]
```

2.5. Modules 23

2.5.11 Imports

The imports component of a module defines a set of *imports* that are required for *instantiation*.

```
\begin{array}{lll} import & ::= & \{ module \ name, name \ name, desc \ import desc \} \\ import desc & ::= & func \ typeidx \\ & | & table \ table type \\ & | & mem \ mem type \\ & | & global \ global type \end{array}
```

Each import is labeled by a two-level *name* space, consisting of a module name and a name for an entity within that module. Importable definitions are *functions*, *tables*, *memories*, and *globals*. Each import is specified by a descriptor with a respective type that a definition provided during instantiation is required to match.

Every import defines an index in the respective *index space*. In each index space, the indices of imports go before the first index of any definition contained in the module itself.

Note: Unlike export names, import names are not necessarily unique. It is possible to import the same module/name pair multiple times; such imports may even have different type descriptions, including different kinds of entities. A module with such imports can still be instantiated depending on the specifics of how an *embedder* allows resolving and supplying imports. However, embedders are not required to support such overloading, and a WebAssembly module itself cannot implement an overloaded name.

CHAPTER 3

Validation

3.1 Conventions

Validation checks that a WebAssembly module is well-formed. Only valid modules can be instantiated.

Validity is defined by a *type system* over the *abstract syntax* of a *module* and its contents. For each piece of abstract syntax, there is a typing rule that specifies the constraints that apply to it. All rules are given in two *equivalent* forms:

- 1. In prose, describing the meaning in intuitive form.
- 2. In *formal notation*, describing the rule in mathematical form. ¹³

Note: The prose and formal rules are equivalent, so that understanding of the formal notation is *not* required to read this specification. The formalism offers a more concise description in notation that is used widely in programming languages semantics and is readily amenable to mathematical proof.

In both cases, the rules are formulated in a *declarative* manner. That is, they only formulate the constraints, they do not define an algorithm. The skeleton of a sound and complete algorithm for type-checking instruction sequences according to this specification is provided in the *appendix*.

3.1.1 Contexts

Validity of an individual definition is specified relative to a *context*, which collects relevant information about the surrounding *module* and the definitions in scope:

- *Types*: the list of types defined in the current module.
- Functions: the list of functions declared in the current module, represented by their function type.
- Tables: the list of tables declared in the current module, represented by their table type.
- Memories: the list of memories declared in the current module, represented by their memory type.
- Globals: the list of globals declared in the current module, represented by their global type.

¹³ The semantics is derived from the following article: Andreas Haas, Andreas Rossberg, Derek Schuff, Ben Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman. Bringing the Web up to Speed with WebAssembly¹⁴. Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017). ACM 2017.

¹⁴ https://dl.acm.org/citation.cfm?doid=3062341.3062363

- *Element Segments*: the list of element segments declared in the current module, represented by their element type.
- Data Segments: the list of data segments declared in the current module, each represented by an ok entry.
- *Locals*: the list of locals declared in the current function (including parameters), represented by their local type.
- Labels: the stack of labels accessible from the current position, represented by their result type.
- *Return*: the return type of the current function, represented as an optional result type that is absent when no return is allowed, as in free-standing expressions.
- References: the list of function indices that occur in the module outside functions and can hence be used to form references inside them.

In other words, a context contains a sequence of suitable *types* for each *index space*, describing each defined entry in that space. Locals, labels and return type are only used for validating *instructions* in *function bodies*, and are left empty elsewhere. The label stack is the only part of the context that changes as validation of an instruction sequence proceeds.

More concretely, contexts are defined as records C with abstract syntax:

```
C ::= \{ \text{ types }
                      functype^*,
            funcs
                     functype^*
            tables table type^*.
            mems memtype^*.
            globals globaltype*.
                      reftype^*,
            elems
            datas
                     ok*,
            locals
                     local type^*,
            labels
                     result type*
            return
                     resulttype?
            refs
                      funcidx^*
```

In addition to field access written C field the following notation is adopted for manipulating contexts:

- When spelling out a context, empty fields are omitted.
- C, field A^* denotes the same context as C but with the elements A^* prepended to its field component sequence.

Note: We use *indexing notation* like C.labels[i] to look up indices in their respective *index space* in the context. Context extension notation C, field A is primarily used to locally extend *relative* index spaces, such as *label indices*. Accordingly, the notation is defined to append at the *front* of the respective sequence, introducing a new relative index 0 and shifting the existing ones.

3.1.2 Prose Notation

Validation is specified by stylised rules for each relevant part of the *abstract syntax*. The rules not only state constraints defining when a phrase is valid, they also classify it with a type. The following conventions are adopted in stating these rules.

• A phrase A is said to be "valid with type T" if and only if all constraints expressed by the respective rules are met. The form of T depends on what A is.

Note: For example, if A is a function, then T is a function type; for an A that is a global, T is a global type; and so on.

• The rules implicitly assume a given *context C*.

• In some places, this context is locally extended to a context C' with additional entries. The formulation "Under context C', ... statement ..." is adopted to express that the following statement must apply under the assumptions embodied in the extended context.

3.1.3 Formal Notation

Note: This section gives a brief explanation of the notation for specifying typing rules formally. For the interested reader, a more thorough introduction can be found in respective text books. ¹⁵

The proposition that a phrase A has a respective type T is written A:T. In general, however, typing is dependent on a context C. To express this explicitly, the complete form is a *judgement* $C \vdash A:T$, which says that A:T holds under the assumptions encoded in C.

The formal typing rules use a standard approach for specifying type systems, rendering them into *deduction rules*. Every rule has the following general form:

$$\frac{premise_1}{conclusion} \quad \frac{premise_2}{conclusion} \quad \dots \quad \frac{premise_n}{conclusion}$$

Such a rule is read as a big implication: if all premises hold, then the conclusion holds. Some rules have no premises; they are *axioms* whose conclusion holds unconditionally. The conclusion always is a judgment $C \vdash A$: T, and there is one respective rule for each relevant construct A of the abstract syntax.

Note: For example, the typing rule for the i32.add instruction can be given as an axiom:

$$\overline{C \vdash \mathsf{i32.add} : [\mathsf{i32} \; \mathsf{i32}] \rightarrow [\mathsf{i32}]}$$

The instruction is always valid with type $[i32\ i32] \rightarrow [i32]$ (saying that it consumes two i32 values and produces one), independent of any side conditions.

An instruction like local get can be typed as follows:

$$\frac{C.\mathsf{globals}[x] = mut \ t}{C \vdash \mathsf{global.get} \ x : [] \to [t]}$$

Here, the premise enforces that the immediate *global index* x exists in the context. The instruction produces a value of its respective type t (and does not consume any values). If $C.\mathsf{globals}[x]$ does not exist then the premise does not hold, and the instruction is ill-typed.

Finally, a *structured* instruction requires a recursive rule, where the premise is itself a typing judgement:

$$\frac{C \vdash blocktype: [t_1^*] \rightarrow [t_2^*] \qquad C, \mathsf{label}\: [t_2^*] \vdash instr^*: [t_1^*] \rightarrow [t_2^*]}{C \vdash \mathsf{block}\: blocktype\:\: instr^*\: \mathsf{end}: [t_1^*] \rightarrow [t_2^*]}$$

A block instruction is only valid when the instruction sequence in its body is. Moreover, the result type must match the block's annotation blocktype. If so, then the block instruction has the same type as the body. Inside the body an additional label of the corresponding result type is available, which is expressed by extending the context C with the additional label information for the premise.

3.1. Conventions 27

¹⁵ For example: Benjamin Pierce. Types and Programming Languages¹⁶. The MIT Press 2002

¹⁶ https://www.cis.upenn.edu/~bcpierce/tapl/

3.2 Types

Simple *types*, such as *number types* are universally valid. However, restrictions apply to most other types, such as *reference types*, *function types*, as well as the *limits* of *table types* and *memory types*, which must be checked during validation.

Moreover, block types are converted to plain function types for ease of processing.

3.2.1 Number Types

Number types are always valid.

 $\overline{C \vdash numtype \text{ ok}}$

3.2.2 Vector Types

Vector types are always valid.

 $C \vdash vectype \text{ ok}$

3.2.3 Heap Types

Concrete *Heap types* are only valid when the *type index* is.

func

• The heap type is valid.

 $\overline{C \vdash \mathsf{func}\; \mathsf{ok}}$

extern

• The heap type is valid.

 $\overline{C \vdash \mathsf{extern} \; \mathsf{ok}}$

typeidx

- The type $C.\mathsf{types}[\mathit{typeidx}]$ must be defined in the context.
- Then the heap type is valid.

 $\frac{C.\mathsf{types}[typeidx] = functype}{C \vdash typeidx \ \mathbf{ok}}$

bot

• The heap type is valid.

 $\overline{C \vdash \mathsf{bot} \; \mathsf{ok}}$

3.2.4 Reference Types

Reference types are valid when the referenced heap type is.

ref null? heaptype

- The heap type *heaptype* must be *valid*.
- Then the reference type is valid.

$$\frac{C \vdash heaptype \text{ ok}}{C \vdash \text{ref null}? \ heaptype \text{ ok}}$$

3.2.5 Value Types

Valid value types are either valid number type, reference type, or the bottom type.

bot

• The value type is valid.

 $\overline{C \vdash \mathsf{bot} \; \mathsf{ok}}$

3.2.6 Block Types

Block types may be expressed in one of two forms, both of which are converted to *instruction types* by the following rules.

typeidx

- The type C.types [typeidx] must be defined in the context.
- Let $[t_1^*] o [t_2^*]$ be the function type C types [typeidx].
- Then the block type is valid as instruction type $[t_1^*] o [t_2^*].$

$$\frac{C.\mathsf{types}[\mathit{typeidx}] = [t_1^*] \to [t_2^*]}{C \vdash \mathit{typeidx}: [t_1^*] \to [t_2^*]}$$

3.2. Types 29

[valtype?]

- The value type valtype must either be absent, or valid.
- Then the block type is valid as *instruction type* $[] \rightarrow [valtype^?]$.

$$\frac{(C \vdash valtype \text{ ok})^?}{C \vdash [valtype^?] : [] \rightarrow [valtype^?]}$$

3.2.7 Result Types

 $[t^*]$

- Each value type t_i in the type sequence t^* must be valid.
- Then the result type is valid.

$$\frac{(C \vdash t \text{ ok})^*}{C \vdash [t^*] \text{ ok}}$$

3.2.8 Instruction Types

$$[t_1^*] \to {}_{x^*}[t_2^*]$$

- The result type $[t_1^*]$ must be valid.
- The result type $[t_2^*]$ must be valid.
- Each local index x_i in x^* must be defined in the context.
- Then the instruction type is valid.

$$\frac{C \vdash [t_1^*] \text{ ok} \qquad C \vdash [t_2^*] \text{ ok} \qquad (C.\mathsf{locals}[x] = localtype)^*}{C \vdash [t_1^*] \rightarrow_{x^*}[t_2^*] \text{ ok}}$$

3.2.9 Function Types

 $[t_1^*] \rightarrow [t_2^*]$

- The *result type* $[t_1^*]$ must be *valid*.
- The result type $[t_2^*]$ must be valid.
- Then the function type is valid.

$$rac{C dash [t_1^*] ext{ ok } \qquad C dash [t_2^*] ext{ ok }}{C dash [t_1^*] o [t_2^*] ext{ ok }}$$

3.2.10 Limits

Limits must have meaningful bounds that are within a given range.

 $\{\min n, \max m^?\}$

- The value of n must not be larger than k.
- If the maximum $m^{?}$ is not empty, then:
 - Its value must not be larger than k.
 - Its value must not be smaller than n.
- Then the limit is valid within range k.

$$\frac{n \leq k \qquad (m \leq k)^? \qquad (n \leq m)^?}{C \vdash \{\min n, \max m^?\} : k}$$

3.2.11 Table Types

limits reftype

- The limits limits must be valid within range $2^{32} 1$.
- The reference type *reftype* must be *valid*.
- Then the table type is valid.

$$\frac{C \vdash limits: 2^{32} - 1 \qquad C \vdash \textit{reftype ok}}{C \vdash \textit{limits reftype ok}}$$

3.2.12 Memory Types

limits

- The limits *limits* must be *valid* within range 2^{16} .
- Then the memory type is valid.

$$\frac{C \vdash \mathit{limits}: 2^{16}}{C \vdash \mathit{limits} \ \mathsf{ok}}$$

3.2.13 Global Types

mut valtype

- The value type valtype must be valid.
- Then the global type is valid.

$$\frac{C \vdash \mathit{valtype} \ \mathsf{ok}}{C \vdash \mathit{mut} \ \mathit{valtype} \ \mathsf{ok}}$$

3.2. Types 31

3.2.14 External Types

$func\ functype$

- The function type functype must be valid.
- Then the external type is valid.

$$\frac{C \vdash \mathit{functype} \ \mathsf{ok}}{C \vdash \mathsf{func} \ \mathit{functype} \ \mathsf{ok}}$$

${\sf table}\ tabletype$

- The *table type tabletype* must be *valid*.
- Then the external type is valid.

$$\frac{C \vdash tabletype \text{ ok}}{C \vdash table \ tabletype \ \text{ok}}$$

mem memtype

- The *memory type memtype* must be *valid*.
- Then the external type is valid.

$$\frac{C \vdash memtype \text{ ok}}{C \vdash mem \ memtype \text{ ok}}$$

$global\ globaltype$

- The global type globaltype must be valid.
- Then the external type is valid.

$$\frac{C \vdash globaltype \text{ ok}}{C \vdash \text{global} \ globaltype \text{ ok}}$$

3.2.15 Defaultable Types

A type is defaultable if it has a default value for initialization.

Value Types

- A defaultable *value type t* must be:
 - either a number type,
 - or a vector type,
 - or a nullable reference type.

 $\overline{C \vdash numtype}$ defaultable

 $C \vdash vectype \text{ defaultable}$

 $\overline{C \vdash (\text{ref null } heaptype)} \text{ defaultable}$

Table Types

- A defaultable *table type* must be:
 - of the form limits t, where t is a defaultable reference type.

 $\frac{C \vdash \textit{reftype} \text{ defaultable}}{C \vdash \textit{limits reftype} \text{ defaultable}}$

3.3 Matching

On most types, a simple notion of subtyping is defined that is applicable in validation rules or during *module instantiation* when checking the types of imports.

Todo: externtype matching is used on semantic types; need to define how to reinterpret C for semantic types

3.3.1 Number Types

A number type $numtype_1$ matches a number type $numtype_2$ if and only if:

• Both $numtype_1$ and $numtype_2$ are the same.

$$\overline{C \vdash numtype \leq numtype}$$

3.3.2 Vector Types

A vector type vectype₁ matches a vector type vectype₂ if and only if:

• Both $vectype_1$ and $vectype_2$ are the same.

$$\overline{C \vdash vectype \leq vectype}$$

3.3.3 Heap Types

A heap type heaptype₁ matches a heap type heaptype₂ if and only if:

- Either both $heaptype_1$ and $heaptype_2$ are the same.
- Or $heaptype_1$ is a type index that defines a function type and $heaptype_2$ is FUNC.
- Or heaptype₁ is a type index that defines a function type functype₁, and heaptype₂ is a type index that defines a function type functype₂, and functype₁ matches functype₂.

$$\frac{C.\mathsf{types}[\mathit{typeidx}] = \mathit{functype}}{C \vdash \mathit{typeidx}_1] = \mathit{functype}_1} \qquad \frac{C.\mathsf{types}[\mathit{typeidx}] = \mathit{functype}}{C \vdash \mathit{typeidx}_2] = \mathit{functype}_2} \\ \frac{C.\mathsf{types}[\mathit{typeidx}_1] = \mathit{functype}_1}{C \vdash \mathit{typeidx}_1} \leq \mathit{typeidx}_2} \qquad C \vdash \mathit{functype}_1 \leq \mathit{functype}_2}{C \vdash \mathit{typeidx}_1} \leq \mathit{typeidx}_2}$$

3.3. Matching 33

3.3.4 Reference Types

A reference type ref null? heaptype₁ matches a reference type ref null? heaptype₂ if and only if:

- The heap type heaptype₁ matches heaptype₂.
- null₁ is absent or null₂ is present.

$$\frac{C \vdash heaptype_1 \leq heaptype_2}{C \vdash \mathsf{ref}\ heaptype_1 \leq \mathsf{ref}\ heaptype_2} \qquad \frac{C \vdash heaptype_1 \leq heaptype_2}{C \vdash \mathsf{ref}\ \mathsf{null}\ heaptype_1 \leq \mathsf{ref}\ \mathsf{null}^?\ heaptype_2}$$

3.3.5 Value Types

A value type valtype₁ matches a value type valtype₂ if and only if:

- Either both valtype₁ and valtype₂ are number types and valtype₁ matches valtype₂.
- ullet Or both $valtype_1$ and $valtype_2$ are reference types and $valtype_1$ matches $valtype_2$.
- Or *valtype*₁ is bot.

$$\overline{C \vdash \mathsf{bot} \leq \mathit{valtype}}$$

3.3.6 Result Types

Subtyping is lifted to *result types* in a pointwise manner. That is, a *result type* $[t_1^*]$ matches a *result type* $[t_2^*]$ if and only if:

• Every value type t_1 in $[t_1^*]$ matches the corresponding value type t_2 in $[t_2^*]$.

$$\frac{(C \vdash t_1 \le t_2)^*}{C \vdash [t_1^*] \le [t_2^*]}$$

3.3.7 Function Types

Subtyping is also defined for *function types*. However, it is required that they match in both directions, effectively demanding type equivalence. That is, a *function type* $[t_{11}^*] \to [t_{12}^*]$ matches a type $[t_{21}^a st] \to [t_{22}^*]$ if and only if:

- The result type $[t_{11}^*]$ matches $[t_{21}^*]$, and vice versa.
- The result type $[t_{12}^*]$ matches $[t_{22}^*]$, and vice versa.

$$\begin{split} \frac{C \vdash [t_{11}^*] \leq [t_{21}^*] & C \vdash [t_{12}^*] \leq [t_{22}^*] \\ C \vdash [t_{21}^*] \leq [t_{11}^*] & C \vdash [t_{22}^*] \leq [t_{12}^*] \\ \hline C \vdash [t_{11}^*] \to [t_{12}^*] \leq [t_{21}^*] \to [t_{22}^*] \end{split}$$

Note: In future versions of WebAssembly, subtyping on function types may be relaxed to support co- and contravariance.

3.3.8 Limits

Limits $\{\min n_1, \max m_1^?\}$ match limits $\{\min n_2, \max m_2^?\}$ if and only if:

- n_1 is larger than or equal to n_2 .
- Either:
 - m_2^2 is empty.
- Or:
 - Both $m_1^?$ and $m_2^?$ are non-empty.
 - m_1 is smaller than or equal to m_2 .

$$\frac{n_1 \geq n_2}{C \vdash \{\min n_1, \max m_1^2\} \leq \{\min n_2, \max \epsilon\}} \quad \frac{n_1 \geq n_2}{C \vdash \{\min n_1, \max m_1\} \leq \{\min n_2, \max m_2\}}$$

3.3.9 Table Types

A table type (limits₁ reftype₁) matches (limits₂ reftype₂) if and only if:

- Limits $limits_1$ match $limits_2$.
- The reference type reftype₁ matches reftype₂, and vice versa.

$$\frac{C \vdash limits_1 \leq limits_2 \quad C \vdash reftype_1 \leq reftype_2 \quad C \vdash reftype_2 \leq reftype_1}{C \vdash limits_1 \ reftype_1 \leq limits_2 \ reftype_2}$$

3.3.10 Memory Types

A memory type $limits_1$ matches $limits_2$ if and only if:

• Limits $limits_1$ match $limits_2$.

$$\frac{C \vdash limits_1 \leq limits_2}{C \vdash limits_1 \leq limits_2}$$

3.3.11 Global Types

A global type $(mut_1 t_1)$ matches $(mut_2 t_2)$ if and only if:

- Either both mut_1 and mut_2 are var and t_1 and t_2 are the same.
- Or both mut_1 and mut_2 are const and t_1 matches t_2 .

$$\frac{C \vdash t_1 \leq t_2}{C \vdash \mathsf{var}\, t \leq \mathsf{var}\, t} \qquad \frac{C \vdash t_1 \leq t_2}{C \vdash \mathsf{const}\, t_1 \leq \mathsf{const}\, t_2}$$

3.3. Matching 35

3.3.12 External Types

Functions

An external type func functype₁ matches func functype₂ if and only if:

• Function type functype₁ matches functype₂.

$$\frac{C \vdash functype_1 \leq functype_2}{C \vdash \mathsf{func}\, functype_1 \leq \mathsf{func}\, functype_2}$$

Tables

An external type table $table type_1$ matches table $table type_2$ if and only if:

• Table type tabletype₁ matches tabletype₂.

$$\frac{C \vdash tabletype_1 \leq tabletype_2}{C \vdash \mathsf{table}\ tabletype_1 \leq \mathsf{table}\ tabletype_2}$$

Memories

An external type mem $memtype_1$ matches mem $memtype_2$ if and only if:

• Memory type memtype₁ matches memtype₂.

$$\frac{C \vdash memtype_1 \leq memtype_2}{C \vdash mem \ memtype_1 \leq mem \ memtype_2}$$

Globals

An external type global globaltype₁ matches global globaltype₂ if and only if:

• Global type globaltype₁ matches globaltype₂.

$$\frac{C \vdash globaltype_1 \leq globaltype_2}{C \vdash \mathsf{global} \ globaltype_1 \leq \mathsf{global} \ globaltype_2}$$

3.4 Instructions

Instructions are classified by instruction types that describe how they manipulate the operand stack and initialize locals: A type $[t_1^*] \to {}_{x^*}[t_2^*]$ describes the required input stack with argument values of types t_1^* that an instruction pops off and the provided output stack with result values of types t_2^* that it pushes back. Moreover, it enumerates the indices x^* of locals that have been set by the instruction. In most cases, this is empty.

Note: For example, the instruction i32.add has type [i32 i32] \rightarrow [i32], consuming two i32 values and producing one. The instruction $LOCALSET\ x$ has type $[t] \rightarrow {}_x[]$, provided t is the type declared for the local x.

Typing extends to instruction sequences instr*. Such a sequence has an instruction type $[t_1^*] \to {}_{x^*}[t_2^*]$ if the accumulative effect of executing the instructions is consuming values of types t_1^* off the operand stack, pushing new values of types t_2^* , and setting all locals x^* .

For some instructions, the typing rules do not fully constrain the type, and therefore allow for multiple types. Such instructions are called *polymorphic*. Two degrees of polymorphism can be distinguished:

- *value-polymorphic*: the *value type t* of one or several individual operands is unconstrained. That is the case for all *parametric instructions* like drop and select.
- stack-polymorphic: the entire (or most of the) instruction type $[t_1^*] \to {}_{x^*}[t_2^*]$ of the instruction is unconstrained. That is the case for all *control instructions* that perform an *unconditional control transfer*, such as unreachable, br, br_table, and return.

In both cases, the unconstrained types or type sequences can be chosen arbitrarily, as long as they meet the constraints imposed for the surrounding parts of the program.

Note: For example, the select instruction is valid with type $[t \ t \ i32] \rightarrow [t]$, for any possible *number type t*. Consequently, both instruction sequences

and

are valid, with t in the typing of select being instantiated to i32 or f64, respectively.

The unreachable instruction is stack-polymorphic, and hence valid with type $[t_1^*] \to {}_{x^*}[t_2^*]$ for any possible sequences of value types t_1^* and t_2^* and sequence of locals x^* . Consequently,

is valid by assuming type [] \rightarrow [i32] for the unreachable instruction. In contrast,

is invalid, because there is no possible type to pick for the unreachable instruction that would make the sequence well-typed.

The *Appendix* describes a type checking *algorithm* that efficiently implements validation of instruction sequences as prescribed by the rules given here.

3.4.1 Numeric Instructions

 $t.\mathsf{const}\ c$

• The instruction is valid with type $[] \rightarrow [t]$.

$$\overline{C \vdash t.\mathsf{const}\ c : [] \to [t]}$$

t.unop

• The instruction is valid with type $[t] \rightarrow [t]$.

$$\overline{C \vdash t.unop : [t] \rightarrow [t]}$$

t.binop

• The instruction is valid with type $[t\ t] \rightarrow [t]$.

$$\overline{C \vdash t.binop : [t\ t] \rightarrow [t]}$$

t.testop

• The instruction is valid with type [t] o [i32].

$$C \vdash t.testop : [t] \rightarrow [i32]$$

t.relop

• The instruction is valid with type $[t\ t] \rightarrow [i32]$.

$$\overline{C \vdash t.relop : [t\ t] \rightarrow [\mathsf{i32}]}$$

$$t_2.cvtop_t_1_sx$$
?

• The instruction is valid with type $[t_1] \rightarrow [t_2]$.

$$\overline{C \vdash t_2.cvtop_t_1_sx^? : [t_1] \to [t_2]}$$

3.4.2 Reference Instructions

$\mathsf{ref.null}\ ht$

- The *heap type ht* must be *valid*.
- Then the instruction is valid with type $[] o [(\mathsf{ref} \; \mathsf{null} \; ht)].$

$$\frac{C \vdash ht \text{ ok}}{C \vdash \mathsf{ref.null} \ ht : [] \to [(\mathsf{ref.null} \ ht)]}$$

$\mathsf{ref}.\mathsf{func}\; x$

- The function C-funcs[x] must be defined in the context.
- There must exist a type index y such that C.types[y] is the same function type as C.funcs[x].
- ullet The function index x must be contained in C.refs.
- The instruction is valid with type $[] \rightarrow [(\text{ref } y)].$

$$\frac{C.\mathsf{funcs}[x] = C.\mathsf{types}[y] \qquad x \in C.\mathsf{refs}}{C \vdash \mathsf{ref.func}\; x : [] \to [(\mathsf{ref}\; y)]}$$

ref.is_null

• The instruction is valid with type $[(\text{ref null } ht)] \rightarrow [\text{i32}]$, for any valid heap type ht.

$$\frac{C \vdash ht \text{ ok}}{C \vdash \mathsf{ref.is_null} : [(\mathsf{ref} \; \mathsf{null} \; ht)] \to [\mathsf{i32}]}$$

ref.as_non_null

• The instruction is valid with type $[(ref null ht)] \rightarrow [(ref ht)]$, for any valid heap type ht.

$$\frac{C \vdash ht \text{ ok}}{C \vdash \mathsf{ref.as_non_null} : [(\mathsf{ref} \; \mathsf{null} \; ht)] \to [(\mathsf{ref} \; ht)]}$$

3.4.3 Vector Instructions

Vector instructions can have a prefix to describe the *shape* of the operand. Packed numeric types, i8 and i16, are not *value type*, we define an auxiliary function to map such packed types into value types:

unpacked(
$$i8x16$$
) = $i32$
unpacked($i16x8$) = $i32$
unpacked(txN) = t

We also define an auxiliary function to get number of packed numeric types in a v128, dimension:

$$\dim(t \times N) = N$$

v128.const $\it c$

• The instruction is valid with type $[] \rightarrow [v128]$.

$$\overline{C \vdash \mathsf{v}128.\mathsf{const}\ c : [] \to [\mathsf{v}128]}$$

 $\mathsf{v}128.\mathit{vvunop}$

• The instruction is valid with type [v128] \rightarrow [v128].

$$\overline{C \vdash \mathsf{v}128.vvunop : [\mathsf{v}128] \rightarrow [\mathsf{v}128]}$$

v128.vvbinop

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$\overline{C \vdash \mathsf{v128}.vvbinop : [\mathsf{v128}\,\mathsf{v128}] \to [\mathsf{v128}]}$$

v128.vvternop

• The instruction is valid with type [v128 v128 v128] \rightarrow [v128].

$$C \vdash v128.vvternop : [v128 v128 v128] \rightarrow [v128]$$

v128.vvtestop

• The instruction is valid with type [v128] \rightarrow [i32].

$$\overline{C \vdash \mathsf{v}128.vvtestop : [\mathsf{v}128] \to [\mathsf{i}32]}$$

i8x16.swizzle

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$C \vdash \mathsf{i8x16}.\mathsf{swizzle} : [\mathsf{v}128 \ \mathsf{v}128] \rightarrow [\mathsf{v}128]$$

i8x16.shuffle $laneidx^{16}$

- For all $laneidx_i$, in $laneidx^{16}$, $laneidx_i$ must be smaller than 32.
- The instruction is valid with type [v128 v128] \rightarrow [v128].

$$\frac{(laneidx < 32)^{16}}{C \vdash \mathsf{i8x16.shuffle}\ laneidx^{16} : [\mathsf{v128}\ \mathsf{v128}] \to [\mathsf{v128}]}$$

$shape.\mathsf{splat}$

- Let t be unpacked (shape).
- The instruction is valid with type $[t] \rightarrow [v128]$.

$$\overline{C \vdash shape.\mathsf{splat} : [\mathsf{unpacked}(shape)] \rightarrow [\mathsf{v}128]}$$

shape.extract lane $sx^?$ laneidx

- The lane index laneidx must be smaller than dim(shape).
- The instruction is valid with type $[v128] \rightarrow [unpacked(shape)]$.

$$\frac{laneidx < \dim(shape)}{C \vdash t \texttt{x} N.\texttt{extract_lane_} sx^? \ laneidx : [\texttt{v128}] \rightarrow [\texttt{unpacked}(shape)]}$$

$shape.{\sf replace_lane}\ laneidx$

- The lane index laneidx must be smaller than dim(shape).
- Let t be unpacked(shape).
- The instruction is valid with type [v128 t] \rightarrow [v128].

$$\frac{laneidx < \dim(shape)}{C \vdash shape.\mathsf{replace_lane}\ laneidx : [v128\ \mathrm{unpacked}(shape)] \rightarrow [v128]}$$

shape.vunop

• The instruction is valid with type [v128] \rightarrow [v128].

$$\overline{C \vdash shape.vunop : [v128] \rightarrow [v128]}$$

shape.vbinop

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$\overline{C \vdash shape.vbinop : [v128 v128] \rightarrow [v128]}$$

shape.vrelop

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$\overline{C \vdash shape.vrelop : [v128 v128] \rightarrow [v128]}$$

ishape.vishiftop

• The instruction is valid with type [v128 i32] \rightarrow [v128].

$$\overline{C \vdash \mathit{ishape.vishiftop} : [\mathsf{v128}\:\mathsf{i32}] \to [\mathsf{v128}]}$$

shape.vtestop

• The instruction is valid with type [v128] \rightarrow [i32].

$$C \vdash shape.vtestop : [v128] \rightarrow [i32]$$

• The instruction is valid with type [v128] \rightarrow [v128].

$$C \vdash shape.vcvtop\ half?\ shape\ sx?\ \mathsf{zero}^?: [v128] \to [v128]$$

$ishape_1.\mathsf{narrow}_ishape_2_sx$

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$\overline{C \vdash ishape_1.narrow_ishape_2_sx : [v128 v128] \rightarrow [v128]}$$

$ishape. \mathsf{bitmask}$

- The instruction is valid with type [v128] \rightarrow [i32].

$$\overline{C \vdash ishape.bitmask : [v128] \rightarrow [i32]}$$

 $ishape_1.\mathsf{dot}_ishape_2_\mathsf{s}$

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$C \vdash ishape_1.\mathsf{dot}_ishape_2_s : [v128 \ v128] \rightarrow [v128]$$

 $ishape_1.extmul_half_ishape_2_sx$

• The instruction is valid with type [v128 v128] \rightarrow [v128].

$$C \vdash ishape_1.\mathsf{extmul_}half_ishape_2_sx : [v128 v128] \rightarrow [v128]$$

 $ishape_1.\mathsf{extadd_pairwise_} ishape_2_sx$

• The instruction is valid with type [v128] \rightarrow [v128].

$$C \vdash ishape_1.\mathsf{extadd_pairwise_} ishape_2_sx : [v128] \rightarrow [v128]$$

3.4.4 Parametric Instructions

drop

• The instruction is valid with type $[t] \rightarrow []$, for any valid value type t.

$$\frac{C \vdash t \text{ ok}}{C \vdash \mathsf{drop} : [t] \to []}$$

Note: Both drop and select without annotation are *value-polymorphic* instructions.

select (t^*) ?

- If t^* is present, then:
 - The result type $[t^*]$ must be valid.
 - The length of t^* must be 1.
 - Then the instruction is valid with type $[t^* \ t^* \ i32] \rightarrow [t^*]$.
- Else:
 - The instruction is valid with type $[t \ t \ i32] \rightarrow [t]$, for any valid value type t that matches some number type or vector type.

$$\frac{C \vdash [t] \text{ ok}}{C \vdash \text{select } t : [t \text{ } t \text{ } \text{i} \text{32}] \rightarrow [t]} \qquad \frac{C \vdash [t] \text{ ok} \qquad C \vdash [t] \leq [numtype]}{C \vdash \text{select} : [t \text{ } t \text{ } \text{i} \text{32}] \rightarrow [t]} \qquad \frac{\vdash t \leq vectype}{C \vdash \text{select} : [t \text{ } t \text{ } \text{i} \text{32}] \rightarrow [t]}$$

Note: In future versions of WebAssembly, select may allow more than one value per choice.

3.4.5 Variable Instructions

local.get x

- The local C-locals[x] must be defined in the context.
- Let $init\ t$ be the $local\ type\ C.locals[x]$.
- The initialization status init must be set.
- Then the instruction is valid with type $[] \rightarrow [t]$.

$$\frac{C.\mathsf{locals}[x] = \mathsf{set}\ t}{C \vdash \mathsf{local.get}\ x : [] \to [t]}$$

local.set x

- The local C.locals[x] must be defined in the context.
- Let $init\ t$ be the $local\ type\ C.locals[x]$.
- Then the instruction is valid with type $[t] \rightarrow_x []$.

$$\frac{C.\mathsf{locals}[x] = init \ t}{C \vdash \mathsf{local.set} \ x : [t] \to {}_x[]}$$

local.tee x

- The local C.locals[x] must be defined in the context.
- Let init t be the local type C.locals[x].
- Then the instruction is valid with type $[t] \rightarrow {}_x[t]$.

$$\frac{C.\mathsf{locals}[x] = init \ t}{C \vdash \mathsf{local.tee} \ x : [t] \rightarrow_x [t]}$$

global.get x

- The global C.globals[x] must be defined in the context.
- Let $mut\ t$ be the $global\ type\ C$.globals[x].
- Then the instruction is valid with type [] o [t].

$$\frac{C.\mathsf{globals}[x] = mut \; t}{C \vdash \mathsf{global.get} \; x : [] \to [t]}$$

global.set x

- The global C.globals[x] must be defined in the context.
- Let $mut\ t$ be the global type C.globals[x].
- ullet The mutability mut must be var.
- Then the instruction is valid with type $[t] \rightarrow []$.

$$\frac{C.\mathsf{globals}[x] = \mathsf{var}\ t}{C \vdash \mathsf{global.set}\ x : [t] \to []}$$

3.4.6 Table Instructions

$\mathsf{table}.\mathsf{get}\; x$

- The table C.tables[x] must be defined in the context.
- Let $limits\ t$ be the $table\ type\ C$.tables[x].
- Then the instruction is valid with type [i32] \rightarrow [t].

$$\frac{C.\mathsf{tables}[x] = \mathit{limits}\; t}{C \vdash \mathsf{table.get}\; x : [\mathsf{i32}] \to [t]}$$

table.set x

- The table C.tables[x] must be defined in the context.
- Let $limits\ t$ be the $table\ type\ C$.tables[x].
- Then the instruction is valid with type [i32 t] \rightarrow [].

$$\frac{C.\mathsf{tables}[x] = \mathit{limits}\; t}{C \vdash \mathsf{table.set}\; x : [\mathsf{i32}\; t] \to []}$$

table.size x

- The table C.tables[x] must be defined in the context.
- Then the instruction is valid with type [] \rightarrow [i32].

$$\frac{C.\mathsf{tables}[x] = \mathit{tabletype}}{C \vdash \mathsf{table.size}\; x : [] \to [\mathsf{i32}]}$$

table.grow x

- The table C.tables [x] must be defined in the context.
- Let *limits t* be the *table type C*.tables[x].
- Then the instruction is valid with type [t i32] \rightarrow [i32].

$$\frac{C.\mathsf{tables}[x] = limits\ t}{C \vdash \mathsf{table.grow}\ x : [t\ \mathsf{i32}] \to [\mathsf{i32}]}$$

table.fill x

- The table C.tables[x] must be defined in the context.
- Let $limits\ t$ be the $table\ type\ C$.tables[x].
- Then the instruction is valid with type [i32 t i32] \rightarrow [].

$$\frac{C.\mathsf{tables}[x] = \mathit{limits}\; t}{C \vdash \mathsf{table.fill}\; x : [\mathsf{i32}\; t\; \mathsf{i32}] \to []}$$

table.copy x y

- The table C.tables [x] must be defined in the context.
- Let $limits_1 t_1$ be the table type C.tables[x].
- The table C.tables[y] must be defined in the context.
- Let $limits_2 t_2$ be the table type C.tables[y].
- The reference type t_2 must match t_1 .
- Then the instruction is valid with type [i32 i32 i32] \rightarrow [].

$$\frac{C.\mathsf{tables}[x] = \mathit{limits}_1 \ t_1 \qquad C.\mathsf{tables}[x] = \mathit{limits}_2 \ t_2 \qquad C \vdash t_2 \leq t_1}{C \vdash \mathsf{table.copy} \ x \ y : [\mathsf{i32} \ \mathsf{i32}] \rightarrow []}$$

table.init x y

- The table C.tables[x] must be defined in the context.
- Let $limits t_1$ be the table type C.tables[x].
- The element segment C-elems [y] must be defined in the context.
- Let t_2 be the reference type C.elems[y].
- The reference type t_2 must match t_1 .
- Then the instruction is valid with type [i32 i32 i32] \rightarrow [].

$$\frac{C.\mathsf{tables}[x] = \mathit{limits}\ t_1 \qquad C.\mathsf{elems}[y] = t_2 \qquad C \vdash t_2 \leq t_1}{C \vdash \mathsf{table.init}\ x\ y : [\mathsf{i32}\ \mathsf{i32}] \rightarrow []}$$

$\mathsf{elem}.\mathsf{drop}\; x$

- The element segment C-elems [x] must be defined in the context.
- Then the instruction is valid with type $[] \rightarrow []$.

$$\frac{C.\mathsf{elems}[x] = t}{C \vdash \mathsf{elem.drop}\; x : \lceil \rceil \to \lceil \rceil}$$

3.4.7 Memory Instructions

t.load memarg

- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than the *bit width* of t divided by 8.
- Then the instruction is valid with type [i32] \rightarrow [t].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype} \quad \ 2^{\mathit{memarg}.\mathsf{align}} \leq |t|/8}{C \vdash t.\mathsf{load} \ \mathit{memarg} : [\mathsf{i32}] \rightarrow [t]}$$

$t.loadN_sx\ memarg$

- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than N/8.
- Then the instruction is valid with type [i32] \rightarrow [t].

$$\frac{C.\mathsf{mems}[0] = \textit{memtype} \qquad 2^{\textit{memarg}.\mathsf{align}} \leq \textit{N}/8}{\textit{C} \vdash t.\mathsf{load}N_\textit{sx memarg} : [\mathsf{i32}] \rightarrow [t]}$$

$t.\mathsf{store}\ memarg$

- The memory C.mems[0] must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than the bit width of t divided by 8.
- Then the instruction is valid with type [i32 t] \rightarrow [].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype} \quad \ 2^{\mathit{memarg}.\mathsf{align}} \leq |t|/8}{C \vdash t.\mathsf{store} \ \mathit{memarg} : [\mathsf{i32} \ t] \rightarrow []}$$

$t.\mathsf{store} N\ memarg$

- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than N/8.
- Then the instruction is valid with type [i32 t] \rightarrow [].

$$\frac{C.\mathsf{mems}[0] = \textit{memtype} \qquad 2^{\textit{memarg}.\mathsf{align}} \leq N/8}{C \vdash t.\mathsf{store}N \; \textit{memarg} : [\mathsf{i32}\;t] \rightarrow []}$$

v128.load $N \times M _sx\ memarg$

- The memory C.mems[0] must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than $N/8\cdot M.$
- Then the instruction is valid with type [i32] \rightarrow [v128].

$$\frac{C.\mathsf{mems}[0] = \textit{memtype}}{C \vdash \mathsf{v128}.\mathsf{load}N \mathsf{x} M_\textit{sx memarg} : [\mathsf{i32}] \rightarrow [\mathsf{v128}]}$$

v128.loadN_splat memarg

- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than N/8.
- Then the instruction is valid with type [i32] \rightarrow [v128].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype}}{C \vdash \mathsf{v128}.\mathsf{load}N_\mathsf{splat}\ \mathit{memarg}: [\mathsf{i32}] \to [\mathsf{v128}]}$$

v128.loadN_zero memarg

- The memory C.mems[0] must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than N/8.
- Then the instruction is valid with type [i32] \rightarrow [v128].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype} \qquad 2^{\mathit{memarg.align}} \leq N/8}{C \vdash \mathsf{v128.load}N_\mathsf{zero} \ \mathit{memarg} : [\mathsf{i32}] \rightarrow [\mathsf{v128}]}$$

v128.loadN_lane $memarg\ laneidx$

- The lane index laneidx must be smaller than 128/N.
- The memory C.mems[0] must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than N/8.
- Then the instruction is valid with type [i32 v128] \rightarrow [v128].

$$\frac{laneidx < 128/N \qquad C.\mathsf{mems}[0] = memtype \qquad 2^{memarg.\mathsf{align}} < N/8}{C \vdash \mathsf{v}128.\mathsf{load}N_\mathsf{lane} \ memarg \ laneidx : [\mathsf{i}32 \ \mathsf{v}128] \to [\mathsf{v}128]}$$

v128.storeN_lane $memarg\ laneidx$

- The lane index laneidx must be smaller than 128/N.
- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- The alignment $2^{memarg.align}$ must not be larger than N/8.
- Then the instruction is valid with type [i32 v128] \rightarrow [v128].

$$\frac{laneidx < 128/N \qquad C.\mathsf{mems}[0] = memtype \qquad 2^{memarg.align} < N/8}{C \vdash \mathsf{v128}.\mathsf{store}N_\mathsf{lane} \ memarg \ laneidx : [\mathsf{i32}\ \mathsf{v128}] \to []}$$

memory.size

- The memory C.mems[0] must be defined in the context.
- Then the instruction is valid with type [] \rightarrow [i32].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype}}{C \vdash \mathsf{memory.size} : [] \to [\mathsf{i}32]}$$

memory.grow

- The memory C.mems[0] must be defined in the context.
- Then the instruction is valid with type [i32] \rightarrow [i32].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype}}{C \vdash \mathsf{memory.grow} : [\mathsf{i32}] \to [\mathsf{i32}]}$$

memory.fill

- The memory C.mems[0] must be defined in the context.
- Then the instruction is valid with type [i32 i32 i32] \rightarrow [].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype}}{C \vdash \mathsf{memory.fill} : [\mathsf{i32}\;\mathsf{i32}\;\mathsf{i32}] \to []}$$

memory.copy

- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- Then the instruction is valid with type [i32 i32 i32] \rightarrow [].

$$\frac{C.\mathsf{mems}[0] = \mathit{memtype}}{C \vdash \mathsf{memory.copy} : [\mathsf{i32}\ \mathsf{i32}\ \mathsf{i32}] \to []}$$

${\it memory.init} \; x$

- The memory $C.\mathsf{mems}[0]$ must be defined in the context.
- The data segment $C.\mathsf{datas}[x]$ must be defined in the context.
- Then the instruction is valid with type [i32 i32 i32] \rightarrow [].

$$\frac{C.\mathsf{mems}[0] = memtype \qquad C.\mathsf{datas}[x] = \mathsf{ok}}{C \vdash \mathsf{memory.init} \ x : [\mathsf{i32} \ \mathsf{i32} \ \mathsf{i32}] \to []}$$

data.drop x

- The data segment $C.\mathsf{datas}[x]$ must be defined in the context.
- Then the instruction is valid with type $[] \rightarrow []$.

$$\frac{C.\mathsf{datas}[x] = \mathsf{ok}}{C \vdash \mathsf{data.drop}\ x : [] \to []}$$

3.4.8 Control Instructions

nop

• The instruction is valid with type $[] \rightarrow []$.

$$\overline{C \vdash \mathsf{nop} : \lceil \rceil \to \lceil \rceil}$$

unreachable

• The instruction is valid with any *valid* type $[t_1^*] \rightarrow {}_{x^*}[t_2^*]$.

$$\frac{C \vdash [t_1^*] \rightarrow_{x^*} [t_2^*] \text{ ok}}{C \vdash \text{unreachable} : [t_1^*] \rightarrow_{x^*} [t_2^*]}$$

Note: The unreachable instruction is stack-polymorphic.

block blocktype instr* end

- The block type must be valid as some function type $[t_1^*] \rightarrow [t_2^*]$.
- Let C' be the same *context* as C, but with the *result type* $[t_2^*]$ prepended to the labels vector.
- Under context C', the instruction sequence $instr^*$ must be valid with type $[t_1^*] \to {}_{x^*}[t_2^*]$, for any sequence of $local indices x^*$.
- Then the compound instruction is valid with type $[t_1^*] \to [t_2^*]$.

$$\frac{C \vdash blocktype: [t_1^*] \rightarrow [t_2^*] \qquad C, \mathsf{labels}\, [t_2^*] \vdash instr^*: [t_1^*] \rightarrow {}_{x^*}[t_2^*]}{C \vdash \mathsf{block}\, blocktype\,\, instr^* \, \mathsf{end}: [t_1^*] \rightarrow [t_2^*]}$$

Note: The *notation* C, labels $[t^*]$ inserts the new label type at index 0, shifting all others.

loop blocktype instr* end

- The block type must be valid as some instruction type $[t_1^*] \to {}_{x^*}[t_2^*]$.
- Let C' be the same *context* as C, but with the *result type* $[t_1^*]$ prepended to the labels vector.
- Under context C', the instruction sequence $instr^*$ must be valid with type $[t_1^*] \to {}_{x^*}[t_2^*]$, for any sequence of $local indices x^*$.
- Then the compound instruction is valid with type $[t_1^*] o [t_2^*]$.

$$\frac{C \vdash blocktype: [t_1^*] \rightarrow [t_2^*] \qquad C, \mathsf{labels}\, [t_1^*] \vdash instr^*: [t_1^*] \rightarrow {}_{x^*}[t_2^*]}{C \vdash \mathsf{loop}\, blocktype\,\, instr^* \; \mathsf{end}: [t_1^*] \rightarrow [t_2^*]}$$

Note: The *notation* C, labels $[t^*]$ inserts the new label type at index 0, shifting all others.

if $blocktype \ instr_1^*$ else $instr_2^*$ end

- The block type must be valid as some function type $[t_1^*] o [t_2^*]$.
- Let C' be the same *context* as C, but with the *result type* $[t_2^*]$ prepended to the labels vector.
- Under context C', the instruction sequence $instr_1^*$ must be valid with type $[t_1^*] \to {}_{x_1^*}[t_2^*]$, for any sequence of local indices x_1^* .
- Under context C', the instruction sequence $instr_2^*$ must be valid with type $[t_1^*] \to x_2^*[t_2^*]$, for any sequence of local indices x_2^* .
- Then the compound instruction is valid with type $[t_1^* i32] \rightarrow [t_2^*]$.

