# Water Stock Portfolio

September 29, 2021

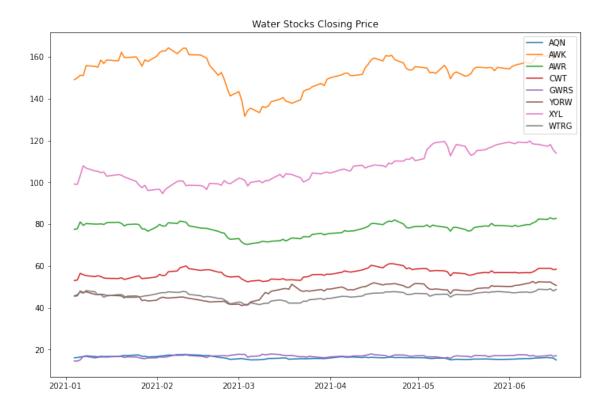
#### 1 Water Stock Portfolio Risk and Returns

```
[1]: import numpy as np
    import pandas as pd
    import matplotlib.pyplot as plt
    import seaborn as sns
    import math
    from sklearn.linear_model import LinearRegression
    import warnings
    warnings.filterwarnings("ignore")
    # yahoo finance is used to fetch data
    import yfinance as yf
    yf.pdr_override()
[2]: # input
    # Water Stock
    title = 'Water'
    symbols = ['AQN','AWK','AWR','CWT', 'GWRS', 'YORW', 'XYL', 'WTRG']
    start = '2021-01-01'
    end = '2021-06-18'
[3]: df = pd.DataFrame()
    for s in symbols:
        df[s] = yf.download(s,start,end)['Adj Close']
    [******** 100%********* 1 of 1 completed
```

```
[4]: from datetime import datetime
    from dateutil import relativedelta
    d1 = datetime.strptime(start, "%Y-%m-%d")
    d2 = datetime.strptime(end, "%Y-%m-%d")
    delta = relativedelta.relativedelta(d2,d1)
    print('How many years of investing?')
    print('%s years' % delta.years)
    How many years of investing?
    0 years
[5]: number_of_years = delta.years
[6]: months = (d2.year - d1.year) * 12 + (d2.month - d1.month)
    months
[6]: 5
[7]: days = (df.index[-1] - df.index[0]).days
    days
[7]: 164
[8]: df.head()
[8]:
                                  AWK
                                             AWR
                                                        CWT
                                                                  GWRS
                                                                             YORW \
                      AQN
    Date
    2021-01-04 16.091688 149.145187
                                       77.538078 53.019135 14.546535
                                                                        45.562466
    2021-01-05 16.180811 149.988983
                                       77.835579 53.277039 14.457294 45.721775
    2021-01-06 16.418472 151.249741
                                       81.088226 56.490925 15.081991 47.991936
    2021-01-07 16.646231 151.021408
                                       79.422234 55.856083 16.708191 47.304913
    2021-01-08 17.002724 155.836060
                                       80.304817 55.350193 16.737936 47.633492
                       XYL
                                 WTRG
    Date
    2021-01-04
                 99.169624
                            45.696087
    2021-01-05
                 99.050247
                            46.309460
    2021-01-06 103.228317
                            47.526310
    2021-01-07
                107.913742
                            46.972294
    2021-01-08 106.819481
                            48.199036
[9]: df.tail()
[9]:
                                  AWK
                                             AWR
                                                        CWT
                                                                  GWRS
                                                                             YORW
                      AQN
    Date
    2021-06-11 16.010000 160.360001 82.449997 58.830002 16.746450 52.470001
```

```
2021-06-14 16.200001 160.479996
                                        82.230003
                                                   58.849998 17.066000
                                                                        52.270000
     2021-06-15 16.080000
                            161.789993
                                        83.089996 58.910000 17.360001
                                                                        52.330002
     2021-06-16 15.950000
                            158.470001
                                        82.430000
                                                   58.250000
                                                             16.809999
                                                                        51.410000
     2021-06-17 15.000000
                            162.199997
                                        82.839996
                                                   58.430000
                                                             17.080000
                                                                        50.660000
                        XYL
                                  WTRG
     Date
     2021-06-11 118.160004
                             48.860001
     2021-06-14 117.269997
                             48.660000
     2021-06-15 118.089996
                             49.090000
     2021-06-16 115.489998
                             48.070000
     2021-06-17 113.940002 48.770000
[10]: plt.figure(figsize=(12,8))
     plt.plot(df)
     plt.title(title + ' Stocks Closing Price')
     plt.legend(labels=df.columns)
```

