

Introduction

COMP90049 COMP30018 Knowledge Technologies

String Search

Exact Approximate

Methods

Edit Distance

......

References

Ganomic

Introduction

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Jeremy Nicholson and Justin Zobel and Karin Verspoor

Semester 2, 2018





Summary

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Week 3:

- Approximate String Search and Matching
- Common Applications
- Methods:
 - Neighbourhood Search
 - Edit Distance
 - N-Gram Distance
 - [Phonetic methods]
- Evaluation
- [Genomics]



Exact String Search

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Consider:

- Given a string, is some substring contained within it?
- Given a string (document), find all occurrences of some substring

For example, find Exxon in:

In exes for foxes rex dux mixes a pox of waxed luxes.

An axe, and an axon, to exo Exxon max oxen.

Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Not (really) a Knowledge Technology!



Approximate String Search

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Approximate

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Find exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.

Not present!

...But what is the "closest" or "best" match?

This is a Knowledge Technology!



Important problems

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Two main applications for Approximate String Search:

- Spelling correction
- Computational Genomics



Spelling Correction

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Application

3:44 PM Optus 3G Messages Edit xyzzy 14/09/2013 3:44 PM В corridor × You are in a maze of dark and twisty corridr Send W Е R U 0 P Q S D F G Н K A X В M X .?123 space return



Spelling Correction

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Need the notion of a dictionary:

- Here, a list of entries that are "correct"
- We can break our input into substrings that we wish to match, and compare each of them against the entries in the dictionary
- An item in the input which doesn't appear in the dictionary is misspelled
- An item in the input which does appear in the dictionary might be correctly spelled or misspelled (probably slightly beyond the scope of this subject)



Spelling Correction

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Therefore, the problem here:

Given some item of interest — which does not appear in our dictionary — which entry from the dictionary was truly intended?

Depends on the person who wrote the original string!



Other Problems of Interest

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- Computational Genomics (later, if we have time)
- Name matching
- Query repair
- Phonetic matching (later, if we have time)
- Data cleaning
- ...



What's a "best" match?

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Find approximate match(es) for exon in:

In exes for foxes rex dux mixes a pox of waxed luxes. An axe, and an axon, to exo Exxon max oxen. Grexit or Brexit as quixotic haxxers with buxom rex taxation.



Neighbourhood Search

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For a given string *w* of interest:

- Generate all variants of w that utilise at most k changes (Insertions/Deletions/Replacements) — neighbours
- Check whether generated variants exist in dictionary
- All results found in dictionary are returned

Unix command-line utility agrep is an efficient mechanism for finding these.



Neighbourhood Search

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For example:

... proceed if you can see no **ther** option ...

Intended word: other

Requires 1 insertion (o) so intended word will be found using neighbourhood search (and some unintended words...)



Neighbourhood Search Efficiency

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Neighbourhood search is suprisingly fast!

Consider: alphabet size is Σ , length of string is |w|:

For k edits, roughly $\mathcal{O}(\Sigma^k \cdot |w|^k)$ neighbours

...But Σ is a small constant, string of interest is usually short, and k is usually small

For each neighbour, need a dictionary read (dict has D entries): Binary search yields $\mathcal{O}(|w|^k \log D)$ string comparisons



Neighbourhood Search Effectiveness

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So, efficiency isn't our problem.

 $({\tt agrep}\ example)$



Global Edit Distance

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Alternative methods:

Scan through each dictionary entry looking for the "best" match



Global Edit Distance

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O---:

Global Edit Distance:

Transform the string of interest into each dictionary entry, using the operations Insert, Delete, Replace, and Match (character)

Each operation is associated with a score;
Best match is the dictionary entry with best aggregate **score**



Global Edit Distance

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For example:

Item of interest: crat

Dictionary: cart, arts

Score: Match +1, Insert -1, Delete -1, Replace -1

 $\mathtt{crat} \to \mathtt{cart}$:

Match c (+1), Delete r (-1), Match a (+1), Insert r (-1), Match t (+1) = +1

 $\mathtt{crat} o \mathtt{arts}$:

Replace c with a (-1), Match r (+1), Delete a (-1), Match t (+1), Insert s (-1) = -1

cart is the better match



Global Edit Distance Parameter

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Confusingly, Global Edit Distance isn't a "distance"

...But depends on parameter

Match (0), Insert (+1), Delete (+1), Replace (+1)

This is the Levenshtein Distance (which is a "distance"): it counts the number of edits required to transform one string into the other



Global Edit Distance Parameter

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Hypothetically, any parameter is possible!

But some choices make no sense, e.g.:

Match (+4), Insert (-2), Delete (+8), Replace (0)

aba: Which corresponds to best match?

- foo: Insert, Delete, Insert, Delete, Insert, Delete = +18
- aba: Match, Match, Match = +12
- cbc: Replace, Match, Replace = +4



Global Edit Distance Parameter

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Often, "direction" doesn't matter: Insert = Delete ("Indel")

Sometimes, score of Replace depends on which character is being replaced:

Consider:

Is faxing more likely to be facing or faking?



