DATA 621 Homework 3

Critical Thinking Group 1

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DATA 621 – Business Analytics and Data Mining

Home Work 3

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Introduction

Crime has a high cost to all parts of society and it can have severe long term impact on neighborhoods. If crime rises in the neighborhood, it affects the neighborhood. Additionally, crime can even have a health cost to the community in that the perception of a dangerous neighborhood was associated with significantly lower odds of having high physical activity among both men and women. It is important to understand the propensity for crime levels of a neighborhood before investing in that neighborhood.

Statement of the Problem

The purpose of this report is to develop a binary logistic regression model to determine if the neighborhood will be at risk for high crime level.

Data Exploration

Let's take a look to the first few rows of our train data set

```
##
      zn indus chas
                                    age
                                           dis rad tax ptratio 1stat medv target
                       nox
                              rm
## 1
       0 19.58
                   0 0.605 7.929
                                  96.2 2.0459
                                                  5 403
                                                                 3.70 50.0
                                                           14.7
                                                                                  1
## 2
       0 19.58
                   1 0.871 5.403 100.0 1.3216
                                                 5 403
                                                           14.7 26.82 13.4
                                                                                  1
       0 18.10
                   0 0.740 6.485 100.0 1.9784
                                                 24 666
                                                           20.2 18.85 15.4
## 3
                                                                                  1
## 4
      30
          4.93
                   0 0.428 6.393
                                    7.8 7.0355
                                                 6 300
                                                           16.6 5.19 23.7
                                                                                  0
## 5
       0
          2.46
                   0 0.488 7.155
                                  92.2 2.7006
                                                  3 193
                                                           17.8
                                                                 4.82 37.9
                                                                                  0
          8.56
                   0 0.520 6.781
                                  71.3 2.8561
                                                 5 384
## 6
       0
                                                           20.9
                                                                 7.67 26.5
                                                                                  0
## 7
       0 18.10
                   0 0.693 5.453 100.0 1.4896
                                                 24 666
                                                           20.2 30.59
                                                                        5.0
                                                                                  1
## 8
       0 18.10
                   0 0.693 4.519 100.0 1.6582
                                                 24 666
                                                           20.2 36.98
                                                                        7.0
                                                                                  1
## 9
       0
          5.19
                   0 0.515 6.316
                                  38.1 6.4584
                                                  5 224
                                                           20.2 5.68 22.2
                                                                                  0
          3.64
                   0 0.392 5.876 19.1 9.2203
                                                           16.4 9.25 20.9
## 10 80
                                                  1 315
                                                                                  0
```

Looks like all the columns are numerical. The target variable is a binary variable indicating if the crime rate above the median rate (1) or not (0)

Means

Column means of our train data set are as follows:

```
##
                         indus
              zn
                                        chas
                                                       nox
                                                                       rm
                                                                                    age
##
    11.57725322
                  11.10502146
                                  0.07081545
                                                0.55431052
                                                              6.29067382
                                                                           68.36759657
##
                                                                                   medv
             dis
                           rad
                                         tax
                                                   ptratio
                                                                    lstat
##
     3.79569292
                   9.53004292 409.50214592
                                              18.39849785
                                                             12.63145923
                                                                           22.58927039
##
         target
##
     0.49141631
```

Standard Deviation

Now let's take a look at the standard deviation of our predictor variables:

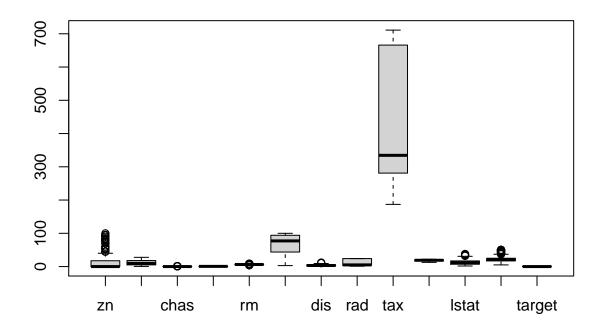
```
##
                      indus
                                    chas
            zn
                                                  nox
                                                                rm
                                                                            age
##
    23.3646511
                  6.8458549
                               0.2567920
                                            0.1166667
                                                         0.7048513
                                                                    28.3213784
                                                             lstat
##
           dis
                        rad
                                     tax
                                              ptratio
                                                                           medv
##
     2.1069496
                  8.6859272 167.9000887
                                            2.1968447
                                                         7.1018907
                                                                      9.2396814
##
        target
##
     0.5004636
```

