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# Understanding the Effect of Bias in Deep Anomaly Detection

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CHICAGO

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(An illustrative example of Pokémon.)

Normal



Abnormal



Known types in source distribution



Unknown types in target distribution



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→ Challenging to get a *representative anomaly set*.

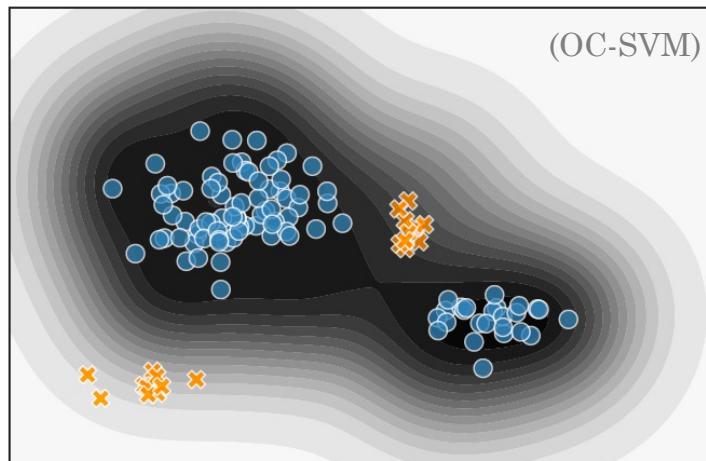
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## Semi-Supervised (AD)

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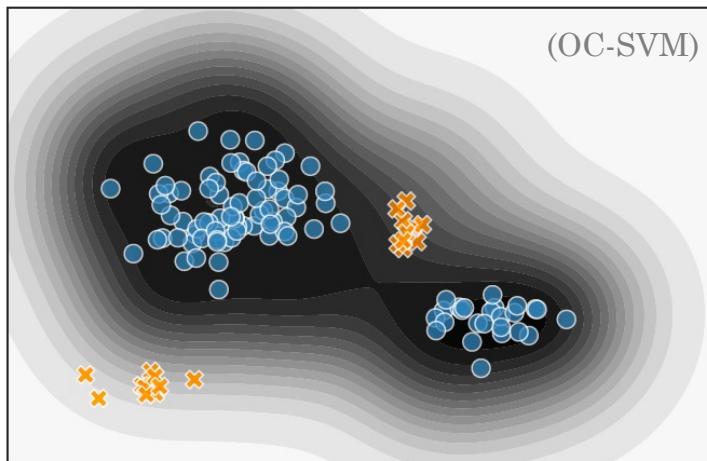


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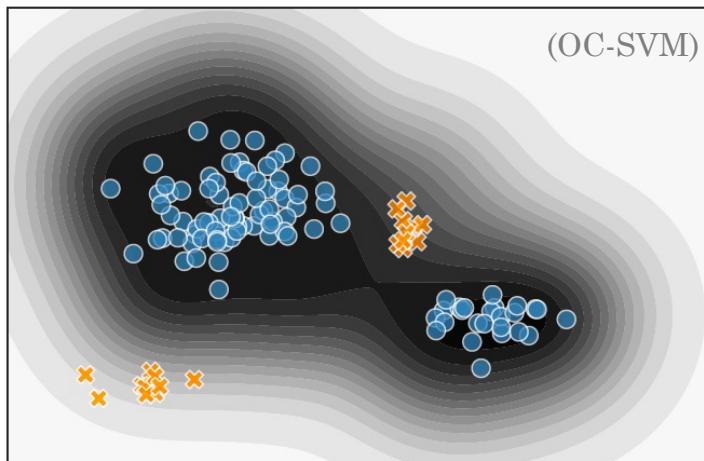
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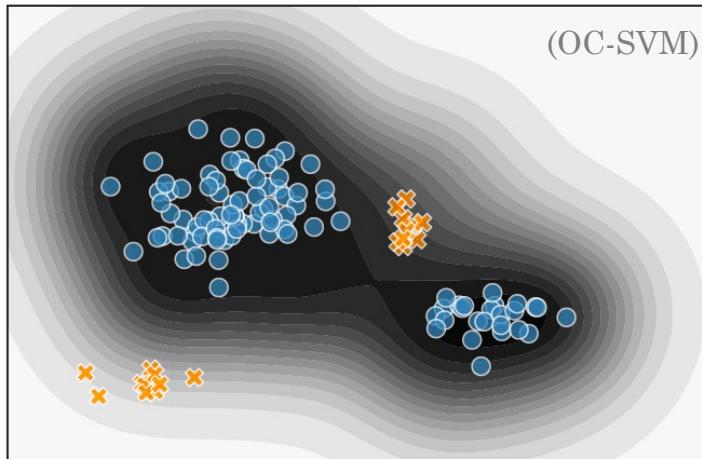
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Can we make use of *additional labeled anomalies*?

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# Existing Approaches for AD

Low

High

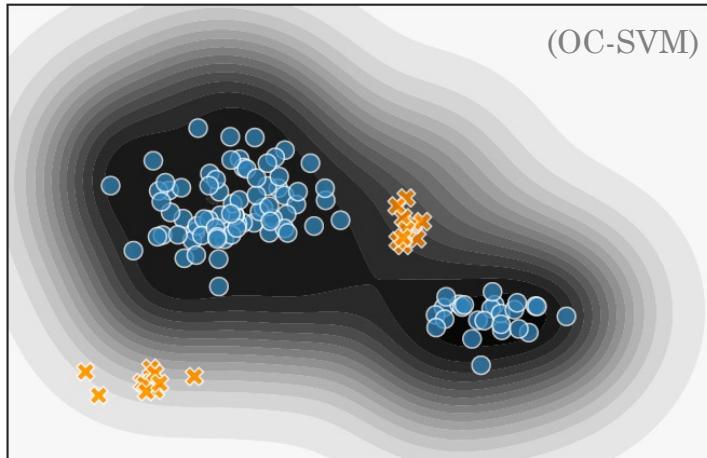
Anomaly Score

Normal Data

Abnormal Data

## Semi-Supervised (AD)

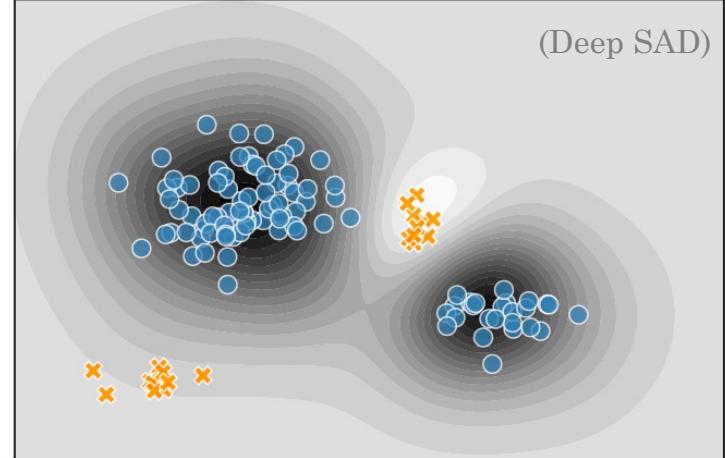
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Train with *additional labeled anomalies*

## Supervised (AD)

[Pan+19], [Yam+19], [Hen+19], [Ruf+20], [Goy+20], ...



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Discriminating on *known anomalies*.

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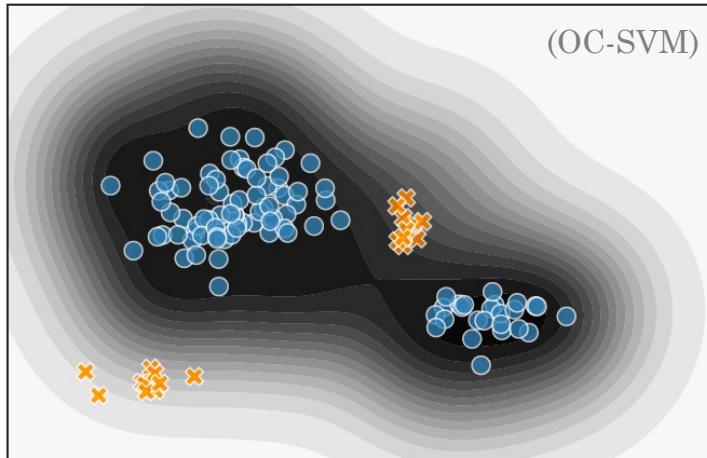
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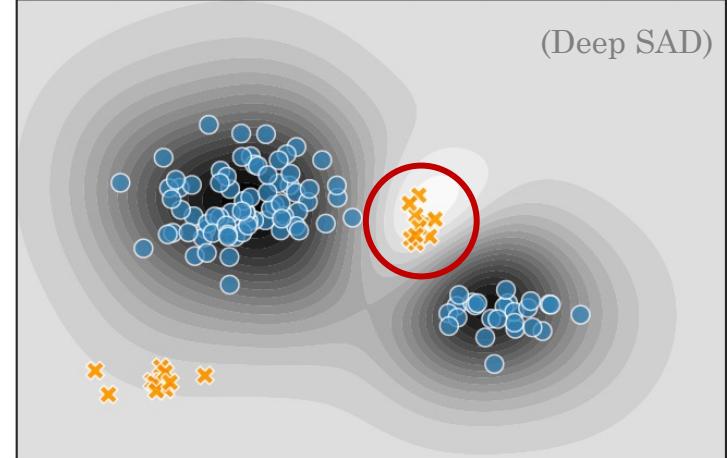
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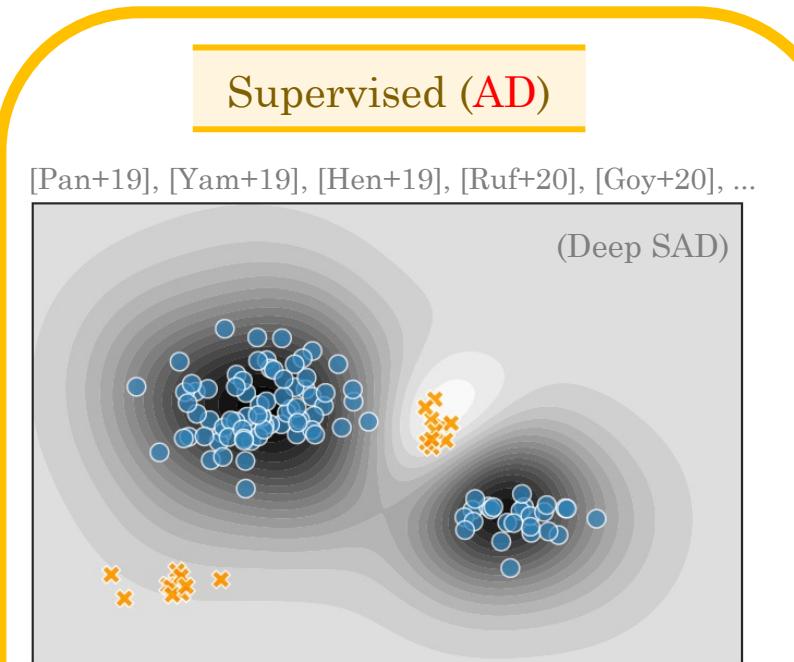
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# Motivation



Will *additional labels* do *harm*?