Global Edit Distance Algorithm

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From string f to string t, given array A of |f|+1 columns and |t|+1 rows, we can solve using the Needleman–Wunsch algorithm:

equal() returns *m* if characters match, *r* otherwise

Final score is at A[It][If]



Global Edit Distance in Action

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Edit Distance

In action: from crat to arts, Match (+1), Insert/Delete/Replace (-1)

	ε	С	r	a	t
ε	0	-1	-2	-3	-4
a	-1	-1	-2	-1	-2
r	-2	-2	0	-1	-2
t	-3	-3	-1	-1	0
s	-4	-4	-2	-3 -1 -1 -1 -2	-1

Global Edit Distance: -1 (Replace, Match, Delete, Match, Insert)



More parameter concerns

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Algorithm actually depends on parameter!

```
A[j][k] = max3(
    A[j][k-1] + d, //Deletion
    A[j-1][k] + i, //Insertion
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

→ Match score greater than Insert/Delete/Replace

```
e.g. Match (+1), Insert/Delete/Replace (-1)
```



More parameter concerns

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Algorithm actually depends on parameter!

```
A[j][k] = min3(
    A[j][k-1] + d, //Deletion
    A[j-1][k] + i, //Insertion
    A[j-1][k-1] + equal(f[k-1],t[j-1])); //Replace or match
```

→ Match score less than Insert/Delete/Replace