Median Value

Let's take a look at the median value of our predictor variables:

```
##
                   indus
                               chas
           zn
                                           nox
                                                                            dis
                                                                                       rad
                                                       {\tt rm}
                                                                 age
     0.00000
                9.69000
                           0.00000
                                      0.53800
                                                 6.21000
                                                           77.15000
##
                                                                        3.19095
                                                                                   5.00000
##
          tax
                ptratio
                              lstat
                                          medv
                                                   target
## 334.50000
               18.90000
                          11.35000
                                     21.20000
                                                 0.00000
```

Bar chart or box plot



Correlation matrix

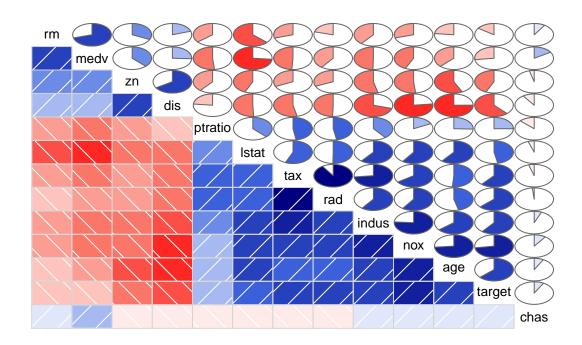
```
## zn indus chas nox rm age

## zn 1.0000000 -0.53826643 -0.04016203 -0.51704518 0.31981410 -0.57258054

## indus -0.53826643 1.00000000 0.06118317 0.75963008 -0.39271181 0.63958182
```

```
-0.04016203 0.06118317 1.00000000 0.09745577 0.09050979 0.07888366
## chas
## nox
          -0.51704518 0.75963008 0.09745577 1.00000000 -0.29548972 0.73512782
           0.31981410 -0.39271181 0.09050979 -0.29548972 1.00000000 -0.23281251
## rm
          -0.57258054 0.63958182 0.07888366 0.73512782 -0.23281251 1.00000000
## age
## dis
           0.66012434 -0.70361886 -0.09657711 -0.76888404 0.19901584 -0.75089759
## rad
          -0.31548119 \quad 0.60062839 \ -0.01590037 \quad 0.59582984 \ -0.20844570 \quad 0.46031430
          -0.31928408 0.73222922 -0.04676476 0.65387804 -0.29693430 0.51212452
## 1stat
          -0.43299252 \quad 0.60711023 \quad -0.05142322 \quad 0.59624264 \quad -0.63202445 \quad 0.60562001
           0.37671713 \ -0.49617432 \ \ 0.16156528 \ -0.43012267 \ \ \ 0.70533679 \ -0.37815605
## medv
## target -0.43168176 0.60485074 0.08004187 0.72610622 -0.15255334 0.63010625
##
                  dis
                             rad
                                         tax
                                                ptratio
                                                             lstat
## zn
           0.66012434 -0.31548119 -0.31928408 -0.3910357 -0.43299252 0.3767171
          -0.70361886 0.60062839 0.73222922 0.3946898 0.60711023 -0.4961743
## indus
          -0.09657711 \ -0.01590037 \ -0.04676476 \ -0.1286606 \ -0.05142322 \ \ 0.1615653
## chas
          ## nox
           0.19901584 -0.20844570 -0.29693430 -0.3603471 -0.63202445 0.7053368
## rm
## age
          -0.75089759 0.46031430 0.51212452 0.2554479 0.60562001 -0.3781560
           1.00000000 -0.49499193 -0.53425464 -0.2333394 -0.50752800 0.2566948
## dis
          -0.49499193 1.00000000 0.90646323 0.4714516 0.50310125 -0.3976683
## rad
## tax
          -0.53425464 0.90646323 1.00000000 0.4744223 0.56418864 -0.4900329
## ptratio -0.23333940 0.47145160 0.47442229 1.0000000 0.37735605 -0.5159153
          -0.50752800 \quad 0.50310125 \quad 0.56418864 \quad 0.3773560 \quad 1.00000000 \quad -0.7358008
## 1stat
           0.25669476 -0.39766826 -0.49003287 -0.5159153 -0.73580078 1.0000000
## medv
         -0.61867312  0.62810492  0.61111331  0.2508489  0.46912702  -0.2705507
## target
               target
## zn
          -0.43168176
           0.60485074
## indus
## chas
           0.08004187
## nox
           0.72610622
## rm
          -0.15255334
## age
           0.63010625
## dis
          -0.61867312
## rad
           0.62810492
## tax
           0.61111331
## ptratio 0.25084892
## 1stat
           0.46912702
## medv
          -0.27055071
## target
           1.00000000
```