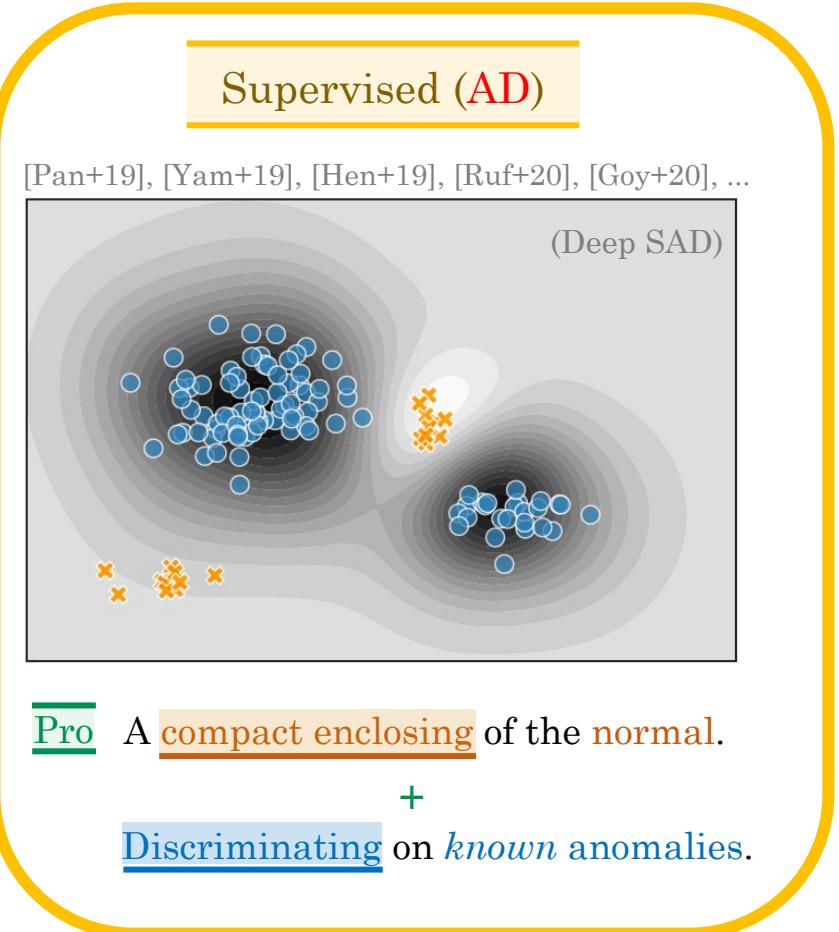
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# Motivation



Will *additional labels* do *harm*?

Can **unseen anomalies** suffer from **bias\***?



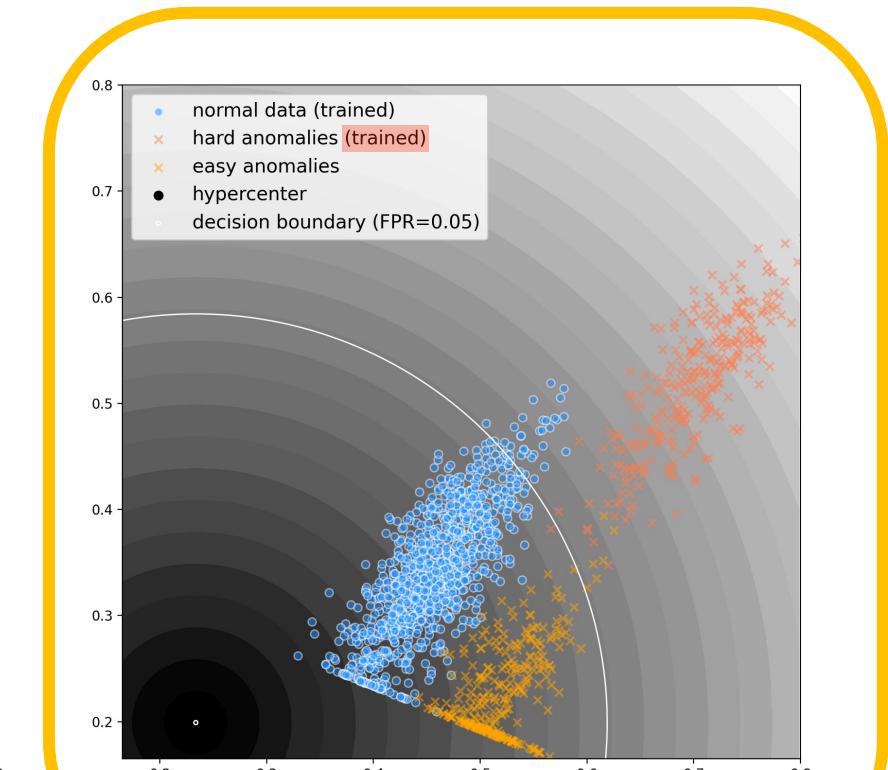
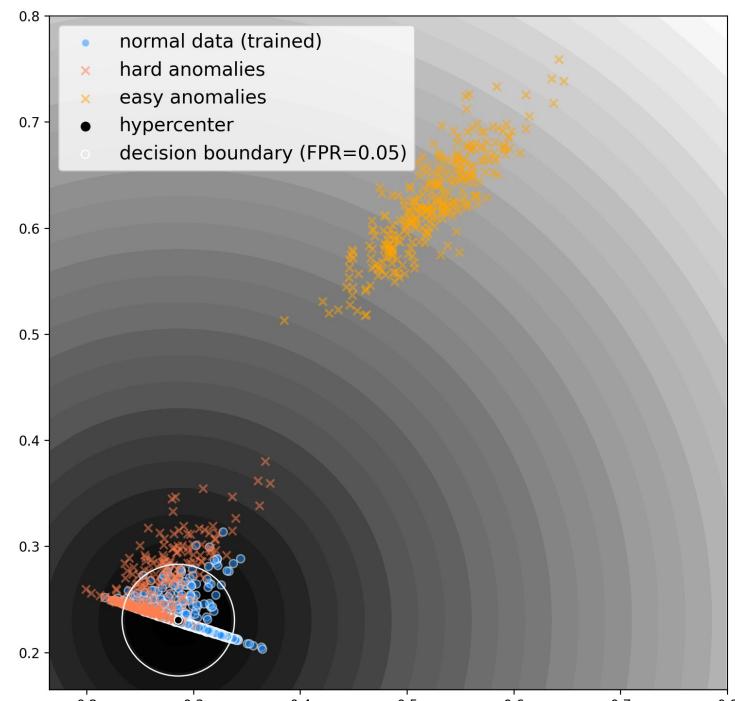
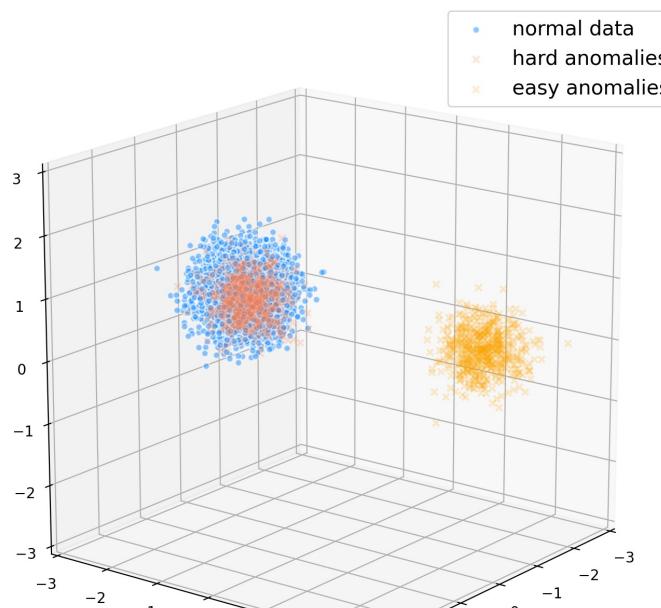
\* Note that such bias is novel compared to the aforementioned in literature (c.f. Section 2 of our paper).

## A Counter-Intuitive Example

Training with *additional labeled anomalies* can bring *disastrous harmful bias.*

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# Our Contributions

1

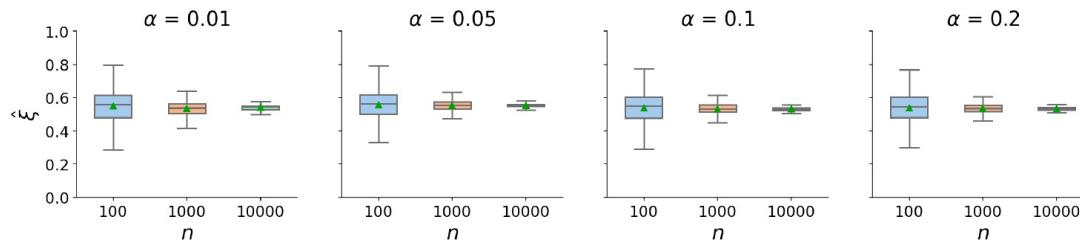
## Define Bias: A formal ERM Framework

$$\text{bias}(\hat{s}_\theta, \hat{\tau}_\theta) := \arg \max_{(s_\theta, \tau_\theta): \theta \in \Theta} \text{TPR}(s_\theta, \tau_\theta) - \text{TPR}(\hat{s}_\theta, \hat{\tau}_\theta)$$

2

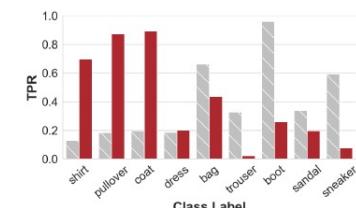
## Estimate Bias: The First PAC Analysis

$$n \geq \frac{8}{\epsilon^2} \cdot \left( \log \frac{2}{1-\sqrt{1-\delta}} \cdot \left( \frac{2-\alpha}{\alpha} \right)^2 + \log \frac{2}{\delta} \cdot \frac{1}{1-\alpha} \left( \left( \frac{\ell_a}{\ell_0^-} \right)^2 + \left( \frac{\ell'_a}{\ell_0'} \right)^2 \right) \right)$$

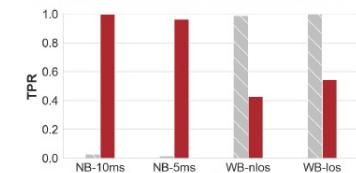


3

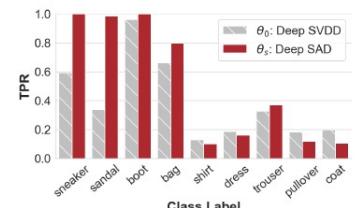
## Characterize Bias: Empirical Experiments



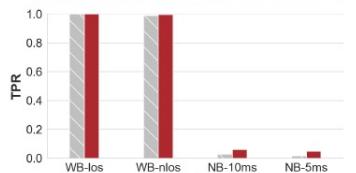
(a) Fashion-MNIST: Scenario 1



(c) Spectrum Misuse: Scenario 1



(b) Fashion-MNIST: Scenario 2



(d) Spectrum Misuse: Scenario 2

[Clarification] Bias in  $AD \neq$  Bias in *Supervised Learning*

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Problem formulation is different.

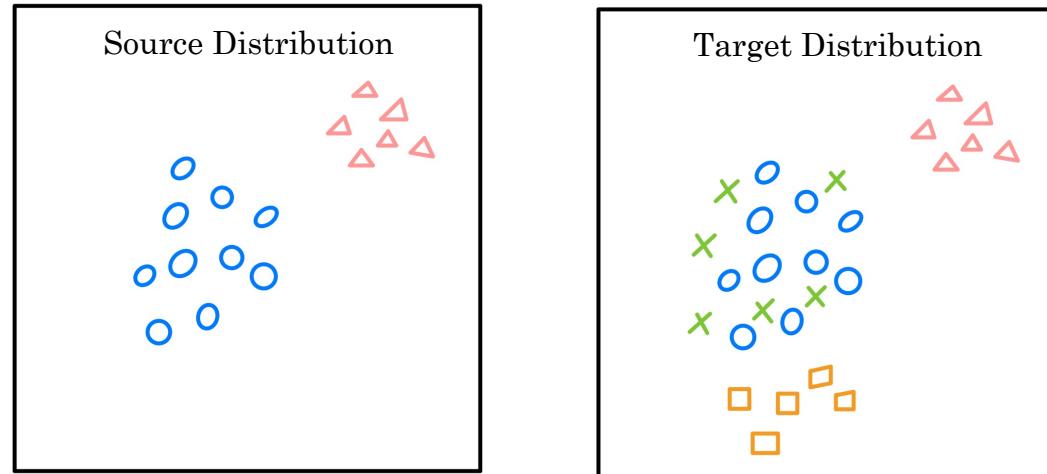


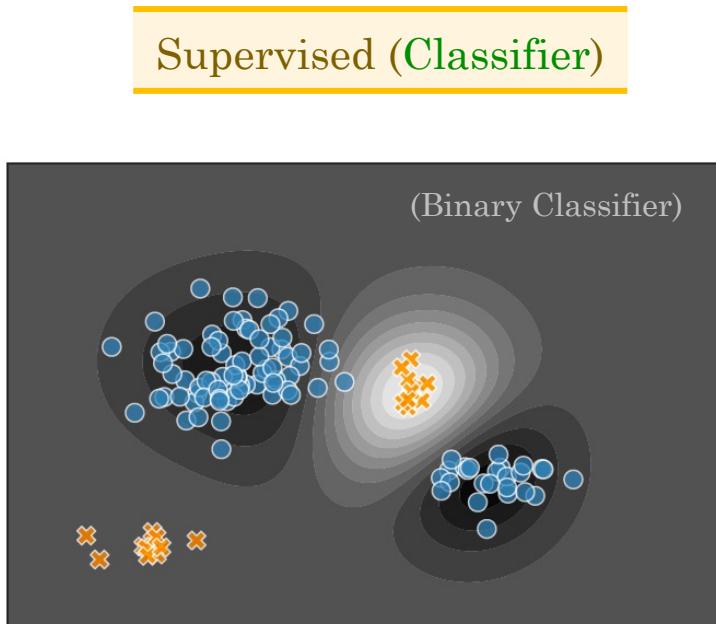
Fig 1. Data distribution of AD problem. The blue represent the normal data, and other different colors represent different subtypes of anomalies.