```
\frac{C \vdash blocktype: [t_1^*] \rightarrow [t_2^*] \quad C, \mathsf{labels}\,[t_2^*] \vdash instr_1^*: [t_1^*] \rightarrow {}_{x_1^*}[t_2^*] \quad C, \mathsf{labels}\,[t_2^*] \vdash instr_2^*: [t_1^*] \rightarrow {}_{x_2^*}[t_2^*]}{C \vdash \mathsf{if}\,\, blocktype\,\, instr_1^*\,\, \mathsf{else}\,\, instr_2^*\,\, \mathsf{end}: [t_1^*\,\, \mathsf{i32}] \rightarrow [t_2^*]}
```

Note: The *notation* C, labels $[t^*]$ inserts the new label type at index 0, shifting all others.

br l

- The label C-labels [l] must be defined in the context.
- Let $[t^*]$ be the result type C.labels [l].
- Then the instruction is valid with type $[t_1^* \ t^*] \to {}_{x^*}[t_2^*]$, for any valid type $[t_1^*] \to {}_{x^*}[t_2^*]$.

$$\frac{C.\mathsf{labels}[l] = [t^*] \qquad C \vdash [t_1^*] \rightarrow {}_{x^*}[t_2^*] \; \mathsf{ok}}{C \vdash \mathsf{br} \; l : [t_1^* \; t^*] \rightarrow {}_{x^*}[t_2^*]}$$

Note: The *label index* space in the *context* C contains the most recent label first, so that C.labels[l] performs a relative lookup as expected.

The br instruction is *stack-polymorphic*.

 $\mathsf{br}_\mathsf{if}\ \mathit{l}$

- The label C-labels [l] must be defined in the context.
- Let $[t^*]$ be the result type C.labels [l].
- Then the instruction is valid with type $[t^* \text{ i32}] \rightarrow [t^*]$.

$$\frac{C.\mathsf{labels}[l] = [t^*]}{C \vdash \mathsf{br_if}\ l : [t^*\ \mathsf{i32}] \to [t^*]}$$

Note: The *label index* space in the *context* C contains the most recent label first, so that C.labels[l] performs a relative lookup as expected.

br_table $l^*\ l_N$

- The label $C.\mathsf{labels}[l_N]$ must be defined in the context.
- For all l_i in l^* , the label C-labels $[l_i]$ must be defined in the context.
- There must be a *result type* $[t^*]$, such that:
 - The result type $[t^*]$ matches C.labels $[l_N]$.
 - For all l_i in l^* , the result type $[t^*]$ matches C.labels $[l_i]$.
- Then the instruction is valid with type $[t_1^* \ t^* \ i32] \to {}_{x^*}[t_2^*]$, for any valid type $[t_1^*] \to {}_{x^*}[t_2^*]$.

$$\frac{(C \vdash [t^*] \leq C.\mathsf{labels}[l])^* \quad C \vdash [t^*] \leq C.\mathsf{labels}[l_N] \quad C \vdash [t_1^*] \rightarrow {}_{x^*}[t_2^*] \text{ ok}}{C \vdash \mathsf{br_table} \ l^* \ l_N : [t_1^* \ t^* \ \mathsf{i32}] \rightarrow {}_{x^*}[t_2^*]}$$

Note: The *label index* space in the *context* C contains the most recent label first, so that C-labels $[l_i]$ performs a relative lookup as expected.

The br_table instruction is *stack-polymorphic*.

Furthermore, the *result type* $[t^*]$ is also chosen non-deterministically in this rule. Although it may seem necessary to compute $[t^*]$ as the greatest lower bound of all label types in practice, a simple *linear algorithm* does not require this.

$br_on_null\ l$

- The label C-labels [l] must be defined in the context.
- Let $[t^*]$ be the result type C.labels [l].
- Then the instruction is valid with type $[t^* \text{ (ref null } ht)] \rightarrow [t^* \text{ (ref } ht)]$ for any valid heap type ht.

$$\frac{C.\mathsf{labels}[l] = [t^*] \qquad C \vdash ht \text{ ok}}{C \vdash \mathsf{br_on_null} \ l : [t^* \text{ (ref null } ht)] \rightarrow [t^* \text{ (ref } ht)]}$$

$br_on_non_null\ l$

- The label C.labels [l] must be defined in the context.
- Let $[t'^*]$ be the result type C.labels [l].
- The result type $[t'^*]$ must contain at least one type.
- Let the *value type* t_l be the last element in the sequence t'^* , and $[t^*]$ the remainder of the sequence preceding it.
- The value type t_l must be a reference type of the form ref null? ht.
- Then the instruction is valid with type $[t^* \text{ (ref null } ht)] \rightarrow [t^*]$.

$$\frac{C.\mathsf{labels}[l] = [t^* \; (\mathsf{ref} \; ht)]}{C \vdash \mathsf{br_on_non_null} \; l : [t^* \; (\mathsf{ref} \; \mathsf{null} \; ht)] \to [t^*]}$$

return

- The return type C.return must not be absent in the context.
- Let $[t^*]$ be the *result type* of C.return.
- Then the instruction is valid with type $[t_1^*\ t^*] o {}_{x^*}[t_2^*]$, for any valid type $[t_1^*] o {}_{x^*}[t_2^*]$.

$$\frac{C.\mathsf{return} = [t^*] \qquad C \vdash [t_1^*] \rightarrow_{x^*} [t_2^*] \; \mathsf{ok}}{C \vdash \mathsf{return} : [t_1^* \; t^*] \rightarrow_{x^*} [t_2^*]}$$

Note: The return instruction is *stack-polymorphic*.

C.return is absent (set to ϵ) when validating an *expression* that is not a function body. This differs from it being set to the empty result type ($[\epsilon]$), which is the case for functions not returning anything.

$\mathsf{call}\ x$

- The function C.funcs[x] must be defined in the context.
- Then the instruction is valid with type C.funcs[x].

$$\frac{C.\mathsf{funcs}[x] = [t_1^*] \to [t_2^*]}{C \vdash \mathsf{call}\ x : [t_1^*] \to [t_2^*]}$$

call ref

- Let x be some type index for which C.types[x] is a function type of the form $[t_1^*] \to [t_2^*]$.
- Then the instruction is valid with type $[t_1^* \text{ (ref null } x)] \rightarrow [t_2^*]$.

$$\frac{C.\mathsf{types}[x] = [t_1^*] \to [t_2^*]}{C \vdash \mathsf{call_ref} : [t_1^* \ (\mathsf{ref} \ \mathsf{null} \ x)] \to [t_2^*]}$$

call_indirect x y

- The table C.tables[x] must be defined in the context.
- Let $limits\ t$ be the $table\ type\ C$.tables[x].
- ullet The $\it reference\ type\ t\ must\ match\ type\ ref\ null\ func.$
- ullet The type $C.\mathsf{types}[y]$ must be defined in the context.
- Let $[t_1^*] \rightarrow [t_2^*]$ be the function type C.types[y].
- Then the instruction is valid with type $[t_1^* \text{ i32}] \rightarrow [t_2^*]$.

$$\frac{C.\mathsf{tables}[x] = \mathit{limits}\; t \qquad C \vdash t \leq \mathsf{ref}\; \mathsf{null}\; \mathsf{func} \qquad C.\mathsf{types}[y] = [t_1^*] \to [t_2^*]}{C \vdash \mathsf{call_indirect}\; x\; y: [t_1^*\; \mathsf{i32}] \to [t_2^*]}$$

3.4.9 Instruction Sequences

Typing of instruction sequences is defined recursively.

Empty Instruction Sequence: ϵ

• The empty instruction sequence is valid with type $[t^*] \to [t^*]$, for any sequence of *value types* t^* .

$$\overline{C \vdash \epsilon : [t^*] \to [t^*]}$$

Non-empty Instruction Sequence: $instr^*$ $instr_N$

- The instruction sequence $instr^*$ must be valid with type $[t_1^*] \to {}_{x_1^*}[t_2^*]$, for some sequences of value types t_1^* and t_2^* .
- Let C' be the same *context* as C, but with:
 - locals the same as in C, except that for every *local index* x in x_1^* , the *local type* locals[x] has been updated to *initialization status SET*.
- Under context C', the instruction $instr_N$ must be valid with type $[t^*] \to {}_{x_2^*}[t_3^*]$, for some sequences of value types t^* and t_3^* .
- There must be a sequence of value types t_0^* , such that $t_2^* = t_0^* t'^*$ where the type sequence t'^* is as long as t^* .
- For each value type t'_i in t'^* and corresponding type t_i in t^* , the type t'_i must match t_i .
- Then the combined instruction sequence is valid with type $[t_1^*] \to x_1^* x_2^* [t_0^* \ t_3^*]$.

$$\frac{C \vdash instr^* : [t_1^*] \to {}_{x_1^*}[t_0^* \ t'^*]}{(init \ t = C.\mathsf{locals}[x_1])^*} \quad \frac{(C \vdash t' \le t)^* \quad C' \vdash instr_N : [t^*] \to {}_{x_2^*}[t_3^*]}{C' = C \ (\mathsf{with} \ C.\mathsf{locals}[x_1] = \mathsf{set} \ \ t)^*}{C \vdash instr^* \ instr_N : [t_1^*] \to {}_{x_1^* x_2^*}[t_0^* \ t_3^*]}$$

3.4.10 Expressions

Expressions expr are classified by result types of the form $[t^*]$.

 $instr^*$ end

- The instruction sequence $instr^*$ must be *valid* with some $type [] \rightarrow {}_{x^*}[{t'}^*]$.
- For each value type t'_i in t'^* and corresponding valid value type type t_i in t^* , t'_i matches t_i .
- Then the expression is valid with *result type* $[t^*]$.

$$\frac{C \vdash instr^* : [] \rightarrow_{x^*}[{t'}^*] \qquad C \vdash [t^*] \text{ ok} \qquad (C \vdash t' \leq t)^*}{C \vdash instr^* \text{ end } : [t^*]}$$

Constant Expressions

- In a constant expression $instr^*$ end all instructions in $instr^*$ must be constant.
- A constant instruction *instr* must be:
 - either of the form t.const c,
 - or of the form ref.null,
 - or of the form ref.func x,
 - or of the form global.get x, in which case C.globals[x] must be a global type of the form const t.

Note: Currently, constant expressions occurring as initializers of *globals* are further constrained in that contained global.get instructions are only allowed to refer to *imported* globals. This is enforced in the *validation rule for modules* by constraining the context C accordingly.

The definition of constant expression may be extended in future versions of WebAssembly.

3.5 Modules

Modules are valid when all the components they contain are valid. Furthermore, most definitions are themselves classified with a suitable type.

3.5. Modules 53

3.5.1 Functions

Functions func are classified by function types of the form $[t_1^*] \rightarrow [t_2^*]$.

{type x, locals t^* , body expr}

- The type C.types[x] must be defined in the context.
- Let $[t_1^*] \rightarrow [t_2^*]$ be the function type C.types[x].
- For each local declared by a *value type* t in t^* :
 - The local for type t must be valid with local type localtype_i.
- Let $local type^*$ be the concatenation of all $local type_i$.
- Let C' be the same *context* as C, but with:
 - locals set to the sequence of value types (set t_1)* localtype*, concatenating parameters and locals,
 - labels set to the singular sequence containing only result type $[t_2^*]$.
 - return set to the *result type* $[t_2^*]$.
- Under the context C', the expression expr must be valid with type $[t_2^*]$.
- Then the function definition is valid with type $[t_1^*] o [t_2^*].$

$$\frac{C.\mathsf{types}[x] = [t_1^*] \to [t_2^*] \qquad (C \vdash t : \mathit{init}\ t)^* \qquad C, \mathsf{locals}\ (\mathsf{set}\ t_1)^*\ (\mathit{init}\ t)^*, \mathsf{labels}\ [t_2^*], \mathsf{return}\ [t_2^*] \vdash \mathit{expr}: [t_2^*]}{C \vdash \{\mathsf{type}\ x, \mathsf{locals}\ t^*, \mathsf{body}\ \mathit{expr}\}: [t_1^*] \to [t_2^*]}$$

3.5.2 Locals

Locals are classified with local types.

 $\{type\ valtype\}$

- The value type valtype must be valid.
- If valtype is defaultable, then:
 - The local is valid with *local type* set *valtype*.
- Else:
 - The local is valid with *local type* unset *valtype*.

$$\begin{tabular}{ll} $C \vdash t$ ok & $C \vdash t$ defaultable} \\ \hline $C \vdash \{ \mbox{type } t \} : \mbox{set } t$ ok} \\ \hline $C \vdash t$ ok} \\ \hline $C \vdash \{ \mbox{LTYPE } t \} : \mbox{unset } t$ ok} \\ \hline \end{tabular}$$

Note: For cases where both rules are applicable, the former yields the more permissable type.

3.5.3 Tables

Tables table are classified by table types.

{type tabletype}

- The *table type tabletype* must be *valid*.
- Then the table definition is valid with type *tabletype*.

$$\frac{C \vdash tabletype \text{ ok} \qquad C \vdash tabletype \text{ defaultable}}{C \vdash \{\text{type } tabletype\}: tabletype}$$

3.5.4 Memories

Memories mem are classified by memory types.

{type memtype}

- The *memory type memtype* must be *valid*.
- Then the memory definition is valid with type memtype.

$$\frac{C \vdash \mathit{memtype} \ \mathsf{ok}}{C \vdash \{\mathsf{type} \ \mathit{memtype}\} : \mathit{memtype}}$$

3.5.5 Globals

Globals global are classified by global types of the form $mut\ t$.

 $\{ \text{type } mut \ t, \text{init } expr \}$

- The global type $mut\ t$ must be valid.
- The expression expr must be valid with result type [t].
- The expression *expr* must be *constant*.
- Then the global definition is valid with type $mut\ t$.

$$\frac{C \vdash \textit{mut } t \; \text{ok} \qquad C \vdash \textit{expr} : [t] \qquad C \vdash \textit{expr} \; \text{const}}{C \vdash \{ \text{type } \textit{mut } t, \text{init } \textit{expr} \} : \textit{mut } t}$$

3.5.6 Element Segments

Element segments *elem* are classified by the *reference type* of their elements.

3.5. Modules 55

 $\{ \text{type } t, \text{init } e^*, \text{mode } elemmode \}$

- The reference type t must be valid.
- For each e_i in e^* ,
 - The expression e_i must be *valid* with some *result type* [t].
 - The expression e_i must be *constant*.
- The element mode elemmode must be valid with some reference type t'.
- The reference type t must match the reference type t'.
- Then the element segment is valid with *reference type t*.

$$\frac{C \vdash t \text{ ok} \qquad (C \vdash e : [t])^* \qquad (C \vdash e \text{ const})^* \qquad C \vdash elemmode : t' \qquad C \vdash t \leq t'}{C \vdash \{\text{type } t, \text{init } e^*, \text{mode } elemmode\} : t}$$

passive

• The element mode is valid with any valid reference type.

$$\frac{C \vdash reftype \text{ ok}}{C \vdash passive : reftype}$$

active $\{ table \ x, offset \ expr \}$

- The table C.tables [x] must be defined in the context.
- Let $limits\ t$ be the $table\ type\ C$.tables[x].
- The expression *expr* must be *valid* with *result type* [i32].
- The expression *expr* must be *constant*.
- Then the element mode is valid with reference type t.

$$\begin{aligned} &C. \mathsf{tables}[x] = \mathit{limits}\ t \\ &C \vdash \mathit{expr}: [\mathsf{i32}] \quad C \vdash \mathit{expr}\ \mathsf{const} \\ &C \vdash \mathsf{active}\ \{\mathsf{table}\ x, \mathsf{offset}\ \mathit{expr}\}: t \end{aligned}$$

declarative

• The element mode is valid with any valid reference type.

$$\frac{C \vdash \mathit{reftype} \ \mathsf{ok}}{C \vdash \mathsf{declarative} : \mathit{reftype}}$$

3.5.7 Data Segments

Data segments data are not classified by any type but merely checked for well-formedness.

{init b^* , mode datamode}

- The data mode datamode must be valid.
- Then the data segment is valid.

$$\frac{C \vdash \textit{datamode ok}}{C \vdash \{\mathsf{init}\ b^*, \mathsf{mode}\ \textit{datamode}\}\ \mathsf{ok}}$$

passive

• The data mode is valid.

$$\overline{C \vdash \mathsf{passive} \; \mathsf{ok}}$$

active {memory x, offset expr}

- The memory $C.\mathsf{mems}[x]$ must be defined in the context.
- The expression *expr* must be *valid* with *result type* [i32].
- The expression *expr* must be *constant*.
- Then the data mode is valid.

$$\frac{C.\mathsf{mems}[x] = limits \qquad C \vdash expr: [\mathsf{i32}] \qquad C \vdash expr\; \mathsf{const}}{C \vdash \mathsf{active}\; \{\mathsf{memory}\; x, \mathsf{offset}\; expr\} \; \mathsf{ok}}$$

3.5.8 Start Function

Start function declarations start are not classified by any type.

 $\{ \mathsf{func} \ x \}$

- The function C.funcs[x] must be defined in the context.
- The type of $C.\mathsf{funcs}[x]$ must be $[] \to []$.
- Then the start function is valid.

$$\frac{C.\mathsf{funcs}[x] = [] \to []}{C \vdash \{\mathsf{func}\ x\} \ \mathsf{ok}}$$

3.5.9 Exports

Exports export and export descriptions exportdesc are classified by their external type.

3.5. Modules 57

{name name, desc exportdesc}

- The export description exportdesc must be valid with external type externtype.
- Then the export is valid with external type externtype.

$$\frac{C \vdash export desc : externtype}{C \vdash \{\mathsf{name}\ name, \mathsf{desc}\ export desc\} : externtype}$$

$\operatorname{func} x$

- The function C-funcs[x] must be defined in the context.
- Then the export description is valid with external type func C-funcs[x].

$$\frac{C.\mathsf{funcs}[x] = \mathit{functype}}{C \vdash \mathsf{func}\; x : \mathsf{func}\; \mathit{functype}}$$

table x

- The table C.tables[x] must be defined in the context.
- Then the export description is valid with *external type* table C.tables [x].

$$\frac{C.\mathsf{tables}[x] = \mathit{tabletype}}{C \vdash \mathsf{table}\; x : \mathsf{table}\; \mathit{tabletype}}$$

mem x

- The memory $C.\mathsf{mems}[x]$ must be defined in the context.
- Then the export description is valid with external type mem C.mems[x].

$$\frac{C.\mathsf{mems}[x] = \mathit{memtype}}{C \vdash \mathsf{mem}\; x : \mathsf{mem}\; \mathit{memtype}}$$

$\mathsf{global}\ x$

- The global C.globals[x] must be defined in the context.
- Then the export description is valid with ${\it external\ type\ global\ } C.{\it globals}[x].$

$$\frac{C.\mathsf{globals}[x] = \mathit{globaltype}}{C \vdash \mathsf{global} \; x : \mathsf{global} \; \mathit{globaltype}}$$

3.5.10 Imports

Imports import and import descriptions importdesc are classified by external types.

{module $name_1$, name $name_2$, desc importdesc}

- The import description *importdesc* must be valid with type *externtype*.
- Then the import is valid with type *externtype*.

$$\frac{C \vdash importdesc : externtype}{C \vdash \{\mathsf{module}\ name_1, \mathsf{name}\ name_2, \mathsf{desc}\ importdesc\} : externtype}$$

func x

- The function type C.types[x] must be defined in the context.
- Let $[t_1^*] \to [t_2^*]$ be the function type C.types [x].
- Then the import description is valid with type func $[t_1^*] o [t_2^*]$.

$$\frac{C.\mathsf{types}[x] = [t_1^*] \rightarrow [t_2^*]}{C \vdash \mathsf{func}\ x : \mathsf{func}\ [t_1^*] \rightarrow [t_2^*]}$$

table tabletype

- The table type tabletype must be valid.
- Then the import description is valid with type table *tabletype*.

$$\frac{C \vdash tabletype \text{ ok}}{C \vdash \mathsf{table} \ tabletype} : \mathsf{table} \ tabletype}$$

$mem \ mem type$

- The memory type *memtype* must be *valid*.
- Then the import description is valid with type mem memtype.

$$\frac{C \vdash \mathit{memtype} \ \mathsf{ok}}{C \vdash \mathsf{mem} \ \mathit{memtype} : \mathsf{mem} \ \mathit{memtype}}$$

global globaltype

- The global type globaltype must be valid.
- Then the import description is valid with type global globaltype.

$$\frac{C \vdash \mathit{globaltype} \ \mathsf{ok}}{C \vdash \mathsf{global} \ \mathit{globaltype}} : \mathsf{global} \ \mathit{globaltype}$$

3.5.11 Modules

Modules are classified by their mapping from the external types of their imports to those of their exports.

A module is entirely *closed*, that is, its components can only refer to definitions that appear in the module itself. Consequently, no initial *context* is required. Instead, the context C for validation of the module's content is constructed from the definitions in the module.

- Let *module* be the module to validate.
- Let C be a *context* where:
 - C.types is module.types,

3.5. Modules 59

- C.funcs is funcs(it^*) concatenated with ft^* , with the import's external types it^* and the internal function types ft^* as determined below,
- C.tables is tables (it^*) concatenated with tt^* , with the import's external types it^* and the internal table types tt^* as determined below,
- C.mems is mems(it^*) concatenated with mt^* , with the import's external types it^* and the internal memory types mt^* as determined below,
- C.globals is globals(it^*) concatenated with gt^* , with the import's external types it^* and the internal global types gt^* as determined below,
- C.elems is rt^* as determined below,
- C.datas is okⁿ, where n is the length of the vector module.datas,
- C.locals is empty,
- C.labels is empty,
- C.return is empty.
- C.refs is the set funcidx(module with funcs = ϵ with start = ϵ), i.e., the set of function indices occurring in the module, except in its functions or start function.
- For each function type $functype_i$ in module.types:
 - Let C'_i be the *context* where C'_i types is C types [0:i] and all other fields are empty.
 - The function $functype_i$ must be valid under context C'_i .
- Let C'' be the *context* where:
 - C''.globals is the sequence globals(it^*),
 - C''.types is the same as C.types,
 - C''.funcs is the same as C.funcs,
 - C''.refs is the same as C.refs,
 - all other fields are empty.
- Under the context C:
 - For each $func_i$ in module funcs, the definition $func_i$ must be valid with a function type ft_i .
 - For each $table_i$ in module.tables, the definition $table_i$ must be valid with a table type tt_i .
 - For each mem_i in module mems, the definition mem_i must be valid with a memory type mt_i.
 - For each *global*_i in *module*.globals:
 - * Under the context C'', the definition $global_i$ must be valid with a global type gt_i .
 - For each elem_i in module.elems, the segment elem_i must be valid with reference type rt_i.
 - For each $data_i$ in module.datas, the segment $data_i$ must be valid.
 - If *module*.start is non-empty, then *module*.start must be *valid*.
 - For each $import_i$ in module imports, the segment $import_i$ must be valid with an external type it_i .
 - For each $export_i$ in module exports, the segment $export_i$ must be valid with external type et_i .
- The length of C-mems must not be larger than 1.
- All export names $export_i$.name must be different.
- Let ft^* be the concatenation of the internal function types ft_i , in index order.
- Let tt^* be the concatenation of the internal table types tt_i , in index order.
- Let mt^* be the concatenation of the internal memory types mt_i , in index order.
- Let gt^* be the concatenation of the internal global types gt_i , in index order.

- Let rt^* be the concatenation of the reference types rt_i , in index order.
- Let it^* be the concatenation of external types it_i of the imports, in index order.
- Let et^* be the concatenation of external types et_i of the exports, in index order.
- Then the module is valid with external types $it^* \rightarrow et^*$.

 $\vdash module : it^* \rightarrow et^*$

where:

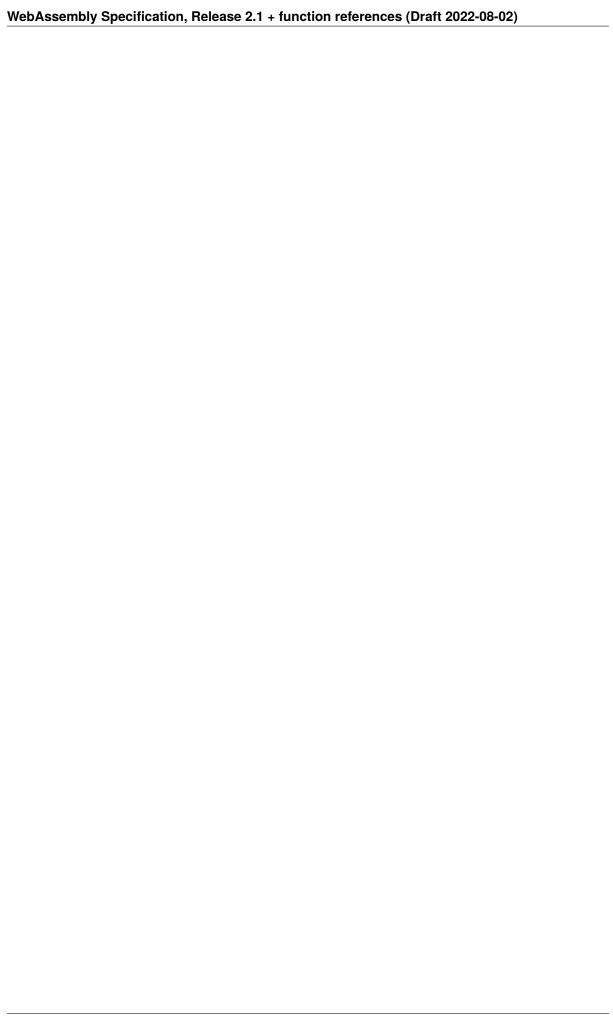
$$\frac{ \vdash \textit{type*} \; \text{ok} \qquad \{ \text{types} \; \textit{type*} \} \vdash \textit{type} \; \text{ok} }{ \vdash \textit{type*} \; \textit{type} \; \text{ok} } \qquad \frac{}{\vdash \epsilon \; \text{ok}}$$

Note: Most definitions in a module – particularly functions – are mutually recursive. Consequently, the definition of the *context* C in this rule is recursive: it depends on the outcome of validation of the function, table, memory, and global definitions contained in the module, which itself depends on C. However, this recursion is just a specification device. All types needed to construct C can easily be determined from a simple pre-pass over the module that does not perform any actual validation.

Globals, however, are not recursive. The effect of defining the limited context C' for validating the module's globals is that their initialization expressions can only access functions and imported globals and nothing else.

Note: The restriction on the number of memories may be lifted in future versions of WebAssembly.

3.5. Modules 61



CHAPTER 4

Execution

4.1 Conventions

WebAssembly code is *executed* when *instantiating* a module or *invoking* an *exported* function on the resulting module *instance*.

Execution behavior is defined in terms of an *abstract machine* that models the *program state*. It includes a *stack*, which records operand values and control constructs, and an abstract *store* containing global state.

For each instruction, there is a rule that specifies the effect of its execution on the program state. Furthermore, there are rules describing the instantiation of a module. As with *validation*, all rules are given in two *equivalent* forms:

- 1. In *prose*, describing the execution in intuitive form.
- 2. In *formal notation*, describing the rule in mathematical form. ¹⁷

Note: As with validation, the prose and formal rules are equivalent, so that understanding of the formal notation is *not* required to read this specification. The formalism offers a more concise description in notation that is used widely in programming languages semantics and is readily amenable to mathematical proof.

4.1.1 Prose Notation

Execution is specified by stylised, step-wise rules for each *instruction* of the *abstract syntax*. The following conventions are adopted in stating these rules.

- ullet The execution rules implicitly assume a given store S.
- The execution rules also assume the presence of an implicit *stack* that is modified by *pushing* or *popping values*, *labels*, and *frames*.
- Certain rules require the stack to contain at least one frame. The most recent frame is referred to as the *current* frame.

¹⁷ The semantics is derived from the following article: Andreas Haas, Andreas Rossberg, Derek Schuff, Ben Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman. Bringing the Web up to Speed with WebAssembly¹⁸. Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017). ACM 2017.

¹⁸ https://dl.acm.org/citation.cfm?doid=3062341.3062363

- Both the store and the current frame are mutated by *replacing* some of their components. Such replacement is assumed to apply globally.
- The execution of an instruction may *trap*, in which case the entire computation is aborted and no further modifications to the store are performed by it. (Other computations can still be initiated afterwards.)
- The execution of an instruction may also end in a *jump* to a designated target, which defines the next instruction to execute.
- Execution can enter and exit instruction sequences that form blocks.
- Instruction sequences are implicitly executed in order, unless a trap or jump occurs.
- In various places the rules contain assertions expressing crucial invariants about the program state.

4.1.2 Formal Notation

Note: This section gives a brief explanation of the notation for specifying execution formally. For the interested reader, a more thorough introduction can be found in respective text books.¹⁹

The formal execution rules use a standard approach for specifying operational semantics, rendering them into *reduction rules*. Every rule has the following general form:

```
configuration \hookrightarrow configuration
```

A *configuration* is a syntactic description of a program state. Each rule specifies one *step* of execution. As long as there is at most one reduction rule applicable to a given configuration, reduction – and thereby execution – is *deterministic*. WebAssembly has only very few exceptions to this, which are noted explicitly in this specification.

For WebAssembly, a configuration typically is a tuple $(S; F; instr^*)$ consisting of the current *store* S, the *call frame* F of the current function, and the sequence of *instructions* that is to be executed. (A more precise definition is given *later*.)

To avoid unnecessary clutter, the store S and the frame F are omitted from reduction rules that do not touch them.

There is no separate representation of the *stack*. Instead, it is conveniently represented as part of the configuration's instruction sequence. In particular, *values* are defined to coincide with const instructions, and a sequence of const instructions can be interpreted as an operand "stack" that grows to the right.

Note: For example, the *reduction rule* for the i32.add instruction can be given as follows:

```
(i32.const n_1) (i32.const n_2) i32.add \hookrightarrow (i32.const (n_1 + n_2) \bmod 2^{32})
```

Per this rule, two const instructions and the add instruction itself are removed from the instruction stream and replaced with one new const instruction. This can be interpreted as popping two values off the stack and pushing the result.

When no result is produced, an instruction reduces to the empty sequence:

$$\mathsf{nop} \;\hookrightarrow\; \epsilon$$

Labels and frames are similarly defined to be part of an instruction sequence.

The order of reduction is determined by the definition of an appropriate evaluation context.

Reduction *terminates* when no more reduction rules are applicable. *Soundness* of the WebAssembly *type system* guarantees that this is only the case when the original instruction sequence has either been reduced to a sequence of const instructions, which can be interpreted as the *values* of the resulting operand stack, or if a *trap* occurred.

¹⁹ For example: Benjamin Pierce. Types and Programming Languages²⁰. The MIT Press 2002

²⁰ https://www.cis.upenn.edu/~bcpierce/tapl/

Note: For example, the following instruction sequence,

```
(f64.const x_1) (f64.const x_2) f64.neg (f64.const x_3) f64.add f64.mul
```

terminates after three steps:

```
\begin{array}{ll} & (\mathsf{f64}.\mathsf{const}\ x_1)\ (\mathsf{f64}.\mathsf{const}\ x_2)\ \mathsf{f64}.\mathsf{neg}\ (\mathsf{f64}.\mathsf{const}\ x_3)\ \mathsf{f64}.\mathsf{add}\ \mathsf{f64}.\mathsf{mul}\\ \hookrightarrow & (\mathsf{f64}.\mathsf{const}\ x_1)\ (\mathsf{f64}.\mathsf{const}\ x_4)\ (\mathsf{f64}.\mathsf{const}\ x_3)\ \mathsf{f64}.\mathsf{add}\ \mathsf{f64}.\mathsf{mul}\\ \hookrightarrow & (\mathsf{f64}.\mathsf{const}\ x_1)\ (\mathsf{f64}.\mathsf{const}\ x_5)\ \mathsf{f64}.\mathsf{mul}\\ \hookrightarrow & (\mathsf{f64}.\mathsf{const}\ x_6) \end{array} where x_4 = -x_2 and x_5 = -x_2 + x_3 and x_6 = x_1 \cdot (-x_2 + x_3).
```

4.2 Runtime Structure

Store, *stack*, and other *runtime structure* forming the WebAssembly abstract machine, such as *values* or *module instances*, are made precise in terms of additional auxiliary syntax.

4.2.1 Values

WebAssembly computations manipulate *values* of either the four basic *number types*, i.e., *integers* and *floating-point data* of 32 or 64 bit width each, or *vectors* of 128 bit width, or of *reference type*.

In most places of the semantics, values of different types can occur. In order to avoid ambiguities, values are therefore represented with an abstract syntax that makes their type explicit. It is convenient to reuse the same notation as for the const *instructions* and ref.null producing them.

References other than null are represented with additional *administrative instructions*. They either are *function references*, pointing to a specific *function address*, or *external references* pointing to an uninterpreted form of *extern address* that can be defined by the *embedder* to represent its own objects.

Note: Future versions of WebAssembly may add additional forms of reference.

Value types can have an associated default value; it is the respective value 0 for number types, 0 for vector types, and null for nullable reference types. For other references, no default value is defined, default_t hence is an optional value val^2 .

```
\begin{array}{lll} \operatorname{default}_t &= & t.\operatorname{const} 0 & (\operatorname{if} \ t = numtype) \\ \operatorname{default}_t &= & t.\operatorname{const} 0 & (\operatorname{if} \ t = vectype) \\ \operatorname{default}_t &= & \operatorname{ref.null} \ t & (\operatorname{if} \ t = (\operatorname{ref.null} \ heaptype)) \\ \operatorname{default}_t &= & \epsilon & (\operatorname{if} \ t = (\operatorname{ref. heaptype})) \end{array}
```

Convention

ullet The meta variable r ranges over reference values where clear from context.

4.2.2 Results

A result is the outcome of a computation. It is either a sequence of values or a trap.

```
result ::= val^*
```

Note: In the current version of WebAssembly, a result can consist of at most one value.

4.2.3 Store

The *store* represents all global state that can be manipulated by WebAssembly programs. It consists of the runtime representation of all *instances* of *functions*, *tables*, *memories*, and *globals*, *element segments*, and *data segments* that have been *allocated* during the life time of the abstract machine.²¹

It is an invariant of the semantics that no element or data instance is *addressed* from anywhere else but the owning module instances.

Syntactically, the store is defined as a *record* listing the existing instances of each category:

```
store ::= \{ \begin{tabular}{ll} funcs & funcinst*, \\ tables & tableinst*, \\ mems & meminst*, \\ globals & globalinst*, \\ elems & eleminst*, \\ datas & datainst* \} \end{tabular}
```

Convention

 $\bullet\,$ The meta variable S ranges over stores where clear from context.

4.2.4 Addresses

Function instances, table instances, memory instances, and global instances, element instances, and data instances in the *store* are referenced with abstract *addresses*. These are simply indices into the respective store component. In addition, an *embedder* may supply an uninterpreted set of *host addresses*.

```
addr
                 0 | 1 | 2 | ...
funcaddr
            ::=
                 addr
table addr
                 addr
            ::=
memaddr
            ::=
                 addr
globaladdr
            ::= addr
elemaddr
            ::= addr
dataaddr
            ::= addr
externaddr ::=
                 addr
```

An *embedder* may assign identity to *exported* store objects corresponding to their addresses, even where this identity is not observable from within WebAssembly code itself (such as for *function instances* or immutable *globals*).

²¹ In practice, implementations may apply techniques like garbage collection to remove objects from the store that are no longer referenced. However, such techniques are not semantically observable, and hence outside the scope of this specification.

Note: Addresses are *dynamic*, globally unique references to runtime objects, in contrast to *indices*, which are *static*, module-local references to their original definitions. A *memory address memaddr* denotes the abstract address *of* a memory *instance* in the store, not an offset *inside* a memory instance.

There is no specific limit on the number of allocations of store objects, hence logical addresses can be arbitrarily large natural numbers.

4.2.5 Module Instances

A *module instance* is the runtime representation of a *module*. It is created by *instantiating* a module, and collects runtime representations of all entities that are imported, defined, or exported by the module.

```
moduleinst ::= { types functype*, funcaddrs funcaddr*, tableaddrs tableaddr*, memaddrs memaddr*, globaladdrs globaladdr*, elemaddrs dataaddr*, dataaddrs dataaddr*, exports exportinst* }
```

Each component references runtime instances corresponding to respective declarations from the original module – whether imported or defined – in the order of their static *indices*. *Function instances*, *table instances*, *memory instances*, and *global instances* are referenced with an indirection through their respective *addresses* in the *store*.

It is an invariant of the semantics that all *export instances* in a given module instance have different *names*.

4.2.6 Function Instances

A *function instance* is the runtime representation of a *function*. It effectively is a *closure* of the original function over the runtime *module instance* of its originating *module*. The module instance is used to resolve references to other definitions during execution of the function.

```
\begin{array}{lll} \textit{funcinst} & ::= & \{ \text{type } \textit{functype}, \text{module } \textit{moduleinst}, \text{code } \textit{func} \} \\ & | & \{ \text{type } \textit{functype}, \text{hostcode } \textit{hostfunc} \} \\ & hostfunc & ::= & \dots \end{array}
```

A *host function* is a function expressed outside WebAssembly but passed to a *module* as an *import*. The definition and behavior of host functions are outside the scope of this specification. For the purpose of this specification, it is assumed that when *invoked*, a host function behaves non-deterministically, but within certain *constraints* that ensure the integrity of the runtime.

Note: Function instances are immutable, and their identity is not observable by WebAssembly code. However, the *embedder* might provide implicit or explicit means for distinguishing their *addresses*.

4.2.7 Table Instances

A table instance is the runtime representation of a table. It records its type and holds a vector of reference values.

```
tableinst ::= \{ type \ table type, elem \ vec(ref) \}
```

Table elements can be mutated through *table instructions*, the execution of an active *element segment*, or by external means provided by the *embedder*.

It is an invariant of the semantics that all table elements have a type *matching* the element type of *tabletype*. It also is an invariant that the length of the element vector never exceeds the maximum size of *tabletype*, if present.

4.2.8 Memory Instances

A memory instance is the runtime representation of a linear memory. It records its type and holds a vector of bytes.

```
meminst ::= \{type memtype, data vec(byte)\}
```

The length of the vector always is a multiple of the WebAssembly $page\ size$, which is defined to be the constant 65536 – abbreviated $64\,\mathrm{Ki}$.

The bytes can be mutated through *memory instructions*, the execution of an active *data segment*, or by external means provided by the *embedder*.

It is an invariant of the semantics that the length of the byte vector, divided by page size, never exceeds the maximum size of *memtype*, if present.

4.2.9 Global Instances

A *global instance* is the runtime representation of a *global* variable. It records its *type* and holds an individual *value*.

```
globalinst ::= \{type globaltype, value val\}
```

The value of mutable globals can be mutated through *variable instructions* or by external means provided by the *embedder*.

It is an invariant of the semantics that the value has a type matching the value type of globaltype.

4.2.10 Element Instances

An *element instance* is the runtime representation of an *element segment*. It holds a vector of references and their common *type*.

```
eleminst ::= \{ type \ reftype, elem \ vec(ref) \}
```

4.2.11 Data Instances

An data instance is the runtime representation of a data segment. It holds a vector of bytes.

```
datainst ::= \{ data \ vec(byte) \}
```

4.2.12 Export Instances

An *export instance* is the runtime representation of an *export*. It defines the export's *name* and the associated *external value*.

```
exportinst ::= \{name \ name, value \ externval\}
```

4.2.13 External Values

An *external value* is the runtime representation of an entity that can be imported or exported. It is an *address* denoting either a *function instance*, *table instance*, *memory instance*, or *global instances* in the shared *store*.

```
\begin{array}{cccc} externval & ::= & \mathsf{func}\,funcaddr \\ & | & \mathsf{table}\,tableaddr \\ & | & \mathsf{mem}\,memaddr \\ & | & \mathsf{global}\,globaladdr \end{array}
```

Conventions

The following auxiliary notation is defined for sequences of external values. It filters out entries of a specific kind in an order-preserving fashion:

```
• funcs(externval^*) = [funcaddr \mid (func funcaddr) \in externval^*]
```

- tables $(externval^*) = [tableaddr \mid (table tableaddr) \in externval^*]$
- $mems(externval^*) = [memaddr \mid (mem\ memaddr) \in externval^*]$
- $globals(externval^*) = [globaladdr | (global globaladdr) \in externval^*]$

4.2.14 Stack

Besides the *store*, most *instructions* interact with an implicit *stack*. The stack contains three kinds of entries:

- Values: the operands of instructions.
- Labels: active structured control instructions that can be targeted by branches.
- Activations: the call frames of active function calls.

These entries can occur on the stack in any order during the execution of a program. Stack entries are described by abstract syntax as follows.

Note: It is possible to model the WebAssembly semantics using separate stacks for operands, control constructs, and calls. However, because the stacks are interdependent, additional book keeping about associated stack heights would be required. For the purpose of this specification, an interleaved representation is simpler.

Values

Values are represented by themselves.

Labels

Labels carry an argument arity n and their associated branch target, which is expressed syntactically as an instruction sequence:

```
label ::= label_n \{instr^*\}
```

Intuitively, $instr^*$ is the *continuation* to execute when the branch is taken, in place of the original control construct.

Note: For example, a loop label has the form

$$label_n\{loop ... end\}$$

When performing a branch to this label, this executes the loop, effectively restarting it from the beginning. Conversely, a simple block label has the form

```
label_n\{\epsilon\}
```

When branching, the empty continuation ends the targeted block, such that execution can proceed with consecutive instructions.

Activations and Frames

Activation frames carry the return arity n of the respective function, hold the values of its *locals* (including arguments) in the order corresponding to their static *local indices*, and a reference to the function's own *module instance*:

```
activation ::= frame_n\{frame\}

frame ::= \{locals (val^?)^*, module module inst\}
```

Locals may be uninitialized, in which case they are empty. Locals are mutated by respective variable instructions.

Conventions

- ullet The meta variable L ranges over labels where clear from context.
- ullet The meta variable F ranges over frames where clear from context.
- The following auxiliary definition takes a *block type* and looks up the *function type* that it denotes in the current frame:

```
\operatorname{expand}_F(typeidx) = F.\mathsf{module.types}[typeidx]

\operatorname{expand}_F([valtype^?]) = [] \to [valtype^?]
```

4.2.15 Administrative Instructions

Note: This section is only relevant for the *formal notation*.

In order to express the reduction of *traps*, *calls*, and *control instructions*, the syntax of instructions is extended to include the following *administrative instructions*:

```
\begin{array}{lll} instr & ::= & \dots \\ & & | & trap \\ & | & ref \ funcaddr \\ & | & ref.extern \ externaddr \\ & | & invoke \ funcaddr \\ & | & label_n \{instr^*\} \ instr^* \ end \\ & | & frame_n \{frame\} \ instr^* \ end \\ \end{array}
```

The trap instruction represents the occurrence of a trap. Traps are bubbled up through nested instruction sequences, ultimately reducing the entire program to a single trap instruction, signalling abrupt termination.

The ref instruction represents function reference values. Similarly, ref.extern represents external references.

The invoke instruction represents the imminent invocation of a *function instance*, identified by its *address*. It unifies the handling of different forms of calls.

The label and frame instructions model *labels* and *frames* "on the stack". Moreover, the administrative syntax maintains the nesting structure of the original structured control instruction or function body and their instruction

sequences with an end marker. That way, the end of the inner instruction sequence is known when part of an outer sequence.

Note: For example, the *reduction rule* for block is:

```
\mathsf{block}\ [t^n]\ instr^*\ \mathsf{end} \quad \hookrightarrow \quad \mathsf{label}_n\{\epsilon\}\ instr^*\ \mathsf{end}
```

This replaces the block with a label instruction, which can be interpreted as "pushing" the label on the stack. When end is reached, i.e., the inner instruction sequence has been reduced to the empty sequence – or rather, a sequence of n const instructions representing the resulting values – then the label instruction is eliminated courtesy of its own reduction rule:

$$label_m\{instr^*\}\ val^n\ end\ \hookrightarrow\ val^n$$

This can be interpreted as removing the label from the stack and only leaving the locally accumulated operand values.

Block Contexts

In order to specify the reduction of *branches*, the following syntax of *block contexts* is defined, indexed by the count k of labels surrounding a *hole* [_] that marks the place where the next step of computation is taking place:

$$B^0$$
 ::= $val^* [_] instr^*$
 B^{k+1} ::= $val^* [abel_n \{ instr^* \} B^k]$ end $instr^*$

This definition allows to index active labels surrounding a *branch* or *return* instruction.

Note: For example, the *reduction* of a simple branch can be defined as follows:

$$label_0\{instr^*\} B^l[br\ l] end \hookrightarrow instr^*$$

Here, the hole $[_]$ of the context is instantiated with a branch instruction. When a branch occurs, this rule replaces the targeted label and associated instruction sequence with the label's continuation. The selected label is identified through the *label index l*, which corresponds to the number of surrounding *label* instructions that must be hopped over – which is exactly the count encoded in the index of a block context.

Configurations

A configuration consists of the current store and an executing thread.

A thread is a computation over *instructions* that operates relative to a current *frame* referring to the *module instance* in which the computation runs, i.e., where the current function originates from.

```
config ::= store; thread

thread ::= frame; instr^*
```

Note: The current version of WebAssembly is single-threaded, but configurations with multiple threads may be supported in the future.

Evaluation Contexts

Finally, the following definition of *evaluation context* and associated structural rules enable reduction inside instruction sequences and administrative forms as well as the propagation of traps:

```
E \quad ::= \quad [\_] \mid val^* \; E \; instr^* \mid \mathsf{label}_n \{instr^*\} \; E \; \mathsf{end} S; F; E[instr^*] \quad \hookrightarrow \quad S'; F'; E[instr'^*] \quad \quad (\mathsf{if} \; S; F; instr^* \hookrightarrow S'; F'; instr'^*) S; F; \mathsf{frame}_n \{F'\} \; instr^* \; \mathsf{end} \quad (\mathsf{if} \; S; F'; \mathsf{frame}_n \{F''\} \; instr'^* \; \mathsf{end} \quad (\mathsf{if} \; S; F'; instr^* \hookrightarrow S'; F''; instr'^*) S; F; E[\mathsf{trap}] \quad \hookrightarrow \quad S; F; \mathsf{trap} \quad (\mathsf{if} \; E \neq [\_]) S; F; \mathsf{frame}_n \{F'\} \; \mathsf{trap} \; \mathsf{end} \quad \hookrightarrow \quad S; F; \mathsf{trap}
```

Reduction terminates when a thread's instruction sequence has been reduced to a *result*, that is, either a sequence of *values* or to a trap.

Note: The restriction on evaluation contexts rules out contexts like $[\]$ and ϵ $[\]$ ϵ for which E[trap] = trap.

For an example of reduction under evaluation contexts, consider the following instruction sequence.

```
(f64.const x_1) (f64.const x_2) f64.neg (f64.const x_3) f64.add f64.mul
```

This can be decomposed into $E[(f64.const x_2) f64.neg]$ where

$$E = (\text{f64.const } x_1) [_] (\text{f64.const } x_3) \text{ f64.add f64.mul}$$

Moreover, this is the *only* possible choice of evaluation context where the contents of the hole matches the left-hand side of a reduction rule.

4.3 Numerics

72

Numeric primitives are defined in a generic manner, by operators indexed over a bit width N.

Some operators are *non-deterministic*, because they can return one of several possible results (such as different *NaN* values). Technically, each operator thus returns a *set* of allowed values. For convenience, deterministic results are expressed as plain values, which are assumed to be identified with a respective singleton set.

Some operators are *partial*, because they are not defined on certain inputs. Technically, an empty set of results is returned for these inputs.

In formal notation, each operator is defined by equational clauses that apply in decreasing order of precedence. That is, the first clause that is applicable to the given arguments defines the result. In some cases, similar clauses are combined into one by using the notation \pm or \mp . When several of these placeholders occur in a single clause, then they must be resolved consistently: either the upper sign is chosen for all of them or the lower sign.

Note: For example, the fcopysign operator is defined as follows:

fcopysign_N(
$$\pm p_1, \pm p_2$$
) = $\pm p_1$
fcopysign_N($\pm p_1, \mp p_2$) = $\mp p_1$

This definition is to be read as a shorthand for the following expansion of each clause into two separate ones:

```
fcopysign<sub>N</sub>(+p<sub>1</sub>, +p<sub>2</sub>) = +p<sub>1</sub>
fcopysign<sub>N</sub>(-p<sub>1</sub>, -p<sub>2</sub>) = -p<sub>1</sub>
fcopysign<sub>N</sub>(+p<sub>1</sub>, -p<sub>2</sub>) = -p<sub>1</sub>
fcopysign<sub>N</sub>(-p<sub>1</sub>, +p<sub>2</sub>) = +p<sub>1</sub>
```

Numeric operators are lifted to input sequences by applying the operator element-wise, returning a sequence of results. When there are multiple inputs, they must be of equal length.

$$op(c_1^n, \dots, c_k^n) = op(c_1^n[0], \dots, c_k^n[0]) \dots op(c_1^n[n-1], \dots, c_k^n[n-1])$$

Note: For example, the unary operator fabs, when given a sequence of floating-point values, return a sequence of floating-point results:

$$fabs_N(z^n) = fabs_N(z[0]) \dots fabs_N(z[n])$$

The binary operator iadd, when given two sequences of integers of the same length, n, return a sequence of integer results:

$$iadd_N(i_1^n, i_2^n) = iadd_N(i_1[0], i_2[0]) \dots iadd_N(i_1[n], i_2[n])$$

Conventions:

- The meta variable d is used to range over single bits.
- The meta variable p is used to range over (signless) *magnitudes* of floating-point values, including nan and ∞ .
- The meta variable q is used to range over (signless) rational magnitudes, excluding nan or ∞ .
- The notation f^{-1} denotes the inverse of a bijective function f.
- Truncation of rational values is written $trunc(\pm q)$, with the usual mathematical definition:

$$\operatorname{trunc}(\pm q) = \pm i \quad (\text{if } i \in \mathbb{N} \land +q -1 < i \le +q)$$

- Saturation of integers is written $\operatorname{sat}^{\mathsf{u}}_{N}(i)$ and $\operatorname{sat}^{\mathsf{s}}_{N}(i)$. The arguments to these two functions range over arbitrary signed integers.
 - Unsigned saturation, $\operatorname{sat}^{\mathsf{u}}_{N}(i)$ clamps i to between 0 and $2^{N}-1$:

$$\begin{array}{lll} \operatorname{sat^u}_N(i) &=& 2^N-1 & & (\text{if } i > 2^N-1) \\ \operatorname{sat^u}_N(i) &=& 0 & & (\text{if } i < 0) \\ \operatorname{sat^u}_N(i) &=& i & & (\text{otherwise}) \end{array}$$

- Signed saturation, sat^s_N(i) clamps i to between -2^{N-1} and $2^{N-1} - 1$:

$$\begin{array}{lll} \operatorname{sat^s}_N(i) & = & \operatorname{signed}_N^{-1}(-2^{N-1}) & \quad \text{(if } i < -2^{N-1}) \\ \operatorname{sat^s}_N(i) & = & \operatorname{signed}_N^{-1}(2^{N-1}-1) & \quad \text{(if } i > 2^{N-1}-1) \\ \operatorname{sat^s}_N(i) & = & i & \quad \text{(otherwise)} \end{array}$$

4.3.1 Representations

Numbers have an underlying binary representation as a sequence of bits:

$$bits_{iN}(i) = ibits_{N}(i)$$

 $bits_{fN}(z) = fbits_{N}(z)$

Each of these functions is a bijection, hence they are invertible.

Integers

Integers are represented as base two unsigned numbers:

$$ibits_N(i) = d_{N-1} \dots d_0 \qquad (i = 2^{N-1} \cdot d_{N-1} + \dots + 2^0 \cdot d_0)$$

Boolean operators like \land , \lor , or \lor are lifted to bit sequences of equal length by applying them pointwise.

Floating-Point

Floating-point values are represented in the respective binary format defined by IEEE 754-2019²² (Section 3.4):

```
\begin{array}{lll} \mathrm{fbits}_N(\pm(1+m\cdot 2^{-M})\cdot 2^e) &=& \mathrm{fsign}(\pm) \, \mathrm{ibits}_E(e+\mathrm{fbias}_N) \, \mathrm{ibits}_M(m) \\ \mathrm{fbits}_N(\pm(0+m\cdot 2^{-M})\cdot 2^e) &=& \mathrm{fsign}(\pm) \, (0)^E \, \mathrm{ibits}_M(m) \\ \mathrm{fbits}_N(\pm\infty) &=& \mathrm{fsign}(\pm) \, (1)^E \, (0)^M \\ \mathrm{fbits}_N(\pm \mathrm{nan}(n)) &=& \mathrm{fsign}(\pm) \, (1)^E \, \mathrm{ibits}_M(n) \\ \mathrm{fbias}_N &=& 2^{E-1}-1 \\ \mathrm{fsign}(+) &=& 0 \\ \mathrm{fsign}(-) &=& 1 \end{array}
```

where $M = \operatorname{signif}(N)$ and $E = \operatorname{expon}(N)$.

Storage

When a number is stored into *memory*, it is converted into a sequence of *bytes* in little endian²³ byte order:

```
bytes<sub>t</sub>(i) = littleendian(bits<sub>t</sub>(i))

littleendian(\epsilon) = \epsilon

littleendian(d^8 d'^*) = littleendian(d'^*) ibits<sub>8</sub><sup>-1</sup>(d^8)
```

Again these functions are invertable bijections.

Vectors

Numeric vectors have the same underlying representation as an i128. They can also be interpreted as a sequence of numeric values packed into a v128 with a particular *shape*.

```
lanes<sub>t×N</sub>(c) = c_0 \dots c_{N-1}

(where B = |t|/8

\land b^{16} = \text{bytes}_{i128}(c)

\land c_i = \text{bytes}_t^{-1}(b^{16}[i \cdot B : B])
```

These functions are bijections, so they are invertible.

4.3.2 Integer Operations

Sign Interpretation

Integer operators are defined on iN values. Operators that use a signed interpretation convert the value using the following definition, which takes the two's complement when the value lies in the upper half of the value range (i.e., its most significant bit is 1):

$$\operatorname{signed}_{N}(i) = i \qquad (0 \le i < 2^{N-1})$$

 $\operatorname{signed}_{N}(i) = i - 2^{N} \qquad (2^{N-1} \le i < 2^{N})$

This function is bijective, and hence invertible.

²² https://ieeexplore.ieee.org/document/8766229

²³ https://en.wikipedia.org/wiki/Endianness#Little-endian

Boolean Interpretation

The integer result of predicates - i.e., *tests* and *relational* operators - is defined with the help of the following auxiliary function producing the value 1 or 0 depending on a condition.

$$bool(C) = 1$$
 (if C)
 $bool(C) = 0$ (otherwise)

 $iadd_N(i_1, i_2)$

• Return the result of adding i_1 and i_2 modulo 2^N .

$$iadd_N(i_1, i_2) = (i_1 + i_2) \bmod 2^N$$

 $isub_N(i_1, i_2)$

• Return the result of subtracting i_2 from i_1 modulo 2^N .

$$isub_N(i_1, i_2) = (i_1 - i_2 + 2^N) \bmod 2^N$$

 $imul_N(i_1, i_2)$

• Return the result of multiplying i_1 and i_2 modulo 2^N .

$$\operatorname{imul}_N(i_1, i_2) = (i_1 \cdot i_2) \bmod 2^N$$

 $idiv_u_N(i_1, i_2)$

- If i_2 is 0, then the result is undefined.
- Else, return the result of dividing i_1 by i_2 , truncated toward zero.

$$\begin{array}{lcl} \operatorname{idiv_u_N}(i_1,0) & = & \{\} \\ \operatorname{idiv_u_N}(i_1,i_2) & = & \operatorname{trunc}(i_1/i_2) \end{array}$$

Note: This operator is *partial*.

 $idiv_s_N(i_1, i_2)$

- Let j_1 be the signed interpretation of i_1 .
- Let j_2 be the signed interpretation of i_2 .
- If j_2 is 0, then the result is undefined.
- Else if j_1 divided by j_2 is 2^{N-1} , then the result is undefined.
- Else, return the result of dividing j_1 by j_2 , truncated toward zero.

```
\begin{array}{lcl} \operatorname{idiv\_s}_N(i_1,0) &=& \{ \} \\ \operatorname{idiv\_s}_N(i_1,i_2) &=& \{ \} \\ \operatorname{idiv\_s}_N(i_1,i_2) &=& \operatorname{signed}_N^{-1}(\operatorname{trunc}(\operatorname{signed}_N(i_1)/\operatorname{signed}_N(i_2))) \end{array}
```

Note: This operator is *partial*. Besides division by 0, the result of $(-2^{N-1})/(-1) = +2^{N-1}$ is not representable as an N-bit signed integer.

irem_ $\mathbf{u}_N(i_1, i_2)$

- If i_2 is 0, then the result is undefined.
- Else, return the remainder of dividing i_1 by i_2 .

Note: This operator is *partial*.

As long as both operators are defined, it holds that $i_1 = i_2 \cdot \mathrm{idiv_u}(i_1, i_2) + \mathrm{irem_u}(i_1, i_2)$.

irem_s_N (i_1, i_2)

- Let j_1 be the signed interpretation of i_1 .
- Let j_2 be the signed interpretation of i_2 .
- If i_2 is 0, then the result is undefined.
- Else, return the remainder of dividing j_1 by j_2 , with the sign of the dividend j_1 .

$$\begin{array}{rcl} \operatorname{irem_s}_N(i_1,0) & = & \{\} \\ \operatorname{irem_s}_N(i_1,i_2) & = & \operatorname{signed}_N^{-1}(j_1-j_2\cdot\operatorname{trunc}(j_1/j_2)) \\ & & (\operatorname{where}\ j_1 = \operatorname{signed}_N(i_1) \wedge j_2 = \operatorname{signed}_N(i_2)) \end{array}$$

Note: This operator is *partial*.

As long as both operators are defined, it holds that $i_1 = i_2 \cdot \text{idiv_s}(i_1, i_2) + \text{irem_s}(i_1, i_2)$.

 $inot_N(i)$

• Return the bitwise negation of i.

$$\operatorname{inot}_{N}(i) = \operatorname{ibits}_{N}^{-1}(\operatorname{ibits}_{N}(i) \vee \operatorname{ibits}_{N}(2^{N} - 1))$$

 $iand_N(i_1, i_2)$

• Return the bitwise conjunction of i_1 and i_2 .

```
\operatorname{iand}_{N}(i_{1}, i_{2}) = \operatorname{ibits}_{N}^{-1}(\operatorname{ibits}_{N}(i_{1}) \wedge \operatorname{ibits}_{N}(i_{2}))
```

 $iandnot_N(i_1, i_2)$

• Return the bitwise conjunction of i_1 and the bitwise negation of i_2 .

```
iandnot_N(i_1, i_2) = iand_N(i_1, inot_N(i_2))
```

$ior_N(i_1, i_2)$

• Return the bitwise disjunction of i_1 and i_2 .

$$ior_N(i_1, i_2) = ibits_N^{-1}(ibits_N(i_1) \vee ibits_N(i_2))$$

$ixor_N(i_1,i_2)$

• Return the bitwise exclusive disjunction of i_1 and i_2 .

$$ixor_N(i_1, i_2) = ibits_N^{-1}(ibits_N(i_1) \vee ibits_N(i_2))$$

$ishl_N(i_1,i_2)$

- Let k be i_2 modulo N.
- Return the result of shifting i_1 left by k bits, modulo 2^N .

$$\operatorname{ishl}_N(i_1,i_2) \quad = \quad \operatorname{ibits}_N^{-1}(d_2^{N-k}\ 0^k) \quad (\text{if } \operatorname{ibits}_N(i_1) = d_1^k\ d_2^{N-k} \wedge k = i_2 \bmod N)$$

$ishr_u_N(i_1, i_2)$

- Let k be i_2 modulo N.
- Return the result of shifting i_1 right by k bits, extended with 0 bits.

$$ishr_u_N(i_1, i_2) = ibits_N^{-1}(0^k d_1^{N-k}) \quad (if \ ibits_N(i_1) = d_1^{N-k} d_2^k \wedge k = i_2 \ mod \ N)$$

$ishr_s_N(i_1, i_2)$

- Let k be i_2 modulo N.
- Return the result of shifting i_1 right by k bits, extended with the most significant bit of the original value.

$$ishr_s_N(i_1, i_2) = ibits_N^{-1}(d_0^{k+1} d_1^{N-k-1})$$
 (if $ibits_N(i_1) = d_0 d_1^{N-k-1} d_2^k \wedge k = i_2 \mod N$)

$irotl_N(i_1, i_2)$

- Let k be i_2 modulo N.
- Return the result of rotating i_1 left by k bits.

$$irotl_N(i_1, i_2) = ibits_N^{-1}(d_2^{N-k} d_1^k)$$
 (if $ibits_N(i_1) = d_1^k d_2^{N-k} \wedge k = i_2 \mod N$)

$irotr_N(i_1, i_2)$

- Let k be i_2 modulo N.
- Return the result of rotating i_1 right by k bits.

$$\operatorname{irotr}_N(i_1,i_2) \quad = \quad \operatorname{ibits}_N^{-1}(d_2^k \ d_1^{N-k}) \quad (\text{if } \operatorname{ibits}_N(i_1) = d_1^{N-k} \ d_2^k \wedge k = i_2 \bmod N)$$

$iclz_N(i)$

• Return the count of leading zero bits in i; all bits are considered leading zeros if i is 0.

$$iclz_N(i) = k$$
 (if $ibits_N(i) = 0^k (1 d^*)$?)

$ictz_N(i)$

• Return the count of trailing zero bits in i; all bits are considered trailing zeros if i is 0.

$$ictz_N(i) = k$$
 (if $ibits_N(i) = (d^* 1)^? 0^k$)

$ipopcnt_N(i)$

• Return the count of non-zero bits in i.

$$ipopcnt_N(i) = k \quad (if ibits_N(i) = (0^* 1)^k 0^*)$$

$ieqz_N(i)$

• Return 1 if i is zero, 0 otherwise.

$$ieqz_N(i) = bool(i = 0)$$

$ieq_N(i_1,i_2)$

• Return 1 if i_1 equals i_2 , 0 otherwise.

$$ieq_N(i_1, i_2) = bool(i_1 = i_2)$$

$ine_N(i_1,i_2)$

• Return 1 if i_1 does not equal i_2 , 0 otherwise.

$$\operatorname{ine}_N(i_1, i_2) = \operatorname{bool}(i_1 \neq i_2)$$

ilt_ $\mathbf{u}_N(i_1, i_2)$

• Return 1 if i_1 is less than i_2 , 0 otherwise.

$$ilt_u_N(i_1, i_2) = bool(i_1 < i_2)$$

ilt_ $s_N(i_1, i_2)$

- Let j_1 be the signed interpretation of i_1 .
- Let j_2 be the signed interpretation of i_2 .
- Return 1 if j_1 is less than j_2 , 0 otherwise.

$$ilt_s_N(i_1, i_2) = bool(signed_N(i_1) < signed_N(i_2))$$

 $\mathrm{igt}\underline{}\mathrm{u}_N(i_1,i_2)$

• Return 1 if i_1 is greater than i_2 , 0 otherwise.

$$\operatorname{igt}_{\mathbf{u}_{N}}(i_{1}, i_{2}) = \operatorname{bool}(i_{1} > i_{2})$$

 $igt_s_N(i_1, i_2)$

- Let j_1 be the signed interpretation of i_1 .
- Let j_2 be the signed interpretation of i_2 .
- Return 1 if j_1 is greater than j_2 , 0 otherwise.

$$igt_s_N(i_1, i_2) = bool(signed_N(i_1) > signed_N(i_2))$$

 $ile_u_N(i_1, i_2)$

• Return 1 if i_1 is less than or equal to i_2 , 0 otherwise.

$$ile_u_N(i_1, i_2) = bool(i_1 \leq i_2)$$

ile_ $s_N(i_1, i_2)$

- Let j_1 be the signed interpretation of i_1 .
- Let j_2 be the signed interpretation of i_2 .
- Return 1 if j_1 is less than or equal to j_2 , 0 otherwise.

$$\mathrm{ile_s}_N(i_1,i_2) \ = \ \mathrm{bool}(\mathrm{signed}_N(i_1) \leq \mathrm{signed}_N(i_2))$$

 $\mathrm{ige}_\mathbf{u}_N(i_1,i_2)$

• Return 1 if i_1 is greater than or equal to i_2 , 0 otherwise.

$$ige_u_N(i_1, i_2) = bool(i_1 \ge i_2)$$

 $ige_s_N(i_1, i_2)$

- Let j_1 be the signed interpretation of i_1 .
- Let j_2 be the signed interpretation of i_2 .
- Return 1 if j_1 is greater than or equal to j_2 , 0 otherwise.

$$ige_s_N(i_1, i_2) = bool(signed_N(i_1) \ge signed_N(i_2))$$

iextend $M_s_N(i)$

• Return extend $_{M,N}(i)$.

$$\operatorname{iextend} M_{s_N}(i) = \operatorname{extend}_{M,N}(i)$$

$ibitselect_N(i_1, i_2, i_3)$

- Let j_1 be the bitwise conjunction of i_1 and i_3 .
- Let j_3' be the bitwise negation of i_3 .
- Let j_2 be the bitwise conjunction of i_2 and j_3' .
- Return the bitwise disjunction of j_1 and j_2 .

$$ibitselect_N(i_1, i_2, i_3) = ior_N(iand_N(i_1, i_3), iand_N(i_2, inot_N(i_3)))$$

$iabs_N(i)$

- Let j be the signed interpretation of i.
- If j is greater than or equal to 0, then return i.
- Else return the negation of j, modulo 2^N .

$$\begin{array}{lll} \mathrm{iabs}_N(i) & = & i & \quad \text{(if } \mathrm{signed}_N(i) \geq 0) \\ \mathrm{iabs}_N(i) & = & -\mathrm{signed}_N(i) \bmod 2^N & \quad \text{(otherwise)} \end{array}$$

$ineg_N(i)$

• Return the result of negating i, modulo 2^N .

$$\operatorname{ineg}_N(i) = (2^N - i) \mod 2^N$$

$\min_{\mathbf{u}} \mathbf{u}_N(i_1, i_2)$

• Return i_1 if $ilt_u_N(i_1, i_2)$ is 1, return i_2 otherwise.

$$\underset{i\min_{N}}{\min_{N}}(i_1, i_2) = i_1 \quad (\text{if } ilt_{N}(i_1, i_2) = 1) \\
\underset{i\min_{N}}{\min_{N}}(i_1, i_2) = i_2 \quad (\text{otherwise})$$

$\min_{s_N(i_1,i_2)}$

• Return i_1 if ilt_s_N (i_1, i_2) is 1, return i_2 otherwise.