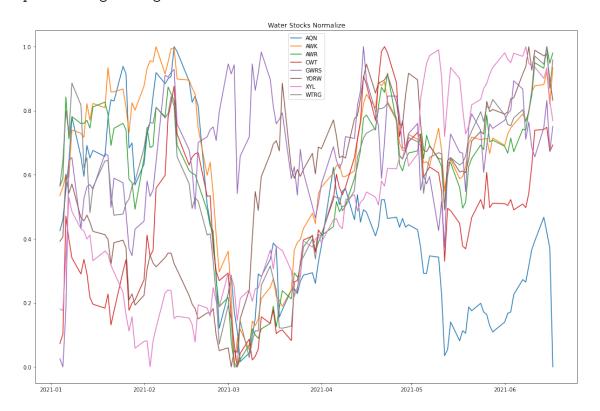
#### [10]: <matplotlib.legend.Legend at 0x1325a351c18>



```
[11]: # Normalize the data
normalize = (df - df.min())/ (df.max() - df.min())
```

```
[12]: plt.figure(figsize=(18,12))
   plt.plot(normalize)
   plt.title(title + ' Stocks Normalize')
   plt.legend(labels=normalize.columns)
```

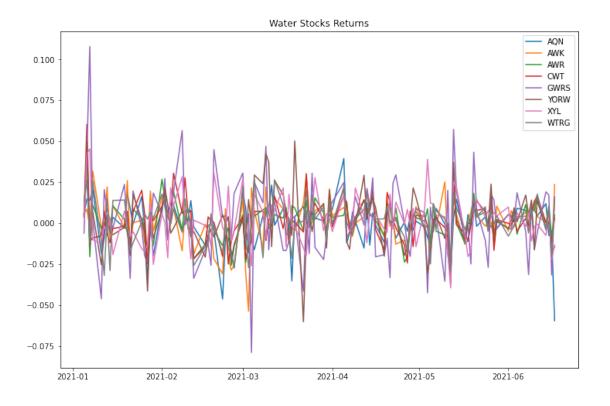
### [12]: <matplotlib.legend.Legend at 0x1325a484da0>



```
[13]: stock_rets = df.pct_change().dropna()

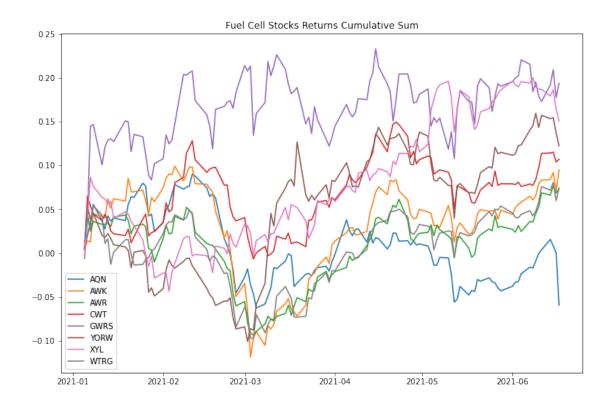
[14]: plt.figure(figsize=(12,8))
    plt.plot(stock_rets)
    plt.title(title +' Stocks Returns')
    plt.legend(labels=stock_rets.columns)
```

