# Expressivity and Autosegmental Structure

Adam Jardine

**RUTGERS** 

Dept. of Linguistics, Rutgers University

December 12, 2016 SBU Computational Phonology Workshop

#### Introduction

- ► Main goal: a restrictive yet sufficient theory of well-formedness in tone
- ► **Tool:** a theory of simple computations over autosegmental grammars
- ► **Side benefit:** further understanding of the relationship between expressivity and phonological representation

#### Introduction

- Result: Graph Strictly Local (GSL) patterns provide a restrictive, sufficient, and unified characterization of the typology of tone
- ► GSL is based on *banned subgraphs* in autosegmental structures
- A sufficient theory from enriched representation; restrictive theory comes from computationally simple nature of banned substructure constraints

- ▶ What is the computational nature of phonological well-formedness?
- Banned substructure grammars over strings have provided a robust, restrictive characterization of segmental phonotactics and stress
- ► Strictly Local (SL) grammar (McNaughton and Papert, 1971; Rogers et al., 2013)

$$R = \{CC, VV\}$$

$$L(R) = \{CV, VC, CVC, VCV, CVCV, VCVC, CVCVC, ...\}$$

▶ \*CCC, \*#bn, \*HH, etc.

► **Tier-based Strictly Local (TSL)** grammars specify *R* and a tier *T* (Heinz et al., 2011)

$$\langle T = \{l, r\}, R = \{ll, rr\} \rangle$$

► A string *w* is well-formed iff erase<sub>T</sub>(*w*) does not contain a substring in *R* 

$$L(\langle T, R \rangle) = \{lVr, rVl, lVCrVl, ...\}$$

$$*rVr, *lVClVl, etc.$$

► Capures long-distance dissimilation and harmony with blocking (Heinz et al., 2011; McMullin and Hansson, 2016)

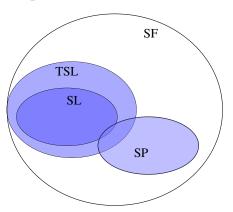
► **Strictly Piecewise (SP)** grammars: sub*sequence* (precedence), not substrings (Heinz, 2010; Rogers et al., 2010)

$$R = \{s...f, f...s\}$$

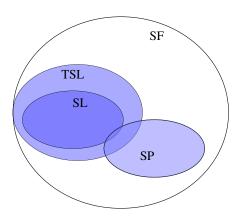
$$L(R) = \{sVs, \int V \int_{S} sCVCVs, \int CVCV \int_{S} ...\}$$

\*sCVCVf, etc.

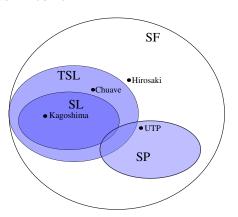
► Good fit to typology of consonant harmony (Heinz, 2010)



- ► SL, TSL, and SP provide a robust, yet restrictive, theory of segmental phonotactics
- Computation is based on banned substructures; differences are representational



▶ Opposed to, ex., **Star Free (SF)** class, which allows for global reasoning about a structure (McNaughton and Papert, 1971; Rogers et al., 2013; Jardine and Heinz, in press)



- ► Tone has both local and non-local patterns (Yip, 2002; Hyman, 2011)
- ► The following sample of *positional*, *obligatoriness*, and *culminativity* generalizations in tone fall in SL, TSL, SP, and SF

#### **Positional**

Kagoshima Japanese: Final or penult H (Hirayama, 1951; Haraguchi, 1977; ?)

| a. | hána        | 'nose'             | HL    |
|----|-------------|--------------------|-------|
| b. | sakúra      | 'cherry blossom'   | LHL   |
| c. | kagaríbi    | 'watch fire'       | LLHL  |
| d. | kagaribí-ga | 'watch fire' + NOM | LLLHL |
|    |             |                    |       |
| e. | haná        | 'flower'           | LH    |
| f. | usagí       | 'rabbit'           | LLH   |
| g. | kakimonó    | 'document'         | LLLH  |
| h. | kakimono-gá | 'document' + NOM   | LLLLH |
|    |             |                    |       |