visualize the data in correlation matrices

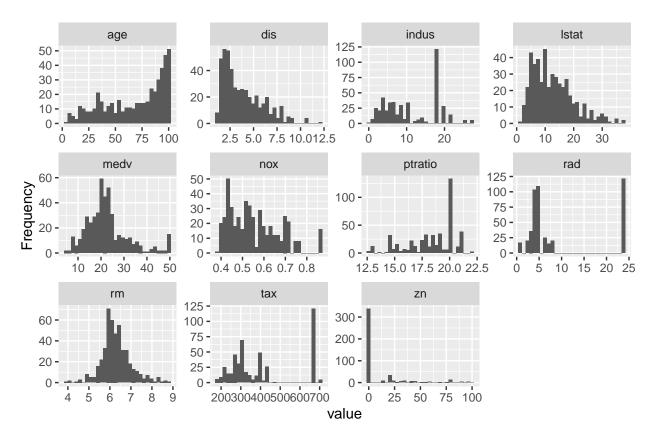


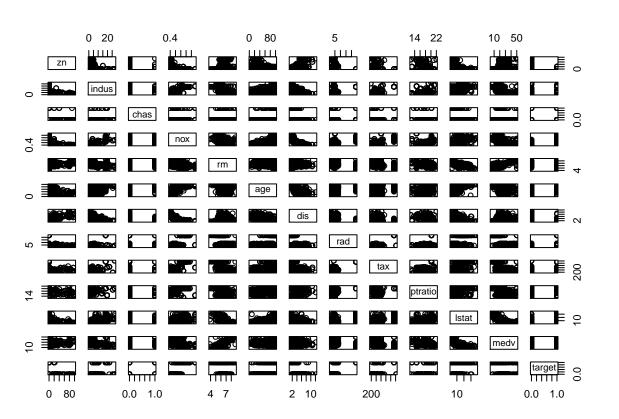
Compare Target in Training

We make sure there are no issues with an inappropriate distribution of the target variable in our training data.

