

07_pairs_trading_backtest

September 29, 2021

1 Pair Trading: Backtest with Backtrader

1.1 Imports & Settings

```
[1]: import warnings
warnings.filterwarnings('ignore')
```

```
[2]: import csv
from collections import defaultdict
from dataclasses import dataclass, asdict
from datetime import date
from pathlib import Path
from time import time

import numpy as np
import pandas as pd
import pandas_datareader.data as web

import matplotlib.pyplot as plt
import seaborn as sns

import backtrader as bt
from backtrader.feeds import PandasData

import pyfolio as pf
```

```
[3]: sns.set_style('dark')
pd.set_option('display.float_format', lambda x: f'{x:,.2f}')
idx = pd.IndexSlice
```

```
[4]: STORE = 'backtest.h5'
```

```
[5]: def format_time(t):
    m_, s = divmod(t, 60)
    h, m = divmod(m_, 60)
    return f'{h:>02.0f}:{m:>02.0f}:{s:>02.0f}'
```

1.2 Pairs Trading Backtest

1.2.1 Pairs DataClass

```
[6]: @dataclass
class Pair:
    period: int
    s1: str
    s2: str
    size1: float
    size2: float
    long: bool
    hr: float
    p1: float
    p2: float
    pos1: float
    pos2: float
    exec1: bool = False
    exec2: bool = False
    active: bool = False
    entry_date: date = None
    exit_date: date = None
    entry_spread: float = np.nan
    exit_spread: float = np.nan

    def executed(self):
        return self.exec1 and self.exec2

    def get_constituent(self, name):
        if name == self.s1:
            return 1
        elif name == self.s2:
            return 2
        else:
            return 0

    def compute_spread(self, p1, p2):
        return p1 * self.size1 + p2 * self.size2

    def compute_spread_return(self, p1, p2):
        current_spread = self.compute_spread(p1, p2)
        delta = self.entry_spread - current_spread
        return (delta / (np.sign(self.entry_spread) *
                        self.entry_spread))
```

1.2.2 PandasData definition

```
[7]: class CustomData(PandasData):
    """
    Define pandas DataFrame structure
    """
    cols = ['open', 'high', 'low', 'close', 'volume']

    # create lines
    lines = tuple(cols)

    # define parameters
    params = {c: -1 for c in cols}
    params.update({'datetime': None})
    params = tuple(params.items())
```

1.2.3 Define Trading Strategy

```
[8]: class StatisticalArbitrageCointegration(bt.Strategy):
    params = (('trades', None),
              ('risk_limit', -.2),
              ('verbose', True),
              ('log_file', 'backtest.csv'))

    def __init__(self):
        self.active_pairs = {}
        self.closing_pairs = {}
        self.exposure = []
        self.metrics = []
        self.last_close = {}
        self.cnt = 0
        self.today = None
        self.clear_log()
        self.order_status = dict(enumerate(['Created', 'Submitted', 'Accepted',
                                             'Partial', 'Completed', 'Canceled',
                                             'Expired', 'Margin', 'Rejected']))

    def clear_log(self):
        if Path(self.p.log_file).exists():
            Path(self.p.log_file).unlink()
        with Path(self.p.log_file).open('a') as f:
            log_writer = csv.writer(f)
            log_writer.writerow(
                ['Date', 'Pair', 'Symbol', 'Order #', 'Reason',
                 'Status', 'Long', 'Price', 'Size', 'Position'])

    def log(self, txt, dt=None):
```

```

        """ Logger for the strategy """
        dt = dt or self.datas[0].datetime.datetime(0)
        with Path(self.p.log_file).open('a') as f:
            log_writer = csv.writer(f)
            log_writer.writerow([dt.date()] + txt.split(','))

    def get_pair_id(self, s1, s2, period):
        return f'{s1}.{s2}.{period}'

    def check_risk_limit(self):
        for pair_id, pair in list(self.active_pairs.items()):
            if pair.active:
                p1 = self.last_close.get(pair.s1)
                p2 = self.last_close.get(pair.s2)
                ret = pair.compute_spread_return(p1, p2)
                if ret < self.p.risk_limit:
                    self.log(f'{pair_id},{pair.s1},{pair.s2},Risk Limit,{ret},')
                    del self.active_pairs[pair_id]
                    self.sell_pair(pair_id, pair)

    def sell_pair(self, pair_id, pair, reason='close'):
        info = {'pair': pair_id, 'type': reason}
        if pair.long:
            o1 = self.sell(data=pair.s1, size=abs(pair.size1), info=info)
            o2 = self.buy(data=pair.s2, size=abs(pair.size2), info=info)
        else:
            o1 = self.buy(data=pair.s1, size=abs(pair.size1), info=info)
            o2 = self.sell(data=pair.s2, size=abs(pair.size2), info=info)
        pair.active = False
        pair.exec1 = pair.exec2 = False
        self.closing_pairs[pair_id] = pair

        self.log(f'{pair_id},{pair.s1},{o1.ref},{reason},Created,{pair.
→long},,{pair.size1},')
        self.log(f'{pair_id},{pair.s2},{o2.ref},{reason},Created,{pair.
→long},,{pair.size2},')

    def notify_order(self, order):
        symbol = order.data._name
        if order.status in [order.Submitted, order.Accepted]:
            return
        if order.status in [order.Completed]:
            p = order.executed.price
            s = order.executed.size
            order_type = order.info.info['type']
            if order_type in ['open', 'close']:
                pair_id = order.info.info['pair']

