

06_evaluate_trading_signals

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1 Long-Short Strategy, Part 3: Evaluating our Boosting Model Signals

In this section, we'll start designing, implementing, and evaluating a trading strategy for US equities driven by daily return forecasts produced by gradient boosting models.

As in the previous examples, we'll lay out a framework and build a specific example that you can adapt to run your own experiments. There are numerous aspects that you can vary, from the asset class and investment universe to more granular aspects like the features, holding period, or trading rules. See, for example, the **Alpha Factor Library** in the [Appendix](#) for numerous additional features.

We'll keep the trading strategy simple and only use a single ML signal; a real-life application will likely use multiple signals from different sources, such as complementary ML models trained on different datasets or with different lookahead or lookback periods. It would also use sophisticated risk management, from simple stop-loss to value-at-risk analysis.

Six notebooks cover our workflow sequence:

1. [preparing_the_model_data](#): we engineer a few simple features from the Quandl Wiki data
2. [trading_signals_with_lightgbm_and_catboost](#): we tune hyperparameters for LightGBM and CatBoost to select a model, using 2015/16 as our validation period.
3. [evaluate_trading_signals](#) (this notebook): we compare the cross-validation performance using various metrics to select the best model.
4. [model_interpretation](#): we take a closer look at the drivers behind the best model's predictions.
5. [making_out_of_sample_predictions](#): we generate predictions for our out-of-sample test period 2017.
6. [backtesting_with_zipline](#): evaluate the historical performance of a long-short strategy based on our predictive signals using Zipline.

Cross-validation of numerous configurations has produced a large number of results. Now, we need to evaluate the predictive performance to identify the model that generates the most reliable and profitable signals for our prospective trading strategy.

1.1 Imports & Settings

```
[1]: import warnings  
warnings.filterwarnings('ignore')
```

```
[2]: %matplotlib inline

from time import time
from io import StringIO
import sys, os
import warnings
from pathlib import Path
import pandas as pd
import statsmodels.api as sm
import matplotlib.pyplot as plt
import seaborn as sns

import lightgbm as lgb

from scipy.stats import spearmanr, pearsonr

from alphalens import plotting
from alphalens import performance as perf
from alphalens.utils import get_clean_factor_and_forward_returns, ▾
    ↳rate_of_return, std_conversion
from alphalens.tears import (create_summary_tear_sheet,
                             create_full_tear_sheet)

[3]: sys.path.insert(1, os.path.join(sys.path[0], '..'))
from utils import MultipleTimeSeriesCV

[4]: sns.set_style('whitegrid')

[5]: YEAR = 252
idx = pd.IndexSlice

[6]: scope_params = ['lookahead', 'train_length', 'test_length']
daily_ic_metrics = ['daily_ic_mean', 'daily_ic_mean_n', 'daily_ic_median', ▾
    ↳'daily_ic_median_n']
lgb_train_params = ['learning_rate', 'num_leaves', 'feature_fraction', ▾
    ↳'min_data_in_leaf']
catboost_train_params = ['max_depth', 'min_child_samples']

[7]: results_path = Path('results', 'us_stocks')
if not results_path.exists():
    results_path.mkdir(parents=True)
```

1.2 Collect Data

We produced a larger number of LightGBM models because it runs an order of magnitude faster than CatBoost and will demonstrate some evaluation strategies accordingly.

1.2.1 LightGBM

Summary Metrics by Fold First, we collect the summary metrics computed for each fold and hyperparameter combination:

```
[8]: with pd.HDFStore(results_path / 'tuning_lgb.h5') as store:
    for i, key in enumerate(
        [k[1:] for k in store.keys() if k[1:].startswith('metrics')]):
        _, t, train_length, test_length = key.split('/')[-4]
        attrs = {
            'lookahead': t,
            'train_length': train_length,
            'test_length': test_length
        }
        s = store[key].to_dict()
        s.update(attrs)
        if i == 0:
            lgb_metrics = pd.Series(s).to_frame(i)
        else:
            lgb_metrics[i] = pd.Series(s)

    id_vars = scope_params + lgb_train_params + daily_ic_metrics
    lgb_metrics = pd.melt(lgb_metrics.T.drop('t', axis=1),
                          id_vars=id_vars,
                          value_name='ic',
                          var_name='boost_rounds').dropna().apply(pd.to_numeric)
```

```
[9]: lgb_metrics.to_hdf('data/model_tuning.h5', 'lgb/metrics')
lgb_metrics.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 2457 entries, 0 to 2456
Data columns (total 13 columns):
 #   Column           Non-Null Count  Dtype  
--- 
 0   lookahead        2457 non-null    int64  
 1   train_length     2457 non-null    int64  
 2   test_length      2457 non-null    int64  
 3   learning_rate    2457 non-null    float64 
 4   num_leaves       2457 non-null    float64 
 5   feature_fraction 2457 non-null    float64 
 6   min_data_in_leaf 2457 non-null    float64 
 7   daily_ic_mean    2457 non-null    float64 
 8   daily_ic_mean_n  2457 non-null    float64 
 9   daily_ic_median  2457 non-null    float64 
 10  daily_ic_median_n 2457 non-null    float64 
 11  boost_rounds     2457 non-null    int64  
 12  ic               2457 non-null    float64
```

```
dtypes: float64(9), int64(4)
memory usage: 268.7 KB
```

```
[10]: lgb_metrics.groupby(scope_params).size()
```

```
[10]: lookahead  train_length  test_length
      1          756           63        351
                  1134           63        486
      5          756           63        324
                  1134           63        486
     21          756           63        324
                  1134           63        486
      dtype: int64
```

Information Coefficient by Day Next, we retrieve the IC per day computed during cross-validation:

```
[11]: int_cols = ['lookahead', 'train_length', 'test_length', 'boost_rounds']
```

```
[12]: lgb_ic = []
with pd.HDFStore(results_path / 'tuning_lgb.h5') as store:
    keys = [k[1:] for k in store.keys()]
    for key in keys:
        _, t, train_length, test_length = key.split('/')[-4]
        if key.startswith('daily_ic'):
            df = (store[key]
                    .drop(['boosting', 'objective', 'verbose'], axis=1)
                    .assign(lookahead=t,
                           train_length=train_length,
                           test_length=test_length))
            lgb_ic.append(df)
lgb_ic = pd.concat(lgb_ic).reset_index()
```

```
[13]: id_vars = ['date'] + scope_params + lgb_train_params
lgb_ic = pd.melt(lgb_ic,
                 id_vars=id_vars,
                 value_name='ic',
                 var_name='boost_rounds').dropna()
lgb_ic.loc[:, int_cols] = lgb_ic.loc[:, int_cols].astype(int)
```

```
[14]: lgb_ic.to_hdf('data/model_tuning.h5', 'lgb/ic')
lgb_ic.info(null_counts=True)
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 1564369 entries, 0 to 1788695
Data columns (total 10 columns):
 #   Column           Non-Null Count  Dtype  
---  -- 
 0   date             1564369 non-null  datetime64[ns]
 1   ic               1564369 non-null  float64
 2   boost_rounds     1564369 non-null  int64  
 3   lookahead        1564369 non-null  int64  
 4   train_length     1564369 non-null  int64  
 5   test_length      1564369 non-null  int64  
 6   objective        1564369 non-null  float64
 7   verbose          1564369 non-null  float64
 8   boosting         1564369 non-null  float64
 9   null_counts      1564369 non-null  int64 
```

```

0    date          1564369 non-null  datetime64[ns]
1    lookahead     1564369 non-null  int64
2    train_length  1564369 non-null  int64
3    test_length   1564369 non-null  int64
4    learning_rate 1564369 non-null  float64
5    num_leaves    1564369 non-null  int64
6    feature_fraction 1564369 non-null  float64
7    min_data_in_leaf 1564369 non-null  int64
8    boost_rounds   1564369 non-null  int64
9    ic             1564369 non-null  float64
dtypes: datetime64[ns](1), float64(3), int64(6)
memory usage: 131.3 MB

```

```
[15]: lgb_daily_ic = lgb_ic.groupby(id_vars[1:] + ['boost_rounds']).ic.mean()
      .to_frame('ic').reset_index()
lgb_daily_ic.to_hdf('data/model_tuning.h5', 'lgb/daily_ic')
lgb_daily_ic.info()
```

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 3105 entries, 0 to 3104
Data columns (total 9 columns):
 #   Column           Non-Null Count  Dtype  
---  --  
 0   lookahead        3105 non-null   int64  
 1   train_length     3105 non-null   int64  
 2   test_length      3105 non-null   int64  
 3   learning_rate    3105 non-null   float64 
 4   num_leaves       3105 non-null   int64  
 5   feature_fraction 3105 non-null   float64 
 6   min_data_in_leaf 3105 non-null   int64  
 7   boost_rounds     3105 non-null   int64  
 8   ic               3105 non-null   float64 
dtypes: float64(3), int64(6)
memory usage: 218.4 KB

```

```
[16]: lgb_ic = pd.read_hdf('data/model_tuning.h5', 'lgb/ic')
lgb_daily_ic = pd.read_hdf('data/model_tuning.h5', 'lgb/daily_ic')
```

1.2.2 CatBoost

We proceed similarly for CatBoost:

Summary Metrics

```
[17]: with pd.HDFStore(results_path / 'tuning_catboost.h5') as store:
    for i, key in enumerate(
        [k[1:] for k in store.keys() if k[1:].startswith('metrics')]):
        _, t, train_length, test_length = key.split('/')[-4]
```

```

        attrs = {
            'lookahead' : t,
            'train_length': train_length,
            'test_length' : test_length
        }
        s = store[key].to_dict()
        s.update(attrs)
        if i == 0:
            catboost_metrics = pd.Series(s).to_frame(i)
        else:
            catboost_metrics[i] = pd.Series(s)

    id_vars = scope_params + catboost_train_params + daily_ic_metrics
    catboost_metrics = pd.melt(catboost_metrics.T.drop('t', axis=1),
                               id_vars=id_vars,
                               value_name='ic',
                               var_name='boost_rounds').dropna().apply(pd.
→to_numeric)

```

[18]: catboost_metrics.info()