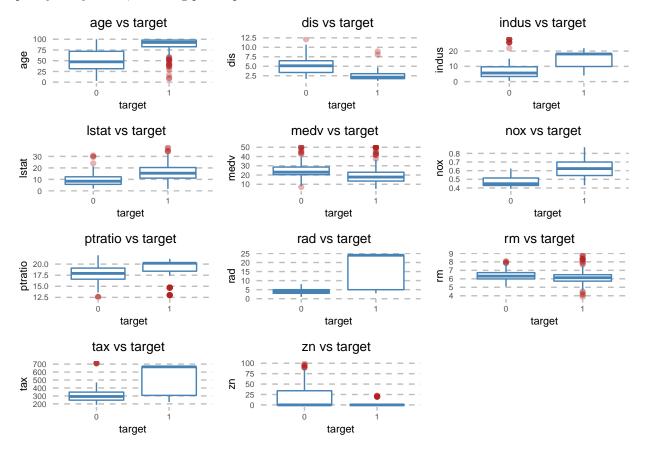
Var1	Freq
0	237
1	229

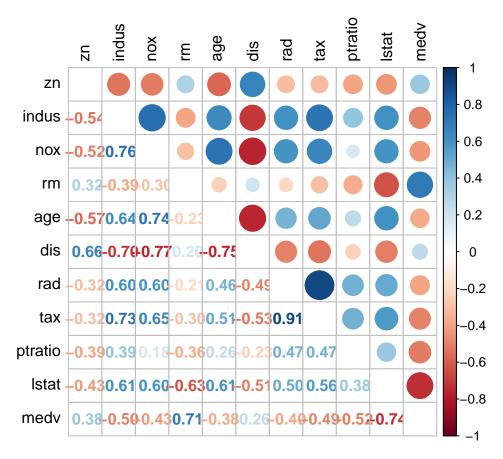
Histogram of Variables





Now that we have a basic familiarity with our data, we can analyze the relationship between the numeric variables we've brought in and the target variable. We can employ boxplots and a correlation matrix to quickly analyze this, including paired plots of the numeric feature variables.





There are a couple of items to note in the above graphics. First, in the boxplots, we observe many outliers, which could impact our regression, limiting its predictive value. Age, nox, and dis all appear to be highly correlated with our target, and numerous other features appear to have some weaker correlative relationship. Now that we've assessed the relationship between our features and the target, we can take a quick look, through our correlation matrix, at the relationship between the variables themselves. Our correlation matrix makes clear that multicollinearity is a potential issue within our observations, and we need to keep this in mind as we create and select our models.

Data Preparation

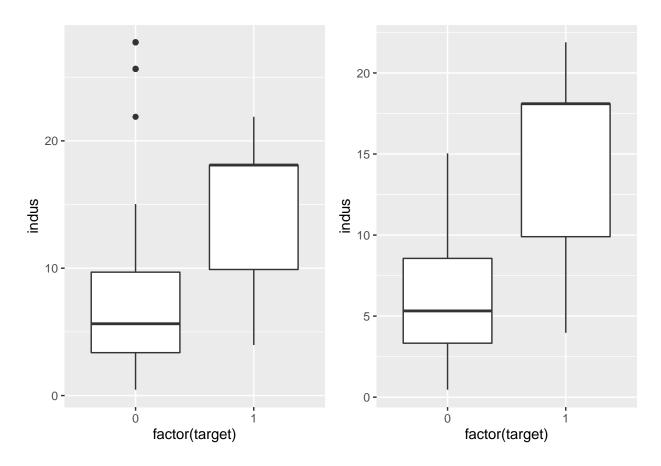
Looking at the results from our chas variable it doesn't seem to be needed here so we can remove it.

```
test_url <- 'https://raw.githubusercontent.com/ahussan/DATA_621_Group1/main/HW3/crime-evaluation-data_m
test <- read.csv(test_url, header=TRUE)
trainchas <- as.factor(train$chas)
train$chas <- NULL
traintarget <- as.factor(train$target)
train$target <- traintarget
testchas <- as.factor(test$chas)
test$chas <- NULL</pre>
```

Indus

We see a lot of outliers in the indus variable, so we'll removed the rows which indus is greater than 20 and target is 0.

```
attach(train)
p0 <- ggplot(train, aes(factor(target), indus)) + geom_boxplot()
train <- train[-which(target==0 & indus > 20),]
p1 <- ggplot(train, aes(factor(target), indus)) + geom_boxplot()
grid.arrange(p0, p1,ncol=2,nrow=1)</pre>
```