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### **Obligatoriness**

► Chuave: **At least one H** (Donohue, 1997)

| a. | kán  | 'stick'  | e. | gíngódí | 'snore'    |       |
|----|------|----------|----|---------|------------|-------|
|    | Н    |          |    | HHH     |            | *L    |
| b. | gáán | 'child'  | f. | dénkábu | 'mosquito' |       |
|    | HH   |          |    | HHL     |            | *LL   |
| c. | gáam | 'skim'   | g. | énugú   | 'smoke'    |       |
|    | HL   |          |    | HLH     |            | *LLL  |
| d. | kubá | 'bamboo' | h. | amámó   | 'k.o. yam' |       |
|    | LH   |          |    | LHH     |            | *LLLL |
|    |      |          | i. | kóiom   | 'wing'     |       |
|    |      |          |    | HLL     |            |       |
|    |      |          | j. | komári  | 'before'   |       |
|    |      |          |    | LHL     |            |       |
|    |      |          | k. | koiyóm  | 'navel'    |       |
|    |      |          |    | LLH     |            |       |

### **Culminativity**

▶ Unbounded Tone Plateauing (UTP): **At most one** *span* **of H** (Hyman, 2011; Jardine, 2016)

```
kitabo
                    'book'
                                  LLL
a.
                    'chopper'
                                  LHL
h.
    mutéma
    kisikí
                   'log'
                                  LLH
    mutémá+bísíkí 'log chopper' LHHHHH
   *mutéma+bisikí
                   11 11
                                 *LHLLLH
                    (Luganda; Hyman, 2011; Hyman and Katamba, 2010)
```

### Positional + obligatoriness + culminativity

► Hirosaki Japanese: Exactly one H or F, F only word final (Haraguchi, 1977)

| Noun         | Isolation | +Nom   | Noun           | Isolation |
|--------------|-----------|--------|----------------|-----------|
| a. 'handle'  | é         | e-gá   | f. 'chicken'   | niwatorí  |
|              | H         | LH     |                | LLLH      |
| b. 'picture' | ê         | é-ga   | g. 'lightning' | kaminarî  |
|              | F         | HL     |                | LLLF      |
| c. 'candy'   | amé       | ame-gá | h. 'fruit'     | kudamóno  |
|              | LH        | LLH    |                | LLHL      |
| d. 'rain'    | amê       | amé-ga | i. 'trunk'     | toránku   |
|              | LF        | LHL    |                | LHLL      |
| e. 'autumn'  | áki       | áki-ga | j. 'bat'       | kóomori   |
|              | HL        | HLL    |                | HLLL      |
|              | *LLLL     | *HLLH  | *HLLF          | *FLLL     |

► **Kagoshima:** penult or final H

▶ **Chuave:** at least one H

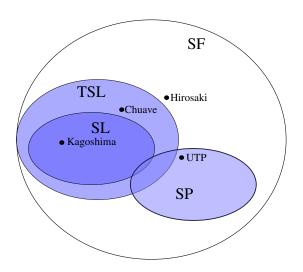
▶ **UTP:** At most one plateau of H

▶ **Hirosaki:** exactly one H or F; F word-final

positional obligatoriness

culminativity

all 3



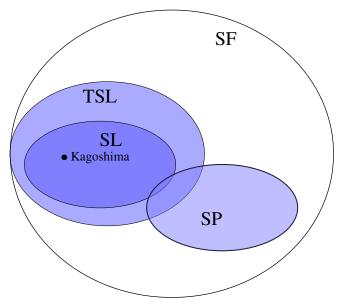
#### **Positional** constraints are SL

```
Kagoshima pattern: \{ \forall HL \lor, \forall LH \lor, \forall LH \lor, \forall LHL \lor, \forall LLH \lor, \forall LLHL \lor, \forall LLLH \lor, \dots \}

R = \{HLL, HH, HLH, LL \lor, \forall L \lor\}

*\forall HLLLL \lor, \forall HLLHL \lor, \forall LLLL \lor, \dots

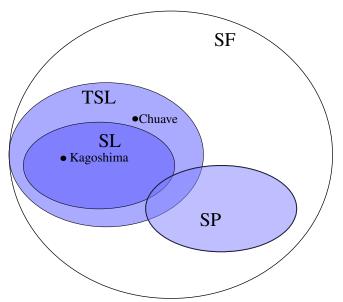
*\forall LLHHL \lor, \forall HLHL \lor, \forall LLLL \lor, \dots
```



