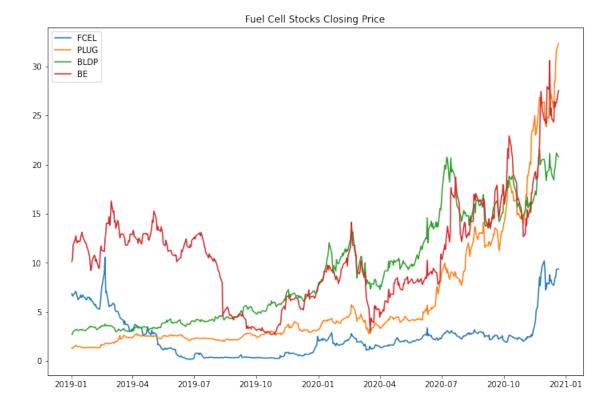
Fuel Cell Portfolio

September 29, 2021

1 Fuel Cell Portfolio Risk and Returns

```
[2]: import numpy as np
    import pandas as pd
    import matplotlib.pyplot as plt
    import seaborn as sns
    import math
    import warnings
    warnings.filterwarnings("ignore")
    # yahoo finance is used to fetch data
    import yfinance as yf
    yf.pdr_override()
[3]: # input
    # 4 Fuel Cell
    symbols = ['FCEL', 'PLUG', 'BLDP', 'BE']
    start = '2019-01-01'
    end = '2020-12-22'
[4]: df = pd.DataFrame()
    for s in symbols:
        df[s] = yf.download(s,start,end)['Adj Close']
    [******** 100%*********** 1 of 1 completed
    [********* 100%********** 1 of 1 completed
    [********* 100%*********** 1 of 1 completed
    [******** 100%************ 1 of 1 completed
[5]: from datetime import datetime
    from dateutil import relativedelta
    d1 = datetime.strptime(start, "%Y-%m-%d")
    d2 = datetime.strptime(end, "%Y-%m-%d")
    delta = relativedelta.relativedelta(d2,d1)
    print('How many years of investing?')
    print('%s years' % delta.years)
```

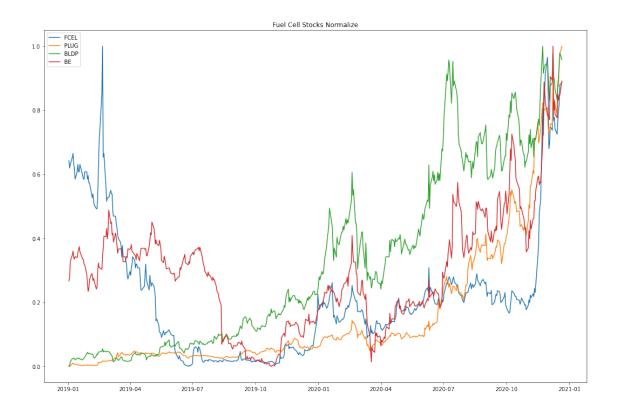
```
How many years of investing?
     1 years
 [6]: number_of_years = delta.years
 [7]: months = (d2.year - d1.year) * 12 + (d2.month - d1.month)
     months
 [7]: 23
 [8]: days = (df.index[-1] - df.index[0]).days
     days
 [8]: 719
 [9]: df.head()
 [9]:
                 FCEL PLUG BLDP
                                      ΒE
     Date
     2019-01-02 6.84
                       1.33 2.71
                                  10.12
     2019-01-03 6.60 1.26 2.77
                                   10.47
     2019-01-04 6.72 1.34 2.98
                                  11.83
     2019-01-07 6.96 1.53 3.17
                                   12.41
     2019-01-08 7.08 1.60 3.18
                                  12.73
[10]: df.tail()
[10]:
                 FCEL
                            PLUG
                                       BLDP
                                                   ΒE
     Date
     2020-12-15 8.14
                       28.469999 19.389999 26.420000
     2020-12-16 8.45
                       28.459999 19.639999 25.879999
     2020-12-17 8.66 30.570000 20.480000 26.330000
     2020-12-18 9.30
                       31.629999 21.180000 26.309999
     2020-12-21 9.38 32.369999 20.790001 27.549999
[11]: plt.figure(figsize=(12,8))
     plt.plot(df)
     plt.title('Fuel Cell Stocks Closing Price')
     plt.legend(labels=df.columns)
[11]: <matplotlib.legend.Legend at 0x172d3ed8a58>
```



```
[12]: # Normalize the data
normalize = (df - df.min())/ (df.max() - df.min())

[13]: plt.figure(figsize=(18,12))
   plt.plot(normalize)
   plt.title('Fuel Cell Stocks Normalize')
   plt.legend(labels=normalize.columns)
```