```

<class 'pandas.core.frame.DataFrame'>
Int64Index: 1176 entries, 0 to 1175
Data columns (total 11 columns):
 #   Column           Non-Null Count  Dtype  
--- 
 0   lookahead        1176 non-null   int64  
 1   train_length     1176 non-null   int64  
 2   test_length      1176 non-null   int64  
 3   max_depth        1176 non-null   float64 
 4   min_child_samples 1176 non-null   float64 
 5   daily_ic_mean    1176 non-null   float64 
 6   daily_ic_mean_n  1176 non-null   float64 
 7   daily_ic_median  1176 non-null   float64 
 8   daily_ic_median_n 1176 non-null   float64 
 9   boost_rounds     1176 non-null   int64  
 10  ic               1176 non-null   float64 

dtypes: float64(7), int64(4)
memory usage: 110.2 KB

```

[19]: catboost_metrics.groupby(scope_params).size()

	lookahead	train_length	test_length
1	252	21	168
	756	63	168
	1134	63	168
5	252	21	168

```

    756      63      168
21     252      63      168
        756      63      168
dtype: int64

```

Daily Information Coefficient

```
[20]: catboost_ic = []
with pd.HDFStore(results_path / 'tuning_catboost.h5') as store:
    keys = [k[1:] for k in store.keys()]
    for key in keys:
        _, t, train_length, test_length = key.split('/')[-4]
        if key.startswith('daily_ic'):
            df = (store[key].drop('task_type', axis=1)
                  .assign(lookahead=t,
                          train_length=train_length,
                          test_length=test_length))
            catboost_ic.append(df)
catboost_ic = pd.concat(catboost_ic).reset_index()
```

```
[21]: id_vars = ['date'] + scope_params + catboost_train_params
catboost_ic = pd.melt(catboost_ic,
                      id_vars=id_vars,
                      value_name='ic',
                      var_name='boost_rounds').dropna()
catboost_ic.loc[:, int_cols] = catboost_ic.loc[:, int_cols].astype(int)
```

```
[22]: catboost_ic.to_hdf('data/model_tuning.h5', 'catboost/ic')
catboost_ic.info(null_counts=True)
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 592704 entries, 0 to 592703
Data columns (total 8 columns):
 #   Column           Non-Null Count  Dtype  
--- 
 0   date             592704 non-null   datetime64[ns]
 1   lookahead         592704 non-null   int64  
 2   train_length      592704 non-null   int64  
 3   test_length       592704 non-null   int64  
 4   max_depth         592704 non-null   int64  
 5   min_child_samples 592704 non-null   int64  
 6   boost_rounds      592704 non-null   int64  
 7   ic                592704 non-null   float64
dtypes: datetime64[ns](1), float64(1), int64(6)
memory usage: 40.7 MB
```

```
[23]: catboost_daily_ic = catboost_ic.groupby(id_vars[1:] + ['boost_rounds']).ic.
    ↪mean().to_frame('ic').reset_index()
catboost_daily_ic.to_hdf('data/model_tuning.h5', 'catboost/daily_ic')
catboost_daily_ic.info()
```

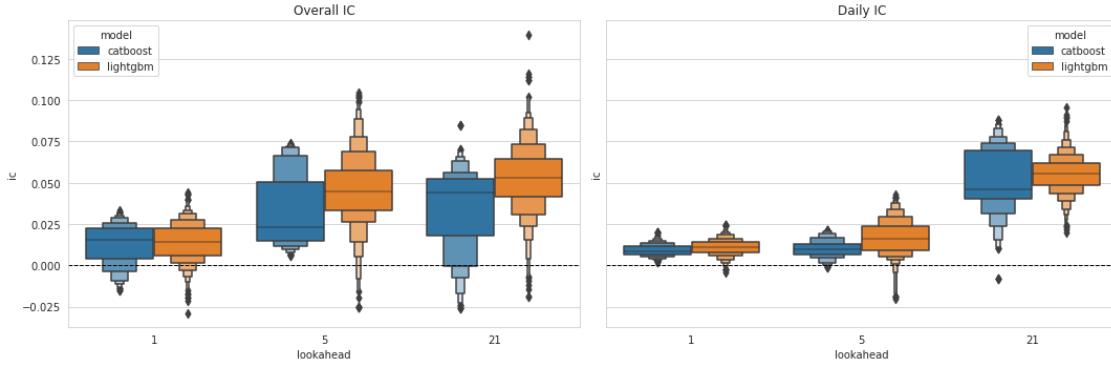
```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1176 entries, 0 to 1175
Data columns (total 7 columns):
 #   Column           Non-Null Count  Dtype  
---  --  
 0   lookahead        1176 non-null    int64  
 1   train_length     1176 non-null    int64  
 2   test_length      1176 non-null    int64  
 3   max_depth        1176 non-null    int64  
 4   min_child_samples 1176 non-null    int64  
 5   boost_rounds     1176 non-null    int64  
 6   ic               1176 non-null    float64 
dtypes: float64(1), int64(6)
memory usage: 64.4 KB
```

```
[24]: catboost_ic = pd.read_hdf('data/model_tuning.h5', 'catboost/ic')
catboost_daily_ic = pd.read_hdf('data/model_tuning.h5', 'catboost/daily_ic')
```

1.3 Validation Performance: Daily vs Overall Information Coefficient

The following image shows that LightGBM (in orange) performs (slightly) better than CatBoost, especially for longer horizons. This is not an entirely fair comparison because we ran more configurations for LightGBM, which also, unsurprisingly, shows a wider dispersion of outcomes:

```
[25]: fig, axes = plt.subplots(ncols=2, figsize=(15, 5), sharey=True)
sns.boxenplot(x='lookahead', y='ic', hue='model',
               data=catboost_metrics.assign(model='catboost')
                  .append(lgb_metrics.assign(model='lightgbm')), ax=axes[0])
axes[0].axhline(0, ls='--', lw=1, c='k')
axes[0].set_title('Overall IC')
sns.boxenplot(x='lookahead', y='ic', hue='model',
               data=catboost_daily_ic.assign(model='catboost')
                  .append(lgb_daily_ic.assign(model='lightgbm')), ax=axes[1])
axes[1].axhline(0, ls='--', lw=1, c='k')
axes[1].set_title('Daily IC')
fig.tight_layout()
```



1.4 HyperParameter Impact: Linear Regression

Next, we'd like to understand if there's a systematic, statistical relationship between the hyperparameters and the outcomes across daily predictions. To this end, we will run a linear regression using the various LightGBM hyperparameter settings as dummy variables and the daily validation IC as the outcome.

The below chart shows the coefficient estimates and their confidence intervals for 1- and 21-day forecast horizons. - For the shorter horizon, a longer lookback period, a higher learning rate, and deeper trees (more leaf nodes) have a positive impact. - For the longer horizon, the picture is a little less clear: shorter trees do better, but the lookback period is not significant. A higher feature sampling rate also helps. In both cases, a larger ensemble does better.

Note that these results apply to this specific example only.

```
[29]: lin_reg = {}
for t in [1, 21]:
    df_ = lgb_ic[lgb_ic.lookahead==t]
    y, X = df_.ic, df_.drop(['ic'], axis=1)
    X = sm.add_constant(pd.get_dummies(X, columns=X.columns, drop_first=True))
    model = sm.OLS(endog=y, exog=X)
    lin_reg[t] = model.fit()
    s = lin_reg[t].summary()
    coefs = pd.read_csv(StringIO(s.tables[1].as_csv())).rename(columns=lambda x: x.strip())
    coefs.columns = ['variable', 'coef', 'std_err', 't', 'p_value', 'ci_low', 'ci_high']
    coefs.to_csv(f'results/linreg_result_{t:02}.csv', index=False)
```

```
[30]: def visualize_lr_result(model, ax):
    ci = model.conf_int()
    errors = ci[1].sub(ci[0]).div(2)

    coefs = (model.params.to_frame('coef').assign(error=errors)
             .reset_index().rename(columns={'index': 'variable'}))
```

```

coefs = coefs[~coefs['variable'].str.startswith('date') & (coefs.variable != 'const')]

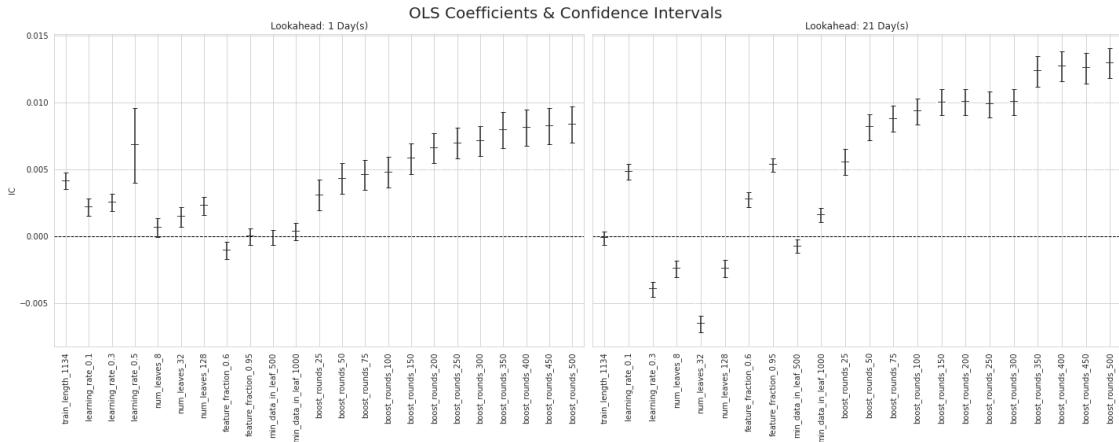
coefs.plot(x='variable', y='coef', kind='bar',
           ax=ax, color='none', capsize=3,
           yerr='error', legend=False)
ax.set_ylabel('IC')
ax.set_xlabel('')
ax.scatter(x=pd.np.arange(len(coefs)), marker='_', s=120, y=coefs['coef'], color='black')
ax.axhline(y=0, linestyle='--', color='black', linewidth=1)
ax.xaxis.set_ticks_position('none')

```

```

[31]: fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(20, 8), sharey=True)
axes = axes.flatten()
for i, t in enumerate([1, 21]):
    visualize_lr_result(lin_reg[t], axes[i])
    axes[i].set_title(f'Lookahead: {t} Day(s)')
fig.suptitle('OLS Coefficients & Confidence Intervals', fontsize=20)
fig.tight_layout()
fig.subplots_adjust(top=.92);

```



1.5 Cross-validation Result: Best Hyperparameters

1.5.1 LightGBM

The top-performing LightGBM models use the following parameters for the three different prediction horizons.