[14]: <matplotlib.legend.Legend at 0x1325a52f2b0>



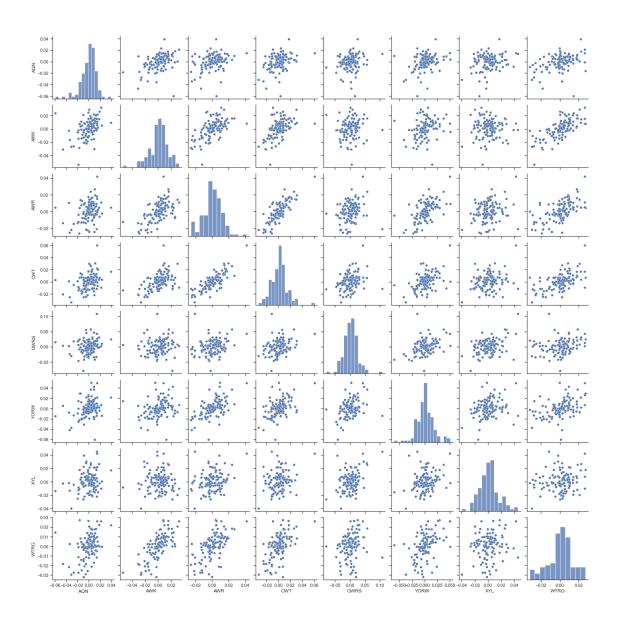
```
[15]: plt.figure(figsize=(12,8))
   plt.plot(stock_rets.cumsum())
   plt.title('Fuel Cell Stocks Returns Cumulative Sum')
   plt.legend(labels=stock_rets.columns)
```

[15]: <matplotlib.legend.Legend at 0x1325a59b940>

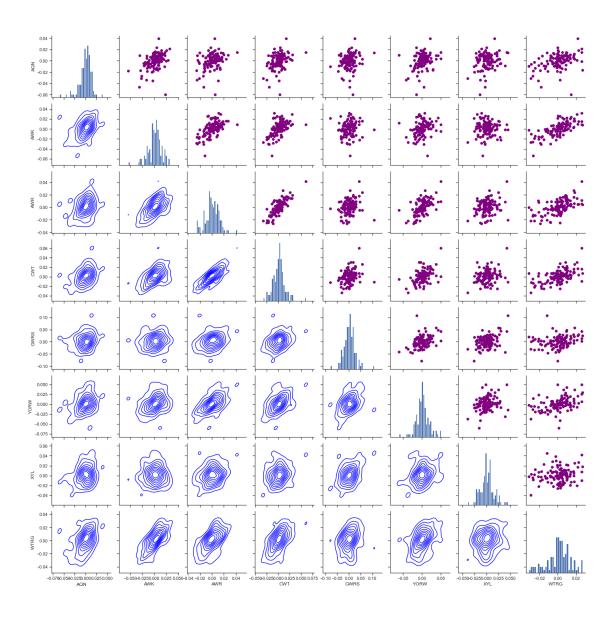


```
[16]: sns.set(style='ticks')
ax = sns.pairplot(stock_rets, diag_kind='hist')

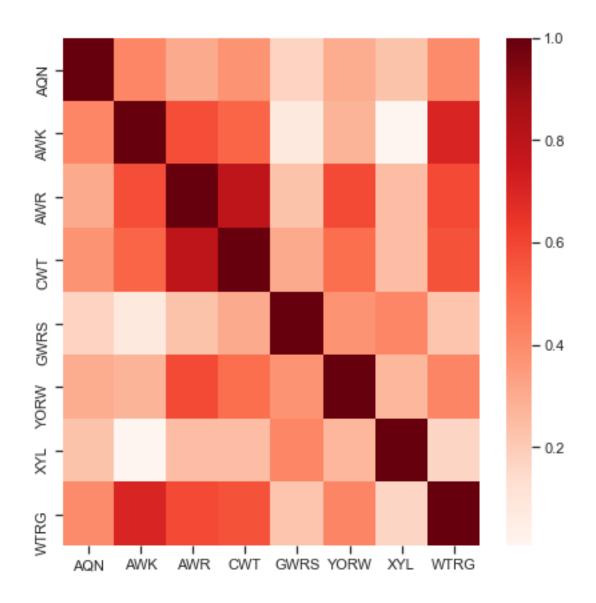
nplot = len(stock_rets.columns)
for i in range(nplot) :
    for j in range(nplot) :
        ax.axes[i, j].locator_params(axis='x', nbins=6, tight=True)
```



```
[17]: ax = sns.PairGrid(stock_rets)
ax.map_upper(plt.scatter, color='purple')
ax.map_lower(sns.kdeplot, color='blue')
ax.map_diag(plt.hist, bins=30)
for i in range(nplot) :
    for j in range(nplot) :
        ax.axes[i, j].locator_params(axis='x', nbins=6, tight=True)
```