```
\begin{array}{lcl} \mathrm{imin\_s}_N(i_1,i_2) &=& i_1 & (\mathrm{if} \ \mathrm{ilt\_s}_N(i_1,i_2) = 1) \\ \mathrm{imin\_s}_N(i_1,i_2) &=& i_2 & (\mathrm{otherwise}) \end{array}
```

$\max_{\mathbf{u}} \mathbf{u}_{N}(i_1, i_2)$

• Return i_1 if $igt_u_N(i_1, i_2)$ is 1, return i_2 otherwise.

$$\begin{array}{lcl} \mathrm{imax_u}_N(i_1,i_2) &=& i_1 & (\mathrm{if} \ \mathrm{igt_u}_N(i_1,i_2) = 1) \\ \mathrm{imax_u}_N(i_1,i_2) &=& i_2 & (\mathrm{otherwise}) \end{array}$$

$\max_{s_N(i_1, i_2)}$

• Return i_1 if $igt_s_N(i_1, i_2)$ is 1, return i_2 otherwise.

$$\begin{array}{lcl} \operatorname{imax_s}_N(i_1,i_2) & = & i_1 & (\operatorname{if} \operatorname{igt_s}_N(i_1,i_2) = 1) \\ \operatorname{imax_s}_N(i_1,i_2) & = & i_2 & (\operatorname{otherwise}) \end{array}$$

$iaddsat_u_N(i_1, i_2)$

- Let i be the result of adding i_1 and i_2 .
- Return $\operatorname{sat}^{\mathsf{u}}_{N}(i)$.

$$iaddsat_u_N(i_1, i_2) = sat^u_N(i_1 + i_2)$$

$iaddsat_s_N(i_1, i_2)$

- Let j_1 be the signed interpretation of i_1
- Let j_2 be the signed interpretation of i_2
- Let j be the result of adding j_1 and j_2 .
- Return $\operatorname{sat}^{\mathsf{s}}_{N}(j)$.

$$iaddsat_s_N(i_1, i_2) = sat_N^s(signed_N(i_1) + signed_N(i_2))$$

isubsat_ $\mathbf{u}_N(i_1, i_2)$

- Let i be the result of subtracting i_2 from i_1 .
- Return $\operatorname{sat}^{\mathsf{u}}_{N}(i)$.

$$isubsat_u_N(i_1, i_2) = sat^u_N(i_1 - i_2)$$

isubsat_s_N (i_1, i_2)

- Let j_1 be the signed interpretation of i_1
- $\bullet \ \ \mbox{Let} \ j_2$ be the signed interpretation of i_2
- Let j be the result of subtracting j_2 from j_1 .
- Return $\operatorname{sat}^{\mathsf{s}}_{N}(j)$.

```
isubsat_s_N(i_1, i_2) = sat_N^s(signed_N(i_1) - signed_N(i_2))
```

 $iavgr_u_N(i_1, i_2)$

- Let j be the result of adding i_1 , i_2 , and 1.
- Return the result of dividing j by 2, truncated toward zero.

$$iavgr_u_N(i_1, i_2) = trunc((i_1 + i_2 + 1)/2)$$

 $iq15mulrsat_s_N(i_1, i_2)$

• Return the result of sat^s_N(ishr_s_N($i_1 \cdot i_2 + 2^{14}, 15$)).

```
iq15mulrsat_s_N(i_1, i_2) = sat_N^s(ishr_s_N(i_1 \cdot i_2 + 2^{14}, 15))
```

4.3.3 Floating-Point Operations

Floating-point arithmetic follows the IEEE 754-2019²⁴ standard, with the following qualifications:

- All operators use round-to-nearest ties-to-even, except where otherwise specified. Non-default directed rounding attributes are not supported.
- Following the recommendation that operators propagate *NaN* payloads from their operands is permitted but not required.
- All operators use "non-stop" mode, and floating-point exceptions are not otherwise observable. In particular, neither alternate floating-point exception handling attributes nor operators on status flags are supported. There is no observable difference between quiet and signalling NaNs.

Note: Some of these limitations may be lifted in future versions of WebAssembly.

Rounding

Rounding always is round-to-nearest ties-to-even, in correspondence with IEEE 754-2019²⁵ (Section 4.3.1).

An exact floating-point number is a rational number that is exactly representable as a floating-point number of given bit width N.

A *limit* number for a given floating-point bit width N is a positive or negative number whose magnitude is the smallest power of 2 that is not exactly representable as a floating-point number of width N (that magnitude is 2^{128} for N=32 and 2^{1024} for N=64).

A candidate number is either an exact floating-point number or a positive or negative limit number for the given bit width N.

A candidate pair is a pair z_1, z_2 of candidate numbers, such that no candidate number exists that lies between the two.

A real number r is converted to a floating-point value of bit width N as follows:

- If r is 0, then return +0.
- Else if r is an exact floating-point number, then return r.
- Else if r greater than or equal to the positive limit, then return $+\infty$.
- Else if r is less than or equal to the negative limit, then return $-\infty$.
- Else if z_1 and z_2 are a candidate pair such that $z_1 < r < z_2$, then:

²⁴ https://ieeexplore.ieee.org/document/8766229

²⁵ https://ieeexplore.ieee.org/document/8766229

```
- If |r - z_1| < |r - z_2|, then let z be z_1.
             - Else if |r - z_1| > |r - z_2|, then let z be z_2.
             - Else if |r-z_1| = |r-z_2| and the significand of z_1 is even, then let z be z_1.
             - Else, let z be z_2.
     • If z is 0, then:
             - If r < 0, then return -0.
             - Else, return +0.
     • Else if z is a limit number, then:
             - If r < 0, then return -\infty.
             - Else, return +\infty.
     • Else, return z.
          float_N(0)
                                                    +0
          float_N(r)
                                                                                         (if r \in \text{exact}_N)
                                              = r
          float_N(r)
                                              = +\infty
                                                                                         (if r \geq + \text{limit}_N)
          float_N(r)
                                              = -\infty
                                                                                         (if r \leq -limit_N)
                                             = \operatorname{closest}_N(r, z_1, z_2)
          float_N(r)
                                                                                         (if z_1 < r < z_2 \land (z_1, z_2) \in \text{candidatepair}_N)
                                              = \operatorname{rectify}_{N}(r, z_1)
                                                                                         (if |r - z_1| < |r - z_2|)
          \operatorname{closest}_N(r, z_1, z_2)
          \operatorname{closest}_N(r, z_1, z_2) = \operatorname{rectify}_N(r, z_2)
                                                                                         (if |r - z_1| > |r - z_2|)
          \begin{array}{lll} \operatorname{closest}_N(r,z_1,z_2) & = & \operatorname{rectify}_N(r,z_1) \\ \operatorname{closest}_N(r,z_1,z_2) & = & \operatorname{rectify}_N(r,z_2) \end{array}
                                                                                         (if |r - z_1| = |r - z_2| \wedge even_N(z_1))
                                                                                        (\text{if } |r-z_1| = |r-z_2| \wedge \text{even}_N(z_2))
          \operatorname{rectify}_{N}(r, \pm \operatorname{limit}_{N}) = \pm \infty
          \operatorname{rectify}_{N}(r,0)
                                              = +0
                                                                  (r \geq 0)
          \operatorname{rectify}_{N}(r,0)
                                              = -0
                                                                  (r < 0)
         \operatorname{rectify}_{N}(r,z)
where:
                                               = fN \cap \mathbb{Q}
= 2^{2^{\exp\operatorname{on}(N)-1}}
 \operatorname{exact}_N
 \lim_{N}
                                               = \operatorname{exact}_N \cup \{+\operatorname{limit}_N, -\operatorname{limit}_N\}
 candidate_N
                                               = \{(z_1, z_2) \in \operatorname{candidate}_N^2 \mid z_1 < z_2 \land \forall z \in \operatorname{candidate}_N, z \le z_1 \lor z \ge z_2\}
 {\rm candidate pair}_N
```

NaN Propagation

 $even_N(\pm limit_N)$

 $\operatorname{even}_N((d+m\cdot 2^{-M})\cdot 2^e) \iff m \bmod 2 = 0$

⇔ true

When the result of a floating-point operator other than fneg, fabs, or fcopysign is a *NaN*, then its sign is non-deterministic and the *payload* is computed as follows:

- If the payload of all NaN inputs to the operator is *canonical* (including the case that there are no NaN inputs), then the payload of the output is canonical as well.
- Otherwise the payload is picked non-deterministically among all *arithmetic NaNs*; that is, its most significant bit is 1 and all others are unspecified.

This non-deterministic result is expressed by the following auxiliary function producing a set of allowed outputs from a set of inputs:

```
\operatorname{nans}_N\{z^*\} = \{+\operatorname{nan}(n), -\operatorname{nan}(n) \mid n = \operatorname{canon}_N\} (if \forall \operatorname{nan}(n) \in z^*, n = \operatorname{canon}_N) \operatorname{nans}_N\{z^*\} = \{+\operatorname{nan}(n), -\operatorname{nan}(n) \mid n \ge \operatorname{canon}_N\} (otherwise)
```

$fadd_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return an element of $nans_N\{z_1, z_2\}$.
- Else if both z_1 and z_2 are infinities of opposite signs, then return an element of $nans_N\{\}$.
- ullet Else if both z_1 and z_2 are infinities of equal sign, then return that infinity.
- Else if either z_1 or z_2 is an infinity, then return that infinity.
- Else if both z_1 and z_2 are zeroes of opposite sign, then return positive zero.
- Else if both z_1 and z_2 are zeroes of equal sign, then return that zero.
- Else if either z_1 or z_2 is a zero, then return the other operand.
- Else if both z_1 and z_2 are values with the same magnitude but opposite signs, then return positive zero.
- Else return the result of adding z_1 and z_2 , rounded to the nearest representable value.

```
fadd_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
fadd_N(z_1, \pm nan(n)) = nans_N\{\pm nan(n), z_1\}
fadd_N(\pm \infty, \mp \infty) = nans_N\{\}
fadd_N(\pm \infty, \pm \infty) = \pm \infty
                        = \pm \infty
fadd_N(z_1,\pm\infty)
fadd_N(\pm\infty,z_2)
                          = \pm \infty
fadd_N(\pm 0, \mp 0)
                          = +0
fadd_N(\pm 0, \pm 0)
                          = \pm 0
fadd_N(z_1,\pm 0)
                          = z_1
fadd_N(\pm 0, z_2)
fadd_N(\pm q, \mp q)
                        = +0
                          = \operatorname{float}_N(z_1 + z_2)
fadd_N(z_1,z_2)
```

$fsub_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return an element of $nans_N\{z_1, z_2\}$.
- Else if both z_1 and z_2 are infinities of equal signs, then return an element of $nans_N\{\}$.
- Else if both z_1 and z_2 are infinities of opposite sign, then return z_1 .
- Else if z_1 is an infinity, then return that infinity.
- Else if z_2 is an infinity, then return that infinity negated.
- Else if both z_1 and z_2 are zeroes of equal sign, then return positive zero.
- Else if both z_1 and z_2 are zeroes of opposite sign, then return z_1 .
- Else if z_2 is a zero, then return z_1 .
- Else if z_1 is a zero, then return z_2 negated.
- Else if both z_1 and z_2 are the same value, then return positive zero.
- Else return the result of subtracting z_2 from z_1 , rounded to the nearest representable value.

```
fsub_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
                                    \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_1\}
fsub_N(z_1, \pm nan(n)) =
fsub_N(\pm\infty,\pm\infty)
                              = \operatorname{nans}_{N}\{\}
fsub_N(\pm\infty,\mp\infty)
                              = \pm \infty
fsub_N(z_1,\pm\infty)
                              = \mp \infty
fsub_N(\pm\infty,z_2)
                              = \pm \infty
fsub_N(\pm 0, \pm 0)
                              = +0
fsub_N(\pm 0, \mp 0)
                              = \pm 0
fsub_N(z_1,\pm 0)
                              = z_1
fsub_N(\pm 0, \pm q_2)
                              = \mp q_2
fsub_N(\pm q, \pm q)
                              = +0
\mathrm{fsub}_N(z_1,z_2)
                              = \operatorname{float}_N(z_1 - z_2)
```

Note: Up to the non-determinism regarding NaNs, it always holds that $fsub_N(z_1, z_2) = fadd_N(z_1, fneg_N(z_2))$.

$\operatorname{fmul}_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return an element of $nans_N\{z_1, z_2\}$.
- Else if one of z_1 and z_2 is a zero and the other an infinity, then return an element of $nans_N\{\}$.
- Else if both z_1 and z_2 are infinities of equal sign, then return positive infinity.
- Else if both z_1 and z_2 are infinities of opposite sign, then return negative infinity.
- Else if either z_1 or z_2 is an infinity and the other a value with equal sign, then return positive infinity.
- Else if either z_1 or z_2 is an infinity and the other a value with opposite sign, then return negative infinity.
- Else if both z_1 and z_2 are zeroes of equal sign, then return positive zero.
- Else if both z_1 and z_2 are zeroes of opposite sign, then return negative zero.
- Else return the result of multiplying z_1 and z_2 , rounded to the nearest representable value.

```
\operatorname{fmul}_N(\pm \operatorname{nan}(n), z_2) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_2\}
\operatorname{fmul}_N(z_1, \pm \operatorname{nan}(n)) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_1\}
\text{fmul}_N(\pm\infty,\pm0)
                                         = \operatorname{nans}_{N}\{\}
\text{fmul}_N(\pm\infty,\mp0)
                                         = \operatorname{nans}_{N}\{\}
\text{fmul}_N(\pm 0, \pm \infty)
                                          = \operatorname{nans}_{N}\{\}
\operatorname{fmul}_N(\pm 0, \mp \infty)
                                          = \operatorname{nans}_{N}\{\}
\text{fmul}_N(\pm\infty,\pm\infty)
                                          = +\infty
\text{fmul}_N(\pm\infty,\mp\infty)
                                          = -\infty
\text{fmul}_N(\pm q_1,\pm\infty)
                                          = +\infty
\operatorname{fmul}_N(\pm q_1, \mp \infty)
\text{fmul}_N(\pm\infty,\pm q_2)
                                          = +\infty
\operatorname{fmul}_N(\pm\infty,\mp q_2)
                                          = -\infty
\text{fmul}_N(\pm 0, \pm 0)
                                          = +0
\text{fmul}_N(\pm 0, \mp 0)
                                         = -0
                                          = \operatorname{float}_N(z_1 \cdot z_2)
\mathrm{fmul}_N(z_1,z_2)
```

$fdiv_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return an element of $nans_N\{z_1, z_2\}$.
- Else if both z_1 and z_2 are infinities, then return an element of $nans_N\{\}$.
- Else if both z_1 and z_2 are zeroes, then return an element of $nans_N\{z_1, z_2\}$.
- Else if z_1 is an infinity and z_2 a value with equal sign, then return positive infinity.
- Else if z_1 is an infinity and z_2 a value with opposite sign, then return negative infinity.
- Else if z_2 is an infinity and z_1 a value with equal sign, then return positive zero.
- Else if z_2 is an infinity and z_1 a value with opposite sign, then return negative zero.
- Else if z_1 is a zero and z_2 a value with equal sign, then return positive zero.
- Else if z_1 is a zero and z_2 a value with opposite sign, then return negative zero.
- Else if z_2 is a zero and z_1 a value with equal sign, then return positive infinity.
- Else if z_2 is a zero and z_1 a value with opposite sign, then return negative infinity.
- Else return the result of dividing z_1 by z_2 , rounded to the nearest representable value.

```
fdiv_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
fdiv_N(z_1, \pm nan(n)) = nans_N \{\pm nan(n), z_1\}
fdiv_N(\pm \infty, \pm \infty) = nans_N\{\}
fdiv_N(\pm\infty,\mp\infty)
                        = \operatorname{nans}_{N}\{\}
fdiv_N(\pm 0, \pm 0) = nans_N\{\}
fdiv_N(\pm 0, \mp 0)
                           = \operatorname{nans}_{N}\{\}
fdiv_N(\pm\infty,\pm q_2)
                           = +\infty
fdiv_N(\pm\infty,\mp q_2)
                           = -\infty
fdiv_N(\pm q_1, \pm \infty)
                           = +0
fdiv_N(\pm q_1, \mp \infty)
                                -0
fdiv_N(\pm 0, \pm q_2)
                           = +0
fdiv_N(\pm 0, \mp q_2)
                           = -0
fdiv_N(\pm q_1, \pm 0)
                          = +\infty
fdiv_N(\pm q_1, \mp 0)
                           = -\infty
fdiv_N(z_1, z_2)
                           = \operatorname{float}_N(z_1/z_2)
```

$fmin_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return an element of $nans_N\{z_1, z_2\}$.
- Else if either z_1 or z_2 is a negative infinity, then return negative infinity.
- Else if either z_1 or z_2 is a positive infinity, then return the other value.
- Else if both z_1 and z_2 are zeroes of opposite signs, then return negative zero.
- Else return the smaller value of z_1 and z_2 .

```
fmin_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
fmin_N(z_1, \pm nan(n)) = nans_N\{\pm nan(n), z_1\}
fmin_N(+\infty, z_2)
                         = z_2
fmin_N(-\infty, z_2)
                             -\infty
                        = z_1
fmin_N(z_1, +\infty)
fmin_N(z_1, -\infty)
                        = -\infty
fmin_N(\pm 0, \mp 0)
                        = -0
fmin_N(z_1,z_2)
                         = z_1
                                                        (if z_1 \le z_2)
fmin_N(z_1, z_2)
                         = z_2
                                                        (if z_2 \leq z_1)
```

$fmax_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return an element of $nans_N\{z_1, z_2\}$.
- Else if either z_1 or z_2 is a positive infinity, then return positive infinity.
- Else if either z_1 or z_2 is a negative infinity, then return the other value.
- ullet Else if both z_1 and z_2 are zeroes of opposite signs, then return positive zero.
- Else return the larger value of z_1 and z_2 .

```
fmax_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
\operatorname{fmax}_N(z_1, \pm \operatorname{nan}(n)) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_1\}
\max_N(+\infty, z_2)
                              = +\infty
                             = z_2
\text{fmax}_N(-\infty, z_2)
                             = +\infty
\max_N(z_1,+\infty)
\max_N(z_1,-\infty)
                               = z_1
fmax_N(\pm 0, \mp 0)
                             = +0
\operatorname{fmax}_N(z_1,z_2)
                              = z_1
                                                                      (if z_1 \geq z_2)
\operatorname{fmax}_N(z_1, z_2)
                                                                      (if z_2 \ge z_1)
```

$fcopysign_N(z_1, z_2)$

- If z_1 and z_2 have the same sign, then return z_1 .
- Else return z_1 with negated sign.

```
fcopysign<sub>N</sub>(\pm p_1, \pm p_2) = \pm p_1
fcopysign<sub>N</sub>(\pm p_1, \mp p_2) = \mp p_1
```

$fabs_N(z)$

- If z is a NaN, then return z with positive sign.
- Else if z is an infinity, then return positive infinity.
- Else if z is a zero, then return positive zero.
- Else if z is a positive value, then z.
- Else return z negated.

```
\begin{array}{lll} \operatorname{fabs}_N(\pm \operatorname{nan}(n)) & = & +\operatorname{nan}(n) \\ \operatorname{fabs}_N(\pm \infty) & = & +\infty \\ \operatorname{fabs}_N(\pm 0) & = & +0 \\ \operatorname{fabs}_N(\pm q) & = & +q \end{array}
```

$fneg_N(z)$

- If z is a NaN, then return z with negated sign.
- ullet Else if z is an infinity, then return that infinity negated.
- Else if z is a zero, then return that zero negated.
- Else return z negated.

```
\begin{array}{lll} \operatorname{fneg}_N(\pm \operatorname{nan}(n)) & = & \mp \operatorname{nan}(n) \\ \operatorname{fneg}_N(\pm \infty) & = & \mp \infty \\ \operatorname{fneg}_N(\pm 0) & = & \mp 0 \\ \operatorname{fneg}_N(\pm q) & = & \mp q \end{array}
```

$fsqrt_N(z)$

- If z is a NaN, then return an element of $nans_N\{z\}$.
- Else if z is negative infinity, then return an element of $nans_N\{\}$.
- ullet Else if z is positive infinity, then return positive infinity.
- Else if z is a zero, then return that zero.
- Else if z has a negative sign, then return an element of $nans_N$ {}.
- Else return the square root of z.

```
\begin{array}{lll} \operatorname{fsqrt}_N(\pm \operatorname{nan}(n)) & = & \operatorname{nans}_N\{\pm \operatorname{nan}(n)\} \\ \operatorname{fsqrt}_N(-\infty) & = & \operatorname{nans}_N\{\} \\ \operatorname{fsqrt}_N(\pm \infty) & = & +\infty \\ \operatorname{fsqrt}_N(\pm 0) & = & \pm 0 \\ \operatorname{fsqrt}_N(-q) & = & \operatorname{nans}_N\{\} \\ \operatorname{fsqrt}_N(+q) & = & \operatorname{float}_N\left(\sqrt{q}\right) \end{array}
```

$fceil_N(z)$

- If z is a NaN, then return an element of $nans_N\{z\}$.
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is smaller than 0 but greater than -1, then return negative zero.
- Else return the smallest integral value that is not smaller than z.

```
\begin{array}{lll} \operatorname{fceil}_N(\pm \operatorname{nan}(n)) & = & \operatorname{nans}_N\{\pm \operatorname{nan}(n)\} \\ \operatorname{fceil}_N(\pm \infty) & = & \pm \infty \\ \operatorname{fceil}_N(\pm 0) & = & \pm 0 \\ \operatorname{fceil}_N(-q) & = & -0 & (\text{if } -1 < -q < 0) \\ \operatorname{fceil}_N(\pm q) & = & \operatorname{float}_N(i) & (\text{if } \pm q \leq i < \pm q + 1) \end{array}
```

$ffloor_N(z)$

- If z is a NaN, then return an element of $nans_N\{z\}$.
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is greater than 0 but smaller than 1, then return positive zero.
- Else return the largest integral value that is not larger than z.

```
\begin{array}{lll} \mathrm{ffloor}_N(\pm \mathrm{nan}(n)) &=& \mathrm{nans}_N\{\pm \mathrm{nan}(n)\} \\ \mathrm{ffloor}_N(\pm \infty) &=& \pm \infty \\ \mathrm{ffloor}_N(\pm 0) &=& \pm 0 \\ \mathrm{ffloor}_N(+q) &=& +0 \\ \mathrm{ffloor}_N(\pm q) &=& \mathrm{float}_N(i) & (\mathrm{if}\ 0 < +q < 1) \\ \mathrm{ffloor}_N(\pm q) &=& \mathrm{float}_N(i) & (\mathrm{if}\ \pm q - 1 < i \leq \pm q) \end{array}
```

$ftrunc_N(z)$

- If z is a NaN, then return an element of $nans_N\{z\}$.
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is greater than 0 but smaller than 1, then return positive zero.
- Else if z is smaller than 0 but greater than -1, then return negative zero.
- Else return the integral value with the same sign as z and the largest magnitude that is not larger than the magnitude of z.

```
\begin{array}{lll} {\rm ftrunc}_N(\pm {\rm nan}(n)) & = & {\rm nans}_N\{\pm {\rm nan}(n)\} \\ {\rm ftrunc}_N(\pm \infty) & = & \pm \infty \\ {\rm ftrunc}_N(\pm 0) & = & \pm 0 \\ {\rm ftrunc}_N(+q) & = & +0 & ({\rm if} \ 0 < +q < 1) \\ {\rm ftrunc}_N(-q) & = & -0 & ({\rm if} \ -1 < -q < 0) \\ {\rm ftrunc}_N(\pm q) & = & {\rm float}_N(\pm i) & ({\rm if} \ +q - 1 < i \le +q) \end{array}
```

$fnearest_N(z)$

- If z is a NaN, then return an element of $nans_N\{z\}$.
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is greater than 0 but smaller than or equal to 0.5, then return positive zero.
- Else if z is smaller than 0 but greater than or equal to -0.5, then return negative zero.
- Else return the integral value that is nearest to z; if two values are equally near, return the even one.

```
\begin{array}{lll} \operatorname{fnearest}_N(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N\{\pm \operatorname{nan}(n)\} \\ \operatorname{fnearest}_N(\pm \infty) &=& \pm \infty \\ \operatorname{fnearest}_N(\pm 0) &=& \pm 0 \\ \operatorname{fnearest}_N(+q) &=& +0 & (\text{if } 0 < +q \leq 0.5) \\ \operatorname{fnearest}_N(-q) &=& -0 & (\text{if } -0.5 \leq -q < 0) \\ \operatorname{fnearest}_N(\pm q) &=& \operatorname{float}_N(\pm i) & (\text{if } |i-q| < 0.5) \\ \operatorname{fnearest}_N(\pm q) &=& \operatorname{float}_N(\pm i) & (\text{if } |i-q| = 0.5 \wedge i \text{ even}) \\ \end{array}
```

$feq_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return 0.
- Else if both z_1 and z_2 are zeroes, then return 1.
- Else if both z_1 and z_2 are the same value, then return 1.
- Else return 0.

```
\begin{array}{lcl} \mathrm{feq}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ \mathrm{feq}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{feq}_N(\pm 0, \mp 0) & = & 1 \\ \mathrm{feq}_N(z_1, z_2) & = & \mathrm{bool}(z_1 = z_2) \end{array}
```

$\operatorname{fne}_N(z_1,z_2)$

- If either z_1 or z_2 is a NaN, then return 1.
- Else if both z_1 and z_2 are zeroes, then return 0.
- Else if both z_1 and z_2 are the same value, then return 0.
- Else return 1.

```
\begin{array}{lclcrcl} & & & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ &
```

$\operatorname{flt}_N(z_1,z_2)$

- If either z_1 or z_2 is a NaN, then return 0.
- Else if z_1 and z_2 are the same value, then return 0.
- Else if z_1 is positive infinity, then return 0.
- Else if z_1 is negative infinity, then return 1.
- Else if z_2 is positive infinity, then return 1.
- Else if z_2 is negative infinity, then return 0.
- Else if both z_1 and z_2 are zeroes, then return 0.
- Else if z_1 is smaller than z_2 , then return 1.
- Else return 0.

```
\begin{array}{lll} \mathrm{flt}_N(\pm \mathrm{nan}(n),z_2) & = & 0 \\ \mathrm{flt}_N(z_1,\pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{flt}_N(z,z) & = & 0 \\ \mathrm{flt}_N(+\infty,z_2) & = & 0 \\ \mathrm{flt}_N(-\infty,z_2) & = & 1 \\ \mathrm{flt}_N(z_1,+\infty) & = & 1 \\ \mathrm{flt}_N(z_1,-\infty) & = & 0 \\ \mathrm{flt}_N(\pm 0,\mp 0) & = & 0 \\ \mathrm{flt}_N(z_1,z_2) & = & \mathrm{bool}(z_1 < z_2) \end{array}
```

$fgt_N(z_1, z_2)$

- If either z_1 or z_2 is a NaN, then return 0.
- Else if z_1 and z_2 are the same value, then return 0.
- Else if z_1 is positive infinity, then return 1.
- Else if z_1 is negative infinity, then return 0.
- Else if z_2 is positive infinity, then return 0.
- Else if z_2 is negative infinity, then return 1.
- Else if both z_1 and z_2 are zeroes, then return 0.
- Else if z_1 is larger than z_2 , then return 1.
- Else return 0.

```
\begin{array}{llll} \mathrm{fgt}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ \mathrm{fgt}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{fgt}_N(z, z) & = & 0 \\ \mathrm{fgt}_N(+\infty, z_2) & = & 1 \\ \mathrm{fgt}_N(-\infty, z_2) & = & 0 \\ \mathrm{fgt}_N(z_1, +\infty) & = & 0 \\ \mathrm{fgt}_N(z_1, -\infty) & = & 1 \\ \mathrm{fgt}_N(\pm 0, \mp 0) & = & 0 \\ \mathrm{fgt}_N(z_1, z_2) & = & \mathrm{bool}(z_1 > z_2) \end{array}
```

$fle_N(z_1,z_2)$

- If either z_1 or z_2 is a NaN, then return 0.
- Else if z_1 and z_2 are the same value, then return 1.
- Else if z_1 is positive infinity, then return 0.
- Else if z_1 is negative infinity, then return 1.
- Else if z_2 is positive infinity, then return 1.
- Else if z_2 is negative infinity, then return 0.
- Else if both z_1 and z_2 are zeroes, then return 1.
- Else if z_1 is smaller than or equal to z_2 , then return 1.
- Else return 0.

```
\begin{array}{lll} \mathrm{fle}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ \mathrm{fle}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{fle}_N(z, z) & = & 1 \\ \mathrm{fle}_N(+\infty, z_2) & = & 0 \\ \mathrm{fle}_N(-\infty, z_2) & = & 1 \\ \mathrm{fle}_N(z_1, +\infty) & = & 1 \\ \mathrm{fle}_N(z_1, -\infty) & = & 0 \\ \mathrm{fle}_N(\pm 0, \mp 0) & = & 1 \\ \mathrm{fle}_N(z_1, z_2) & = & \mathrm{bool}(z_1 \leq z_2) \end{array}
```

$fge_N(z_1,z_2)$

- If either z_1 or z_2 is a NaN, then return 0.
- Else if z_1 and z_2 are the same value, then return 1.
- Else if z_1 is positive infinity, then return 1.
- $\bullet \;$ Else if z_1 is negative infinity, then return 0.
- Else if z_2 is positive infinity, then return 0.
- $\bullet\,$ Else if z_2 is negative infinity, then return 1.
- Else if both z_1 and z_2 are zeroes, then return 1.
- Else if z_1 is smaller than or equal to z_2 , then return 1.
- Else return 0.

```
\begin{array}{llll} & \mathrm{fge}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ & \mathrm{fge}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ & \mathrm{fge}_N(z, z) & = & 1 \\ & \mathrm{fge}_N(+\infty, z_2) & = & 1 \\ & \mathrm{fge}_N(-\infty, z_2) & = & 0 \\ & \mathrm{fge}_N(z_1, +\infty) & = & 0 \\ & \mathrm{fge}_N(z_1, -\infty) & = & 1 \\ & \mathrm{fge}_N(\pm 0, \mp 0) & = & 1 \\ & \mathrm{fge}_N(z_1, z_2) & = & \mathrm{bool}(z_1 \geq z_2) \end{array}
```

$fpmin_N(z_1, z_2)$

- If z_2 is less than z_1 then return z_2 .
- Else return z_1 .

$$\begin{array}{lcl} \mathrm{fpmin}_N(z_1,z_2) & = & z_2 & (\mathrm{if} \ \mathrm{flt}_N(z_2,z_1) = 1) \\ \mathrm{fpmin}_N(z_1,z_2) & = & z_1 & (\mathrm{otherwise}) \end{array}$$

$fpmax_N(z_1, z_2)$

- If z_1 is less than z_2 then return z_2 .
- Else return z_1 .

$$\begin{array}{lcl} \mathrm{fpmax}_N(z_1,z_2) & = & z_2 & (\mathrm{if} \ \mathrm{flt}_N(z_1,z_2) = 1) \\ \mathrm{fpmax}_N(z_1,z_2) & = & z_1 & (\mathrm{otherwise}) \end{array}$$

4.3.4 Conversions

$\operatorname{extend}^{\mathsf{u}}_{M,N}(i)$

• Return i.

$$\operatorname{extend}^{\mathsf{u}}_{M,N}(i) = i$$

Note: In the abstract syntax, unsigned extension just reinterprets the same value.

$\operatorname{extend}^{\mathsf{s}}_{M,N}(i)$

- Let j be the *signed interpretation* of i of size M.
- Return the two's complement of j relative to size N.

$$\operatorname{extend}^{\mathsf{s}}_{M,N}(i) = \operatorname{signed}_{N}^{-1}(\operatorname{signed}_{M}(i))$$

$\operatorname{wrap}_{M,N}(i)$

• Return $i \mod 2^N$.

$$\operatorname{wrap}_{M,N}(i) = i \operatorname{mod} 2^N$$

$\operatorname{trunc}^{\mathsf{u}}_{M,N}(z)$

- If z is a NaN, then the result is undefined.
- ullet Else if z is an infinity, then the result is undefined.
- Else if z is a number and trunc(z) is a value within range of the target type, then return that value.
- Else the result is undefined.

```
\begin{array}{lll} \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm \operatorname{nan}(n)) & = & \{\} \\ \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm \infty) & = & \{\} \\ \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm q) & = & \operatorname{trunc}(\pm q) & (\operatorname{if} -1 < \operatorname{trunc}(\pm q) < 2^N) \\ \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm q) & = & \{\} & (\operatorname{otherwise}) \end{array}
```

Note: This operator is *partial*. It is not defined for NaNs, infinities, or values for which the result is out of range.

$\operatorname{trunc}^{\mathsf{s}}_{M,N}(z)$

- If z is a NaN, then the result is undefined.
- Else if z is an infinity, then the result is undefined.
- If z is a number and trunc(z) is a value within range of the target type, then return that value.
- Else the result is undefined.

```
\begin{array}{lll} {\rm trunc}^{\rm s}{}_{M,N}(\pm {\rm nan}(n)) & = & \{ \} \\ {\rm trunc}^{\rm s}{}_{M,N}(\pm \infty) & = & \{ \} \\ {\rm trunc}^{\rm s}{}_{M,N}(\pm q) & = & {\rm trunc}(\pm q) & ({\rm if} -2^{N-1} - 1 < {\rm trunc}(\pm q) < 2^{N-1}) \\ {\rm trunc}^{\rm s}{}_{M,N}(\pm q) & = & \{ \} & ({\rm otherwise}) \end{array}
```

Note: This operator is *partial*. It is not defined for NaNs, infinities, or values for which the result is out of range.

trunc_sat_ $\mathbf{u}_{M,N}(z)$

- If z is a NaN, then return 0.
- ullet Else if z is negative infinity, then return 0.
- Else if z is positive infinity, then return $2^N 1$.
- Else, return $\operatorname{sat}^{\mathsf{u}}_{N}(\operatorname{trunc}(z))$.

```
\begin{array}{llll} \operatorname{trunc\_sat\_u}_{M,N}(\pm \operatorname{nan}(n)) & = & 0 \\ \operatorname{trunc\_sat\_u}_{M,N}(-\infty) & = & 0 \\ \operatorname{trunc\_sat\_u}_{M,N}(+\infty) & = & 2^N - 1 \\ \operatorname{trunc\_sat\_u}_{M,N}(z) & = & \operatorname{sat^u}_{N}(\operatorname{trunc}(z)) \end{array}
```

trunc_sat_s $_{M,N}(z)$

- If z is a NaN, then return 0.
- Else if z is negative infinity, then return -2^{N-1} .
- Else if z is positive infinity, then return $2^{N-1} 1$.
- Else, return $\operatorname{sat}^{\mathsf{s}}_{N}(\operatorname{trunc}(z))$.

```
\begin{array}{llll} \operatorname{trunc\_sat\_s}_{M,N}(\pm \operatorname{nan}(n)) & = & 0 \\ \operatorname{trunc\_sat\_s}_{M,N}(-\infty) & = & -2^{N-1} \\ \operatorname{trunc\_sat\_s}_{M,N}(+\infty) & = & 2^{N-1} - 1 \\ \operatorname{trunc\_sat\_s}_{M,N}(z) & = & \operatorname{sat^s}_{N}(\operatorname{trunc}(z)) \end{array}
```

$promote_{M,N}(z)$

- If z is a canonical NaN, then return an element of $nans_N\{\}$ (i.e., a canonical NaN of size N).
- Else if z is a NaN, then return an element of $nans_N\{\pm nan(1)\}\$ (i.e., any arithmetic NaN of size N).
- Else, return z.

```
\begin{array}{llll} \operatorname{promote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N \{\} & & (\text{if } n = \operatorname{canon}_N) \\ \operatorname{promote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N \{+\operatorname{nan}(1)\} & & (\text{otherwise}) \\ \operatorname{promote}_{M,N}(z) &=& z & & \end{array}
```

$demote_{M,N}(z)$

- If z is a canonical NaN, then return an element of $nans_N\{\}$ (i.e., a canonical NaN of size N).
- Else if z is a NaN, then return an element of $nans_N\{\pm nan(1)\}\$ (i.e., any NaN of size N).
- Else if z is an infinity, then return that infinity.
- Else if z is a zero, then return that zero.
- Else, return float $_N(z)$.

```
\begin{array}{lll} \operatorname{demote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N\{\} & \text{ (if } n = \operatorname{canon}_N) \\ \operatorname{demote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N\{+\operatorname{nan}(1)\} & \text{ (otherwise)} \\ \operatorname{demote}_{M,N}(\pm \infty) &=& \pm \infty \\ \operatorname{demote}_{M,N}(\pm 0) &=& \pm 0 \\ \operatorname{demote}_{M,N}(\pm q) &=& \operatorname{float}_N(\pm q) \end{array}
```

$\operatorname{convert}^{\mathsf{u}}_{M,N}(i)$

• Return $float_N(i)$.

```
\operatorname{convert}^{\mathsf{u}}_{M,N}(i) = \operatorname{float}_{N}(i)
```

 $\operatorname{convert}^{\mathsf{s}}_{M,N}(i)$

- Let j be the signed interpretation of i.
- Return float $_N(j)$.

$$convert^{s}_{M,N}(i) = float_{N}(signed_{M}(i))$$

reinterpret $_{t_1,t_2}(c)$

- Let d^* be the bit sequence $\operatorname{bits}_{t_1}(c)$.
- Return the constant c' for which $\operatorname{bits}_{t_2}(c') = d^*$.

 $narrow^{s}_{M,N}(i)$

- Let j be the *signed interpretation* of i of size M.
- Return $\operatorname{sat}^{\mathsf{s}}_{N}(j)$.

$$\operatorname{narrow}^{s}_{M,N}(i) = \operatorname{sat}^{s}_{N}(\operatorname{signed}_{M}(i))$$

 $\operatorname{narrow}^{\mathsf{u}}_{M,N}(i)$

- Let j be the signed interpretation of i of size M.
- Return $\operatorname{sat}^{\mathsf{u}}_{N}(j)$.

$$\operatorname{narrow}^{\mathsf{u}}_{M,N}(i) = \operatorname{sat}^{\mathsf{u}}_{N}(\operatorname{signed}_{M}(i))$$

4.4 Instructions

WebAssembly computation is performed by executing individual *instructions*.

4.4.1 Numeric Instructions

Numeric instructions are defined in terms of the generic *numeric operators*. The mapping of numeric instructions to their underlying operators is expressed by the following definition:

$$\begin{array}{rcl} op_{\mathsf{i}N}(n_1,\ldots,n_k) & = & \mathsf{i}op_N(n_1,\ldots,n_k) \\ op_{\mathsf{f}N}(z_1,\ldots,z_k) & = & \mathsf{f}op_N(z_1,\ldots,z_k) \end{array}$$

And for *conversion operators*:

$$cvtop_{t_1,t_2}^{sx^?}(c) = cvtop_{|t_1|,|t_2|}^{sx^?}(c)$$

Where the underlying operators are partial, the corresponding instruction will *trap* when the result is not defined. Where the underlying operators are non-deterministic, because they may return one of multiple possible *NaN* values, so are the corresponding instructions.

Note: For example, the result of instruction i32.add applied to operands i_1, i_2 invokes $\operatorname{add}_{i32}(i_1, i_2)$, which maps to the generic $\operatorname{iadd}_{32}(i_1, i_2)$ via the above definition. Similarly, i64.trunc_f32_s applied to z invokes $\operatorname{trunc}_{f32,i64}^s(z)$, which maps to the generic $\operatorname{trunc}_{32,64}^s(z)$.

4.4. Instructions 95

$t.\mathsf{const}\ c$

1. Push the value t.const c to the stack.

Note: No formal reduction rule is required for this instruction, since const instructions already are values.

t.unop

- 1. Assert: due to *validation*, a value of *value type* t is on the top of the stack.
- 2. Pop the value t.const c_1 from the stack.
- 3. If $unop_t(c_1)$ is defined, then:
 - a. Let c be a possible result of computing $unop_t(c_1)$.
 - b. Push the value t.const c to the stack.
- 4. Else:
 - a. Trap.

```
 \begin{array}{cccc} (t.\mathsf{const}\ c_1)\ t.unop &\hookrightarrow & (t.\mathsf{const}\ c) & & (\text{if}\ c \in unop_t(c_1)) \\ (t.\mathsf{const}\ c_1)\ t.unop &\hookrightarrow & \text{trap} & & (\text{if}\ unop_t(c_1) = \{\}) \end{array}
```

t.binop

- 1. Assert: due to *validation*, two values of *value type t* are on the top of the stack.
- 2. Pop the value t.const c_2 from the stack.
- 3. Pop the value t.const c_1 from the stack.
- 4. If $binop_t(c_1, c_2)$ is defined, then:
 - a. Let c be a possible result of computing $binop_t(c_1, c_2)$.
 - b. Push the value t.const c to the stack.
- 5. Else:
 - a. Trap.

```
(t.\mathsf{const}\ c_1)\ (t.\mathsf{const}\ c_2)\ t.\mathit{binop}\ \hookrightarrow\ (t.\mathsf{const}\ c) \qquad (\mathsf{if}\ c\in \mathit{binop}_t(c_1,c_2)) \ (t.\mathsf{const}\ c_1)\ (t.\mathsf{const}\ c_2)\ t.\mathit{binop}\ \hookrightarrow\ \mathsf{trap} \qquad (\mathsf{if}\ \mathit{binop}_t(c_1,c_2)=\{\})
```

t.testop

- 1. Assert: due to *validation*, a value of *value type t* is on the top of the stack.
- 2. Pop the value t.const c_1 from the stack.
- 3. Let c be the result of computing $testop_t(c_1)$.
- 4. Push the value i32.const c to the stack.

```
(t.\mathsf{const}\ c_1)\ t.testop \hookrightarrow (\mathsf{i32.const}\ c) \quad (\mathsf{if}\ c = testop_t(c_1))
```

t.relop

- 1. Assert: due to *validation*, two values of *value type t* are on the top of the stack.
- 2. Pop the value t.const c_2 from the stack.
- 3. Pop the value t.const c_1 from the stack.
- 4. Let c be the result of computing $relop_t(c_1, c_2)$.
- 5. Push the value i32.const c to the stack.

$t_2.cvtop_t_1_sx^?$

- 1. Assert: due to *validation*, a value of *value type* t_1 is on the top of the stack.
- 2. Pop the value t_1 .const c_1 from the stack.
- 3. If $cvtop_{t_1,t_2}^{sx^?}(c_1)$ is defined:
 - a. Let c_2 be a possible result of computing $\operatorname{cvtop}_{t_1,t_2}^{sx^2}(c_1)$.
 - b. Push the value t_2 .const c_2 to the stack.
- 4. Else:
 - a. Trap.

4.4.2 Reference Instructions

$ref.null\ ht$

1. Push the value ref.null ht to the stack.

Note: No formal reduction rule is required for this instruction, since the ref.null instruction is already a *value*.

ref.func x

- 1. Let F be the current frame.
- 2. Assert: due to validation, F.module.funcaddrs[x] exists.
- 3. Let a be the function address F.module.funcaddrs[x].
- 4. Push the value ref a to the stack.

```
F; ref.func x \hookrightarrow F; ref a (if a = F.module.funcaddrs[x])
```

4.4. Instructions 97

ref.is_null

- 1. Assert: due to validation, a reference value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If val is ref.null ht, then:
 - a. Push the value i32.const 1 to the stack.
- 4. Else:
 - a. Push the value i32.const 0 to the stack.

```
val \text{ ref.is\_null} \hookrightarrow i32.\text{const } 1 \qquad \text{(if } val = \text{ref.null } ht\text{)} \\ val \text{ ref.is\_null} \hookrightarrow i32.\text{const } 0 \qquad \text{(otherwise)}
```

ref.as_non_null

- 1. Assert: due to validation, a reference value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If val is ref.null ht, then:
 - a. Trap.
- 4. Push the value *val* back to the stack.

```
val \text{ ref.as\_non\_null } \hookrightarrow \text{ trap } \text{ (if } val = \text{ref.null } ht)
val \text{ ref.as\_non\_null } \hookrightarrow val \text{ (otherwise)}
```

4.4.3 Vector Instructions

Most vector instructions are defined in terms of generic numeric operators applied lane-wise based on the *shape*.

$$op_{t \times N}(n_1, \dots, n_k) = \operatorname{lanes}_{t \times N}^{-1}(op_t(\operatorname{lanes}_{t \times N}(n_1) \dots \operatorname{lanes}_{t \times N}(n_k))$$

Note: For example, the result of instruction i32x4.add applied to operands i_1, i_2 invokes $\operatorname{add}_{i32x4}(i_1, i_2)$, which maps to $\operatorname{lanes}_{i32x4}^{-1}(\operatorname{add}_{i32}(i_1^+, i_2^+))$, where i_1^+ and i_2^+ are sequences resulting from invoking $\operatorname{lanes}_{i32x4}(i_1)$ and $\operatorname{lanes}_{i32x4}(i_2)$ respectively.

v128.const c

1. Push the value v128.const c to the stack.

Note: No formal reduction rule is required for this instruction, since const instructions coincide with *values*.

v128.vvunop

- 1. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 2. Pop the value $\vee 128$.const c_1 from the stack.
- 3. Let c be the result of computing $vvunop_{i128}(c_1)$.
- 4. Push the value v128.const c to the stack.

```
(v128.const c_1) v128.vvunop \hookrightarrow (v128.const c)  (if c = vvunop_{i128}(c_1))
```

v128.vvbinop

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_2 from the stack.
- 3. Pop the value v128.const c_1 from the stack.
- 4. Let c be the result of computing $vvbinop_{i128}(c_1, c_2)$.
- 5. Push the value v128.const c to the stack.

```
(v128.const c_1) (v128.const c_2) v128.vvbinop \hookrightarrow (v128.const c)  (if c = vvbinop_{i128}(c_1, c_2))
```

v128.vvternop

- 1. Assert: due to *validation*, three values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_3 from the stack.
- 3. Pop the value v128.const c_2 from the stack.
- 4. Pop the value v128.const c_1 from the stack.
- 5. Let c be the result of computing $vvternop_{i128}(c_1, c_2, c_3)$.
- 6. Push the value v128.const c to the stack.

```
(v128.const c_1) (v128.const c_2) (v128.const c_3) v128.vvternop \hookrightarrow (v128.const c)  (if c = vvternop_{i128}(c_1, c_2, c_3))
```

v128.any_true

- 1. Assert: due to *validation*, a value of *value type* v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let i be the result of computing $ine_{128}(c_1, 0)$.
- 4. Push the value i32.const i onto the stack.

```
(v128.const c_1) v128.any_true \hookrightarrow (i32.const i) (if i = ine_{128}(c_1, 0))
```

4.4. Instructions 99

i8x16.swizzle

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_2 from the stack.
- 3. Let i^* be the sequence lanes_{i8x16} (c_2) .
- 4. Pop the value v128.const c_1 from the stack.
- 5. Let j^* be the sequence lanes_{i8x16} (c_1) .
- 6. Let c^* be the concatenation of the two sequences j^* 0^{240}
- 7. Let c' be the result of lanes $_{i8x16}^{-1}(c^*[i^*[0]]\dots c^*[i^*[15]])$.
- 8. Push the value v128.const c' onto the stack.

```
 \begin{array}{lll} \text{(v128.const $c_1$) (v128.const $c_2$) v128.swizzle} & \hookrightarrow & \text{(v128.const $c'$)} \\ \text{(if $i^* = \mathrm{lanes}_{i8x16}(c_2)$} \\ & \wedge c^* = \mathrm{lanes}_{i8x16}(c_1) \ 0^{240} \\ & \wedge c' = \mathrm{lanes}_{i8x16}^{-1} \big(c^*[i^*[0]] \dots c^*[i^*[15]]\big)) \end{array}
```

i8x16.shuffle x^*

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Assert: due to *validation*, for all x_i in x^* it holds that $x_i < 32$.
- 3. Pop the value v128.const c_2 from the stack.
- 4. Let i_2^* be the sequence lanes_{i8x16} (c_2) .
- 5. Pop the value v128.const c_1 from the stack.
- 6. Let i_1^* be the sequence lanes_{i8x16} (c_1) .
- 7. Let i^* be the concatenation of the two sequences i_1^* i_2^* .
- 8. Let c be the result of lanes $_{i8x16}^{-1}(i^*[x^*[0]]...i^*[x^*[15]])$.
- 9. Push the value v128.const c onto the stack.

```
 \begin{array}{lll} \text{(v128.const $c_1$) (v128.const $c_2$) v128.shuffle $x^*$} &\hookrightarrow & \text{(v128.const $c$)} \\ \text{(if $i^* = \mathrm{lanes}_{i8x16}(c_1) \ \mathrm{lanes}_{i8x16}(c_2)$} \\ &\wedge c = \mathrm{lanes}_{i8x16}^{-1}(i^*[x^*[0]] \dots i^*[x^*[15]])) \end{array}
```

shape.splat

- 1. Let t be the type unpacked (shape).
- 2. Assert: due to validation, a value of value type t is on the top of the stack.
- 3. Pop the value t.const c_1 from the stack.
- 4. Let N be the integer $\dim(shape)$.
- 5. Let c be the result of lanes $_{shape}^{-1}(c_1^N)$.
- 6. Push the value v128.const c to the stack.

```
(t.\mathsf{const}\ c_1)\ \mathit{shape}.\mathsf{splat}\ \hookrightarrow\ (\mathsf{v128}.\mathsf{const}\ c) \qquad (\mathsf{if}\ t = \mathsf{unpacked}(\mathit{shape}) \land c = \mathsf{lanes}_{\mathit{shape}}^{-1}(c_1^{\dim(\mathit{shape})}))
```

$t_1 \times N$.extract_lane_sx? x

- 1. Assert: due to validation, x < N.
- 2. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 3. Pop the value $\vee 128$.const c_1 from the stack.
- 4. Let i^* be the sequence $lanes_{t_1 \times N}(c_1)$.
- 5. Let t_2 be the type unpacked $(t_1 \times N)$.
- 6. Let c_2 be the result of computing extend $c_1^{sx^2}(i^*[x])$.
- 7. Push the value t_2 .const c_2 to the stack.

shape.replace_lane x

- 1. Assert: due to validation, $x < \dim(shape)$.
- 2. Let t_1 be the type unpacked(*shape*).
- 3. Assert: due to *validation*, a value of *value type* t_1 is on the top of the stack.
- 4. Pop the value t_1 .const c_1 from the stack.
- 5. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 6. Pop the value v128.const c_2 from the stack.
- 7. Let i^* be the sequence lanes_{shape} (c_2) .
- 8. Let c be the result of computing lanes $_{shape}^{-1}(i^* \text{ with } [x] = c_1)$
- 9. Push v128.const c on the stack.

```
\begin{array}{ll} (t_1.\mathsf{const}\ c_1)\ (\mathsf{v}128.\mathsf{const}\ c_2)\ shape.\mathsf{replace\_lane}\ x\ \hookrightarrow\ (\mathsf{v}128.\mathsf{const}\ c)\\ (\mathsf{if}\ i^* = \mathsf{lanes}_{shape}(c_2)\\ \land\ c = \mathsf{lanes}_{shape}^{-1}(i^*\ \mathsf{with}\ [x] = c_1)) \end{array}
```

shape.vunop

- 1. Assert: due to *validation*, a value of *value type* v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let c be the result of computing $vunop_{shape}(c_1)$.
- 4. Push the value v128.const c to the stack.

```
(v128.const c_1) v128.vunop \hookrightarrow (v128.const c)  (if c = vunop_{shape}(c_1))
```

4.4. Instructions

shape.vbinop

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_2 from the stack.
- 3. Pop the value v128.const c_1 from the stack.
- 4. If $vbinop_{shape}(c_1, c_2)$ is defined:
 - a. Let c be a possible result of computing $vbinop_{shape}(c_1, c_2)$.
 - b. Push the value v128.const c to the stack.
- 5. Else:
 - a. Trap.

```
        \text{(v128.const } c_1 \text{) (v128.const } c_2 \text{) } shape.vbinop \quad \hookrightarrow \quad         \text{(v128.const } c \text{)} \qquad          \text{(if } c \in vbinop_{shape}(c_1, c_2) \text{)}           \text{(v128.const } c_1 \text{) (v128.const } c_2 \text{) } shape.vbinop \quad \hookrightarrow \quad         \text{trap}           \text{(if } vbinop_{shape}(c_1, c_2) = \{\} \text{)}
```

txN.vrelop

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_2 from the stack.
- 3. Pop the value v128.const c_1 from the stack.
- 4. Let i^* be the sequence lanes_{t×N} (c_1) .
- 5. Let j^* be the sequence lanes $_{t \times N}(c_2)$.
- 6. Let c be the result of computing lanes $_{t \times N}^{-1}(\operatorname{extend}^{\mathsf{s}}_{1,|t|}(\operatorname{vrelop}_t(i^*,j^*)))$.
- 7. Push the value v128.const c to the stack.

txN.vishiftop

- 1. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 2. Pop the value i32.const s from the stack.
- 3. Assert: due to *validation*, a value of *value type* v128 is on the top of the stack.
- 4. Pop the value v128.const c_1 from the stack.
- 5. Let i^* be the sequence lanes $_{t\times N}(c_1)$.
- 6. Let c be lanes $_{t \times N}^{-1}(vishiftop_t(i^*, s^N))$.
- 7. Push the value v128.const c to the stack.

```
 \begin{array}{lll} \mbox{(v128.const $c_1$) (i32.const $s$) $txN.vishiftop} &\hookrightarrow & \mbox{(v128.const $c$)} \\ \mbox{(if $i^* = {\rm lanes}_{txN}(c_1)$} \\ \mbox{$\wedge$ $c = {\rm lanes}_{txN}^{-1}(vishiftop_t(i^*, s^N)))$} \end{array}
```

shape.all true

- 1. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let i_1^* be the sequence lanes_{shape} (c_1)
- 4. Let i be the result of computing bool($\bigwedge(i_1 \neq 0)^*$).
- 5. Push the value i32.const i onto the stack.

```
(v128.const c_1) shape.all\_true \hookrightarrow (i32.const <math>i)

(if i_1^* = lanes_{shape}(c)

\land i = bool(\bigwedge(i_1 \neq 0)^*))
```

txN.bitmask

- 1. Assert: due to *validation*, a value of *value type* v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let i_1^N be the sequence lanes $_{t \times N}(c)$.
- 4. Let B be the bit width |t| of value type t.
- 5. Let i_2^N be the sequence as a result of computing ilt_s_B $(i_1^N, 0^N)$.
- 6. Let c be the integer $\mathrm{ibits}_{32}^{-1}(i_2^N\ 0^{32-N})$.
- 7. Push the value i32.const c onto the stack.

```
(v128.\mathsf{const}\ c_1)\ t \times N.\mathsf{bitmask} \ \hookrightarrow \ (\mathsf{i32.const}\ c) \qquad (\mathsf{if}\ c = \mathsf{ibits}_{32}^{-1}(\mathsf{ilt\_s}_{|t|}(\mathsf{lanes}_{t \times N}(c), 0^N)))
```

$t_2 \times N$.narrow $t_1 \times M$ sx

- 1. Assert: due to syntax, $N = 2 \cdot M$.
- 2. Assert: due to validation, two values of value type v128 are on the top of the stack.
- 3. Pop the value v128.const c_2 from the stack.
- 4. Let d_2^M be the result of computing $\underset{|t_1|,|t_2|}{\operatorname{narrow}} \overset{sx}{\underset{|t_1|,|t_2|}{\operatorname{lanes}}} (\operatorname{lanes}_{t_1 \times M}(c_2))$.
- 5. Pop the value v128.const c_1 from the stack.
- 6. Let d_1^M be the result of computing $\underset{|t_1|,|t_2|}{\operatorname{narrow}}_{|t_1|,|t_2|}^{sx}(\operatorname{lanes}_{t_1 \times M}(c_1))$.
- 7. Let c be the result of lanes $_{t_2 \times N}^{-1}(d_1^M d_2^M)$.
- 8. Push the value $v128.const\ c$ onto the stack.