```

[32]: group_cols = scope_params + lgb_train_params + ['boost_rounds']
lgb_daily_ic.groupby('lookahead', group_keys=False).apply(lambda x: x.
    nlargest(3, 'ic'))

```

```
[32]:      lookahead train_length test_length learning_rate num_leaves \
595          1        1134         63        0.01       128
596          1        1134         63        0.01       128
610          1        1134         63        0.01       128
1569         5        1134         63        0.10        4
1568         5        1134         63        0.10        4
1570         5        1134         63        0.10        4
2260        21        756          63        0.10       128
2261        21        756          63        0.10       128
2262        21        756          63        0.10       128

      feature_fraction min_data_in_leaf boost_rounds      ic
595            0.95           250        400  0.024674
596            0.95           250        450  0.024292
610            0.95           500        500  0.024198
1569            0.30           500        400  0.042814
1568            0.30           500        350  0.041771
1570            0.30           500        450  0.041151
2260            0.95          1000         25  0.095405
2261            0.95          1000         50  0.091278
2262            0.95          1000         75  0.089669
```

```
[33]: lgb_metrics.groupby('lookahead', group_keys=False).apply(lambda x: x.
    ↪nlargest(3, 'ic'))
lgb_metrics.groupby('lookahead', group_keys=False).apply(lambda x: x.
    ↪nlargest(3, 'ic')).to_csv('results/best_lgb_model.csv', index=False)
```

```
[34]: lgb_metrics.groupby('lookahead', group_keys=False).apply(lambda x: x.
    ↪nlargest(3, 'daily_ic_mean'))
```

```
[34]:      lookahead train_length test_length learning_rate num_leaves \
267          1        1134         63        0.01      128.0
540          1        1134         63        0.01      128.0
813          1        1134         63        0.01      128.0
63           5        1134         63        0.10      4.0
336          5        1134         63        0.10      4.0
609          5        1134         63        0.10      4.0
120         21        756          63        0.10      128.0
393         21        756          63        0.10      128.0
666         21        756          63        0.10      128.0

      feature_fraction min_data_in_leaf daily_ic_mean daily_ic_mean_n \
267            0.95           250.0     0.024674      400.0
540            0.95           250.0     0.024674      400.0
813            0.95           250.0     0.024674      400.0
63             0.30           500.0     0.042814      400.0
336            0.30           500.0     0.042814      400.0
```

609	0.30	500.0	0.042814	400.0
120	0.95	1000.0	0.095405	25.0
393	0.95	1000.0	0.095405	25.0
666	0.95	1000.0	0.095405	25.0
267	0.023807	500.0	10 -0.002447	
540	0.023807	500.0	25 -0.000077	
813	0.023807	500.0	50 -0.000030	
63	0.038330	500.0	10 0.055980	
336	0.038330	500.0	25 0.055506	
609	0.038330	500.0	50 0.045449	
120	0.099453	25.0	10 0.082795	
393	0.099453	25.0	25 0.076064	
666	0.099453	25.0	50 0.072365	

1.5.2 CatBoost

```
[35]: group_cols = scope_params + catboost_train_params + ['boost_rounds']
catboost_daily_ic.groupby('lookahead', group_keys=False).apply(lambda x: x.
    ↪nlargest(3, 'ic'))
```

341	1	1134	63	3	20
355	1	1134	63	3	250
369	1	1134	63	3	500
679	5	756	63	3	20
693	5	756	63	3	250
707	5	756	63	3	500
1051	21	756	63	5	20
1065	21	756	63	5	250
1079	21	756	63	5	500
341	200	0.019974			
355	200	0.019974			
369	200	0.019973			
679	400	0.021375			
693	400	0.021375			
707	400	0.021375			
1051	25	0.088109			
1065	25	0.088109			
1079	25	0.088109			

```
[36]: catboost_metrics.groupby('lookahead', group_keys=False).apply(lambda x: x.
    ↪nlargest(3, 'ic'))
```

```
[36]:      lookahead  train_length  test_length  max_depth  min_child_samples \
920          1           1134          63        5.0            500.0
836          1           1134          63        5.0            500.0
1172         1           1134          63        5.0            500.0
935          5            756          63        3.0            500.0
1102         5            756          63        3.0            250.0
513          5            756          63        3.0            20.0
33           21           756          63        3.0            20.0
34           21           756          63        3.0            250.0
35           21           756          63        3.0            500.0

      daily_ic_mean  daily_ic_mean_n  daily_ic_median  daily_ic_median_n \
920       0.015616          10.0       0.016628          10.0
836       0.015616          10.0       0.016628          10.0
1172      0.015616          10.0       0.016628          10.0
935       0.021375         400.0       0.021886         600.0
1102      0.021375         400.0       0.021290         300.0
513       0.021375         400.0       0.021886         600.0
33        0.077041         500.0       0.094301         300.0
34        0.077041         500.0       0.094301         300.0
35        0.076753         500.0       0.094931         300.0

      boost_rounds      ic
920          700  0.032989
836          600  0.032336
1172         1000 0.032125
935          800  0.073752
1102         1000 0.073468
513          300  0.073285
33           10   0.085074
34           10   0.085074
35           10   0.085074
```

```
[37]: catboost_metrics.groupby('lookahead', group_keys=False).apply(lambda x: x.
    ↪nlargest(3, 'daily_ic_mean'))
```

```
[37]:      lookahead  train_length  test_length  max_depth  min_child_samples \
81           1           1134          63        3.0            20.0
82           1           1134          63        3.0            250.0
165          1           1134          63        3.0            20.0
9            5            756          63        3.0            20.0
10           5            756          63        3.0            250.0
11           5            756          63        3.0            500.0
30          21           756          63        5.0            20.0
31          21           756          63        5.0            250.0
32          21           756          63        5.0            500.0
```

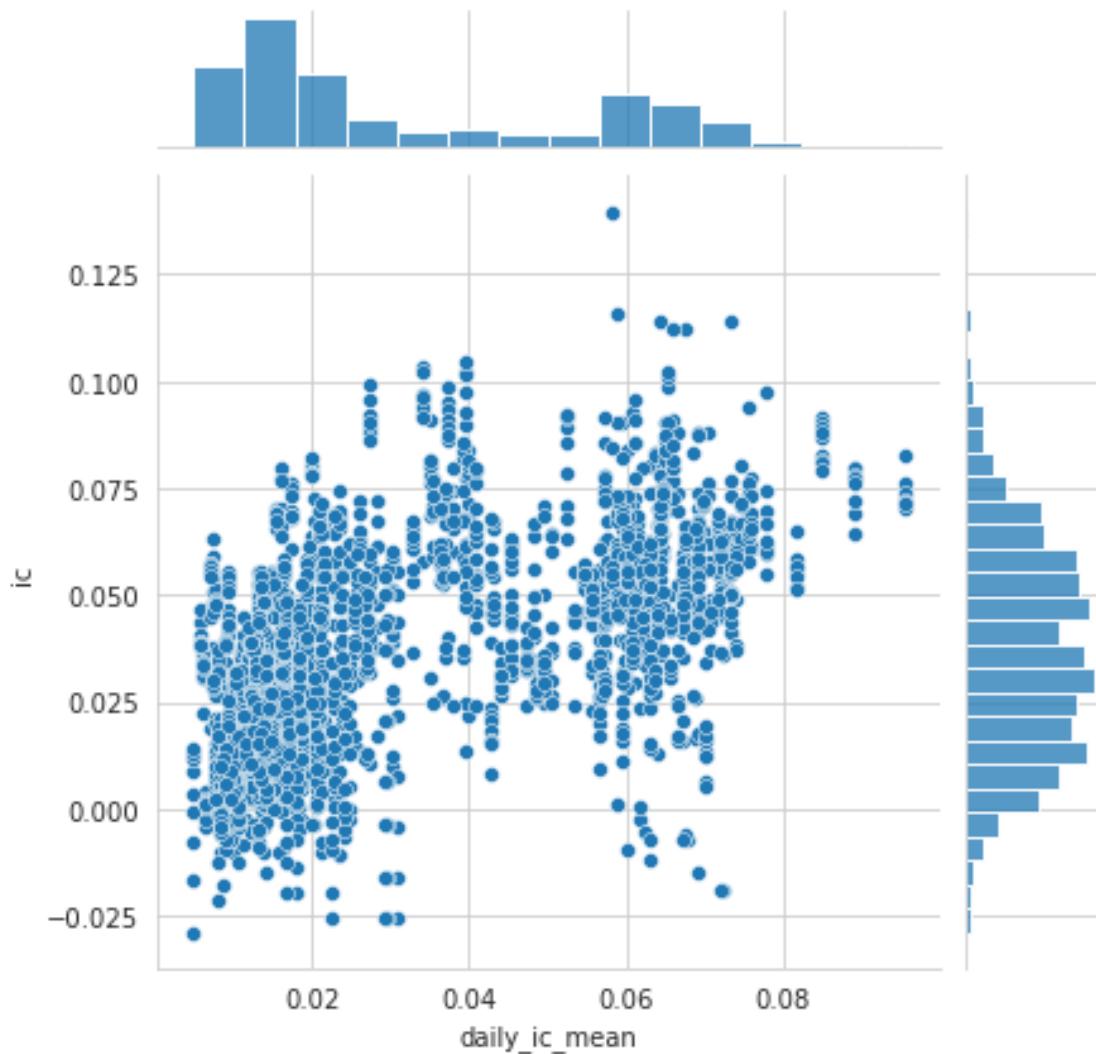
```