Task Type	Distribution Shift	Known Target Distribution	Known Target Label Set
Imbalanced Classification [Johnson and Khoshgoftaar, 2019]	No	N/A	N/A
Closed Set Domain Adaptation [Saenko <i>et al.</i> , 2010]	Yes	Yes	Yes
Open Set Domain Adaptation [Panareda Bustos and Gall, 2017]	Yes	Yes	No
Anomaly Detection [Chalapathy and Chawla, 2019]	Yes	No	No

Table 1: Comparison of anomaly detection tasks with other relevant classification tasks.

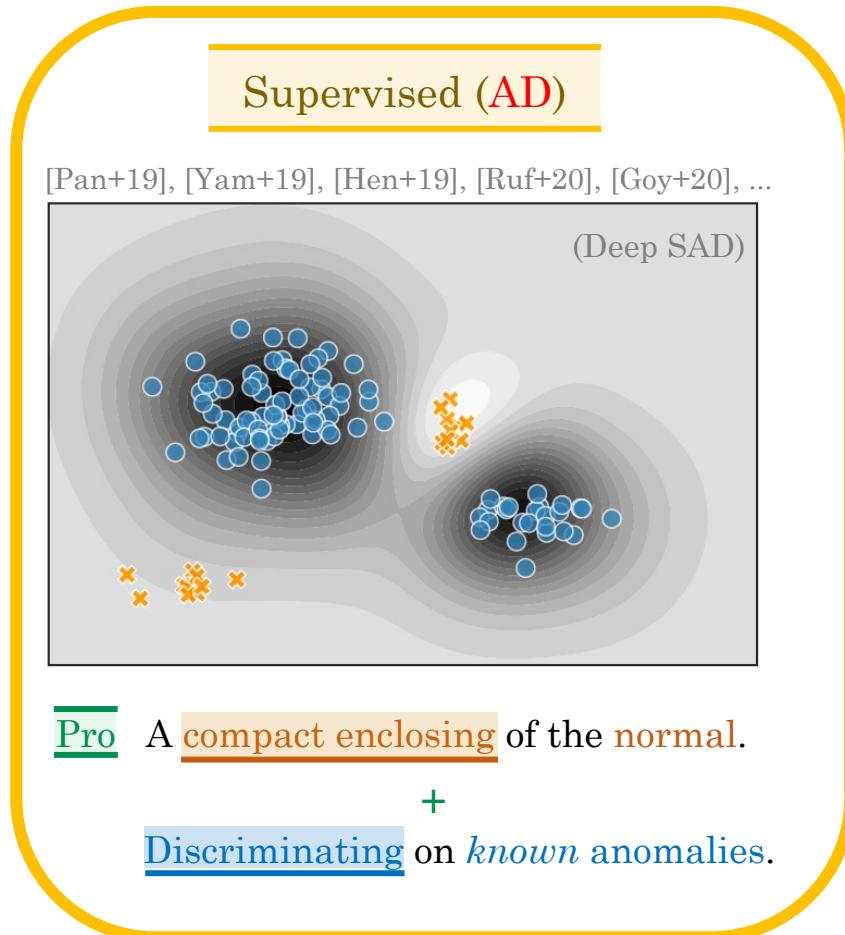
# [Clarification] Bias in *AD* ≠ Bias in *Supervised Learning*

- Training mechanism is different.



**Pro** Discriminating on *known* anomalies.

**Con** Overfitting to *known* anomalies.  
→ Overfitting bias.





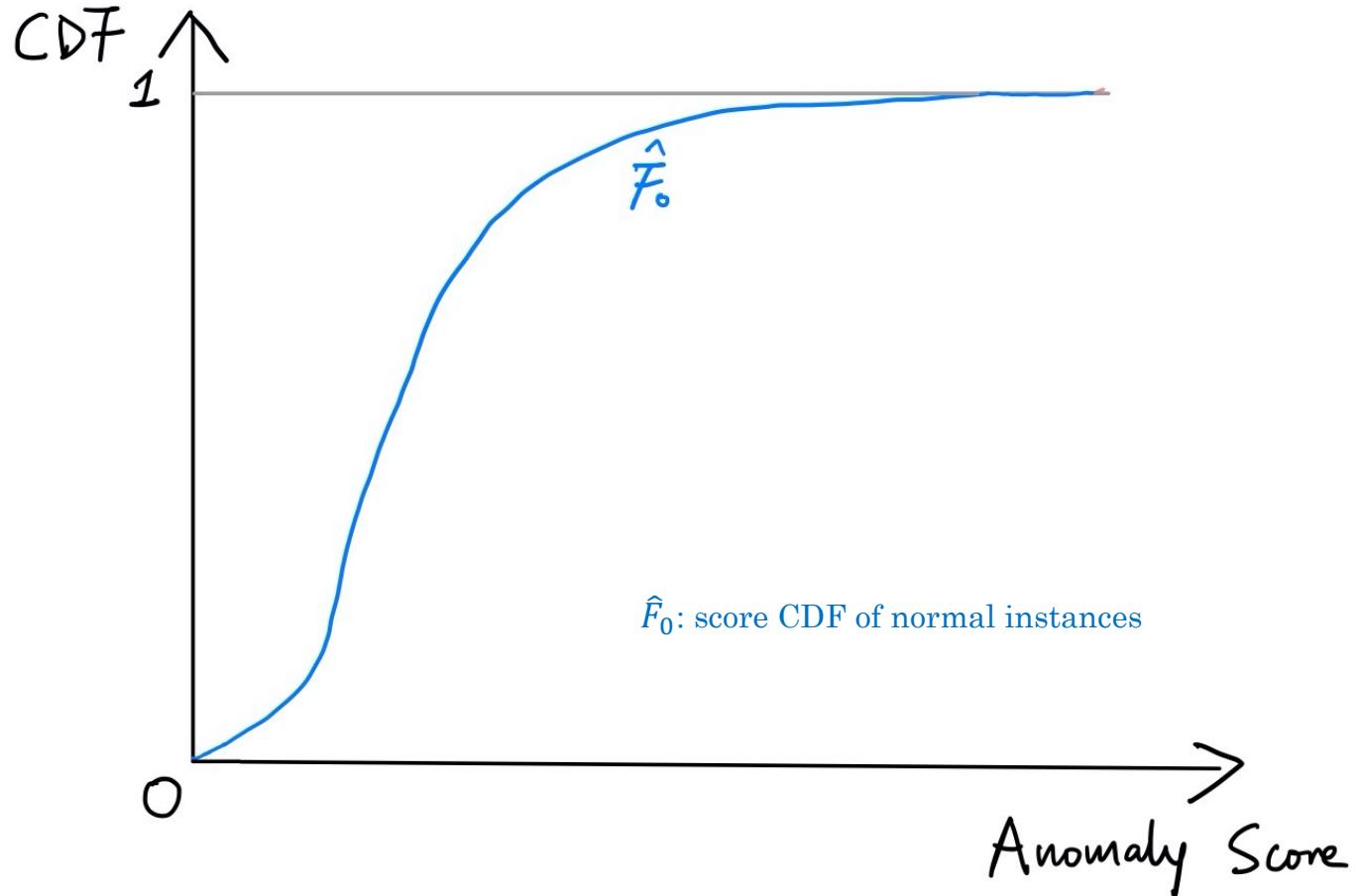
## How to *Define* Bias in AD?

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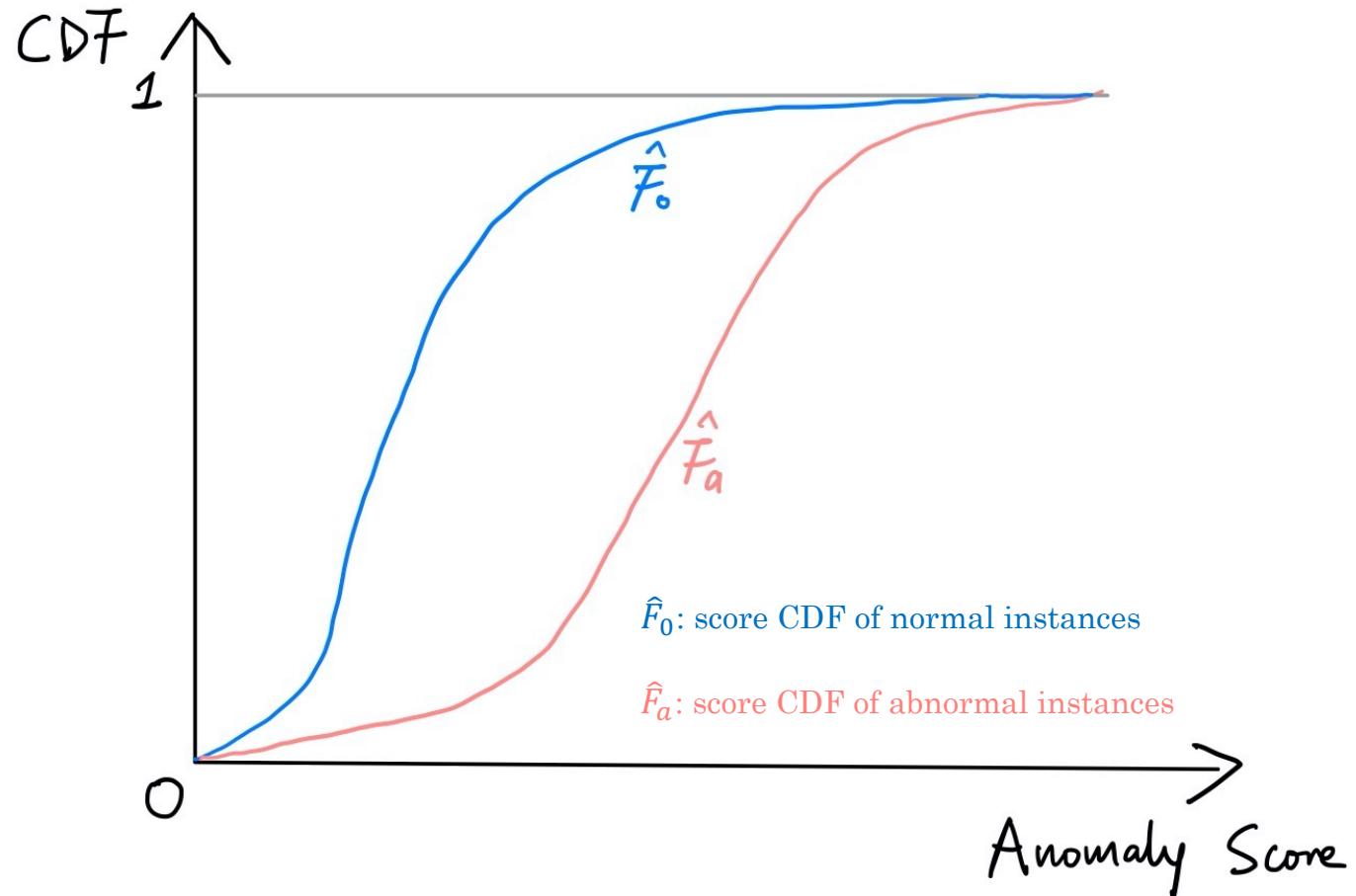
## A General AD Framework