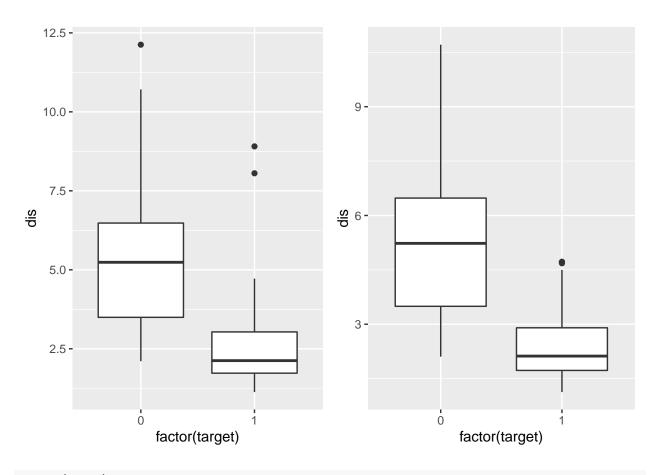


```
detach(train)
```

Dis

Dis also has some outliers so we'll remove rows where dis was greater than 11 and target was 0, and where dis was greater than 7.5 and target was 1.

```
attach(train)
p0 <- ggplot(train, aes(factor(target), dis)) + geom_boxplot()
train <- train[-which(target==0 & dis > 11),]
train <- train[-which(target==1 & dis > 7.5),]
p1 <- ggplot(train, aes(factor(target), dis)) + geom_boxplot()
grid.arrange(p0, p1, ncol=2,nrow=1)</pre>
```



detach(train)

Data Summary

Let's take a quick look at what variables we have remaining.

```
names(train)

## [1] "zn"     "indus" "nox"     "rm"     "age"     "dis"     "rad"

## [8] "tax"     "ptratio" "lstat"     "medv"     "target"     "dataset"

dim(train)
```

[1] 452 13

Build Models

Model 1 - All Variables

First we will be creating a model with all the variables in the original dataset to create a baseline for other models. Based on the p-values results from this model we will be able to eliminate variables with large p-values

```
m1 = glm(target ~ zn + indus + nox + rm + age + dis + rad + tax + ptratio + lstat + medv, data=train, f
summary(m1)
##
## Call:
## glm(formula = target ~ zn + indus + nox + rm + age + dis + rad +
      tax + ptratio + lstat + medv, family = binomial, data = train)
##
## Deviance Residuals:
##
      Min
                1Q
                    Median
                                  3Q
                                          Max
## -2.3349 -0.0799
                    0.0000
                              0.0012
                                       3.1976
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -38.029594 7.489999 -5.077 3.83e-07 ***
## zn
               -0.048542 0.035405 -1.371 0.170361
## indus
                0.199630 0.089639
                                     2.227 0.025944 *
## nox
               45.790310 8.194404
                                     5.588 2.30e-08 ***
## rm
               -0.511858
                          0.813749 -0.629 0.529341
                0.035180
                          0.014517
                                     2.423 0.015378 *
## age
                          0.253439
                                     0.971 0.331397
## dis
                0.246166
## rad
                0.926188
                           0.200821
                                     4.612 3.99e-06 ***
## tax
               -0.022971
                           0.006322 -3.634 0.000279 ***
## ptratio
                0.501234
                           0.162414
                                     3.086 0.002028 **
                0.098382
                           0.057781
                                      1.703 0.088630 .
## lstat
                0.162372
                          0.077550
                                     2.094 0.036281 *
## medv
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 626.60 on 451 degrees of freedom
## Residual deviance: 157.53 on 440 degrees of freedom
## AIC: 181.53
##
## Number of Fisher Scoring iterations: 9
```

We can see that variables indus, nox, age, rad, tax, ptratio, lstat, and medv have p values that are close to and or smaller than 0.05 which will be used in the next model

