04 manifold learning asset prices

September 29, 2021

1 Manifold Learning: t-SNE and UMAP for Equity Return

This notebook explores how t-SNE and UMAP perform on equity returns.

1.1 Imports & Settings

```
[]: from pathlib import Path
     from os.path import join
     import pandas as pd
     import numpy as np
     from numpy.random import choice, randint, uniform, randn
     import seaborn as sns
     import matplotlib.pyplot as plt
     import ipyvolume as ipv
     from sklearn.datasets import fetch_openml, make swiss_roll, make_blobs
     from sklearn.decomposition import PCA
     from sklearn.manifold import TSNE
     import umap
     from plotly.offline import init_notebook_mode, iplot
     from plotly.graph_objs import *
     import colorlover as cl
[2]: %matplotlib inline
```

```
[2]: %matplotlib inline
plt.style.use('ggplot')
pd.options.display.float_format = '{:,.2f}'.format
```

1.2 Load equity returns

```
[4]: returns = returns.dropna(thresh=int(returns.shape[0] * .95), axis=1)
    returns = returns.dropna(thresh=int(returns.shape[1] * .95))
    returns.info()

    <class 'pandas.core.frame.DataFrame'>
        DatetimeIndex: 951 entries, 2000-01-16 to 2018-04-01
        Freq: W-SUN
        Columns: 1890 entries, A to ZQK
        dtypes: float64(1890)
        memory usage: 13.7 MB

[5]: returns = returns.sample(n=250)
        daily_avg = returns.mean(1)
        returns = returns.apply(lambda x: x.fillna(daily_avg))

[6]: pca = PCA(n_components=2)
```

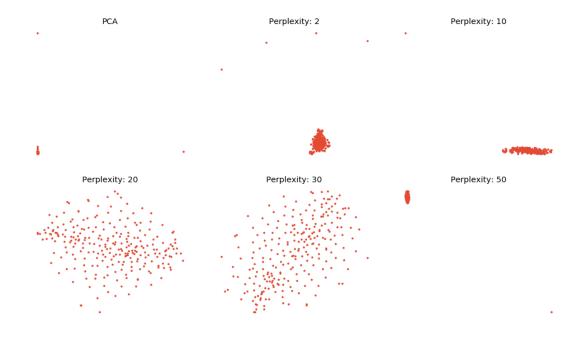
1.3 T-Stochastic Neighbor Embedding (TSNE): Parameter Settings

1.3.1 Perplexity: emphasis on local vs global structure

```
fig, axes = plt.subplots(nrows=2, ncols=3, figsize=(14,8))
axes = axes.flatten()

axes[0].scatter(*pca.fit_transform(returns).T, s=10)
axes[0].set_title('PCA')
axes[0].axis('off')

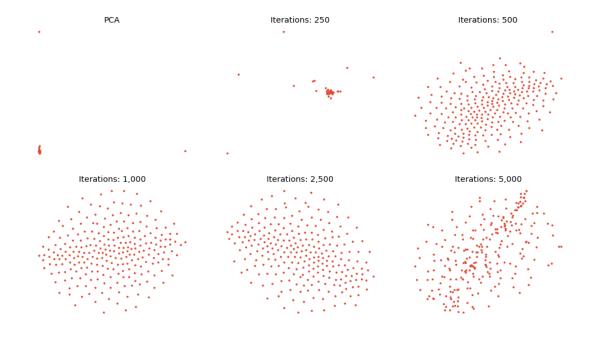
for i, p in enumerate([2,10, 20, 30, 50], 1):
    embedding = TSNE(perplexity=p, n_iter=5000).fit_transform(returns)
    axes[i].scatter(embedding[:, 0], embedding[:, 1], s=10)
    axes[i].set_title('Perplexity: {:.0f}'.format(p))
    axes[i].axis('off')
fig.tight_layout()
```



1.3.2 Convergence with n_iter

```
[8]: fig, axes = plt.subplots(nrows=2, ncols=3, figsize=(14, 8))
    axes = axes.flatten()
    axes[0].scatter(*pca.fit_transform(returns).T, s=10)
    axes[0].set_title('PCA')
    axes[0].axis('off')

for i, n in enumerate([250, 500, 1000, 2500, 5000], 1):
    embedding=TSNE(perplexity=30, n_iter=n).fit_transform(returns)
    axes[i].scatter(embedding[:, 0], embedding[:, 1], s=10)
    axes[i].set_title('Iterations: {:,.0f}'.format(n))
    axes[i].axis('off')
    fig.tight_layout()
```



${\bf 1.4}\quad {\bf Uniform\ Manifold\ Approximation\ and\ Projection\ (UMAP):\ Parameter\ Settings}$

1.4.1 Neighbors

```
[9]: fig, axes = plt.subplots(nrows=2, ncols=3, figsize=(14,8))
    axes = axes.flatten()

axes[0].scatter(*pca.fit_transform(returns).T, s=10)
    axes[0].set_title('PCA')
    axes[0].axis('off')

for i, n in enumerate([2,10, 20, 30, 50], 1):
    embedding = umap.UMAP(n_neighbors=n, min_dist=0.1).fit_transform(returns)
    axes[i].scatter(embedding[:, 0], embedding[:, 1], s=10)
    axes[i].set_title('Neighbors: {:.0f}'.format(n))
    axes[i].axis('off')
    fig.tight_layout()
```

/home/stefan/.pyenv/versions/miniconda3-latest/envs/ml4t/lib/python3.7/site-packages/umap/spectral.py:229: UserWarning:

Embedding a total of 3 separate connected components using meta-embedding (experimental)



1.4.2 Minimum Distance

```
[10]: fig, axes = plt.subplots(nrows=2, ncols=3, figsize=(14,8))
    axes = axes.flatten()

axes[0].scatter(*pca.fit_transform(returns).T, s=10)
    axes[0].set_title('PCA')
    axes[0].axis('off')

for i, d in enumerate([.001, .01, .1, .2, .5], 1):
    embedding = umap.UMAP(n_neighbors=30, min_dist=d).fit_transform(returns)
    axes[i].scatter(embedding[:, 0], embedding[:, 1], s=10)
    axes[i].set_title('Min. Distance: {:.3f}'.format(d))
    axes[i].axis('off')
    fig.tight_layout()
```