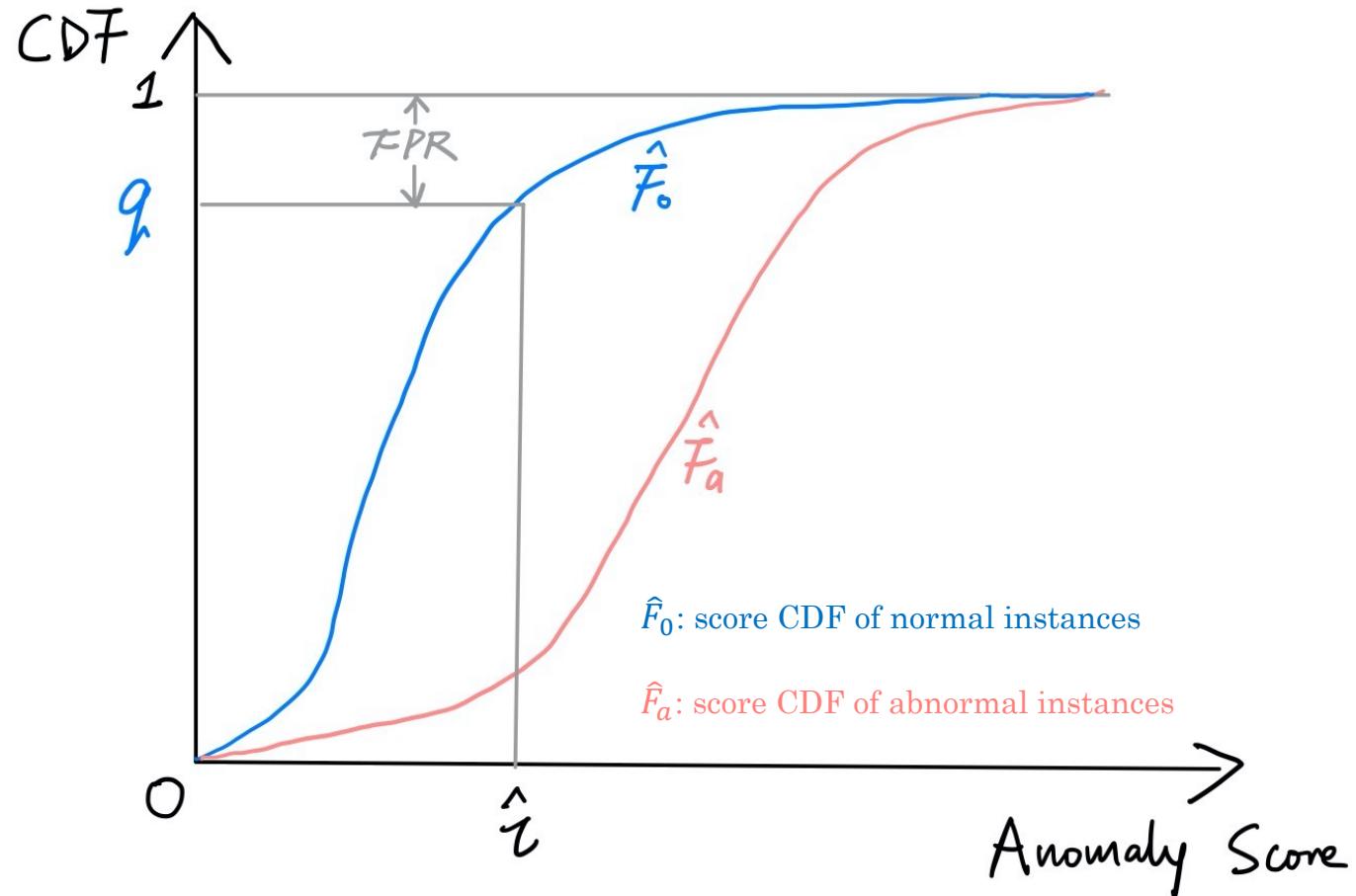
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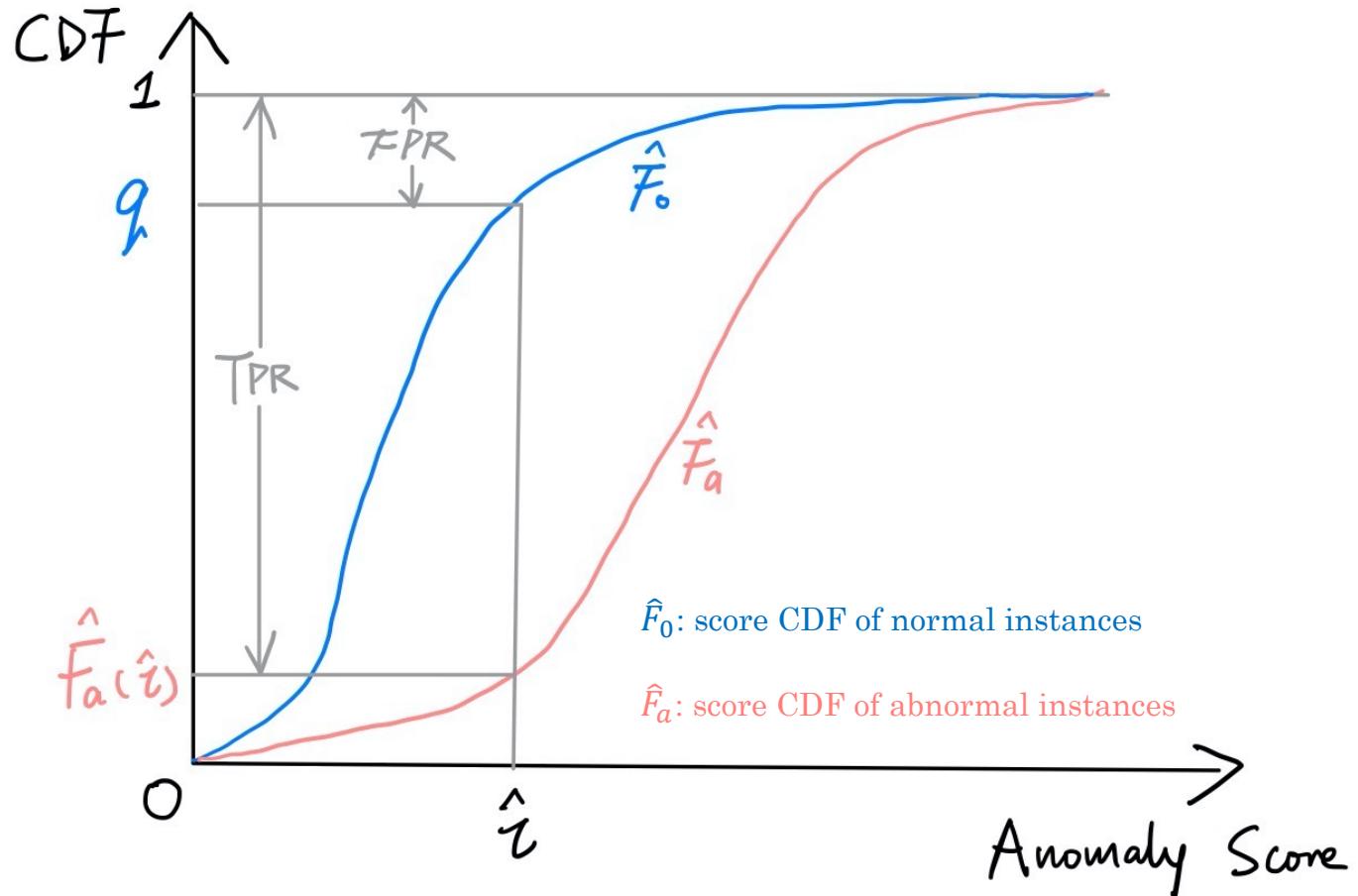
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# ERM-Style Scoring Bias

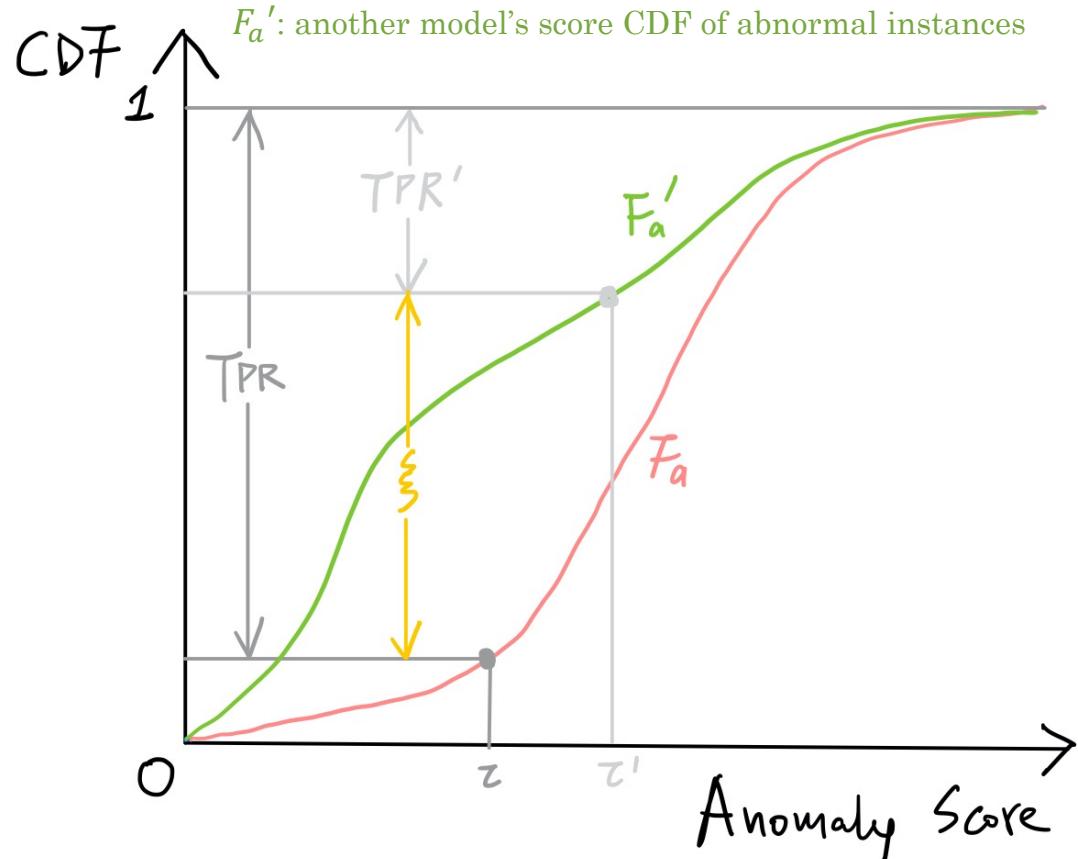
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## Scoring Bias

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# ERM-Style Scoring Bias

$F_a$ : one model's score CDF of abnormal instances



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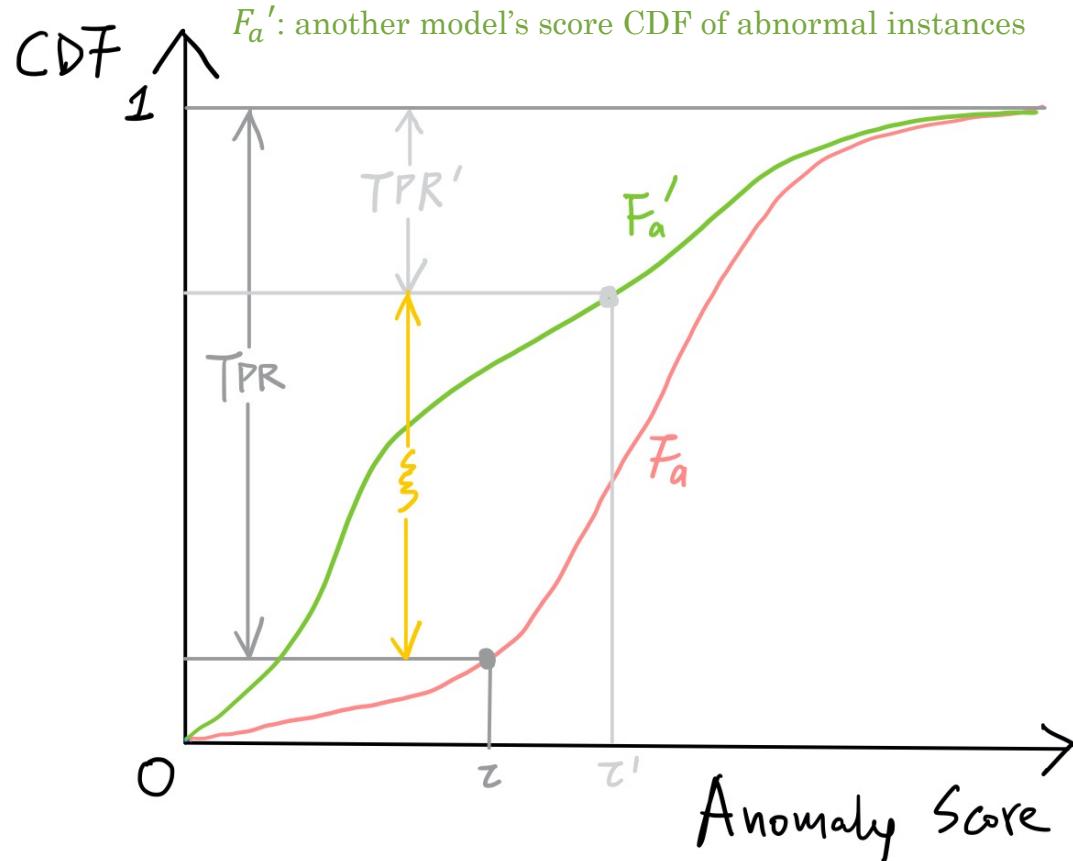
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## Relative Scoring Bias

$$\begin{aligned}\xi(s, s') &:= \text{bias}(s, \tau) - \text{bias}(s', \tau') \\ &= \text{TPR}(s', \tau') - \text{TPR}(s, \tau)\end{aligned}$$