```
 \begin{array}{lll}  (\text{v128.const } c_1) & (\text{v128.const } c_2) & t_2 \times N. \mathsf{narrow}\_t_1 \times M\_sx & \hookrightarrow & (\text{v128.const } c) \\  & & (\text{if } d_1^M = \mathsf{narrow}_{|t_1|,|t_2|}^{sx} (\mathsf{lanes}_{t_1 \times M}(c_1)) \\  & & \wedge d_2^M = \mathsf{narrow}_{|t_1|,|t_2|}^{sx} (\mathsf{lanes}_{t_1 \times M}(c_2)) \\  & & \wedge c = \mathsf{lanes}_{t_2 \times N}^{-1} (d_1^M & d_2^M)) \end{array}
```

4.4. Instructions 103

$t_2 \times N.vcvtop_t_1 \times M_sx$

- 1. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let i^* be the sequence $lanes_{t_1 \times M}(c_1)$.
- 4. Let c be the result of computing lanes $_{t imes XN}^{-1}(vcvtop_{|t_1|,|t_2|}^{sx}(i^*))$
- 5. Push the value v128.const c onto the stack.

$t_2 \times N.vcvtop_half_t_1 \times M_sx^?$

- 1. Assert: due to *validation*, a value of *value type* v128 is on the top of the stack.
- 2. Pop the value $\vee 128$.const c_1 from the stack.
- 3. If *half* is low, then:
 - a. Let i^* be the sequence $lanes_{t_1 \times M}(c_1)[0:N]$.
- 4. Else:
 - a. Let i^* be the sequence lanes $_{t_1 \times M}(c_1)[N:N]$.
- 5. Let j^* be the result of computing $vcvtop_{\lfloor t_1 \rfloor, \lfloor t_2 \rfloor}^{sx^2}(i^*)$.
- 6. Let c be the result of computing lanes $_{t_2 \times N}^{-1}(j^*)$.
- 7. Push the value v128.const c onto the stack.

where:

$$\begin{array}{lcl} \mathsf{low}(x,y) & = & x \\ \mathsf{high}(x,y) & = & y \end{array}$$

$t_2 \times N.vcvtop$ $t_1 \times M$ sx zero

- 1. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let i^* be the sequence $lanes_{t_1 \times M}(c_1)$.
- 4. Let j^* be the result of computing $vcvtop^{sx}_{|t_1|,|t_2|}(i^*)$ concatenated with the vector 0^M .
- 5. Let c be the result of computing lanes $_{t_2 \times N}^{-1}(j^*)$.
- 6. Push the value v128.const c onto the stack.

```
 \begin{array}{lll} \left( \texttt{v128.const} \ c_1 \right) \ t_2 \texttt{x} N. vcvtop\_t_1 \texttt{x} M\_sx\_{\texttt{zero}} &\hookrightarrow & \left( \texttt{v128.const} \ c \right) \\ \left( \texttt{if} \ c = \texttt{lanes}_{t_2 \texttt{x} N}^{-1} \big( vcvtop_{|t_1|, |t_2|}^{sx} \big) \big( \texttt{lanes}_{t_1 \texttt{x} M} \big( c_1 \big) \big) \ 0^M \big) \big) \end{array}
```

i32x4.dot_i16x8_s

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_2 from the stack.
- 3. Pop the value v128.const c_1 from the stack.
- 4. Let $(i_1 i_2)^*$ be the result of computing $imul_{32}(extend_{16,32}^s(lanes_{i16x8}(c_1)), extend_{16,32}^s(lanes_{i16x8}(c_2)))$
- 5. Let j^* be the result of computing $iadd_{32}(i_1, i_2)^*$.
- 6. Let c be the result of computing lanes $_{332\times4}^{-1}(j^*)$.
- 7. Push the value v128.const c onto the stack.

```
(v128.const c_1) (v128.const c_2) i32x4.dot_i16x8_s \hookrightarrow (v128.const c) (if (i_1 \ i_2)^* = \operatorname{imul}_{32}(\operatorname{extend}^{\mathfrak{s}}_{16,32}(\operatorname{lanes}_{i16x8}(c_1)), \operatorname{extend}^{\mathfrak{s}}_{16,32}(\operatorname{lanes}_{i16x8}(c_2))) \land j^* = \operatorname{iadd}_{32}(i_1, i_2)^* \land c = \operatorname{lanes}_{i32x4}^{-1}(j^*))
```

t_2 xN.extmul $_half_t_1$ x M_sx

- 1. Assert: due to *validation*, two values of *value type* v128 are on the top of the stack.
- 2. Pop the value v128.const c_2 from the stack.
- 3. Pop the value v128.const c_1 from the stack.
- 4. If *half* is low, then:
 - a. Let i^* be the sequence lanes $_{t_1 \times M}(c_1)[0:N]$.
 - b. Let j^* be the sequence lanes $_{t_1 \times M}(c_2)[0:N]$.
- 5. Else:
 - a. Let i^* be the sequence $lanes_{t_1 \times M}(c_1)[N:N]$.
 - b. Let j^* be the sequence $lanes_{t_1 \times M}(c_2)[N:N]$.
- 6. Let c be the result of computing $lanes_{t_2 \times N}^{-1}(imul_{t_2 \times N}(extend_{|t_1|,|t_2|}^{sx}(i^*), extend_{|t_1|,|t_2|}^{sx}(j^*)))$
- 7. Push the value v128.const c onto the stack.

where:

$$\begin{array}{lcl} \mathsf{low}(x,y) & = & x \\ \mathsf{high}(x,y) & = & y \end{array}$$

$t_2 \times N$.extadd_pairwise_ $t_1 \times M$ _sx

- 1. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 2. Pop the value v128.const c_1 from the stack.
- 3. Let $(i_1 i_2)^*$ be the sequence extend $^{sx}_{|t_1|,|t_2|}(lanes_{t_1 \times M}(c_1))$.
- 4. Let j^* be the result of computing iadd $_N(i_1, i_2)^*$.
- 5. Let c be the result of computing lanes $_{t imes N}^{-1}(j^*)$.
- 6. Push the value v128.const c to the stack.

4.4.4 Parametric Instructions

drop

- 1. Assert: due to *validation*, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.

```
val \ \mathsf{drop} \ \hookrightarrow \ \epsilon
```

select (t^*) ?

- 1. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 2. Pop the value i32.const c from the stack.
- 3. Assert: due to *validation*, two more values (of the same *value type*) are on the top of the stack.
- 4. Pop the value val_2 from the stack.
- 5. Pop the value val_1 from the stack.
- 6. If c is not 0, then:
 - a. Push the value val_1 back to the stack.
- 7. Else:
 - a. Push the value val_2 back to the stack.

```
\begin{array}{lll} val_1 \ val_2 \ ({\rm i32.const} \ c) \ {\rm select} \ t^? & \hookrightarrow & val_1 & \quad ({\rm if} \ c \neq 0) \\ val_1 \ val_2 \ ({\rm i32.const} \ c) \ {\rm select} \ t^? & \hookrightarrow & val_2 & \quad ({\rm if} \ c = 0) \end{array}
```

Note: In future versions of WebAssembly, select may allow more than one value per choice.

4.4.5 Variable Instructions

local.get x

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, F.locals[x] exists and is non-empty.
- 3. Let val be the value F.locals[x].
- 4. Push the value val to the stack.

$$F$$
; (local.get x) \hookrightarrow F ; val (if F .locals[x] = val)

local.set x

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, F.locals[x] exists.
- 3. Assert: due to *validation*, a value is on the top of the stack.
- 4. Pop the value *val* from the stack.
- 5. Replace F.locals[x] with the value val.

```
F; val (local.set x) \hookrightarrow F'; \epsilon (if F' = F with locals[x] = val)
```

local.tee x

- 1. Assert: due to *validation*, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. Push the value *val* to the stack.
- 4. Push the value *val* to the stack.
- 5. *Execute* the instruction (local.set x).

```
val 	ext{ (local.tee } x) 	ext{ } \hookrightarrow 	ext{ } val 	ext{ (local.set } x)
```

$\mathsf{global}.\mathsf{get}\ x$

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, F.module.globaladdrs[x] exists.
- 3. Let a be the global address F.module.globaladdrs[x].
- 4. Assert: due to *validation*, S.globals[a] exists.
- 5. Let glob be the global instance S.globals[a].
- 6. Let *val* be the value *glob*.value.
- 7. Push the value *val* to the stack.

```
S; F; (\mathsf{global}.\mathsf{get}\ x) \hookrightarrow S; F; val 
(if S.\mathsf{globals}[F.\mathsf{module}.\mathsf{globaladdrs}[x]].\mathsf{value} = val)
```

global.set x

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, F.module.globaladdrs[x] exists.
- 3. Let a be the global address F.module.globaladdrs[x].
- 4. Assert: due to *validation*, S.globals[a] exists.
- 5. Let glob be the global instance S.globals[a].
- 6. Assert: due to *validation*, a value is on the top of the stack.
- 7. Pop the value *val* from the stack.
- 8. Replace glob.value with the value val.

```
S; F; val \text{ (global.set } x) \hookrightarrow S'; F; \epsilon
(if S' = S \text{ with globals}[F. module. global addrs}[x]]. value = <math>val)
```

Note: Validation ensures that the global is, in fact, marked as mutable.

4.4.6 Table Instructions

$\mathsf{table}.\mathsf{get}\;x$

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, F.module.tableaddrs[x] exists.
- 3. Let a be the *table address F*.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[a] exists.
- 5. Let tab be the *table instance* S.tables[a].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const i from the stack.
- 8. If i is not smaller than the length of tab.elem, then:
 - a. Trap.
- 9. Let val be the value tab.elem[i].
- 10. Push the value val to the stack.

```
S; F; (i32.const i) (table.get x) \hookrightarrow S; F; val (if S.tables[F.module.tableaddrs[x]].elem[i] = val) S; F; (i32.const i) (table.get x) \hookrightarrow S; F; trap (otherwise)
```

table.set x

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, F.module.tableaddrs[x] exists.
- 3. Let a be the table address F.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[a] exists.
- 5. Let tab be the table instance S.tables[a].
- 6. Assert: due to *validation*, a *reference value* is on the top of the stack.
- 7. Pop the value val from the stack.
- 8. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 9. Pop the value i32.const i from the stack.
- 10. If i is not smaller than the length of tab.elem, then:
 - a. Trap.
- 11. Replace the element tab.elem[i] with val.

```
S; F; (i32.const i) val (table.set x) \hookrightarrow S'; F; \epsilon (if S' = S with tables [F].module.tableaddrs [x]].elem [i] = val) S; F; (i32.const i) val (table.set x) \hookrightarrow S; F; trap (otherwise)
```

table.size x

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, F.module.tableaddrs[x] exists.
- 3. Let a be the table address F.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[a] exists.
- 5. Let tab be the table instance S.tables[a].
- 6. Let sz be the length of tab.elem.
- 7. Push the value i32.const sz to the stack.

```
S; F; table.size x \hookrightarrow S; F; (i32.const sz)
(if |S.tables[F.module.tableaddrs[x]].elem|=sz)
```

table.grow x

- 1. Let F be the *current frame*.
- 2. Assert: due to *validation*, F.module.tableaddrs[x] exists.
- 3. Let a be the *table address* F.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[a] exists.
- 5. Let tab be the table instance S.tables[a].
- 6. Let sz be the length of S.tables[a].
- 7. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 8. Pop the value i32.const n from the stack.
- 9. Assert: due to validation, a reference value is on the top of the stack.
- 10. Pop the value val from the stack.
- 11. Either, try growing table by n entries with initialization value val:
- a. If it succeeds, push the value i32.const $\it sz$ to the stack.
- b. Else, push the value i32.const (-1) to the stack.
- 12. Or, push the value i32.const (-1) to the stack.

```
S; F; val \ (i32.\mathsf{const} \ n) \ \mathsf{table.grow} \ x \hookrightarrow S'; F; (i32.\mathsf{const} \ sz) \ (\mathsf{if} \ F.\mathsf{module.tableaddrs}[x] = a \ \land sz = |S.\mathsf{tables}[a].\mathsf{elem}| \ \land S' = S \ \mathsf{with} \ \mathsf{tables}[a] = \mathsf{growtable}(S.\mathsf{tables}[a], n, val)) \ S; F; (i32.\mathsf{const} \ n) \ \mathsf{table.grow} \ x \hookrightarrow S; F; (i32.\mathsf{const} \ -1)
```

Note: The table grow instruction is non-deterministic. It may either succeed, returning the old table size sz, or fail, returning -1. Failure *must* occur if the referenced table instance has a maximum size defined that would be exceeded. However, failure *can* occur in other cases as well. In practice, the choice depends on the *resources* available to the *embedder*.

table.fill x

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, F.module.tableaddrs[x] exists.
- 3. Let ta be the *table address F*.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[ta] exists.
- 5. Let tab be the table instance S.tables[ta].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const n from the stack.
- 8. Assert: due to *validation*, a *reference value* is on the top of the stack.
- 9. Pop the value *val* from the stack.
- 10. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 11. Pop the value i32.const i from the stack.
- 12. If i + n is larger than the length of tab.elem, then:
 - a. Trap.
- 12. If n is 0, then:
 - a. Return.
- 13. Push the value i32.const i to the stack.
- 14. Push the value val to the stack.
- 15. Execute the instruction table.set x.
- 16. Push the value i32.const (i + 1) to the stack.
- 17. Push the value *val* to the stack.
- 18. Push the value i32.const (n-1) to the stack.
- 19. Execute the instruction table.fill x.

```
S; F; (\mathsf{i32.const}\ i)\ val\ (\mathsf{i32.const}\ n)\ (\mathsf{table.fill}\ x) \ \hookrightarrow \ S; F; \mathsf{trap}\ (\mathsf{if}\ i+n>|S.\mathsf{tables}[F.\mathsf{module.tableaddrs}[x]].\mathsf{elem}|) S; F; (\mathsf{i32.const}\ i)\ val\ (\mathsf{i32.const}\ 0)\ (\mathsf{table.fill}\ x) \ \hookrightarrow \ S; F; \epsilon\ (\mathsf{otherwise}) S; F; (\mathsf{i32.const}\ i)\ val\ (\mathsf{i32.const}\ n+1)\ (\mathsf{table.fill}\ x) \ \hookrightarrow \ S; F; (\mathsf{i32.const}\ i)\ val\ (\mathsf{table.set}\ x)\ (\mathsf{i32.const}\ i)\ val\ (\mathsf{i32.const}\ i)\ val\ (\mathsf{i32.const}\ n)\ (\mathsf{table.fill}\ x) (otherwise)
```

table.copy x y

- 1. Let *F* be the *current frame*.
- 2. Assert: due to validation, F.module.tableaddrs[x] exists.
- 3. Let ta_x be the *table address F.*module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[ta_x] exists.
- 5. Let tab_x be the *table instance* S.tables[ta_x].
- 6. Assert: due to *validation*, F.module.tableaddrs[y] exists.
- 7. Let ta_y be the *table address F*.module.tableaddrs[y].

- 8. Assert: due to *validation*, S.tables[ta_y] exists.
- 9. Let tab_y be the *table instance* S.tables[ta_y].
- 10. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 11. Pop the value i32.const n from the stack.
- 12. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 13. Pop the value i32.const s from the stack.
- 14. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 15. Pop the value i32.const d from the stack.
- 16. If s + n is larger than the length of tab_y elem or d + n is larger than the length of tab_x elem, then:
 - a. Trap.
- 17. If n = 0, then:
- a. Return.
- 18. If $d \leq s$, then:
- a. Push the value i32.const d to the stack.
- b. Push the value i32.const s to the stack.
- c. Execute the instruction table.get y.
- d. Execute the instruction table.set x.
- e. Assert: due to the earlier check against the table size, $d+1 < 2^{32}$.
- f. Push the value i32.const (d+1) to the stack.
- g. Assert: due to the earlier check against the table size, $s+1<2^{32}$.
- h. Push the value i32.const (s+1) to the stack.
- 19. Else:
 - a. Assert: due to the earlier check against the table size, $d + n 1 < 2^{32}$.
 - b. Push the value i32.const (d + n 1) to the stack.
 - c. Assert: due to the earlier check against the table size, $s + n 1 < 2^{32}$.
 - d. Push the value i32.const (s + n 1) to the stack.
 - c. Execute the instruction table.get y.
 - f. Execute the instruction table.set x.
 - g. Push the value i32.const d to the stack.
 - h. Push the value i32.const s to the stack.
- 20. Push the value i32.const (n-1) to the stack.
- 21. Execute the instruction table.copy x y.

```
S; F; (\mathrm{i}32.\mathsf{const}\ d)\ (\mathrm{i}32.\mathsf{const}\ s)\ (\mathrm{i}32.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{copy}\ x\ y) \ \hookrightarrow \ S; F; \mathsf{trap}\ (\mathsf{if}\ s+n>|S.\mathsf{tables}[F.\mathsf{module}.\mathsf{tableaddrs}[y]].\mathsf{elem}| \ \lor d+n>|S.\mathsf{tables}[F.\mathsf{module}.\mathsf{tableaddrs}[x]].\mathsf{elem}|) S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ 0)\ (\mathsf{table}.\mathsf{copy}\ x\ y) \ \hookrightarrow \ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ n+1)\ (\mathsf{table}.\mathsf{copy}\ x\ y) \ \hookrightarrow \ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{table}.\mathsf{get}\ y)\ (\mathsf{table}.\mathsf{set}\ x)\ (\mathsf{i}32.\mathsf{const}\ d+1)\ (\mathsf{i}32.\mathsf{const}\ s+1)\ (\mathsf{i}32.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{copy}\ x\ y) (otherwise, if d \le s) S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ s+n-1)\ (\mathsf{table}.\mathsf{copy}\ x\ y)\ (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{copy}\ x\ y) (otherwise, if d > s)
```

table.init x y

- 1. Let *F* be the *current frame*.
- 2. Assert: due to validation, F.module.tableaddrs[x] exists.
- 3. Let ta be the *table address F*.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[ta] exists.
- 5. Let tab be the table instance S.tables[ta].
- 6. Assert: due to *validation*, F.module.elemaddrs[y] exists.
- 7. Let ea be the $element\ address\ F$.module.elemaddrs[y].
- 8. Assert: due to *validation*, S.elems[ea] exists.
- 9. Let *elem* be the *element instance* S.elems[ea].
- 10. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 11. Pop the value i32.const n from the stack.
- 12. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 13. Pop the value i32.const s from the stack.
- 14. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 15. Pop the value i32.const d from the stack.
- 16. If s + n is larger than the length of elem.elem or d + n is larger than the length of tab.elem, then:
 - a. Trap.
- 17. If n = 0, then:
 - a. Return.
- 18. Let val be the reference value elem. elem[s].
- 19. Push the value i32.const d to the stack.
- 20. Push the value *val* to the stack.
- 21. Execute the instruction table.set x.
- 22. Assert: due to the earlier check against the table size, $d + 1 < 2^{32}$.
- 23. Push the value i32.const (d+1) to the stack.
- 24. Assert: due to the earlier check against the segment size, $s+1<2^{32}$.
- 25. Push the value i32.const (s+1) to the stack.

- 26. Push the value i32.const (n-1) to the stack.
- 27. Execute the instruction table init x y.

```
S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{init}\ x\ y) \quad\hookrightarrow\quad S; F; \mathsf{trap}\\ (\mathsf{if}\ s+n>|S.\mathsf{elems}[F.\mathsf{module}.\mathsf{elemaddrs}[y]].\mathsf{elem}|\\ \vee\ d+n>|S.\mathsf{tables}[F.\mathsf{module}.\mathsf{tableaddrs}[x]].\mathsf{elem}|)\\ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ 0)\ (\mathsf{table}.\mathsf{init}\ x\ y) \quad\hookrightarrow\quad S; F; \epsilon\\ (\mathsf{otherwise})\\ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ n+1)\ (\mathsf{table}.\mathsf{init}\ x\ y) \quad\hookrightarrow\quad S; F; (\mathsf{i}32.\mathsf{const}\ d)\ val\ (\mathsf{table}.\mathsf{set}\ x)\\ (\mathsf{i}32.\mathsf{const}\ d+1)\ (\mathsf{i}32.\mathsf{const}\ s+1)\ (\mathsf{i}32.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{init}\ x\ y)\\ (\mathsf{otherwise}, \mathsf{if}\ val=S.\mathsf{elems}[F.\mathsf{module}.\mathsf{elemaddrs}[y]].\mathsf{elem}[s])
```

elem.drop x

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, F.module.elemaddrs[x] exists.
- 3. Let a be the *element address* F.module.elemaddrs[x].
- 4. Assert: due to *validation*, S.elems[a] exists.
- 5. Replace S.elems[a] with the element instance {elem ϵ }.

```
S; F; (\mathsf{elem.drop}\ x) \hookrightarrow S'; F; \epsilon
(if S' = S with \mathsf{elems}[F.\mathsf{module}.\mathsf{elemaddrs}[x]] = \{\mathsf{elem}\ \epsilon\})
```

4.4.7 Memory Instructions

Note: The alignment memarg.align in load and store instructions does not affect the semantics. It is an indication that the offset ea at which the memory is accessed is intended to satisfy the property $ea \mod 2^{memarg.align} = 0$. A WebAssembly implementation can use this hint to optimize for the intended use. Unaligned access violating that property is still allowed and must succeed regardless of the annotation. However, it may be substantially slower on some hardware.

$t.\mathsf{load}\ memarg\ \mathbf{and}\ t.\mathsf{load}N_sx\ memarg$

- 1. Let F be the *current frame*.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the *memory address F*.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If N is not part of the instruction, then:
 - a. Let N be the bit width |t| of number type t.

- 10. If ea + N/8 is larger than the length of mem.data, then:
 - a. Trap.
- 11. Let b^* be the byte sequence mem.data[ea:N/8].
- 12. If N and sx are part of the instruction, then:
 - a. Let n be the integer for which bytes_{iN} $(n) = b^*$.
 - b. Let c be the result of computing extend $\sum_{N,|t|}^{sx}(n)$.
- 13. Else:
 - a. Let c be the constant for which bytes_t(c) = b^* .
- 14. Push the value t.const c to the stack.

```
\begin{array}{lll} S; F; (\mathrm{i}32.\mathsf{const}\ i)\ (t.\mathsf{load}\ memarg) &\hookrightarrow &S; F; (t.\mathsf{const}\ c) \\ &(\mathrm{if}\ ea = i + memarg.\mathsf{offset} \\ &\land ea + |t|/8 \leq |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}| \\ &\land \mathsf{bytes}_t(c) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[ea:|t|/8]) \\ S; F; (\mathrm{i}32.\mathsf{const}\ i)\ (t.\mathsf{load}N\_sx\ memarg) &\hookrightarrow &S; F; (t.\mathsf{const}\ \mathrm{extend}_{N,|t|}^{sx}(n)) \\ &(\mathrm{if}\ ea = i + memarg.\mathsf{offset} \\ &\land ea + N/8 \leq |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}| \\ &\land \mathsf{bytes}_{iN}(n) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[ea:N/8]) \\ S; F; (\mathrm{i}32.\mathsf{const}\ k)\ (t.\mathsf{load}(N\_sx)^?\ memarg) &\hookrightarrow &S; F; \mathsf{trap} \\ &(\mathsf{otherwise}) \end{array}
```

v128.load $M \times N _sx \ memarg$

- 1. Let *F* be the *current frame*.
- 2. Assert: due to validation, F.module.memaddrs[0] exists.
- 3. Let a be the *memory address F*.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If $ea + M \cdot N/8$ is larger than the length of mem.data, then:
 - a. Trap.
- 10. Let b^* be the byte sequence $mem.data[ea: M \cdot N/8]$.
- 11. Let m_k be the integer for which by $tes_{iM}(m_k) = b^*[k \cdot M/8 : M/8]$.
- 12. Let W be the integer $M \cdot 2$.
- 13. Let n_k be the result of extend $M,W(m_k)$.
- 14. Let c be the result of computing lanes $_{iW\times N}^{-1}(n_0\dots n_{N-1})$.
- 15. Push the value v128.const c to the stack.

```
S; F; (\mathsf{i}32.\mathsf{const}\ i)\ (\mathsf{v}128.\mathsf{load}M\mathsf{x}N\_\mathit{sx}\ \mathit{memarg}) \ \hookrightarrow \ S; F; (\mathsf{v}128.\mathsf{const}\ c)  (\mathsf{if}\ \mathit{ea} = i + \mathit{memarg}.\mathsf{offset}  \land \mathit{ea} + M \cdot N/8 \leq |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}|  \land \mathit{bytes}_{iM}(m_k) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[\mathit{ea} + k \cdot M/8 : M/8]  \land W = M \cdot 2  \land c = \mathsf{lanes}_{iW \times N}^{-1}(\mathsf{extend}_{M,W}^{\mathit{sx}}(m_0) \ldots \mathsf{extend}_{M,W}^{\mathit{sx}}(m_{N-1})))  S; F; (\mathsf{i}32.\mathsf{const}\ k)\ (\mathsf{v}128.\mathsf{load}M\mathsf{x}N\_\mathit{sx}\ \mathit{memarg}) \ \hookrightarrow \ S; F; \mathsf{trap}  (\mathsf{otherwise})
```

v128.loadN splat memarg

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the *memory address* F.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If ea + N/8 is larger than the length of mem.data, then:
 - a. Trap.
- 10. Let b^* be the byte sequence mem.data[ea: N/8].
- 11. Let n be the integer for which bytes_{iN} $(n) = b^*$.
- 12. Let L be the integer 128/N.
- 13. Let c be the result of computing lanes $_{iN\times L}^{-1}(n^L)$.
- 14. Push the value v128.const c to the stack.

```
S; F; (\mathsf{i32.const}\ i)\ (\mathsf{v128.load}\ N\_\mathsf{splat}\ memarg) \ \hookrightarrow \ S; F; (\mathsf{v128.const}\ c)  (\mathsf{if}\ ea = i + memarg.\mathsf{offset}  \land ea + N/8 \le |S.\mathsf{mems}[F.\mathsf{module.memaddrs}[0]].\mathsf{data}| \land \mathsf{bytes}_{iN}(n) = S.\mathsf{mems}[F.\mathsf{module.memaddrs}[0]].\mathsf{data}[ea : N/8] \land c = \mathsf{lanes}_{iN \times L}^{-1}(n^L)) S; F; (\mathsf{i32.const}\ k)\ (\mathsf{v128.load}\ N\_\mathsf{splat}\ memarg) \ \hookrightarrow \ S; F; \mathsf{trap} (\mathsf{otherwise})
```

v128.loadN_zero memarg

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the memory address F.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.

- 9. If ea + N/8 is larger than the length of mem.data, then:
 - a. Trap.
- 10. Let b^* be the byte sequence mem.data[ea: N/8].
- 11. Let n be the integer for which bytes_{iN} $(n) = b^*$.
- 12. Let c be the result of extend $_{N,128}^{\mathsf{u}}(n)$.
- 13. Push the value v128.const c to the stack.

```
S; F; (\mathsf{i}32.\mathsf{const}\ i)\ (\mathsf{v}128.\mathsf{load}N\_\mathsf{zero}\ memarg) \ \hookrightarrow \ S; F; (\mathsf{v}128.\mathsf{const}\ c)  (if ea = i + memarg.\mathsf{o}\mathsf{f}\mathsf{f}\mathsf{set}  \land ea + N/8 \le |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}|   \land \mathsf{bytes}_{iN}(n) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[ea : N/8]   \land c = \mathsf{extend}^\mathsf{u}_{N,128}(n))  S; F; (\mathsf{i}32.\mathsf{const}\ k)\ (\mathsf{v}128.\mathsf{load}N\_\mathsf{zero}\ memarg) \ \hookrightarrow \ S; F; \mathsf{trap}  (otherwise)
```

v128.loadN_lane memarg x

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the *memory address F*.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 7. Pop the value v128.const v from the stack.
- 8. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 9. Pop the value i32.const i from the stack.
- 10. Let ea be the integer i + memarg.offset.
- 11. If ea + N/8 is larger than the length of mem.data, then:
 - a. Trap.
- 12. Let b^* be the byte sequence mem.data[ea:N/8].
- 13. Let r be the constant for which by $tes_{iN}(r) = b^*$.
- 14. Let *L* be 128/N.
- 15. Let c be the result of computing lanes $_{iN\times L}^{-1}(lanes_{iN\times L}(v))$ with [x]=r.
- 16. Push the value v128.const c to the stack.

```
S; F; (\mathsf{i}32.\mathsf{const}\ i)\ (\mathsf{v}128.\mathsf{const}\ v)\ (\mathsf{v}128.\mathsf{load}N_{\mathsf{lane}}\ memarg\ x) \ \hookrightarrow \ S; F; (\mathsf{v}128.\mathsf{const}\ c)\ (\mathsf{if}\ ea = i + memarg.\mathsf{offset}\ \land ea + N/8 \leq |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}|\ \land \mathsf{bytes}_{iN}(r) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[ea : N/8]\ \land L = 128/N\ \land c = \mathsf{lanes}_{\mathsf{i}N\times L}^{-1}(\mathsf{lanes}_{\mathsf{i}N\times L}(v)\ \mathsf{with}\ [x] = r))\ S; F; (\mathsf{i}32.\mathsf{const}\ k)\ (\mathsf{v}128.\mathsf{const}\ v)\ (\mathsf{v}128.\mathsf{load}N_{\mathsf{lane}}\ memarg\ x) \ \hookrightarrow \ S; F; \mathsf{trap}\ (\mathsf{otherwise})
```

t.store memarg and t.storeN memarg

- 1. Let F be the current frame.
- 2. Assert: due to validation, F.module.memaddrs[0] exists.
- 3. Let a be the *memory address F*.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to *validation*, a value of *value type t* is on the top of the stack.
- 7. Pop the value t.const c from the stack.
- 8. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 9. Pop the value i32.const i from the stack.
- 10. Let ea be the integer i + memarg.offset.
- 11. If N is not part of the instruction, then:
 - a. Let N be the bit width |t| of number type t.
- 12. If ea + N/8 is larger than the length of mem.data, then:
 - a. Trap.
- 13. If N is part of the instruction, then:
 - a. Let n be the result of computing $\operatorname{wrap}_{|t|,N}(c)$.
 - b. Let b^* be the byte sequence bytes_{iN}(n).
- 14. Else:
 - a. Let b^* be the byte sequence bytes_t(c).
- 15. Replace the bytes mem.data[ea:N/8] with b^* .

```
S; F; (\mathsf{i32.const}\ i)\ (t.\mathsf{const}\ c)\ (t.\mathsf{store}\ memarg) \ \hookrightarrow \ S'; F; \epsilon \\ (\mathsf{if}\ ea = i + memarg.\mathsf{offset} \\ \land ea + |t|/8 \le |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}| \\ \land S' = S\ \mathsf{with}\ \mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[ea : |t|/8] = \mathsf{bytes}_t(c)) \\ S; F; (\mathsf{i32.const}\ i)\ (t.\mathsf{const}\ c)\ (t.\mathsf{store}N\ memarg) \ \hookrightarrow \ S'; F; \epsilon \\ (\mathsf{if}\ ea = i + memarg.\mathsf{offset} \\ \land ea + N/8 \le |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}| \\ \land S' = S\ \mathsf{with}\ \mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}[ea : N/8] = \mathsf{bytes}_{iN}(\mathsf{wrap}_{|t|,N}(c))) \\ S; F; (\mathsf{i32.const}\ k)\ (t.\mathsf{const}\ c)\ (t.\mathsf{store}N^{?}\ memarg) \ \hookrightarrow \ S; F; \mathsf{trap}\ (\mathsf{otherwise})
```

v128.storeN lane memarg x

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the *memory address* F.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 7. Pop the value v128.const c from the stack.

- 8. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 9. Pop the value i32.const i from the stack.
- 10. Let ea be the integer i + memarg.offset.
- 11. If ea + N/8 is larger than the length of mem.data, then:
 - a. Trap.
- 12. Let L be 128/N.
- 13. Let b^* be the byte sequence bytes_{iN}(lanes_{iN×L}(c)[x]).
- 14. Replace the bytes mem.data[ea: N/8] with b^* .

```
S; F; (\mathsf{i32.const}\ i)\ (\mathsf{v128.const}\ c)\ (\mathsf{v128.store}N\_\mathsf{lane}\ memarg\ x) \ \hookrightarrow \ S'; F; \epsilon \\ (\mathsf{if}\ ea = i + memarg.\mathsf{offset} \\ \land \ ea + N \le |S.\mathsf{mems}[F.\mathsf{module.memaddrs}[0]].\mathsf{data}| \\ \land \ L = 128/N \\ \land \ S' = S\ \mathsf{with}\ \mathsf{mems}[F.\mathsf{module.memaddrs}[0]].\mathsf{data}[ea : N/8] = \mathsf{bytes}_{iN}(\mathsf{lanes}_{\mathsf{i}N\times L}(c)[x])) \\ S; F; (\mathsf{i32.const}\ k)\ (\mathsf{v128.const}\ c)\ (\mathsf{v128.store}N\_\mathsf{lane}\ memarg\ x) \ \hookrightarrow \ S; F; \mathsf{trap}\ (\mathsf{otherwise})
```

memory.size

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the *memory address* F.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Let sz be the length of mem.data divided by the page size.
- 7. Push the value i32.const sz to the stack.

```
\begin{array}{ll} S; F; \mathsf{memory.size} & \hookrightarrow & S; F; (\mathsf{i32.const}\ sz) \\ & (\mathsf{if}\ |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{memaddrs}[0]].\mathsf{data}| = sz \cdot 64\,\mathrm{Ki}) \end{array}
```

memory.grow

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let a be the *memory address F*.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Let sz be the length of S.mems[a] divided by the page size.
- 7. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 8. Pop the value i32.const n from the stack.
- 9. Let err be the i32 value $2^{32} 1$, for which signed₃₂(err) is -1.
- 10. Either, try growing mem by n pages:
- a. If it succeeds, push the value i32.const sz to the stack.
- b. Else, push the value i32.const err to the stack.

11. Or, push the value i32.const err to the stack.

```
\begin{split} S; F; & (\mathsf{i32.const}\ n)\ \mathsf{memory.grow} &\hookrightarrow S'; F; (\mathsf{i32.const}\ sz) \\ & (\mathsf{if}\ F.\mathsf{module.memaddrs}[0] = a \\ & \land sz = |S.\mathsf{mems}[a].\mathsf{data}|/64\,\mathsf{Ki} \\ & \land S' = S\ \mathsf{with}\ \mathsf{mems}[a] = \mathsf{growmem}(S.\mathsf{mems}[a], n)) \\ S; F; & (\mathsf{i32.const}\ n)\ \mathsf{memory.grow} &\hookrightarrow S; F; (\mathsf{i32.const}\ \mathsf{signed}_{32}^{-1}(-1)) \end{split}
```

Note: The memory.grow instruction is non-deterministic. It may either succeed, returning the old memory size sz, or fail, returning -1. Failure *must* occur if the referenced memory instance has a maximum size defined that would be exceeded. However, failure *can* occur in other cases as well. In practice, the choice depends on the *resources* available to the *embedder*.

memory.fill

- 1. Let *F* be the *current frame*.
- 2. Assert: due to validation, F.module.memaddrs[0] exists.
- 3. Let *ma* be the *memory address F*.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[ma] exists.
- 5. Let mem be the memory instance S.mems[ma].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const n from the stack.
- 8. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 9. Pop the value *val* from the stack.
- 10. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 11. Pop the value i32.const d from the stack.
- 12. If d + n is larger than the length of mem.data, then:
 - a. Trap.
- 13. If n = 0, then:
 - a. Return.
- 14. Push the value i32.const d to the stack.
- 15. Push the value *val* to the stack.
- 16. Execute the instruction i32.store8 {offset 0, align 0}.
- 17. Assert: due to the earlier check against the memory size, $d + 1 < 2^{32}$.
- 18. Push the value i32.const (d+1) to the stack.
- 19. Push the value *val* to the stack.
- 20. Push the value i32.const (n-1) to the stack.
- 21. Execute the instruction memory.fill.

```
\begin{split} S; F; & \text{ (i32.const } d) \text{ } val \text{ (i32.const } n) \text{ memory.fill } &\hookrightarrow S; F; \text{ trap } \\ & \text{ (if } d+n > |S.\text{mems}[F.\text{module.memaddrs}[x]].\text{data}|) \\ S; F; & \text{ (i32.const } d) \text{ } val \text{ (i32.const } 0) \text{ memory.fill } &\hookrightarrow S; F; \epsilon \\ & \text{ (otherwise)} \\ S; F; & \text{ (i32.const } d) \text{ } val \text{ (i32.const } n+1) \text{ memory.fill } &\hookrightarrow S; F; \text{ (i32.const } d) \text{ } val \text{ (i32.store8 } \{\text{offset } 0, \text{align } 0\}) \\ & \text{ (i32.const } d+1) \text{ } val \text{ (i32.const } n) \text{ memory.fill } \\ & \text{ (otherwise)} \end{split}
```

memory.copy

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, *F*.module.memaddrs[0] exists.
- 3. Let ma be the memory address F.module.memaddrs[0].
- 4. Assert: due to *validation*, S.mems[ma] exists.
- 5. Let mem be the memory instance S.mems[ma].
- 6. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 7. Pop the value i32.const n from the stack.
- 8. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 9. Pop the value i32.const s from the stack.
- 10. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 11. Pop the value i32.const d from the stack.
- 12. If s + n is larger than the length of mem.data or d + n is larger than the length of mem.data, then:
 - a. Trap.
- 13. If n = 0, then:
- a. Return.
- 14. If $d \le s$, then:
- a. Push the value i32.const d to the stack.
- b. Push the value i32.const s to the stack.
- c. Execute the instruction i32.load8_u {offset 0, align 0}.
- d. Execute the instruction i32.store8 {offset 0, align 0}.
- e. Assert: due to the earlier check against the memory size, $d+1 < 2^{32}$.
- f. Push the value i32.const (d+1) to the stack.
- g. Assert: due to the earlier check against the memory size, $s + 1 < 2^{32}$.
- h. Push the value i32.const (s+1) to the stack.
- 15. Else:
- a. Assert: due to the earlier check against the memory size, $d + n 1 < 2^{32}$.
- b. Push the value i32.const (d + n 1) to the stack.
- c. Assert: due to the earlier check against the memory size, $s + n 1 < 2^{32}$.
- d. Push the value i32.const (s + n 1) to the stack.
- e. Execute the instruction i32.load8_u {offset 0, align 0}.

- f. Execute the instruction i32.store8 {offset 0, align 0}.
- g. Push the value i32.const d to the stack.
- h. Push the value i32.const s to the stack.
- 16. Push the value i32.const (n-1) to the stack.
- 17. Execute the instruction memory.copy.

```
S; F; (i32.const d) (i32.const s) (i32.const n) memory.copy
                                                                      S; F; \mathsf{trap}
     (if s + n > |S.mems[F.module.memaddrs[0]].data|
      \lor d + n > |S.mems[F.module.memaddrs[0]].data|)
S; F; (i32.const d) (i32.const s) (i32.const s) memory.copy
                                                                      S; F; \epsilon
     (otherwise)
S; F; (i32.const d) (i32.const s) (i32.const n+1) memory.copy
     S; F; (i32.const d)
           (i32.const s) (i32.load8_u \{offset 0, align 0\})
           (i32.store8 \{offset 0, align 0\})
           (i32.const d+1) (i32.const s+1) (i32.const n) memory.copy
     (otherwise, if d \leq s)
S; F; (i32.const d) (i32.const s) (i32.const n+1) memory.copy
     S; F; (i32.const d + n - 1)
           (i32.const s + n - 1) (i32.load8_u {offset 0, align 0})
           (i32.store8 \{offset 0, align 0\})
           (i32.const d) (i32.const s) (i32.const n) memory.copy
     (otherwise, if d > s)
```

memory.init x

- 1. Let F be the *current frame*.
- 2. Assert: due to validation, F.module.memaddrs[0] exists.
- 3. Let ma be the memory address F.module.memaddrs[0].
- 4. Assert: due to validation, S.mems[ma] exists.
- 5. Let mem be the memory instance S.mems[ma].
- 6. Assert: due to validation, F.module.dataaddrs[x] exists.
- 7. Let da be the data address F.module.dataaddrs[x].
- 8. Assert: due to validation, S.datas[da] exists.
- 9. Let data be the data instance S.datas[da].
- 10. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 11. Pop the value i32.const n from the stack.
- 12. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 13. Pop the value i32.const s from the stack.
- 14. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 15. Pop the value i32.const d from the stack.
- 16. If s + n is larger than the length of data.data or d + n is larger than the length of mem.data, then:
 - a. Trap.
- 17. If n = 0, then:
 - a. Return.

- 18. Let b be the byte data.data[s].
- 19. Push the value i32.const d to the stack.
- 20. Push the value i32.const *b* to the stack.
- 21. Execute the instruction i32.store8 {offset 0, align 0}.
- 22. Assert: due to the earlier check against the memory size, $d+1 < 2^{32}$.
- 23. Push the value i32.const (d+1) to the stack.
- 24. Assert: due to the earlier check against the memory size, $s + 1 < 2^{32}$.
- 25. Push the value i32.const (s+1) to the stack.
- 26. Push the value i32.const (n-1) to the stack.
- 27. Execute the instruction memory init x.

```
S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ n)\ (\mathsf{memory.init}\ x) \quad \hookrightarrow \quad S; F; \mathsf{trap} \\ (\mathsf{if}\ s+n>|S.\mathsf{datas}[F.\mathsf{module.dataaddrs}[x]].\mathsf{data}| \\ \lor d+n>|S.\mathsf{mems}[F.\mathsf{module.memaddrs}[x]].\mathsf{data}|) \\ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ 0)\ (\mathsf{memory.init}\ x) \quad \hookrightarrow \quad S; F; \epsilon \\ (\mathsf{otherwise}) \\ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ s)\ (\mathsf{i}32.\mathsf{const}\ n+1)\ (\mathsf{memory.init}\ x) \quad \hookrightarrow \\ S; F; (\mathsf{i}32.\mathsf{const}\ d)\ (\mathsf{i}32.\mathsf{const}\ b)\ (\mathsf{i}32.\mathsf{store8}\ \{\mathsf{offset}\ 0, \mathsf{align}\ 0\}) \\ (\mathsf{i}32.\mathsf{const}\ d+1)\ (\mathsf{i}32.\mathsf{const}\ s+1)\ (\mathsf{i}32.\mathsf{const}\ n)\ (\mathsf{memory.init}\ x) \\ (\mathsf{otherwise}, \mathsf{if}\ b=S.\mathsf{datas}[F.\mathsf{module.dataaddrs}[x]].\mathsf{data}[s]) \\ \end{cases}
```

data.drop x

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, F.module.dataaddrs[x] exists.
- 3. Let a be the *data address* F.module.dataaddrs[x].
- 4. Assert: due to *validation*, S.datas[a] exists.
- 5. Replace S.datas[a] with the data instance {data ϵ }.

```
S; F; (\mathsf{data.drop}\ x) \hookrightarrow S'; F; \epsilon
(if S' = S with \mathsf{datas}[F.\mathsf{module.dataaddrs}[x]] = {\mathsf{data}\ \epsilon})
```

4.4.8 Control Instructions

nop

1. Do nothing.

 $\mathsf{nop} \;\hookrightarrow\; \epsilon$

unreachable

1. Trap.

unreachable \hookrightarrow trap

block blocktype instr* end

- 1. Assert: due to *validation*, $expand_F(blocktype)$ is defined.
- 2. Let $[t_1^m] \to [t_2^n]$ be the function type expand_F (blocktype).
- 3. Let L be the label whose arity is n and whose continuation is the end of the block.
- 4. Assert: due to validation, there are at least m values on the top of the stack.
- 5. Pop the values val^m from the stack.
- 6. Enter the block val^m $instr^*$ with label L.

$$F; val^m ext{ block } bt ext{ } instr^* ext{ end } \hookrightarrow F; ext{label}_n\{\epsilon\} ext{ } val^m ext{ } instr^* ext{ end } ext{ } (ext{if } \operatorname{expand}_F(bt) = [t_1^m] \to [t_2^n])$$

loop blocktype instr* end

- 1. Assert: due to *validation*, $expand_F(blocktype)$ is defined.
- 2. Let $[t_1^m] \to [t_2^n]$ be the function type expand F(blocktype).
- 3. Let L be the label whose arity is m and whose continuation is the start of the loop.
- 4. Assert: due to *validation*, there are at least m values on the top of the stack.
- 5. Pop the values val^m from the stack.
- 6. Enter the block val^m $instr^*$ with label L.

```
F; val^m \text{ loop } bt \; instr^* \; \text{end} \; \hookrightarrow \; F; \text{label}_m \{ \text{loop } bt \; instr^* \; \text{end} \} \; val^m \; instr^* \; \text{end}  (if \exp \operatorname{and}_F(bt) = [t_1^m] \to [t_2^n] )
```

if $blocktype \ instr_1^*$ else $instr_2^*$ end

- 1. Assert: due to *validation*, $expand_F(blocktype)$ is defined.
- 2. Let $[t_1^m] \to [t_2^n]$ be the function type expand_F (blocktype).
- 3. Let L be the label whose arity is n and whose continuation is the end of the if instruction.
- 4. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 5. Pop the value i32.const c from the stack.
- 6. Assert: due to *validation*, there are at least m values on the top of the stack.
- 7. Pop the values val^m from the stack.
- 8. If c is non-zero, then:
 - a. Enter the block val^m $instr_1^*$ with label L.
- 9. Else:
 - a. Enter the block val^m $instr_2^*$ with label L.

$\mathsf{br}\ l$

- 1. Assert: due to *validation*, the stack contains at least l+1 labels.
- 2. Let L be the l-th label appearing on the stack, starting from the top and counting from zero.
- 3. Let n be the arity of L.
- 4. Assert: due to *validation*, there are at least n values on the top of the stack.
- 5. Pop the values val^n from the stack.
- 6. Repeat l+1 times:
 - a. While the top of the stack is a value, do:
 - i. Pop the value from the stack.
 - b. Assert: due to *validation*, the top of the stack now is a label.
 - c. Pop the label from the stack.
- 7. Push the values val^n to the stack.
- 8. Jump to the continuation of L.

$$label_n\{instr^*\}$$
 $B^l[val^n (br l)]$ end $\hookrightarrow val^n instr^*$

$\quad \text{br if } l$

- 1. Assert: due to *validation*, a value of *value type* i32 is on the top of the stack.
- 2. Pop the value i32.const c from the stack.
- 3. If c is non-zero, then:
 - a. *Execute* the instruction (br l).
- 4. Else:
 - a. Do nothing.

(i32.const
$$c$$
) (br_if l) \hookrightarrow (br l) (if $c \neq 0$) (i32.const c) (br_if l) \hookrightarrow ϵ (if $c = 0$)

$br_table l^* l_N$

- 1. Assert: due to validation, a value of value type i32 is on the top of the stack.
- 2. Pop the value i32.const i from the stack.
- 3. If i is smaller than the length of l^* , then:
 - a. Let l_i be the label $l^*[i]$.
 - b. *Execute* the instruction (br l_i).
- 4. Else:
 - a. *Execute* the instruction (br l_N).

```
(i32.const i) (br_table l^* l_N) \hookrightarrow (br l_i) (if l^*[i] = l_i) (i32.const i) (br_table l^* l_N) \hookrightarrow (br l_N) (if |l^*| \le i)
```

$br_on_null\ l$

- 1. Assert: due to *validation*, a *reference value* is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If val is ref.null ht, then:
 - a. Execute the instruction (br l).
- 4. Else:
 - a. Push the value val back to the stack.

```
\begin{array}{lll} \mathit{val}\; (\mathsf{br\_on\_null}\; l) & \hookrightarrow & (\mathsf{br}\; l) & (\mathsf{if}\; \mathit{val} = \mathsf{ref.null}\; \mathit{ht}) \\ \mathit{val}\; (\mathsf{br\_on\_null}\; l) & \hookrightarrow & \mathit{val} & (\mathsf{otherwise}) \end{array}
```

$br_on_non_null\ l$

- 1. Assert: due to validation, a reference value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If val is ref.null ht, then:
 - a. Do nothing.
- 4. Else:
 - a. Push the value val back to the stack.
 - b. *Execute* the instruction (br l).

```
val 	ext{ (br_on_non_null } l) \hookrightarrow \epsilon 	ext{ (if } val = \text{ref.null } ht)
val 	ext{ (br_on_non_null } l) \hookrightarrow val 	ext{ (br } l) 	ext{ (otherwise)}
```

return

- 1. Let *F* be the *current frame*.
- 2. Let n be the arity of F.
- 3. Assert: due to validation, there are at least n values on the top of the stack.
- 4. Pop the results val^n from the stack.
- 5. Assert: due to validation, the stack contains at least one frame.
- 6. While the top of the stack is not a frame, do:
 - a. Pop the top element from the stack.
- 7. Assert: the top of the stack is the frame F.
- 8. Pop the frame from the stack.
- 9. Push val^n to the stack.
- 10. Jump to the instruction after the original call that pushed the frame.

$$\mathsf{frame}_n\{F\}\ B^k[\mathit{val}^n\ \mathsf{return}]\ \mathsf{end}\ \hookrightarrow\ \mathit{val}^n$$

$\operatorname{call} x$

- 1. Let F be the current frame.
- 2. Assert: due to *validation*, F.module.funcaddrs[x] exists.
- 3. Let a be the function address F.module.funcaddrs[x].
- 4. *Invoke* the function instance at address a.

$$F$$
; (call x) \hookrightarrow F ; (invoke a) (if F .module.funcaddrs[x] = a)

call_ref

- 1. Assert: due to validation, a function reference is on the top of the stack.
- 2. Pop the value ref a from the stack.
- 3. *Invoke* the function instance at address a.

$$F$$
; (ref a) call_ref \hookrightarrow F ; (invoke a)

$\mathsf{call_indirect}\; x\; y$

- 1. Let *F* be the *current frame*.
- 2. Assert: due to *validation*, F.module.tableaddrs[x] exists.
- 3. Let ta be the table address F.module.tableaddrs[x].
- 4. Assert: due to *validation*, S.tables[ta] exists.
- 5. Let tab be the table instance S.tables [ta].
- 6. Assert: due to *validation*, F.module.types[y] exists.
- 7. Let ft_{expect} be the function type F.module.types[y].
- 8. Assert: due to validation, a value with value type i32 is on the top of the stack.
- 9. Pop the value i32.const i from the stack.
- 10. If i is not smaller than the length of tab.elem, then:
 - a. Trap.
- 11. Let r be the reference tab.elem[i].
- 12. If r is ref.null ht, then:
 - a. Trap.
- 13. Assert: due to validation of table mutation, r is a function reference.
- 14. Let ref a be the function reference r.
- 15. Assert: due to validation of table mutation, S.funcs[a] exists.
- 16. Let f be the function instance S.funcs[a].
- 17. Let ft_{actual} be the function type f.type.
- 18. If $ft_{
 m actual}$ and $ft_{
 m expect}$ differ, then:
 - a. Trap.
- 19. *Invoke* the function instance at address a.

```
\begin{array}{lll} S; F; (\mathsf{i32.const}\ i)\ (\mathsf{call\_indirect}\ x\ y) &\hookrightarrow & S; F; (\mathsf{invoke}\ a) \\ & (\mathsf{if}\ S.\mathsf{tables}[F.\mathsf{module.tableaddrs}[x]].\mathsf{elem}[i] = \mathsf{ref}\ a \\ & \land S.\mathsf{funcs}[a] = f \\ & \land F.\mathsf{module.types}[y] = f.\mathsf{type}) \\ S; F; (\mathsf{i32.const}\ i)\ (\mathsf{call\_indirect}\ x\ y) &\hookrightarrow & S; F; \mathsf{trap}\ (\mathsf{otherwise}) \end{array}
```

4.4.9 Blocks

The following auxiliary rules define the semantics of executing an instruction sequence that forms a block.

Entering $instr^*$ with label L

- 1. Push L to the stack.
- 2. Jump to the start of the instruction sequence $instr^*$.

Note: No formal reduction rule is needed for entering an instruction sequence, because the label L is embedded in the *administrative instruction* that structured control instructions reduce to directly.

Exiting $instr^*$ with label L

When the end of a block is reached without a jump or trap aborting it, then the following steps are performed.

- 1. Let m be the number of values on the top of the stack.
- 2. Pop the values val^m from the stack.
- 3. Assert: due to *validation*, the label L is now on the top of the stack.
- 4. Pop the label from the stack.
- 5. Push val^m back to the stack.
- 6. Jump to the position after the end of the *structured control instruction* associated with the label L.

```
label_n\{instr^*\}\ val^m\ end\ \hookrightarrow\ val^m
```

Note: This semantics also applies to the instruction sequence contained in a loop instruction. Therefore, execution of a loop falls off the end, unless a backwards branch is performed explicitly.

4.4.10 Function Calls

The following auxiliary rules define the semantics of invoking a *function instance* through one of the *call instructions* and returning from it.

Invocation of function address a

- 1. Assert: due to *validation*, S.funcs[a] exists.
- 2. Let f be the function instance, S.funcs[a].
- 3. Let $[t_1^n] \rightarrow [t_2^m]$ be the function type f.type.
- 4. Let $local^*$ be the list of locals f.code.locals.
- 5. Let $instr^*$ end be the expression f.code.body.
- 6. Assert: due to *validation*, n values are on the top of the stack.
- 7. Pop the values val^n from the stack.
- 8. Let F be the frame {module f.module, locals val^n (default_t)*}.
- 9. Push the activation of F with arity m to the stack.
- 10. Let L be the *label* whose arity is m and whose continuation is the end of the function.
- 11. *Enter* the instruction sequence $instr^*$ with label L.

```
\begin{split} S; val^n \text{ (invoke } a) &\hookrightarrow S; \text{frame}_m\{F\} \text{ label}_m\{\} \text{ } instr^* \text{ end end } \\ \text{ (if } S. \text{funcs}[a] &= f \\ &\land f. \text{type} = [t_1^n] \to [t_2^m] \\ &\land f. \text{code} = \{ \text{type } x, \text{locals } \{ \text{type } t \}^k, \text{body } instr^* \text{ end} \} \\ &\land F = \{ \text{module } f. \text{module, locals } val^n \text{ } (\text{default}_t)^k \} ) \end{split}
```

Note: For non-defaultable types, the respective local is left uninitialized by these rules.

Returning from a function

When the end of a function is reached without a jump (i.e., return) or trap aborting it, then the following steps are performed.

- 1. Let F be the current frame.
- 2. Let n be the arity of the activation of F.
- 3. Assert: due to validation, there are n values on the top of the stack.
- 4. Pop the results val^n from the stack.
- 5. Assert: due to *validation*, the frame F is now on the top of the stack.
- 6. Pop the frame from the stack.
- 7. Push val^n back to the stack.
- 8. Jump to the instruction after the original call.

$$frame_n\{F\} \ val^n \ end \ \hookrightarrow \ val^n$$

Host Functions

Invoking a *host function* has non-deterministic behavior. It may either terminate with a *trap* or return regularly. However, in the latter case, it must consume and produce the right number and types of WebAssembly *values* on the stack, according to its *function type*.

A host function may also modify the *store*. However, all store modifications must result in an *extension* of the original store, i.e., they must only modify mutable contents and must not have instances removed. Furthermore, the resulting store must be *valid*, i.e., all data and code in it is well-typed.

```
\begin{split} S; val^n \; &(\mathsf{invoke} \; a) \; \hookrightarrow \; S'; result \\ &(\mathsf{if} \; S.\mathsf{funcs}[a] = \{\mathsf{type} \; [t_1^n] \to [t_2^m], \mathsf{hostcode} \; hf\} \\ &\wedge (S'; result) \in hf(S; val^n)) \\ S; val^n \; &(\mathsf{invoke} \; a) \; \hookrightarrow \; S; val^n \; &(\mathsf{invoke} \; a) \\ &(\mathsf{if} \; S.\mathsf{funcs}[a] = \{\mathsf{type} \; [t_1^n] \to [t_2^m], \mathsf{hostcode} \; hf\} \\ &\wedge \bot \in hf(S; val^n)) \end{split}
```

Here, $hf(S; val^n)$ denotes the implementation-defined execution of host function hf in current store S with arguments val^n . It yields a set of possible outcomes, where each element is either a pair of a modified store S' and a *result* or the special value \bot indicating divergence. A host function is non-deterministic if there is at least one argument for which the set of outcomes is not singular.

For a WebAssembly implementation to be *sound* in the presence of host functions, every *host function instance* must be *valid*, which means that it adheres to suitable pre- and post-conditions: under a *valid store* S, and given arguments val^n matching the ascribed parameter types t_1^n , executing the host function must yield a non-empty set of possible outcomes each of which is either divergence or consists of a valid store S' that is an *extension* of S and a result matching the ascribed return types t_2^m . All these notions are made precise in the *Appendix*.

Note: A host function can call back into WebAssembly by *invoking* a function *exported* from a *module*. However, the effects of any such call are subsumed by the non-deterministic behavior allowed for the host function.

4.4.11 Expressions

An expression is evaluated relative to a current frame pointing to its containing module instance.

- 1. Jump to the start of the instruction sequence $instr^*$ of the expression.
- 2. Execute the instruction sequence.
- 3. Assert: due to validation, the top of the stack contains a value.
- 4. Pop the *value val* from the stack.

The value val is the result of the evaluation.

