

Core_and_Satellite

September 29, 2021

1 Core and Satellite

<https://www.investopedia.com/articles/financial-theory/08/core-satellite-investing.asp>

Portfolio Construction

Managed passively

Actively managed

High-yield bond

```
[1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import math

import warnings
warnings.filterwarnings("ignore")

# yfinance is used to fetch data
import yfinance as yf
yf.pdr_override()
```

S&P 500 Index Fund

Actively Managed High-Yield Bond Fund

Actively Managed Biotechnology Fund

Actively Managed Commodities Fund

```
[2]: # input
symbols = ['SPY', 'FIHBX', 'FBTAX', 'DBC']
start = '2014-01-01'
end = '2019-01-01'

# Read data
dataset = yf.download(symbols, start, end)['Adj Close']

# View Columns
dataset.head()
```

```
[*****100%*****] 4 of 4 completed
```

```
[2]:
```

	DBC	FBTAX	FIHBX	SPY
Date				
2014-01-02	24.572100	16.094238	6.937886	160.925400
2014-01-03	24.416641	16.017763	6.944685	160.898972
2014-01-06	24.445789	15.813823	6.944685	160.432693
2014-01-07	24.426357	16.068747	6.958275	161.418060
2014-01-08	24.193171	16.374655	6.958275	161.453278

```
[3]: dataset.tail()
```

```
[3]:
```

	DBC	FBTAX	FIHBX	SPY
Date				
2018-12-24	14.163118	20.312393	8.307596	227.638824
2018-12-26	14.478073	21.567284	8.289378	239.140244
2018-12-27	14.340280	21.632837	8.298485	240.976212
2018-12-28	14.222172	21.632837	8.334924	240.665375
2018-12-31	14.261541	22.101082	8.388957	242.773315

```
[4]: from datetime import datetime

def calculate_years(start, end):
    date_format = "%Y-%m-%d"
    a = datetime.strptime(start, date_format).year
    b = datetime.strptime(end, date_format).year
    years = b - a

    return years
```

```
[5]: print(calculate_years(start, end), 'years')
```

5 years

```
[6]: # Calculate Daily Returns
returns = dataset.pct_change()
returns = returns.dropna()
```

```
[7]: # Calculate mean returns
meanDailyReturns = returns.mean()
print(meanDailyReturns)
```

```
DBC      -0.000388
FBTAX     0.000403
FIHBX     0.000155
SPY       0.000362
dtype: float64
```

```
[8]: # Calculate std returns
stdDailyReturns = returns.std()
print(stdDailyReturns)
```

```
DBC      0.009496
FBTAX    0.017337
FIHBX    0.002734
SPY      0.008306
dtype: float64
```

```
[9]: # Define weights for the portfolio
weights = np.array([0.50, 0.10, 0.20, 0.20])
```

```
[10]: # Calculate the covariance matrix on daily returns
cov_matrix = (returns.cov())*250
print (cov_matrix)
```

	DBC	FBTAX	FIHBX	SPY
DBC	0.022544	0.005441	0.001920	0.006348
FBTAX	0.005441	0.075140	0.003101	0.023501
FIHBX	0.001920	0.003101	0.001869	0.002384
SPY	0.006348	0.023501	0.002384	0.017247

```
[11]: # Calculate expected portfolio performance
portReturn = np.sum(meanDailyReturns*weights)
```

```
[12]: # Print the portfolio return
print(portReturn)
```

```
-5.022474207717689e-05
```

```
[13]: # Create portfolio returns column
returns['Portfolio'] = returns.dot(weights)
```

```
[14]: returns.head()
```

```
[14]:
```

	DBC	FBTAX	FIHBX	SPY	Portfolio
Date					
2014-01-03	-0.006327	-0.004752	0.000980	-0.000164	-0.003475
2014-01-06	0.001194	-0.012732	0.000000	-0.002898	-0.001256
2014-01-07	-0.000795	0.016120	0.001957	0.006142	0.002834
2014-01-08	-0.009547	0.019037	0.000000	0.000218	-0.002826
2014-01-09	-0.008032	0.047743	0.000000	0.000654	0.000889

```
[15]: returns.tail()
```