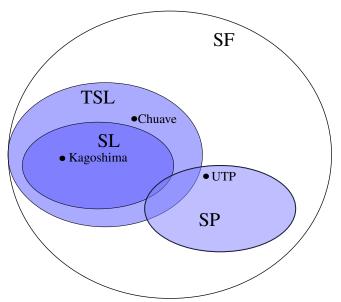
#### **Obligatoriness** constraints are TSL

```
Chuave pattern: \{ \forall LH \bowtie, \forall HL \bowtie, \forall HH \bowtie, \}
                          ALLHK, ALHLK, ALHHK,
                          MHLLK, MHLHK, MHHLK
                          ×HHH⋉, ×LLLH⋉, ...

ightharpoonup \langle T = \{H\}, R = \{ \times \times \} \rangle
                        erase_T(\rtimes LLH \ltimes) = \rtimes H \ltimes
                        erase_T(\rtimes LLL \ltimes) = \rtimes \kappa
            *XLX.*XLLX.*XLLLX.*XLLLX....
```



#### Culminativity constraints are SP



#### Combined constraints are not necessarily SL, TSL, or SP

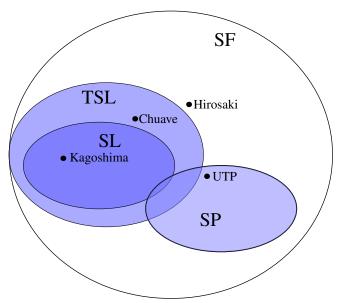
Hirosaki pattern:  $\{ \forall LLH \bowtie, \forall LLF \bowtie, \}$ 

```
MHLLK, MLLLLFK,
                         ×LLLH⋉, ×LLLLLF⋉,

ightharpoonup TSL: \langle T = \{H,F\}, R = \{ \bowtie \bowtie, HF, FH \} \rangle

ightharpoonup SL: R = \{FL\}
     *XLLLK,*XLLLLK,*XLLLLLK,...
     *AHLFK, *AHLLFK, *AHLLLFK, *AHLLLFK, ...
  *XLFLK, *XFLLK, *XLLFLK, *XLFLLK, *XFLLLK, ...
```

 $\bowtie LHL\bowtie$ ,  $\bowtie LLLF\bowtie$ ,



# Local graph grammars

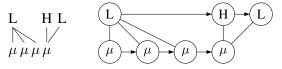
- String-based complexity classes provide a restrictive, but not entirely *sufficient* nor *unified*, characterization of tone
- ▶ Not unsurprising; tone has been claimed to be fundamentally autosegmental (Goldsmith, 1976; Yip, 2002; Hyman, 2011)

kaminarî LLLF 'lightning' L H L (Hirosaki)



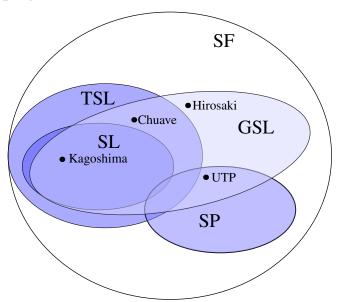
### Local graph grammars

► Autosegmental representations are **graphs** (Goldsmith, 1976; Coleman and Local, 1991)



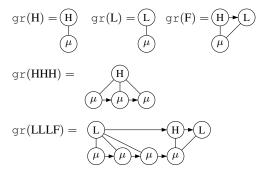
► We can instead consider **Graph Strictly Local** grammars, defined by restricted sub**graphs** 