```
S; F; instr^* \hookrightarrow S'; F'; instr'^* (if S; F; instr^* end \hookrightarrow S'; F'; instr'^* end)
```

Note: Evaluation iterates this reduction rule until reaching a value. Expressions constituting *function* bodies are executed during function *invocation*.

4.5 Modules

For modules, the execution semantics primarily defines *instantiation*, which *allocates* instances for a module and its contained definitions, initializes *tables* and *memories* from contained *element* and *data* segments, and invokes the *start function* if present. It also includes *invocation* of exported functions.

Instantiation depends on a number of auxiliary notions for type-checking imports and allocating instances.

4.5.1 External Typing

For the purpose of checking *external values* against *imports*, such values are classified by *external types*. The following auxiliary typing rules specify this typing relation relative to a *store* S in which the referenced instances live.

$\mathsf{func}\; a$

- The store entry $S.\mathsf{funcs}[a]$ must exist.
- Then func a is valid with external type func S.funcs[a].type.

$$\overline{S \vdash \mathsf{func}\ a : \mathsf{func}\ S.\mathsf{funcs}[a].\mathsf{type}}$$

$\mathsf{table}\; a$

- The store entry S.tables[a] must exist.
- Then table a is valid with external type table S.tables[a].type.

$$\overline{S} \vdash \mathsf{table} \ a : \mathsf{table} \ S. \mathsf{tables}[a]. \mathsf{type}$$

mem a

- The store entry S.mems[a] must exist.
- Then mem a is valid with external type mem S.mems[a].type.

$$S \vdash \mathsf{mem}\ a : \mathsf{mem}\ S.\mathsf{mems}[a].\mathsf{type}$$

$\operatorname{\mathsf{global}} a$

- The store entry S.globals[a] must exist.
- Then global a is valid with external type global S.globals[a].type.

$$\overline{S \vdash \mathsf{global}\ a : \mathsf{global}\ S.\mathsf{globals}[a].\mathsf{type}}$$

4.5.2 Value Typing

For the purpose of checking argument *values* against the parameter types of exported *functions*, values are classified by *value types*. The following auxiliary typing rules specify this typing relation relative to a *store* S in which possibly referenced addresses live.

Numeric Values t.const c

• The value is valid with number type t.

 $\overline{S \vdash t.\mathsf{const}\ c:t}$

Null References ref.null t

• The value is valid with reference type t.

 $\overline{S \vdash \mathsf{ref.null}\ t : t}$

Function References ref a

- The external value func a must be valid.
- Then the value is valid with reference type funcref.

 $\frac{S \vdash \mathsf{func}\ a : \mathsf{func}\ \mathit{functype}}{S \vdash \mathsf{ref}\ a : \mathsf{funcref}}$

External References ref.extern a

• The value is valid with reference type externref.

 $\overline{S \vdash \mathsf{ref.extern}\ a : \mathsf{externref}}$

4.5.3 Allocation

New instances of *functions*, *tables*, *memories*, and *globals* are *allocated* in a *store* S, as defined by the following auxiliary functions.

Functions

- 1. Let func be the function to allocate and module instance.
- 2. Let a be the first free function address in S.
- 3. Let functype be the function type moduleinst.types[func.type].
- 4. Let funcinst be the function instance {type functype, module moduleinst, code func}.
- 5. Append funcinst to the funcs of S.
- 6. Return a.

4.5. Modules 131

Host Functions

- 1. Let hostfunc be the host function to allocate and functype its function type.
- 2. Let a be the first free function address in S.
- 3. Let funcinst be the function instance {type functype, hostcode hostfunc}.
- 4. Append funcinst to the funcs of S.
- 5. Return a.

```
allochostfunc(S, functype, hostfunc) = S', funcaddr

where:
funcaddr = |S. funcs|
funcinst = \{type functype, hostcode hostfunc\}
S' = S \oplus \{funcs funcinst\}
```

Note: Host functions are never allocated by the WebAssembly semantics itself, but may be allocated by the *embedder*.

Tables

- 1. Let *tabletype* be the *table type* to allocate and *ref* the initialization value.
- 2. Let $(\{\min n, \max m^?\} \text{ reftype})$ be the structure of table type tabletype.
- 3. Let a be the first free *table address* in S.
- 4. Let table instance $\{\text{type } table type, \text{elem } ref^n\}$ with n elements set to ref.
- 5. Append tableinst to the tables of S.
- 6. Return a.

```
alloctable(S, tabletype, ref) = S', tableaddr

where:
tabletype = \{\min n, \max m^?\} reftype
tableaddr = |S.tables|
tableinst = \{type \ tabletype, elem \ ref^n\}
S' = S \oplus \{tables \ tableinst\}
```

Memories

- 1. Let *memtype* be the *memory type* to allocate.
- 2. Let $\{\min n, \max m^2\}$ be the structure of memory type memtype.
- 3. Let a be the first free *memory address* in S.
- 4. Let *meminst* be the *memory instance* {type memtype, data $(0x00)^{n\cdot64\,\mathrm{Ki}}$ } that contains n pages of zeroed *bytes*.
- 5. Append meminst to the mems of S.
- 6. Return a.

```
\begin{array}{rcl} \operatorname{allocmem}(S, memtype) & = & S', memaddr \\ & & \operatorname{where:} \\ & memtype & = & \{\min n, \max m^?\} \\ & memaddr & = & |S.\operatorname{mems}| \\ & meminst & = & \{\operatorname{type} \ memtype, \operatorname{data} \ (\operatorname{0x00})^{n\cdot 64 \operatorname{Ki}}\} \\ & S' & = & S \oplus \{\operatorname{mems} \ meminst\} \end{array}
```

Globals

- 1. Let *globaltype* be the *global type* to allocate and *val* the *value* to initialize the global with.
- 2. Let a be the first free global address in S.
- 3. Let *globalinst* be the *global instance* {type *globaltype*, value *val*}.
- 4. Append globalinst to the globals of S.
- 5. Return a.

```
\begin{array}{rcl} \operatorname{allocglobal}(S, \operatorname{globaltype}, \operatorname{val}) &=& S', \operatorname{globaladdr} \\ & \operatorname{where:} \\ & \operatorname{globaladdr} &=& |S.\operatorname{globals}| \\ & \operatorname{globalinst} &=& \{\operatorname{type} \operatorname{globaltype}, \operatorname{value} \operatorname{val}\} \\ & S' &=& S \oplus \{\operatorname{globals} \operatorname{globalinst}\} \end{array}
```

Element segments

- 1. Let reftype be the elements' type and ref^* the vector of references to allocate.
- 2. Let a be the first free *element address* in S.
- 3. Let *eleminst* be the *element instance* {type t, elem ref^* }.
- 4. Append *eleminst* to the elems of S.
- 5. Return a.

```
\begin{array}{rcl} \text{allocelem}(S,\textit{reftype},\textit{ref*}) & = & S',\textit{elemaddr} \\ & & \text{where:} \\ & \textit{elemaddr} & = & |S.\text{elems}| \\ & \textit{eleminst} & = & \{\text{type}\;\textit{reftype},\text{elem}\;\textit{ref*}\} \\ & S' & = & S \oplus \{\text{elems}\;\textit{eleminst}\} \end{array}
```

4.5. Modules 133

Data segments

- 1. Let bytes be the vector of *bytes* to allocate.
- 2. Let a be the first free data address in S.
- 3. Let *datainst* be the *data instance* {data bytes}.
- 4. Append datainst to the datas of S.
- 5. Return a.

```
allocdata(S, bytes) = S', dataaddr

where:
dataaddr = |S.datas|
datainst = \{data bytes\}
S' = S \oplus \{datas datainst\}
```

Growing tables

- 1. Let tableinst be the table instance to grow, n the number of elements by which to grow it, and ref the initialization value.
- 2. Let len be n added to the length of tableinst.elem.
- 3. If len is larger than or equal to 2^{32} , then fail.
- 4. Let $limits\ t$ be the structure of $table\ type\ tableinst$.type.
- 5. Let *limits'* be *limits* with min updated to *len*.
- 6. If *limits'* is not *valid*, then fail.
- 7. Append ref^n to tableinst.elem.
- 8. Set tableinst.type to the $table type \ limits' \ t.$

```
growtable(tableinst, n, ref) = tableinst with type = limits' t with elem = tableinst.elem ref^n (if len = n + |tableinst.elem| \land len < 2^{32} \land limits \ t = tableinst.type \land limits' = limits with min = len \land \vdash limits' ok)
```

Growing memories

- 1. Let meminst be the memory instance to grow and n the number of pages by which to grow it.
- 2. Assert: The length of meminst.data is divisible by the page size 64 Ki.
- 3. Let *len* be *n* added to the length of *meminst*.data divided by the *page size* 64 Ki.
- 4. If len is larger than 2^{16} , then fail.
- 5. Let *limits* be the structure of *memory type meminst*.type.
- 6. Let *limits'* be *limits* with min updated to *len*.
- 7. If *limits'* is not *valid*, then fail.
- 8. Append n times $64 \,\mathrm{Ki}\ bytes$ with value 0x00 to meminst.data.
- 9. Set *meminst*.type to the *memory type limits'*.

Modules

The allocation function for *modules* requires a suitable list of *external values* that are assumed to *match* the *import* vector of the module, a list of initialization *values* for the module's *globals*, and list of *reference* vectors for the module's *element segments*.

- 1. Let *module* be the *module* to allocate and *externval** the vector of *external values* providing the module's imports, *val** the initialization *values* of the module's *globals*, and $(ref^*)^*$ the *reference* vectors of the module's *element segments*.
- 2. For each function $func_i$ in module.funcs, do:
 - a. Let $funcaddr_i$ be the function address resulting from allocating $func_i$ for the module instance module inst defined below.
- 3. For each $table\ table_i$ in module.tables, do:
 - a. Let $limits_i$ t_i be the table type $table_i$.type.
 - b. Let $tableaddr_i$ be the table address resulting from allocating $table_i$.type with initialization value ref.null t_i .
- 4. For each *memory* mem_i in module.mems, do:
 - a. Let $memaddr_i$ be the memory address resulting from allocating mem_i type.
- 5. For each global global in module globals, do:
 - a. Let $globaladdr_i$ be the global address resulting from allocating $global_i$.type with initializer value $val^*[i]$.
- 6. For each element segment $elem_i$ in module.elems, do:
 - a. Let $elemaddr_i$ be the element address resulting from allocating an element instance of reference type $elem_i$. type with contents $(ref^*)^*[i]$.
- 7. For each data segment $data_i$ in module.datas, do:
 - a. Let $dataaddr_i$ be the data address resulting from allocating a data instance with contents $data_i$.init.
- 8. Let $funcaddr^*$ be the concatenation of the function addresses $funcaddr_i$ in index order.
- 9. Let $tableaddr^*$ be the concatenation of the table addresses $tableaddr_i$ in index order.
- 10. Let $memaddr^*$ be the concatenation of the *memory addresses* $memaddr_i$ in index order.
- 11. Let $globaladdr^*$ be the concatenation of the global addresses $globaladdr_i$ in index order.
- 12. Let $elemaddr^*$ be the concatenation of the $element\ addresses\ elemaddr_i$ in index order.
- 13. Let $dataaddr^*$ be the concatenation of the data addresses $dataaddr_i$ in index order.
- 14. Let $funcaddr_{mod}^*$ be the list of $function\ addresses$ extracted from $externval_{im}^*$, concatenated with $funcaddr^*$.
- 15. Let $tableaddr_{mod}^*$ be the list of table addresses extracted from $externval_{im}^*$, concatenated with $tableaddr^*$.
- 16. Let $memaddr_{mod}^*$ be the list of memory addresses extracted from $externval_{im}^*$, concatenated with $memaddr^*$.
- 17. Let $globaladdr^*_{mod}$ be the list of global addresses extracted from $externval^*_{im}$, concatenated with $globaladdr^*$.

4.5. Modules 135

- 18. For each export export, in module exports, do:
 - a. If $export_i$ is a function export for function index x, then let $externval_i$ be the external value func $(funcaddr_{mod}^*[x])$.
 - b. Else, if $export_i$ is a table export for table index x, then let $externval_i$ be the external value table $(tableaddr^*_{mod}[x])$.
 - c. Else, if $export_i$ is a memory export for memory index x, then let $externval_i$ be the external value $mem (memaddr^*_{mod}[x])$.
 - d. Else, if $export_i$ is a global export for global index x, then let $externval_i$ be the external value global $(globaladdr_{mod}^*[x])$.
 - e. Let $exportinst_i$ be the export instance {name ($export_i$.name), value $externval_i$ }.
- 19. Let exportinst* be the concatenation of the export instances exportinst_i in index order.
- 20. Let module inst be the module instance {types (module.types), funcaddrs $funcaddr^*_{mod}$, tableaddrs $tableaddr^*_{mod}$, memaddrs $memaddr^*_{mod}$, globaladdrs $globaladdr^*_{mod}$, exports $exportinst^*$ }.
- 21. Return moduleinst.

 $allocmodule(S, module, externval_{im}^*, val^*, (ref^*)^*) = S', module inst$

where:

```
table^*
                           = module.tables
                 mem^* = module.mems
                global^* = module.globals
                 elem^* = module.elems
                 data^* = module.datas
               export^* = module.exports
           moduleinst = \{ \text{ types } module. \text{types}, \}
                                   funcaddrs funcs(externval_{im}^*) funcaddr^*,
                                   tableaddrs tables (externval_{im}^*) tableaddr^*,
                                   memaddrs mems(externval_{im}^*) memaddr^*,
                                   globaladdrs globals (externval_{im}^*) globaladdr*,
                                   elemaddrs elemaddr^*,
                                   dataaddrs dataaddr^*
                                   exports exportinst^* }
       S_1, funcaddr^* = allocfunc^*(S, module.funcs, moduleinst)
       S_2, tableaddr^* = alloctable^*(S_1, (table.type)^*, (ref.null <math>t)^*) (where (table.type)^* = (limits t)^*)
      S_3, memaddr^* = allocmem^*(S_2, (mem.type)^*)
      S_4, globaladdr^* = allocglobal^*(S_3, (global.type)^*, val^*)
       S_5, elemaddr^* = allocelem^*(S_4, (elem.type)^*, (ref^*)^*)

S', dataaddr^* = allocelem^*(S_5, (data.init)^*)
          exportinst^* = \{name (export.name), value externval_{ex}\}^*
\begin{array}{lll} \mathrm{funcs}(externval_{\mathrm{ex}}^*) & = & (moduleinst.\mathrm{funcaddrs}[x])^* \\ \mathrm{tables}(externval_{\mathrm{ex}}^*) & = & (moduleinst.\mathrm{tableaddrs}[x])^* \end{array}
                                                                        (where x^* = \text{funcs}(export^*))
                                                                        (where x^* = \text{tables}(export^*))
 mems(externval_{ex}^*) = (moduleinst.memaddrs[x])^*
                                                                        (where x^* = mems(export^*))
globals(externval_{ex}^*) = (moduleinst.globaladdrs[x])^*
                                                                        (where x^* = globals(export^*))
```

Here, the notation allocx* is shorthand for multiple *allocations* of object kind X, defined as follows:

```
\begin{aligned} \text{allocx}^*(S_0, X^n, \dots) &= S_n, a^n \\ \text{where for all } i < n : \\ S_{i+1}, a^n[i] &= \text{allocx}(S_i, X^n[i], \dots) \end{aligned}
```

Moreover, if the dots \dots are a sequence A^n (as for globals or tables), then the elements of this sequence are passed to the allocation function pointwise.

Note: The definition of module allocation is mutually recursive with the allocation of its associated functions, because the resulting module instance *moduleinst* is passed to the function allocator as an argument, in order to form the necessary closures. In an implementation, this recursion is easily unraveled by mutating one or the other in a secondary step.

4.5.4 Instantiation

Given a store S, a module module is instantiated with a list of external values externvalⁿ supplying the required imports as follows.

Instantiation checks that the module is *valid* and the provided imports *match* the declared types, and may *fail* with an error otherwise. Instantiation can also result in a *trap* from executing the start function. It is up to the *embedder* to define how such conditions are reported.

- 1. If module is not valid, then:
 - a. Fail.
- 2. Assert: module is valid with external types $externtype^m_{im}$ classifying its imports.
- 3. If the number m of *imports* is not equal to the number n of provided *external values*, then:
 - a. Fail.
- 4. For each external value externval_i in externvalⁿ and external type externtype'_i in externtype'_{im}, do:
 - a. If $externval_i$ is not valid with an external type $externtype_i$ in store S, then:
 - i. Fail.
 - b. If $externtype_i$ does not match $externtype'_i$, then:
 - i. Fail.
- 5. Let $module inst_{init}$ be the auxiliary module instance {globaladdrs globals($externval^n$), funcaddrs module inst.funcaddrs} that only consists of the imported globals and the imported and allocated functions from the final module instance module inst, defined below.
- 6. Let F_{init} be the auxiliary frame {module module inst_{init}, locals ϵ }.
- 7. Push the frame $F_{\rm init}$ to the stack.
- 8. Let val^* be the vector of global initialization values determined by module and $externval^n$. These may be calculated as follows.
 - a. For each global global in module globals, do:
 - i. Let val_i be the result of evaluating the initializer expression $global_i$.init.
 - b. Assert: due to *validation*, the frame F_{init} is now on the top of the stack.
 - c. Let val^* be the concatenation of val_i in index order.
- 9. Let $(ref^*)^*$ be the list of *reference* vectors determined by the *element segments* in *module*. These may be calculated as follows.
 - a. For each element segment elem_i in module.elems, and for each element $expression \ expr_{ij}$ in $elem_i$.init, do:
 - i. Let ref_{ij} be the result of evaluating the initializer expression $expr_{ij}$.
 - b. Let ref_i^* be the concatenation of function elements ref_{ij} in order of index j.
 - c. Let $(ref^*)^*$ be the concatenation of function element vectors ref_i^* in order of index i.
- 10. Pop the frame $F_{\rm init}$ from the stack.

4.5. Modules 137

- 11. Let module inst be a new module instance allocated from module in store S with imports $externval^n$, global initializer values val^* , and element segment contents $(ref^*)^*$, and let S' be the extended store produced by module allocation.
- 12. Let F be the auxiliary frame {module module inst, locals ϵ }.
- 13. Push the frame F to the stack.
- 14. For each *element segment elem_i* in *module*.elems whose *mode* is of the form active {table $tableidx_i$, offset $einstr_i^*$ end}, do:
 - a. Let n be the length of the vector $elem_i$.init.
 - b. *Execute* the instruction sequence $einstr_i^*$.
 - c. *Execute* the instruction i32.const 0.
 - d. Execute the instruction i32.const n.
 - e. Execute the instruction table.init $tableidx_i$ i.
 - f. Execute the instruction elem.drop i.
- 15. For each data segment $data_i$ in module.datas whose mode is of the form $active \{memory \ memidx_i, offset \ dinstr_i^* \ end\}, do:$
 - a. Assert: $memidx_i$ is 0.
 - b. Let n be the length of the vector $data_i$.init.
 - c. *Execute* the instruction sequence $dinstr_i^*$.
 - d. *Execute* the instruction i32.const 0.
 - e. Execute the instruction i32.const n.
 - f. Execute the instruction memory.init i.
 - g. Execute the instruction data.drop i.
- 16. If the *start function module*.start is not empty, then:
 - a. Let start be the start function module.start.
 - b. *Execute* the instruction call *start*.func.
- 17. Assert: due to *validation*, the frame F is now on the top of the stack.
- 18. Pop the frame F from the stack.

```
instantiate(S, module, externval^k)
                                                              S'; F; \text{runelem}_0(elem^n[0]) \dots \text{runelem}_{n-1}(elem^n[n-1])
                                                                       \operatorname{rundata}_0(\operatorname{data}^m[0]) \dots \operatorname{rundata}_{m-1}(\operatorname{data}^m[m-1])
                                                                       (call start.func)?
                                                              \vdash \mathit{module} : \mathit{externtype}_{im}^k \rightarrow \mathit{externtype}_{ex}^*
                                                              (S \vdash externval : externtype)^k
                                                              (\vdash externtype \leq externtype_{im})^k
                                                             module.globals = global^*
                                                             module.elems = elem^n
                                                             module.\mathsf{datas} = data^m
                                                             module.start = start?
                                                       Λ
                                                            (expr_{g} = global.init)^{*}
                                                       \wedge
                                                            (expr_{\mathbf{e}}^* = elem.\mathsf{init})^n
                                                              S', module inst = allocmodule (S, module, externval^k, val^*, (ref^*)^n)
                                                             F = \{ \text{module } module inst, \text{locals } \epsilon \}
                                                        \land \quad (S'; F; expr_{\mathbf{g}} \hookrightarrow {}^*S'; F; val \text{ end})^* \\ \land \quad ((S'; F; expr_{\mathbf{e}} \hookrightarrow {}^*S'; F; ref \text{ end})^*)^n 
                                                       \land (tableaddr = moduleinst.tableaddrs[elem.table])*
                                                             (memaddr = moduleinst.memaddrs[data.memory])^*
                                                              (funcaddr = moduleinst.funcaddrs[start.func])^{?})
where:
                        runelem<sub>i</sub>({type et, init ref^n, mode passive}) = \epsilon
                        runelem<sub>i</sub>({type et, init ref^n, mode active{table 0, offset instr^* end}})
                               instr^* (i32.const 0) (i32.const n) (table.init i) (elem.drop i)
                        runelem<sub>i</sub>({type et, init ref^n, mode declarative})
                               (elem.drop i)
                        \operatorname{rundata}_i(\{\operatorname{init} b^n, \operatorname{mode passive}\})
                        \operatorname{rundata}_{i}(\{\operatorname{init} b^{n}, \operatorname{mode active}\{\operatorname{memory} 0, \operatorname{offset} \operatorname{instr}^{*} \operatorname{end}\}\})
                               instr^* (i32.const 0) (i32.const n) (memory.init i) (data.drop i)
```

Note: Module *allocation* and the *evaluation* of *global* initializers and *element segments* are mutually recursive because the global initialization *values val** and element segment contents $(ref^*)^*$ are passed to the module allocator while depending on the module instance *moduleinst* and store S' returned by allocation. However, this recursion is just a specification device. In practice, the initialization values can *be determined* beforehand by staging module allocation such that first, the module's own *function instances* are pre-allocated in the store, then the initializer expressions are evaluated, then the rest of the module instance is allocated, and finally the new function instances' module fields are set to that module instance. This is possible because *validation* ensures that initialization expressions cannot actually call a function, only take their reference.

All failure conditions are checked before any observable mutation of the store takes place. Store mutation is not atomic; it happens in individual steps that may be interleaved with other threads.

Evaluation of constant expressions does not affect the store.

4.5.5 Invocation

Once a module has been instantiated, any exported function can be invoked externally via its function address funcaddr in the store S and an appropriate list val^* of argument values.

Invocation may *fail* with an error if the arguments do not fit the *function type*. Invocation can also result in a *trap*. It is up to the *embedder* to define how such conditions are reported.

Note: If the *embedder* API performs type checks itself, either statically or dynamically, before performing an invocation, then no failure other than traps can occur.

4.5. Modules 139

The following steps are performed:

- 1. Assert: S.funcs[funcaddr] exists.
- 2. Let funcinst be the function instance S.funcs[funcaddr].
- 3. Let $[t_1^n] \to [t_2^m]$ be the function type functinst.type.
- 4. If the length $|val^*|$ of the provided argument values is different from the number n of expected arguments, then:
 - a. Fail.
- 5. For each value type t_i in t_1^n and corresponding value val_i in val^* , do:
 - a. If val_i is not valid with value type t_i , then:
 - i. Fail.
- 6. Let F be the dummy frame $\{\text{module } \{\}, \text{locals } \epsilon\}$.
- 7. Push the frame F to the stack.
- 8. Push the values val^* to the stack.
- 9. *Invoke* the function instance at address *funcaddr*.

Once the function has returned, the following steps are executed:

- 1. Assert: due to *validation*, *m values* are on the top of the stack.
- 2. Pop val_{res}^m from the stack.

The values val_{res}^m are returned as the results of the invocation.

```
\begin{array}{lll} \operatorname{invoke}(S, \operatorname{funcaddr}, \operatorname{val}^n) & = & S; F; \operatorname{val}^n \text{ (invoke } \operatorname{funcaddr}) \\ & (\operatorname{if} & S.\operatorname{funcs}[\operatorname{funcaddr}].\operatorname{type} = [t_1^n] \to [t_2^m] \\ & \wedge & (S \vdash \operatorname{val}:t_1)^n \\ & \wedge & F = \{\operatorname{module}\,\{\},\operatorname{locals}\epsilon\}) \end{array}
```

Binary Format

5.1 Conventions

The binary format for WebAssembly *modules* is a dense linear *encoding* of their *abstract syntax*.²⁷

The format is defined by an *attribute grammar* whose only terminal symbols are *bytes*. A byte sequence is a well-formed encoding of a module if and only if it is generated by the grammar.

Each production of this grammar has exactly one synthesized attribute: the abstract syntax that the respective byte sequence encodes. Thus, the attribute grammar implicitly defines a *decoding* function (i.e., a parsing function for the binary format).

Except for a few exceptions, the binary grammar closely mirrors the grammar of the abstract syntax.

Note: Some phrases of abstract syntax have multiple possible encodings in the binary format. For example, numbers may be encoded as if they had optional leading zeros. Implementations of decoders must support all possible alternatives; implementations of encoders can pick any allowed encoding.

The recommended extension for files containing WebAssembly modules in binary format is ".wasm" and the recommended Media Type 26 is "application/wasm".

5.1.1 Grammar

The following conventions are adopted in defining grammar rules for the binary format. They mirror the conventions used for *abstract syntax*. In order to distinguish symbols of the binary syntax from symbols of the abstract syntax, typewriter font is adopted for the former.

- Terminal symbols are bytes expressed in hexadecimal notation: 0x0F.
- Nonterminal symbols are written in typewriter font: valtype, instr.
- B^n is a sequence of $n \ge 0$ iterations of B.
- B^* is a possibly empty sequence of iterations of B. (This is a shorthand for B^n used where n is not relevant.)

²⁷ Additional encoding layers – for example, introducing compression – may be defined on top of the basic representation defined here. However, such layers are outside the scope of the current specification.

²⁶ https://www.iana.org/assignments/media-types/media-types.xhtml

- $B^{?}$ is an optional occurrence of B. (This is a shorthand for B^{n} where $n \leq 1$.)
- x:B denotes the same language as the nonterminal B, but also binds the variable x to the attribute synthesized for B.
- Productions are written sym ::= $B_1 \Rightarrow A_1 \mid \ldots \mid B_n \Rightarrow A_n$, where each A_i is the attribute that is synthesized for sym in the given case, usually from attribute variables bound in B_i .
- Some productions are augmented by side conditions in parentheses, which restrict the applicability of the production. They provide a shorthand for a combinatorial expansion of the production into many separate cases.
- If the same meta variable or non-terminal symbol appears multiple times in a production (in the syntax or in an attribute), then all those occurrences must have the same instantiation. (This is a shorthand for a side condition requiring multiple different variables to be equal.)

Note: For example, the *binary grammar* for *number types* is given as follows:

```
numtype ::= 0x7F \Rightarrow i32

| 0x7E \Rightarrow i64

| 0x7D \Rightarrow f32

| 0x7C \Rightarrow f64
```

Consequently, the byte 0x7F encodes the type i32, 0x7E encodes the type i64, and so forth. No other byte value is allowed as the encoding of a number type.

The binary grammar for limits is defined as follows:

That is, a limits pair is encoded as either the byte 0x00 followed by the encoding of a u32 value, or the byte 0x01 followed by two such encodings. The variables n and m name the attributes of the respective u32 nonterminals, which in this case are the actual unsigned integers those decode into. The attribute of the complete production then is the abstract syntax for the limit, expressed in terms of the former values.

5.1.2 Auxiliary Notation

When dealing with binary encodings the following notation is also used:

- ϵ denotes the empty byte sequence.
- ||B|| is the length of the byte sequence generated from the production B in a derivation.

5.1.3 Vectors

Vectors are encoded with their u32 length followed by the encoding of their element sequence.

```
\operatorname{vec}(\mathbf{B}) ::= n: \mathrm{u32} (x:\mathbf{B})^n \Rightarrow x^n
```

5.2 Values

5.2.1 Bytes

Bytes encode themselves.

byte ::=
$$0x00 \Rightarrow 0x00$$

 $\begin{vmatrix} & & & \\ & & \ddots & \\ & & 0xFF \Rightarrow & 0xFF \end{vmatrix}$

5.2.2 Integers

All *integers* are encoded using the LEB128²⁸ variable-length integer encoding, in either unsigned or signed variant.

Unsigned integers are encoded in unsigned LEB128²⁹ format. As an additional constraint, the total number of bytes encoding a value of type uN must not exceed ceil(N/7) bytes.

$$\begin{array}{lll} \mathbf{u} N & ::= & n \text{:byte} & \Rightarrow & n & \qquad & \text{(if } n < 2^7 \wedge n < 2^N \text{)} \\ & & | & n \text{:byte} & m \text{:} \mathbf{u} (N-7) & \Rightarrow & 2^7 \cdot m + (n-2^7) & \qquad & \text{(if } n \geq 2^7 \wedge N > 7 \text{)} \end{array}$$

Signed integers are encoded in signed LEB128³⁰ format, which uses a two's complement representation. As an additional constraint, the total number of bytes encoding a value of type sN must not exceed ceil(N/7) bytes.

$$\begin{array}{lll} \mathtt{s} N & ::= & n : \mathtt{byte} & \Rightarrow & n & \qquad & (\mathrm{if} \; n < 2^6 \wedge n < 2^{N-1}) \\ & \mid & n : \mathtt{byte} & \Rightarrow & n - 2^7 & \qquad & (\mathrm{if} \; 2^6 \leq n < 2^7 \wedge n \geq 2^7 - 2^{N-1}) \\ & \mid & n : \mathtt{byte} \; \; m : \mathtt{s} (N-7) \; \Rightarrow \; 2^7 \cdot m + (n-2^7) & \qquad & (\mathrm{if} \; n \geq 2^7 \wedge N > 7) \end{array}$$

Uninterpreted integers are encoded as signed integers.

$$iN ::= n:sN \Rightarrow i$$
 (if $n = signed_N(i)$)

Note: The side conditions N>7 in the productions for non-terminal bytes of the u and s encodings restrict the encoding's length. However, "trailing zeros" are still allowed within these bounds. For example, 0x03 and 0x83 0x00 are both well-formed encodings for the value 3 as a u8. Similarly, either of 0x7e and 0xFE 0x7F and 0xFE 0xFF 0x7F are well-formed encodings of the value -2 as a s16.

The side conditions on the value n of terminal bytes further enforce that any unused bits in these bytes must be 0 for positive values and 1 for negative ones. For example, 0x83 0x10 is malformed as a u8 encoding. Similarly, both 0x83 0x3E and 0xFF 0x7B are malformed as s8 encodings.

5.2.3 Floating-Point

Floating-point values are encoded directly by their IEEE 754-2019³¹ (Section 3.4) bit pattern in little endian³² byte order:

$$fN ::= b^*: byte^{N/8} \Rightarrow bytes_{fN}^{-1}(b^*)$$

5.2. Values 143

²⁸ https://en.wikipedia.org/wiki/LEB128

²⁹ https://en.wikipedia.org/wiki/LEB128#Unsigned LEB128

³⁰ https://en.wikipedia.org/wiki/LEB128#Signed_LEB128

³¹ https://ieeexplore.ieee.org/document/8766229

³² https://en.wikipedia.org/wiki/Endianness#Little-endian

5.2.4 Names

Names are encoded as a *vector* of bytes containing the Unicode³³ (Section 3.9) UTF-8 encoding of the name's character sequence.

```
name ::= b^*:vec(byte) \Rightarrow name (if utf8(name) = b^*)
```

The auxiliary utf8 function expressing this encoding is defined as follows:

```
\begin{array}{lll} \mathrm{utf8}(c^*) & = & (\mathrm{utf8}(c))^* \\ \mathrm{utf8}(c) & = & b & & (\mathrm{if}\ c < \mathrm{U} + 80 \\ & & \wedge c = b) \\ \mathrm{utf8}(c) & = & b_1\ b_2 & & (\mathrm{if}\ \mathrm{U} + 80 \le c < \mathrm{U} + 800 \\ & & \wedge c = 2^6(b_1 - \mathrm{0xC0}) + (b_2 - \mathrm{0x80})) \\ \mathrm{utf8}(c) & = & b_1\ b_2\ b_3 & & (\mathrm{if}\ \mathrm{U} + 800 \le c < \mathrm{U} + \mathrm{D}800 \lor \mathrm{U} + \mathrm{E}000 \le c < \mathrm{U} + 10000 \\ & & \wedge c = 2^{12}(b_1 - \mathrm{0xE0}) + 2^6(b_2 - \mathrm{0x80}) + (b_3 - \mathrm{0x80})) \\ \mathrm{utf8}(c) & = & b_1\ b_2\ b_3\ b_4 & & (\mathrm{if}\ \mathrm{U} + 10000 \le c < \mathrm{U} + 110000 \\ & & \wedge c = 2^{18}(b_1 - \mathrm{0xF0}) + 2^{12}(b_2 - \mathrm{0x80}) + 2^6(b_3 - \mathrm{0x80}) + (b_4 - \mathrm{0x80})) \\ \mathrm{where}\ b_2, b_3, b_4 < \mathrm{0xC0} & & & \end{array}
```

Note: Unlike in some other formats, name strings are not 0-terminated.

5.3 Types

Note: In some places, possible types include both type constructors or types denoted by type indices. Thus, the binary format for type constructors corresponds to the encodings of small negative sN values, such that they can unambiguously occur in the same place as (positive) type indices.

5.3.1 Number Types

Number types are encoded by a single byte.

```
numtype ::= 0x7F \Rightarrow 132

0x7E \Rightarrow 164

0x7D \Rightarrow f32

0x7C \Rightarrow f64
```

5.3.2 Vector Types

Vector types are also encoded by a single byte.

```
vectype ::= 0x7B \Rightarrow v128
```

³³ https://www.unicode.org/versions/latest/

5.3.3 Heap Types

Heap types are encoded as either a single byte, or as a type index encoded as a positive signed integer.

5.3.4 Reference Types

Reference types are either encoded by a single byte followed by a *heap type*, or, as a short form, directly as a non-index heap type.

5.3.5 Value Types

Value types are encoded with their respective encoding as a *number type*, *vector type*, or *reference type*.

Note: The type bot cannot occur in a module.

Value types can occur in contexts where *type indices* are also allowed, such as in the case of *block types*. Thus, the binary format for types corresponds to the signed LEB128³⁴ *encoding* of small negative sN values, so that they can coexist with (positive) type indices in the future.

5.3.6 Result Types

Result types are encoded by the respective vectors of value types.

```
\texttt{resulttype} \ ::= \ t^* : \texttt{vec}(\texttt{valtype}) \ \Rightarrow \ [t^*]
```

5.3.7 Function Types

Function types are encoded by the byte 0x60 followed by the respective vectors of parameter and result types.

```
functype ::= 0x60 rt_1:resulttype rt_2:resulttype \Rightarrow rt_1 \rightarrow rt_2
```

5.3. Types 145

³⁴ https://en.wikipedia.org/wiki/LEB128#Signed_LEB128

5.3.8 Limits

Limits are encoded with a preceding flag indicating whether a maximum is present.

```
limits ::= 0x00 \ n:u32 \Rightarrow \{\min n, \max \epsilon\}
| 0x01 \ n:u32 \ m:u32 \Rightarrow \{\min n, \max m\}
```

5.3.9 Memory Types

Memory types are encoded with their limits.

```
memtype ::= lim:limits \Rightarrow lim
```

5.3.10 Table Types

Table types are encoded with their limits and the encoding of their element reference type.

```
tabletype ::= et:reftype lim:limits \Rightarrow lim et
```

5.3.11 Global Types

Global types are encoded by their value type and a flag for their mutability.

5.4 Instructions

Instructions are encoded by *opcodes*. Each opcode is represented by a single byte, and is followed by the instruction's immediate arguments, where present. The only exception are *structured control instructions*, which consist of several opcodes bracketing their nested instruction sequences.

Note: Gaps in the byte code ranges for encoding instructions are reserved for future extensions.

5.4.1 Control Instructions

Control instructions have varying encodings. For structured instructions, the instruction sequences forming nested blocks are terminated with explicit opcodes for end and else.

Block types are encoded in special compressed form, by either the byte 0x40 indicating the empty type, as a single *value type*, or as a *type index* encoded as a positive *signed integer*.

```
blocktype ::=
                     0x40
                                                                                               \Rightarrow
                                                                                                    \epsilon
                     t:valtype
                                                                                               \Rightarrow t
                                                                                                                              (if x \ge 0)
                     x:s33
                                                                                               \Rightarrow x
instr
               ::= 0x00
                                                                                                   unreachable
                     0x01
                                                                                               \Rightarrow nop
                     0x02 bt:blocktype (in:instr)^* 0x0B
                                                                                               \Rightarrow block bt in^* end
                                                                                               \Rightarrow loop bt in^* end
                     0x03 bt:blocktype (in:instr)^* 0x0B
                                                                                               \Rightarrow if bt \ in^* \ {\sf else} \ \epsilon \ {\sf end}
                     0x04 bt:blocktype (in:instr)^* 0x0B
                     0x04 bt:blocktype (in_1:instr)^* 0x05 (in_2:instr)^* 0x0B \Rightarrow if bt in_1^* else in_2^* end
                     0x0C l:labelidx
                                                                                               \Rightarrow br l
                     0x0D l:labelidx
                                                                                               \Rightarrow br_if l
                     OxOE l^*:vec(labelidx) l_N:labelidx
                                                                                               \Rightarrow br_table l^* l_N
                     0x0F
                                                                                               \Rightarrow return
                     0x10 x:funcidx
                                                                                               \Rightarrow call x
                     0x11 y:typeidx x:tableidx
                                                                                               \Rightarrow call_indirect x y
                     0x14
                                                                                               \Rightarrow call_ref
                     0xD4 x:funcidx
                                                                                               ⇒ br_on_null
                     0xD6 x:funcidx
                                                                                               ⇒ br_on_non_null
```

Note: The else opcode 0x05 in the encoding of an if instruction can be omitted if the following instruction sequence is empty.

Unlike any *other occurrence*, the *type index* in a *block type* is encoded as a positive *signed integer*, so that its signed LEB128 bit pattern cannot collide with the encoding of *value types* or the special code 0x40, which correspond to the LEB128 encoding of negative integers. To avoid any loss in the range of allowed indices, it is treated as a 33 bit signed integer.

5.4.2 Reference Instructions

Reference instructions are represented by single byte codes.

5.4.3 Parametric Instructions

Parametric instructions are represented by single byte codes, possibly followed by a type annotation.

5.4. Instructions

5.4.4 Variable Instructions

Variable instructions are represented by byte codes followed by the encoding of the respective index.

5.4.5 Table Instructions

Table instructions are represented either by a single byte or a one byte prefix followed by a variable-length *unsigned integer*.

5.4.6 Memory Instructions

Each variant of *memory instruction* is encoded with a different byte code. Loads and stores are followed by the encoding of their *memarg* immediate.

```
{align a, offset o}
memarg := a:u32 o:u32
instr
                     ::=
                                   0x28 m:memarg
                                                                                                           \Rightarrow i32.load m
                                   0x29 m:memarg
                                                                                                           \Rightarrow i64.load m
                                                                                                      \Rightarrow f32.load m
                                   0x2A m:memarg
                                                                                     \begin{array}{ll} \Rightarrow & \text{f32.load} \ m \\ \Rightarrow & \text{f64.load} \ m \\ \Rightarrow & \text{i32.load8\_s} \ m \\ \Rightarrow & \text{i32.load16\_s} \ m \\ \Rightarrow & \text{i32.load16\_s} \ m \\ \Rightarrow & \text{i32.load16\_u} \ m \\ \Rightarrow & \text{i64.load8\_u} \ m \\ \Rightarrow & \text{i64.load36\_u} \ m \\ \Rightarrow & \text{i64.load36\_u} \ m \\ \Rightarrow & \text{i64.load32\_s} \ m \\ \Rightarrow & \text{i64.load32\_u} \ m \\ \Rightarrow & \text{i64.store} \ m \\ \Rightarrow & \text{i32.store} \ m \\ \Rightarrow & \text{i34.store} \ m \\ \Rightarrow & \text{i64.store} \ m \\ \end{array}
                                   0x2B m:memarg
                                                                                                      \Rightarrow f64.load m
                                   0x2C m:memarg
                                   0x2D m:memarg
                                   0x2E m:memarg
                                   0x2F m:memarg
                                   0x30 m:memarg
                                   0x31 m:memarg
                                   0x32 m:memarg
                                   0x33 m:memarg
                                   0x34 m:memarg
                                   0x35 m:memarg
                                   0x36 m:memarg
                                   0x37 m:memarg
                                   0x38 m:memarg
                                   0x39 m:memarg
                                   Ox3A m:memarg
                                   0x3B m:memarg
                                   0x3C m:memarg
                                                                                                      \Rightarrow i64.store16 m
                                   0x3D m:memarg
                                  Ox3E m:memarg
                                                                                                      \Rightarrow i64.store32 m
                                   0x3F 0x00
                                                                                                           ⇒ memory.size
                                   0x40 0x00
                                                                                                          ⇒ memory.grow
                                   0xFC 8:u32 x:dataidx 0x00 \Rightarrow memory.init x
                                   \texttt{OxFC} \ 9{:} \texttt{u32} \ x{:} \texttt{dataidx} \qquad \Rightarrow \quad \mathsf{data.drop} \ x
                                   0xFC 10:u32 0x00 0x00
                                                                                                       ⇒ memory.copy
                                   0xFC 11:u32 0x00
                                                                                                      ⇒ memory.fill
```

Note: In future versions of WebAssembly, the additional zero bytes occurring in the encoding of the memory.size, memory.grow, memory.copy, and memory.fill instructions may be used to index additional memories.

5.4.7 Numeric Instructions

All variants of *numeric instructions* are represented by separate byte codes.

The const instructions are followed by the respective literal.

```
instr ::= ...

| 0x41 n:i32 \Rightarrow i32.const n

| 0x42 n:i64 \Rightarrow i64.const n

| 0x43 z:f32 \Rightarrow f32.const z

| 0x44 z:f64 \Rightarrow f64.const z
```

All other numeric instructions are plain opcodes without any immediates.

5.4. Instructions 149

```
instr ::=
                 0x45 \Rightarrow i32.eqz
                 0x46 \Rightarrow i32.eq
                 0x47 \Rightarrow i32.ne
                 0x48 \Rightarrow i32.lt_s
                 0x49 \Rightarrow i32.lt_u
                 0x4A \Rightarrow i32.gt_s
                 0x4B \Rightarrow i32.gt_u
                 0x4C \Rightarrow i32.le_s
                 0x4D \Rightarrow i32.le u
                 0x4E \Rightarrow i32.ge\_s
                 0x4F \Rightarrow i32.ge_u
                 0x50 \Rightarrow i64.eqz
                 0x51 \Rightarrow i64.eq
                 0x52 \Rightarrow i64.ne
                 0x53 \Rightarrow i64.lt_s
                 0x54 \Rightarrow i64.lt_u
                 0x55 \Rightarrow i64.gt_s
                 0x56 \Rightarrow i64.gt_u
                 0x57 \Rightarrow i64.le s
                 0x58 \Rightarrow i64.le_u
                 0x59 \Rightarrow i64.ge_s
                 0x5A \Rightarrow i64.ge_u
                 0x5B \Rightarrow f32.eq
                 0x5C \Rightarrow f32.ne
                 0x5D \Rightarrow f32.lt
                 0x5E \Rightarrow f32.gt
                 0x5F \Rightarrow f32.le
                 0x60 \Rightarrow f32.ge
                 0x61 \Rightarrow
                                f64.eq
                 0x62 \Rightarrow f64.ne
                 0x63 \Rightarrow f64.lt
                 0x64 \Rightarrow f64.gt
                 0x65 \Rightarrow f64.le
                 0x66 \Rightarrow f64.ge
                 0x67 \Rightarrow i32.clz
                 0x68 \Rightarrow i32.ctz
                 0x69 \Rightarrow i32.popcnt
                 0x6A \Rightarrow i32.add
                 0x6B \Rightarrow i32.sub
                 0x6C \Rightarrow i32.mul
                 0x6D \Rightarrow i32.div_s
                 0x6E \Rightarrow i32.div_u
                 0x6F \Rightarrow i32.rem\_s
                 0x70 \Rightarrow i32.rem_u
                 0x71 \Rightarrow i32.and
                 0x72 \Rightarrow i32.or
                 0x73 \Rightarrow i32.xor
                 0x74 \Rightarrow i32.shl
                 0x75 \Rightarrow i32.shr s
                 0x76 \Rightarrow i32.shr_u
                 0x77 \Rightarrow i32.rotl
                 0x78 \Rightarrow i32.rotr
```

```
i64.clz
0x79
        \Rightarrow
0x7A \Rightarrow
              i64.ctz
0x7B \Rightarrow
              i64.popcnt
0x7C \Rightarrow i64.add
0x7D \Rightarrow i64.sub
0x7E \Rightarrow i64.mul
0x7F \Rightarrow i64.div s
0x80 \Rightarrow i64.div_u
0x81
        \Rightarrow
              i64.rem_s
0x82
        \Rightarrow
              i64.rem_u
0x83 \Rightarrow
              i64.and
0x84 \Rightarrow i64.or
0x85 \Rightarrow i64.xor
0x86 \Rightarrow i64.shl
0x87 \Rightarrow i64.shr_s
0x88 \Rightarrow i64.shr_u
0x89 \Rightarrow i64.rotl
0x8A \Rightarrow i64.rotr
0x8B \Rightarrow f32.abs
0x8C \Rightarrow f32.neg
0x8D \Rightarrow f32.ceil
0x8E \Rightarrow f32.floor
0x8F \Rightarrow f32.trunc
0x90 \Rightarrow f32.nearest
0x91 \Rightarrow f32.sqrt
0x92 \Rightarrow f32.add
0x93 \Rightarrow f32.sub
0x94 \Rightarrow f32.mul
0x95 \Rightarrow f32.div
0x96 \Rightarrow f32.min
0x97 \Rightarrow f32.max
0x98 \Rightarrow f32.copysign
0x99
              f64.abs
0x9A \Rightarrow f64.neg
0x9B \Rightarrow f64.ceil
0x9C \Rightarrow f64.floor
0x9D \Rightarrow f64.trunc
0x9E \Rightarrow f64.nearest
0x9F \Rightarrow f64.sqrt
0xA0 \Rightarrow f64.add
0xA1 \Rightarrow f64.sub
0xA2 \Rightarrow f64.mul
0xA3 \Rightarrow f64.div
0xA4 \Rightarrow f64.min
0xA5 \Rightarrow
              f64.max
0xA6 \Rightarrow f64.copysign
```

5.4. Instructions

```
0xA7 \Rightarrow i32.wrap i64
0xA8 \Rightarrow i32.trunc_f32_s
0xA9 \Rightarrow i32.trunc_f32_u
0xAA \Rightarrow i32.trunc_f64_s
0xAB \Rightarrow i32.trunc f64 u
0xAC \Rightarrow i64.extend i32 s
0xAD \Rightarrow i64.extend_i32_u
0xAE \Rightarrow i64.trunc_f32_s
0xAF \Rightarrow i64.trunc_f32_u
0xB0 \Rightarrow i64.trunc_f64_s
0xB1 \Rightarrow i64.trunc_f64_u
0xB2 \Rightarrow f32.convert_i32_s
0xB3 \Rightarrow f32.convert_i32_u
0xB4 \Rightarrow f32.convert_i64_s
0xB5 \Rightarrow f32.convert_i64_u
0xB6 \Rightarrow f32.demote f64
0xB7 \Rightarrow f64.convert i32 s
0xB8 \Rightarrow f64.convert_i32_u
0xB9 \Rightarrow f64.convert_i64_s
0xBA \Rightarrow f64.convert i64 u
0xBB \Rightarrow f64.promote_f32
0xBC \Rightarrow i32.reinterpret_f32
0xBD
        ⇒ i64.reinterpret_f64
0xBE \Rightarrow f32.reinterpret i32
0xBF \Rightarrow f64.reinterpret_i64
0xC0 \Rightarrow i32.extend8_s
0xC1 \Rightarrow i32.extend16_s
0xC2 \Rightarrow i64.extend8 s
0xC3 \Rightarrow i64.extend16 s
0xC4 \Rightarrow i64.extend32_s
```

The saturating truncation instructions all have a one byte prefix, whereas the actual opcode is encoded by a variable-length *unsigned integer*.

5.4.8 Vector Instructions

All variants of *vector instructions* are represented by separate byte codes. They all have a one byte prefix, whereas the actual opcode is encoded by a variable-length *unsigned integer*.

Vector loads and stores are followed by the encoding of their memarg immediate.

The const instruction is followed by 16 immediate bytes, which are converted into a *i128* in littleendian byte order:

```
instr ::= ...

| OxFD 12:u32 (b:byte)^{16} \Rightarrow v128.const bytes_{i128}^{-1}(b_0 \dots b_{15})
```

The shuffle instruction is also followed by the encoding of 16 laneidx immediates.

extract_lane and replace_lane instructions are followed by the encoding of a laneidx immediate.

5.4. Instructions

All other vector instructions are plain opcodes without any immediates.

```
instr ::=
                0xFD 14:u32 \Rightarrow i8x16.swizzle
                0xFD 15:u32 \Rightarrow i8x16.splat
                0xFD 16:u32 \Rightarrow i16x8.splat
                0xFD 17:u32 \Rightarrow i32x4.splat
                0xFD 18:u32 \Rightarrow i64x2.splat
                0xFD 19:u32 \Rightarrow f32x4.splat
                0xFD 20:u32 \Rightarrow f64x2.splat
                0xFD 35:u32 \Rightarrow i8x16.eq
                0xFD 36:u32 \Rightarrow i8x16.ne
                0xFD 37:u32 \Rightarrow i8x16.lt s
                0xFD 38:u32 \Rightarrow i8x16.lt_u
                0xFD 39:u32 \Rightarrow i8x16.gt_s
                0xFD \ 40:u32 \Rightarrow i8x16.gt_u
                0xFD 41:u32 \Rightarrow i8x16.le_s
                0xFD 42:u32 \Rightarrow i8x16.le u
                0xFD \ 43:u32 \Rightarrow i8x16.ge_s
                0xFD 44:u32 \Rightarrow i8x16.ge_u
                0xFD \ 45:u32 \Rightarrow i16x8.eq
                0xFD \ 46:u32 \Rightarrow i16x8.ne
                0xFD 47:u32 \Rightarrow i16x8.lt_s
                0xFD 48:u32 \Rightarrow i16x8.lt u
                0xFD 49:u32 \Rightarrow i16x8.gt_s
                0xFD 50:u32 \Rightarrow i16x8.gt_u
                0xFD 51:u32 \Rightarrow i16x8.le_s
                0xFD 52:u32 \Rightarrow i16x8.le_u
                0xFD 53:u32 \Rightarrow i16x8.ge_s
                \texttt{0xFD} \ 54{:} \texttt{u32} \ \Rightarrow \ \mathsf{i16x8.ge\_u}
                0xFD 55:u32 \Rightarrow i32x4.eq
                0xFD 56:u32 \Rightarrow i32x4.ne
                0xFD 57:u32 \Rightarrow i32x4.lt s
                0xFD 58:u32 \Rightarrow i32\times4.lt u
                0xFD 59:u32 \Rightarrow i32x4.gt_s
                0xFD 60:u32 \Rightarrow i32x4.gt_u
                0xFD 61:u32 \Rightarrow i32x4.le_s
                0xFD 62:u32 \Rightarrow i32x4.le_u
                0xFD 63:u32 \Rightarrow i32x4.ge_s
                0xFD 64:u32 \Rightarrow i32x4.ge\_u
               0xFD 214:u32 \Rightarrow i64x2.eq
               \texttt{0xFD} \ 215{:}\texttt{u32} \ \Rightarrow \ \mathsf{i64x2.ne}
               0xFD 216:u32 \Rightarrow i64x2.lt_s
               0xFD 217:u32 \Rightarrow i64x2.gt_s
               0xFD 218:u32 \Rightarrow i64x2.le s
               0xFD 219:u32 \Rightarrow i64x2.ge_s
                0xFD 65:u32 \Rightarrow f32x4.eq
                0xFD 66:u32 \Rightarrow f32x4.ne
                0xFD 67:u32 \Rightarrow f32\times4.lt
                0xFD 68:u32 \Rightarrow f32x4.gt
                0xFD 69:u32 \Rightarrow f32x4.le
                0xFD 70:u32 \Rightarrow f32x4.ge
```

```
0xFD 71:u32 \Rightarrow f64x2.eq
0xFD 72:u32 \Rightarrow f64x2.ne
0xFD 73:u32 \Rightarrow f64x2.lt
0xFD 74:u32 \Rightarrow f64x2.gt
0xFD 75:u32 \Rightarrow f64x2.le
0xFD 76:u32 \Rightarrow f64x2.ge
0xFD 77:u32 \Rightarrow v128.not
0xFD 78:u32 \Rightarrow v128.and
0xFD 79:u32 \Rightarrow v128.andnot
0xFD 80:u32 \Rightarrow v128.or
0xFD 81:u32 \Rightarrow v128.xor
0xFD 82:u32 \Rightarrow v128.bitselect
0xFD 83:u32 \Rightarrow v128.any\_true
0xFD 96:u32 \Rightarrow i8x16.abs
0xFD 97:u32 \Rightarrow i8x16.neg
0xFD 98:u32 \Rightarrow i8x16.popcnt
0xFD 99:u32 \Rightarrow i8x16.all true
0xFD 100:u32 \Rightarrow i8x16.bitmask
0xFD 101:u32 \Rightarrow i8x16.narrow_i16x8_s
0xFD 102:u32 \Rightarrow i8x16.narrow_i16x8_u
0xFD 107:u32 \Rightarrow i8x16.shl
0xFD 108:u32 \Rightarrow i8x16.shr_s
0xFD 109:u32 \Rightarrow i8x16.shr_u
0xFD 110:u32 \Rightarrow i8x16.add
\texttt{0xFD} \ 111{:}u32 \ \Rightarrow \ i8{\times}16.\mathsf{add\_sat\_s}
0xFD 112:u32 \Rightarrow i8x16.add_sat_u
0xFD 113:u32 \Rightarrow i8x16.sub
0xFD 114:u32 \Rightarrow i8x16.sub sat s
0xFD 115:u32 \Rightarrow i8x16.sub sat u
0xFD 118:u32 \Rightarrow i8x16.min_s
0xFD 119:u32 \Rightarrow i8x16.min_u
0xFD 120:u32 \Rightarrow i8x16.max_s
0xFD 121:u32 \Rightarrow i8x16.max_u
\texttt{0xFD} \ 123{:}\texttt{u}32 \ \Rightarrow \ \mathsf{i8x}16.\mathsf{avgr\_u}
```

5.4. Instructions

```
i16x8.extadd_pairwise_i8x16_s
0xFD 124:u32 \Rightarrow
0xFD 125:u32
                      i16x8.extadd_pairwise_i8x16_u
0xFD 128:u32 \Rightarrow i16x8.abs
0xFD 129:u32 \Rightarrow i16x8.neg
0xFD 130:u32 \Rightarrow i16x8.q15mulr_sat_s
0xFD 131:u32 \Rightarrow i16x8.all true
0xFD 132:u32 \Rightarrow i16x8.bitmask
0xFD 133:u32 \Rightarrow i16x8.narrow i32x4 s
0xFD 134:u32 \Rightarrow i16x8.narrow i32x4 u
0xFD 135:u32 \Rightarrow i16x8.extend_low_i8x16_s
0xFD 136:u32 \Rightarrow i16x8.extend_high_i8x16_s
0xFD 137:u32 \Rightarrow i16x8.extend_low_i8x16_u
0xFD 138:u32 \Rightarrow i16x8.extend_high_i8x16_u
0xFD 139:u32 \Rightarrow i16x8.shl
0xFD 140:u32 \Rightarrow i16x8.shr_s
0xFD 141:u32 \Rightarrow i16x8.shr_u
0xFD 142:u32 \Rightarrow i16x8.add
0xFD 143:u32 \Rightarrow i16x8.add sat s
0xFD 144:u32 \Rightarrow i16x8.add_sat_u
0xFD 145:u32 \Rightarrow i16x8.sub
0xFD 146:u32 \Rightarrow i16x8.sub\_sat\_s
0xFD 147:u32 \Rightarrow i16x8.sub sat u
0xFD 149:u32 \Rightarrow i16x8.mul
0xFD 150:u32 \Rightarrow i16x8.min_s
0xFD 151:u32 \Rightarrow i16x8.min_u
0xFD 152:u32 \Rightarrow i16x8.max s
0xFD 153:u32 \Rightarrow i16x8.max_u
0xFD 155:u32 \Rightarrow i16x8.avgr u
0xFD 156:u32 \Rightarrow i16x8.extmul_low_i8x16_s
0xFD 157:u32 \Rightarrow i16x8.extmul high i8x16 s
0xFD 158:u32 \Rightarrow i16x8.extmul_low_i8x16_u
0xFD 159:u32 \Rightarrow i16x8.extmul_high_i8x16_u
0xFD 126:u32 \Rightarrow i32x4.extadd_pairwise_i16x8_s
0xFD 127:u32 \Rightarrow i32x4.extadd_pairwise_i16x8_u
0xFD 160:u32 \Rightarrow i32x4.abs
0xFD 161:u32 \Rightarrow i32x4.neg
0xFD 163:u32 \Rightarrow i32x4.all\_true
0xFD 164:u32 \Rightarrow i32x4.bitmask
0xFD 167:u32 \Rightarrow i32x4.extend_low_i16x8_s
0xFD 168:u32 \Rightarrow i32x4.extend_high_i16x8_s
0xFD 169:u32 \Rightarrow i32x4.extend_low_i16x8_u
0xFD 170:u32 \Rightarrow i32x4.extend_high_i16x8_u
0xFD 171:u32 \Rightarrow i32x4.shl
0xFD 172:u32 \Rightarrow i32x4.shr s
0xFD 173:u32 \Rightarrow i32x4.shr_u
0xFD 174:u32 \Rightarrow i32x4.add
0xFD 177:u32 \Rightarrow i32x4.sub
0xFD 181:u32 \Rightarrow i32x4.mul
0xFD 182:u32 \Rightarrow i32\times4.min_s
0xFD 183:u32 \Rightarrow i32x4.min_u
0xFD 184:u32 \Rightarrow i32x4.max_s
0xFD 185:u32 \Rightarrow i32x4.max_u
0xFD 186:u32 \Rightarrow i32x4.dot_i16x8_s
0xFD 188:u32 \Rightarrow i32x4.extmul_low_i16x8_s
0xFD 189:u32 \Rightarrow i32x4.extmul_high_i16x8_s
0xFD 190:u32 \Rightarrow i32x4.extmul_low_i16x8_u
0xFD 191:u32 \Rightarrow i32x4.extmul_high_i16x8_u
```

```
i64x2.abs
0xFD 192:u32 \Rightarrow
0xFD 193:u32
                       i64x2.neg
0xFD 195:u32 \Rightarrow i64x2.all true
0xFD 196:u32 \Rightarrow i64x2.bitmask
0xFD 199:u32 \Rightarrow i64x2.extend_low_i32x4_s
0xFD 200:u32 \Rightarrow i64x2.extend_high_i32x4_s
0xFD 201:u32 \Rightarrow i64x2.extend low i32x4 u
0xFD 202:u32 \Rightarrow i64x2.extend_high_i32x4_u
0xFD 203:u32 \Rightarrow i64x2.shl
0xFD 204:u32 \Rightarrow i64x2.shr_s
0xFD 205:u32 \Rightarrow i64x2.shr_u
0xFD 206:u32 \Rightarrow i64x2.add
0xFD 209:u32 \Rightarrow i64x2.sub
0xFD 213:u32 \Rightarrow i64x2.mul
0xFD 220:u32 \Rightarrow i64x2.extmul_low_i32x4_s
0xFD 221:u32 \Rightarrow i64x2.extmul_high_i32x4_s
0xFD 222:u32 \Rightarrow i64x2.extmul_low_i32x4_u
0xFD 223:u32 \Rightarrow i64x2.extmul_high_i32x4_u
0xFD 103:u32 \Rightarrow f32x4.ceil
0xFD 104:u32 \Rightarrow f32x4.floor
0xFD 105:u32 \Rightarrow f32x4.trunc
0xFD 106:u32 \Rightarrow f32x4.nearest
0xFD 224:u32 \Rightarrow f32x4.abs
0xFD 225:u32 \Rightarrow f32x4.neg
0xFD 227:u32 \Rightarrow f32x4.sqrt
0xFD 228:u32 \Rightarrow f32\times4.add
0xFD 229:u32 \Rightarrow f32x4.sub
0xFD 230:u32 \Rightarrow f32x4.mul
0xFD 231:u32 \Rightarrow f32x4.div
0xFD 232:u32 \Rightarrow f32x4.min
0xFD 233:u32 \Rightarrow f32x4.max
0xFD 234:u32 \Rightarrow f32x4.pmin
0xFD 235:u32 \Rightarrow f32x4.pmax
0xFD 116:u32 \Rightarrow f64x2.ceil
0xFD 117:u32 \Rightarrow f64x2.floor
0xFD 122:u32 <math>\Rightarrow f64x2.trunc
0xFD 148:u32 \Rightarrow f64x2.nearest
0xFD 236:u32 \Rightarrow f64x2.abs
0xFD 237:u32 \Rightarrow f64x2.neg
0xFD 239:u32 \Rightarrow f64\times 2.sgrt
0xFD 240:u32 \Rightarrow f64x2.add
0xFD 241:u32 \Rightarrow f64x2.sub
0xFD 242:u32 \Rightarrow f64x2.mul
0xFD 243:u32 \Rightarrow f64x2.div
0xFD 244:u32 \Rightarrow f64x2.min
0xFD 245:u32 \Rightarrow f64x2.max
0xFD 246:u32 \Rightarrow f64x2.pmin
0xFD 247:u32 \Rightarrow f64x2.pmax
```

5.4. Instructions 157

5.4.9 Expressions

Expressions are encoded by their instruction sequence terminated with an explicit 0x0B opcode for end.