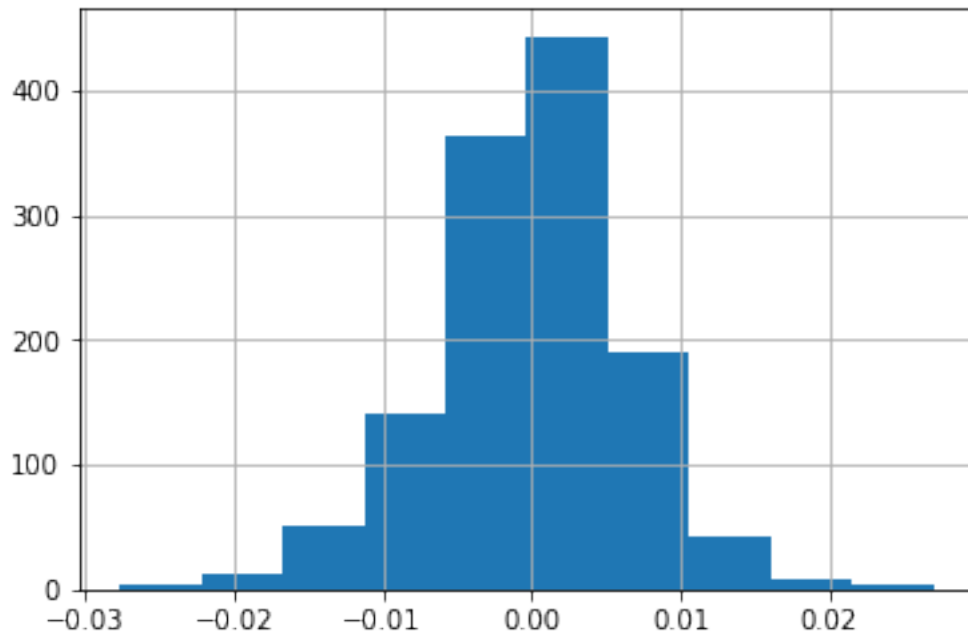
```
[15]:
```

	DBC	FBTAX	FIHBX	SPY	Portfolio
Date					
2018-12-24	-0.011065	-0.010944	-0.003279	-0.026423	-0.012567
2018-12-26	0.022238	0.061780	-0.002193	0.050525	0.026963
2018-12-27	-0.009517	0.003039	0.001099	0.007677	-0.002700
2018-12-28	-0.008236	0.000000	0.004391	-0.001290	-0.003498
2018-12-31	0.002768	0.021645	0.006483	0.008759	0.006597

```
[16]: # Calculate cumulative returns
daily_cum_ret=(1+returns).cumprod()
print(daily_cum_ret.tail())
```

	DBC	FBTAX	FIHBX	SPY	Portfolio
Date					
2018-12-24	0.576390	1.262091	1.197425	1.414561	0.889783
2018-12-26	0.589208	1.340062	1.194799	1.486032	0.913774
2018-12-27	0.583600	1.344136	1.196111	1.497441	0.911307
2018-12-28	0.578794	1.344136	1.201364	1.495509	0.908120
2018-12-31	0.580396	1.373229	1.209152	1.508608	0.914110

```
[17]: returns['Portfolio'].hist()
plt.show()
```