```

```

        if order_type == 'open':
            pair = self.active_pairs.get(pair_id)
        else:
            pair = self.closing_pairs.get(pair_id)
        if pair is None:
            self.log(f'{pair_id},{symbol},{order.
→ref},{order_type},Completed (missing),,{p},{s},{p * s}')
            return
        component = pair.get_constituent(symbol)
        if component == 1:
            pair.p1 = p
            pair.exec1 = True
        elif component == 2:
            pair.p2 = p
            pair.exec2 = True
        if pair.executed():
            pair.exec1 = False
            pair.exec2 = False
            if order_type == 'open':
                pair.entry_spread = pair.compute_spread(p1=pair.p1,
→p2=pair.p2)

                pair.entry_date = self.today
                pair.active = True
            elif order_type == 'close':
                pair.exit_spread = pair.compute_spread(p1=pair.p1,
→p2=pair.p2)

                pair.exit_date = self.today
                pair.active = False
                self.closing_pairs.pop(pair_id)
            self.log(f'{pair_id},{symbol},{order.
→ref},{order_type},Completed,{pair.long},{p},{s},{p * s}')
        else:
            self.log(f',{symbol},{order.
→ref},{order_type},Completed,,{p},{s},{p * s}')

        elif order.status in [order.Canceled, order.Margin, order.Rejected]:
            order_type = order.info.info['type']
            self.log(f',{symbol},{order.ref},{order_type},{self.
→order_status[order.status]},,,')

    def enter_pairs(self, df, long=True):
        for s1, s2, hr, period in zip(df.s1, df.s2, df.hedge_ratio, df.period):
            pair_id = self.get_pair_id(s1, s2, period)
            if self.active_pairs.get(pair_id):
                continue

```

```

p1 = self.last_close[s1]
p2 = self.last_close[s2]
if long:
    size1 = self.target_value / p1
    size2 = hr * size1
else:
    size2 = self.target_value / p2
    size1 = 1 / hr * size2

pair = Pair(s1=s1, s2=s2, period=period, size1=size1, size2=size2,
            pos1=p1 * size1, pos2=p2 * size2,
            hr=hr, long=long, p1=p1, p2=p2, entry_date=self.today)
info = {'pair': pair_id, 'type': 'open'}
if long:
    o1 = self.buy(data=s1, size=size1, info=info)
    o2 = self.sell(data=s2, size=abs(size2), info=info)
else:
    o1 = self.sell(data=pair.s1, size=abs(pair.size1), info=info)
    o2 = self.buy(data=pair.s2, size=abs(pair.size2), info=info)

self.active_pairs[pair_id] = pair

self.log(f'{pair_id},{s1},{o1.
→ref},Open,Created,{long},{p1},{size1},{pair.pos1}')
self.log(f'{pair_id},{s2},{o2.
→ref},Open,Created,{long},{p2},{size2},{pair.pos2}')

def adjust_pairs(self):
    orders = defaultdict(float)
    pairs = defaultdict(list)
    for pair_id, pair in self.active_pairs.items():
        p1, p2 = self.last_close[pair.s1], self.last_close[pair.s2]
        pos1, pos2 = pair.size1 * p1, pair.size2 * p2

        if pair.long:
            target_size1 = self.target_value / p1
            orders[pair.s1] += target_size1 - pair.size1
            target_size2 = pos2 / pos1 * self.target_value / p2
            orders[pair.s2] += target_size2 - pair.size2
        else:
            target_size2 = self.target_value / p2
            orders[pair.s2] += target_size2 - pair.size2
            target_size1 = pos1 / pos2 * self.target_value / p1
            orders[pair.s1] += target_size1 - pair.size1
        pair.size1 = target_size1
        pair.size2 = target_size2
        pairs[pair.s1].append(pair_id)