    daily_ic_mean   daily_ic_mean_n   daily_ic_median   daily_ic_median_n  \
81      0.019974           200.0      0.019573          300.0
82      0.019974           200.0      0.019452          300.0
165     0.019974           200.0      0.019573          300.0
9       0.021375           400.0      0.021886          600.0
10      0.021375           400.0      0.021290          300.0
11      0.021375           400.0      0.021886          600.0
30      0.088109            25.0      0.098979          50.0
31      0.088109            25.0      0.098979          50.0
32      0.088109            25.0      0.098979          50.0

  boost_rounds      ic
81        10  0.011191
82        10  0.011191
165       25  0.013491
9         10  0.012467
10        10  0.012467
11        10  0.012467
30        10 -0.004620
31        10 -0.004620
32        10 -0.004620

```

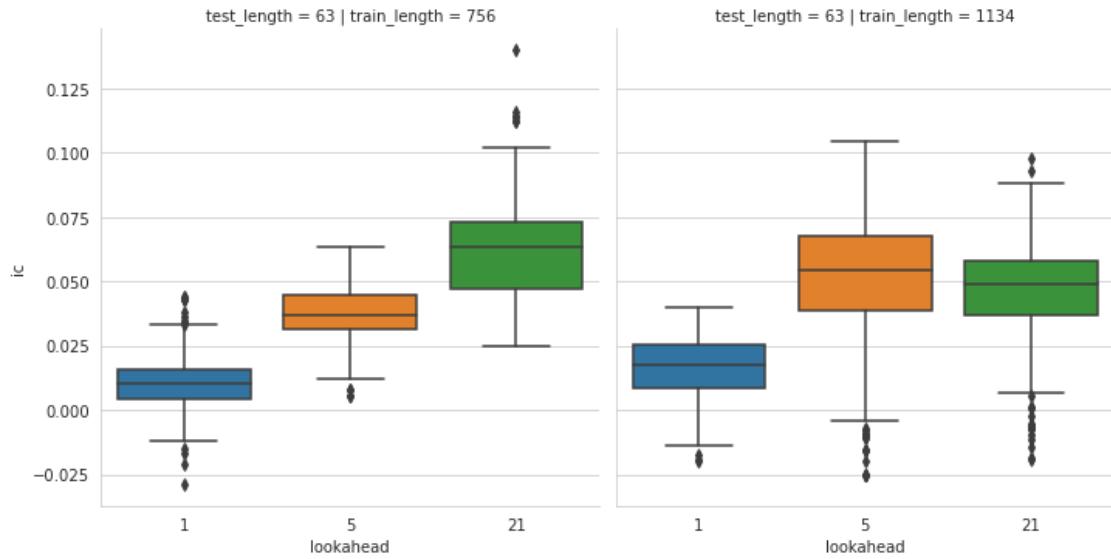
```
[39]: sns.jointplot(x=lgb_metrics.daily_ic_mean,y=lgb_metrics.ic);
```



1.5.3 Visualization

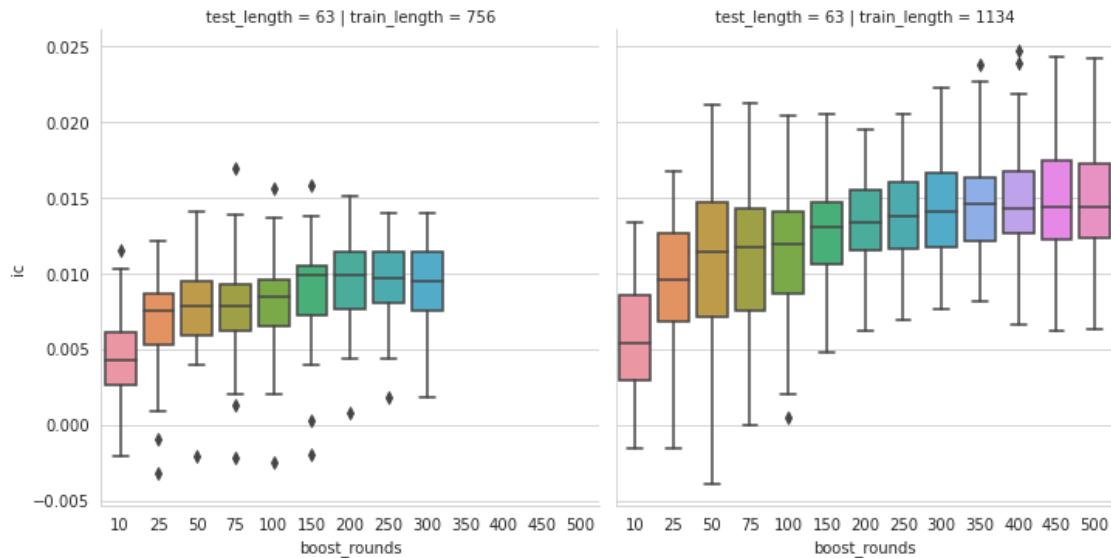
LightGBM

```
[40]: g = sns.catplot(x='lookahead', y='ic',
                     col='train_length', row='test_length',
                     data=lgb_metrics,
                     kind='box')
```



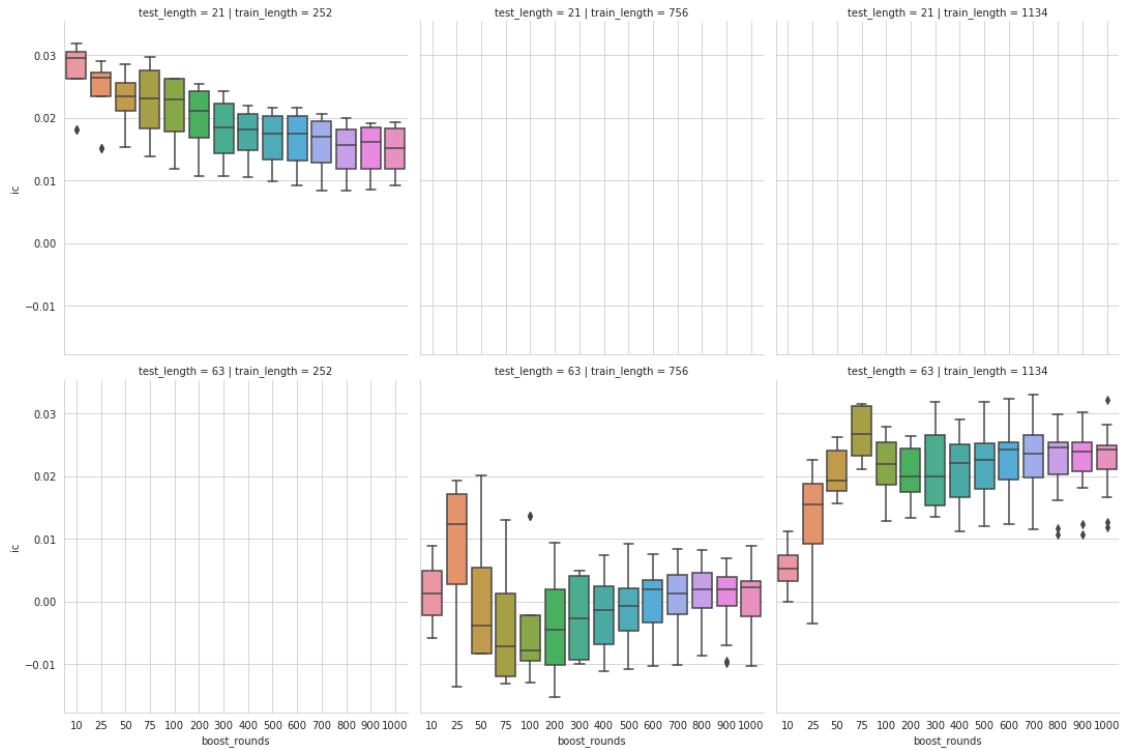
[41]: t=1

```
g=sns.catplot(x='boost_rounds',
               y='ic',
               col='train_length',
               row='test_length',
               data=lgb_daily_ic[lgb_daily_ic.lookahead == t],
               kind='box')
```

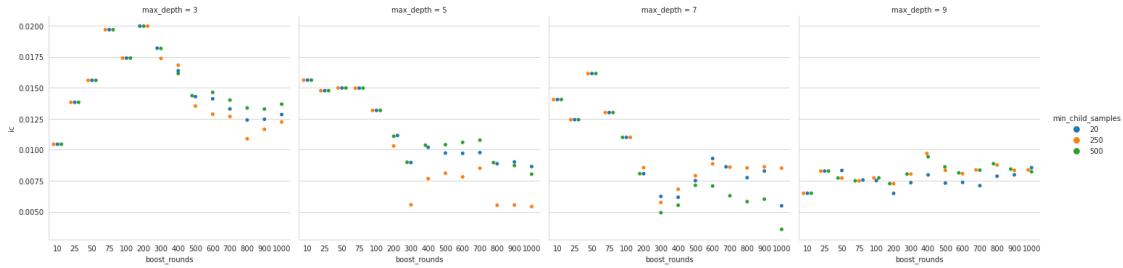


CatBoost Some figures are empty because we did not run those parameter combinations.