```
expr ::= (in:instr)^* \circ oxob \Rightarrow in^* end
```

5.5 Modules

The binary encoding of modules is organized into *sections*. Most sections correspond to one component of a *module* record, except that *function definitions* are split into two sections, separating their type declarations in the *function section* from their bodies in the *code section*.

Note: This separation enables *parallel* and *streaming* compilation of the functions in a module.

5.5.1 Indices

All *indices* are encoded with their respective value.

5.5.2 Sections

Each section consists of

- a one-byte section id,
- the u32 size of the contents, in bytes,
- the actual *contents*, whose structure is depended on the section id.

Every section is optional; an omitted section is equivalent to the section being present with empty contents.

The following parameterized grammar rule defines the generic structure of a section with id N and contents described by the grammar B.

For most sections, the contents B encodes a *vector*. In these cases, the empty result ϵ is interpreted as the empty vector

Note: Other than for unknown *custom sections*, the *size* is not required for decoding, but can be used to skip sections when navigating through a binary. The module is malformed if the size does not match the length of the binary contents B.

The following section ids are used:

ld	Section
0	custom section
1	type section
2	import section
3	function section
4	table section
5	memory section
6	global section
7	export section
8	start section
9	element section
10	code section
11	data section
12	data count section

5.5.3 Custom Section

Custom sections have the id 0. They are intended to be used for debugging information or third-party extensions, and are ignored by the WebAssembly semantics. Their contents consist of a *name* further identifying the custom section, followed by an uninterpreted sequence of bytes for custom use.

```
\begin{array}{lll} \text{customsec} & ::= & \text{section}_0(\text{custom}) \\ \text{custom} & ::= & \text{name byte}^* \end{array}
```

Note: If an implementation interprets the data of a custom section, then errors in that data, or the placement of the section, must not invalidate the module.

5.5.4 Type Section

The *type section* has the id 1. It decodes into a vector of *function types* that represent the types component of a *module*.

```
typesec ::= ft^*:section<sub>1</sub>(vec(functype)) \Rightarrow ft^*
```

5.5. Modules 159

5.5.5 Import Section

The *import section* has the id 2. It decodes into a vector of *imports* that represent the imports component of a *module*.

5.5.6 Function Section

The *function section* has the id 3. It decodes into a vector of *type indices* that represent the type fields of the *functions* in the funcs component of a *module*. The locals and body fields of the respective functions are encoded separately in the *code section*.

```
funcsec ::= x^*:section<sub>3</sub>(vec(typeidx)) \Rightarrow x^*
```

5.5.7 Table Section

The table section has the id 4. It decodes into a vector of tables that represent the tables component of a module.

```
tablesec ::= tab^*:section<sub>4</sub>(vec(table)) \Rightarrow tab^*
table ::= tt:tabletype \Rightarrow {type tt}
```

5.5.8 Memory Section

The *memory section* has the id 5. It decodes into a vector of *memories* that represent the mems component of a *module*.

```
memsec ::= mem^*:section<sub>5</sub>(vec(mem)) \Rightarrow mem^*
mem ::= mt:memtype \Rightarrow {type mt}
```

5.5.9 Global Section

The *global section* has the id 6. It decodes into a vector of *globals* that represent the globals component of a *module*.

```
globalsec ::= glob^*:section<sub>6</sub>(vec(global)) \Rightarrow glob^*
global ::= gt:globaltype e:expr \Rightarrow {type gt, init e}
```

5.5.10 Export Section

The *export section* has the id 7. It decodes into a vector of *exports* that represent the exports component of a *module*.

5.5.11 Start Section

The *start section* has the id 8. It decodes into an optional *start function* that represents the start component of a *module*.

```
startsec ::= st^?:section<sub>8</sub>(start) \Rightarrow st^?
start ::= x:funcidx \Rightarrow {func x}
```

5.5.12 Element Section

The *element section* has the id 9. It decodes into a vector of *element segments* that represent the elems component of a *module*.

```
elemsec
              := seg^*:section_9(vec(elem))
                                                                                                               seg^*
              := 0:u32 \ e:expr \ y^*:vec(funcidx)
elem
                                                                                                          \Rightarrow
                       {type funcref, init ((ref.func y) end)*, mode active {table 0, offset e}}
                    1:u32 et:elemkind y^*:vec(funcidx)
                       {type et, init ((ref.func y) end)*, mode passive}
                     2:u32 x:tableidx e:expr et:elemkind y^*:vec(funcidx)
                       \{\text{type } et, \text{ init } ((\text{ref.func } y) \text{ end})^*, \text{ mode active } \{\text{table } x, \text{ offset } e\}\}
                     3:u32 et:elemkind y^*:vec(funcidx)
                       {type et, init ((ref.func y) end)*, mode declarative}
                    4:u32 \ e:expr \ el^*:vec(expr)
                       {type funcref, init el^*, mode active {table 0, offset e}}
                    5:u32 et:reftype el^*:vec(expr)
                       \{ \text{type } et, \text{ init } el^*, \text{ mode passive} \}
                    6:u32 x:tableidx e:expr et:reftype el^*:vec(expr)
                       \{\text{type } et, \text{ init } el^*, \text{ mode active } \{\text{table } x, \text{ offset } e\}\}
                     7:u32 et:reftype el^*:vec(expr)
                       {type et, init el^*, mode declarative}
elemkind ::= 0x00
                                                                                                               funcref
```

Note: The initial integer can be interpreted as a bitfield. Bit 0 indicates a passive or declarative segment, bit 1 indicates the presence of an explicit table index for an active segment and otherwise distinguishes passive from declarative segments, bit 2 indicates the use of element type and element *expressions* instead of element kind and element indices.

Additional element kinds may be added in future versions of WebAssembly.

5.5. Modules 161

5.5.13 Code Section

The *code section* has the id 10. It decodes into a vector of *code* entries that are pairs of *value type* vectors and *expressions*. They represent the locals and body field of the *functions* in the funcs component of a *module*. The type fields of the respective functions are encoded separately in the *function section*.

The encoding of each code entry consists of

- the u32 size of the function code in bytes,
- the actual function code, which in turn consists of
 - the declaration of *locals*,
 - the function body as an expression.

Local declarations are compressed into a vector whose entries consist of

- a *u32 count*,
- a value type,

denoting *count* locals of the same value type.

Here, code ranges over pairs $(valtype^*, expr)$. The meta function $concat((local^*)^*)$ concatenates all sequences $local_i^*$ in $(local^*)^*$. Any code for which the length of the resulting sequence is out of bounds of the maximum size of a *vector* is malformed.

Note: Like with *sections*, the code *size* is not needed for decoding, but can be used to skip functions when navigating through a binary. The module is malformed if a size does not match the length of the respective function code.

5.5.14 Data Section

The *data section* has the id 11. It decodes into a vector of *data segments* that represent the datas component of a *module*.

```
\begin{array}{lll} \texttt{datasec} & ::= & seg^* : \mathtt{section_{11}}(\mathtt{vec}(\mathtt{data})) & \Rightarrow & seg^* \\ \texttt{data} & ::= & 0 : \mathtt{u32} \ e : \mathtt{eexpr} \ b^* : \mathtt{vec}(\mathtt{byte}) & \Rightarrow & \{\mathtt{init} \ b^*, \mathtt{mode} \ \mathtt{active} \ \{\mathtt{memory} \ 0, \mathtt{offset} \ e\} \} \\ & & | & 1 : \mathtt{u32} \ b^* : \mathtt{vec}(\mathtt{byte}) & \Rightarrow & \{\mathtt{init} \ b^*, \mathtt{mode} \ \mathtt{passive} \} \\ & & | & 2 : \mathtt{u32} \ x : \mathtt{memidx} \ e : \mathtt{expr} \ b^* : \mathtt{vec}(\mathtt{byte}) & \Rightarrow & \{\mathtt{init} \ b^*, \mathtt{mode} \ \mathtt{active} \ \{\mathtt{memory} \ x, \mathtt{offset} \ e\} \} \end{array}
```

Note: The initial integer can be interpreted as a bitfield. Bit 0 indicates a passive segment, bit 1 indicates the presence of an explicit memory index for an active segment.

In the current version of WebAssembly, at most one memory may be defined or imported in a single module, so all valid *active* data segments have a memory value of 0.

5.5.15 Data Count Section

The *data count section* has the id 12. It decodes into an optional *u32* that represents the number of *data segments* in the *data section*. If this count does not match the length of the data segment vector, the module is malformed.

datacountsec ::=
$$n^?$$
:section₁₂(u32) $\Rightarrow n^?$

Note: The data count section is used to simplify single-pass validation. Since the data section occurs after the code section, the memory.init and data.drop instructions would not be able to check whether the data segment index is valid until the data section is read. The data count section occurs before the code section, so a single-pass validator can use this count instead of deferring validation.

5.5.16 Modules

The encoding of a *module* starts with a preamble containing a 4-byte magic number (the string '\Oasm') and a version field. The current version of the WebAssembly binary format is 1.

The preamble is followed by a sequence of *sections*. *Custom sections* may be inserted at any place in this sequence, while other sections must occur at most once and in the prescribed order. All sections can be empty.

The lengths of vectors produced by the (possibly empty) function and code section must match up.

Similarly, the optional data count must match the length of the data segment vector. Furthermore, it must be present

5.5. Modules 163

if any data index occurs in the code section.

```
::= 0x00 0x61 0x73 0x6D
version ::= 0x01 0x00 0x00 0x00
module
         ::= magic
                version
                 customsec^*
                functype*:typesec
                 customsec*
                 import*:importsec
                 customsec*
                 typeidx^n: funcsec
                 customsec*
                 table^*:tablesec
                 customsec*
                 mem^*:memsec
                 customsec*
                 global^*: globalsec
                 customsec*
                 export*:exportsec
                 customsec*
                 start?:startsec
                 customsec*
                 elem^*:elemsec
                 customsec*
                m^?: datacountsec
                 customsec*
                 code^n: codesec
                 customsec*
                 data^m: datasec
                 customsec*
                                     \{ \text{ types } functype^*, 
                                       funcs func^n,
                                       tables table^*,
                                       mems mem^*,
                                       globals global^*,
                                       elems elem^*,
                                       datas data^m,
                                       start start?,
                                       imports import*,
                                       exports export* }
                (if m^? \neq \epsilon \vee \operatorname{dataidx}(code^n) = \emptyset)
```

where for each t_i^* , e_i in $code^n$,

```
func^n[i] = \{ type \ type idx^n[i], locals \ t_i^*, body \ e_i \}
```

Note: The version of the WebAssembly binary format may increase in the future if backward-incompatible changes have to be made to the format. However, such changes are expected to occur very infrequently, if ever. The binary format is intended to be forward-compatible, such that future extensions can be made without incrementing its version.

Text Format

6.1 Conventions

The textual format for WebAssembly *modules* is a rendering of their *abstract syntax* into S-expressions³⁵.

Like the *binary format*, the text format is defined by an *attribute grammar*. A text string is a well-formed description of a module if and only if it is generated by the grammar. Each production of this grammar has at most one synthesized attribute: the abstract syntax that the respective character sequence expresses. Thus, the attribute grammar implicitly defines a *parsing* function. Some productions also take a *context* as an inherited attribute that records bound *identifiers*.

Except for a few exceptions, the core of the text grammar closely mirrors the grammar of the abstract syntax. However, it also defines a number of *abbreviations* that are "syntactic sugar" over the core syntax.

The recommended extension for files containing WebAssembly modules in text format is ".wat". Files with this extension are assumed to be encoded in UTF-8, as per Unicode³⁶ (Section 2.5).

6.1.1 Grammar

The following conventions are adopted in defining grammar rules of the text format. They mirror the conventions used for *abstract syntax* and for the *binary format*. In order to distinguish symbols of the textual syntax from symbols of the abstract syntax, typewriter font is adopted for the former.

- Terminal symbols are either literal strings of characters enclosed in quotes or expressed as Unicode³⁷ scalar values: 'module', U+0A. (All characters written literally are unambiguously drawn from the 7-bit ASCII³⁸ subset of Unicode.)
- \bullet Nonterminal symbols are written in typewriter font: valtype, instr.
- T^n is a sequence of $n \ge 0$ iterations of T.
- T^* is a possibly empty sequence of iterations of T. (This is a shorthand for T^n used where n is not relevant.)
- T^+ is a sequence of one or more iterations of T. (This is a shorthand for T^n where $n \ge 1$.)
- $T^{?}$ is an optional occurrence of T. (This is a shorthand for T^{n} where $n \leq 1$.)

³⁵ https://en.wikipedia.org/wiki/S-expression

³⁶ https://www.unicode.org/versions/latest/

³⁷ https://www.unicode.org/versions/latest/

 $^{^{38}}$ https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

- x:T denotes the same language as the nonterminal T, but also binds the variable x to the attribute synthesized
 for T.
- Productions are written sym ::= $T_1 \Rightarrow A_1 \mid \dots \mid T_n \Rightarrow A_n$, where each A_i is the attribute that is synthesized for sym in the given case, usually from attribute variables bound in T_i .
- Some productions are augmented by side conditions in parentheses, which restrict the applicability of the production. They provide a shorthand for a combinatorial expansion of the production into many separate cases.
- If the same meta variable or non-terminal symbol appears multiple times in a production (in the syntax or in an attribute), then all those occurrences must have the same instantiation.
- A distinction is made between *lexical* and *syntactic* productions. For the latter, arbitrary *white space* is allowed in any place where the grammar contains spaces. The productions defining *lexical syntax* and the syntax of *values* are considered lexical, all others are syntactic.

Note: For example, the *textual grammar* for *number types* is given as follows:

```
numtype ::= 'i32' \Rightarrow i32 | 'i64' \Rightarrow i64 | 'f32' \Rightarrow f32 | 'f64' \Rightarrow f64
```

The textual grammar for limits is defined as follows:

```
limits ::= n:u32 \Rightarrow \{\min n, \max \epsilon\}
 \mid n:u32 \ m:u32 \ \Rightarrow \{\min n, \max m\}
```

The variables n and m name the attributes of the respective u32 nonterminals, which in this case are the actual unsigned integers those parse into. The attribute of the complete production then is the abstract syntax for the limit, expressed in terms of the former values.

6.1.2 Abbreviations

In addition to the core grammar, which corresponds directly to the *abstract syntax*, the textual syntax also defines a number of *abbreviations* that can be used for convenience and readability.

Abbreviations are defined by rewrite rules specifying their expansion into the core syntax:

```
abbreviation\ syntax \equiv expanded\ syntax
```

These expansions are assumed to be applied, recursively and in order of appearance, before applying the core grammar rules to construct the abstract syntax.

6.1.3 Contexts

The text format allows the use of symbolic *identifiers* in place of *indices*. To resolve these identifiers into concrete indices, some grammar productions are indexed by an *identifier context* I as a synthesized attribute that records the declared identifiers in each *index space*. In addition, the context records the types defined in the module, so that *parameter* indices can be computed for *functions*.

It is convenient to define identifier contexts as records I with abstract syntax as follows:

```
I \quad ::= \quad \{ \text{ types }
                            (id^?)^*,
              funcs
                            (id^?)^*,
                            (id^?)^*,
              tables
                            (id^?)^*,
               mems
               globals
                            (id^?)^*,
                            (id^?)^*,
              elem
               data
                            (id^?)^*
                            (id^?)^*.
              locals
                            (id^?)^*,
               labels
               typedefs functype* }
```

For each index space, such a context contains the list of *identifiers* assigned to the defined indices. Unnamed indices are associated with empty (ϵ) entries in these lists.

An identifier context is well-formed if no index space contains duplicate identifiers.

Conventions

To avoid unnecessary clutter, empty components are omitted when writing out identifier contexts. For example, the record {} is shorthand for an *identifier context* whose components are all empty.

6.1.4 Vectors

Vectors are written as plain sequences, but with a restriction on the length of these sequence.

$$\operatorname{vec}(\mathbf{A}) ::= (x:\mathbf{A})^n \Rightarrow x^n$$
 (if $n < 2^{32}$)

6.2 Lexical Format

6.2.1 Characters

The text format assigns meaning to *source text*, which consists of a sequence of *characters*. Characters are assumed to be represented as valid Unicode³⁹ (Section 2.4) *scalar values*.

Note: While source text may contain any Unicode character in *comments* or *string* literals, the rest of the grammar is formed exclusively from the characters supported by the 7-bit ASCII⁴⁰ subset of Unicode.

6.2. Lexical Format 167

³⁹ https://www.unicode.org/versions/latest/

⁴⁰ https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

6.2.2 Tokens

The character stream in the source text is divided, from left to right, into a sequence of *tokens*, as defined by the following grammar.

```
token ::= keyword |uN| sN |fN| string |id| '('|')' | reserved keyword ::= ('a' | ... | 'z') idchar* (if occurring as a literal terminal in the grammar) reserved ::= idchar<sup>+</sup>
```

Tokens are formed from the input character stream according to the *longest match* rule. That is, the next token always consists of the longest possible sequence of characters that is recognized by the above lexical grammar. Tokens can be separated by *white space*, but except for strings, they cannot themselves contain whitespace.

The set of *keyword* tokens is defined implicitly, by all occurrences of a *terminal symbol* in literal form, such as 'keyword', in a *syntactic* production of this chapter.

Any token that does not fall into any of the other categories is considered reserved, and cannot occur in source text.

Note: The effect of defining the set of reserved tokens is that all tokens must be separated by either parentheses or *white space*. For example, '0\$x' is a single reserved token. Consequently, it is not recognized as two separate tokens '0' and '\$x', but instead disallowed. This property of tokenization is not affected by the fact that the definition of reserved tokens overlaps with other token classes.

6.2.3 White Space

White space is any sequence of literal space characters, formatting characters, or *comments*. The allowed formatting characters correspond to a subset of the ASCII⁴¹ format effectors, namely, horizontal tabulation (U+09), line feed (U+0A), and carriage return (U+0D).

```
space ::= (' ' | format | comment)^*
format ::= U+09 | U+0A | U+0D
```

The only relevance of white space is to separate *tokens*. It is otherwise ignored.

6.2.4 Comments

A *comment* can either be a *line comment*, started with a double semicolon ';;' and extending to the end of the line, or a *block comment*, enclosed in delimiters '(;' . . . ';)'. Block comments can be nested.

Here, the pseudo token eof indicates the end of the input. The *look-ahead* restrictions on the productions for blockchar disambiguate the grammar such that only well-bracketed uses of block comment delimiters are allowed.

Note: Any formatting and control characters are allowed inside comments.

 $^{^{41}}$ https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

6.3 Values

The grammar productions in this section define lexical syntax, hence no white space is allowed.

6.3.1 Integers

All *integers* can be written in either decimal or hexadecimal notation. In both cases, digits can optionally be separated by underscores.

The allowed syntax for integer literals depends on size and signedness. Moreover, their value must lie within the range of the respective type.

Uninterpreted integers can be written as either signed or unsigned, and are normalized to unsigned in the abstract syntax.

6.3.2 Floating-Point

Floating-point values can be represented in either decimal or hexadecimal notation.

```
::= d:digit
            | d:digit '_', p:frac
                                                                           \Rightarrow (d+p/10)/10
            ::= h:hexdigit
                                                                          \Rightarrow h/16
            h:hexdigit '_', p:hexfrac
                                                                          \Rightarrow (h+p/16)/16
            := p:num'.?
float
             p:num '.' q:frac
                                                                          \Rightarrow p+q
                 p:num '.'? ('E' | 'e') \pm:sign e:num
                                                                          \Rightarrow p \cdot 10^{\pm e}
             p:num '.' q:frac ('E' | 'e') \pm:sign e:num
                                                                               (p+q)\cdot 10^{\pm e}
hexfloat ::= '0x' p:hexnum'.'?
            '0x' p:hexnum '.' q:hexfrac
                                                                          \Rightarrow p+q
                  '0x' p:hexnum '.'? ('P' | 'p') ±:sign e:num
                                                                          \Rightarrow p \cdot 2^{\pm e}
                  '0x' p:hexnum '.' q:hexfrac ('P' | 'p') \pm:sign e:num \Rightarrow (p+q) \cdot 2^{\pm e}
```

The value of a literal must not lie outside the representable range of the corresponding IEEE 754-2019⁴² type (that is, a numeric value must not overflow to \pm infinity), but it may be *rounded* to the nearest representable value.

6.3. Values 169

⁴² https://ieeexplore.ieee.org/document/8766229

Note: Rounding can be prevented by using hexadecimal notation with no more significant bits than supported by the required type.

Floating-point values may also be written as constants for *infinity* or *canonical NaN* (*not a number*). Furthermore, arbitrary NaN values may be expressed by providing an explicit payload value.

```
\begin{array}{llll} \mathrm{f} N & ::= & \pm : \mathrm{sign} \, z : \mathrm{f} N \mathrm{mag} & \Rightarrow & \pm z \\ \mathrm{f} N \mathrm{mag} & ::= & z : \mathrm{float} & \Rightarrow & \mathrm{float}_N(z) & (\mathrm{if} \, \mathrm{float}_N(z) \neq \pm \infty) \\ & | & z : \mathrm{hexfloat} & \Rightarrow & \mathrm{float}_N(z) & (\mathrm{if} \, \mathrm{float}_N(z) \neq \pm \infty) \\ & | & \mathrm{inf'} & \Rightarrow & \infty \\ & | & \mathrm{'nan'} & \Rightarrow & \mathrm{nan}(2^{\mathrm{signif}(N)-1}) \\ & | & & \mathrm{'nan:0x'} \, n : \mathrm{hexnum} & \Rightarrow & \mathrm{nan}(n) & (\mathrm{if} \, 1 \leq n < 2^{\mathrm{signif}(N)}) \end{array}
```

6.3.3 Strings

Strings denote sequences of bytes that can represent both textual and binary data. They are enclosed in quotation marks and may contain any character other than $ASCII^{43}$ control characters, quotation marks ('"'), or backslash ('\'), except when expressed with an *escape sequence*.

```
\begin{array}{lll} \text{string} & ::= & ``` (b^*: \text{stringelem})^* ``` & \Rightarrow & \operatorname{concat}((b^*)^*) & \text{ (if } |\operatorname{concat}((b^*)^*)| < 2^{32}) \\ \text{stringelem} & ::= & c: \text{stringchar} & \Rightarrow & \operatorname{utf8}(c) \\ & | & `` n: \text{hexdigit } m: \text{hexdigit} & \Rightarrow & 16 \cdot n + m \\ \end{array}
```

Each character in a string literal represents the byte sequence corresponding to its UTF-8 Unicode⁴⁴ (Section 2.5) encoding, except for hexadecimal escape sequences 'hh', which represent raw bytes of the respective value.

6.3.4 Names

Names are strings denoting a literal character sequence. A name string must form a valid UTF-8 encoding as defined by Unicode⁴⁵ (Section 2.5) and is interpreted as a string of Unicode scalar values.

```
name ::= b^*:string \Rightarrow c^* (if b^* = \text{utf8}(c^*))
```

Note: Presuming the source text is itself encoded correctly, strings that do not contain any uses of hexadecimal byte escapes are always valid names.

⁴³ https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

⁴⁴ https://www.unicode.org/versions/latest/

⁴⁵ https://www.unicode.org/versions/latest/

6.3.5 Identifiers

Indices can be given in both numeric and symbolic form. Symbolic *identifiers* that stand in lieu of indices start with '\$', followed by any sequence of printable ASCII⁴⁶ characters that does not contain a space, quotation mark, comma, semicolon, or bracket.

Conventions

The expansion rules of some abbreviations require insertion of a *fresh* identifier. That may be any syntactically valid identifier that does not already occur in the given source text.

6.4 Types

6.4.1 Number Types

6.4.2 Vector Types

$$vectype_I ::= 'v128' \Rightarrow v128$$

6.4.3 Heap Types

6.4.4 Reference Types

6.4. Types 171

⁴⁶ https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

Abbreviations

There are shorthands for references to abstract heap types.

6.4.5 Value Types

6.4.6 Function Types

```
\begin{array}{llll} \texttt{functype}_I & ::= & `(\text{'`func'}\ t_1^* \colon \texttt{vec}(\texttt{param}_I)\ t_2^* \colon \texttt{vec}(\texttt{result}_I)\ `)' & \Rightarrow & [t_1^*] \to [t_2^*] \\ \texttt{param}_I & ::= & `(\text{'`faram'}\ id^?\ t \colon \texttt{valtype}_I\ `)' & \Rightarrow & t \\ \texttt{result}_I & ::= & `(\text{'`fresult'}\ t \colon \texttt{valtype}_I\ `)' & \Rightarrow & t \\ \end{array}
```

Note: The optional identifier names for parameters in a function type only have documentation purpose. They cannot be referenced from anywhere.

Abbreviations

Multiple anonymous parameters or results may be combined into a single declaration:

```
'(' 'param' valtype* ')' \equiv ('(' 'param' valtype ')')* '(' 'result' valtype* ')' \equiv ('(' 'result' valtype ')')*
```

6.4.7 Limits

```
\begin{array}{cccc} \text{limits} & ::= & n: \text{u32} & \Rightarrow & \{\min n, \max \epsilon\} \\ & | & n: \text{u32} & m: \text{u32} & \Rightarrow & \{\min n, \max m\} \end{array}
```

6.4.8 Memory Types

```
memtype_I ::= lim:limits \Rightarrow lim
```

6.4.9 Table Types

```
tabletype_I ::= lim:limits et:reftype_I \Rightarrow lim et
```

6.4.10 Global Types

6.5 Instructions

Instructions are syntactically distinguished into *plain* and *structured* instructions.

```
instr_I ::= in:plaininstr_I \Rightarrow in
in:blockinstr_I \Rightarrow in
```

In addition, as a syntactic abbreviation, instructions can be written as S-expressions in *folded* form, to group them visually.

6.5.1 Labels

Structured control instructions can be annotated with a symbolic label identifier. They are the only symbolic identifiers that can be bound locally in an instruction sequence. The following grammar handles the corresponding update to the identifier context by composing the context with an additional label entry.

Note: The new label entry is inserted at the *beginning* of the label list in the identifier context. This effectively shifts all existing labels up by one, mirroring the fact that control instructions are indexed relatively not absolutely.

6.5.2 Control Instructions

Structured control instructions can bind an optional symbolic *label identifier*. The same label identifier may optionally be repeated after the corresponding end and else pseudo instructions, to indicate the matching delimiters.

Their *block type* is given as a *type use*, analogous to the type of *functions*. However, the special case of a type use that is syntactically empty or consists of only a single *result* is not regarded as an *abbreviation* for an inline *function type*, but is parsed directly into an optional *value type*.

```
\begin{aligned} \operatorname{blocktype}_I &::= & (t : \operatorname{result}_I)^? &\Rightarrow & t^? \\ &\mid & x, I' : \operatorname{typeuse}_I &\Rightarrow & x & (\operatorname{if} I' = \{\operatorname{locals}(\epsilon)^*\}) \\ \operatorname{blockinstr}_I &::= & \operatorname{'block'} & I' : \operatorname{label}_I & bt : \operatorname{blocktype}_I & (in : \operatorname{instr}_{I'})^* & \operatorname{'end'} & \operatorname{id}^? \\ &\Rightarrow & \operatorname{block} & bt & in^* & \operatorname{end} & (\operatorname{if} & \operatorname{id}^? = \epsilon \vee \operatorname{id}^? = \operatorname{label}) \\ &\mid & \operatorname{'loop'} & I' : \operatorname{label}_I & bt : \operatorname{blocktype}_I & (in : \operatorname{instr}_{I'})^* & \operatorname{'end'} & \operatorname{id}^? \\ &\Rightarrow & \operatorname{loop} & bt & in^* & \operatorname{end} & (\operatorname{if} & \operatorname{id}^? = \epsilon \vee \operatorname{id}^? = \operatorname{label}) \\ &\mid & \operatorname{'if'} & I' : \operatorname{label}_I & bt : \operatorname{blocktype}_I & (in_1 : \operatorname{instr}_{I'})^* & \operatorname{'else'} & \operatorname{id}^? & (in_2 : \operatorname{instr}_{I'})^* & \operatorname{'end'} & \operatorname{id}^? \\ &\Rightarrow & \operatorname{if} & bt & in_1^* & \operatorname{else} & in_2^* & \operatorname{end} & (\operatorname{if} & \operatorname{id}^? = \epsilon \vee \operatorname{id}^? = \operatorname{label}) & \end{aligned}
```

6.5. Instructions

Note: The side condition stating that the *identifier context* I' must only contain unnamed entries in the rule for typeuse block types enforces that no identifier can be bound in any param declaration for a block type.

All other control instruction are represented verbatim.

```
plaininstr_I ::=
                         'unreachable'
                                                                                           ⇒ unreachable
                           'nop'
                                                                                           \Rightarrow nop
                           'br' l:labelidx_I
                                                                                           \Rightarrow br l
                           'br_if' l:labelidx_I
                                                                                           \Rightarrow br_if l
                           \texttt{`br\_table'}\ l^* : \texttt{vec}(\texttt{labelidx}_I)\ l_N : \texttt{labelidx}_I \ \Rightarrow \ \mathsf{br\_table}\ l^*\ l_N
                           \verb"br_on_null" $l$: labelidx_I
                                                                                          \Rightarrow br_on_null l
                           \verb"br_on_non_null" l:labelidx_I
                                                                                         \Rightarrow br_on_non_null l
                           'return'
                                                                                          \Rightarrow return
                           'call' x: funcidx_I
                                                                                           \Rightarrow call x
                           'call ref'
                                                                                           \Rightarrow call ref
                           'call_indirect' x:tableidx y, I':typeuseI \Rightarrow \text{call_indirect } x y \quad (\text{if } I' = \{ \text{locals } (\epsilon)^* \})
```

Note: The side condition stating that the *identifier context* I' must only contain unnamed entries in the rule for call_indirect enforces that no identifier can be bound in any param declaration appearing in the type annotation.

Abbreviations

The 'else' keyword of an 'if' instruction can be omitted if the following instruction sequence is empty.

```
'if' label blocktype_I instr^* 'end' \equiv 'if' label blocktype_I instr^* 'else' 'end'
```

Also, for backwards compatibility, the table index to 'call_indirect' can be omitted, defaulting to 0.

```
'call_indirect' typeuse \equiv 'call_indirect' 0 typeuse
```

6.5.3 Reference Instructions

6.5.4 Parametric Instructions

6.5.5 Variable Instructions

6.5.6 Table Instructions

Abbreviations

For backwards compatibility, all *table indices* may be omitted from table instructions, defaulting to 0.

```
'table.get' \equiv 'table.get' '0'
'table.set' \equiv 'table.set' '0'
'table.size' \equiv 'table.size' '0'
'table.grow' \equiv 'table.grow' '0'
'table.fill' \equiv 'table.fill' '0'
'table.copy' \equiv 'table.copy' '0' '0'
'table.init' x:=== 'table.init' '0' x:=====
```

6.5. Instructions

6.5.7 Memory Instructions

The offset and alignment immediates to memory instructions are optional. The offset defaults to 0, the alignment to the storage size of the respective memory access, which is its *natural alignment*. Lexically, an offset or align phrase is considered a single *keyword token*, so no *white space* is allowed around the '='.

```
:= o:offset a:align_N
                                                            \Rightarrow {align n, offset o} (if a = 2^n)
memarg_N
offset
                  ::= 'offset='0:u32
                                                            \Rightarrow o
                  \epsilon
                                                            \Rightarrow 0
                       'align='a:u32
{\tt align}_N
                  ::=
                                                            \Rightarrow a
                                                            \Rightarrow N
                  \epsilon
plaininstr_I ::= ...
                        'i32.load' m:memarg<sub>4</sub> \Rightarrow i32.load m
                                                          \Rightarrow i64.load m
                        'i64.load' m:memarg<sub>8</sub>
                        'f32.load' m:memarg_4
                                                          \Rightarrow f32.load m
                        'f64.load' m:memarg_8
                                                          \Rightarrow f64.load m
                        \verb"i32.load8_s" \ m : \verb"memarg"_1 \quad \Rightarrow \quad \verb"i32.load8_s" \ m
                         \verb"i32.load8_u" \ m : \verb"memarg"_1 \quad \Rightarrow \quad \verb"i32.load8_u" \ m
                         'i32.load16_s' m:memarg_2 \Rightarrow i32.load16\_s m
                        'i32.load16_u' m:memarg_2 \Rightarrow i32.load16_u m
                        'i64.load8_s' m:memarg<sub>1</sub> \Rightarrow i64.load8_s m
                         'i64.load8_u' m:memarg<sub>1</sub> \Rightarrow i64.load8_u m
                         'i64.load16_s' m:memarg_2 \Rightarrow i64.load16 s m
                         'i64.load16_u' m:memarg_2 \Rightarrow i64.load16_u m
                         'i64.load32_s' m:memarg<sub>4</sub> \Rightarrow i64.load32_s m
                         'i64.load32_u' m:memarg_4 \Rightarrow i64.load32\_u m
                         'i32.store' m:memarg<sub>4</sub> \Rightarrow i32.store m
                                                          \Rightarrow i64.store m
                         'i64.store' m:memarg_8
                                                          \Rightarrow f32.store m
                         'f32.store' m:memarg<sub>4</sub>
                         'f64.store' m:memarg<sub>8</sub>
                                                          \Rightarrow f64.store m
                         'i32.store8' m:memarg<sub>1</sub> \Rightarrow i32.store8 m
                         'i32.store16' m:memarg<sub>2</sub> \Rightarrow i32.store16 m
                         'i64.store8' m:memarg_1
                                                            \Rightarrow i64.store8 m
                                                          \Rightarrow i64.store16 m
                         'i64.store16' m:memarg<sub>2</sub>
                         'i64.store32' m:memarg<sub>4</sub> \Rightarrow i64.store32 m
                         'memory.size'
                                                           ⇒ memory.size
                         'memory.grow'
                                                          ⇒ memory.grow
                         'memory.fill'
                                                          ⇒ memory.fill
                         'memory.copy'
                                                          ⇒ memory.copy
                         \hbox{`memory.init'} \ x\hbox{:} \hbox{dataidx}_I \quad \Rightarrow \quad \hbox{memory.init} \ x
                         'data.drop' x:dataidx<sub>I</sub> \Rightarrow data.drop x
```

6.5.8 Numeric Instructions

```
plaininstr_I ::= ...
                         'i32.const' n:i32 \Rightarrow i32.const n
                         'i64.const' n:i64 \Rightarrow i64.const n
                         \texttt{`f32.const'}\ z \texttt{:} \texttt{f32} \ \Rightarrow \ \texttt{f32.const}\ z
                        'f64.const' z:f64 \Rightarrow f64.const z
                     'i32.clz'
                                       \Rightarrow i32.clz
                      'i32.ctz'
                                       ⇒ i32.ctz
                      'i32.popcnt' \Rightarrow i32.popcnt
                      'i32.add' \Rightarrow i32.add
                     'i32.sub'
                                      ⇒ i32.sub
                     'i32.mul'
                                       ⇒ i32.mul
                      'i32.div_s' \Rightarrow i32.div_s
                      "i32.div_u" \Rightarrow i32.div_u"
                      'i32.rem_s' \Rightarrow i32.rem_s
                      'i32.rem_u' \Rightarrow i32.rem_u
                     'i32.and' \Rightarrow i32.and
                     'i32.or'
                                      \Rightarrow i32.or
                     'i32.xor'
                                     \Rightarrow i32.xor
                      'i32.shl' ⇒ i32.shl
                      i32.shr_s' \Rightarrow i32.shr_s
                      \text{`i32.shr\_u'} \quad \Rightarrow \quad \text{i32.shr\_u}
                                     ⇒ i32.rotl
                      'i32.rotl'
                      'i32.rotr'
                                      \Rightarrow i32.rotr
                      'i64.clz'
                                       ⇒ i64.clz
                      'i64.ctz'
                                       \Rightarrow i64.ctz
                      'i64.popcnt' \Rightarrow i64.popcnt
                     'i64.add' \Rightarrow i64.add
                     'i64.sub'
                                      ⇒ i64.sub
                     'i64.mul' ⇒ i64.mul
                      i64.div_s \Rightarrow i64.div_s
                      \text{`i64.div\_u'} \Rightarrow \text{i64.div\_u}
                      'i64.rem_s'
                                        ⇒ i64.rem s
                      'i64.rem_u'
                                       ⇒ i64.rem_u
                      'i64.and' \Rightarrow i64.and
                                      \Rightarrow i64.or
                      'i64.or'
                      'i64.xor'
                                      \Rightarrow i64.xor
                      'i64.shl'
                                      \Rightarrow i64.shl
                      i64.shr_s' \Rightarrow i64.shr_s
                      'i64.shr_u' ⇒ i64.shr_u
                      \begin{array}{lll} \mbox{`i64.rotl'} & \Rightarrow & \mbox{i64.rotl} \\ \mbox{`i64.rotr'} & \Rightarrow & \mbox{i64.rotr} \end{array}
```

```
'f32.abs'
                        \Rightarrow f32.abs
 'f32.neg'
                          \Rightarrow f32.neg
'f32.ceil' ⇒ f32.ceil

'f32.floor' ⇒ f32.floor

'f32.trunc' ⇒ f32.trunc
'f32.ceil'
'f32.nearest' \Rightarrow f32.nearest
'f32.sqrt' \Rightarrow f32.sqrt
'f32.add' \Rightarrow f32.add
'f32.sub'
'f32.mul'

⇒ f32.sub

                         ⇒ f32.mul
 'f32.div'
                        ⇒ f32.div
'f32.min' ⇒ f32.min
'f32.max' ⇒ f32.max
\texttt{`f32.copysign'} \ \Rightarrow \ \mathsf{f32.copysign}
                      \Rightarrow f64.abs
'f64.abs'
'f64.neg'
                        \Rightarrow f64.neg
'f64.ceil'
                       ⇒ f64.ceil
'f64.floor' ⇒ f64.floor
'f64.trunc' ⇒ f64.trunc
                          ⇒ f64.trunc
'f64.nearest' ⇒ f64.nearest
'f64.sqrt' ⇒ f64.sqrt
'f64.add' → f64.add
'f64.add' ⇒ f64.add

'f64.sub' ⇒ f64.sub

'f64.mul' ⇒ f64.mul

'f64.div' ⇒ f64.div
'f64.min'
'f64.copysign' \Rightarrow f64.copysign
 i32.eqz' ⇒ i32.eqz

'i32.eq' ⇒ i32.eq

'i32.ne' ⇒ :00
 'i32.ne' ⇒ i32.ne

'i32.lt_s' ⇒ i32.lt_s

'i32.lt_u' ⇒ i32.lt_u
 i32.gt_s \Rightarrow i32.gt_s
 'i32.gt_u' ⇒ i32.gt_u
  i32.le_s \Rightarrow i32.le_s
  \begin{array}{ccc} \text{`i32.le\_u'} & \Rightarrow & \text{i32.le\_u} \\ \text{`i32.ge\_s'} & \Rightarrow & \text{i32.ge\_s} \\ \end{array}
 'i32.ge_u' ⇒ i32.ge_u
 \begin{array}{lll} \text{`i64.eqz'} & \Rightarrow & \text{i64.eqz} \\ \text{`i64.eq'} & \Rightarrow & \text{i64.eq} \\ \text{`i64.ne'} & \Rightarrow & \text{i64.ne} \\ \end{array}
                         \Rightarrow i64.eqz
 'i64.ne' ⇒ i64.ne
'i64.lt_s' ⇒ i64.lt_s
'i64.lt_u' ⇒ i64.lt_u
 i64.gt_s' \Rightarrow i64.gt_s
  i64.gt_u' \Rightarrow i64.gt_u
  i64.le_s \Rightarrow i64.le_s
  'i64.le_u' ⇒ i64.le_u

'i64.ge_s' ⇒ i64.ge_s

'i64.ge_u' ⇒ i64.ge_u
```

```
'f32.eq'
                           \Rightarrow f32.eq
       'f32.ne'
                           \Rightarrow f32.ne
       'f32.1t'
                          \Rightarrow f32.lt
       'f32.gt'
                        \Rightarrow f32.gt
       'f32.le'
                        \Rightarrow f32.le
       'f32.ge'

⇒ f32.ge

                         \Rightarrow f64.eq
       'f64.eq'
       'f64.ne'
                        \Rightarrow f64.ne

⇒ f64.lt

       'f64.lt'
       'f64.gt'
                        \Rightarrow f64.gt
       'f64.le'

⇒ f64.le

       'f64.ge'
                        \Rightarrow f64.ge

      'i32.wrap_i64'
      ⇒ i32.wrap_i64

      'i32.trunc_f32_s'
      ⇒ i32.trunc_f32_s

      'i32.trunc_f32_u'
      ⇒ i32.trunc_f32_u

      'i32.trunc_f64_s'
      ⇒ i32.trunc_f64_s

      'i32.trunc_f64_u'
      ⇒ i32.trunc_f64_u

'i32.trunc_sat_f32_s' \Rightarrow i32.trunc_sat_f32_s
i32.trunc_sat_f32_u' \Rightarrow i32.trunc_sat_f32_u
'i32.trunc_sat_f64_s' \Rightarrow i32.trunc_sat_f64_s
\verb|`i32.trunc_sat_f64_u'| \Rightarrow | i32.trunc_sat_f64_u| \\
'i64.extend_i32_s' ⇒ i64.extend_i32_s
'i64.extend_i32_u' ⇒ i64.extend_i32_u
'i64.trunc_f32_s' ⇒ i64.trunc_f32_s
'i64.trunc_f64_s' ⇒ i64.trunc_f64_s
'i64.trunc_f64_u' ⇒ i64.trunc_f64_u
'i64.trunc_sat_f32_s' \Rightarrow i64.trunc_sat_f32_s
'i64.trunc_sat_f32_u' ⇒ i64.trunc_sat_f32_u
'i64.trunc_sat_f64_s' \Rightarrow i64.trunc_sat_f64_s
'i64.trunc_sat_f64_u' ⇒ i64.trunc_sat_f64_u
\begin{tabular}{llll} `f32.convert\_i32\_s' & $\Rightarrow$ & $f32.convert\_i32\_s' \\ `f32.convert\_i32\_u' & $\Rightarrow$ & $f32.convert\_i32\_u$ \\ \end{tabular}
'f32.convert_i64_s' \Rightarrow f32.convert_i64 s
`f64.convert_i32_s' \Rightarrow f64.convert_i32_s
^{\circ} f64.convert_i64_u' \Rightarrow f64.convert_i64_u
'f64.promote f32' \Rightarrow f64.promote f32
'i32.reinterpret f32' ⇒ i32.reinterpret f32
'i64.reinterpret_f64' ⇒ i64.reinterpret_f64
'f32.reinterpret_i32' ⇒ f32.reinterpret_i32
'f64.reinterpret_i64' ⇒ f64.reinterpret_i64
    'i32.extend8_s' \Rightarrow i32.extend8_s
    'i32.extend16_s' \Rightarrow i32.extend16_s
    'i64.extend8_s' \Rightarrow i64.extend8_s
    i64.extend16_s \Rightarrow i64.extend16_s
    'i64.extend32_s' \Rightarrow i64.extend32_s
```

6.5.9 Vector Instructions

Vector memory instructions have optional offset and alignment immediates, like the memory instructions.

```
plaininstr_I ::=
                       'v128.load' m:memarg_{16}
                                                                             \Rightarrow v128.load m
                       'v128.load8x8_s' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load8x8_s m
                       'v128.load8x8_u' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load8x8 u m
                       'v128.load16x4_s' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load16x4_s m
                       'v128.load16x4_u' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load16x4 u m
                       'v128.load32x2_s' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load32x2 s m
                       \verb|`v128.load32x2_u'| m: memarg_8|
                                                                             \Rightarrow v128.load32x2 u m
                       'v128.load8_splat' m:memarg<sub>1</sub>
                                                                             \Rightarrow v128.load8_splat m
                                                                             \Rightarrow v128.load16_splat m
                       'v128.load16_splat' m:memarg2
                       'v128.load32_splat' m:memarg<sub>4</sub>
                                                                             \Rightarrow v128.load32 splat m
                       'v128.load64_splat' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load64_splat m
                       'v128.load32_zero' m:memarg4
                                                                             \Rightarrow v128.load32_zero m
                       'v128.load64_zero' m:memarg<sub>8</sub>
                                                                             \Rightarrow v128.load64 zero m
                       'v128.store' m:memarg_{16}
                                                                             \Rightarrow v128.store m
                       'v128.load8_lane' m:memarg<sub>1</sub> laneidx:u8
                                                                             \Rightarrow v128.load8 lane m \ lane idx
                                                                             \Rightarrow v128.load16_lane m \ lane idx
                       'v128.load16_lane' m:memarg2 laneidx:u8
                                                                             \Rightarrow v128.load32_lane m \ lane idx
                       'v128.load32_lane' m:memarg4 laneidx:u8
                       'v128.load64_lane' m:memarg<sub>8</sub> laneidx:u8
                                                                             \Rightarrow v128.load64 lane m \ lane idx
                       'v128.store8_lane' m:memarg<sub>1</sub> laneidx:u8
                                                                             \Rightarrow v128.store8_lane m \ lane idx
                       'v128.store16_lane' m:memarg_ laneidx:u8 \Rightarrow v128.store16_lane m laneidx
                       'v128.store32_lane' m:memarg<sub>4</sub> laneidx:u8
                                                                             \Rightarrow v128.store32_lane m \ lane idx
                       'v128.store64_lane' m:memarg_8 laneidx:u8 \Rightarrow v128.store64_lane m laneidx
```

Vector constant instructions have a mandatory *shape* descriptor, which determines how the following values are parsed.