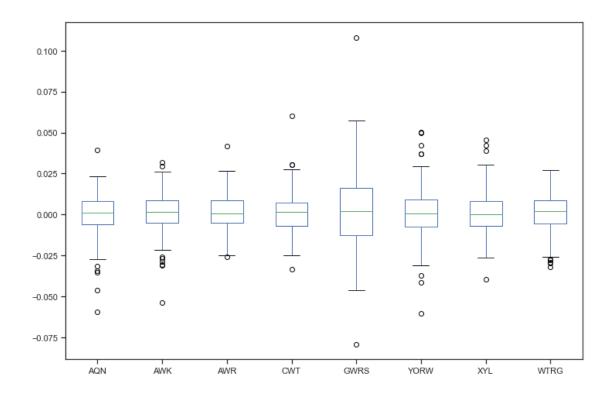


## [18]: <AxesSubplot:>



```
[19]: # Box plot
stock_rets.plot(kind='box',figsize=(12,8))
```

[19]: <AxesSubplot:>

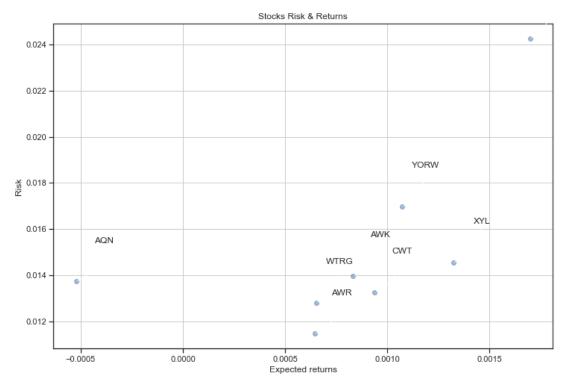


```
[20]: rets = stock_rets.dropna()

plt.figure(figsize=(12,8))
plt.scatter(rets.mean(), rets.std(),alpha = 0.5)

plt.title('Stocks Risk & Returns')
plt.xlabel('Expected returns')
plt.ylabel('Risk')
plt.grid(which='major')

for label, x, y in zip(rets.columns, rets.mean(), rets.std()):
    plt.annotate(
        label,
        xy = (x, y), xytext = (50, 50),
        textcoords = 'offset points', ha = 'right', va = 'bottom',
        arrowprops = dict(arrowstyle = '-', connectionstyle = 'arc3,rad=-0.3'))
```





```
[22]: rest_rets = rets.corr()
     pair_value = rest_rets.abs().unstack()
     pair_value.sort_values(ascending = False)
[22]: WTRG WTRG
                  1.000000
     XYL
          XYL
                  1.000000
     AWK
          AWK
                  1.000000
     AWR
          AWR
                  1.000000
     CWT
          CWT
                  1.000000
     WTRG XYL
                 0.165724
     AWK
          GWRS
                 0.078229
     GWRS AWK
                 0.078229
     AWK
          XYL
                 0.006517
     XYL
          AWK
                 0.006517
     Length: 64, dtype: float64
[23]: # Normalized Returns Data
     Normalized_Value = ((rets[:] - rets[:].min()) /(rets[:].max() - rets[:].min()))
     Normalized_Value.head()
[23]:
                    AQN
                             AWK
                                      AWR
                                               CWT
                                                       GWRS
                                                                YORW \
     Date
```

```
0.545905 0.258465
     2021-01-08 0.817866
                           1.000000
                                                         0.432362
                                                                   0.608553
                                     0.330224 0.270988 0.175484 0.314726
     2021-01-11 0.413332 0.602547
                      XYL
                               WTRG
     Date
     2021-01-05 0.451331 0.766759
     2021-01-06 0.962227
                           0.983909
     2021-01-07 1.000000 0.343059
     2021-01-08 0.346098 0.981202
     2021-01-11 0.316362 0.352744
     Normalized_Value.corr()
[24]:
[24]:
                AQN
                          AWK
                                    AWR
                                              CWT
                                                       GWRS
                                                                 YORW
                                                                            XYL \
     AQN
           1.000000 \quad 0.414033 \quad 0.308962 \quad 0.377098 \quad 0.176483 \quad 0.300493 \quad 0.230793
     AWK
           0.414033 1.000000 0.580059
                                         0.515210 0.078229
                                                             0.277962 0.006517
     AWR
           0.308962 0.580059 1.000000 0.792928 0.229248 0.586184 0.248382
           0.377098 0.515210 0.792928 1.000000 0.307307 0.490191 0.248592
     CWT
     GWRS 0.176483 0.078229 0.229248 0.307307 1.000000 0.374658 0.414804
     YORW 0.300493 0.277962 0.586184 0.490191 0.374658 1.000000 0.269311
     XYL
           0.230793 0.006517 0.248382 0.248592 0.414804 0.269311 1.000000
     WTRG 0.400459 0.708625 0.592487 0.565928 0.221932 0.420316 0.165724
                WTRG
     AQN
           0.400459
     AWK
           0.708625
     AWR
           0.592487
     CWT
           0.565928
     GWRS 0.221932
     YORW 0.420316
     XYL
           0.165724
     WTRG 1.000000
[25]: normalized_rets = Normalized_Value.corr()
     normalized_pair_value = normalized_rets.abs().unstack()
     normalized_pair_value.sort_values(ascending = False)
[25]: WTRG WTRG
                   1.000000
     XYL
           XYL
                   1.000000
     AWK
           AWK
                   1.000000
     AWR
           AWR
                   1.000000
     CWT
           CWT
                   1.000000
     WTRG
           XYL
                   0.165724
     AWK
           GWRS
                   0.078229
```