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## 3 Empirical Relative Scoring Bias

$$\hat{\xi}(s, s') := \widehat{\text{TPR}}(s', \tau') - \widehat{\text{TPR}}(s, \tau)$$



## How to *Estimate* Bias in AD?

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# Finite Sample Guarantee

 **Goal:** a theoretical guarantee on model performance in terms of bias.

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**Theorem 3.** Assume that  $F_a, F'_a, F_0^-, F_0'^-$  are Lipschitz continuous with Lipschitz constant  $\ell_a, \ell'_a, \ell_0^-, \ell_0'^-$ , respectively. Let  $\alpha$  be the fraction of abnormal data from the mixture distribution. Then, w.p. at least  $1 - \delta$ , with

$$n = \mathcal{O}\left(\frac{1}{\alpha^2 \epsilon^2} \log \frac{1}{\delta}\right)$$

the empirical relative scoring bias satisfies  $|\hat{\xi} - \xi| \leq \epsilon$ .

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# Convergence of Scoring Bias: *Empirical Results*

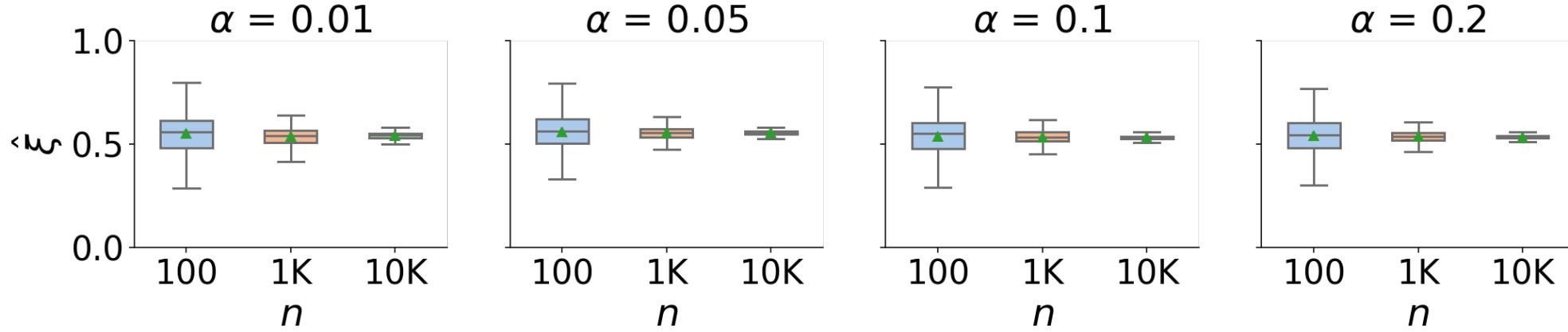


Fig 1.  $\hat{\xi}$  is the scoring bias of Deep SVDD relative to Deep SAD.

- The estimation error  $\epsilon$  decreases at the rate of  $\frac{1}{\sqrt{n}}$ .
- The sample complexity  $n$  grows as  $\mathcal{O}\left(\frac{1}{\alpha^2 \epsilon^2} \log \frac{1}{\delta}\right)$ .



## How does Bias *Impact* AD?

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# Recall on Our Observations...

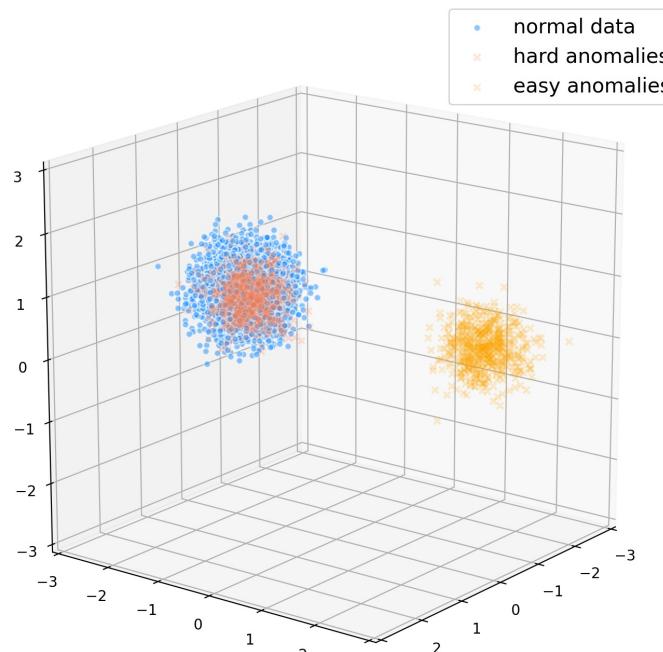


Fig 1. Original 3D Space

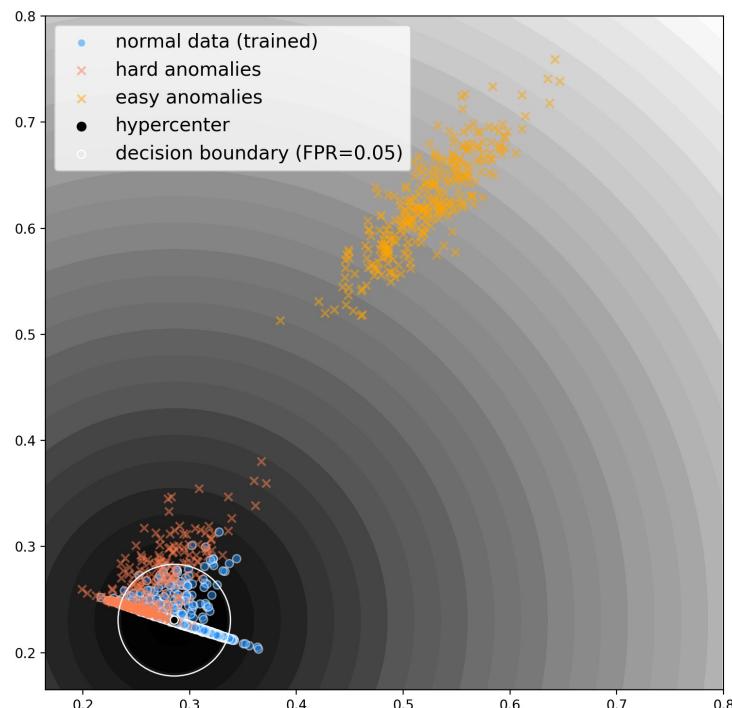


Fig 2. 2D Latent Space (*Semi-Supervised AD*)

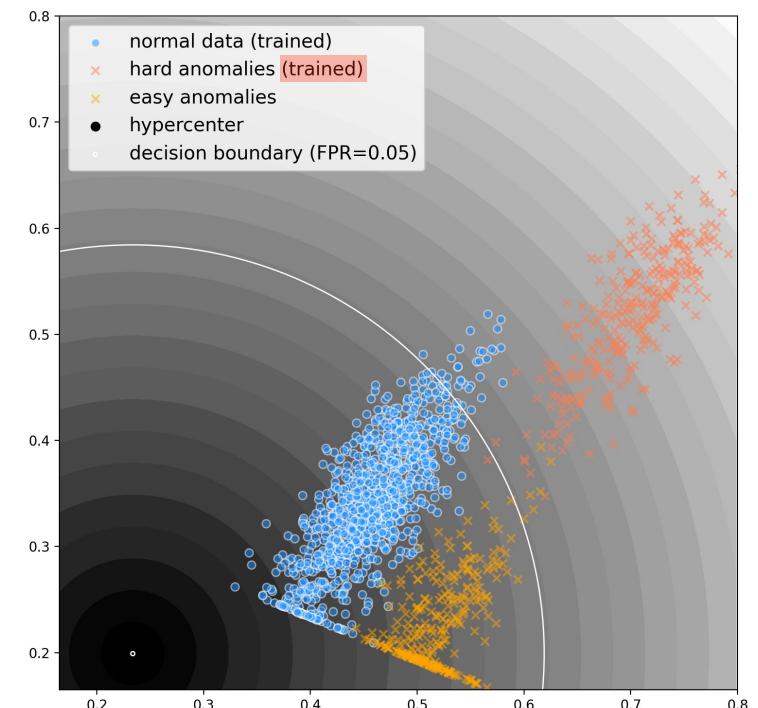


Fig 3. 2D Latent Space (*Supervised AD*)

# Recall on Our Observations...

Training with **different distributions** affects **normal enclosing unevenly**.

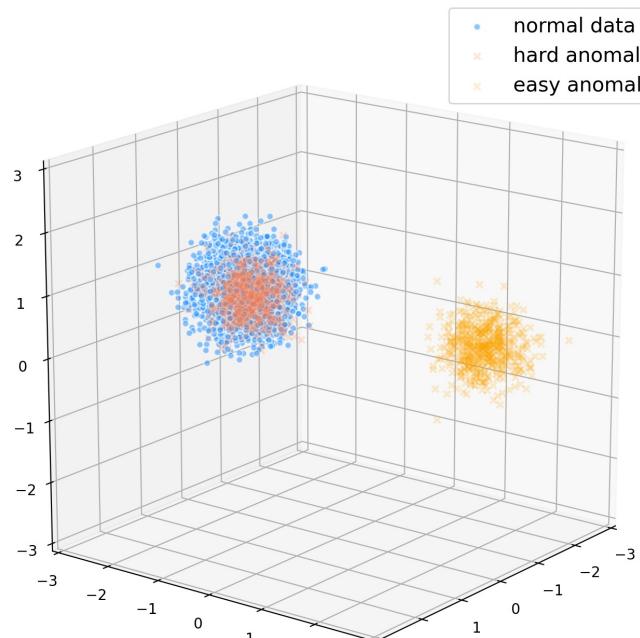


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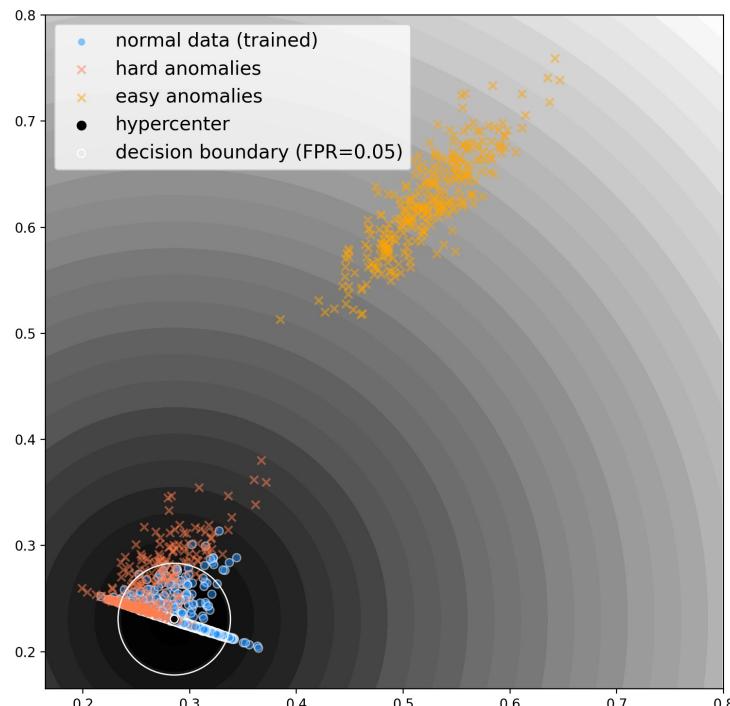