```
\Rightarrow \text{ v128.const bytes}_{i128}^{-1}(\text{bytes}_{i8}(n)^{16})
\Rightarrow \text{ v128.const bytes}_{i128}^{-1}(\text{bytes}_{i16}(n)^{8})
\Rightarrow \text{ v128.const bytes}_{i128}^{-1}(\text{bytes}_{i32}(n)^{4})
\Rightarrow \text{ v128.const bytes}_{i128}^{-1}(\text{bytes}_{i64}(n)^{2})
\Rightarrow \text{ v128.const bytes}_{i128}^{-1}(\text{bytes}_{f32}(z)^{4})
\Rightarrow \text{ v128.const bytes}_{i128}^{-1}(\text{bytes}_{i64}(n)^{2})
'v128.const' 'i8x16' (n:i8)<sup>16</sup>
'v128.const' 'i16x8' (n:i16)^8
'v128.const' 'i32x4' (n:i32)^4 'v128.const' 'i64x2' (n:i64)^2
'v128.const' 'f32x4' (z:f32)^4
'v128.const' 'f64x2' (z:f64)^2
                                                                                   \Rightarrow v128.const bytes_{i128}^{-1}(bytes_{f64}(z)^2)
'i8x16.shuffle' (laneidx:u8)^{16}
                                                                                   \Rightarrow i8x16.shuffle laneidx^{16}
'i8x16.swizzle'
                                                                                            i8x16.swizzle
'i8x16.splat'
                                                                                   \Rightarrow i8x16.splat
'i16x8.splat'
                                                                                   \Rightarrow i16x8.splat
'i32x4.splat'
                                                                                   \Rightarrow i32x4.splat
'i64x2.splat'
                                                                                   \Rightarrow i64x2.splat
'f32x4.splat'
                                                                                   \Rightarrow f32x4.splat
'f64x2.splat'
                                                                                   \Rightarrow f64x2.splat
```

```
'i8x16.extract_lane_s' laneidx:u8
                                                    i8x16.extract_lane_s laneidx
'i8x16.extract_lane_u' laneidx:u8
                                                   i8x16.extract lane u laneidx
'i8x16.replace_lane' laneidx:u8
                                               \Rightarrow i8x16.replace lane laneidx
'i16x8.extract_lane_s' laneidx:u8
                                               \Rightarrow i16x8.extract lane s laneidx
'i16x8.extract_lane_u' laneidx:u8
                                               \Rightarrow i16x8.extract_lane_u laneidx
'i16x8.replace_lane' laneidx:u8
                                               \Rightarrow i16x8.replace_lane laneidx
'i32x4.extract lane' laneidx:u8
                                               \Rightarrow i32x4.extract lane laneidx
'i32x4.replace lane' laneidx:u8
                                               \Rightarrow i32×4.replace lane laneidx
'i64x2.extract lane' laneidx:u8
                                               \Rightarrow i64x2.extract lane laneidx
'i64x2.replace_lane' laneidx:u8
                                               \Rightarrow i64x2.replace_lane laneidx
'f32x4.extract_lane' laneidx:u8
                                               \Rightarrow f32x4.extract lane laneidx
'f32x4.replace_lane' laneidx:u8
                                               \Rightarrow f32x4.replace_lane laneidx
'f64x2.extract_lane' laneidx:u8
                                               \Rightarrow f64x2.extract_lane laneidx
'f64x2.replace_lane' laneidx:u8
                                               \Rightarrow f64x2.replace_lane laneidx
'i8x16.eq'
                                               \Rightarrow i8x16.eq
'i8x16.ne'
                                               \Rightarrow i8x16.ne
'i8x16.lt s'
                                               \Rightarrow i8x16.lt s
'i8x16.lt_u'
                                               \Rightarrow i8x16.lt u
'i8x16.gt_s'
                                               \Rightarrow i8x16.gt s
'i8x16.gt u'
                                               \Rightarrow i8x16.gt u
'i8x16.le s'
                                               \Rightarrow i8x16.le s
'i8x16.le u'
                                               \Rightarrow i8x16.le u
'i8x16.ge_s'
                                               \Rightarrow i8x16.ge_s
'i8x16.ge_u'
                                               \Rightarrow i8x16.ge_u
'i16x8.eq'
                                               \Rightarrow i16x8.eq
'i16x8.ne'
                                               \Rightarrow i16x8.ne
'i16x8.lt s'
                                               \Rightarrow i16x8.lt s
'i16x8.lt u'
                                               \Rightarrow i16x8.lt u
'i16x8.gt s'
                                               \Rightarrow i16x8.gt s
'i16x8.gt_u'
                                               \Rightarrow i16x8.gt_u
'i16x8.le s'
                                               \Rightarrow i16x8.le s
'i16x8.le u'
                                               \Rightarrow i16x8.le u
                                               \Rightarrow i16x8.ge_s
'i16x8.ge_s'
'i16x8.ge_u'
                                               \Rightarrow i16x8.ge_u
'i32x4.eq'
                                               \Rightarrow i32x4.eq
'i32x4.ne'
                                               \Rightarrow i32x4.ne
'i32x4.1t s'
                                               \Rightarrow i32x4.lt s
'i32x4.1t u'
                                               \Rightarrow i32x4.lt u
'i32x4.gt s'
                                               \Rightarrow i32x4.gt s
'i32x4.gt_u'
                                               \Rightarrow i32x4.gt u
'i32x4.le s'
                                               \Rightarrow i32x4.le s
'i32x4.le u'
                                               \Rightarrow i32x4.le u
'i32x4.ge_s'
                                               \Rightarrow i32x4.ge_s
'i32x4.ge_u'
                                               \Rightarrow i32x4.ge_u
'i64x2.eq'
                                               \Rightarrow i64x2.eq
'i64x2.ne'
                                               \Rightarrow i64x2.ne
'i64x2.lt s'
                                               \Rightarrow i64x2.lt s
'i64x2.gt_s'
                                               \Rightarrow i64x2.gt_s
'i64x2.le_s'
                                               \Rightarrow i64x2.le s
'i64x2.ge_s'
                                               \Rightarrow i64x2.ge_s
```

```
'f32x4.eq'
                                                  \Rightarrow f32x4.eq
                                                  \Rightarrow f32x4.ne
'f32x4.ne'
'f32x4.1t'
                                                  \Rightarrow f32x4.lt
'f32x4.gt'
                                                  \Rightarrow f32x4.gt
'f32x4.le'
                                                  \Rightarrow f32x4.le
'f32x4.ge'
                                                  \Rightarrow f32x4.ge
'f64x2.eq'
                                                  \Rightarrow f64x2.eq
'f64x2.ne'
                                                  \Rightarrow f64x2.ne
'f64x2.1t'
                                                  \Rightarrow f64x2.lt
'f64x2.gt'
                                                  \Rightarrow f64x2.gt
'f64x2.le'
                                                  \Rightarrow f64x2.le
'f64x2.ge'
                                                  \Rightarrow f64x2.ge
'v128.not'
                                                  \Rightarrow v128.not
'v128.and'
                                                  \Rightarrow v128.and
'v128.andnot'
                                                  ⇒ v128.andnot
'v128.or'
                                                  \Rightarrow v128.or
'v128.xor'
                                                  \Rightarrow v128.xor
'v128.bitselect'
                                                  ⇒ v128.bitselect
'v128.any_true'
                                                  \Rightarrow v128.any_true
'i8x16.abs'
                                                  \Rightarrow i8x16.abs
                                                  \Rightarrow i8x16.neg
'i8x16.neg'
'i8x16.all_true'
                                                  \Rightarrow i8x16.all_true
'i8x16.bitmask'
                                                 \Rightarrow i8×16.bitmask
'i8x16.narrow_i16x8_s'
                                                 \Rightarrow i8x16.narrow_i16x8_s
\verb|`i8x16.narrow_i16x8_u||\\
                                                  \Rightarrow \quad \mathsf{i8x}16.\mathsf{narrow\_i}16\mathsf{x}8\_\mathsf{u}
'i8x16.shl'
                                                  \Rightarrow i8x16.shl
'i8x16.shr_s'
                                                  \Rightarrow i8x16.shr_s
'i8x16.shr_u'
                                                 ⇒ i8x16.shr_u
'i8x16.add'
                                                 \Rightarrow i8x16.add
'i8x16.add_sat_s'
                                                 \Rightarrow i8x16.add_sat_s
'i8x16.add_sat_u'
                                                  \Rightarrow i8x16.add_sat_u
'i8x16.sub'
                                                  \Rightarrow i8x16.sub
'i8x16.sub_sat_s'
                                                  \Rightarrow i8x16.sub_sat_s
'i8x16.sub sat u'
                                                  \Rightarrow i8x16.sub sat u
'i8x16.min s'
                                                  \Rightarrow i8x16.min s
'i8x16.min_u'
                                                  \Rightarrow i8x16.min_u
'i8x16.max_s'
                                                  \Rightarrow i8x16.max_s
'i8x16.max u'
                                                 \Rightarrow i8x16.max u
'i8x16.avgr_u'
                                                 ⇒ i8x16.avgr_u
'i8x16.popcnt'
                                                 \Rightarrow i8x16.popcnt
```

```
'i16x8.abs'
                                           \Rightarrow i16x8.abs
'i16x8.neg'
                                           \Rightarrow i16x8.neg
'i16x8.all true'
                                          \Rightarrow i16x8.all true
                                          \Rightarrow i16x8.bitmask
'i16x8.bitmask'
                                          ⇒ i16x8.narrow_i32x4_s
'i16x8.narrow_i32x4_s'
'i16x8.narrow_i32x4_u'
                                          ⇒ i16x8.narrow_i32x4_u
'i16x8.extend_low_i8x16_s'
                                          \Rightarrow i16x8.extend low i8x16 s
'i16x8.extend_high_i8x16_s'
                                          \Rightarrow i16x8.extend high i8x16 s
'i16x8.extend_low_i8x16_u'
                                           \Rightarrow i16x8.extend low i8x16 u
'i16x8.extend_high_i8x16_u'
                                           ⇒ i16x8.extend_high_i8x16_u
'i16x8.shl'
                                          \Rightarrow i16x8.shl
'i16x8.shr s'
                                          \Rightarrow i16x8.shr s
'i16x8.shr_u'
                                          \Rightarrow i16x8.shr_u
'i16x8.add'
                                          \Rightarrow i16x8.add
'i16x8.add_sat_s'
                                          \Rightarrow i16x8.add_sat_s
'i16x8.add_sat_u'
                                          \Rightarrow i16x8.add_sat_u
'i16x8.sub'
                                           \Rightarrow i16x8.sub
'i16x8.sub sat s'
                                           \Rightarrow i16x8.sub sat s
'i16x8.sub_sat_u'
                                          ⇒ i16x8.sub_sat_u
'i16x8.mul'
                                           \Rightarrow i16x8.mul
'i16x8.min s'
                                           \Rightarrow i16x8.min s
'i16x8.min u'
                                           \Rightarrow i16x8.min u
'i16x8.max s'
                                           \Rightarrow i16x8.max s
\verb|`i16x8.max_u'|
                                           \Rightarrow i16x8.max_u
'i16x8.avgr_u'
                                           \Rightarrow i16x8.avgr_u
'i16x8.q15mulr_sat_s'
                                          \Rightarrow i16x8.q15mulr sat s
'i16x8.extmul_low_i8x16_s'
                                          ⇒ i16x8.extmul_low_i8x16_s
                                          \Rightarrow i16x8.extmul high i8x16 s
'i16x8.extmul high i8x16 s'
'i16x8.extmul_low_i8x16_u'
                                          ⇒ i16x8.extmul_low_i8x16_u
'i16x8.extmul_high_i8x16_u'
                                           \Rightarrow i16x8.extmul high i8x16 u
'i16x8.extadd_pairwise_i8x16_s'
                                           ⇒ i16x8.extadd_pairwise_i8x16_s
'i16x8.extadd_pairwise_i8x16_u'
                                           ⇒ i16x8.extadd_pairwise_i8x16_u
'i32x4.abs'
                                           \Rightarrow i32x4.abs
'i32x4.neg'
                                           \Rightarrow i32x4.neg
'i32x4.all_true'
                                           \Rightarrow i32x4.all_true
'i32x4.bitmask'
                                           ⇒ i32×4.bitmask
'i32x4.extadd_pairwise_i16x8_s'
                                          ⇒ i32x4.extadd_pairwise_i16x8_s
                                          ⇒ i32x4.extend_low_i16x8_s
'i32x4.extend_low_i16x8_s'
'i32x4.extend_high_i16x8_s'
                                           ⇒ i32x4.extend_high_i16x8_s
'i32x4.extend_low_i16x8_u'
                                          ⇒ i32x4.extend_low_i16x8_u
\verb|`i32x4.extend_high_i16x8_u||\\
                                          ⇒ i32x4.extend_high_i16x8_u
'i32x4.shl'
                                           \Rightarrow i32x4.shl
'i32x4.shr s'
                                           \Rightarrow i32x4.shr s
'i32x4.shr u'
                                           \Rightarrow i32x4.shr u
'i32x4.add'
                                           \Rightarrow i32x4.add
'i32x4.sub'
                                           \Rightarrow i32x4.sub
'i32x4.mul'
                                           \Rightarrow i32x4.mul
'i32x4.min_s'
                                           \Rightarrow i32x4.min s
\verb|`i32x4.min_u'|
                                           \Rightarrow i32x4.min_u
'i32x4.max_s'
                                           \Rightarrow i32x4.max_s
'i32x4.max u'
                                          \Rightarrow i32x4.max u
'i32x4.dot i16x8 s'
                                          \Rightarrow i32x4.dot_i16x8_s
'i32x4.extmul_low_i16x8_s'
                                          ⇒ i32x4.extmul_low_i16x8_s
'i32x4.extmul_high_i16x8_s'
                                          \Rightarrow i32x4.extmul_high_i16x8_s
'i32x4.extmul_low_i16x8_u'
                                          \Rightarrow i32x4.extmul low i16x8 u
                                          \Rightarrow i32x4.extmul_high_i16x8_u
'i32x4.extmul_high_i16x8_u'
```

```
'i64x2.abs'
                                           \Rightarrow i64x2.abs
'i64x2.neg'
                                           \Rightarrow i64x2.neg
'i64x2.all true'
                                          \Rightarrow i64x2.all true
                                          ⇒ i64x2.bitmask
'i64x2.bitmask'
'i64x2.extend_low_i32x4_s'
                                         ⇒ i64x2.extend_low_i32x4_s
'i64x2.extend_high_i32x4_s'
                                         \Rightarrow i64x2.extend_high_i32x4_s
'i64x2.extend low i32x4 u'
                                          \Rightarrow i64x2.extend low i32x4 u
'i64x2.extend_high_i32x4_u'
                                          ⇒ i64x2.extend_high_i32x4_u
'i64x2.shl'
                                           \Rightarrow i64x2.shl
'i64x2.shr_s'
                                           \Rightarrow i64x2.shr_s
'i64x2.shr u'
                                           \Rightarrow i64x2.shr u
                                          \Rightarrow i64×2.add
'i64x2.add'
'i64x2.sub'
                                          \Rightarrow i64x2.sub
'i64x2.mul'
                                          \Rightarrow i64x2.mul
'i64x2.extmul_low_i32x4_s'
                                          ⇒ i64x2.extmul_low_i32x4_s
'i64x2.extmul_high_i32x4_s'
                                          ⇒ i64x2.extmul_high_i32x4_s
'i64x2.extmul_low_i32x4_u'
                                          ⇒ i64x2.extmul_low_i32x4_u
'i64x2.extmul_high_i32x4_u'
                                          ⇒ i64x2.extmul_high_i32x4_u
'f32x4.abs'
                                           \Rightarrow f32x4.abs
'f32x4.neg'
                                           \Rightarrow f32x4.neg
'f32x4.sqrt'
                                           \Rightarrow f32x4.sart
'f32x4.add'
                                           \Rightarrow f32x4.add
                                           \Rightarrow f32x4.sub
'f32x4.sub'
'f32x4.mul'
                                           \Rightarrow f32x4.mul
'f32x4.div'
                                           \Rightarrow f32x4.div
                                           \Rightarrow f32x4.min
'f32x4.min'
'f32x4.max'
                                           \Rightarrow f32x4.max
'f32x4.pmin'
                                           \Rightarrow f32x4.pmin
'f32x4.pmax'
                                           \Rightarrow f32x4.pmax
'f64x2.abs'
                                           \Rightarrow f64x2.abs
'f64x2.neg'
                                           \Rightarrow f64x2.neg
'f64x2.sqrt'
                                           \Rightarrow f64x2.sqrt
'f64x2.add'
                                           \Rightarrow f64x2.add
                                           \Rightarrow f64x2.sub
'f64x2.sub'
                                           \Rightarrow f64x2.mul
'f64x2.mul'
'f64x2.div'
                                           \Rightarrow f64x2.div
'f64x2.min'
                                           \Rightarrow f64x2.min
'f64x2.max'
                                           \Rightarrow f64x2.max
'f64x2.pmin'
                                           \Rightarrow f64x2.pmin
'f64x2.pmax'
                                          \Rightarrow f64x2.pmax
'i32x4.trunc sat f32x4 s'
                                          \Rightarrow i32x4.trunc sat f32x4 s
'i32x4.trunc_sat_f32x4_u'
                                          ⇒ i32x4.trunc_sat_f32x4_u
'i32x4.trunc_sat_f64x2_s_zero'
                                          ⇒ i32x4.trunc_sat_f64x2_s_zero
'i32x4.trunc_sat_f64x2_u_zero'
                                         ⇒ i32x4.trunc_sat_f64x2_u_zero
'f32x4.convert_i32x4_s'
                                         \Rightarrow f32x4.convert_i32x4_s
'f32x4.convert_i32x4_u'
                                         \Rightarrow f32x4.convert_i32x4_u
'f64x2.convert_low_i32x4_s'
                                         ⇒ f64x2.convert_low_i32x4_s
                                         ⇒ f64x2.convert_low_i32x4_u
'f64x2.convert_low_i32x4_u'
'f32x4.demote f64x2 zero'
                                          \Rightarrow f32x4.demote f64x2 zero
'f64x2.promote_low_f32x4'
                                         \Rightarrow f64x2.promote_low_f32x4
```

6.5.10 Folded Instructions

Instructions can be written as S-expressions by grouping them into *folded* form. In that notation, an instruction is wrapped in parentheses and optionally includes nested folded instructions to indicate its operands.

In the case of *block instructions*, the folded form omits the 'end' delimiter. For if instructions, both branches have to be wrapped into nested S-expressions, headed by the keywords 'then' and 'else'.

The set of all phrases defined by the following abbreviations recursively forms the auxiliary syntactic class foldedinstr. Such a folded instruction can appear anywhere a regular instruction can.

```
'('plaininstr foldedinstr*')' \(\equiv \text{foldedinstr* plaininstr}\)' (''block' label blocktype instr*')' \(\equiv \text{'block' label blocktype instr*'} \text{'end'}\)' (''loop' label blocktype instr*')' \(\equiv \text{'loop' label blocktype instr*' end'}\)' (''if' label blocktype foldedinstr*' (''then' instr**')' ('(''else' instr**')')' \(\equiv \text{foldedinstr*'} \text{'if' label blocktype instr**' else' (instr**)' end'}\)
```

Note: For example, the instruction sequence

```
(local.get $x) (i32.const 2) i32.add (i32.const 3) i32.mul
```

can be folded into

```
(i32.mul (i32.add (local.get $x) (i32.const 2)) (i32.const 3))
```

Folded instructions are solely syntactic sugar, no additional syntactic or type-based checking is implied.

6.5.11 Expressions

Expressions are written as instruction sequences. No explicit 'end' keyword is included, since they only occur in bracketed positions.

```
expr_I ::= (in:instr_I)^* \Rightarrow in^* end
```

6.6 Modules

6.6.1 Indices

Indices can be given either in raw numeric form or as symbolic *identifiers* when bound by a respective construct. Such identifiers are looked up in the suitable space of the *identifier context* I.

```
\mathsf{typeidx}_I
                ::= x:u32 \Rightarrow
                v:id \Rightarrow x \text{ (if } I.types[x] = v)
funcidx_I ::= x:u32 \Rightarrow x
                v:id \Rightarrow x \text{ (if } I.funcs[x] = v)
tableidx_I ::= x:u32 \Rightarrow x
                v:id \Rightarrow x \text{ (if } I.tables[x] = v)
                ::= x:u32 \Rightarrow x
memidx_I
                 v:id \Rightarrow x \text{ (if } I.mems[x] = v)
globalidx_I ::= x:u32 \Rightarrow x
                | \quad v \text{:id} \quad \Rightarrow \quad x \quad (\text{if $I$.globals}[x] = v)
elemidx_I
                ::= x:u32 \Rightarrow x
                 v:id \Rightarrow x \text{ (if } I.elem[x] = v)
dataidx_I ::= x:u32 \Rightarrow x
                 v:id \Rightarrow x \text{ (if } I.data[x] = v)
localidx_I ::= x:u32 \Rightarrow x
                v:id \Rightarrow x \text{ (if } I.locals[x] = v)
labelidx_I ::= l:u32 \Rightarrow l
                v:id \Rightarrow l \quad (if I.labels[l] = v)
```

6.6.2 Types

Type definitions can bind a symbolic type identifier.

```
type_I ::= '('type'id' ft:functype_I')' \Rightarrow ft
```

6.6.3 Type Uses

A *type use* is a reference to a *type definition*. It may optionally be augmented by explicit inlined *parameter* and *result* declarations. That allows binding symbolic *identifiers* to name the *local indices* of parameters. If inline declarations are given, then their types must match the referenced *function type*.

The synthesized attribute of a typeuse is a pair consisting of both the used *type index* and the updated *identifier context* including possible parameter identifiers. The following auxiliary function extracts optional identifiers from parameters:

```
id('(' 'param' id' ... ')') = id'
```

Note: Both productions overlap for the case that the function type is $[] \rightarrow []$. However, in that case, they also produce the same results, so that the choice is immaterial.

The well-formedness condition on I' ensures that the parameters do not contain duplicate identifiers.

Abbreviations

A typeuse may also be replaced entirely by inline *parameter* and *result* declarations. In that case, a *type index* is automatically inserted:

```
(t_1:param)^* (t_2:result)^* \equiv '(''type' x')' param* result*
```

where x is the smallest existing type index whose definition in the current module is the function type $[t_1^*] \rightarrow [t_2^*]$. If no such index exists, then a new type definition of the form

```
'(' 'type' '(' 'func' param* result* ')' ')'
```

is inserted at the end of the module.

Abbreviations are expanded in the order they appear, such that previously inserted type definitions are reused by consecutive expansions.

6.6.4 Imports

The descriptors in imports can bind a symbolic function, table, memory, or global *identifier*.

```
\begin{array}{lll} \operatorname{import}_I & ::= & \text{`(``import' } mod : \operatorname{name } nm : \operatorname{name } d : \operatorname{importdesc}_I \text{ `)'} \\ & \Rightarrow & \{\operatorname{module } mod, \operatorname{name } nm, \operatorname{desc } d\} \\ \\ \operatorname{importdesc}_I & ::= & \text{`(``func' } \operatorname{id}^2 x, I' : \operatorname{typeuse}_I \text{`)'} & \Rightarrow & \operatorname{func } x \\ & | & \text{`(``table' } \operatorname{id}^2 tt : \operatorname{tabletype}_I \text{`)'} & \Rightarrow & \operatorname{table } tt \\ & | & \text{`(``memory' } \operatorname{id}^2 mt : \operatorname{memtype}_I \text{`)'} & \Rightarrow & \operatorname{mem } mt \\ & | & \text{`(``global' } \operatorname{id}^2 gt : \operatorname{globaltype}_I \text{`)'} & \Rightarrow & \operatorname{global} gt \\ \end{array}
```

Abbreviations

As an abbreviation, imports may also be specified inline with *function*, *table*, *memory*, or *global* definitions; see the respective sections.

6.6.5 Functions

Function definitions can bind a symbolic function identifier, and local identifiers for its parameters and locals.

```
\begin{array}{lll} \text{func}_I & ::= & \text{`(``func' id}^? \ x, I': \text{typeuse}_I \ (loc: \text{local}_I)^* \ (in: \text{instr}_{I''})^* \ `)' \\ & \Rightarrow & \{ \text{type} \ x, \text{locals} \ loc^*, \text{body} \ in^* \text{ end} \} \\ & & (\text{if} \ I'' = I' \oplus \{ \text{locals} \ \text{id}(\text{local})^* \} \ \text{well-formed}) \\ \\ \text{local}_I & ::= & \text{`(``local' id}^? \ t: \text{valtype}_I \ `)' & \Rightarrow & \{ \text{type} \ t \} \end{array}
```

The definition of the local *identifier context* I'' uses the following auxiliary function to extract optional identifiers from locals:

```
id('('') cal' id'' ... ')') = id''
```

Note: The *well-formedness* condition on I'' ensures that parameters and locals do not contain duplicate identifiers.

6.6. Modules 187

Abbreviations

Multiple anonymous locals may be combined into a single declaration:

```
'(' 'local' valtype^* ')' \equiv ('(' 'local' valtype ')')^*
```

Functions can be defined as *imports* or *exports* inline:

```
'(' 'func' id' '(' 'import' name<sub>1</sub> name<sub>2</sub> ')' typeuse ')' \equiv '(' 'import' name<sub>1</sub> name<sub>2</sub> '(' 'func' id' typeuse ')' ')'
'(' 'func' id' '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'func' id' ')' ')' '(' 'func' id' ... ')' \equiv '(if id' \neq \epsilon \land id' = id' \lor id' = \epsilon \land id' fresh)
```

Note: The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a function declaration can contain any number of exports, possibly followed by an import.

6.6.6 Tables

Table definitions can bind a symbolic *table identifier*.

```
table_I ::= '('table' id' tt:tabletype_I')' \Rightarrow \{type tt\}
```

Abbreviations

An *element segment* can be given inline with a table definition, in which case its offset is 0 and the *limits* of the *table type* are inferred from the length of the given segment:

```
'(' 'table' id' reftype '(' 'elem' expr^n:vec(elemexpr) ')' ')' \equiv '(' 'table' id' n n reftype ')' '(' 'elem' '(' 'table' id' ')' '(' 'i32.const' '0' ')' vec(elemexpr) ')' (\text{if id}^? \neq \epsilon \land \text{id}' = \text{id}^? \lor \text{id}^? = \epsilon \land \text{id}' \text{ fresh})
'(' 'table' id' reftype '(' 'elem' x^n:vec(funcidx) ')' ')' \equiv '(' 'table' id' n n reftype ')' '(' 'elem' '(' 'table' id' ')' '(' 'i32.const' '0' ')' vec(funcidx) ')' (\text{if id}^? \neq \epsilon \land \text{id}' = \text{id}^? \lor \text{id}^? = \epsilon \land \text{id}' \text{ fresh})
```

Tables can be defined as *imports* or *exports* inline:

```
'(' 'table' id' '(' 'import' name1 name2')' tabletype')' \equiv '(' 'import' name1 name2 '(' 'table' id' tabletype')' ')' '(' 'table' id' '(' 'export' name')' ... ')' \equiv '(' 'export' name '(' 'table' id')' ')' '(' 'table' id' ... ')' \equiv '(if id' \neq \epsilon \land id' = id' \lor id' = \epsilon \land id' fresh)
```

Note: The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a table declaration can contain any number of exports, possibly followed by an import.

6.6.7 Memories

Memory definitions can bind a symbolic memory identifier.

```
mem_I ::= '('memory'id' mt:memtype_I')' \Rightarrow \{type mt\}
```

Abbreviations

A *data segment* can be given inline with a memory definition, in which case its offset is 0 and the *limits* of the *memory type* are inferred from the length of the data, rounded up to *page size*:

```
'(''memory' \operatorname{id}' '(''data' b^n:datastring')'')' \equiv '(''memory' \operatorname{id}' m m')' '(''data''(''memory' \operatorname{id}'')''(''i32.const''0'')' datastring')' (\operatorname{if}\operatorname{id}^2\neq\epsilon\wedge\operatorname{id}'=\operatorname{id}^2\vee\operatorname{id}^2=\epsilon\wedge\operatorname{id}'\operatorname{fresh},m=\operatorname{ceil}(n/64\operatorname{Ki}))
```

Memories can be defined as imports or exports inline:

```
'(' 'memory' id' '(' 'import' name1 name2 ')' memtype ')' \equiv '(' 'import' name1 name2 '(' 'memory' id' memtype ')' ')' '(' 'memory' id' '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'memory' id' ')' ')' '(' 'memory' id' ... ')' (\text{if id}? \neq \epsilon \wedge \text{id}' = \text{id}? \vee \text{id}? = \epsilon \wedge \text{id}' \text{ fresh})
```

Note: The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a memory declaration can contain any number of exports, possibly followed by an import.

6.6.8 Globals

Global definitions can bind a symbolic global identifier.

```
global_I ::= '(''global'' id'' gt:globaltype_I e:expr_I')' \Rightarrow \{type gt, init e\}
```

Abbreviations

Globals can be defined as *imports* or *exports* inline:

```
'(' 'global' id' '(' 'import' name_1 name_2 ')' globaltype ')' \equiv '(' 'import' name_1 name_2 '(' 'global' id' globaltype ')' ')' '(' 'global' id' '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'global' id' ')' ')' '(' 'global' id' ... ')' (\text{if id}^? \neq \epsilon \wedge \text{id}' = \text{id}^? \vee \text{id}^? = \epsilon \wedge \text{id}' \text{ fresh})
```

Note: The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a global declaration can contain any number of exports, possibly followed by an import.

6.6. Modules 189

6.6.9 Exports

The syntax for exports mirrors their abstract syntax directly.

Abbreviations

As an abbreviation, exports may also be specified inline with *function*, *table*, *memory*, or *global* definitions; see the respective sections.

6.6.10 Start Function

A *start function* is defined in terms of its index.

```
start_I ::= '('start' x:funcidx_I')' \Rightarrow \{func x\}
```

Note: At most one start function may occur in a module, which is ensured by a suitable side condition on the module grammar.

6.6.11 Element Segments

Element segments allow for an optional *table index* to identify the table to initialize.

```
\begin{array}{lll} \text{elem}_I & ::= & \text{`(``elem'\ id'} & (et,y^*) : \text{elemlist}_I \text{ `)'} \\ & \Rightarrow & \{ \text{type}\ et, \text{init}\ y^*, \text{mode passive} \} \\ & | & \text{`(``elem'\ id'} & x : \text{tableuse}_I \text{ `('`offset'\ } e : \text{expr}_I \text{ `)'} & (et,y^*) : \text{elemlist}_I \text{ `)'} \\ & \Rightarrow & \{ \text{type}\ et, \text{init}\ y^*, \text{mode active} \{ \text{table}\ x, \text{offset}\ e \} \} \\ & \text{`(``elem'\ id'} & \text{`declare'} & (et,y^*) : \text{elemlist}_I \text{ `)'} \\ & \Rightarrow & \{ \text{type}\ et, \text{init}\ y^*, \text{mode declarative} \} \\ & \text{elemlist}_I & ::= & t : \text{reftype}_I & y^* : \text{vec}(\text{elemexpr}_I) & \Rightarrow & (\text{type}\ t, \text{init}\ y^*) \\ & \text{elemexpr}_I & ::= & \text{`(``item'\ } e : \text{expr}_I \text{ `)'} & \Rightarrow & e \\ & \text{tableuse}_I & ::= & \text{`(``table'\ } x : \text{tableidx}_I \text{ `)'} & \Rightarrow & x \\ \end{array}
```

Abbreviations

As an abbreviation, a single instruction may occur in place of the offset of an active element segment or as an element expression:

```
'('instr')' \equiv '('offset'instr')'
'('instr')' \equiv '('item'instr')'
```

Also, the element list may be written as just a sequence of function indices:

```
'func' vec(funcidx_I) \equiv 'funcref' vec('(' 'ref.func' funcidx_I ')')
```

A table use can be omitted, defaulting to 0. Furthermore, for backwards compatibility with earlier versions of WebAssembly, if the table use is omitted, the 'func' keyword can be omitted as well.

As another abbreviation, element segments may also be specified inline with *table* definitions; see the respective section.

6.6.12 Data Segments

Data segments allow for an optional *memory index* to identify the memory to initialize. The data is written as a *string*, which may be split up into a possibly empty sequence of individual string literals.

```
\begin{array}{lll} \operatorname{data}_I & ::= & \text{`(``data' id}^? \ b^*: \operatorname{datastring ')'} \\ & \Rightarrow & \{\operatorname{init} b^*, \operatorname{mode passive}\} \\ & | & \text{`(``data' id}^? \ x: \operatorname{memuse}_I \ `(``\operatorname{offset'} \ e: \operatorname{expr}_I \ `)' \ b^*: \operatorname{datastring ')'} \\ & \Rightarrow & \{\operatorname{init} b^*, \operatorname{mode active} \{\operatorname{memory} \ x', \operatorname{offset} \ e\}\} \\ \operatorname{datastring} & ::= & (b^*: \operatorname{string})^* & \Rightarrow & \operatorname{concat}((b^*)^*) \\ \operatorname{memuse}_I & ::= & \text{`(``memory' } x: \operatorname{memidx}_I \ `)' & \Rightarrow \ x \\ \end{array}
```

Note: In the current version of WebAssembly, the only valid memory index is 0 or a symbolic *memory identifier* resolving to the same value.

Abbreviations

As an abbreviation, a single instruction may occur in place of the offset of an active data segment:

```
'('instr')' \equiv '('offset' instr')'
```

Also, a memory use can be omitted, defaulting to 0.

```
\epsilon \equiv \text{`('`memory'`0'')'}
```

As another abbreviation, data segments may also be specified inline with *memory* definitions; see the respective section.

6.6.13 Modules

A module consists of a sequence of fields that can occur in any order. All definitions and their respective bound *identifiers* scope over the entire module, including the text preceding them.

A module may optionally bind an *identifier* that names the module. The name serves a documentary role only.

Note: Tools may include the module name in the *name section* of the *binary format*.

```
::= '(''module' id'' (m:modulefield_I)*')' \Rightarrow
module
                                (if I = \bigoplus idc(modulefield)^* well-formed)
modulefield_I ::= ty:type_I
                                           \Rightarrow {types ty}
                          im:import_I \Rightarrow \{imports im\}
                                           \Rightarrow {funcs fn}
                          fn:\mathtt{func}_I
                          ta:table_I
                                           \Rightarrow {tables ta}
                                           \Rightarrow \{\text{mems } me\}
                          me:\mathtt{mem}_I
                           gl:global_I \Rightarrow \{globals gl\}
                           ex:export_I \Rightarrow \{exports \ ex\}
                                           \Rightarrow {start st}
                           st:start_I
                                            \Rightarrow {elems el}
                           el:elem_I
                           da:data_I
                                           \Rightarrow {datas da}
```

The following restrictions are imposed on the composition of *modules*: $m_1 \oplus m_2$ is defined if and only if

- $m_1.\mathsf{start} = \epsilon \lor m_2.\mathsf{start} = \epsilon$
- m_1 .funcs = m_1 .tables = m_1 .mems = m_1 .globals = $\epsilon \vee m_2$.imports = ϵ

6.6. Modules 191

Note: The first condition ensures that there is at most one start function. The second condition enforces that all *imports* must occur before any regular definition of a *function*, *table*, *memory*, or *global*, thereby maintaining the ordering of the respective *index spaces*.

The well-formedness condition on I in the grammar for module ensures that no namespace contains duplicate identifiers.

The definition of the initial *identifier context* I uses the following auxiliary definition which maps each relevant definition to a singular context with one (possibly empty) identifier:

```
\begin{array}{llll} & \operatorname{idc}(`('\text{ 'type' id'} ft: \operatorname{functype'})') & = & \{\operatorname{types}(\operatorname{id'}), \operatorname{typedefs} ft\} \\ & \operatorname{idc}(`('\text{ 'func' id'} \dots ')') & = & \{\operatorname{funcs}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'table' id'} \dots ')') & = & \{\operatorname{tables}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'memory' id'} \dots ')') & = & \{\operatorname{globals}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'global' id'} \dots ')') & = & \{\operatorname{globals}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'elem' id'} \dots ')') & = & \{\operatorname{data}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'import'} \dots '('\text{ 'func' id'} \dots ')',')') & = & \{\operatorname{funcs}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'import'} \dots '('\text{ 'table' id'} \dots ')',')') & = & \{\operatorname{tables}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'import'} \dots '('\text{ 'memory' id'} \dots ')',')') & = & \{\operatorname{globals}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'import'} \dots '('\text{ 'global' id'} \dots ')',')') & = & \{\operatorname{globals}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ 'import'} \dots '('\text{ 'global' id'} \dots ')',')') & = & \{\operatorname{globals}(\operatorname{id'})\} \\ & \operatorname{idc}(`('\text{ '...}')') & = & \{\{\operatorname{globals}(\operatorname{id'})\}\} \\ & \operatorname{idc}(`('\text{ '...}')') & = & \{\operatorname{globals}(\operatorname{id'})\} \\
```

Abbreviations

In a source file, the toplevel (module ...) surrounding the module body may be omitted.

```
modulefield* \equiv '(''module' modulefield*')'
```

Appendix

7.1 Embedding

A WebAssembly implementation will typically be *embedded* into a *host* environment. An *embedder* implements the connection between such a host environment and the WebAssembly semantics as defined in the main body of this specification. An embedder is expected to interact with the semantics in well-defined ways.

This section defines a suitable interface to the WebAssembly semantics in the form of entry points through which an embedder can access it. The interface is intended to be complete, in the sense that an embedder does not need to reference other functional parts of the WebAssembly specification directly.

Note: On the other hand, an embedder does not need to provide the host environment with access to all functionality defined in this interface. For example, an implementation may not support *parsing* of the *text format*.

7.1.1 Types

In the description of the embedder interface, syntactic classes from the *abstract syntax* and the *runtime's abstract machine* are used as names for variables that range over the possible objects from that class. Hence, these syntactic classes can also be interpreted as types.

For numeric parameters, notation like n:u32 is used to specify a symbolic name in addition to the respective value range.

7.1.2 Errors

Failure of an interface operation is indicated by an auxiliary syntactic class:

error ::= error

In addition to the error conditions specified explicitly in this section, implementations may also return errors when specific *implementation limitations* are reached.

Note: Errors are abstract and unspecific with this definition. Implementations can refine it to carry suitable classifications and diagnostic messages.

7.1.3 Pre- and Post-Conditions

Some operations state *pre-conditions* about their arguments or *post-conditions* about their results. It is the embedder's responsibility to meet the pre-conditions. If it does, the post conditions are guaranteed by the semantics.

In addition to pre- and post-conditions explicitly stated with each operation, the specification adopts the following conventions for *runtime objects* (*store*, *moduleinst*, *externval*, *addresses*):

- Every runtime object passed as a parameter must be *valid* per an implicit pre-condition.
- Every runtime object returned as a result is *valid* per an implicit post-condition.

Note: As long as an embedder treats runtime objects as abstract and only creates and manipulates them through the interface defined here, all implicit pre-conditions are automatically met.

7.1.4 Store

```
store_init(): store
```

1. Return the empty *store*.

```
store_init() = {funcs \epsilon, mems \epsilon, tables \epsilon, globals \epsilon}
```

7.1.5 Modules

```
module\_decode(byte^*) : module \mid error
```

- 1. If there exists a derivation for the *byte* sequence $byte^*$ as a module according to the *binary grammar for modules*, yielding a *module m*, then return m.
- 2. Else, return error.

```
\begin{array}{lll} \operatorname{module\_decode}(b^*) & = & m & \quad (\operatorname{if} \operatorname{module} \stackrel{*}{\Longrightarrow} m . b^*) \\ \operatorname{module\_decode}(b^*) & = & \operatorname{error} & \quad (\operatorname{otherwise}) \end{array}
```

```
module parse(char^*): module \mid error
```

- 1. If there exists a derivation for the *source* $char^*$ as a module according to the *text grammar for modules*, yielding a *module* m, then return m.
- 2. Else, return error.

```
\begin{array}{lll} \operatorname{module\_parse}(c^*) & = & m & \quad (\operatorname{if} \operatorname{module} \stackrel{*}{\Longrightarrow} m {:} c^*) \\ \operatorname{module\_parse}(c^*) & = & \operatorname{error} & \quad (\operatorname{otherwise}) \end{array}
```

 $module validate(module) : error^?$

- 1. If *module* is *valid*, then return nothing.
- 2. Else, return error.

```
\begin{array}{lll} \text{module\_validate}(m) & = & \epsilon & \text{ (if } \vdash m : externtype^* \rightarrow externtype'^*) \\ \text{module\_validate}(m) & = & \text{error} & \text{ (otherwise)} \end{array}
```

module instantiate(store, module, $externval^*$): (store, moduleinst | error)

- 1. Try instantiating module in store with external values externval* as imports:
- a. If it succeeds with a module instance moduleinst, then let result be moduleinst.
- b. Else, let result be error.
- 2. Return the new store paired with result.

```
\begin{array}{lll} \operatorname{module\_instantiate}(S,m,ev^*) & = & (S',F.\mathsf{module}) & (\operatorname{if\ instantiate}(S,m,ev^*) \hookrightarrow *S';F;\epsilon) \\ \operatorname{module\_instantiate}(S,m,ev^*) & = & (S',\operatorname{error}) & (\operatorname{if\ instantiate}(S,m,ev^*) \hookrightarrow *S';F;\operatorname{trap}) \end{array}
```

Note: The store may be modified even in case of an error.

 $module_imports(module) : (name, name, externtype)^*$

- 1. Pre-condition: module is valid with external import types $externtype^*$ and external export types $externtype'^*$.
- 2. Let *import** be the *imports module*.imports.
- 3. Assert: the length of *import** equals the length of *externtype**.
- 4. For each $import_i$ in $import^*$ and corresponding $externtype_i$ in $externtype^*$, do:
- a. Let $result_i$ be the triple $(import_i.module, import_i.name, externtype_i)$.
- 5. Return the concatenation of all $result_i$, in index order.
- 6. Post-condition: each $externtype_i$ is valid.

```
module\_imports(m) = (im.module, im.name, externtype)^* 
(if im^* = m.imports \land \vdash m : externtype^* \rightarrow externtype'^*)
```

 $module exports(module) : (name, externtype)^*$

- 1. Pre-condition: module is valid with external import types $externtype^*$ and external export types $externtype'^*$.
- 2. Let *export** be the *exports module*.exports.
- 3. Assert: the length of export* equals the length of externtype'*.
- 4. For each export_i in export^{*} and corresponding externtype'_i in externtype'^{*}, do:
- a. Let $result_i$ be the pair ($export_i$.name, $externtype'_i$).
- 5. Return the concatenation of all $result_i$, in index order.
- 6. Post-condition: each externtype' is valid.

7.1. Embedding 195

```
module\_exports(m) = (ex.name, externtype')^* 
(if ex^* = m.exports \land \vdash m : externtype^* \rightarrow externtype'^*)
```

7.1.6 Module Instances

 $instance_export(moduleinst, name) : externval \mid error$

- 1. Assert: due to validity of the module instance moduleinst, all its export names are different.
- 2. If there exists an $exportinst_i$ in module inst exports such that name $exportinst_i$ name equals name, then:
 - a. Return the external value exportins t_i value.
- 3. Else, return error.

```
instance\_export(m, name) = m.exports[i].value (if m.exports[i].name = name) instance\_export(m, name) = error (otherwise)
```

7.1.7 Functions

 $func_alloc(store, functype, hostfunc) : (store, funcaddr)$

- 1. Pre-condition: functype is valid.
- 2. Let funcaddr be the result of allocating a host function in store with function type functype and host function code host func.
- 3. Return the new store paired with *funcaddr*.

```
func\_alloc(S, ft, code) = (S', a) (if allochostfunc(S, ft, code) = S', a)
```

Note: This operation assumes that *hostfunc* satisfies the *pre- and post-conditions* required for a function instance with type *functype*.

Regular (non-host) function instances can only be created indirectly through module instantiation.

 $func_type(store, funcaddr) : functype$

- 1. Return S.funcs[a].type.
- 2. Post-condition: the returned *function type* is *valid*.

$$\operatorname{func_type}(S, a) = S.\operatorname{funcs}[a].\operatorname{type}$$

 $func_invoke(store, funcaddr, val^*) : (store, val^* \mid error)$

- 1. Try invoking the function funcaddr in store with values val* as arguments:
- a. If it succeeds with values val'* as results, then let result be val'*.
- b. Else it has trapped, hence let *result* be error.
- 2. Return the new store paired with result.

```
\begin{array}{lll} \mathrm{func\_invoke}(S,a,v^*) & = & (S',v'^*) & & (\mathrm{if\ invoke}(S,a,v^*) \hookrightarrow {}^*S';F;v'^*) \\ \mathrm{func\_invoke}(S,a,v^*) & = & (S',\mathrm{error}) & & (\mathrm{if\ invoke}(S,a,v^*) \hookrightarrow {}^*S';F;\mathrm{trap}) \end{array}
```

Note: The store may be modified even in case of an error.

7.1.8 Tables

table alloc(store, tabletype): (store, tableaddr, ref)

- 1. Pre-condition: tabletype is valid.
- 2. Let tableaddr be the result of allocating a table in store with table type tabletype and initialization value ref.
- 3. Return the new store paired with *tableaddr*.

```
table\_alloc(S, tt, r) = (S', a) (if alloctable(S, tt, r) = S', a)
```

 $table_type(store, tableaddr) : tabletype$

- 1. Return S.tables[a].type.
- 2. Post-condition: the returned *table type* is *valid*.

$$table_type(S, a) = S.tables[a].type$$

 $table_read(store, tableaddr, i : u32) : ref \mid error$

- 1. Let ti be the table instance store.tables[tableaddr].
- 2. If i is larger than or equal to the length of ti.elem, then return error.
- 3. Else, return the *reference value ti.elem[i]*.

```
 \begin{array}{lll} {\rm table\_read}(S,a,i) &=& r & \quad & ({\rm if} \ S.{\rm tables}[a].{\rm elem}[i] = r) \\ {\rm table\_read}(S,a,i) &=& {\rm error} & \quad & ({\rm otherwise}) \\ \end{array}
```

 ${\tt table_write}(store, tableaddr, i: u32, ref): store \mid error$

- 1. Let *ti* be the *table instance store*.tables[*tableaddr*].
- 2. If i is larger than or equal to the length of ti.elem, then return error.
- 3. Replace ti.elem[i] with the reference value ref.
- 4. Return the updated store.

```
\begin{array}{lll} {\rm table\_write}(S,a,i,r) &=& S' & \quad & ({\rm if}\ S'=S\ {\rm with}\ {\rm tables}[a].{\rm elem}[i]=r) \\ {\rm table\_write}(S,a,i,r) &=& {\rm error} & \quad & ({\rm otherwise}) \end{array}
```

7.1. Embedding 197

table size(store, tableaddr): u32

1. Return the length of *store*.tables[tableaddr].elem.

```
table\_size(S, a) = n (if |S.tables[a].elem| = n)
```

 $table_grow(store, tableaddr, n : u32, ref) : store \mid error$

- 1. Try growing the table instance store.tables [tableaddr] by n elements with initialization value ref:
 - a. If it succeeds, return the updated store.
 - b. Else, return error.

```
 \begin{array}{lll} {\rm table\_grow}(S,a,n,r) & = & S' & {\rm (if} \ S' = S \ {\rm with} \ {\rm table}[a] = {\rm growtable}(S.{\rm tables}[a],n,r)) \\ {\rm table\_grow}(S,a,n,r) & = & {\rm error} & {\rm (otherwise)} \\ \end{array}
```

7.1.9 Memories

 $mem_alloc(store, memtype) : (store, memaddr)$

- 1. Pre-condition: *memtype* is *valid*.
- 2. Let memaddr be the result of allocating a memory in store with memory type memtype.
- 3. Return the new store paired with *memaddr*.

$$\operatorname{mem_alloc}(S, mt) = (S', a)$$
 (if $\operatorname{allocmem}(S, mt) = S', a$)

 $mem_type(store, memaddr) : memtype$

- 1. Return S.mems[a].type.
- 2. Post-condition: the returned *memory type* is *valid*.

$$mem_type(S, a) = S.mems[a].type$$

mem read(store, memaddr, i: u32): $byte \mid error$

- 1. Let mi be the memory instance store.mems[memaddr].
- 2. If i is larger than or equal to the length of mi.data, then return error.
- 3. Else, return the *byte* mi.data[i].

```
\begin{array}{lll} \operatorname{mem\_read}(S,a,i) & = & b & \quad \text{(if $S$.mems}[a].data[i] = b) \\ \operatorname{mem\_read}(S,a,i) & = & \operatorname{error} & \quad \text{(otherwise)} \end{array}
```

 $mem_write(store, memaddr, i : u32, byte) : store \mid error$

- 1. Let mi be the memory instance store.mems[memaddr].
- 2. If u32 is larger than or equal to the length of mi.data, then return error.
- 3. Replace mi.data[i] with byte.
- 4. Return the updated store.

```
\begin{array}{lll} \operatorname{mem\_write}(S,a,i,b) & = & S' & \quad \text{(if } S' = S \text{ with } \operatorname{mems}[a].\operatorname{data}[i] = b) \\ \operatorname{mem\_write}(S,a,i,b) & = & \operatorname{error} & \quad \text{(otherwise)} \end{array}
```

mem size(store, memaddr): u32

1. Return the length of *store*.mems[memaddr].data divided by the page size.

```
\operatorname{mem\_size}(S, a) = n \quad (\text{if } |S.\mathsf{mems}[a].\mathsf{data}| = n \cdot 64 \, \mathrm{Ki})
```

 $mem_grow(store, memaddr, n : u32) : store \mid error$

- 1. Try growing the memory instance store.mems[memaddr] by n pages:
 - a. If it succeeds, return the updated store.
 - b. Else, return error.

```
\begin{array}{lll} \operatorname{mem\_grow}(S,a,n) & = & S' & \quad \text{(if } S' = S \text{ with } \operatorname{mems}[a] = \operatorname{growmem}(S.\operatorname{mems}[a],n)) \\ \operatorname{mem\_grow}(S,a,n) & = & \operatorname{error} & \quad \text{(otherwise)} \end{array}
```

7.1.10 Globals

 $global_alloc(store, globaltype, val) : (store, globaladdr)$

- 1. Pre-condition: *globaltype* is *valid*.
- 2. Let globaladdr be the result of allocating a global in store with global type globaltype and initialization value val.
- 3. Return the new store paired with *globaladdr*.

```
global\_alloc(S, gt, v) = (S', a) (if allocglobal(S, gt, v) = S', a)
```

global type(store, globaladdr): globaltype

- 1. Return S.globals[a].type.
- 2. Post-condition: the returned *global type* is *valid*.

$${\tt global_type}(S,a) \ = \ S.{\tt globals}[a].{\tt type}$$

7.1. Embedding 199

 $global_read(store, globaladdr) : val$

- 1. Let gi be the global instance store.globals[globaladdr].
- 2. Return the *value gi*.value.

```
global_read(S, a) = v (if S.globals[a].value = v)
```

 $global_write(store, globaladdr, val) : store \mid error$

- 1. Let gi be the global instance store.globals[globaladdr].
- 2. Let *mut t* be the structure of the *global type gi*.type.
- 3. If *mut* is not var, then return error.
- 4. Replace *qi*.value with the *value val*.
- 5. Return the updated store.

```
 \begin{split} & \text{global\_write}(S, a, v) &= S' & \text{ (if $S$.globals}[a]. \\ & \text{type} = \text{var } t \land S' = S \text{ with globals}[a]. \\ & \text{value} = v) \\ & \text{global\_write}(S, a, v) &= \text{error} \\ & \text{ (otherwise)} \\ \end{aligned}
```

7.2 Implementation Limitations

Implementations typically impose additional restrictions on a number of aspects of a WebAssembly module or execution. These may stem from:

- physical resource limits,
- constraints imposed by the embedder or its environment,
- limitations of selected implementation strategies.

This section lists allowed limitations. Where restrictions take the form of numeric limits, no minimum requirements are given, nor are the limits assumed to be concrete, fixed numbers. However, it is expected that all implementations have "reasonably" large limits to enable common applications.

Note: A conforming implementation is not allowed to leave out individual *features*. However, designated subsets of WebAssembly may be specified in the future.

7.2.1 Syntactic Limits

Structure

An implementation may impose restrictions on the following dimensions of a module:

- the number of types in a module
- the number of *functions* in a *module*, including imports
- the number of tables in a module, including imports
- the number of *memories* in a *module*, including imports
- the number of globals in a module, including imports
- the number of element segments in a module
- the number of data segments in a module

- the number of *imports* to a *module*
- the number of exports from a module
- the number of parameters in a function type
- the number of results in a function type
- the number of parameters in a *block type*
- the number of results in a block type
- the number of *locals* in a *function*
- the size of a function body
- the size of a structured control instruction
- the number of structured control instructions in a function
- the nesting depth of structured control instructions
- the number of *label indices* in a br_table instruction
- the length of an element segment
- the length of a data segment
- the length of a name
- the range of *characters* in a *name*

If the limits of an implementation are exceeded for a given module, then the implementation may reject the *validation*, compilation, or *instantiation* of that module with an embedder-specific error.

Note: The last item allows *embedders* that operate in limited environments without support for Unicode⁴⁷ to limit the names of *imports* and *exports* to common subsets like ASCII⁴⁸.

Binary Format

For a module given in binary format, additional limitations may be imposed on the following dimensions:

- the size of a module
- the size of any section
- the size of an individual function's code
- the number of sections

Text Format

For a module given in text format, additional limitations may be imposed on the following dimensions:

- the size of the source text
- the size of any syntactic element
- the size of an individual token
- the nesting depth of folded instructions
- the length of symbolic *identifiers*
- the range of literal *characters* allowed in the *source text*

⁴⁷ https://www.unicode.org/versions/latest/

⁴⁸ https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

7.2.2 Validation

An implementation may defer validation of individual functions until they are first invoked.

If a function turns out to be invalid, then the invocation, and every consecutive call to the same function, results in a *trap*.

Note: This is to allow implementations to use interpretation or just-in-time compilation for functions. The function must still be fully validated before execution of its body begins.

7.2.3 Execution

Restrictions on the following dimensions may be imposed during execution of a WebAssembly program:

- the number of allocated *module instances*
- the number of allocated function instances
- the number of allocated table instances
- the number of allocated memory instances
- the number of allocated global instances
- the size of a table instance
- the size of a memory instance
- the number of frames on the stack
- the number of *labels* on the *stack*
- the number of values on the stack

If the runtime limits of an implementation are exceeded during execution of a computation, then it may terminate that computation and report an embedder-specific error to the invoking code.

Some of the above limits may already be verified during instantiation, in which case an implementation may report exceedance in the same manner as for *syntactic limits*.

Note: Concrete limits are usually not fixed but may be dependent on specifics, interdependent, vary over time, or depend on other implementation- or embedder-specific situations or events.

7.3 Validation Algorithm

The specification of WebAssembly *validation* is purely *declarative*. It describes the constraints that must be met by a *module* or *instruction* sequence to be valid.

This section sketches the skeleton of a sound and complete *algorithm* for effectively validating code, i.e., sequences of *instructions*. (Other aspects of validation are straightforward to implement.)

In fact, the algorithm is expressed over the flat sequence of opcodes as occurring in the *binary format*, and performs only a single pass over it. Consequently, it can be integrated directly into a decoder.

The algorithm is expressed in typed pseudo code whose semantics is intended to be self-explanatory.

7.3.1 Data Structures

Types

Value types are representable as a set of enumerations.

```
type num_type = I32 | I64 | F32 | F64
type vec_type = V128
type heap_type = Def(idx : nat) | Func | Extern | Bot
type ref_type = Ref(heap : heap_type, null : bool)
type val_type = num_type | vec_type | ref_type | Bot

func is_num(t : val_type) : bool =
   return t = I32 || t = I64 || t = F32 || t = F64 || t = Bot

func is_vec(t : val_type) : bool =
   return t = V128 || t = Bot

func is_ref(t : val_type) : bool =
   return not (is_num t || is_vec t) || t = Bot
```

Equivalence and subtyping checks can be defined on these types.

```
func eq_def(n1, n2) =
 ... // check that both type definitions are equivalent (TODO)
func matches_null(null1 : bool, null2 : bool) : bool =
 return null1 = null2 || null2
func matches_heap(t1 : heap_type, t2 : heap_type) : bool =
 switch (t1, t2)
   case (Def(n1), Def(n2))
     return eq_def(n1, n2)
   case (Def(_), Func)
     return true
   case (Bot, _)
     return true
   case (_, _)
     return t1 = t2
func matches_ref(t1 : ref_type, t2 : ref_type) : bool =
 return matches_heap(t1.heap, t2.heap) && matches_null(t1.null, t2.null)
func matches(t1 : val_type, t2 : val_type) : bool =
 switch (t1, t2)
   case (Ref(_), Ref(_))
     return matches_ref(t1, t2)
   case (Bot, _)
     return true
   case (_, _)
     return t1 = t2
```

Context

Validation requires a *context* for checking uses of *indices*. For the purpose of presenting the algorithm, it is maintained in a set of global variables:

```
var locals : array(val_type)
var locals_init : array(bool)
var globals : array(global_type)
var funcs : array(func_type)
var tables : array(table_type)
var mems : array(mem_type)
```

This assumes suitable representations for the various types besides val_type, which are omitted here.

For locals, there is an additional array recording the initialization status of each local.

Stacks

The algorithm uses three separate stacks: the *value stack*, the *control stack*, and the *initialization stack*. The value stack tracks the *types* of operand values on the *stack*. The control stack tracks surrounding *structured control instructions* and their associated *blocks*. The initialization stack records all *locals* that have been initialized since the beginning of the function.

```
type val_stack = stack(val_type)
type init_stack = stack(u32)

type ctrl_stack = stack(ctrl_frame)
type ctrl_frame = {
  opcode : opcode
  start_types : list(val_type)
  end_types : list(val_type)
  val_height : nat
  init_height : nat
  unreachable : bool
}
```

For each entered block, the control stack records a *control frame* with the originating opcode, the types on the top of the operand stack at the start and end of the block (used to check its result as well as branches), the height of the operand stack at the start of the block (used to check that operands do not underflow the current block), the height of the initialization stack at the start of the block (used to reset initialization status at the end of the block), and a flag recording whether the remainder of the block is unreachable (used to handle *stack-polymorphic* typing after branches).

For the purpose of presenting the algorithm, these stacks are simply maintained as global variables:

```
var vals : val_stack
var inits : init_stack
var ctrls : ctrl_stack
```

However, these variables are not manipulated directly by the main checking function, but through a set of auxiliary functions:

```
func push_val(type : val_type) =
  vals.push(type)

func pop_val() : val_type =
  if (vals.size() = ctrls[0].height && ctrls[0].unreachable) return Bot
  error_if(vals.size() = ctrls[0].height)
```

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```
return vals.pop()
func pop_val(expect : val_type) : val_type =
 let actual = pop_val()
  error_if(not matches(actual, expect))
 return actual
func pop_num() : num_type | Bot =
 let actual = pop_val()
  error_if(not is_num(actual))
 return actual
func pop_ref() : ref_type =
 let actual = pop_val()
 error_if(not is_ref(actual))
 if (actual = Bot) return Ref(Bot, false)
 return actual
func push_vals(types : list(val_type)) = foreach (t in types) push_val(t)
func pop_vals(types : list(val_type)) : list(val_type) =
 var popped := []
  foreach (t in reverse(types)) popped.prepend(pop_val(t))
 return popped
```

Pushing an operand value simply pushes the respective type to the value stack.

Popping an operand value checks that the value stack does not underflow the current block and then removes one type. But first, a special case is handled where the block contains no known values, but has been marked as unreachable. That can occur after an unconditional branch, when the stack is typed *polymorphically*. In that case, the Bot type is returned, because that is a *principal* choice trivially satisfying all use constraints.

A second function for popping an operand value takes an expected type, which the actual operand type is checked against. The types may differ by subtyping, including the case where the actual type is Bot, and thereby matches unconditionally. The function returns the actual type popped from the stack.

Finally, there are accumulative functions for pushing or popping multiple operand types.

Note: The notation stack[i] is meant to index the stack from the top, so that, e.g., ctrls[0] accesses the element pushed last.

The initialization stack and the initialization status of locals is manipulated through the following functions:

```
func get_local(idx : u32) =
  error_if(not (locals_init[idx] || ctrls[0].unreachable))

func set_local(idx : u32) =
  if (not locals_init[idx])
    inits.push(idx)
    locals_init[idx] := true

func reset_locals(height : nat) =
  while (inits.size() > height)
    locals_init[inits.pop()] := false
```

Getting a local verifies that it is either known to be initialized, or that that the operation is unreachable in the current stack frame. When a local is set that was not set already, then its initialization status is updated and the change is recorded in the initialization stack. Thus, the initialization status of all locals can be reset to a previous state by denoting a specific height in the initialization stack.

The size of the initialization stack is bounded by the number of (non-defaultable) locals in a function, so can be preallocated by an algorithm.

The control stack is likewise manipulated through auxiliary functions:

```
func push_ctrl(opcode : opcode, in : list(val_type), out : list(val_type)) =
 let frame = ctrl_frame(opcode, in, out, vals.size(), inits.size(), false)
 ctrls.push(frame)
 push_vals(in)
func pop_ctrl() : ctrl_frame =
 error_if(ctrls.is_empty())
 let frame = ctrls[0]
 pop_vals(frame.end_types)
 error_if(vals.size() =/= frame.val_height)
 reset_locals(frame.init_height)
 ctrls.pop()
 return frame
func label_types(frame : ctrl_frame) : list(val_types) =
 return (if (frame.opcode = loop) frame.start_types else frame.end_types)
func unreachable() =
 vals.resize(ctrls[0].height)
 ctrls[0].unreachable := true
```

Pushing a control frame takes the types of the label and result values. It allocates a new frame record recording them along with the current height of the operand stack and marks the block as reachable.

Popping a frame first checks that the control stack is not empty. It then verifies that the operand stack contains the right types of values expected at the end of the exited block and pops them off the operand stack. Afterwards, it checks that the stack has shrunk back to its initial height. Finally, it undoes all changes to the initialization status of locals that happend inside the block.

The type of the *label* associated with a control frame is either that of the stack at the start or the end of the frame, determined by the opcode that it originates from.

Finally, the current frame can be marked as unreachable. In that case, all existing operand types are purged from the value stack, in order to allow for the *stack-polymorphism* logic in pop_val to take effect.

Note: Even with the unreachable flag set, consecutive operands are still pushed to and popped from the operand stack. That is necessary to detect invalid *examples* like (unreachable (i32.const) i64.add). However, a polymorphic stack cannot underflow, but instead generates Bot types as needed.