2021-01-06 0.749913 0.725958 1.000000 1.000000 0.654129 0.995270

0.077275 0.235155

1.000000 0.416023

2021-01-07 0.741674 0.610208

```
0.078229
      GWRS AWK
      AWK
           XYL
                    0.006517
      XYL
            AWK
                    0.006517
      Length: 64, dtype: float64
[26]: print("Stock returns: ")
      print(rets.mean())
      print('-' * 50)
      print("Stock risks:")
      print(rets.std())
     Stock returns:
     AQN
            -0.000522
     AWK
             0.000833
     AWR
             0.000645
     CWT
             0.000939
     GWRS
             0.001699
     YORW
             0.001073
     XYL
             0.001323
     WTRG
             0.000653
     dtype: float64
     Stock risks:
     AQN
             0.013730
     AWK
             0.013953
             0.011456
     AWR.
     CWT
             0.013260
             0.024254
     GWRS
     YORW
             0.016962
     XYL
             0.014544
     WTRG
             0.012803
     dtype: float64
[27]: table = pd.DataFrame()
      table['Returns'] = rets.mean()
      table['Risk'] = rets.std()
      table.sort_values(by='Returns')
[27]:
            Returns
                          Risk
      AQN -0.000522 0.013730
      AWR
            0.000645 0.011456
      WTRG 0.000653 0.012803
      AWK
            0.000833 0.013953
      CWT
            0.000939 0.013260
      YORW 0.001073 0.016962
      XYL
            0.001323 0.014544
      GWRS 0.001699 0.024254
```

```
[28]: table.sort_values(by='Risk')
[28]:
            Returns
                         Risk
      AWR
            0.000645 0.011456
      WTRG 0.000653 0.012803
      CWT
            0.000939
                     0.013260
      AQN -0.000522 0.013730
      AWK
            0.000833 0.013953
      XYL
           0.001323 0.014544
      YORW 0.001073 0.016962
      GWRS 0.001699 0.024254
[29]: rf = 0.001
      table['Sharpe Ratio'] = (table['Returns'] - rf) / table['Risk']
      table
[29]:
            Returns
                         Risk Sharpe Ratio
      AQN
         -0.000522 0.013730
                                   -0.110819
      AWK
            0.000833 0.013953
                                   -0.011943
      AWR
           0.000645 0.011456
                                   -0.030960
      CWT
           0.000939 0.013260
                                   -0.004572
      GWRS 0.001699 0.024254
                                   0.028803
      YORW 0.001073 0.016962
                                   0.004315
      XYL
            0.001323 0.014544
                                    0.022207
      WTRG 0.000653 0.012803
                                   -0.027123
[30]: table['Max Returns'] = rets.max()
[31]: table['Min Returns'] = rets.min()
[32]: table['Median Returns'] = rets.median()
[33]: total_return = stock_rets[-1:].transpose()
      table['Total Return'] = 100 * total_return
      table
[33]:
            Returns
                         Risk Sharpe Ratio Max Returns Min Returns \
      AQN
         -0.000522 0.013730
                                   -0.110819
                                                 0.039449
                                                             -0.059561
      AWK
           0.000833 0.013953
                                   -0.011943
                                                 0.031881
                                                             -0.053781
      AWR
            0.000645 0.011456
                                   -0.030960
                                                 0.041789
                                                             -0.025766
      CWT
           0.000939 0.013260
                                                 0.060324
                                   -0.004572
                                                             -0.033240
      GWRS 0.001699 0.024254
                                                             -0.078992
                                   0.028803
                                                 0.107824
      YORW
           0.001073 0.016962
                                                 0.050174
                                                             -0.060257
                                    0.004315
      XYL
            0.001323 0.014544
                                   0.022207
                                                 0.045389
                                                             -0.039531
      WTRG 0.000653 0.012803
                                   -0.027123
                                                 0.027229
                                                             -0.031964
```