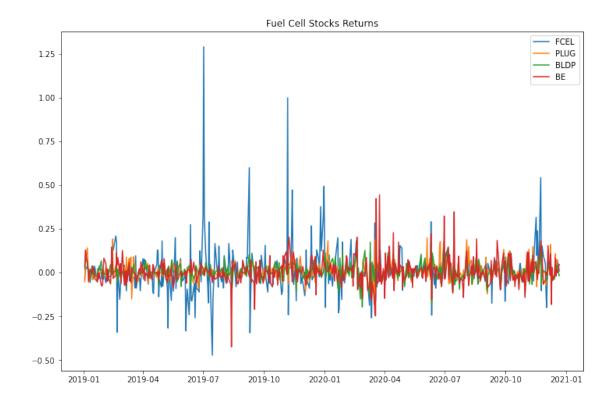
[13]: <matplotlib.legend.Legend at 0x172d4634cc0>



```
[14]: stock_rets = df.pct_change().dropna()

[15]: plt.figure(figsize=(12,8))
    plt.plot(stock_rets)
    plt.title('Fuel Cell Stocks Returns')
    plt.legend(labels=stock_rets.columns)
```

[15]: <matplotlib.legend.Legend at 0x172d3d80f60>



```
[16]: plt.figure(figsize=(12,8))
    plt.plot(stock_rets.cumsum())
    plt.title('Fuel Cell Stocks Returns Cumulative Sum')
    plt.legend(labels=stock_rets.columns)
```

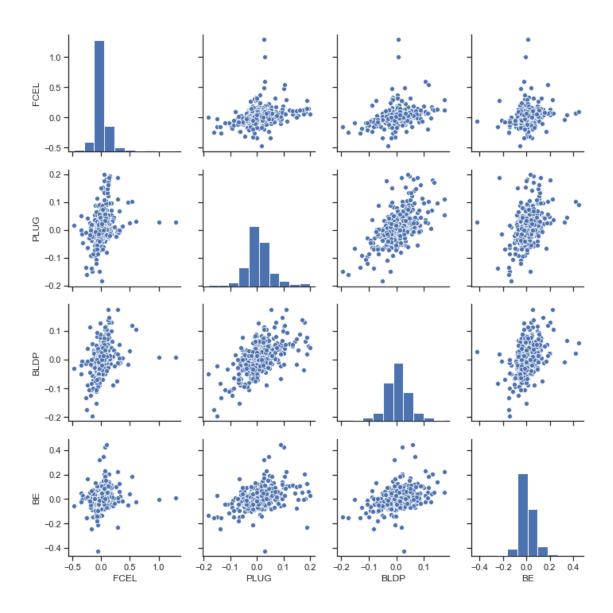
[16]: <matplotlib.legend.Legend at 0x172d471d780>