# Local graph grammars



#### **Building structure**

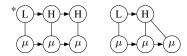
▶ We can define a function gr(w) that generates an autosegmental representation from strings (Jardine and Heinz, 2015)



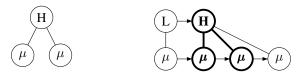
 Association preserves precedence relations (the No-Crossing Constraint (NCC))



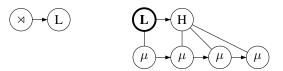
► Adjacent nodes on tonal tier cannot be identical (the Obligatory Contour Principle (OCP)



► Let a **subgraph** be some finite, connected piece of a graph



➤ Subgraphs may refer to boundaries on each tier (not depicted in full graphs)

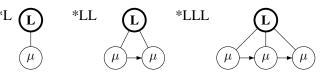


► *R* is some set of restricted subgraphs

$$L(R) = \{ w \mid \text{no graph in } R \text{ is a subgraph of } gr(w) \}$$

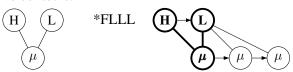
Let us consider strings over  $\{H, L, F\}$ 

▶ No all L toned words:

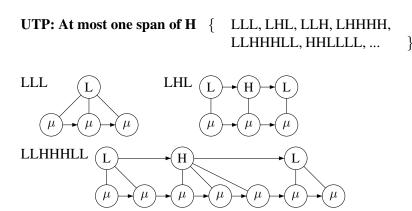


► First banned subgraph: (×) → (L) → (×)

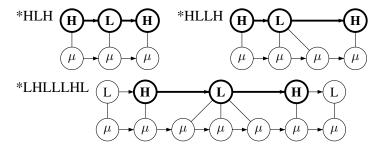
▶ No contours:



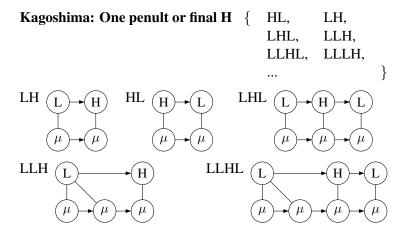
$$R = \left\{ (M) \rightarrow (L) \rightarrow (M) , \quad (H) \downarrow L \right\}$$



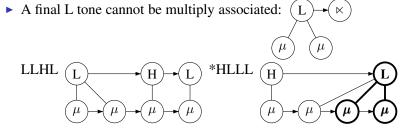
▶ Only one H tone per word: (H) → (L) → (H)



$$\qquad \qquad R = \left\{ \begin{array}{c} \text{H} \\ \text{L} \\ \text{H} \end{array} \right. , \qquad \begin{array}{c} \text{H} \\ \text{\mu} \\ \end{array} \right\}$$



Kagoshima: One penult or final H { HL, LH, LLH, LLH, LLHL, LLLH, ... }



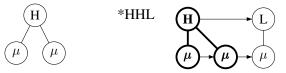
Only one H tone per word



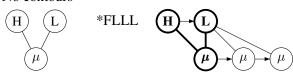
▶ No all L toned words



▶ No spreading of H



No contours



Kagoshima: One penult or final H 
$$\{HL, LH, LLH, LLH, LLHL, LLLH, LLHL, LLLH, LLHL, LLLH, ... \}$$

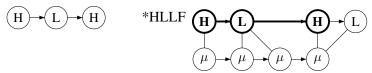
•  $R = \{ \begin{array}{c} L \\ \mu \end{array}, \begin{array}{c} H \\ \mu \end{array}, \begin{array}{c} H \\ \mu \end{array}, \begin{array}{c} H \\ \mu \end{array}, \begin{array}{c} L \\ \mu \end{array}, \begin{array}{c} L$ 

```
Hirosaki: Exactly one H or F; F always final
    LLH, LHL, HLL, LLLH, ...
    LLF, LLLF, LLLLF, LLLLLF, . . . }
LLH
                     LHL
                                          HLL
LLF
                          LLLF
```