```
[42]: t = 1
g=sns.catplot(x='boost_rounds',
               y='ic',
               col='train_length',
               row='test_length',
               data=catboost_metrics[catboost_metrics.lookahead == t],
               kind='box')
```



```
[43]: t = 1
train_length = 1134
test_length = 63
g = sns.catplot(
    x='boost_rounds',
    y='ic',
    col='max_depth',
    hue='min_child_samples',
    data=catboost_daily_ic[(catboost_daily_ic.lookahead == t) &
                           (catboost_daily_ic.train_length == train_length) &
                           (catboost_daily_ic.test_length == test_length)],
    kind='swarm')
```



1.6 AlphaLens Analysis - Validation Performance

1.6.1 LightGBM

Select Parameters

```
[44]: lgb_daily_ic = pd.read_hdf('data/model_tuning.h5', 'lgb/daily_ic')
lgb_daily_ic.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 3105 entries, 0 to 3104
Data columns (total 9 columns):
 #   Column           Non-Null Count  Dtype  
---  --  
 0   lookahead        3105 non-null   int64  
 1   train_length     3105 non-null   int64  
 2   test_length      3105 non-null   int64  
 3   learning_rate    3105 non-null   float64 
 4   num_leaves       3105 non-null   int64  
 5   feature_fraction 3105 non-null   float64 
 6   min_data_in_leaf 3105 non-null   int64  
 7   boost_rounds     3105 non-null   int64  
 8   ic               3105 non-null   float64 
dtypes: float64(3), int64(6)
memory usage: 242.6 KB
```

```
[45]: def get_lgb_params(data, t=5, best=0):
    param_cols = scope_params[1:] + lgb_train_params + ['boost_rounds']
    df = data[data.lookahead==t].sort_values('ic', ascending=False).iloc[best]
    return df.loc[param_cols]
```

```
[46]: def get_lgb_key(t, p):
    key = f'{t}/{int(p.train_length)}/{int(p.test_length)}/{p.learning_rate}/'
    return key + f'{int(p.num_leaves)}/{p.feature_fraction}/{int(p.
    ↴min_data_in_leaf)}'
```

```
[47]: best_params = get_lgb_params(lgb_daily_ic, t=1, best=0)
best_params
```

```
[47]: train_length      1134.00
test_length        63.00
learning_rate       0.01
num_leaves         128.00
feature_fraction    0.95
min_data_in_leaf   250.00
boost_rounds        400.00
Name: 595, dtype: float64
```

```
[48]: best_params.to_hdf('data.h5', 'best_params')
```

Plot rolling IC

```
[49]: def select_ic(params, ic_data, lookahead):
    return ic_data.loc[(ic_data.lookahead == lookahead) &
                        (ic_data.train_length == params.train_length) &
                        (ic_data.test_length == params.test_length) &
                        (ic_data.learning_rate == params.learning_rate) &
                        (ic_data.num_leaves == params.num_leaves) &
                        (ic_data.feature_fraction == params.feature_fraction) &
                        (ic_data.boost_rounds == params.boost_rounds), ['date', ↴'ic']].set_index('date')
```

```
[50]: fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(20, 5))
axes = axes.flatten()
for i, t in enumerate([1, 21]):
    params = get_lgb_params(lgb_daily_ic, t=t)
    data = select_ic(params, lgb_ic, lookahead=t).sort_index()
    rolling = data.rolling(63).ic.mean().dropna()
    avg = data.ic.mean()
    med = data.ic.median()
    rolling.plot(ax=axes[i], title=f'Horizon: {t} Day(s) | IC: Mean={avg*100:.2f} Median={med*100:.2f}')
    axes[i].axhline(avg, c='darkred', lw=1)
    axes[i].axhline(0, ls='--', c='k', lw=1)

fig.suptitle('3-Month Rolling Information Coefficient', fontsize=16)
fig.tight_layout()
fig.subplots_adjust(top=0.92);
```



Get Predictions for Validation Period We retrieve the predictions for the 10 validation runs:

```
[51]: lookahead = 1
topn = 10
for best in range(topn):
    best_params = get_lgb_params(lgb_daily_ic, t=lookahead, best=best)
    key = get_lgb_key(lookahead, best_params)
    rounds = str(int(best_params.boost_rounds))
    if best == 0:
        best_predictions = pd.read_hdf(results_path / 'tuning_lgb.h5', ↵
                                         'predictions/' + key)
        best_predictions = best_predictions[rounds].to_frame(best)
    else:
        best_predictions[best] = pd.read_hdf(results_path / 'tuning_lgb.h5',
                                              'predictions/' + key)[rounds]
best_predictions = best_predictions.sort_index()
```

```
[52]: best_predictions.to_hdf('data/predictions.h5', f'lgb/train/[lookahead:02]')
best_predictions.info()
```

```
<class 'pandas.core.frame.DataFrame'>
MultiIndex: 501310 entries, ('A', Timestamp('2015-01-02 00:00:00')) to ('ZION',
Timestamp('2016-12-30 00:00:00'))
Data columns (total 10 columns):
 #   Column  Non-Null Count  Dtype  
---  -- 
 0   0       501310 non-null   float64
 1   1       501310 non-null   float64
 2   2       501310 non-null   float64
 3   3       501310 non-null   float64
 4   4       501310 non-null   float64
 5   5       501310 non-null   float64
 6   6       501310 non-null   float64
 7   7       501310 non-null   float64
 8   8       501310 non-null   float64
 9   9       501310 non-null   float64
dtypes: float64(10)
memory usage: 40.2+ MB
```

Get Trade Prices Using next available prices.

```
[53]: def get_trade_prices(tickers):
    idx = pd.IndexSlice
    DATA_STORE = '../data/assets.h5'
```

```

prices = (pd.read_hdf(DATA_STORE, 'quandl/wiki/prices').swaplevel().
    ↪sort_index())
prices.index.names = ['symbol', 'date']
return (prices.loc[idx[tickers], '2015': '2017'], 'adj_open']
    .unstack('symbol')
    .sort_index()
    .shift(-1)
    .tz_localize('UTC'))

```

[54]: test_tickers = best_predictions.index.get_level_values('symbol').unique()

[55]: trade_prices = get_trade_prices(test_tickers)
trade_prices.info()

```

<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 755 entries, 2015-01-02 00:00:00+00:00 to 2017-12-29
00:00:00+00:00
Columns: 995 entries, A to ZION
dtypes: float64(995)
memory usage: 5.7 MB

```

[56]: # persist result in case we want to rerun:
trade_prices.to_hdf('data/model_tuning.h5', 'trade_prices/model_selection')
trade_prices = pd.read_hdf('data/model_tuning.h5', 'trade_prices/
 ↪model_selection')

We average the top five models and provide the corresponding prices to Alphalens, in order to compute the mean period-wise return earned on an equal-weighted portfolio invested in the daily factor quintiles for various holding periods:

[57]: factor = best_predictions.iloc[:, :5].mean(1).dropna().tz_localize('UTC', ↪level='date').swaplevel()

Create AlphaLens Inputs

[58]: factor_data = get_clean_factor_and_forward_returns(factor=factor,
 prices=trade_prices,
 quantiles=5,
 periods=(1, 5, 10, 21))

Dropped 0.0% entries from factor data: 0.0% in forward returns computation and 0.0% in binning phase (set max_loss=0 to see potentially suppressed Exceptions). max_loss is 35.0%, not exceeded: OK!

Compute Alphalens metrics

[59]: mean_quant_ret_bydate, std_quant_daily = perf.mean_return_by_quantile(
 factor_data,

```

        by_date=True,
        by_group=False,
        demeaned=True,
        group_adjust=False,
    )

```

[60]: factor_returns = perf.factor_returns(factor_data)

[61]: mean_quant_ret, std_quantile = perf.mean_return_by_quantile(factor_data,
 by_group=False,
 demeaned=True)

```

mean_quant_rateret = mean_quant_ret.apply(rate_of_return, axis=0,
                                           base_period=mean_quant_ret.columns[0])

```

[62]: mean_quant_ret_bydate, std_quant_daily = perf.mean_return_by_quantile(
 factor_data,
 by_date=True,
 by_group=False,
 demeaned=True,
 group_adjust=False,
)

mean_quant_rateret_bydate = mean_quant_ret_bydate.apply(
 rate_of_return,
 base_period=mean_quant_ret_bydate.columns[0],
)
compstd_quant_daily = std_quant_daily.apply(std_conversion,
 base_period=std_quant_daily.
 columns[0])

alpha_beta = perf.factor_alpha_beta(factor_data,
 demeaned=True)

mean_ret_spread_quant, std_spread_quant = perf.compute_mean_returns_spread(
 mean_quant_rateret_bydate,
 factor_data["factor_quantile"].max(),
 factor_data["factor_quantile"].min(),
 std_err=compstd_quant_daily,
)

[63]: mean_ret_spread_quant.mean().mul(10000).to_frame('Mean Period Wise Spread
↪(bps)').join(alpha_beta.T).T

[63] :

	1D	5D	10D	21D
Mean Period Wise Spread (bps)	12.165432	6.951403	4.946450	4.407920
Ann. alpha	0.175933	0.077596	0.044649	0.037394
beta	0.089060	0.151587	0.191898	0.198344

[64] : fig, axes = plt.subplots(ncols=3, figsize=(18, 4))

```

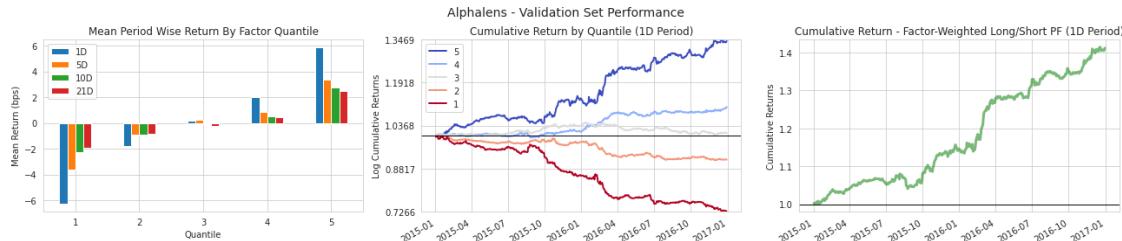
plotting.plot_quantile_returns_bar(mean_quant_rateret, ax=axes[0])
plt.setp(axes[0].xaxis.get_majorticklabels(), rotation=0)
axes[0].set_xlabel('Quantile')

plotting.plot_cumulative_returns_by_quantile(mean_quant_ret_bydate['1D'],
                                             freq=pd.tseries.offsets.BDay(),
                                             period='1D',
                                             ax=axes[1])
axes[1].set_title('Cumulative Return by Quantile (1D Period)')

title = "Cumulative Return - Factor-Weighted Long/Short PF (1D Period)"
plotting.plot_cumulative_returns(factor_returns['1D'],
                                 period='1D',
                                 freq=pd.tseries.offsets.BDay(),
                                 title=title,
                                 ax=axes[2])