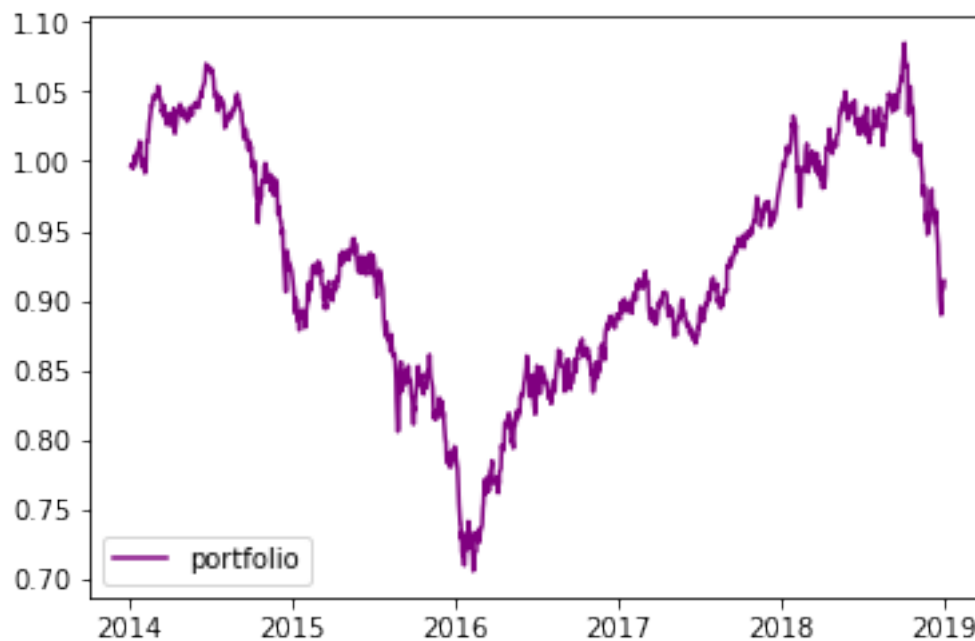


```
[18]: import matplotlib.dates
```

```

# Plot the portfolio cumulative returns only
fig, ax = plt.subplots()
ax.plot(daily_cum_ret.index, daily_cum_ret.Portfolio, color='purple',
        label="portfolio")
ax.xaxis.set_major_locator(matplotlib.dates.YearLocator())
plt.legend()
plt.show()

```



```

[19]: # Print the mean
print("mean : ", returns['Portfolio'].mean()*100)

# Print the standard deviation
print("Std. dev: ", returns['Portfolio'].std()*100)

# Print the skewness
print("skew: ", returns['Portfolio'].skew())

# Print the kurtosis
print("kurt: ", returns['Portfolio'].kurtosis())

```

```

mean : -0.005022474207717679
Std. dev: 0.6512920236657875
skew: -0.22605463679872187
kurt: 1.299622507098448

```

```
[20]: # Calculate the standard deviation by taking the square root
port_standard_dev = np.sqrt(np.dot(weights.T, np.dot(weights, cov_matrix)))

# Print the results
print(str(np.round(port_standard_dev, 4) * 100) + '%')
```

10.299999999999999%

```
[21]: # Calculate the portfolio variance
port_variance = np.dot(weights.T, np.dot(cov_matrix, weights))

# Print the result
print(str(np.round(port_variance, 4) * 100) + '%')
```

1.06%

```
[22]: # Calculate total return and annualized return from price data
total_return = (returns['Portfolio'][-1] - returns['Portfolio'][0]) /
↳ returns['Portfolio'][0]

# Annualize the total return over 5 year
annualized_return = ((1+total_return)**(1/5))-1
```

```
[23]: # Calculate annualized volatility from the standard deviation
vol_port = returns['Portfolio'].std() * np.sqrt(250)
```

```
[24]: # Calculate the Sharpe ratio
rf = 0.01
sharpe_ratio = ((annualized_return - rf) / vol_port)
print(sharpe_ratio)
```

nan

```
[25]: # Create a downside return column with the negative returns only
target = 0
downside_returns = returns.loc[returns['Portfolio'] < target]

# Calculate expected return and std dev of downside
expected_return = returns['Portfolio'].mean()
down_stdev = downside_returns.std()

# Calculate the sortino ratio
rf = 0.01
sortino_ratio = (expected_return - rf)/down_stdev

# Print the results
print("Expected return: ", expected_return*100)
```

```

print('-' * 50)
print("Downside risk:")
print(down_stdev*100)
print('-' * 50)
print("Sortino ratio:")
print(sortino_ratio)

```

Expected return: -0.005022474207717679

Downside risk:

```

DBC          0.717214
FBTAX        1.608918
FIHBX        0.269959
SPY          0.779532
Portfolio    0.459835
dtype: float64