7.3.2 Validation of Opcode Sequences

The following function shows the validation of a number of representative instructions that manipulate the stack. Other instructions are checked in a similar manner.

```
func validate(opcode) =
   switch (opcode)
   case (i32.add)
      pop_val(I32)
      pop_val(I32)
      push_val(I32)
      case (drop)
```

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```
pop_val()
case (select)
  pop_val(I32)
  let t1 = pop_val()
  let t2 = pop_val()
  error_if(not (is_num(t1) \&\& is_num(t2) || is_vec(t1) \&\& is_vec(t2)))
  error_if(t1 =/= t2 && t1 =/= Bot && t2 =/= Bot)
  push_val(if (t1 = Bot) t2 else t1)
case (select t)
  pop_val(I32)
  pop_val(t)
 pop_val(t)
 push_val(t)
case (ref.is_null)
 pop_ref()
 push_val(I32)
case (ref.as_non_null)
  let rt = pop_ref()
  push_val(Ref(rt.heap, false))
case (local.get x)
  get_local(x)
  push_val(locals[x])
case (local.set x)
 pop_val(locals[x])
  set_local(x)
case (unreachable)
 unreachable()
case (block t1*->t2*)
 pop_vals([t1*])
  push_ctrl(block, [t1*], [t2*])
case (loop t1*->t2*)
 pop_vals([t1*])
  push_ctrl(loop, [t1*], [t2*])
case (if t1*->t2*)
 pop_val(I32)
 pop_vals([t1*])
 push_ctrl(if, [t1*], [t2*])
case (end)
  let frame = pop_ctrl()
  push_vals(frame.end_types)
case (else)
 let frame = pop_ctrl()
  error_if(frame.opcode =/= if)
  push_ctrl(else, frame.start_types, frame.end_types)
```

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```
case (br n)
  error_if(ctrls.size() < n)</pre>
  pop_vals(label_types(ctrls[n]))
  unreachable()
case (br_if n)
  error_if(ctrls.size() < n)</pre>
  pop_val(I32)
  pop_vals(label_types(ctrls[n]))
  push_vals(label_types(ctrls[n]))
case (br_table n* m)
  pop_val(I32)
  error_if(ctrls.size() < m)</pre>
  let arity = label_types(ctrls[m]).size()
  foreach (n in n*)
    error_if(ctrls.size() < n)</pre>
    error_if(label_types(ctrls[n]).size() =/= arity)
    push_vals(pop_vals(label_types(ctrls[n])))
  pop_vals(label_types(ctrls[m]))
  unreachable()
case (br_on_null n)
  error_if(ctrls.size() < n)</pre>
  let rt = pop_ref()
  pop_vals(label_types(ctrls[n]))
  push_vals(label_types(ctrls[n]))
  push_val(Ref(rt.heap, false))
case (call_ref)
  let rt = pop_ref()
  if (rt.heap =/= Bot)
    error_if(not is_def(rt.heap))
    let ft = funcs[rt.heap.idx]
    pop_vals(ft.params)
    push_vals(ft.results)
```

Note: It is an invariant under the current WebAssembly instruction set that an operand of Unknown type is never duplicated on the stack. This would change if the language were extended with stack instructions like dup. Under such an extension, the above algorithm would need to be refined by replacing the Unknown type with proper *type variables* to ensure that all uses are consistent.

7.4 Custom Sections

This appendix defines dedicated *custom sections* for WebAssembly's *binary format*. Such sections do not contribute to, or otherwise affect, the WebAssembly semantics, and like any custom section they may be ignored by an implementation. However, they provide useful meta data that implementations can make use of to improve user experience or take compilation hints.

Currently, only one dedicated custom section is defined, the *name section*.

7.4.1 Name Section

The *name section* is a *custom section* whose name string is itself 'name'. The name section should appear only once in a module, and only after the *data section*.

The purpose of this section is to attach printable names to definitions in a module, which e.g. can be used by a debugger or when parts of the module are to be rendered in *text form*.

Note: All *names* are represented in Unicode⁴⁹ encoded in UTF-8. Names need not be unique.

Subsections

The data of a name section consists of a sequence of subsections. Each subsection consists of a

- a one-byte subsection id,
- the u32 size of the contents, in bytes,
- the actual *contents*, whose structure is dependent on the subsection id.

The following subsection ids are used:

ld	Subsection
0	module name
1	function names
2	local names

Each subsection may occur at most once, and in order of increasing id.

Name Maps

A *name map* assigns *names* to *indices* in a given *index space*. It consists of a *vector* of index/name pairs in order of increasing index value. Each index must be unique, but the assigned names need not be.

```
namemap ::= vec(nameassoc)
nameassoc ::= idx name
```

An *indirect name map* assigns *names* to a two-dimensional *index space*, where secondary indices are *grouped* by primary indices. It consists of a vector of primary index/name map pairs in order of increasing index value, where each name map in turn maps secondary indices to names. Each primary index must be unique, and likewise each secondary index per individual name map.

```
\begin{array}{lll} \text{indirectnamemap} & ::= & \text{vec(indirectnameassoc)} \\ \text{indirectnameassoc} & ::= & \text{idx namemap} \end{array}
```

7.4. Custom Sections 209

⁴⁹ https://www.unicode.org/versions/latest/

Module Names

The module name subsection has the id 0. It simply consists of a single name that is assigned to the module itself.

```
modulenamesubsec ::= namesubsection_0(name)
```

Function Names

The function name subsection has the id 1. It consists of a name map assigning function names to function indices.

```
functionamesubsec ::= namesubsection<sub>1</sub>(namemap)
```

Local Names

The *local name subsection* has the id 2. It consists of an *indirect name map* assigning local names to *local indices* grouped by *function indices*.

```
localnamesubsec ::= namesubsection_2(indirectnamemap)
```

7.5 Soundness

Todo: need to operate wrt semantic types

Todo: define "S vdash t ok"

Todo: ensure wf of guessed valtypes

The *type system* of WebAssembly is *sound*, implying both *type safety* and *memory safety* with respect to the WebAssembly semantics. For example:

- All types declared and derived during validation are respected at run time; e.g., every *local* or *global* variable will only contain type-correct values, every *instruction* will only be applied to operands of the expected type, and every *function invocation* always evaluates to a result of the right type (if it does not *trap* or diverge).
- No memory location will be read or written except those explicitly defined by the program, i.e., as a *local*, a *global*, an element in a *table*, or a location within a linear *memory*.
- There is no undefined behavior, i.e., the *execution rules* cover all possible cases that can occur in a *valid* program, and the rules are mutually consistent.

Soundness also is instrumental in ensuring additional properties, most notably, *encapsulation* of function and module scopes: no *locals* can be accessed outside their own function and no *module* components can be accessed outside their own module unless they are explicitly *exported* or *imported*.

The typing rules defining WebAssembly *validation* only cover the *static* components of a WebAssembly program. In order to state and prove soundness precisely, the typing rules must be extended to the *dynamic* components of the abstract *runtime*, that is, the *store*, *configurations*, and *administrative instructions*.⁵⁰

7.5.1 Results

Results can be classified by result types as follows.

Results val*

- For each value val_i in val^* :
 - The value val_i is valid with some value type t_i .
- Let t^* be the concatenation of all t_i .
- Then the result is valid with *result type* $[t^*]$.

$$\frac{(S \vdash val : t)^*}{S \vdash val^* : [t^*]}$$

Results trap

• The result is valid with result type $[t^*]$, for any sequence t^* of valid value types.

$$\overline{S \vdash \mathsf{trap} : [t^*]}$$

7.5.2 Store Validity

The following typing rules specify when a runtime *store* S is *valid*. A valid store must consist of *function*, *table*, *memory*, *global*, and *module* instances that are themselves valid, relative to S.

To that end, each kind of instance is classified by a respective *function*, *table*, *memory*, or *global* type. Module instances are classified by *module contexts*, which are regular *contexts* repurposed as module types describing the *index spaces* defined by a module.

Store S

- Each function instance functionst_i in S. funcs must be valid with some function type functype_i.
- Each table instance tableinst; in S.tables must be valid with some table type tabletype;.
- Each memory instance meminst_i in S.mems must be valid with some memory type memtype_i.
- Each global instance globalinst_i in S.globals must be valid with some global type globaltype_i.
- Each element instance eleminst_i in S.elems must be valid.
- Each data instance datainst_i in S.datas must be valid.
- Then the store is valid.

7.5. Soundness 211

⁵⁰ The formalization and theorems are derived from the following article: Andreas Haas, Andreas Rossberg, Derek Schuff, Ben Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman. Bringing the Web up to Speed with WebAssembly Page 211, 51. Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017). ACM 2017.

⁵¹ https://dl.acm.org/citation.cfm?doid=3062341.3062363

```
(S \vdash funcinst : functype)^* \qquad (S \vdash tableinst : tabletype)^* \\ (S \vdash meminst : memtype)^* \qquad (S \vdash globalinst : globaltype)^* \\ (S \vdash eleminst \ ok)^* \qquad (S \vdash datainst \ ok)^* \\ \underline{S = \{\text{funcs } funcinst^*, \text{tables } tableinst^*, \text{mems } meminst^*, \text{globals } globalinst^*, \text{elems } eleminst^*, \text{datas } datainst^*\}} \\ \vdash S \ ok
```

Function Instances {type functype, module moduleinst, code func}

- The function type functype must be valid.
- The module instance module instance must be valid with some context C.
- Under context C, the function func must be valid with function type functype.
- Then the function instance is valid with function type functype.

Host Function Instances {type *functype*, hostcode *hf* }

- The function type functype must be valid.
- Let $[t_1^*] \rightarrow [t_2^*]$ be the function type functype.
- For every valid store S_1 extending S and every sequence val^* of values whose types coincide with t_1^* :
 - Executing hf in store S_1 with arguments val^* has a non-empty set of possible outcomes.
 - ${\color{red}\textbf{-}}$ For every element R of this set:
 - * Either R must be \bot (i.e., divergence).
 - * Or R consists of a valid store S_2 extending S_1 and a result result whose type coincides with $[t_2^*]$.
- Then the function instance is valid with *function type functype*.

```
 \forall S_1, val^*, \vdash S_1 \text{ ok } \land \vdash S \preceq S_1 \land S_1 \vdash val^* : [t_1^*] \Longrightarrow \\ hf(S_1; val^*) \supset \emptyset \land \\ \forall R \in hf(S_1; val^*), \ R = \bot \lor \\ \vdash [t_1^*] \rightarrow [t_2^*] \text{ ok} \qquad \exists S_2, result, \vdash S_2 \text{ ok } \land \vdash S_1 \preceq S_2 \land S_2 \vdash result : [t_2^*] \land R = (S_2; result) \\ S \vdash \{\text{type } [t_1^*] \rightarrow [t_2^*], \text{hostcode } hf\} : [t_1^*] \rightarrow [t_2^*]
```

Note: This rule states that, if appropriate pre-conditions about store and arguments are satisfied, then executing the host function must satisfy appropriate post-conditions about store and results. The post-conditions match the ones in the *execution rule* for invoking host functions.

Any store under which the function is invoked is assumed to be an extension of the current store. That way, the function itself is able to make sufficient assumptions about future stores.

Table Instances {type ($limits\ t$), elem ref^* }

- The *table type limits t* must be *valid*.
- The length of ref* must equal limits.min.
- For each reference ref_i in the table's elements ref^n :
 - The reference ref_i must be valid with some reference type t'_i .
 - The reference type t'_i must match the reference type t.
- Then the table instance is valid with *table type limits* t.

Todo: reftypematch needs C

$$\frac{\vdash \mathit{limits}\;t\;\mathsf{ok}}{S \vdash \{\mathsf{type}\;(\mathit{limits}\;t), \mathsf{elem}\;\mathit{ref}^n\} : \mathit{limits}\;t} \quad (C \vdash t' \leq t)^n}{S \vdash \{\mathsf{type}\;(\mathit{limits}\;t), \mathsf{elem}\;\mathit{ref}^n\} : \mathit{limits}\;t}$$

Memory Instances {type limits, data b^* }

- The *memory type* $\{\min n, \max m^?\}$ must be *valid*.
- The length of b^* must equal limits.min multiplied by the page size 64 Ki.
- Then the memory instance is valid with *memory type limits*.

$$\frac{\vdash limits \text{ ok} \qquad n = limits.\text{min} \cdot 64 \text{ Ki}}{S \vdash \{\text{type } limits, \text{data } b^n\} : limits}$$

Global Instances {type $(mut\ t)$, value val}

- The *global type mut t* must be *valid*.
- The value val must be valid with some value type t'.
- The value type t' must match the value type t.
- Then the global instance is valid with *global type mut t*.

$$\frac{\vdash \textit{mut } t \text{ ok} \qquad S \vdash \textit{val} : t' \qquad \vdash t' \leq t}{S \vdash \{ \text{type } (\textit{mut } t), \text{value } \textit{val} \} : \textit{mut } t}$$

Element Instances {elem fa^* }

- For each reference ref_i in the elements ref^n :
 - The reference ref_i must be valid with some reference type t'_i .
 - The reference type t'_i must match the reference type t.
- Then the table instance is valid.

Todo: reftypematch needs C

7.5. Soundness 213

$$\frac{(S \vdash \mathit{ref} : t')^* \qquad (C \vdash t' \leq t)^*}{S \vdash \{\mathsf{type}\ t, \mathsf{elem}\ \mathit{ref}^*\}\ \mathsf{ok}}$$

Data Instances {data b^* }

• The data instance is valid.

$$\overline{S \vdash \{\mathsf{data}\ b^*\}\ \mathsf{ok}}$$

Export Instances {name name, value externval}

- The external value externval must be valid with some external type externtype.
- Then the export instance is valid.

$$\frac{S \vdash externval : externtype}{S \vdash \{\mathsf{name}\ name, \mathsf{value}\ externval\}\ \mathsf{ok}}$$

Module Instances moduleinst

- Each function type functype_i in moduleinst.types must be valid.
- For each function address funcaddr_i in moduleinst funcaddrs, the external value func funcaddr_i must be valid with some external type func functype'_i.
- For each table address tableaddr_i in moduleinst.tableaddrs, the external value table tableaddr_i must be valid with some external type table tabletype_i.
- For each memory address $memaddr_i$ in module inst. memaddrs, the external value mem $memaddr_i$ must be valid with some external type mem $memtype_i$.
- For each global address globaladdr_i in moduleinst.globaladdrs, the external value global globaladdr_i must be valid with some external type global globaltype_i.
- For each element address elemadd r_i in module inst. elemaddrs, the element instance S. elems [elemadd r_i] must be valid.
- For each data address data addr $_i$ in module inst. data addrs, the data instance S. datas [data addr $_i$] must be valid.
- Each export instance exportins t_i in module inst. exports must be valid.
- For each export instance exportins t_i in module inst. exports, the name exportins t_i . name must be different from any other name occurring in module inst. exports.
- Let functype'* be the concatenation of all functype' in order.
- Let $table type^*$ be the concatenation of all $table type_i$ in order.
- Let $memtype^*$ be the concatenation of all $memtype_i$ in order.
- Let $globaltype^*$ be the concatenation of all $globaltype_i$ in order.
- Then the module instance is valid with *context* {types *functype**, funcs *functype*'*, tables *tabletype**, mems *memtype**, globals *globaltype**}.

```
(\vdash functype \ ok)^*
   (S \vdash \mathsf{func}\, funcaddr : \mathsf{func}\, functype')^*
                                                           (S \vdash \mathsf{table}\ table\ table\ table\ table\ table\ type)^*
(S \vdash \mathsf{mem}\ memaddr : \mathsf{mem}\ memtype)^*
                                                          (S \vdash \mathsf{global}\ globaladdr : \mathsf{global}\ globaltype)^*
                (S \vdash S.\mathsf{elems}[\mathit{elemaddr}] \ \mathsf{ok})^*
                                                            (S \vdash S.\mathsf{dataa}ddr] \ \mathsf{ok})^*
                      (S \vdash exportinst \text{ ok})^*
                                                        (exportinst.name)* disjoint
                      S \vdash \{\mathsf{types}\}
                                            functype^*,
                             funcaddrs funcaddr^*.
                             tableaddrs tableaddr^*
                             memaddrs memaddr^*
                             globaladdrs globaladdr^*
                             elemaddrs elemaddr^*
                             dataaddrs dataaddr^*
                             exports
                                            exportinst* } : {types functype*,
                                                                  funcs functype'^*.
                                                                  tables table type^*,
                                                                  mems memtype*.
                                                                  globals globaltype* }
```

7.5.3 Configuration Validity

To relate the WebAssembly *type system* to its *execution semantics*, the *typing rules for instructions* must be extended to *configurations* S; T, which relates the *store* to execution *threads*.

Configurations and threads are classified by their *result type*. In addition to the store S, threads are typed under a *return type resulttype*?, which controls whether and with which type a return instruction is allowed. This type is absent (ϵ) except for instruction sequences inside an administrative frame instruction.

Finally, *frames* are classified with *frame contexts*, which extend the *module contexts* of a frame's associated *module instance* with the *locals* that the frame contains.

Configurations S; T

- The store S must be valid.
- Under no allowed return type, the thread T must be valid with some result type $[t^*]$.
- Then the configuration is valid with the *result type* $[t^*]$.

$$\frac{\vdash S \text{ ok} \qquad S; \epsilon \vdash T : [t^*]}{\vdash S; T : [t^*]}$$

Threads F: $instr^*$

- Let *resulttype*? be the current allowed return type.
- The frame F must be valid with a context C.
- Let C' be the same *context* as C, but with return set to resulttype?
- Under context C', the instruction sequence $instr^*$ must be valid with some type $[] \to [t^*]$.
- Then the thread is valid with the *result type* $[t^*]$.

$$\frac{S \vdash F : C \qquad S; C, \mathsf{return} \ resulttype^? \vdash instr^* : [] \to [t^*]}{S; resulttype^? \vdash F; instr^* : [t^*]}$$

7.5. Soundness 215

Frames {locals val^* , module moduleinst}

- The module instance module inst must be valid with some module context C.
- Each value val_i in val^* must be valid with some value type t_i .
- Let t^* be the concatenation of all t_i in order.
- Let C' be the same *context* as C, but with the *value types* t^* prepended to the locals vector.
- Then the frame is valid with frame context C'.

$$\frac{S \vdash moduleinst : C \qquad (S \vdash val : t)^*}{S \vdash \{\mathsf{locals}\ val^*, \mathsf{module}\ moduleinst\} : (C, \mathsf{locals}\ t^*)}$$

7.5.4 Administrative Instructions

Typing rules for *administrative instructions* are specified as follows. In addition to the *context* C, typing of these instructions is defined under a given *store* S. To that end, all previous typing judgements $C \vdash prop$ are generalized to include the store, as in $S; C \vdash prop$, by implicitly adding S to all rules S is never modified by the pre-existing rules, but it is accessed in the extra rules for *administrative instructions* given below.

trap

• The instruction is valid with type $[t_1^*] \to [t_2^*]$, for any sequences of value types t_1^* and t_2^* .

$$\overline{S;C\vdash \mathsf{trap}: [t_1^*] \to [t_2^*]}$$

$ref.extern\ externaddr$

• The instruction is valid with type $[] \rightarrow [externref]$.

$$\overline{S; C \vdash \mathsf{ref.extern}\ externaddr} : [] \to [\mathsf{externref}]$$

ref funcaddr

- The external function value func funcaddr must be valid with external function type func functype.
- Then the instruction is valid with type $[] \rightarrow [funcref]$.

$$\frac{S \vdash \mathsf{func}\,\mathit{funcaddr} : \mathsf{func}\,\mathit{functype}}{S; C \vdash \mathsf{ref}\,\mathit{funcaddr} : [] \to [\mathsf{funcref}]}$$

invoke funcaddr

- The external function value func funcaddr must be valid with external function type func($[t_1^*] \rightarrow [t_2^*]$).
- Then the instruction is valid with type $[t_1^*] \rightarrow [t_2^*]$.

$$\frac{S \vdash \mathsf{func}\,\mathit{funcaddr} : \mathsf{func}\,\,[t_1^*] \to [t_2^*]}{S;C \vdash \mathsf{invoke}\,\mathit{funcaddr} : [t_1^*] \to [t_2^*]}$$

 $label_n\{instr_0^*\}\ instr^*$ end

- The instruction sequence $instr_0^*$ must be valid with some type $[t_1^n] \to [t_2^*]$.
- Let C' be the same *context* as C, but with the *result type* $[t_1^n]$ prepended to the labels vector.
- Under context C', the instruction sequence $instr^*$ must be valid with type $[] \to [t_2^*]$.
- Then the compound instruction is valid with type $[] \rightarrow [t_2^*]$.

$$\frac{S; C \vdash instr_0^* : [t_1^n] \rightarrow [t_2^*] \qquad S; C, \mathsf{labels}\, [t_1^n] \vdash instr^* : [] \rightarrow [t_2^*]}{S; C \vdash \mathsf{label}_n\{instr_0^*\}\ instr^* \ \mathsf{end} : [] \rightarrow [t_2^*]}$$

 $frame_n\{F\}\ instr^*\ end$

- Under the return type $[t^n]$, the thread F; $instr^*$ must be valid with result type $[t^n]$.
- Then the compound instruction is valid with type $[] \rightarrow [t^n]$.

$$\frac{S;[t^n] \vdash F; instr^*:[t^n]}{S; C \vdash \mathsf{frame}_n\{F\} \ instr^* \ \mathsf{end}:[] \to [t^n]}$$

7.5.5 Store Extension

Programs can mutate the *store* and its contained instances. Any such modification must respect certain invariants, such as not removing allocated instances or changing immutable definitions. While these invariants are inherent to the execution semantics of WebAssembly *instructions* and *modules*, *host functions* do not automatically adhere to them. Consequently, the required invariants must be stated as explicit constraints on the *invocation* of host functions. Soundness only holds when the *embedder* ensures these constraints.

The necessary constraints are codified by the notion of store *extension*: a store state S' extends state S, written $S \leq S'$, when the following rules hold.

Note: Extension does not imply that the new store is valid, which is defined separately *above*.

Store S

- ullet The length of S.funcs must not shrink.
- The length of S.tables must not shrink.
- ullet The length of S.mems must not shrink.
- The length of S.globals must not shrink.
- ullet The length of S.elems must not shrink.
- The length of S.datas must not shrink.
- For each function instance funcinst_i in the original S.funcs, the new function instance must be an extension of the old.
- For each table instance tableinst_i in the original S.tables, the new table instance must be an extension of the old.
- For each *memory instance meminst*_i in the original S.mems, the new memory instance must be an *extension* of the old.
- For each global instance globalinst_i in the original S.globals, the new global instance must be an extension of the old.

7.5. Soundness 217

- For each element instance elemins t_i in the original S elems, the new global instance must be an extension of the old.
- For each data instance datainst $_i$ in the original S.datas, the new global instance must be an extension of the old

```
S_1.\mathsf{funcs} = \mathit{funcinst}_1^* \qquad S_2.\mathsf{funcs} = \mathit{funcinst}_1'^* \mathit{funcinst}_2^* \qquad (\vdash \mathit{funcinst}_1 \preceq \mathit{funcinst}_1')^* \\ S_1.\mathsf{tables} = \mathit{tableinst}_1^* \qquad S_2.\mathsf{tables} = \mathit{tableinst}_1'^* \mathit{tableinst}_2^* \qquad (\vdash \mathit{funcinst}_1 \preceq \mathit{funcinst}_1')^* \\ S_1.\mathsf{mems} = \mathit{meminst}_1^* \qquad S_2.\mathsf{mems} = \mathit{meminst}_1'^* \mathit{meminst}_2^* \qquad (\vdash \mathit{tableinst}_1 \preceq \mathit{tableinst}_1')^* \\ S_1.\mathsf{globals} = \mathit{globalinst}_1^* \qquad S_2.\mathsf{globals} = \mathit{globalinst}_1'^* \mathit{globalinst}_2^* \qquad (\vdash \mathit{globalinst}_1 \preceq \mathit{meminst}_1')^* \\ S_1.\mathsf{elems} = \mathit{eleminst}_1^* \qquad S_2.\mathsf{globals} = \mathit{globalinst}_1'^* \mathit{eleminst}_2^* \qquad (\vdash \mathit{globalinst}_1 \preceq \mathit{globalinst}_1')^* \\ S_1.\mathsf{datas} = \mathit{datainst}_1^* \qquad S_2.\mathsf{datas} = \mathit{datainst}_1'^* \mathit{datainst}_2^* \qquad (\vdash \mathit{datainst}_1 \preceq \mathit{datainst}_1')^* \\ \end{cases}
```

Function Instance *funcinst*

· A function instance must remain unchanged.

$$\vdash funcinst \preceq funcinst$$

Table Instance tableinst

- The *table type tableinst*.type must remain unchanged.
- The length of *tableinst*.elem must not shrink.

$$\frac{n_1 \leq n_2}{\vdash \{\mathsf{type}\ tt, \mathsf{elem}\ (fa_1^?)^{n_1}\} \leq \{\mathsf{type}\ tt, \mathsf{elem}\ (fa_2^?)^{n_2}\}}$$

Memory Instance *meminst*

- The *memory type meminst*.type must remain unchanged.
- The length of *meminst*.data must not shrink.

$$\frac{n_1 \leq n_2}{\vdash \{\mathsf{type}\ mt, \mathsf{data}\ b_1^{n_1}\} \leq \{\mathsf{type}\ mt, \mathsf{data}\ b_2^{n_2}\}}$$

Global Instance globalinst

- The *global type globalinst*.type must remain unchanged.
- Let *mut t* be the structure of *globalinst*.type.
- If mut is const, then the value globalinst.value must remain unchanged.

$$\frac{mut = \mathsf{var} \lor val_1 = val_2}{\vdash \{\mathsf{type} \ (mut \ t), \mathsf{value} \ val_1\} \preceq \{\mathsf{type} \ (mut \ t), \mathsf{value} \ val_2\}}$$

Element Instance *eleminst*

• The vector *eleminst*.elem must either remain unchanged or shrink to length 0.

$$\frac{fa_1^* = fa_2^* \vee fa_2^* = \epsilon}{\vdash \{\mathsf{elem}\, fa_1^*\} \preceq \{\mathsf{elem}\, fa_2^*\}}$$

Data Instance datainst

• The vector datainst.data must either remain unchanged or shrink to length 0.

$$\frac{b_1^* = b_2^* \lor b_2^* = \epsilon}{\vdash \{\mathsf{data}\ b_1^*\} \preceq \{\mathsf{data}\ b_2^*\}}$$

7.5.6 Theorems

Given the definition of valid configurations, the standard soundness theorems hold.⁵²

Theorem (Preservation). If a configuration S; T is valid with result type $[t^*]$ (i.e., $\vdash S; T : [t^*]$), and steps to S'; T' (i.e., $S; T \hookrightarrow S'; T'$), then S'; T' is a valid configuration with the same result type (i.e., $\vdash S'; T' : [t^*]$). Furthermore, S' is an extension of S (i.e., $\vdash S \prec S'$).

A *terminal thread* is one whose sequence of *instructions* is a *result*. A terminal configuration is a configuration whose thread is terminal.

Theorem (Progress). If a *configuration* S; T is *valid* (i.e., $\vdash S; T : [t^*]$ for some *result type* $[t^*]$), then either it is terminal, or it can step to some configuration S'; T' (i.e., $S; T \hookrightarrow S'; T'$).

From Preservation and Progress the soundness of the WebAssembly type system follows directly.

Corollary (Soundness). If a *configuration* S; T is *valid* (i.e., $\vdash S; T : [t^*]$ for some *result type* $[t^*]$), then it either diverges or takes a finite number of steps to reach a terminal configuration S'; T' (i.e., $S; T \hookrightarrow *S'; T'$) that is valid with the same result type (i.e., $\vdash S'; T' : [t^*]$) and where S' is an *extension* of S (i.e., $\vdash S \preceq S'$).

In other words, every thread in a valid configuration either runs forever, traps, or terminates with a result that has the expected type. Consequently, given a *valid store*, no computation defined by *instantiation* or *invocation* of a valid module can "crash" or otherwise (mis)behave in ways not covered by the *execution* semantics given in this specification.

7.6 Change History

Since the original release 1.0 of the WebAssembly specification, a number of proposals for extensions have been integrated. The following sections provide an overview of what has changed.

⁵² A machine-verified version of the formalization and soundness proof is described in the following article: Conrad Watt. Mechanising and Verifying the WebAssembly Specification⁵³. Proceedings of the 7th ACM SIGPLAN Conference on Certified Programs and Proofs (CPP 2018). ACM 2018.

⁵³ https://dl.acm.org/citation.cfm?id=3167082

7.6.1 Release 2.0

Sign extension instructions

Added new numeric instructions for performing sign extension within integer representations⁵⁴.

• New *numeric instructions*: inn.extend N_s

Non-trapping float-to-int conversions

Added new conversion instructions that avoid trapping when converting a floating-point number to an integer⁵⁵.

• New *numeric instructions*: inn.trunc_sat_fmm_sx

Multiple values

Generalized the result type of blocks and functions to allow for multiple values; in addition, introduced the ability to have block parameters⁵⁶.

- Function types allow more than one result
- *Block types* can be arbitrary function types

Reference types

Added funcref and externref as new value types and respective instructions⁵⁷.

- New value types: reference types funcref and externref
- New reference instructions: ref.null, ref.func, ref.is_null
- Enrich parametric instruction: select with optional type immediate
- New declarative form of element segment

Table instructions

Added instructions to directly access and modify tables?

- Table types allow any reference type as element type
- New table instructions: table.get, table.set, table.size, table.grow

Multiple tables

Added the ability to use multiple tables per module?.

- Modules may define, import, and export multiple tables
- Table instructions take a table index immediate: table.get, table.set, table.size, table.grow, call_indirect
- Element segments take a table index

⁵⁴ https://github.com/WebAssembly/spec/tree/main/proposals/sign-extension-ops/

⁵⁵ https://github.com/WebAssembly/spec/tree/main/proposals/nontrapping-float-to-int-conversion/

⁵⁶ https://github.com/WebAssembly/spec/tree/main/proposals/multi-value/

⁵⁷ https://github.com/WebAssembly/spec/tree/main/proposals/reference-types/

Bulk memory and table instructions

Added instructions that modify ranges of memory or table entries²⁵⁸

- New memory instructions: memory.fill, memory.init, memory.copy, data.drop
- New table instructions: table.fill, table.init, table.copy, elem.drop
- New passive form of data segment
- New passive form of element segment
- New data count section in binary format
- · Active data and element segments boundaries are no longer checked at compile time but may trap instead

Vector instructions

Added vector type and instructions that manipulate multiple numeric values in parallel (also known as *SIMD*, single instruction multiple data)⁵⁹

- New value type: v128
- New *memory instructions*: v128.load, v128.load NxM_sx , v128.load N_zero , v128.load N_splat , v128.load N_splat , v128.load N_sero , v128.store, v128.store N_sero
- New constant vector instruction: v128.const
- New unary *vector instructions*: v128.not, iNxM.abs, iNxM.neg, i8x16.popcnt, fNxM.abs, fNxM.neg, fNxM.sqrt, fNxM.ceil, fNxM.floor, fNxM.trunc, fNxM.nearest
- New binary *vector instructions*: v128.and, v128.andnot, v128.or, v128.xor, iNxM.add, iNxM.sub, iNxM.mul, iNxM.add_sat_sx, iNxM.sub_sat_sx, iNxM.min_sx, iNxM.max_sx, iNxM.shl, iNxM.shr_sx, fNxM.add, iNxM.extmul_half_iN'xM'_sx, i16x8.q15mulr_sat_s, i32x4.dot_i16x8_s, i16x8.extadd_pairwise_i8x16_sx, i32x4.extadd_pairwise_i16x8_sx, i8x16.avgr_u, i16x8.avgr_u, fNxM.sub, fNxM.mul, fNxM.div, fNxM.min, fNxM.max, fNxM.pmin, fNxM.pmax
- New ternary vector instruction: v128.bitselect
- New test *vector instructions*: v128.any_true, iNxM.all_true
- New relational *vector instructions*: iNxM.eq, iNxM.ne, iNxM.lt_sx, iNxM.gt_sx, iNxM.le_sx, iNxM.ge_sx, fNxM.eq, fNxM.ne, fNxM.lt, fNxM.gt, fNxM.le, fNxM.ge
- New conversion vector instructions:i32x4.trunc_sat_f32x4_sx, i32x4.trunc_sat_f64x2_sx_zero, f32x4.convert_i32x4_sx, f32x4.demote_f64x2_zero, f64x2.convert_low_i32x4_sx, f64x2.promote_low_f32x4
- New lane access *vector instructions*: iNxM.extract_lane_sx?, iNxM.replace_lane, fNxM.extract_lane, fNxM.replace_lane
- New lane splitting/combining *vector instructions*: iNxM.extend_half_iN'xM'_sx, i8x16.narrow_i16x8_sx, i16x8.narrow_i32x4_sx
- New byte reordering vector instructions: i8x16.shuffle, i8x16.swizzle
- New injection/projection vector instructions: iNxM.splat, fNxM.splat, iNxM.bitmask

⁵⁸ https://github.com/WebAssembly/spec/tree/main/proposals/bulk-memory-operations/

⁵⁹ https://github.com/WebAssembly/spec/tree/main/proposals/simd/

7.6.2 Release 2.1

Typeful References

Todo: describe

Symbols	label, 69
: abstract syntax	label index, 20
administrative instruction, 70	limits, 11, 30
, · ·	local, 21, 54
A	local index, 20
abbreviations, 166	local type, 11
abstract syntax, 5 , 141, 165, 200	memory, 21, 55
block type, 18, 29	memory address, 66
byte, 7	memory index, 20
data, 22, 56	memory instance, 67
data address, 66	memory type, 11, 31
data index, 20	module, 20, 59
data instance, 68	module instance, 67
element, 22, 55	mutability, 12
element address, 66	name, 8
element index, 20	notation, 5
element instance, 68	number type, 9, 28
element mode, 22	reference type, 10,29
export, 23, 57	result,66
export instance, 68	result type, 10,30
expression, 20, 52, 129	signed integer,7
external type, 12, 31	start function, 23, 57
external type, 12, 31 external value, 68	store, 66
floating-point number, 7	table, 21, 54
frame, 69	table address,66
function, 21, 53	table index, 20
function address, 66	table instance, 67
function index, 20	table type, 11, 31
function instance, 67	type, 9
function type, 11, 30	type definition, 21
global, 22, 55	type index, 20
global address, 66	uninterpreted integer, 7
global index, 20	unsigned integer,7
global instance, 68	value, 6, 65
global type, 12, 31	value type, 10, 29
grammar, 5	vector, 6, 8
heap type, 9, 28	vector type, 28
host address, 66	activation, 69
import, 23, 58	active, 22 , 22
instruction, 12, 13, 16–18, 37–39, 42, 43, 45,	address, 66, 106, 108, 113, 122, 13
48, 95, 97, 98, 106, 108, 113, 122	data, 66
instruction type, 10, 30	element, 66
integer, 7	function, 66
inceger, /	global, 66

host, 66 memory, 66 table, 66 administrative instruction, 215, 216	uninterpreted integer, 143 unsigned integer, 143 value, 142 value type, 145
: abstract syntax, 70 administrative instructions, 70 algorithm, 202 allocation, 66, 131 , 194, 202 arithmetic NaN, 7 ASCII, 167, 168, 170	vector, 142 vector type, 144 bit, 73 bit width, 7, 9, 72, 113 block, 18, 48, 122, 127, 146, 173, 220 type, 18
В	block context, 71 block type, 18 , 29, 48, 146
binary format, 8, 141 , 194, 201, 202, 208 block type, 146 byte, 143 custom section, 159 data, 162 data count, 162 data index, 158	abstract syntax, 18 binary format, 146 validation, 29 Boolean, 3, 73, 74 bottom type, 10, 29 branch, 18, 48, 71, 122, 146, 173 byte, 7, 8, 22, 56, 67, 68, 74, 132, 141, 143, 162, 170,
element, 161	189, 190, 198, 213, 214
element index, 158 export, 160	abstract syntax, 7 binary format, 143
expression, 158	text format, 170
floating-point number, 143 function, 160, 161	С
function index, 158	call, 69, 70, 127
function type, 145	canonical NaN, 7
global, 160	changes, 219
global index, 158	character, 2, 8, 167 , 167, 168, 170, 200, 201
global type, 146	text format, 167
grammar, 141	closure, 67
heap type, 144	code, 12, 201
import, 159	section, 161
instruction, 146-149, 152	code section, 161
integer, 143	comment, 167, 168
label index, 158	concepts, 3
limits, 145	configuration, 64, 71 , 215, 219
local, 161	constant, 20, 22, 53 , 65
local index, 158	context, 25 , 36, 42, 43, 45, 48, 59, 163, 214–216
memory, 160	control instruction, 18
memory index, 158	control instructions, 48, 122, 146, 173
memory type, 146	custom section, 159, 208
module, 163 mutability, 146	binary format, 159
name, 143	D
notation, 141	
number type, 144	data, 20, 21, 22 , 56, 59, 70, 133, 162, 163, 189–191, 200
reference type, 145	abstract syntax, 22
result type, 145	address, 66
section, 158	binary format, 162
signed integer, 143	index, 20
start function, 161	instance, 68
table, 160	section, 162
table index, 158	segment, 22, 56, 162, 189, 190
table type, 146	text format, 189, 190
type, 144	validation, 56
type index, 158	data address, 67, 133
type section, 159	abstract syntax, 66

```
data count, 162
                                                       section, 160
    binary format, 162
                                                       text format, 187-189
    section, 162
                                                       validation, 57
data count section, 162
                                                   export instance, 67, 68, 135, 196, 214
data index, 20, 22, 158, 186
                                                       abstract syntax, 68
    abstract syntax, 20
                                                   export section, 160
    binary format, 158
                                                   expression, 20, 21, 22, 52, 53, 55, 56, 129, 158, 160-
    text format, 186
                                                            162, 185, 189, 190
data instance, 66, 67, 68, 133, 214, 219
                                                       abstract syntax, 20
    abstract syntax, 68
                                                       binary format, 158
data section, 162
                                                       constant, 20, 52, 158, 185
data segment, 67, 68, 162, 220
                                                       execution, 129
declarative, 22
                                                       text format, 185
decoding, 4
                                                       validation, 52
default value, 65
                                                   extern address, 216
defaultable, 32, 54
                                                   extern type, 216
design goals, 1
                                                   extern value, 216
determinism, 72, 95
                                                   external
                                                       type, 12
F
                                                       value, 68
                                                   external type, 12, 31, 35, 130, 135, 214
element, 11, 20, 21, 22, 55, 59, 70, 133, 161, 163, 188,
                                                       abstract syntax, 12
         190, 191, 197, 200
                                                       validation, 31
    abstract syntax, 22
                                                   external value, 12, 68, 68, 130, 135, 214
    address, 66
                                                       abstract syntax, 68
    binary format, 161
    index. 20
                                                   F
    instance, 68
    mode, 22
                                                   file extension, 141, 165
    section, 161
                                                   floating point, 2
    segment, 22, 55, 161, 188, 190
                                                   floating-point, 3, 7, 8, 9, 12, 65, 72, 73, 82, 220
    text format, 188, 190
                                                   floating-point number, 143, 169
    validation, 55
                                                       abstract syntax, 7
element address, 67, 108, 133
                                                       binary format, 143
    abstract syntax, 66
                                                       text format, 169
element expression, 68
                                                   folded instruction, 184
element index, 20, 22, 158, 186
                                                   frame, 69, 70, 71, 106, 108, 113, 122, 127, 202, 215,
    abstract syntax, 20
                                                            217
    binary format, 158
                                                       abstract syntax, 69
    text format, 186
                                                   function, 2, 3, 10, 11, 18, 20, 21, 23, 25, 53, 59, 67–
element instance, 66, 67, 68, 108, 133, 213, 218
                                                            70, 127, 131, 135, 139, 160, 161, 163, 187,
    abstract syntax, 68
                                                            191, 196, 200, 201, 210, 220
element mode, 22
                                                       abstract syntax, 21, 53
    abstract syntax, 22
                                                       address, 66
element section, 161
                                                       binary format, 160, 161
element segment, 67, 68, 220
                                                       export, 23
element type, 35
                                                       import, 23
embedder, 2, 3, 66-68, 193
                                                       index. 20
embedding, 193
                                                       instance, 67
evaluation context, 64, 71
                                                       section, 160
execution, 4, 9, 10, 63, 202
                                                       text format, 187
    expression, 129
                                                       type, 11
    instruction, 95, 97, 98, 106, 108, 113, 122
                                                   function address, 67, 68, 70, 130-132, 135, 139,
exponent, 7, 74
                                                            196, 197, 212, 216
export, 20, 23, 57, 59, 68, 135, 139, 160, 163, 187-
                                                       abstract syntax, 66
        189, 191, 195, 196, 200
                                                   function index, 18, 20, 21-23, 48, 53, 55, 57, 122,
    abstract syntax, 23
                                                            135, 146, 158, 160, 161, 173, 186–190, 210
    binary format, 160
                                                       abstract syntax, 20
    instance, 68
                                                       binary format, 158
```

```
text format, 186
                                                        address, 66
function instance, 66, 67, 67, 70, 127, 131, 132, host address, 65
         135, 139, 196, 202, 211, 212, 217, 218
                                                        abstract syntax, 66
                                                   host function, 67, 128, 132, 196, 212
    abstract syntax, 67
function section, 160
function type, 10, 11, 12, 18, 20, 21, 23, 25, 30, 31,
         34, 35, 53, 58, 59, 67, 95, 130–132, 139, 145,
                                                   identifier, 165, 166, 186-189, 191, 201
         159–161, 163, 172, 187, 191, 196, 211, 212,
                                                   identifier context, 166, 191
         216
                                                    identifiers, 170
    abstract syntax, 11
                                                        text format, 170
    binary format, 145
                                                   IEEE 754, 2, 3, 7, 9, 74, 82
    text format, 172
                                                    implementation, 193, 200
    validation, 30
                                                    implementation limitations, 200
                                                    import, 2, 12, 20-22, 23, 53, 58, 59, 130, 135, 159,
G
                                                             163, 187–189, 191, 195, 200
global, 12, 17, 20, 22, 23, 55, 59, 68, 133, 135, 160,
                                                        abstract syntax, 23
         163, 189, 191, 199, 200
                                                        binary format, 159
                                                        section, 159
    abstract syntax, 22
    address, 66
                                                        text format, 187-189
    binary format, 160
                                                        validation, 58
    export, 23
                                                    import section, 159
    import, 23
                                                    index, 20, 23, 57, 67, 158, 160, 166, 173, 186–189, 209
    index, 20
                                                        data, 20
    instance, 68
                                                        element, 20
    mutability, 12
                                                        function, 20
    section, 160
                                                        global, 20
    text format, 189
                                                        label, 20
    type, 12
                                                        loca1, 20
    validation, 55
                                                        memory, 20
global address, 67, 68, 106, 130, 133, 135, 199
                                                        table, 20
    abstract syntax, 66
                                                        type, 20
global index, 17, 20, 22, 23, 42, 57, 106, 135, 147, index space, 20, 23, 25, 166, 209
        158, 160, 174, 186, 189
                                                    instance, 67, 137
    abstract syntax, 20
                                                        data, 68
    binary format, 158
                                                        element, 68
    text format, 186
                                                        export, 68
global instance, 66, 67, 68, 106, 133, 135, 199, 202,
                                                        function, 67
         211, 213, 217, 218
                                                        global, 68
    abstract syntax, 68
                                                        memory, 67
global section, 160
                                                        module, 67
global type, 12, 12, 22, 23, 25, 31, 35, 55, 58, 130,
                                                        table, 67
         133, 146, 159, 160, 173, 187, 189, 199, 211,
                                                   instantiation, 4, 9, 23, 137, 195, 219
         213
                                                    instantiation. module, 25
    abstract syntax, 12
                                                    instruction, 3, 10, 12, 20, 36, 52, 67-71, 95, 127,
                                                             146, 173, 200, 202, 215–217, 220
    binary format, 146
    text format, 173
                                                        abstract syntax, 12, 13, 16-18
    validation, 31
                                                        binary format, 146-149, 152
globaltype, 25
                                                        execution, 95, 97, 98, 106, 108, 113, 122
grammar notation, 5, 141, 165
                                                        text format, 173-176, 179
grow, 134
                                                        type, 10
                                                        validation, 37-39, 42, 43, 45, 48
Η
                                                    instruction sequence, 52, 127
                                                   instruction type, 10, 29, 30, 36
heap type, 9, 10, 28, 29, 33, 144, 171
                                                        abstract syntax, 10
    abstract syntax, 9
                                                        validation, 30
    binary format, 144
                                                    instructions, 221
    text format. 171
                                                   integer, 3, 7, 8, 9, 12, 65, 72-74, 108, 113, 143, 169,
    validation, 28
                                                            220
host, 2, 193
```

```
abstract syntax, 7
                                                         export, 23
    binary format, 143
                                                         import, 23
    signed, 7
                                                        index, 20
    text format, 169
                                                        instance, 67
    uninterpreted, 7
                                                        limits, 11
    unsigned, 7
                                                        section, 160
invocation, 4, 67, 139, 196, 219
                                                        text format, 188
                                                        type, 11
K
                                                        validation, 55
                                                    memory address, 67, 68, 113, 130, 132, 134, 135, 198
keyword, 167
                                                        abstract syntax, 66
L
                                                    memory index, 17, 20, 21–23, 45, 56, 57, 113, 135,
                                                             148, 158, 160, 162, 175, 186, 189, 190
label, 18, 48, 69, 70, 71, 122, 127, 146, 173, 202, 216
                                                         abstract syntax, 20
    abstract syntax, 69
                                                        binary format, 158
    index. 20
                                                        text format, 186
label index, 18, 20, 48, 122, 146, 158, 173, 186
                                                    memory instance, 66, 67, 67, 70, 113, 132, 134, 135,
    abstract syntax, 20
                                                             198, 202, 211, 213, 217, 218
    binary format, 158
                                                        abstract syntax, 67
    text format, 173, 186
                                                    memory instruction, 17, 45, 113, 148, 175
lane, 8
                                                    memory section, 160
LEB128, 143, 146
                                                    memory type, 11, 11, 12, 21, 23, 25, 31, 35, 55, 58, 67,
lexical format, 167
                                                             130, 132, 146, 159, 160, 172, 187, 188, 198,
limits, 11, 11, 21, 30, 31, 34, 35, 108, 113, 132, 134,
                                                             211, 213
         145, 146, 172, 212, 213
                                                        abstract syntax, 11
    abstract syntax, 11
                                                        binary format, 146
    binary format, 145
                                                        text format, 172
    memory, 11
                                                        validation, 31
    table, 11
                                                    module, 2, 3, 20, 25, 59, 66, 67, 135, 137, 139, 141,
    text format, 172
                                                             163, 191, 194, 196, 200–202, 209, 219
    validation, 30
                                                         abstract syntax, 20
linear memory, 3
                                                        binary format, 163
little endian, 17, 74, 143
                                                        instance, 67
local, 10, 11, 17, 20, 21, 53, 54, 69, 161, 187, 200,
                                                        text format, 191
         210, 215
                                                        validation, 59
    abstract syntax, 21
                                                    module instance, 67, 69, 131, 135, 139, 195, 196,
    binary format, 161
                                                             202, 214, 215
    index, 20
                                                         abstract syntax, 67
    text format, 187
                                                    module instruction, 71
    type, 11
                                                    mutability, 12, 12, 22, 31, 35, 68, 130, 133, 146, 173,
    validation, 54
                                                             213, 218
local index, 10, 11, 17, 20, 21, 42, 53, 106, 147, 158,
                                                        abstract syntax, 12
         174, 186, 210
                                                        binary format, 146
    abstract syntax, 20
                                                        global, 12
    binary format, 158
                                                        text format, 173
    text format, 186
local type, 11, 25, 52-54
                                                    N
    abstract syntax, 11
                                                    name, 2, 8, 23, 57, 58, 67, 68, 143, 159, 160, 170, 187-
M
                                                             189, 200, 208, 214
                                                        abstract syntax, 8
magnitude, 7
                                                        binary format, 143
matching, 33, 135
                                                        text format, 170
memory, 3, 9, 11, 17, 20, 21, 22, 23, 55, 56, 59, 67, 68,
                                                    name map, 209
         70, 74, 132, 134, 135, 160, 162, 163, 188–
                                                    name section, 191, 208
         191, 198, 200, 220
                                                    NaN, 7, 72, 83, 95
    abstract syntax, 21
                                                        arithmetic, 7
    address, 66
                                                        canonical, 7
    binary format, 160
                                                        payload, 7
    data, 22, 56, 162, 189, 190
```

	0
notation, 5, 141, 165	S
abstract syntax,5	S-expression, 165, 184
binary format, 141	section, 158 , 163, 201, 208
text format, 165	binary format, 158
null, 10, 16	code, 161
number, 13, 65	custom, 159
type, 9	data, 162
number type, 9, 10, 28, 32–34, 65, 144, 145, 171, 172	data count, 162
abstract syntax, 9	element, 161
binary format, 144	export, 160
text format, 171	function, 160
validation, 28	global, 160
numeric instruction, 12 , 37, 95, 149, 176	import, 159
numeric vectors, 8, 13, 74	memory, 160
	name, 191
0	start, 161
offset, 20	table, 160
opcode, 146 , 202, 206	type, 159
operand, 12	security, 2
operand stack, 12, 36	
operation Stack, 12, 30	segment, 70
Р	shape, 74
•	sign, 74
page size, 11, 17, 21, 67 , 146, 172, 189	signed integer, 7, 74, 143, 169
parameter, 11, 20, 200	abstract syntax, 7
parametric instruction, 16, 147, 174	binary format, 143
parametric instructions, 42, 106	text format, 169
passive, 22 , 22	significand, 7, 74
payload, 7	SIMD, 8, 9, 13, 221
phases, 4	soundness, 210 , 219
polymorphism, 36 , 42, 48, 146, 147, 173, 174	source text, 167 , 167, 201
portability, 1	stack, 63, 69 , 139, 202
preservation, 219	stack machine, 12
progress, 219	stack type, 18
R	start function, 20, 23, 57, 59, 161, 163, 190, 191
	abstract syntax, 23
reduction rules, 64	binary format, 161
reference, 10, 16, 65, 97, 108, 213, 220, 222	section, 161
type, 10	text format, 190
reference instruction, 16, 147, 174	validation, 57
reference instructions, 38, 97	start section, 161
reference type, 10 , 10, 11, 29, 31–34, 38, 65, 108,	store, 9, 63, 66 , 66, 68, 69, 71, 95, 106, 108, 113, 122,
145, 146, 171, 172, 220	128, 130, 131, 137, 139, 194, 196–199, 211,
abstract syntax, 10	215–217
binary format, 145	abstract syntax, 66
text format, 171	store extension, 217
validation, 29	string, 170
result, 11, 66 , 196, 200, 211	text format, 170
abstract syntax, 66	structured control, 18 , 48, 122, 146, 173
type, 10	structured control instruction, 200
result type, 10, 10, 11, 25, 30, 34, 52, 122, 145, 146,	subtyping, 33
172, 173, 211, 215–217, 220	т
abstract syntax, 10	Т
binary format, 145	table, 3, 10, 11, 17, 18, 20, 21 , 22, 23, 54, 55, 59,
validation, 30	67, 68, 70, 132, 134, 135, 160, 163, 188, 191,
resulttype, 25	197, 200, 220
rewrite rule, 166	abstract syntax,21
rounding, 82	address, 66
runtime, 65	binary format, 160
,	•

```
element, 22, 55, 161, 188, 190
                                                        memory, 188
                                                        memory index, 186
    export, 23
    import, 23
                                                        memory type, 172
    index, 20
                                                        module, 191
                                                        mutability, 173
    instance, 67
    limits. 11
                                                        name, 170
    section, 160
                                                        notation, 165
    text format, 188
                                                        number type, 171
    type, 11
                                                        reference type, 171
    validation, 54
                                                        signed integer, 169
table address, 67, 68, 108, 122, 130, 132, 134, 135,
                                                        start function, 190
         197
                                                        string, 170
                                                        table, 188
    abstract syntax, 66
table index, 17, 20, 21-23, 43, 55, 57, 108, 135, 148,
                                                        table index, 186
         158, 160, 161, 175, 186, 188–190, 220
                                                        table type, 172
    abstract syntax, 20
                                                        token, 167
    binary format, 158
                                                        type, 171
    text format, 186
                                                        type definition, 186
table instance, 66, 67, 67, 70, 108, 122, 132, 134,
                                                        type index, 186
         135, 197, 202, 211, 212, 217, 218
                                                        type use, 186
    abstract syntax, 67
                                                        uninterpreted integer, 169
table instruction, 17, 43, 108, 148, 175
                                                        unsigned integer, 169
                                                        value, 168
table section, 160
table type, 11, 11, 12, 21, 23, 25, 31, 32, 35, 54, 58,
                                                        value type, 172
        67, 130, 132, 146, 159, 160, 172, 187, 188,
                                                        vector, 167
         197, 211, 212, 220
                                                        vector type, 171
    abstract syntax, 11
                                                        white space, 168
                                                   thread, 71, 215, 219
    binary format, 146
    text format. 172
                                                   token, 167, 201
                                                   trap, 3, 17, 18, 66, 70, 71, 95, 137, 139, 211, 216, 220
    validation, 31
terminal configuration, 219
                                                   two's complement, 3, 7, 12, 74, 143
text format, 2, 165, 194, 201
                                                   type, 9, 135, 144, 171, 200
    byte, 170
                                                        abstract syntax, 9
    character, 167
                                                        binary format, 144
    comment, 168
                                                        block, 18
    data, 189, 190
                                                        external, 12
    data index, 186
                                                        function, 11
    element, 188, 190
                                                        global, 12
    element index, 186
                                                        index, 20
    export, 187-189
                                                        instruction, 10
    expression, 185
                                                        local, 11
    floating-point number, 169
                                                        memory, 11
    function, 187
                                                        number, 9
    function index, 186
                                                        reference, 10
    function type, 172
                                                        result, 10
    global, 189
                                                        section, 159
    global index, 186
                                                        table, 11
    global type, 173
                                                        text format, 171
    grammar, 165
                                                        value, 10
    heap type, 171
                                                   type definition, 20, 21, 59, 159, 163, 186, 191
    identifiers, 170
                                                        abstract syntax, 21
    import, 187-189
                                                        text format, 186
                                                   type index, 9, 18, 20, 21, 23, 48, 53, 122, 146, 158,
    instruction, 173-176, 179
    integer, 169
                                                            160, 161, 173, 186, 187
    label index, 173, 186
                                                        abstract syntax, 20
    limits, 172
                                                        binary format, 158
    local, 187
                                                        text format, 186
    local index, 186
                                                   type section, 159
```

```
binary format, 159
                                                        type, 10
type system, 25, 210
                                                   value type, 10, 10-13, 16, 18, 21, 25, 29-32, 34, 35,
                                                            42, 53, 54, 65, 95, 113, 130, 133, 145–147,
type use, 186
    text format, 186
                                                            172–174, 202, 211, 215, 216, 220, 221
typing rules, 27
                                                       abstract syntax, 10
                                                       binary format, 145
U
                                                       text format, 172
                                                       validation, 29
Unicode, 2, 8, 143, 165, 167, 170, 200
                                                   variable instruction, 17
unicode, 201
                                                   variable instructions, 42, 106, 147, 174
Unicode UTF-8, 208
                                                   vector, 6, 11, 18, 22, 48, 122, 142, 146, 167, 173
uninterpreted integer, 7, 74, 143, 169
                                                        abstract syntax, 6, 8
    abstract syntax, 7
                                                       binary format, 142
    binary format, 143
                                                       text format, 167
    text format, 169
                                                   vector instruction, 13, 39, 98, 152, 179
unsigned integer, 7, 74, 143, 169
                                                   vector number, 65
    abstract syntax, 7
                                                   vector type, 9, 10, 28, 32, 33, 65, 144, 171, 172, 221
    binary format, 143
                                                       binary format, 144
    text format, 169
                                                       text format, 171
unwinding, 18
                                                       validation, 28
UTF-8, 2, 8, 143, 165, 170
                                                   version, 163
                                                   W
validation, 4, 9, 25, 95, 130, 194, 201, 202
                                                   white space, 167, 168
    block type, 29
    data, 56
    element, 55
    export, 57
    expression, 52
    external type, 31
    function type, 30
    global, 55
    global type, 31
    heap type, 28
    import, 58
    instruction, 37-39, 42, 43, 45, 48
    instruction type, 30
    limits, 30
    local, 54
    memory, 55
    memory type, 31
    module, 59
    number type, 28
    reference type, 29
    result type, 30
    start function, 57
    table, 54
    table type, 31
    value type, 29
    vector type, 28
validity, 219
valtype, 25
value, 3, 6, 12, 13, 22, 36, 65, 66, 68, 71, 72, 95, 106,
         108, 113, 130, 133, 139, 142, 168, 196, 199,
        202, 211, 213, 215, 218
    abstract syntax, 6, 65
    binary format, 142
    external, 68
    text format, 168
```