Median Returns Total Return

```
AWK
                  0.001728
                                2.353755
      AWR
                  0.000701
                                0.497387
      CWT
                  0.001505
                                0.309013
      GWRS
                  0.002117
                                1.606190
                               -1.458860
      YORW
                  0.000784
      XYL
                  0.000025
                               -1.342104
      WTRG
                  0.002074
                                1.456211
[34]: table['Average Return Days'] = (1 + total_return)**(1 / days) - 1
      table
[34]:
             Returns
                          Risk
                                Sharpe Ratio Max Returns Min Returns
      AQN -0.000522 0.013730
                                   -0.110819
                                                  0.039449
                                                              -0.059561
      AWK
            0.000833 0.013953
                                   -0.011943
                                                  0.031881
                                                              -0.053781
      AWR
            0.000645 0.011456
                                   -0.030960
                                                              -0.025766
                                                  0.041789
      CWT
            0.000939 0.013260
                                   -0.004572
                                                  0.060324
                                                              -0.033240
      GWRS
           0.001699 0.024254
                                    0.028803
                                                  0.107824
                                                              -0.078992
      YORW
           0.001073 0.016962
                                    0.004315
                                                  0.050174
                                                              -0.060257
      XYL
            0.001323
                      0.014544
                                    0.022207
                                                  0.045389
                                                              -0.039531
      WTRG
           0.000653 0.012803
                                   -0.027123
                                                  0.027229
                                                              -0.031964
            Median Returns
                            Total Return Average Return Days
      AQN
                  0.000896
                               -5.956112
                                                     -0.000374
      AWK
                  0.001728
                                2.353755
                                                      0.000142
      AWR
                  0.000701
                                0.497387
                                                      0.000030
      CWT
                  0.001505
                                0.309013
                                                      0.000019
      GWRS
                  0.002117
                                1.606190
                                                      0.000097
      YORW
                  0.000784
                               -1.458860
                                                     -0.000090
      XYL
                  0.000025
                               -1.342104
                                                     -0.000082
      WTRG
                  0.002074
                                1.456211
                                                      0.000088
[35]: initial_value = df.iloc[0]
      ending_value = df.iloc[-1]
      table['CAGR'] = ((ending_value / initial_value) ** (252.0 / days)) -1
[35]:
                                Sharpe Ratio Max Returns Min Returns \
             Returns
                          Risk
      AQN -0.000522 0.013730
                                   -0.110819
                                                  0.039449
                                                              -0.059561
            0.000833 0.013953
      AWK
                                   -0.011943
                                                  0.031881
                                                              -0.053781
      AWR
            0.000645 0.011456
                                   -0.030960
                                                  0.041789
                                                              -0.025766
      CWT
            0.000939 0.013260
                                   -0.004572
                                                  0.060324
                                                              -0.033240
      GWRS
           0.001699 0.024254
                                    0.028803
                                                  0.107824
                                                              -0.078992
      YORW 0.001073 0.016962
                                    0.004315
                                                  0.050174
                                                              -0.060257
      XYL
            0.001323
                      0.014544
                                    0.022207
                                                  0.045389
                                                              -0.039531
      WTRG 0.000653 0.012803
                                   -0.027123
                                                  0.027229
                                                              -0.031964
```