```

Sortino ratio:

```

DBC          -1.401287
FBTAX        -0.624657
FIHBX        -3.722868
SPY          -1.289263
Portfolio    -2.185616
dtype: float64

```

```

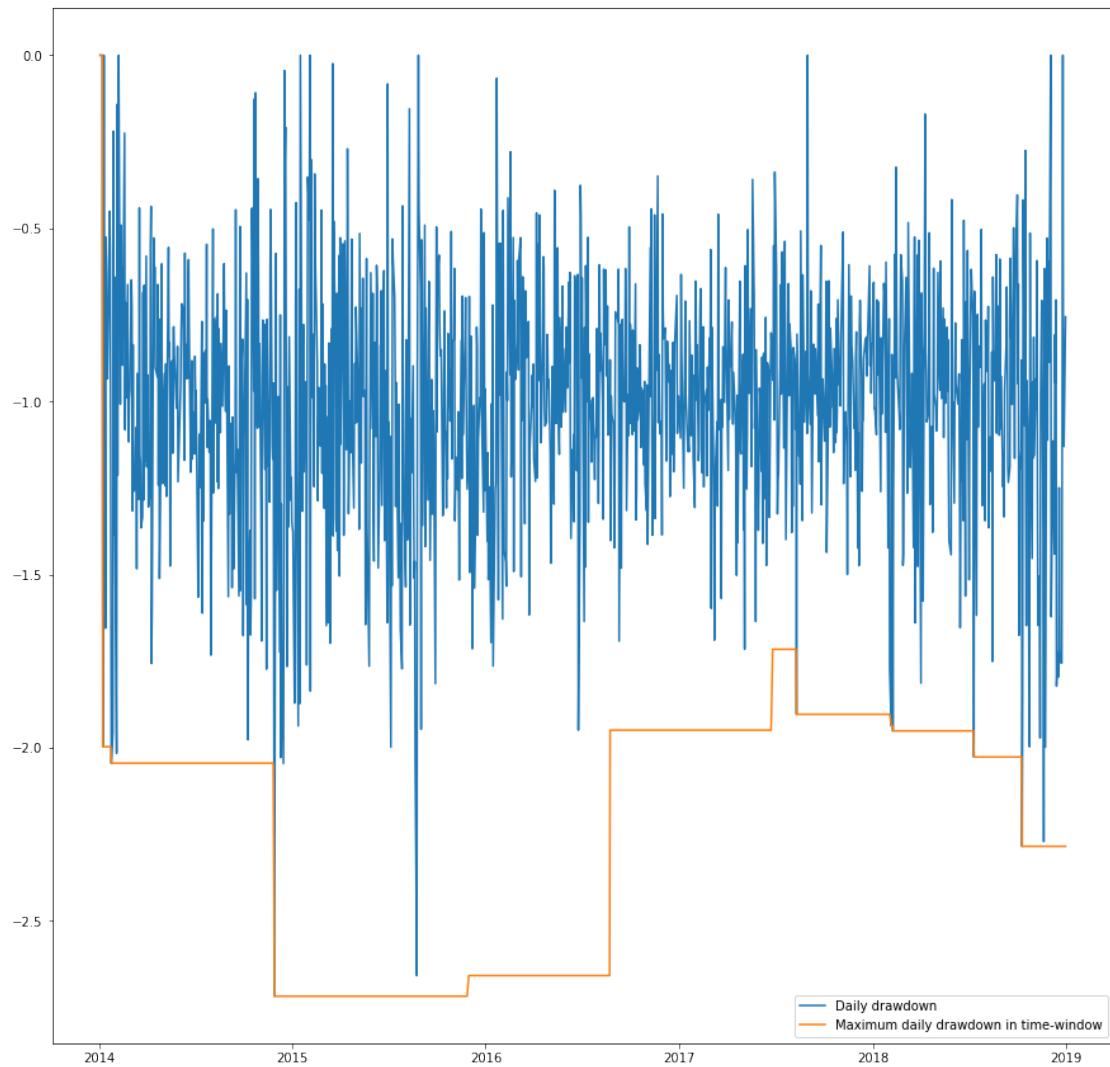
[26]: # Calculate the max value
roll_max = returns['Portfolio'].rolling(center=False,min_periods=1,window=252).
      ↪max()

# Calculate the daily draw-down relative to the max
daily_draw_down = returns['Portfolio']/roll_max - 1.0