```
e.g. Match (0), Insert/Delete/Replace (+1)
```

(Levenshtein Distance)



Local Edit Distance

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Local Edit Distance is like Global Edit Distance, but we are searching for the best substring match

Particularly suitable when comparing two strings of very different lengths, e.g. a word and a sentence



Local Edit Distance Algorithm

lf = strlen(f); lt = strlen(t);

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From string f to string t, given array A of |f|+1 columns and |t|+1 rows, we can solve using the Smith–Waterman algorithm:

equal() returns m if characters match, r otherwise

Final score is greatest value in the entire table (or least value, if m < i, d, r)



Local Edit Distance in Action

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In action: from cart to arts, Match (+1), Insert/Delete/Replace (-1)

	ε	С	a	r	t
ε	0	0	0	0	0
a	0	0	1	0	0
r	0	0	0	2	1
t	0	0	0	1	3
s	0 0 0 0	0	0	0	2

Best match: art with art (+3); ties are possible.



Edit Distance Efficiency

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For strings f and t, Both algorithms above are $\mathcal{O}(|f||t|)$ in both space and time. (Space can be improved, but time (probably) cannot.)

When approximate matching, we have a constant string f which we want to compare to each string t in the dictionary D:

$$\mathcal{O}(|f|\sum_{t\in D}|t|)$$

Hence, integer comparisons are roughly the number of characters in the dictionary. Whether this is feasible depends on the size of the dictionary.

N-Gram Distance

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N-Gram Distance has same goal as Edit Distance: compare two strings to determine "best" match

(character) *n*-gram: substring of length *n*

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

N-Gram Distance between *n*-grams of string $s(G_n(s))$ and $t(G_n(t))$:

$$|G_n(s)|+|G_n(t)|-2\times |G_n(s)\cap G_n(t)|$$

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n-gram: substring of length *n*

2-grams of crat: #c, cr, ra, at, t#

2-grams of cart: #c, ca, ar, rt, t#

2-grams of arts: #a, ar, rt, ts, s#

2-Gram Distance between crat and cart:

$$|\textit{G}_{2}(\texttt{crat})| + |\textit{G}_{2}(\texttt{cart})| - 2 \times |\textit{G}_{2}(\texttt{crat}) \cap \textit{G}_{2}(\texttt{cart})|$$

$$= 5 + 5 - 2 \times 2 = 6$$
 (better)

2-Gram Distance between crat and arts:

$$|G_2(\text{crat})| + |G_2(\text{arts})| - 2 \times |G_2(\text{crat}) \cap G_2(\text{arts})|$$

= 5 + 5 - 2 × 0 = 10



N-Gram Distance Efficiency

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Occasionally useful as a simpler variant of Edit Distance

More sensitive to long substring matches, less sensitive to relative ordering of strings (matches can be anywhere!)

Despite its simplicity, takes roughly the same time to compare entire dictionary

Quite useless for very long strings and/or very small alphabets (Why?)



Orthography

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In English (and some other languages), **orthography** (spelling) isn't a good predictor of **phonetics** (sounds)

Salient concern in speech—to—text systems, e.g.: Georgia Conal George O'Connell

Also relevant in spelling correction (English can be very difficult to spell correctly!)



Soundex

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One mechanism: Soundex

aehiouwy \rightarrow 0 (vowels)

 $bpfv \rightarrow 1$ (labials) cgjkqsxz \rightarrow 2 (misc: fricatives, velars, etc.)

Translation table: 3 (dentals) $\mathtt{dt} \quad o$

 \rightarrow 4 (lateral)

 \rightarrow 5 (nasals) mn

 \rightarrow 6 (rhotic) r

Four step process:

- Except for initial character, translate string characters according to table
- Remove duplicates (e.g. 4444 → 4)
- Remove 0s
- Truncate to four symbols



Soundex

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One mechanism: Soundex

 $\texttt{aehiouwy} \quad \rightarrow \quad 0 \; (\texttt{vowels})$

 $\mathtt{bpfv} \quad \rightarrow \quad \textbf{1 (labials)}$

 $cgjkqsxz \rightarrow 2$ (misc: fricatives, velars, etc.)

Translation table: ${\tt dt} \quad \to \quad 3 \text{ (dentals)}$

 $1 \rightarrow 4$ (lateral)

mn \rightarrow 5 (nasals)

 $r \rightarrow 6$ (rhotic)

Four step process:

king kyngge

k052 k05220

k052 k0520

k52 k52

k52 k52



Other Phonetic Methods

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Better phonetic methods make use of the fact that some letters sounds alike in certain contexts, and different in other contexts

Editex uses the Edit Distance to compare strings based on a similar translation table to Soundex

Ipadist uses a text–to–sound algorithm to represent tokens according to the International Phonetic Alphabet (but context matters a lot)

There are also worse variants, like Phonix.



Evaluating an Approximate Matching System

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Evaluation: consider whether the system is effective at solving the user's problem

In this case: for a misspelled word, does the system identify the correct word?

To evaluate, we need:

- A number of cases of misspelled words
- The <u>intended</u> (correct) word for each case
- An evaluation metric



Evaluation Metrics for Spelling Correction

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We have some cases:

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
corridr	corridor	corridor	✓
cracheyt	crotchety	cachet	×

Accuracy: fraction of correct responses $(\frac{1}{3})$



Evaluation Metrics for Spelling Correction

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More realistic situation:

Misspelled Word	Correct Word	Predicted Word	Right/Wrong?
ther	other	there	×
		other	✓
		their	×
corridr	corridor	corridor	✓
COITIGI		carrier	×
cracheyt	crotchety	???	_

Precision: fraction of correct responses among attempted responses

 $(\frac{2}{5})$

Recall: proportion of words with a correct response (somewhere) $(\frac{2}{3})$



Comparing Systems

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Typically, the value of the evaluation metric has little intrinsic meaning

"This system gets 81% accuracy" — useful for users, or not?

"The system based on the Global Edit Distance gets 81% accuracy, whereas the system based on the N-Gram Distance gets 84% accuracy"

"The basic system gets 81% accuracy, but after making some changes, the accuracy becomes 74%"

"System A gets 45% precision and 80% recall; System B gets 95% precision and 10% recall" — Which one should we use? (Also: why?)

The answer depends on the problem (and the user)!



Summary

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- What is approximate string search?
- What are some common applications of approximate string search; why are they hard?
- What are some methods for finding an approximate match to a string? What do we need to generate them?
- How can we evaluate a typical approximate matching system?



Background Readings

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Extension Readings

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Computational Genomics

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Genomics

Typical Genomics problem:

- Given a nucleotide/amino acid sequence (substring)
- Find whether the sequence occurs within a larger sequence (string)
- Possibly with "errors" (nucleotide/amino acid changes)



Computational Genomics

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Typical Genomics problem:

- Given a substring, find whether the sequence occurs within a larger string, possibly with "errors"
- Almost the same as spelling correction
- But **much** larger strings: a small genomics problem might involve comparing perhaps 1K character sequence against several 100K character sequences; alphabet is smaller



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Recall: we have a "short" (\sim 1K character) nucleotide/amino acid sequence to compare against many long (\sim 100K character) chromosomes/genes/proteins/etc.

For example, if some member of the population has 99% of the sequence of interest, they might be susceptible to some medical condition

We're allowed \sim 10 errors; alphabet is \sim 4 or \sim 20 characters



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Roughly $4^{10} \times 1000^{10}$ possible neighbours.

... Forget it.

Neighbourhood search:



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Global Edit Distance:

One string is $\sim 1 \text{K}$ characters, other is $\sim 100 \text{K}$ characters.

- ... Every string comparison involves ~99K insertions.
- → Prefers shorter chromosomes (not intended behaviour)



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Local Edit Distance:

One string is \sim 1K characters, other is \sim 100K characters.

... Seems like the right idea.



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Local Edit Distance:

One string is $\sim \! 10 K$ characters, other is $\sim \! 1G$ characters.

- ... Can't fit table into memory.
- ... Requires approximate solutions with heuristics, e.g. BLAST, FASTA



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N-Gram Distance:

With huge *n* (e.g. 80% of length of shorter string) can (almost) work!

Tends to prefer shorter chromosomes like Global Edit Distance

But better methods for using *n*-gram information, e.g. de Bruijn graphs