Model 2 - Hand Pick Model

```
m2 = glm(target ~ indus + nox + age + rad + tax + ptratio + lstat + medv, data=train, family=binomial)
summary(m2)

##
## Call:
## glm(formula = target ~ indus + nox + age + rad + tax + ptratio +
## lstat + medv, family = binomial, data = train)
##
```

```
## Deviance Residuals:
##
       Min
                   10
                         Median
                                       30
                                                 Max
  -2.35458 -0.09486
                        0.00002
##
                                  0.00127
                                             2.85518
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -37.745051
                            6.273620 -6.016 1.78e-09 ***
## indus
                 0.228533
                            0.085607
                                       2.670 0.007595 **
## nox
                43.209019
                            7.453316
                                       5.797 6.74e-09 ***
## age
                 0.027807
                            0.010963
                                       2.537 0.011196 *
## rad
                 0.914150
                            0.187390
                                       4.878 1.07e-06 ***
## tax
                -0.024103
                            0.005802
                                      -4.154 3.26e-05 ***
                 0.518734
                            0.142931
                                       3.629 0.000284 ***
## ptratio
## 1stat
                 0.116872
                            0.050616
                                       2.309 0.020944 *
                 0.110928
                            0.042294
                                       2.623 0.008721 **
## medv
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 626.60 on 451 degrees of freedom
## Residual deviance: 160.86
                             on 443 degrees of freedom
## AIC: 178.86
## Number of Fisher Scoring iterations: 9
```

Model 3 - Backward Step Model

We will now build a model using backwards selection in order to compare if using backwards selection is better than hand picking values to create a model In order to create the the backward step model we will be using the MASS package which includes the stepAIC function. The backward step requires us to pass a model which contains all of the predictors. Then the function will fit all the models which contains all but one of the predictors and will then pick the best model using AIC

```
m3 = stepAIC(m1, direction='backward', trace=FALSE)
summary(m3)
```

```
##
## Call:
## glm(formula = target ~ zn + indus + nox + age + rad + tax + ptratio +
##
       lstat + medv, family = binomial, data = train)
##
## Deviance Residuals:
##
        Min
                   1Q
                          Median
                                        3Q
                                                  Max
                        0.00002
##
  -2.41614
            -0.08644
                                   0.00128
                                             3.08111
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -35.751993
                             6.402055
                                      -5.584 2.34e-08 ***
                -0.045663
                                       -1.387
                                                0.1655
## zn
                             0.032925
## indus
                 0.207458
                             0.086225
                                        2.406
                                                0.0161 *
## nox
                42.641987
                             7.490375
                                        5.693 1.25e-08 ***
                 0.027458
                             0.011021
                                        2.491
                                                0.0127 *
## age
```

```
## rad
                 0.939777
                            0.193632
                                       4.853 1.21e-06 ***
                                      -4.230 2.33e-05 ***
## tax
                -0.024982
                            0.005905
## ptratio
                 0.457404
                            0.147306
                                       3.105
                                               0.0019 **
                 0.116084
                                       2.298
                                               0.0215 *
## 1stat
                            0.050509
## medv
                 0.107888
                            0.042022
                                       2.567
                                               0.0102 *
##
  ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 626.60
                              on 451
                                      degrees of freedom
## Residual deviance: 158.64
                             on 442 degrees of freedom
  AIC: 178.64
##
## Number of Fisher Scoring iterations: 9
```

Model 4 - Forward Step Model

We can use the same stepAIC function to build the fourth model. The forward selection approach starts from the null model and adds a variable that improves the model the most, one at a time, until the stopping criterion is met. We can see the result is different compared to the backward selection approach. We can see that the result is same as the saturated model m1.

```
m4 = stepAIC(m1, direction='forward', trace=FALSE)
summary(m4)
```

```
##
## Call:
  glm(formula = target ~ zn + indus + nox + rm + age + dis + rad +
##
       tax + ptratio + lstat + medv, family = binomial, data = train)
##
##
  Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    30
                                            Max
                      0.0000
##
  -2.3349
           -0.0799
                                0.0012
                                         3.1976
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -38.029594
                             7.489999
                                      -5.077 3.83e-07 ***
## zn
                -0.048542
                             0.035405
                                      -1.371 0.170361
## indus
                 0.199630
                             0.089639
                                        2.227 0.025944 *
## nox
                45.790310
                             8.194404
                                        5.588 2.30e-08 ***
## rm
                -0.511858
                             0.813749
                                       -0.629 0.529341
                             0.014517
                                        2.423 0.015378 *
## age
                 0.035180
## dis
                 0.246166
                             0.253439
                                        0.971 0.331397
## rad
                 0.926188
                             0.200821
                                        4.612 3.99e-06 ***
                -0.022971
                             0.006322
                                       -3.634 0.000279 ***
## tax
                                        3.086 0.002028 **
                 0.501234
                             0.162414
## ptratio
                 0.098382
                             0.057781
                                        1.703 0.088630 .
## 1stat
## medv
                 0.162372
                             0.077550
                                        2.094 0.036281 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
```

```
##
## Null deviance: 626.60 on 451 degrees of freedom
## Residual deviance: 157.53 on 440 degrees of freedom
## AIC: 181.53
##
## Number of Fisher Scoring iterations: 9
```