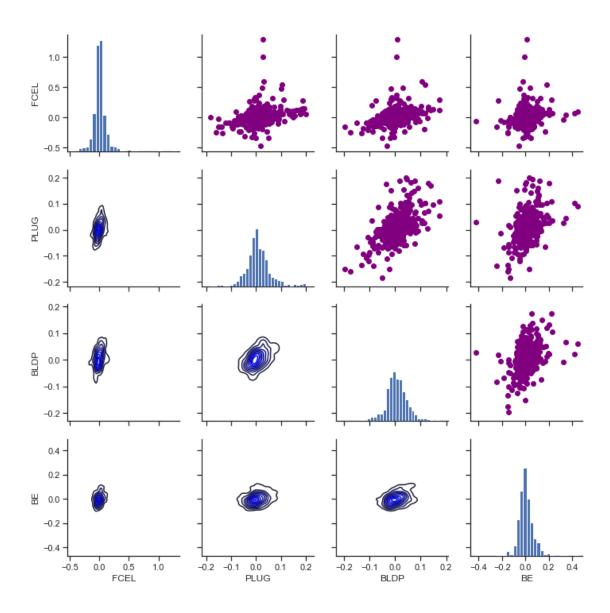


```
[17]: sns.set(style='ticks')
ax = sns.pairplot(stock_rets, diag_kind='hist')

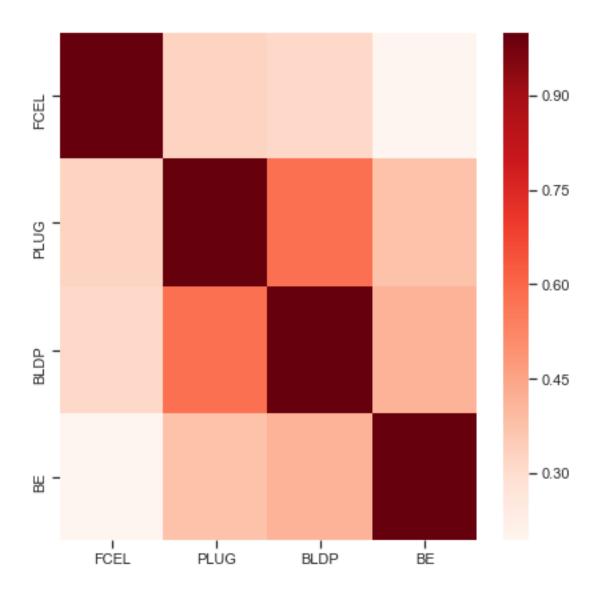
nplot = len(stock_rets.columns)
for i in range(nplot) :
    for j in range(nplot) :
        ax.axes[i, j].locator_params(axis='x', nbins=6, tight=True)
```



```
[18]: ax = sns.PairGrid(stock_rets)
ax.map_upper(plt.scatter, color='purple')
ax.map_lower(sns.kdeplot, color='blue')
ax.map_diag(plt.hist, bins=30)
for i in range(nplot) :
    for j in range(nplot) :
        ax.axes[i, j].locator_params(axis='x', nbins=6, tight=True)
```

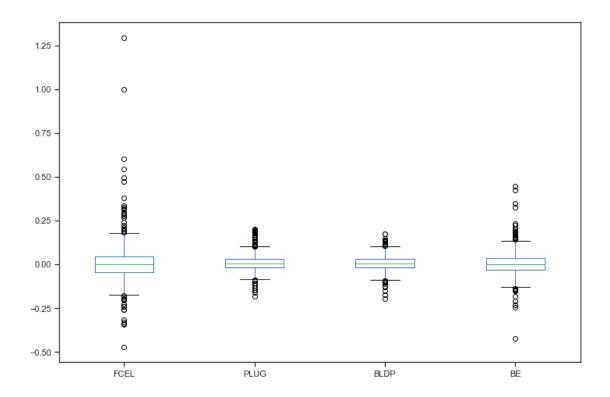


[19]: <AxesSubplot:>



```
[20]: # Box plot
stock_rets.plot(kind='box',figsize=(12,8))
```