### Hirosaki: Exactly one H or F; F always final

```
LLH, LHL, HLL, LLLH, ...
LLF, LLLF, LLLLF, LLLLF, ... }
```

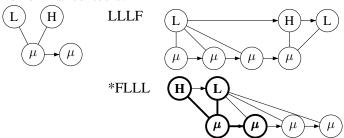
▶ No two Hs in the melody:



### Hirosaki: Exactly one H or F; F always final

```
LLH, LHL, HLL, LLLH, ...
LLF, LLLF, LLLLF, LLLLF, ... }
```

▶ No nonfinal contours:



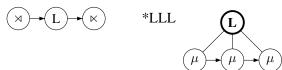
### Hirosaki: Exactly one H or F; F always final

```
\left\{ \begin{array}{cc} \text{LLH, LHL, HLL, LLLH, } \dots \\ \text{LLF, LLLF, LLLLF, LLLLF, } \dots \end{array} \right\}
```

No spreading of H



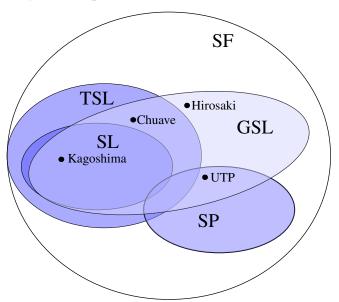
▶ No all L toned words



### Hirosaki: Exactly one H or F; F always final

LLH, LHL, HLL, LLLH, ... LLF, LLLF, LLLLF, LLLLLF, ... }

$$R = \left\{ \begin{array}{c} H \\ \end{array} \right\} \left( \begin{array}{c} L \\ \end{array} \right) \left( \begin{array}{c} H \\ \end{array} \right)$$



### Discussion

- ► Tonal constraints fall into a number of distinct classes of string grammars
- Banned subgraph grammars provide a unified theory of positional, culminativity, and obligatoriness constraints in tone
- ► They are **restrictive** in that we can only *ban* structures—we can't require them (Jardine and Heinz, in press)
  - ▶ Example: 'First last' patterns (Lai, 2012, 2015):  $\bowtie H \leftrightarrow H \bowtie$

### Discussion

- ► We can define mappings like gr(w) through mathematical logic (Courcelle, 1994; Engelfriet and Hoogeboom, 2001)
- ► The *structure* is restrictive because gr(w) is **first-order definable** from strings (using the order <)
- ► The structural relationships in an autosegmental structure are thus equivalent to FO-statements in a string
- ► Thus, using local autosegmental grammars will never take us out of SF
- ▶ (This is also true for  $erase_T(w)$ )

#### Discussion

- ► Such structure-creating functions can aid in **learning**
- ▶ Banned substructure grammars have established learning techniques (García et al., 1990; Heinz, 2010; Heinz and Rogers, 2010)
- ► These techniques can learn long-distance patterns with additional structure known *a priori* (Hayes and Wilson, 2008; Heinz et al., 2011; Jardine and Heinz, 2016b)
- ➤ Tier structure can be learned (Goldsmith and Riggle, 2012; Jardine and Heinz, 2016a; Jardine and McMullin, to appear), but no work yet on autosegmental structure

#### Conclusion

- ► We have characterized tone by extending **banned subgraph** grammars to autosegmental representations
- This provided a sufficient and unified, yet restrictive, characterization of tone
- ▶ What about other structure: correspondence, syllables, stress grids, feet?
- ► How does autosegmental structure interact with the complexity of *transformations*? (Jardine, 2016)

# Acknowledgments

### Thank you!

This work is indebted to Jeff Heinz, Jim Rogers, Jane Chandlee, Bill Idsardi, the UD Phonetics & Phonology group, the students of my Phonology III course at Rutgers (Eileen Blum, Hazel Mitchley, Luca Iacoponi, and Nick Danis), and audiences at the 2016 LSA annual meeting, NAPhC, UPenn, and Rutgers University. The majority of this research was done under the auspices of a University of Delaware dissertation fellowship.