AQN

0.000896

-5.956112

```
Median Returns
                             Total Return
                                           Average Return Days
                                                      -0.000374 -0.102327
      AQN
                  0.000896
                                -5.956112
      AWK
                  0.001728
                                 2.353755
                                                       0.000142
                                                                 0.137616
      AWR
                  0.000701
                                 0.497387
                                                       0.000030 0.106977
      CWT
                  0.001505
                                                       0.000019 0.161045
                                 0.309013
                                 1.606190
      GWRS
                  0.002117
                                                       0.000097
                                                                 0.279804
      YORW
                  0.000784
                                -1.458860
                                                      -0.000090 0.176988
      XYL
                  0.000025
                                -1.342104
                                                      -0.000082
                                                                 0.237805
      WTRG
                                                       0.000088 0.105211
                  0.002074
                                 1.456211
      table.sort values(by='Average Return Days')
[36]:
[36]:
             Returns
                           Risk
                                 Sharpe Ratio
                                               Max Returns
                                                             Min Returns
          -0.000522
                      0.013730
                                    -0.110819
                                                   0.039449
                                                               -0.059561
      AQN
      YORW
            0.001073
                      0.016962
                                     0.004315
                                                   0.050174
                                                               -0.060257
      XYL
            0.001323
                      0.014544
                                     0.022207
                                                   0.045389
                                                               -0.039531
      CWT
            0.000939
                      0.013260
                                                   0.060324
                                                               -0.033240
                                    -0.004572
      AWR
            0.000645
                      0.011456
                                    -0.030960
                                                   0.041789
                                                               -0.025766
      WTRG
            0.000653
                      0.012803
                                    -0.027123
                                                               -0.031964
                                                   0.027229
      GWRS
            0.001699
                      0.024254
                                     0.028803
                                                   0.107824
                                                               -0.078992
      AWK
            0.000833
                      0.013953
                                    -0.011943
                                                   0.031881
                                                               -0.053781
            Median Returns
                             Total Return
                                           Average Return Days
                                                                      CAGR
      AQN
                  0.000896
                                                      -0.000374 -0.102327
                                -5.956112
      YORW
                  0.000784
                                -1.458860
                                                      -0.000090 0.176988
      XYL
                  0.000025
                                -1.342104
                                                      -0.000082
                                                                 0.237805
      CWT
                  0.001505
                                 0.309013
                                                       0.000019
                                                                 0.161045
      AWR
                  0.000701
                                 0.497387
                                                       0.000030
                                                                 0.106977
      WTRG
                  0.002074
                                                       0.000088
                                 1.456211
                                                                 0.105211
      GWRS
                  0.002117
                                 1.606190
                                                       0.000097
                                                                 0.279804
      AWK
                  0.001728
                                 2.353755
                                                       0.000142
                                                                 0.137616
[37]: table['var_99'] = round((rets).quantile(0.01), 3)
      table['var_95'] = round((rets).quantile(0.05), 3)
[38]:
     table.sort_values(by='Returns')
[38]:
             Returns
                           Risk
                                 Sharpe Ratio
                                               Max Returns
                                                             Min Returns
          -0.000522 0.013730
                                    -0.110819
                                                   0.039449
                                                               -0.059561
      AQN
      AWR
            0.000645
                      0.011456
                                    -0.030960
                                                   0.041789
                                                               -0.025766
      WTRG
            0.000653
                      0.012803
                                    -0.027123
                                                   0.027229
                                                               -0.031964
      AWK
            0.000833
                      0.013953
                                    -0.011943
                                                   0.031881
                                                               -0.053781
      CWT
            0.000939
                      0.013260
                                    -0.004572
                                                   0.060324
                                                               -0.033240
      YORW
            0.001073
                      0.016962
                                     0.004315
                                                   0.050174
                                                               -0.060257
      XYL
            0.001323
                      0.014544
                                     0.022207
                                                   0.045389
                                                               -0.039531
      GWRS
            0.001699 0.024254
                                     0.028803
                                                   0.107824
                                                               -0.078992
```