```

```

        pairs[pair.s2].append(pair_id)

    for symbol, size in orders.items():
        info = {'pairs': pairs[symbol], 'type': 'adjust'}
        if size > 0:
            order = self.buy(symbol, size=size, info=info)
        elif size < 0:
            order = self.sell(symbol, size=abs(size), info=info)
        else:
            continue
        self.log(f',{symbol},{order.ref},Adjust,Created,{size}')

    def prenext(self):
        self.next()

    def next(self):
        self.today = pd.Timestamp(self.datas[0].datetime.date())
        if self.today not in self.p.trades.index:
            return
        self.cnt += 1

        pf = self.broker.get_value()
        cash = self.broker.get_cash()

        exp = {d._name: pos.size for d, pos in self.getpositions().items() if
↪pos}

        self.last_close = {d._name: d.close[0] for d in self.datas}
        exposure = pd.DataFrame({'price' : pd.Series(self.last_close),
                                'position': pd.Series(exp)}).replace(0, np.
↪nan).dropna()
        exposure['value'] = exposure.price * exposure.position
        positions = exposure.value.to_dict()
        positions['date'] = self.today
        positions['cash'] = cash
        if not exposure.empty:
            self.exposure.append(positions)
            long_pos = exposure[exposure.value > 0].value.sum()
            short_pos = exposure[exposure.value < 0].value.sum()
            for symbol, row in exposure.iterrows():
                self.log(f',{symbol},,Positions,Log,,{row.price},{row.
↪position},{row.value}')
        else:
            long_pos = short_pos = 0

        trades = self.p.trades.loc[self.today]
        if isinstance(trades, pd.Series):
            trades = trades.to_frame().T

```

```

close = trades[trades.side == 0].sort_values('period')
for s1, s2, period in zip(close.s1, close.s2, close.period):
    pair_id = self.get_pair_id(s1, s2, period)
    pair = self.active_pairs.pop(pair_id, None)
    if pair is None:
        self.log(f'{pair_id},,,Close Attempt,Failed,,,')
        continue
    self.sell_pair(pair_id, pair)

if len(self.active_pairs) > 0:
    self.check_risk_limit()

long = trades[trades.side == 1]
short = trades[trades.side == -1]
if long.empty and short.empty: return
target = 1 / (len(long) + len(short) + len(self.active_pairs))
self.target_value = pf * target
metrics = [self.today, pf, pf - cash, cash, len(exposure), len(self.
→active_pairs), long_pos, short_pos,
            target, self.target_value, len(long), len(short), len(close)]
self.metrics.append(metrics)
if self.cnt % 21 == 0:
    holdings = pf - cash
    msg = f'PF: {pf:11,.0f} | Net: {holdings: 11,.0f} | # Pos:␣
→{len(exposure):3,.0f} | # Pairs: {len(self.active_pairs):3,.0f} | '
    msg += f'Long: {long_pos: 10,.0f} | Short: {short_pos: 10,.0f}'
    print(self.today, msg)

self.adjust_pairs()

if not long.empty:
    self.enter_pairs(long, long=True)

if not short.empty:
    self.enter_pairs(short, long=False)

```

1.2.4 Load Trades

```
[9]: trades = pd.read_hdf(STORE, 'pair_trades').sort_index()
trades.info()
```

```

<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 134450 entries, 2017-01-03 to 2019-12-18
Data columns (total 6 columns):
#   Column          Non-Null Count  Dtype
---  -

```



```

0   s1          134450 non-null  object
1   s2          134450 non-null  object
2   hedge_ratio 134450 non-null  float64
3   period      134450 non-null  int64
4   pair        134450 non-null  int64
5   side        134450 non-null  int64
dtypes: float64(1), int64(3), object(2)
memory usage: 7.2+ MB

```

```
[10]: trade_dates = np.unique(trades.index)
      start = trade_dates.min()
      end = trade_dates.max()
      traded_symbols = trades.s1.append(trades.s2).unique()
```