fig.suptitle('Alphalens - Validation Set Performance', fontsize=14)
fig.tight_layout()
fig.subplots_adjust(top=.85);

```



Summary Tearsheet

[65] : create_summary_tear_sheet(factor_data)

Quantiles Statistics

	min	max	mean	std	count	count %
factor_quantile	-0.043323	0.007629	-0.002025	0.003269	100296	20.006822

2	-0.013078	0.010640	-0.000747	0.002936	100247	19.997048
3	-0.008825	0.012310	-0.000009	0.002950	100223	19.992260
4	-0.008289	0.017452	0.000698	0.003072	100247	19.997048
5	-0.007450	0.052497	0.002109	0.003811	100296	20.006822

Returns Analysis

	1D	5D	10D	21D
Ann. alpha	0.176	0.078	0.045	0.037
beta	0.089	0.152	0.192	0.198
Mean Period Wise Return Top Quantile (bps)	5.884	3.375	2.742	2.496
Mean Period Wise Return Bottom Quantile (bps)	-6.282	-3.603	-2.240	-1.946
Mean Period Wise Spread (bps)	12.165	6.951	4.946	4.408

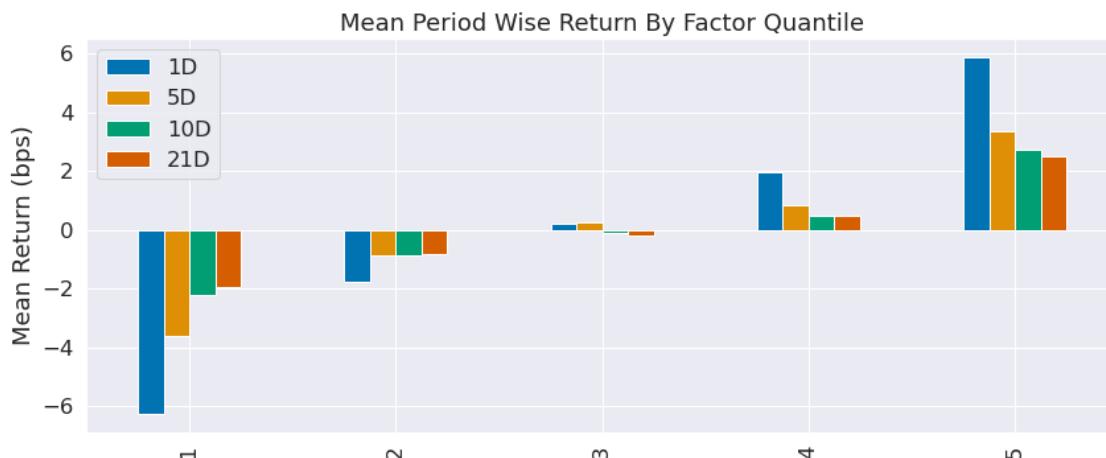
Information Analysis

	1D	5D	10D	21D
IC Mean	0.020	0.021	0.022	0.034
IC Std.	0.126	0.136	0.141	0.140
Risk-Adjusted IC	0.162	0.158	0.156	0.246
t-stat(IC)	3.638	3.545	3.501	5.515
p-value(IC)	0.000	0.000	0.001	0.000
IC Skew	0.065	0.249	0.246	0.087
IC Kurtosis	0.970	1.544	0.567	0.740

Turnover Analysis

	1D	5D	10D	21D
Quantile 1 Mean Turnover	0.634	0.654	0.721	0.770
Quantile 2 Mean Turnover	0.751	0.756	0.779	0.790
Quantile 3 Mean Turnover	0.763	0.769	0.783	0.791
Quantile 4 Mean Turnover	0.752	0.756	0.777	0.795
Quantile 5 Mean Turnover	0.622	0.640	0.695	0.738
	1D	5D	10D	21D
Mean Factor Rank Autocorrelation	0.309	0.283	0.164	0.071

<Figure size 432x288 with 0 Axes>



```
[66]: create_full_tear_sheet(factor_data)
```

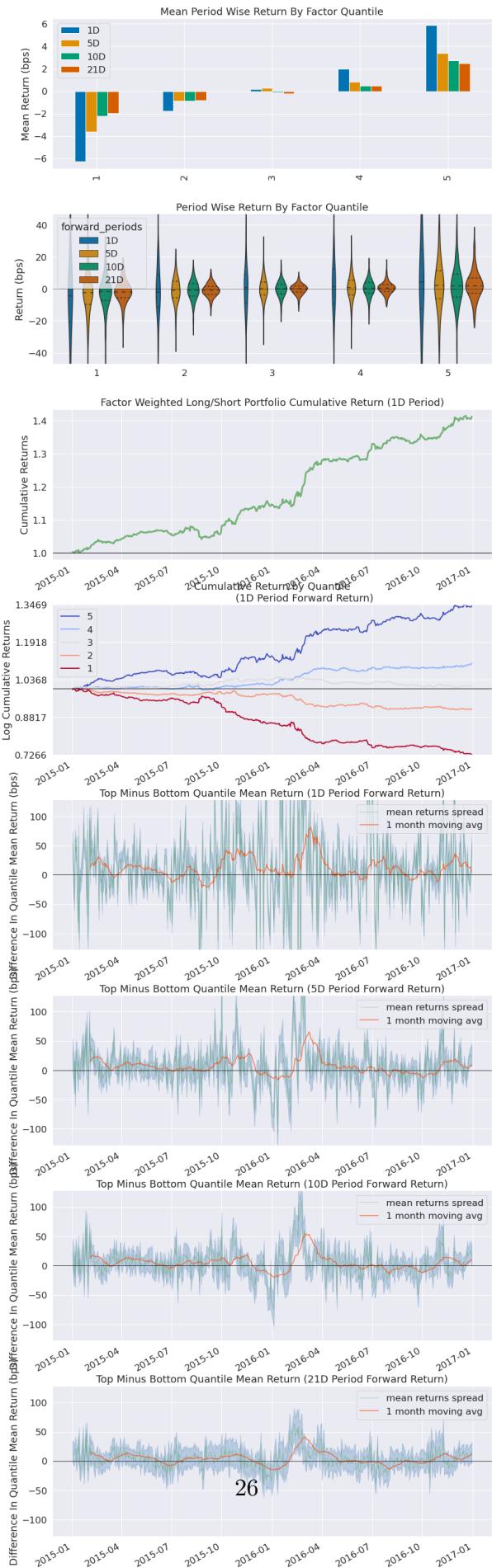
Quantiles Statistics

	min	max	mean	std	count	count %
factor_quantile						
1	-0.043323	0.007629	-0.002025	0.003269	100296	20.006822
2	-0.013078	0.010640	-0.000747	0.002936	100247	19.997048
3	-0.008825	0.012310	-0.000009	0.002950	100223	19.992260
4	-0.008289	0.017452	0.000698	0.003072	100247	19.997048
5	-0.007450	0.052497	0.002109	0.003811	100296	20.006822

Returns Analysis

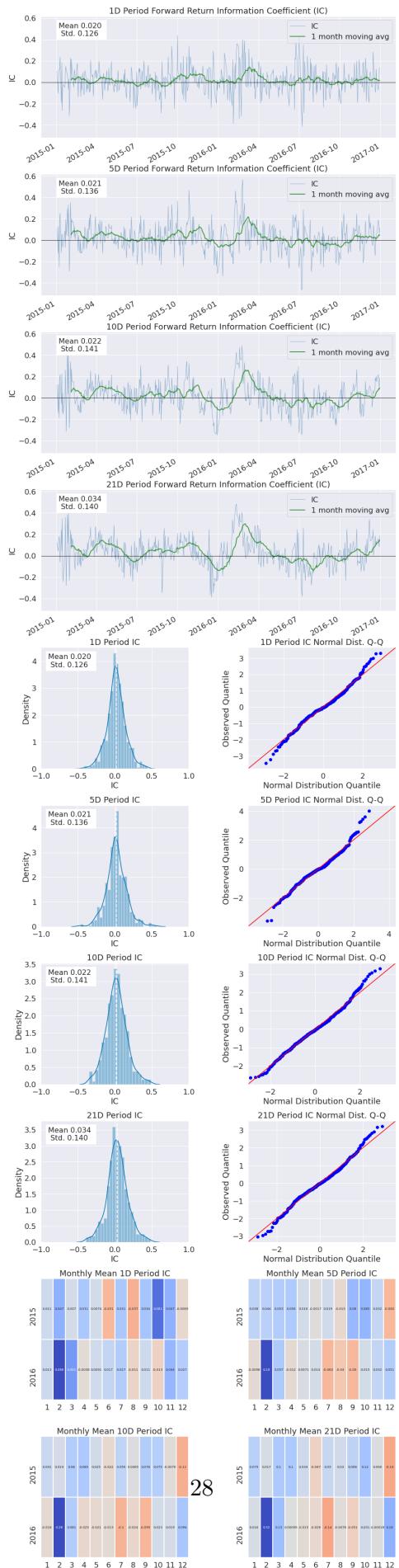
	1D	5D	10D	21D
Ann. alpha	0.176	0.078	0.045	0.037
beta	0.089	0.152	0.192	0.198
Mean Period Wise Return Top Quantile (bps)	5.884	3.375	2.742	2.496
Mean Period Wise Return Bottom Quantile (bps)	-6.282	-3.603	-2.240	-1.946
Mean Period Wise Spread (bps)	12.165	6.951	4.946	4.408

<Figure size 432x288 with 0 Axes>



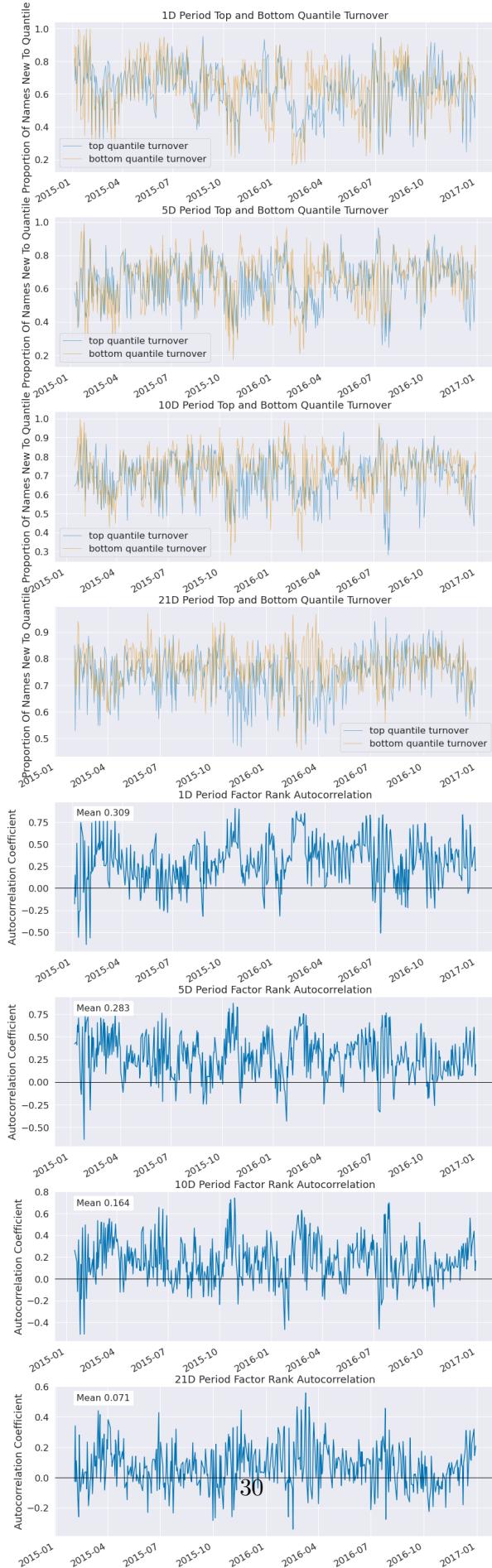
Information Analysis

	1D	5D	10D	21D
IC Mean	0.020	0.021	0.022	0.034
IC Std.	0.126	0.136	0.141	0.140
Risk-Adjusted IC	0.162	0.158	0.156	0.246
t-stat(IC)	3.638	3.545	3.501	5.515
p-value(IC)	0.000	0.000	0.001	0.000
IC Skew	0.065	0.249	0.246	0.087
IC Kurtosis	0.970	1.544	0.567	0.740



Turnover Analysis

	1D	5D	10D	21D
Quantile 1 Mean Turnover	0.634	0.654	0.721	0.770
Quantile 2 Mean Turnover	0.751	0.756	0.779	0.790
Quantile 3 Mean Turnover	0.763	0.769	0.783	0.791
Quantile 4 Mean Turnover	0.752	0.756	0.777	0.795
Quantile 5 Mean Turnover	0.622	0.640	0.695	0.738
Mean Factor Rank Autocorrelation	0.309	0.283	0.164	0.071



1.6.2 CatBoost

Select Parameters