[20]: <AxesSubplot:>

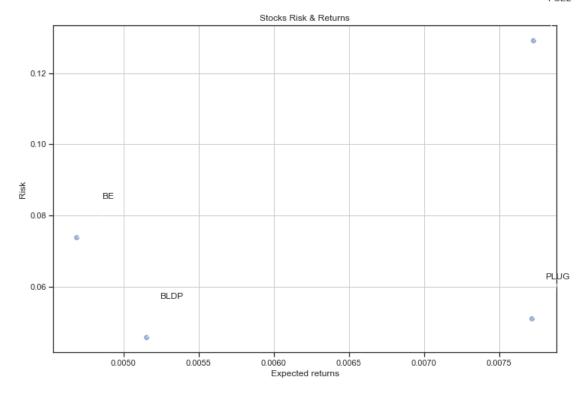


```
[21]: rets = stock_rets.dropna()

plt.figure(figsize=(12,8))
plt.scatter(rets.mean(), rets.std(),alpha = 0.5)

plt.title('Stocks Risk & Returns')
plt.xlabel('Expected returns')
plt.ylabel('Risk')
plt.grid(which='major')

for label, x, y in zip(rets.columns, rets.mean(), rets.std()):
    plt.annotate(
        label,
        xy = (x, y), xytext = (50, 50),
        textcoords = 'offset points', ha = 'right', va = 'bottom',
        arrowprops = dict(arrowstyle = '-', connectionstyle = 'arc3,rad=-0.3'))
```





```
[23]: rest_rets = rets.corr()
      pair_value = rest_rets.abs().unstack()
      pair_value.sort_values(ascending = False)
[23]: BE
                    1.000000
            BE
     BLDP
           BLDP
                    1.000000
     PLUG PLUG
                    1.000000
     FCEL FCEL
                    1.000000
     BLDP PLUG
                    0.583591
                    0.583591
     PLUG BLDP
     ΒE
           BLDP
                    0.414691
     BLDP BE
                    0.414691
     ΒE
           PLUG
                    0.377969
     PLUG BE
                    0.377969
           FCEL
                    0.328346
     FCEL PLUG
                    0.328346
     BLDP FCEL
                    0.315060
     FCEL BLDP
                    0.315060
     ΒE
            FCEL
                    0.193360
      FCEL BE
                    0.193360
      dtype: float64
[24]: # Normalized Returns Data
     Normalized_Value = ((rets[:] - rets[:].min()) /(rets[:].max() - rets[:].min()))
```

```
Normalized_Value.head()
[24]:
                     FCEL
                               PLUG
                                         BLDP
                                                     ΒE
     Date
      2019-01-03 0.247824
                           0.341986 0.589592 0.528423
      2019-01-04 0.278024
                           0.645599
                                     0.734531
                                               0.638008
      2019-01-07 0.287964
                           0.850317
                                     0.701980 0.545029
      2019-01-08 0.277491
                           0.599216 0.538322
                                               0.518305
      2019-01-09 0.238890 0.332526 0.546787 0.435368
[25]:
     Normalized_Value.corr()
[25]:
               FCEL
                         PLUG
                                   BLDP
                                               ΒE
     FCEL
           1.000000
                     0.328346 0.315060 0.193360
      PLUG
           0.328346
                     1.000000 0.583591
                                         0.377969
     BLDP
           0.315060 0.583591 1.000000
                                         0.414691
     BE
            0.193360 0.377969
                                         1.000000
                               0.414691
[26]: normalized_rets = Normalized_Value.corr()
      normalized_pair_value = normalized_rets.abs().unstack()
      normalized_pair_value.sort_values(ascending = False)
[26]: BE
           BE
                   1.000000
     BLDP
           BLDP
                   1.000000
     PLUG PLUG
                   1.000000
     FCEL FCEL
                   1.000000
     BLDP PLUG
                   0.583591
     PLUG BLDP
                   0.583591
           BLDP
     ΒE
                   0.414691
     BLDP BE
                   0.414691
     BF.
           PI.UG
                   0.377969
     PLUG BE
                   0.377969
           FCEL
                   0.328346
     FCEL PLUG
                   0.328346
     BLDP FCEL
                   0.315060
     FCEL BLDP
                   0.315060
           FCEL
      ΒE
                   0.193360
      FCEL BE
                   0.193360
      dtype: float64
[27]: print("Stock returns: ")
      print(rets.mean())
      print('-' * 50)
      print("Stock risks:")
      print(rets.std())
```