# Calculate the minimum (negative) daily draw-down
max_daily_draw_down = daily_draw_down.
      ↪rolling(center=False,min_periods=1,window=252).min()

# Plot the results
plt.figure(figsize=(15,15))
plt.plot(returns.index, daily_draw_down, label='Daily drawdown')
plt.plot(returns.index, max_daily_draw_down, label='Maximum daily drawdown in_
      ↪time-window')
plt.legend()
plt.show()

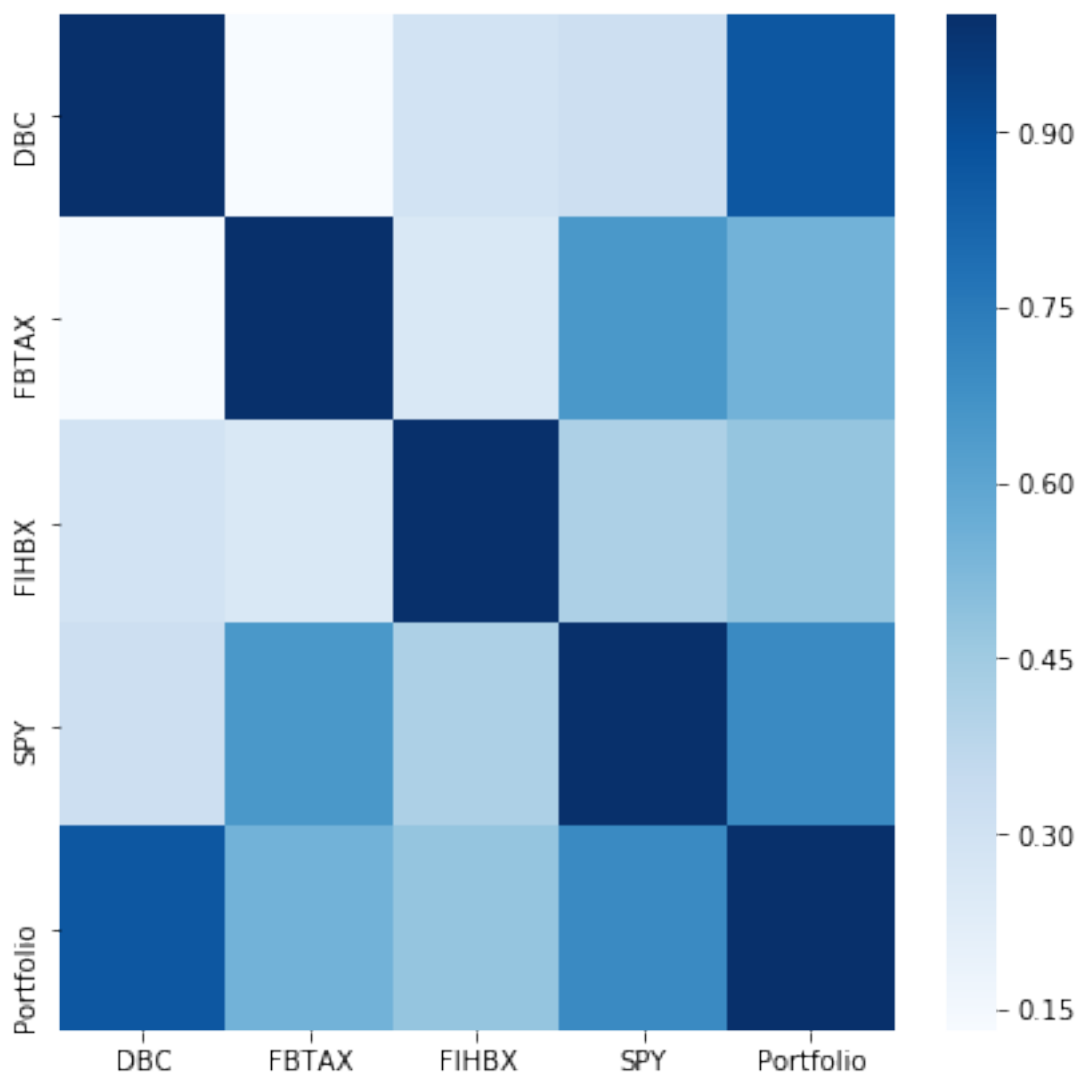
```



```
[27]: plt.figure(figsize=(7,7))