1.2.5 Load Prices

```
[11]: prices = (pd.read_hdf(STORE, 'prices')
               .sort_index()
               .loc[idx[traded_symbols, str(start):str(end)], :])
```

```
[12]: prices.info(show_counts=True)
```

```

<class 'pandas.core.frame.DataFrame'>
MultiIndex: 232003 entries, ('AA.US', Timestamp('2017-01-03 00:00:00')) to
('GS.US', Timestamp('2019-12-18 00:00:00'))
Data columns (total 5 columns):
#   Column  Non-Null Count  Dtype
---  -
0   open    232003 non-null    float64
1   high    232003 non-null    float64
2   low     232003 non-null    float64
3   close   232003 non-null    float64
4   volume  232003 non-null    int64
dtypes: float64(4), int64(1)
memory usage: 10.2+ MB

```

1.2.6 Configure Cerebro

```
[13]: cerebro = bt.Cerebro()
      cash = 1000000
      cerebro.broker.setcash(cash)
```

1.2.7 Add Data

```
[14]: for symbol in traded_symbols:
        df = prices.loc[idx[symbol, :], :].droplevel('ticker', axis=0)
        df.index.name = 'datetime'
        bt_data = CustomData(dataname=df)
        cerebro.adddata(bt_data, name=symbol)
```

1.2.8 Add Strategy & Analyzer

```
[15]: cerebro.addstrategy(StatisticalArbitrageCointegration,
                           trades=trades, verbose=True,
                           log_file='bt_log.csv')

cerebro.addanalyzer(bt.analyzers.PyFolio, _name='pyfolio')
```

1.2.9 Run Strategy

```
[16]: start = time()
       results = cerebro.run()

       ending_value = cerebro.broker.getvalue()
       duration = time() - start

       print(f'Final Portfolio Value: {ending_value:,.2f} | Duration:␣
       ↳{format_time(duration)}')
```

2017-02-01 00:00:00 PF:	1,004,229 Net:	33,384 # Pos: 275 # Pairs:
265 Long:	780,496 Short: -747,113	
2017-03-03 00:00:00 PF:	1,028,845 Net:	55,858 # Pos: 280 # Pairs:
235 Long:	779,003 Short: -723,145	
2017-04-03 00:00:00 PF:	1,029,713 Net:	64,817 # Pos: 292 # Pairs:
689 Long:	813,349 Short: -748,532	
2017-05-03 00:00:00 PF:	1,036,655 Net:	73,245 # Pos: 299 # Pairs:
263 Long:	907,078 Short: -833,833	
2017-06-02 00:00:00 PF:	1,014,250 Net:	80,586 # Pos: 282 # Pairs:
218 Long:	844,852 Short: -764,266	
2017-07-03 00:00:00 PF:	997,286 Net:	65,692 # Pos: 284 # Pairs:
161 Long:	797,628 Short: -731,936	
2017-08-02 00:00:00 PF:	1,031,169 Net:	41,116 # Pos: 307 # Pairs:
445 Long:	719,039 Short: -677,923	
2017-08-31 00:00:00 PF:	1,048,305 Net:	12,173 # Pos: 297 # Pairs:
123 Long:	851,316 Short: -839,143	
2017-10-02 00:00:00 PF:	1,071,228 Net:	57,038 # Pos: 308 # Pairs:
402 Long:	841,222 Short: -784,183	
2017-10-31 00:00:00 PF:	1,073,403 Net:	67,754 # Pos: 302 # Pairs:
308 Long:	828,308 Short: -760,554	