Stock returns:

```
FCEL
             0.007728
     PLUG
             0.007717
     BLDP
             0.005150
     ΒE
             0.004684
     dtype: float64
     Stock risks:
             0.129199
     FCEL
     PLUG
             0.051032
     BLDP
             0.045654
     ΒE
             0.073768
     dtype: float64
[28]: table = pd.DataFrame()
      table['Returns'] = rets.mean()
      table['Risk'] = rets.std()
      table.sort_values(by='Returns')
[28]:
            Returns
                         Risk
      BE
            0.004684 0.073768
     BLDP 0.005150 0.045654
     PLUG 0.007717 0.051032
     FCEL 0.007728 0.129199
[29]: table.sort_values(by='Risk')
[29]:
            Returns
                         Risk
      BLDP 0.005150 0.045654
     PLUG 0.007717 0.051032
     ΒE
           0.004684 0.073768
     FCEL 0.007728 0.129199
[30]: rf = 0.001
      table['Sharpe Ratio'] = (table['Returns'] - rf) / table['Risk']
[30]:
            Returns
                         Risk Sharpe Ratio
      FCEL 0.007728 0.129199
                                   0.052072
     PLUG 0.007717 0.051032
                                   0.131632
     BLDP 0.005150 0.045654
                                   0.090897
     ΒE
           0.004684 0.073768
                                   0.049945
[31]: table['Max Returns'] = rets.max()
[32]: table['Min Returns'] = rets.min()
[33]: table['Median Returns'] = rets.median()
```

```
[34]: total_return = stock_rets[-1:].transpose()
      table['Total Return'] = 100 * total_return
      table
[34]:
            Returns
                          Risk
                               Sharpe Ratio Max Returns Min Returns \
      FCEL 0.007728 0.129199
                                   0.052072
                                                             -0.472222
                                                 1.291667
     PLUG 0.007717 0.051032
                                    0.131632
                                                 0.199041
                                                             -0.183432
      BLDP
           0.005150 0.045654
                                   0.090897
                                                 0.174118
                                                             -0.196191
     BE
           0.004684 0.073768
                                    0.049945
                                                 0.444730
                                                             -0.425000
           Median Returns Total Return
                 0.000000
     FCEL
                                0.860214
     PLUG
                 0.001465
                                2.339550
     BLDP
                  0.002915
                              -1.841357
     BF.
                -0.002473
                                4.713036
[35]: table['Average Return Days'] = (1 + total_return)**(1 / days) - 1
      table
[35]:
            Returns
                          Risk Sharpe Ratio Max Returns Min Returns \
                                   0.052072
                                                             -0.472222
     FCEL 0.007728 0.129199
                                                 1.291667
     PLUG
           0.007717 0.051032
                                    0.131632
                                                 0.199041
                                                             -0.183432
     BLDP 0.005150 0.045654
                                                             -0.196191
                                    0.090897
                                                 0.174118
     BF.
            0.004684 0.073768
                                    0.049945
                                                 0.444730
                                                             -0.425000
           Median Returns Total Return Average Return Days
     FCEL
                 0.000000
                                0.860214
                                                     0.000012
      PLUG
                 0.001465
                                2.339550
                                                     0.000032
     BLDP
                 0.002915
                              -1.841357
                                                    -0.000026
      BE
                -0.002473
                                4.713036
                                                     0.000064
[36]: initial_value = df.iloc[0]
      ending_value = df.iloc[-1]
      table['CAGR'] = ((ending_value / initial_value) ** (252.0 / days)) -1
      table
[36]:
                               Sharpe Ratio Max Returns Min Returns \
            Returns
                          Risk
                                   0.052072
     FCEL
           0.007728 0.129199
                                                 1.291667
                                                             -0.472222
     PLUG 0.007717 0.051032
                                    0.131632
                                                 0.199041
                                                             -0.183432
      BLDP
           0.005150
                     0.045654
                                    0.090897
                                                 0.174118
                                                             -0.196191
      BE
            0.004684 0.073768
                                                 0.444730
                                                             -0.425000
                                    0.049945
           Median Returns Total Return Average Return Days
                                                                   CAGR
     FCEL
                 0.000000
                                0.860214
                                                     0.000012 0.117038
     PLUG
                 0.001465
                                2.339550
                                                     0.000032 2.061094
     BLDP
                                                    -0.000026 1.042399
                  0.002915
                              -1.841357
     BF.
                -0.002473
                                4.713036
                                                     0.000064 0.420500
```

[37]: table.sort_values(by='Average Return Days')

[37]:		Returns	Ri	isk	Sharpe Ra	tio	Max Returns	Min	Returns	\
	BLDP	0.005150	0.045654		0.090897		0.174118	-	0.196191	
	FCEL	0.007728	0.129199		0.052072		1.291667		-0.472222	
	PLUG	0.007717	0.0510)32	0.131	632	0.199041	-	0.183432	
	BE	0.004684	0.073768		0.049945		0.444730	-	0.425000	
		Median Returns		Tota	al Return	Aver	age Return	Days	CAGR	,
	BLDP	0.002915 0.000000 0.001465		-1.841357 0.860214			-0.000026		1.042399	
	FCEL					0.000012 0			0.117038	
	PLUG				2.339550		0.00	0032	2.061094	:
	BE	-0.002473			4.713036		0.00	0064	0.420500	