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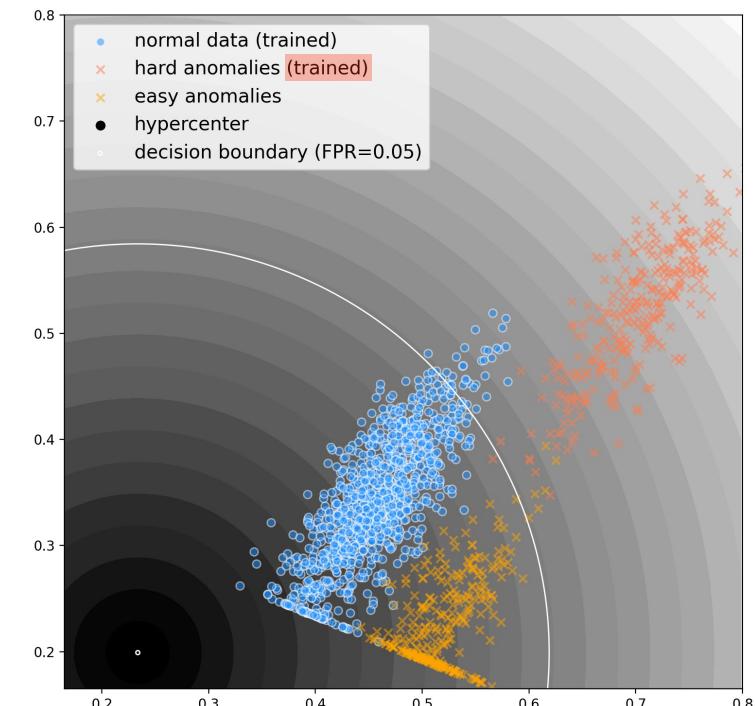


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# Our Hypothesis

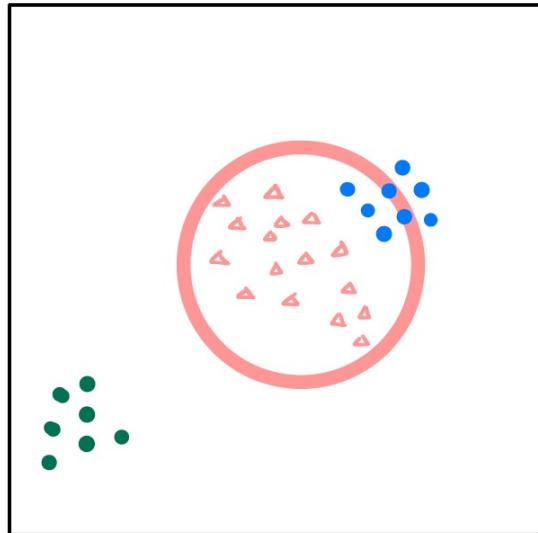
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$\Delta$  : normal data

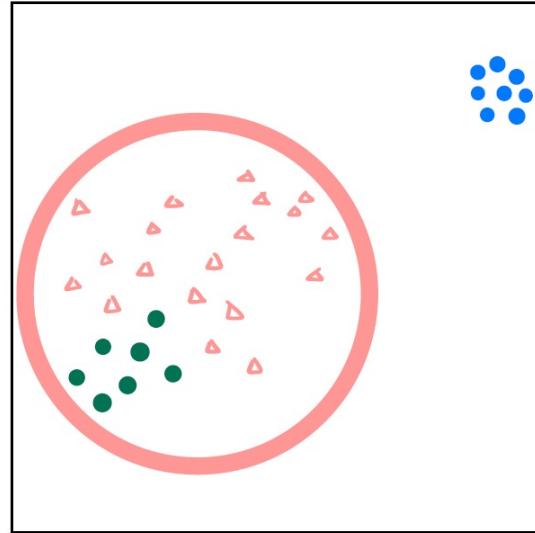
$\circ$  : anomaly type 1 (hard)

$\bullet$  : anomaly type 2 (easy)

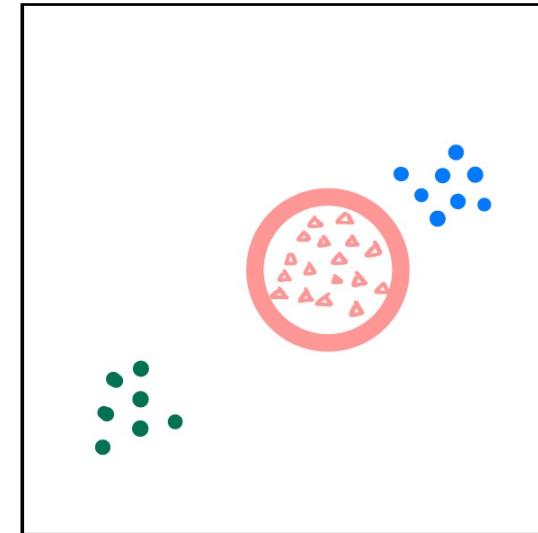
train with  $\Delta$



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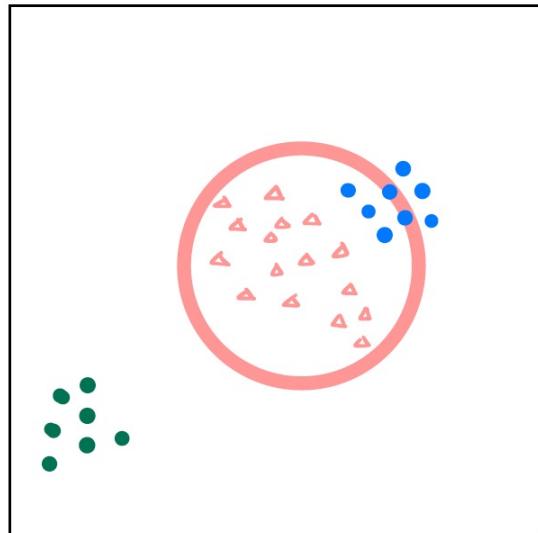
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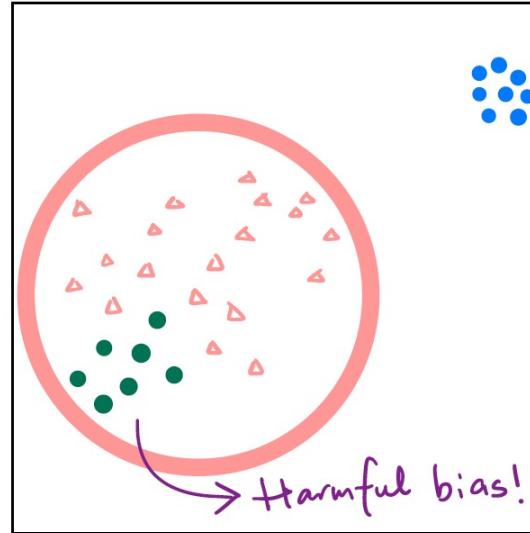
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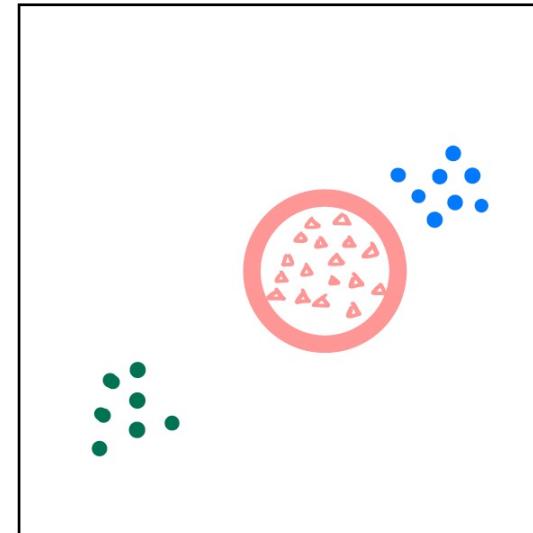
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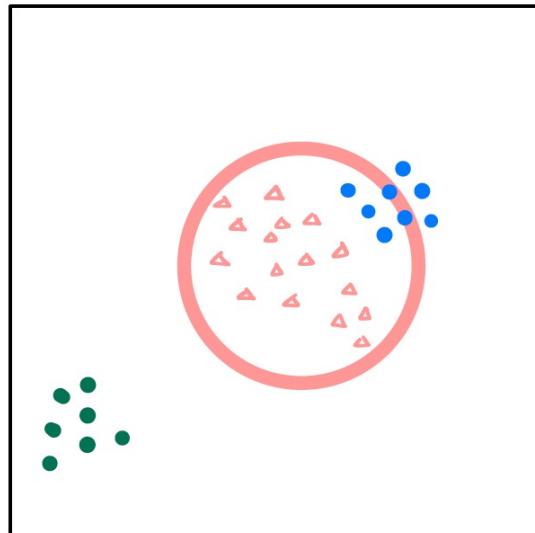
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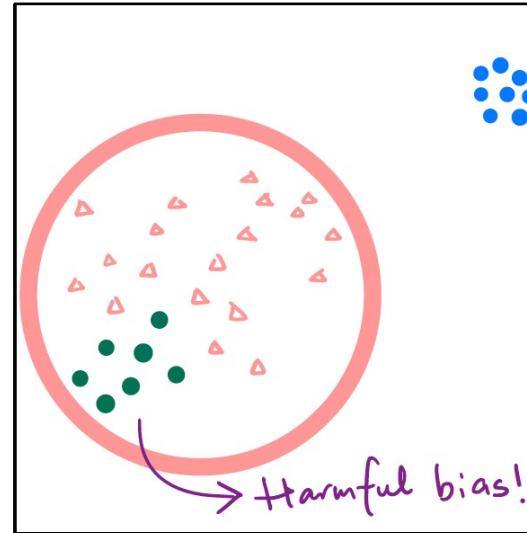
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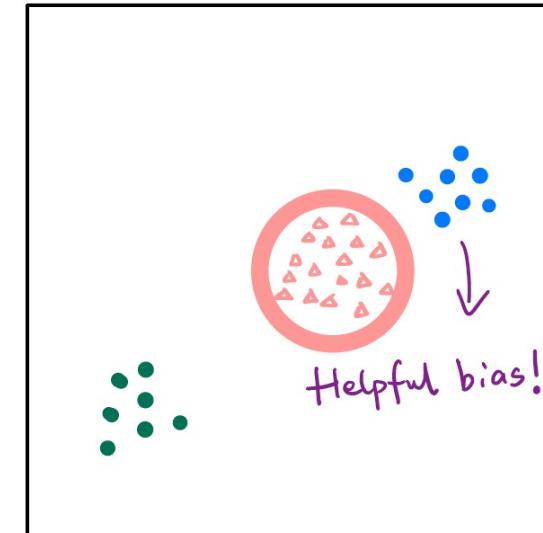
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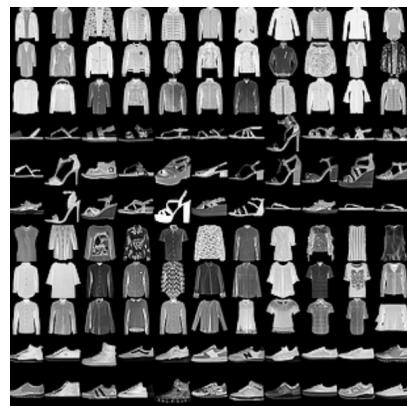


# Experiment Setup

## Models

Type	Semi-supervised (trained on normal data)	Supervised (trained on normal & some abnormal data)
Hypersphere-based	Deep SVDD [Ruff <i>et al.</i> , 2018]	Deep SAD [Ruff <i>et al.</i> , 2020b], Hypersphere Classifier (HSC) [Ruff <i>et al.</i> , 2020a]
Reconstruction-based	Autoencoder (AE) [Zhou and Paffenroth, 2017]	Supervised AE (SAE) <sup>1</sup> , Autoencoding Binary Classifier (ABC) [Yamanaka <i>et al.</i> , 2019]