Model 5 - Stepwise step Model

We also can use the same stepAIC function to build the fifth model using stepwise regression. The stepwise regression method involves adding or removing potential explanatory variables in succession and testing for statistical significance after each iteration. At the very last step stepAIC as shown in the summary table has produced the optimal set of features $\{zn, nox, age, dis, rad, ptratio, medv\}$. This is exactly same result as the backward step model.

```
m5 = stepAIC(m1, direction='both', trace=FALSE)
summary(m5)
```

```
##
## Call:
  glm(formula = target ~ zn + indus + nox + age + rad + tax + ptratio +
##
       lstat + medv, family = binomial, data = train)
##
## Deviance Residuals:
##
        Min
                   10
                         Median
                                        30
                                                 Max
## -2.41614 -0.08644
                         0.00002
                                   0.00128
                                             3.08111
##
##
  Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -35.751993
                             6.402055
                                       -5.584 2.34e-08 ***
                             0.032925
                                       -1.387
                                                0.1655
## zn
                -0.045663
## indus
                 0.207458
                             0.086225
                                                0.0161 *
                                        2.406
## nox
                42.641987
                             7.490375
                                        5.693 1.25e-08 ***
                 0.027458
                             0.011021
                                        2.491
                                                0.0127 *
## age
                 0.939777
                             0.193632
                                        4.853 1.21e-06 ***
## rad
## tax
                -0.024982
                             0.005905
                                       -4.230 2.33e-05 ***
                 0.457404
                             0.147306
                                        3.105
                                                0.0019 **
## ptratio
## lstat
                 0.116084
                             0.050509
                                        2.298
                                                0.0215 *
## medv
                                                0.0102 *
                 0.107888
                             0.042022
                                        2.567
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 626.60
                              on 451
                                       degrees of freedom
## Residual deviance: 158.64
                              on 442 degrees of freedom
## AIC: 178.64
##
## Number of Fisher Scoring iterations: 9
```

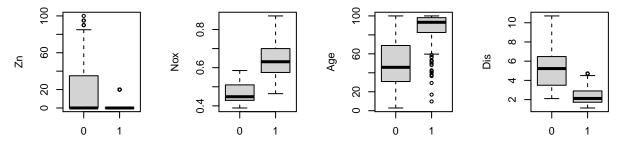
The analysis of deviance table shows further confirms that dropping these 4 variables $\{indus, chas, rm, lstat\}$ either in model 3 or 5 are statistically insignificant and can be dropped.

anova(m5,m1, test="Chi")

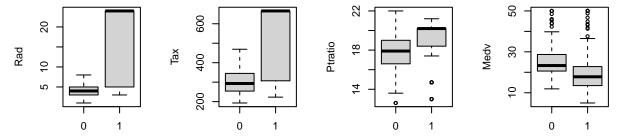
```
## Analysis of Deviance Table
##
  Model 1: target ~ zn + indus + nox + age + rad + tax + ptratio + lstat +
##
##
       medv
## Model 2: target ~ zn + indus + nox + rm + age + dis + rad + tax + ptratio +
##
       1stat + medv
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
           442
                   158.64
## 1
## 2
           440
                   157.53
                            2
                                1.1042
                                         0.5757
```

Model 6 - Transformed Predictors Model

We do a box plot for each predictors used in model m5 to check skewness. Out of the 8 predictors, these 5 predictors $\{zn, nox, rad, tax, Ptratio\}$ are quite skewed. Thus, we shall include log of these predictors in our logistic regression model m5 or m3.