      corr = returns.corr()

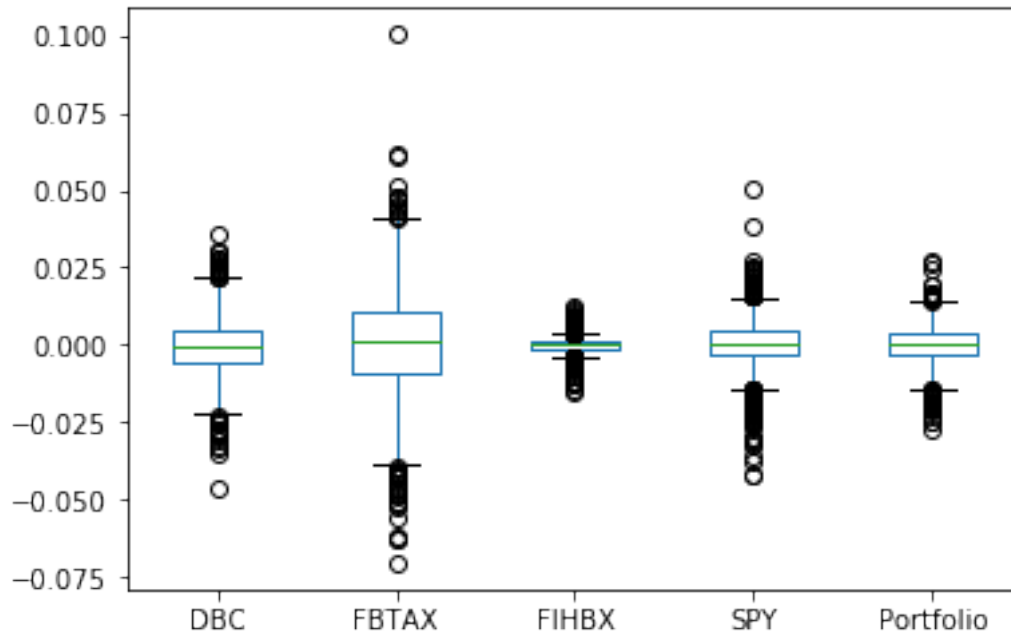
      # plot the heatmap
      sns.heatmap(corr,
                  xticklabels=corr.columns,
                  yticklabels=corr.columns,
                  cmap="Blues")
```

```
[27]: <matplotlib.axes._subplots.AxesSubplot at 0x275d358c2b0>
```

```
[28]: # Box plot
      returns.plot(kind='box')
```

```
[28]: <matplotlib.axes._subplots.AxesSubplot at 0x275d35f83c8>
```