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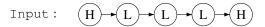
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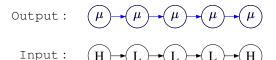
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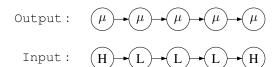
- ► First order logic for strings over {H, L}
  - $\triangleright$  Variables x, y, z, ..., ranging over positions in the string
  - ▶ Predicates H(x) and L(x)
  - ▶ Predicates  $x \triangleleft y$  and x < y
  - ▶ Logical connectives  $\neg \phi$ ,  $\phi \land \psi$ ,  $\phi \lor \psi$ ,  $\phi \to \psi$
  - Quantifiers  $(\forall x)[\phi(x)]$  and  $(\exists x)[\phi(x)]$



- Defining autosegmental positions and relationships in terms of the input string
  - $\mu_A^1(x) \stackrel{\text{def}}{=} \mathrm{H}(x) \vee \mathrm{L}(x)$



- ► Two useful predicates:
  - ▶ LSpanHd(x)  $\stackrel{\text{def}}{=}$  L(x)  $\land$  ( $\forall y$ )[ $y \triangleleft x \rightarrow \neg$ L(x)]
  - ▶  $\operatorname{HSpanHd}(x) \stackrel{\operatorname{def}}{=} \operatorname{H}(x) \wedge (\forall y)[y \triangleleft x \rightarrow \neg \operatorname{H}(x)]$
  - ▶  $\operatorname{span}(x,y) \stackrel{\text{def}}{=} \left( \operatorname{H}(x) \wedge \operatorname{H}(y) \wedge (\forall z) [(x < z \wedge z < y) \to \operatorname{H}(z)] \right)$  $\vee \left( \operatorname{L}(x) \wedge \operatorname{L}(y) \wedge (\forall z) [(x < z \wedge z < y) \to \operatorname{L}(z)] \right)$



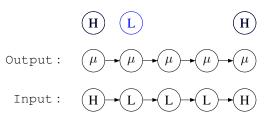
### **Defining** gr(w) in **FO**

- Defining autosegmental positions and relations in terms of the input string
  - ▶  $H_A^2(x) \stackrel{\text{def}}{=} \text{HSpanHd}(x)$

"Copy the first H in a sequence of Hs"

▶  $L_A^2(x) \stackrel{\text{def}}{=} \text{LSpanHd}(x)$ 

"Copy the first L in a sequence of Ls"



### **Defining** gr(w) **in FO**

 Defining autosegmental positions and relations in terms of the input string

▶ 
$$x \triangleleft_A^{2,2} y \stackrel{\text{def}}{=} x < y \land (\text{HSpanHd}(x)) \lor \text{LSpanHd}(x)) \land$$

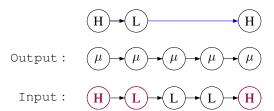
" $x \text{ starts a span...}$ "

 $(\forall z)[(x < z \land z < y) \rightarrow \text{span}(x, z)] \land$ 

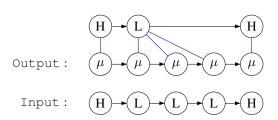
" $everything \text{ in between } x \text{ and } y \text{ is in a span with } x$ "

 $\neg (\text{span}(x, y))$ 

" $x \text{ and } y \text{ are not in a span}$ "



- Defining autosegmental positions and relations in terms of the input string

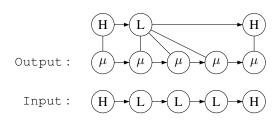


### **Defining** gr(w) in **FO**

• We've defined gr(w) by defining

$$\mu_A(x)$$
,  $H_A(x)$ ,  $L_A(x)$ ,  $x \triangleleft_A^{1,1} y$ ,  $x \triangleleft_A^{2,2} y$ ,  $x \triangleleft_A^{2,1} y$ 

in FO terms of the input string



▶ 
$$\neg(\exists x, y, z) [x \triangleleft_A y \land y \triangleleft_A z \land H(x) \land L(y) \land H(z)]$$
  

$$= x < y \land (HSpanHd(x) \lor LSpanHd(x)) \land (\forall z) [(x < z \land z < y) \rightarrow span(x, z)] \land \neg(span(x, y))$$