```
[67]: catboost_daily_ic = pd.read_hdf('data/model_tuning.h5', 'catboost/daily_ic')
catboost_daily_ic.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 1176 entries, 0 to 1175
Data columns (total 7 columns):
 #   Column           Non-Null Count  Dtype  
---  --  
 0   lookahead        1176 non-null    int64  
 1   train_length     1176 non-null    int64  
 2   test_length      1176 non-null    int64  
 3   max_depth        1176 non-null    int64  
 4   min_child_samples 1176 non-null    int64  
 5   boost_rounds     1176 non-null    int64  
 6   ic               1176 non-null    float64 
dtypes: float64(1), int64(6)
memory usage: 73.5 KB
```

```
[68]: def get_cb_params(data, t=5, best=0):
    param_cols = scope_params[1:] + catboost_train_params + ['boost_rounds']
    df = data[data.lookahead==t].sort_values('ic', ascending=False).iloc[best]
    return df.loc[param_cols]
```

```
[69]: def get_cb_key(t, p):
    key = f'{t}/{int(p.train_length)}/{int(p.test_length)}/'
    return key + f'{int(p.max_depth)}/{int(p.min_child_samples)}'
```

```
[70]: best_params = get_cb_params(catboost_daily_ic, t=1, best=0)
best_params
```

```
[70]: train_length      1134.0
test_length         63.0
max_depth          3.0
min_child_samples  250.0
boost_rounds       200.0
Name: 355, dtype: float64
```

```
[71]: def select_cb_ic(params, ic_data, lookahead):
    return ic_data.loc[(ic_data.lookahead == lookahead) &
                       (ic_data.train_length == params.train_length) &
                       (ic_data.test_length == params.test_length) &
                       (ic_data.max_depth == params.max_depth) &
```

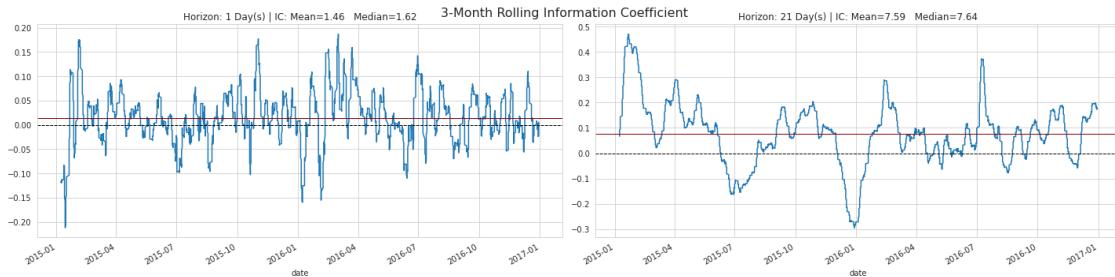
```

        (ic_data.min_child_samples == params.min_child_samples)].
→set_index('date')

[72]: fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(20, 5))
axes = axes.flatten()
for i, t in enumerate([1, 21]):
    params = get_cb_params(catboost_daily_ic, t=t)
    data = select_cb_ic(params, catboost_ic, lookahead=t).sort_index()
    rolling = data.rolling(63).ic.mean().dropna()
    avg = data.ic.mean()
    med = data.ic.median()
    rolling.plot(ax=axes[i], title=f'Horizon: {t} Day(s) | IC: Mean={avg*100:.2f} Median={med*100:.2f}')
    axes[i].axhline(avg, c='darkred', lw=1)
    axes[i].axhline(0, ls='--', c='k', lw=1)

fig.suptitle('3-Month Rolling Information Coefficient', fontsize=16)
fig.tight_layout()
fig.subplots_adjust(top=0.92);

```



Get Predictions

```

[73]: lookahead = 1
topn = 10
for best in range(topn):
    best_params = get_cb_params(catboost_daily_ic, t=lookahead, best=best)
    key = get_cb_key(lookahead, best_params)
    rounds = str(int(best_params.boost_rounds))
    if best == 0:
        best_predictions = pd.read_hdf(results_path / 'tuning_catboost.h5', ↴
→'predictions/' + key)
        best_predictions = best_predictions[rounds].to_frame(best)
    else:
        best_predictions[best] = pd.read_hdf(results_path / 'tuning_catboost. ↴
→h5',
                                         'predictions/' + key)[rounds]

```

```

best_predictions = best_predictions.sort_index()

[74]: best_predictions.to_hdf('data/predictions.h5', f'catboost/train/{lookahead:02}')
best_predictions.info()

<class 'pandas.core.frame.DataFrame'>
MultiIndex: 501310 entries, ('A', Timestamp('2015-01-02 00:00:00')) to ('ZION',
Timestamp('2016-12-30 00:00:00'))
Data columns (total 10 columns):
 #   Column  Non-Null Count  Dtype  
---  --     -----  --    
 0   0       501310 non-null  float64 
 1   1       501310 non-null  float64 
 2   2       501310 non-null  float64 
 3   3       501310 non-null  float64 
 4   4       501310 non-null  float64 
 5   5       501310 non-null  float64 
 6   6       501310 non-null  float64 
 7   7       501310 non-null  float64 
 8   8       501310 non-null  float64 
 9   9       501310 non-null  float64 
dtypes: float64(10)
memory usage: 40.2+ MB

```

Get Trade Prices Using next available prices.

```

[75]: def get_trade_prices(tickers):
    idx = pd.IndexSlice
    DATA_STORE = '../data/assets.h5'
    prices = (pd.read_hdf(DATA_STORE, 'quandl/wiki/prices').swaplevel().
    ↪sort_index())
    prices.index.names = ['symbol', 'date']
    return (prices.loc[idx[tickers], '2015': '2017'], 'adj_open'.
        .unstack('symbol').
        .sort_index().
        .shift(-1).
        .tz_localize('UTC'))

```

```
[76]: test_tickers = best_predictions.index.get_level_values('symbol').unique()
```

```
[77]: trade_prices = get_trade_prices(test_tickers)
trade_prices.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 755 entries, 2015-01-02 00:00:00+00:00 to 2017-12-29
00:00:00+00:00
Columns: 995 entries, A to ZION
```

```
dtypes: float64(995)
memory usage: 5.7 MB
```

```
[78]: # only generate once to save time
trade_prices.to_hdf('data/model_tuning.h5', 'trade_prices/model_selection')
```

```
[79]: trade_prices = pd.read_hdf('data/model_tuning.h5', 'trade_prices/
˓→model_selection')
```

```
[80]: factor = best_predictions.iloc[:, :5].mean(1).dropna().tz_localize('UTC', ˓→
˓→level='date').swaplevel()
```

Create AlphaLens Inputs

```
[81]: factor_data = get_clean_factor_and_forward_returns(factor=factor,
                                                       prices=trade_prices,
                                                       quantiles=5,
                                                       periods=(1, 5, 10, 21))
```

Dropped 0.0% entries from factor data: 0.0% in forward returns computation and 0.0% in binning phase (set max_loss=0 to see potentially suppressed Exceptions). max_loss is 35.0%, not exceeded: OK!

Summary Tearsheet