2017-11-30 00:00:00 PF: 1,082,732 Net: 117 Long: 902,876 Short: -835,634	67,242 # Pos: 301 # Pairs:
2018-01-02 00:00:00 PF: 1,091,401 Net: 76 Long: 999,405 Short: -962,065	37,340 # Pos: 299 # Pairs:
2018-02-01 00:00:00 PF: 1,103,410 Net: 306 Long: 868,493 Short: -819,425	49,068 # Pos: 305 # Pairs:
2018-03-05 00:00:00 PF: 1,107,687 Net: 96 Long: 957,032 Short: -912,928	44,104 # Pos: 302 # Pairs:
2018-04-04 00:00:00 PF: 1,079,159 Net: 2,472 Long: 555,688 Short: -533,376	22,311 # Pos: 311 # Pairs:
2018-05-03 00:00:00 PF: 1,088,873 Net: 518 Long: 764,980 Short: -699,314	65,666 # Pos: 308 # Pairs:
2018-06-04 00:00:00 PF: 1,120,888 Net: 446 Long: 931,262 Short: -796,187	135,075 # Pos: 305 # Pairs:
2018-08-02 00:00:00 PF: 1,070,713 Net: 365 Long: 837,295 Short: -780,409	56,885 # Pos: 305 # Pairs:
2018-08-31 00:00:00 PF: 1,062,973 Net: 235 Long: 828,683 Short: -788,621	40,063 # Pos: 303 # Pairs:
2018-10-31 00:00:00 PF: 1,093,611 Net: 427 Long: 906,958 Short: -820,318	86,639 # Pos: 306 # Pairs:
2018-11-30 00:00:00 PF: 1,069,840 Net: 78 Long: 936,790 Short: -891,661	45,130 # Pos: 304 # Pairs:
2019-02-04 00:00:00 PF: 1,109,595 Net: 187 Long: 946,751 Short: -877,677	69,074 # Pos: 302 # Pairs:
2019-03-06 00:00:00 PF: 1,105,897 Net: 153 Long: 919,108 Short: -840,812	78,295 # Pos: 298 # Pairs:
2019-04-04 00:00:00 PF: 1,064,659 Net: 732 Long: 740,735 Short: -715,616	25,119 # Pos: 311 # Pairs:
2019-05-06 00:00:00 PF: 1,081,817 Net: 528 Long: 831,293 Short: -732,390	98,903 # Pos: 310 # Pairs:
2019-06-05 00:00:00 PF: 1,140,606 Net: 371 Long: 1,051,369 Short: -951,951	99,417 # Pos: 308 # Pairs:
2019-07-05 00:00:00 PF: 1,129,195 Net: 1,554 Long: 475,318 Short: -454,052	21,267 # Pos: 311 # Pairs:
2019-08-05 00:00:00 PF: 1,124,039 Net: 258 Long: 921,601 Short: -847,171	74,430 # Pos: 309 # Pairs:
2019-09-04 00:00:00 PF: 1,133,501 Net: 125 Long: 967,723 Short: -905,064	62,659 # Pos: 304 # Pairs:
Final Portfolio Value: 1,079,614.04 Duration: 00:07:22	

1.2.10 Get PyFolio Inputs

```
[17]: pyfolio_analyzer = results[0].analyzers.getbyname('pyfolio')
      returns, positions, transactions, gross_lev = pyfolio_analyzer.get_pf_items()
```

```
[18]: returns.to_hdf(STORE, 'returns')
      positions.to_hdf(STORE, 'positions')
```

```
transactions.to_hdf(STORE, 'transactions/')
gross_lev.to_hdf(STORE, 'gross_lev')
```

1.2.11 Get Positions

The PyFolio integration is somewhat broken due to API changes after version 0.5.1 so we need to retrieve the positions manually.

```
[19]: traded_pairs = pd.DataFrame(results[0].exposure)
traded_pairs.date = pd.to_datetime(traded_pairs.date)
traded_pairs = traded_pairs.set_index('date').tz_localize('UTC')
traded_pairs.to_hdf(STORE, 'traded_pairs')
traded_pairs.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 736 entries, 2017-01-04 00:00:00+00:00 to 2019-12-18
00:00:00+00:00
Columns: 312 entries, AA.US to cash
dtypes: float64(312)
memory usage: 1.8 MB
```

1.2.12 Get Metrics

```
[20]: metrics = pd.DataFrame(results[0].metrics,
                             columns=['date', 'pf', 'net_holdings', 'cash',
                                     'npositions', 'npairs', 'nlong_pos',
                                     ↪ 'nshort_pos',
                                     'target', 'target_val', 'nlong_trades',
                                     'nshort_trades', 'nclose_trades'])
metrics.to_hdf(STORE, 'metrics')
```

1.3 Run PyFolio Analysis

```
[21]: returns = pd.read_hdf(STORE, 'returns')
transactions = pd.read_hdf(STORE, 'transactions/')
gross_lev = pd.read_hdf(STORE, 'gross_lev')
metrics = pd.read_hdf(STORE, 'metrics').set_index('date')
```

```
[22]: metrics.info()
```