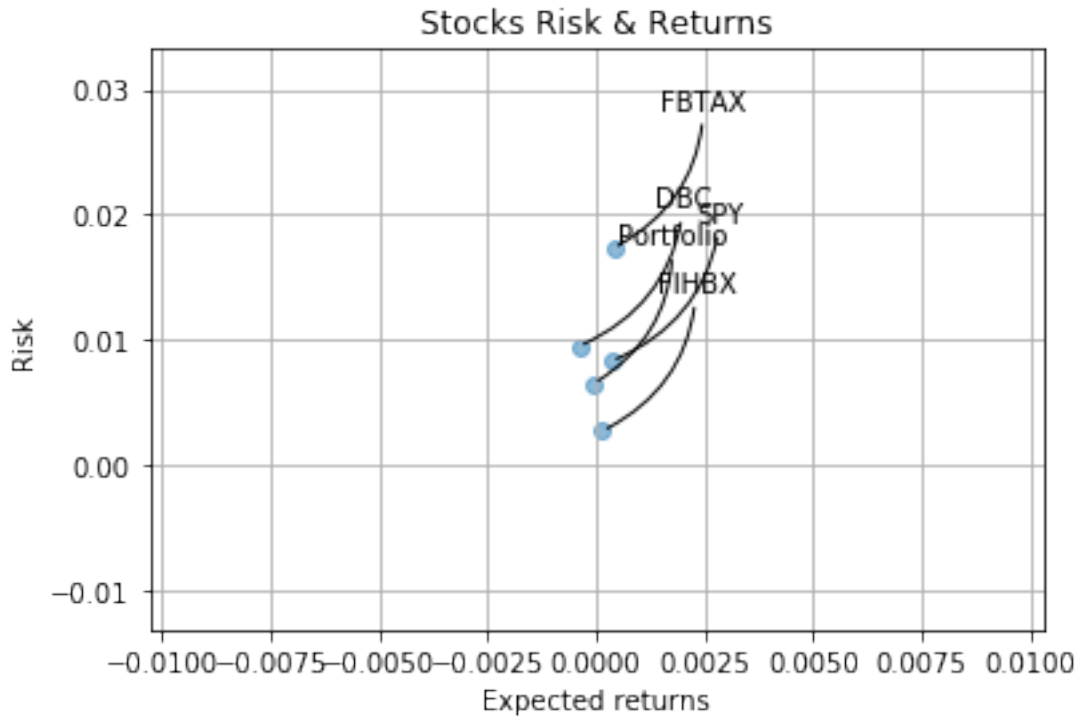


```
[29]: rets = returns.dropna()

plt.scatter(rets.mean(), rets.std(), alpha = 0.5)

plt.title('Stocks Risk & Returns')
plt.xlabel('Expected returns')
plt.ylabel('Risk')
plt.grid(which='major')

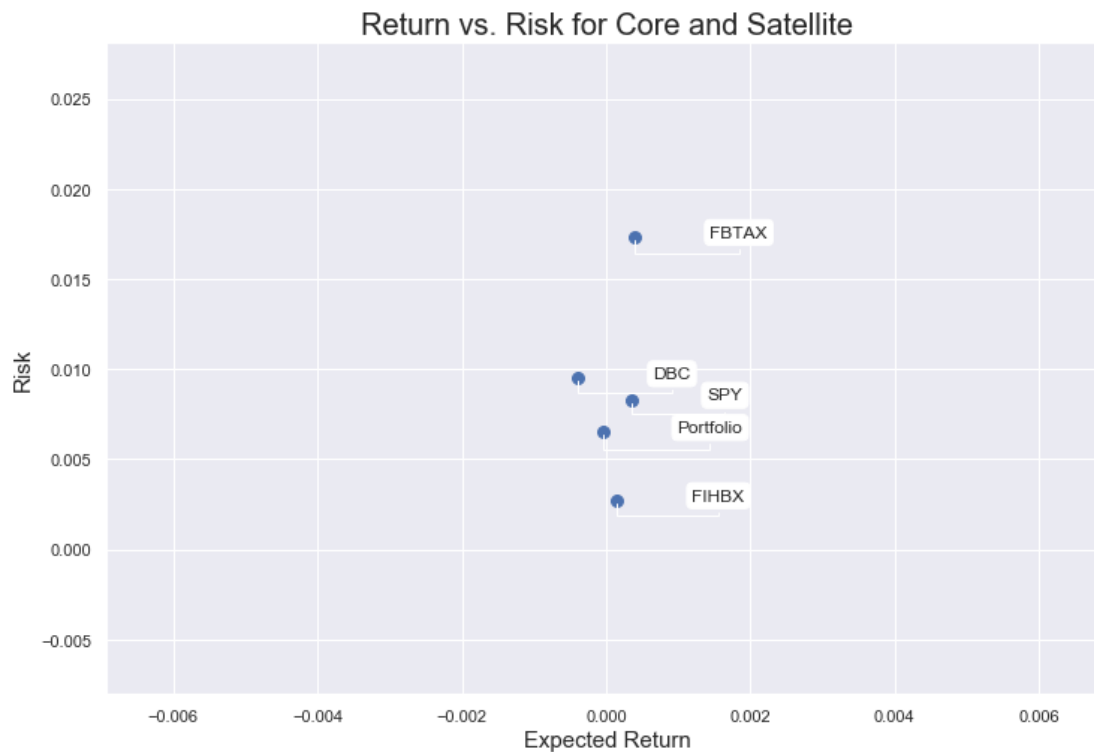
for label, x, y in zip(rets.columns, rets.mean(), rets.std()):
    plt.annotate(
        label,
        xy = (x, y), xytext = (50, 50),
        textcoords = 'offset points', ha = 'right', va = 'bottom',
        arrowprops = dict(arrowstyle = '-', connectionstyle = 'arc3,rad=-0.3'))
```



```
[30]: area = np.pi*20.0

sns.set(style='darkgrid')
plt.figure(figsize=(12,8))
plt.scatter(rets.mean(), rets.std(), s=area)
plt.xlabel("Expected Return", fontsize=15)
plt.ylabel("Risk", fontsize=15)
plt.title("Return vs. Risk for Core and Satellite", fontsize=20)

for label, x, y in zip(rets.columns, rets.mean(), rets.std()):
    plt.annotate(label, xy=(x,y), xytext=(50, 0), textcoords='offset points',
                 arrowprops=dict(arrowstyle='-',
                                   ↪connectionstyle='bar,angle=180,fraction=-0.2'),
                 bbox=dict(boxstyle="round", fc="w"))
```



```
[31]: print("Stock returns: ")
      print(rets.mean())
      print('-' * 50)
      print("Stock risk:")
      print(rets.std())
```