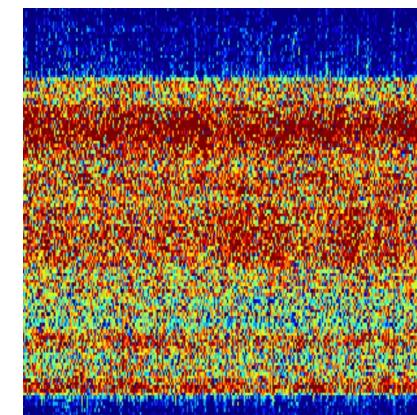
## Datasets



Fashion-MNIST

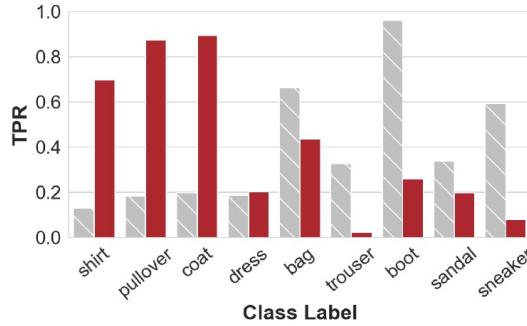


Landsat Satellite



Spectrum Misuse

# Scenario 1: Training w/ the *Hard* Anomalies



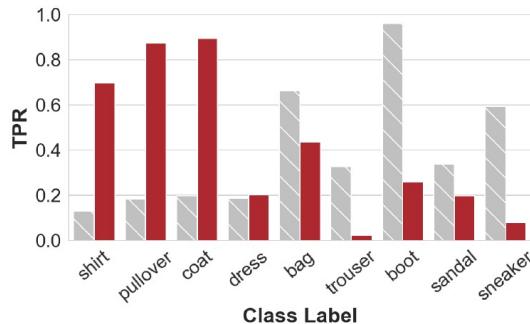
training normal = top, training abnormal = shirt

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	$0.09 \pm 0.01$	$0.71 \pm 0.01 \uparrow$	$0.70 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.72 \pm 0.01 \uparrow$	$0.72 \pm 0.01 \uparrow$	0
pullover	$0.13 \pm 0.02$	$0.90 \pm 0.01 \uparrow$	$0.89 \pm 0.01 \uparrow$	$0.19 \pm 0.02$	$0.84 \pm 0.02 \uparrow$	$0.85 \pm 0.01 \uparrow$	0.01
coat	$0.14 \pm 0.03$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	$0.15 \pm 0.02$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	0.01
dress	$0.17 \pm 0.03$	$0.24 \pm 0.03 \uparrow$	$0.24 \pm 0.03 \uparrow$	$0.11 \pm 0.01$	$0.20 \pm 0.03 \uparrow$	$0.21 \pm 0.03 \uparrow$	0.04
bag	$0.49 \pm 0.07$	$0.38 \pm 0.08 \downarrow$	$0.36 \pm 0.07 \downarrow$	$0.70 \pm 0.03$	$0.52 \pm 0.09 \downarrow$	$0.53 \pm 0.07 \downarrow$	0.04
trouser	$0.32 \pm 0.10$	$0.07 \pm 0.04 \downarrow$	$0.06 \pm 0.03 \downarrow$	$0.59 \pm 0.04$	$0.07 \pm 0.04 \downarrow$	$0.16 \pm 0.07 \downarrow$	0.06
boot	$0.92 \pm 0.03$	$0.29 \pm 0.15 \downarrow$	$0.27 \pm 0.16 \downarrow$	$0.98 \pm 0.02$	$0.90 \pm 0.09 \downarrow$	$0.90 \pm 0.08 \downarrow$	0.08
sandal	$0.30 \pm 0.04$	$0.26 \pm 0.08 \downarrow$	$0.26 \pm 0.12 \downarrow$	$0.82 \pm 0.02$	$0.46 \pm 0.10 \downarrow$	$0.56 \pm 0.09 \downarrow$	0.09
sneaker	$0.55 \pm 0.09$	$0.12 \pm 0.10 \downarrow$	$0.14 \pm 0.12 \downarrow$	$0.74 \pm 0.09$	$0.47 \pm 0.19 \downarrow$	$0.46 \pm 0.18 \downarrow$	0.10

Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class **top** is similar to the abnormal training class **shirt**. Their  $L^2$  distance = 0.02.



# Scenario 1: Training w/ the *Hard* Anomalies

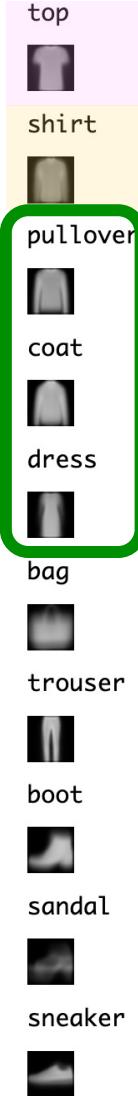


training normal = top, training abnormal = shirt

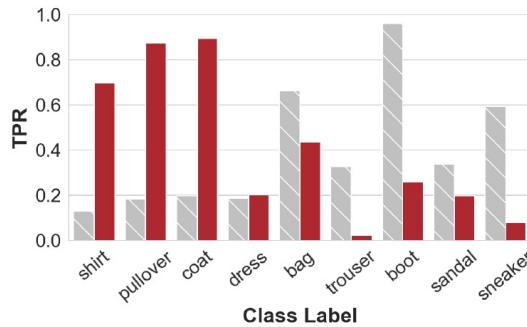
Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	$0.09 \pm 0.01$	$0.71 \pm 0.01 \uparrow$	$0.70 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.72 \pm 0.01 \uparrow$	$0.72 \pm 0.01 \uparrow$	0
pullover	$0.13 \pm 0.02$	$0.90 \pm 0.01 \uparrow$	$0.89 \pm 0.01 \uparrow$	$0.19 \pm 0.02$	$0.84 \pm 0.02 \uparrow$	$0.85 \pm 0.01 \uparrow$	0.01
coat	$0.14 \pm 0.03$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	$0.15 \pm 0.02$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	0.01
dress	$0.17 \pm 0.03$	$0.24 \pm 0.03 \uparrow$	$0.24 \pm 0.03 \uparrow$	$0.11 \pm 0.01$	$0.20 \pm 0.03 \uparrow$	$0.21 \pm 0.03 \uparrow$	0.04
bag	$0.49 \pm 0.07$	$0.38 \pm 0.08 \downarrow$	$0.36 \pm 0.07 \downarrow$	$0.70 \pm 0.03$	$0.52 \pm 0.09 \downarrow$	$0.53 \pm 0.07 \downarrow$	0.04
trouser	$0.32 \pm 0.10$	$0.07 \pm 0.04 \downarrow$	$0.06 \pm 0.03 \downarrow$	$0.59 \pm 0.04$	$0.07 \pm 0.04 \downarrow$	$0.16 \pm 0.07 \downarrow$	0.06
boot	$0.92 \pm 0.03$	$0.29 \pm 0.15 \downarrow$	$0.27 \pm 0.16 \downarrow$	$0.98 \pm 0.02$	$0.90 \pm 0.09 \downarrow$	$0.90 \pm 0.08 \downarrow$	0.08
sandal	$0.30 \pm 0.04$	$0.26 \pm 0.08 \downarrow$	$0.26 \pm 0.12 \downarrow$	$0.82 \pm 0.02$	$0.46 \pm 0.10 \downarrow$	$0.56 \pm 0.09 \downarrow$	0.09
sneaker	$0.55 \pm 0.09$	$0.12 \pm 0.10 \downarrow$	$0.14 \pm 0.12 \downarrow$	$0.74 \pm 0.09$	$0.47 \pm 0.19 \downarrow$	$0.46 \pm 0.18 \downarrow$	0.10

Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class **top** is similar to the abnormal training class **shirt**. Their  $L^2$  distance = 0.02.

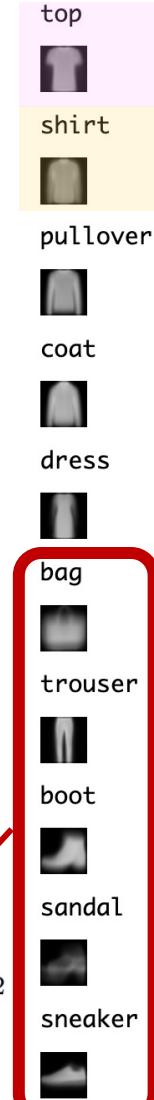
Positive bias!



# Scenario 1: Training w/ the *Hard* Anomalies



training normal = top, training abnormal = shirt

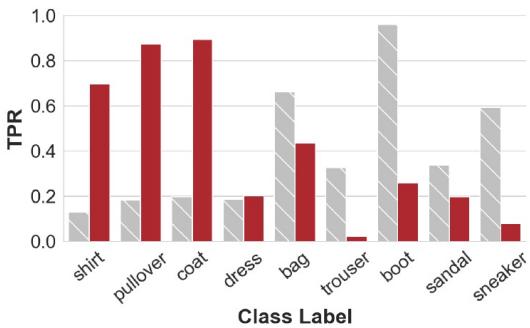


Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	$0.09 \pm 0.01$	$0.71 \pm 0.01 \uparrow$	$0.70 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.72 \pm 0.01 \uparrow$	$0.72 \pm 0.01 \uparrow$	0
pullover	$0.13 \pm 0.02$	$0.90 \pm 0.01 \uparrow$	$0.89 \pm 0.01 \uparrow$	$0.19 \pm 0.02$	$0.84 \pm 0.02 \uparrow$	$0.85 \pm 0.01 \uparrow$	0.01
coat	$0.14 \pm 0.03$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	$0.15 \pm 0.02$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	0.01
dress	$0.17 \pm 0.03$	$0.24 \pm 0.03 \uparrow$	$0.24 \pm 0.03 \uparrow$	$0.11 \pm 0.01$	$0.20 \pm 0.03 \uparrow$	$0.21 \pm 0.03 \uparrow$	0.04
bag	$0.49 \pm 0.07$	$0.38 \pm 0.08 \downarrow$	$0.36 \pm 0.07 \downarrow$	$0.70 \pm 0.03$	$0.52 \pm 0.09 \downarrow$	$0.53 \pm 0.07 \downarrow$	0.04
trouser	$0.32 \pm 0.10$	$0.07 \pm 0.04 \downarrow$	$0.06 \pm 0.03 \downarrow$	$0.59 \pm 0.04$	$0.07 \pm 0.04 \downarrow$	$0.16 \pm 0.07 \downarrow$	0.06
boot	$0.92 \pm 0.03$	$0.29 \pm 0.15 \downarrow$	$0.27 \pm 0.16 \downarrow$	$0.98 \pm 0.02$	$0.90 \pm 0.09 \downarrow$	$0.90 \pm 0.08 \downarrow$	0.08
sandal	$0.30 \pm 0.04$	$0.26 \pm 0.08 \downarrow$	$0.26 \pm 0.12 \downarrow$	$0.82 \pm 0.02$	$0.46 \pm 0.10 \downarrow$	$0.56 \pm 0.09 \downarrow$	0.09
sneaker	$0.55 \pm 0.09$	$0.12 \pm 0.10 \downarrow$	$0.14 \pm 0.12 \downarrow$	$0.74 \pm 0.09$	$0.47 \pm 0.19 \downarrow$	$0.46 \pm 0.18 \downarrow$	0.10

Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class **top** is similar to the abnormal training class **shirt**. Their  $L^2$  distance = 0.02.

Negative bias!