```
[82]: create_summary_tear_sheet(factor_data)
```

Quantiles Statistics

factor_quantile	min	max	mean	std	count	count %
1	-0.048616	0.008704	-0.001321	0.004333	100296	20.006822
2	-0.017568	0.011154	0.000004	0.003696	100247	19.997048
3	-0.012403	0.015290	0.000651	0.003633	100223	19.992260
4	-0.011378	0.022721	0.001284	0.003775	100247	19.997048
5	-0.010400	0.047750	0.002889	0.004981	100296	20.006822

Returns Analysis

	1D	5D	10D	21D
Ann. alpha	0.176	0.077	0.057	0.049
beta	0.086	0.150	0.147	0.189
Mean Period Wise Return Top Quantile (bps)	6.103	4.049	3.508	3.207
Mean Period Wise Return Bottom Quantile (bps)	-6.037	-2.994	-2.581	-2.698
Mean Period Wise Spread (bps)	12.140	7.020	6.066	5.885

Information Analysis

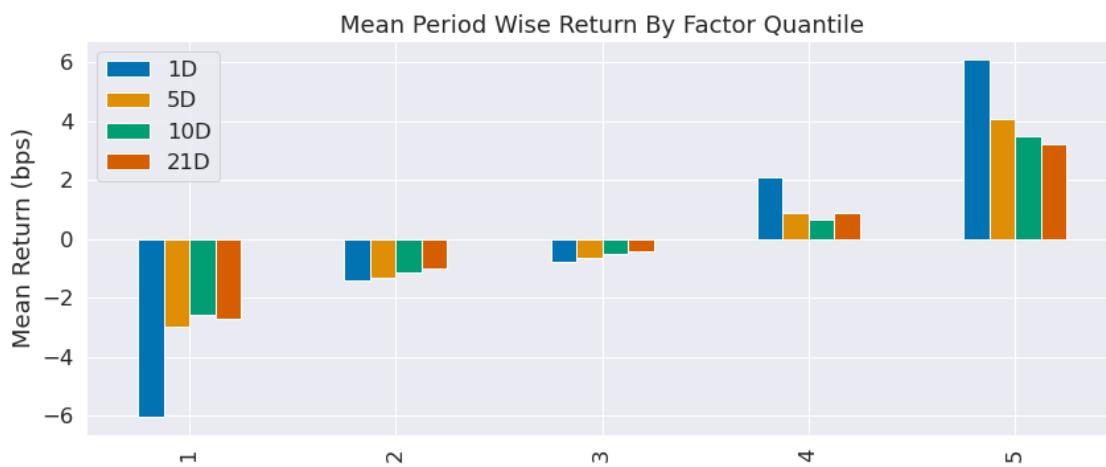
	1D	5D	10D	21D
IC Mean	0.019	0.026	0.033	0.054
IC Std.	0.124	0.136	0.139	0.134

Risk-Adjusted IC	0.152	0.193	0.236	0.401
t-stat(IC)	3.423	4.324	5.299	9.010
p-value(IC)	0.001	0.000	0.000	0.000
IC Skew	-0.073	0.041	0.205	0.231
IC Kurtosis	0.297	0.495	0.058	0.074

Turnover Analysis

	1D	5D	10D	21D
Quantile 1 Mean Turnover	0.524	0.630	0.689	0.756
Quantile 2 Mean Turnover	0.692	0.748	0.764	0.784
Quantile 3 Mean Turnover	0.719	0.765	0.776	0.785
Quantile 4 Mean Turnover	0.689	0.745	0.765	0.787
Quantile 5 Mean Turnover	0.525	0.616	0.667	0.739
	1D	5D	10D	21D
Mean Factor Rank Autocorrelation	0.482	0.328	0.222	0.085

<Figure size 432x288 with 0 Axes>



```
[83]: create_full_tear_sheet(factor_data)
```

Quantiles Statistics

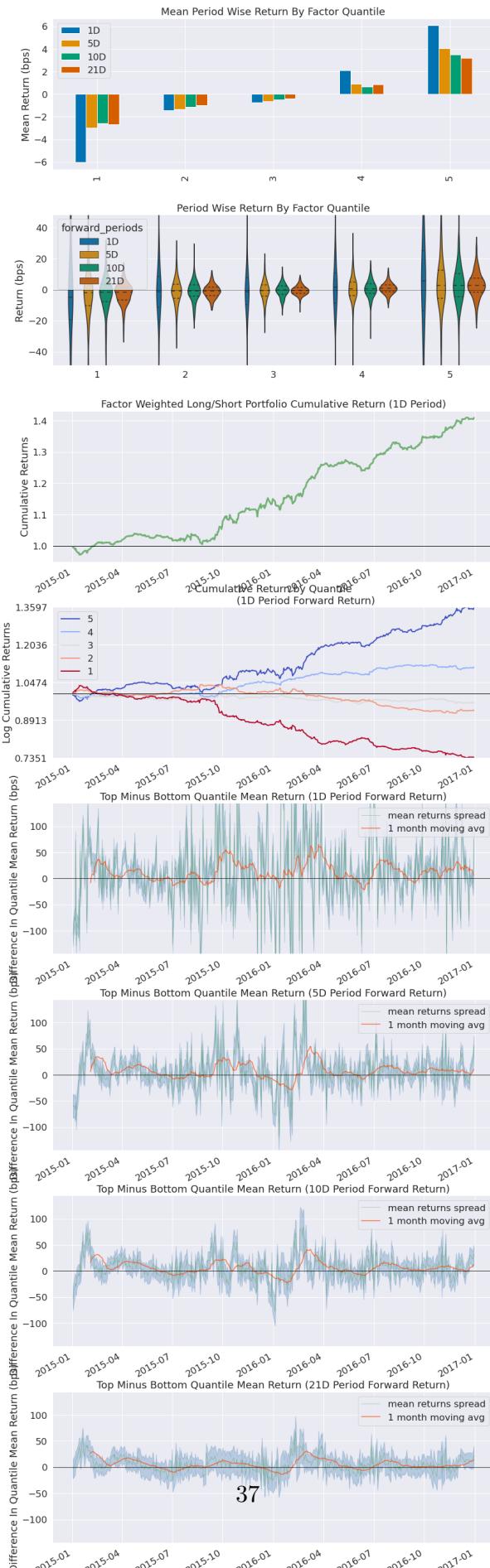
factor_quantile	min	max	mean	std	count	count %
1	-0.048616	0.008704	-0.001321	0.004333	100296	20.006822
2	-0.017568	0.011154	0.000004	0.003696	100247	19.997048
3	-0.012403	0.015290	0.000651	0.003633	100223	19.992260
4	-0.011378	0.022721	0.001284	0.003775	100247	19.997048
5	-0.010400	0.047750	0.002889	0.004981	100296	20.006822

Returns Analysis

1D 5D 10D 21D

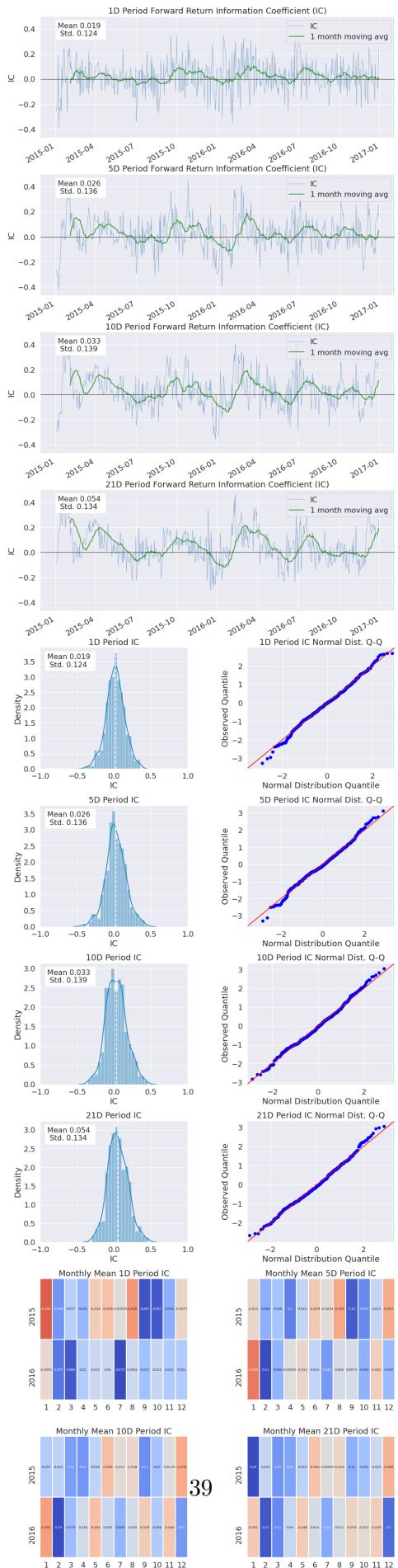
Ann. alpha	0.176	0.077	0.057	0.049
beta	0.086	0.150	0.147	0.189
Mean Period Wise Return Top Quantile (bps)	6.103	4.049	3.508	3.207
Mean Period Wise Return Bottom Quantile (bps)	-6.037	-2.994	-2.581	-2.698
Mean Period Wise Spread (bps)	12.140	7.020	6.066	5.885

<Figure size 432x288 with 0 Axes>



Information Analysis

	1D	5D	10D	21D
IC Mean	0.019	0.026	0.033	0.054
IC Std.	0.124	0.136	0.139	0.134
Risk-Adjusted IC	0.152	0.193	0.236	0.401
t-stat(IC)	3.423	4.324	5.299	9.010
p-value(IC)	0.001	0.000	0.000	0.000
IC Skew	-0.073	0.041	0.205	0.231
IC Kurtosis	0.297	0.495	0.058	0.074



Turnover Analysis

	1D	5D	10D	21D
Quantile 1 Mean Turnover	0.524	0.630	0.689	0.756
Quantile 2 Mean Turnover	0.692	0.748	0.764	0.784
Quantile 3 Mean Turnover	0.719	0.765	0.776	0.785
Quantile 4 Mean Turnover	0.689	0.745	0.765	0.787
Quantile 5 Mean Turnover	0.525	0.616	0.667	0.739
Mean Factor Rank Autocorrelation	0.482	0.328	0.222	0.085