CAGR

```
Median Returns
                             Total Return
                                           Average Return Days
                                                                      CAGR
                                                                            var_99 \
      AQN
                  0.000896
                                                      -0.000374 -0.102327
                                                                            -0.045
                                -5.956112
      AWR
                  0.000701
                                 0.497387
                                                       0.000030
                                                                 0.106977
                                                                            -0.025
                                                                            -0.029
      WTRG
                  0.002074
                                 1.456211
                                                       0.000088
                                                                 0.105211
      AWK
                  0.001728
                                 2.353755
                                                       0.000142 0.137616
                                                                            -0.031
      CWT
                  0.001505
                                 0.309013
                                                       0.000019
                                                                 0.161045
                                                                            -0.025
      YORW
                  0.000784
                                                                            -0.041
                                -1.458860
                                                      -0.000090 0.176988
      XYL
                  0.000025
                                -1.342104
                                                      -0.000082
                                                                 0.237805
                                                                            -0.026
                                                       0.000097 0.279804
      GWRS
                  0.002117
                                 1.606190
                                                                            -0.046
            var 95
      AQN
            -0.023
      AWR
            -0.021
      WTRG
            -0.025
            -0.023
      AWK
      CWT
            -0.021
      YORW
            -0.021
      XYL
            -0.021
      GWRS
            -0.034
[39]: # Pure Profit Score
      df = df.dropna()
      t = np.arange(0, df.shape[0]).reshape(-1, 1)
      regression = LinearRegression().fit(t, df)
      r_squared = regression.score(t, df)
      table['PPS'] = table['CAGR'] * r squared
[40]:
     table
[40]:
             Returns
                           Risk
                                 Sharpe Ratio
                                               Max Returns
                                                            Min Returns
      AQN
          -0.000522
                      0.013730
                                    -0.110819
                                                   0.039449
                                                               -0.059561
      AWK
            0.000833
                      0.013953
                                    -0.011943
                                                               -0.053781
                                                   0.031881
      AWR
            0.000645
                      0.011456
                                    -0.030960
                                                               -0.025766
                                                   0.041789
      CWT
            0.000939
                      0.013260
                                    -0.004572
                                                   0.060324
                                                               -0.033240
      GWRS
            0.001699
                      0.024254
                                     0.028803
                                                   0.107824
                                                               -0.078992
      YORW
            0.001073
                      0.016962
                                     0.004315
                                                   0.050174
                                                               -0.060257
      XYL
            0.001323
                      0.014544
                                     0.022207
                                                   0.045389
                                                               -0.039531
      WTRG
            0.000653
                      0.012803
                                    -0.027123
                                                   0.027229
                                                               -0.031964
            Median Returns
                                           Average Return Days
                                                                            var_99
                             Total Return
                                                                      CAGR
      AQN
                  0.000896
                                -5.956112
                                                      -0.000374 -0.102327
                                                                            -0.045
      AWK
                  0.001728
                                 2.353755
                                                       0.000142 0.137616
                                                                            -0.031
      AWR
                  0.000701
                                 0.497387
                                                       0.000030 0.106977
                                                                            -0.025
      CWT
                  0.001505
                                 0.309013
                                                       0.000019 0.161045
                                                                            -0.025
      GWRS
                  0.002117
                                 1.606190
                                                       0.000097
                                                                 0.279804
                                                                            -0.046
      YORW
                                                                            -0.041
                  0.000784
                                -1.458860
                                                      -0.000090 0.176988
      XYL
                  0.000025
                                -1.342104
                                                      -0.000082 0.237805
                                                                            -0.026
```

WTRG	0.002074		1.456211	0.000088	0.105211	-0.029
	var_95	PPS				
AQN	-0.023	-0.027934				
AWK	-0.023	0.037567				
AWR	-0.021	0.029203				
CWT	-0.021	0.043963				
GWRS	-0.034	0.076382				
YORW	-0.021	0.048315				
XYL	-0.021	0.064917				
WTRG	-0.025	0.028721				