# Scenario 1: Training w/ the *Hard* Anomalies



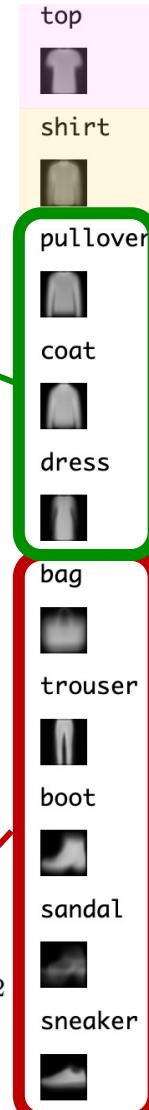
training normal = top, training abnormal = shirt

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to shirt
shirt	$0.09 \pm 0.01$	$0.71 \pm 0.01 \uparrow$	$0.70 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.72 \pm 0.01 \uparrow$	$0.72 \pm 0.01 \uparrow$	0
pullover	$0.13 \pm 0.02$	$0.90 \pm 0.01 \uparrow$	$0.89 \pm 0.01 \uparrow$	$0.19 \pm 0.02$	$0.84 \pm 0.02 \uparrow$	$0.85 \pm 0.01 \uparrow$	0.01
coat	$0.14 \pm 0.03$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	$0.15 \pm 0.02$	$0.92 \pm 0.02 \uparrow$	$0.92 \pm 0.01 \uparrow$	0.01
dress	$0.17 \pm 0.03$	$0.24 \pm 0.03 \uparrow$	$0.24 \pm 0.03 \uparrow$	$0.11 \pm 0.01$	$0.20 \pm 0.03 \uparrow$	$0.21 \pm 0.03 \uparrow$	0.04
bag	$0.49 \pm 0.07$	$0.38 \pm 0.08 \downarrow$	$0.36 \pm 0.07 \downarrow$	$0.70 \pm 0.03$	$0.52 \pm 0.09 \downarrow$	$0.53 \pm 0.07 \downarrow$	0.04
trouser	$0.32 \pm 0.10$	$0.07 \pm 0.04 \downarrow$	$0.06 \pm 0.03 \downarrow$	$0.59 \pm 0.04$	$0.07 \pm 0.04 \downarrow$	$0.16 \pm 0.07 \downarrow$	0.06
boot	$0.92 \pm 0.03$	$0.29 \pm 0.15 \downarrow$	$0.27 \pm 0.16 \downarrow$	$0.98 \pm 0.02$	$0.90 \pm 0.09 \downarrow$	$0.90 \pm 0.08 \downarrow$	0.08
sandal	$0.30 \pm 0.04$	$0.26 \pm 0.08 \downarrow$	$0.26 \pm 0.12 \downarrow$	$0.82 \pm 0.02$	$0.46 \pm 0.10 \downarrow$	$0.56 \pm 0.09 \downarrow$	0.09
sneaker	$0.55 \pm 0.09$	$0.12 \pm 0.10 \downarrow$	$0.14 \pm 0.12 \downarrow$	$0.74 \pm 0.09$	$0.47 \pm 0.19 \downarrow$	$0.46 \pm 0.18 \downarrow$	0.10

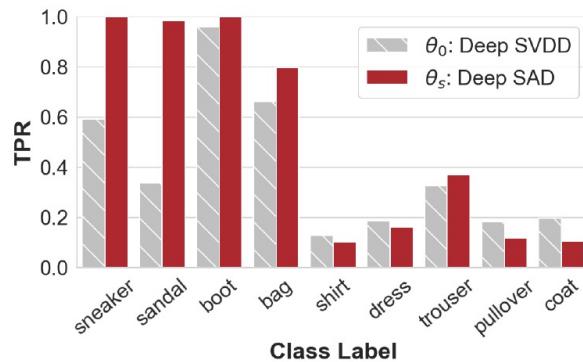
Table 3: The model TPR under scenario 1, Fashion-MNIST. The normal class **top** is similar to the abnormal training class **shirt**. Their  $L^2$  distance = 0.02.

Positive bias!

Negative bias!



## Scenario 2: Training w/ the *Easy* Anomalies



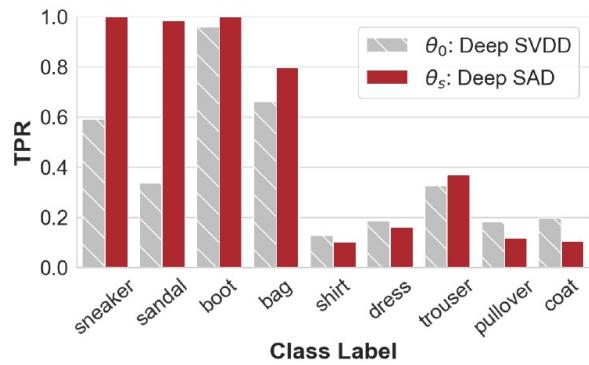
training normal = **top**, training abnormal = **sneaker**

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to sneaker
<b>sneaker</b>	$0.55 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	$0.74 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0
sandal	$0.30 \pm 0.04$	$0.99 \pm 0.01 \uparrow$	$0.98 \pm 0.02 \uparrow$	$0.82 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.02
boot	$0.92 \pm 0.03$	$1.00 \pm 0.00 \uparrow$	$0.97 \pm 0.02 \uparrow$	$0.98 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.07
bag	$0.49 \pm 0.07$	$0.80 \pm 0.05 \uparrow$	$0.81 \pm 0.11 \uparrow$	$0.70 \pm 0.03$	$0.84 \pm 0.03 \uparrow$	$0.82 \pm 0.03 \uparrow$	0.07
shirt	$0.09 \pm 0.01$	$0.11 \pm 0.02 \uparrow$	$0.12 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.13 \pm 0.01 \uparrow$	$0.15 \pm 0.01 \uparrow$	0.10
trouser	$0.32 \pm 0.09$	$0.31 \pm 0.10$	$0.11 \pm 0.12 \downarrow$	$0.58 \pm 0.04$	$0.58 \pm 0.03$	$0.58 \pm 0.05$	0.12
dress	$0.16 \pm 0.03$	$0.16 \pm 0.04$	$0.11 \pm 0.01 \downarrow$	$0.11 \pm 0.01$	$0.11 \pm 0.01$	$0.12 \pm 0.01$	0.13
pullover	$0.13 \pm 0.02$	$0.13 \pm 0.03$	$0.14 \pm 0.05$	$0.19 \pm 0.02$	$0.21 \pm 0.03$	$0.19 \pm 0.02$	0.13
coat	$0.14 \pm 0.03$	$0.13 \pm 0.03$	$0.13 \pm 0.06$	$0.15 \pm 0.02$	$0.16 \pm 0.02$	$0.15 \pm 0.02$	0.14

Table 6: The model TPR under scenario 2, Fashion-MNIST. The normal class **top** is dissimilar to the abnormal training class **sneaker**, and the  $L^2$  distance between the two is 0.13.



## Scenario 2: Training w/ the *Easy* Anomalies

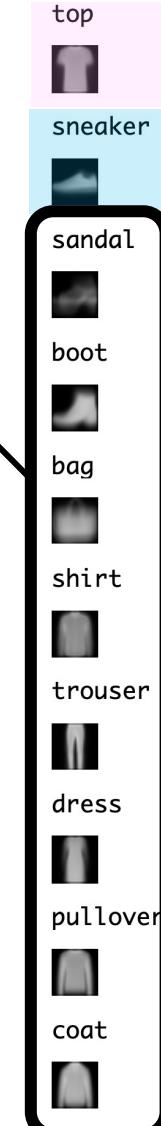


training normal = top, training abnormal = sneaker

Test data	Deep SVDD	Deep SAD	HSC	AE	SAE	ABC	$L^2$ to sneaker
sneaker	$0.55 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	$0.74 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0
sandal	$0.30 \pm 0.04$	$0.99 \pm 0.01 \uparrow$	$0.98 \pm 0.02 \uparrow$	$0.82 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.02
boot	$0.92 \pm 0.03$	$1.00 \pm 0.00 \uparrow$	$0.97 \pm 0.02 \uparrow$	$0.98 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.07
bag	$0.49 \pm 0.07$	$0.80 \pm 0.05 \uparrow$	$0.81 \pm 0.11 \uparrow$	$0.70 \pm 0.03$	$0.84 \pm 0.03 \uparrow$	$0.82 \pm 0.03 \uparrow$	0.07
shirt	$0.09 \pm 0.01$	$0.11 \pm 0.02 \uparrow$	$0.12 \pm 0.01 \uparrow$	$0.12 \pm 0.01$	$0.13 \pm 0.01 \uparrow$	$0.15 \pm 0.01 \uparrow$	0.10
trouser	$0.32 \pm 0.09$	$0.31 \pm 0.10$	$0.11 \pm 0.12 \downarrow$	$0.58 \pm 0.04$	$0.58 \pm 0.03$	$0.58 \pm 0.05$	0.12
dress	$0.16 \pm 0.03$	$0.16 \pm 0.04$	$0.11 \pm 0.01 \downarrow$	$0.11 \pm 0.01$	$0.11 \pm 0.01$	$0.12 \pm 0.01$	0.13
pullover	$0.13 \pm 0.02$	$0.13 \pm 0.03$	$0.14 \pm 0.05$	$0.19 \pm 0.02$	$0.21 \pm 0.03$	$0.19 \pm 0.02$	0.13
coat	$0.14 \pm 0.03$	$0.13 \pm 0.03$	$0.13 \pm 0.06$	$0.15 \pm 0.02$	$0.16 \pm 0.02$	$0.15 \pm 0.02$	0.14

Table 6: The model TPR under scenario 2, Fashion-MNIST. The normal class top is dissimilar to the abnormal training class sneaker, and the  $L^2$  distance between the two is 0.13.

Mostly harmless bias!



# Scenario 3: Mixed Training

training normal = **top**, training abnormal = 50% **shirt** and 50% **sneaker**

Test data	<b>Deep SVDD</b>	<b>Deep SAD</b>	<b>HSC</b>	<b>AE</b>	<b>SAE</b>	<b>ABC</b>	$L^2$ to shirt	$L^2$ to sneaker
shirt	$0.09 \pm 0.01$	$0.69 \pm 0.01 \uparrow$	$0.69 \pm 0.02 \uparrow$	$0.12 \pm 0.01$	$0.67 \pm 0.01 \uparrow$	$0.66 \pm 0.01 \uparrow$	0	0.10
sneaker	$0.55 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	$0.74 \pm 0.09$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.10	0
pullover	$0.13 \pm 0.02$	$0.90 \pm 0.01 \uparrow$	$0.90 \pm 0.01 \uparrow$	$0.19 \pm 0.02$	$0.82 \pm 0.02 \uparrow$	$0.83 \pm 0.02 \uparrow$	0.01	0.13
coat	$0.14 \pm 0.03$	$0.91 \pm 0.02 \uparrow$	$0.90 \pm 0.01 \uparrow$	$0.15 \pm 0.02$	$0.86 \pm 0.02 \uparrow$	$0.87 \pm 0.02 \uparrow$	0.01	0.14
dress	$0.17 \pm 0.03$	$0.23 \pm 0.04 \uparrow$	$0.24 \pm 0.04 \uparrow$	$0.11 \pm 0.01$	$0.19 \pm 0.03 \uparrow$	$0.18 \pm 0.02 \uparrow$	0.04	0.13
bag	$0.49 \pm 0.07$	$0.63 \pm 0.06 \uparrow$	$0.62 \pm 0.07 \uparrow$	$0.70 \pm 0.03$	$0.76 \pm 0.05 \uparrow$	$0.78 \pm 0.03 \uparrow$	0.04	0.07
trouser	$0.32 \pm 0.10$	$0.05 \pm 0.04 \downarrow$	$0.04 \pm 0.02 \downarrow$	$0.59 \pm 0.04$	$0.22 \pm 0.08 \downarrow$	$0.34 \pm 0.06 \downarrow$	0.06	0.12
boot	$0.92 \pm 0.03$	$0.95 \pm 0.03$	$0.95 \pm 0.03$	$0.98 \pm 0.02$	$1.00 \pm 0.00 \uparrow$	$1.00 \pm 0.00 \uparrow$	0.08	0.07
sandal	$0.30 \pm 0.04$	$0.92 \pm 0.04 \uparrow$	$0.92 \pm 0.04 \uparrow$	$0.82 \pm 0.02$	$0.96 \pm 0.01 \uparrow$	$0.97 \pm 0.01 \uparrow$	0.09	0.02

Table 9: The model TPR under configuration 1 of weighted mixture training on Fashion-MNIST.

# Takeaways and Future Directions

Additional labeled data in AD poses a hidden threat for model practitioners.

Potential debiasing strategies:

- Data-based strategy
  - Using active learning and to get representative anomaly labels on the fly.
  - Leveraging synthetic samples;
- Model-based strategy
  - Robust model design (e.g., ensembles).

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