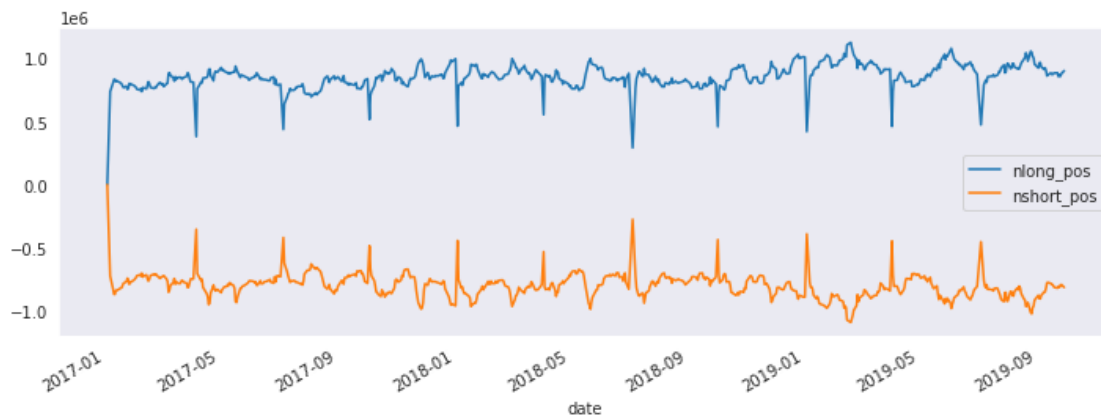
```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 676 entries, 2017-01-03 to 2019-09-30
Data columns (total 12 columns):
#   Column          Non-Null Count  Dtype
---  -
0   pf              676 non-null   float64
1   net_holdings    676 non-null   float64
```

```

2  cash          676 non-null    float64
3  npositions    676 non-null    int64
4  npairs        676 non-null    int64
5  nlong_pos     676 non-null    float64
6  nshort_pos    676 non-null    float64
7  target        676 non-null    float64
8  target_val    676 non-null    float64
9  nlong_trades  676 non-null    int64
10 nshort_trades 676 non-null    int64
11 nclose_trades 676 non-null    int64
dtypes: float64(7), int64(5)
memory usage: 68.7 KB

```

```
[23]: metrics[['nlong_pos', 'nshort_pos']].plot(figsize=(12, 4));
```

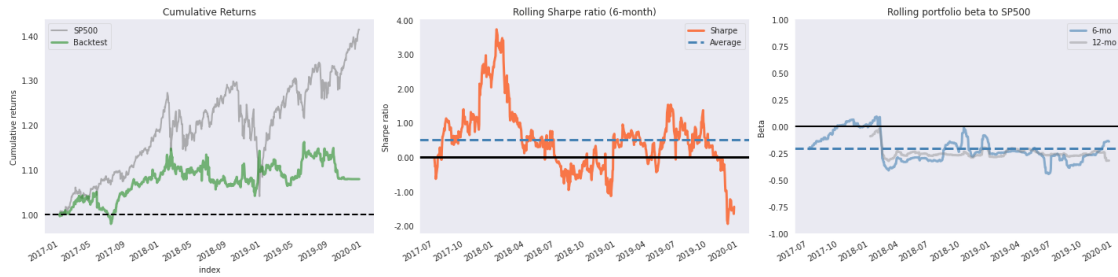


1.3.1 Get Benchmark

```
[24]: start = str(returns.index.min().year)
      end = str(returns.index.max().year + 1)
```

```
[25]: benchmark = web.DataReader('SP500', 'fred',
                                start=start,
                                end=end).squeeze()
      benchmark = benchmark.pct_change().tz_localize('UTC')
```

```
[26]: fig, axes = plt.subplots(ncols=3, figsize=(20,5))
      pf.plotting.plot_rolling_returns(returns, factor_returns=benchmark, ax=axes[0])
      axes[0].set_title('Cumulative Returns')
      pf.plotting.plot_rolling_sharpe(returns, ax=axes[1])
      pf.plotting.plot_rolling_beta(returns, benchmark, ax=axes[2])
      sns.despine()
      fig.tight_layout();
```



1.3.2 Create full tearsheet

```
[27]: pf.create_full_tear_sheet(returns,
                                positions=positions,
                                transactions=transactions,
                                benchmark_rets=benchmark.loc[returns.index],
                                estimate_intraday=False)
```

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