Stock returns:

```
DBC          -0.000388
FBTAX         0.000403
FIHBX         0.000155
SPY           0.000362
Portfolio    -0.000050
dtype: float64
```

Stock risk:

```
DBC          0.009496
FBTAX        0.017337
FIHBX        0.002734
SPY          0.008306
Portfolio    0.006513
dtype: float64
```

```
[32]: table = pd.DataFrame()
table['Returns'] = rets.mean()
table['Risk'] = rets.std()
table.sort_values(by='Returns')
```

```
[32]:
```

	Returns	Risk
DBC	-0.000388	0.009496
Portfolio	-0.000050	0.006513
FIHBX	0.000155	0.002734
SPY	0.000362	0.008306
FBTAX	0.000403	0.017337

```
[33]: table.sort_values(by='Risk')
```

```
[33]:
```

	Returns	Risk
FIHBX	0.000155	0.002734
Portfolio	-0.000050	0.006513
SPY	0.000362	0.008306
DBC	-0.000388	0.009496
FBTAX	0.000403	0.017337

```
[34]: rf = 0.01
table['Sharpe_Ratio'] = (table['Returns'] - rf) / table['Risk']
table
```

```
[34]:
```

	Returns	Risk	Sharpe_Ratio
DBC	-0.000388	0.009496	-1.093885
FBTAX	0.000403	0.017337	-0.553582
FIHBX	0.000155	0.002734	-3.601052
SPY	0.000362	0.008306	-1.160409
Portfolio	-0.000050	0.006513	-1.543121

```
[35]: days_per_year = 52 * 5
total_days_in_simulation = dataset.shape[0]
number_of_years = total_days_in_simulation / days_per_year
```

```
[36]: total_relative_returns = (np.exp(returns['Portfolio'].cumsum()) - 1)
total_portfolio_return = total_relative_returns[-1]

# Average portfolio return assuming compounding of returns
average_yearly_return = (1 + total_portfolio_return)**(1 / number_of_years) - 1
```

```
[37]: print('Total portfolio return is: ' +
          '{:5.2f}'.format(100 * total_portfolio_return) + '%')
print('Average yearly return is: ' +
      '{:5.2f}'.format(100 * average_yearly_return) + '%')
```

Total portfolio return is: -6.12%
Average yearly return is: -1.30%