At Risk for High Crime? (0=No, 1:At Risk for High Crime? (0=No, 1:



At Risk for High Crime? (0=No, 1:At Risk for High Crime? (0=No, 1:

Now, we create a new model to include those log transformed predictors. We can see from the summary table the impact of including transformed predictors give lower deviance and lower AIC.

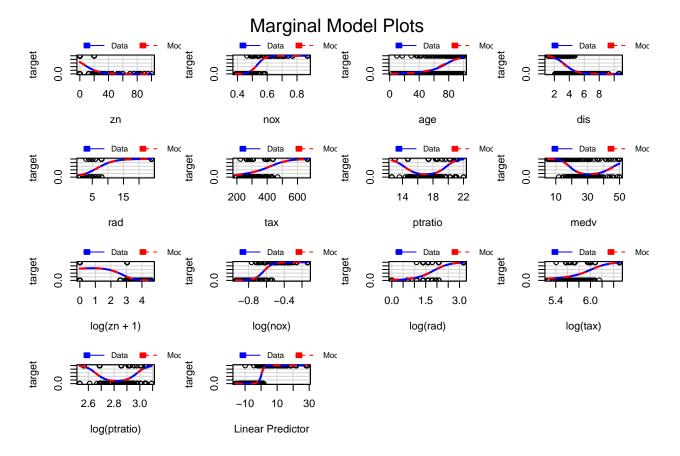
```
m6 = glm(target~zn+nox+age+dis+rad+tax+ptratio+medv+log(zn+1)+log(nox)+log(rad)+log(tax)+log(ptratio),f
summary(m6)
```

##

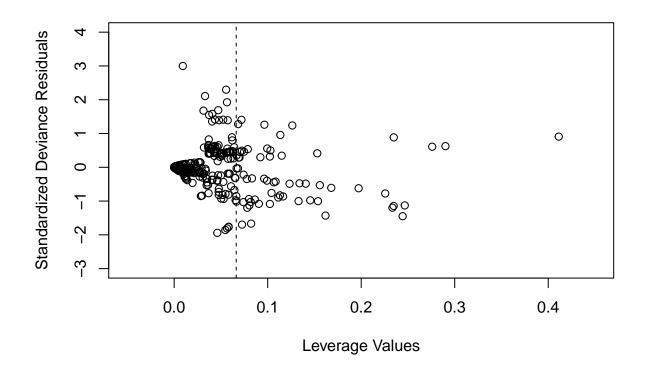
```
## Call:
## glm(formula = target ~ zn + nox + age + dis + rad + tax + ptratio +
      medv + log(zn + 1) + log(nox) + log(rad) + log(tax) + log(ptratio),
       family = binomial(), data = train)
##
##
## Deviance Residuals:
                     Median
      Min
                 10
                                   30
                                           Max
## -1.8952 -0.0908
                      0.0000
                                        4.4420
                               0.0384
##
## Coefficients:
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept) -209.10978 135.24624
                                      -1.546 0.122070
## zn
                 -0.03922
                              0.23346 -0.168 0.866596
## nox
                 254.65099 120.20726
                                        2.118 0.034138 *
                   0.03277
                              0.01316
                                        2.490 0.012765 *
## age
## dis
                   0.30124
                              0.34788
                                        0.866 0.386525
## rad
                   1.17299
                              0.29826
                                        3.933 8.4e-05 ***
## tax
                  -0.14262
                              0.03858
                                       -3.697 0.000218 ***
                              2.28035
                                        2.722 0.006479 **
## ptratio
                   6.20826
## medv
                   0.04257
                              0.05208
                                        0.817 0.413667
## log(zn + 1)
                 -1.08368
                              1.65588 -0.654 0.512825
## log(nox)
                -112.92548
                             63.64789
                                       -1.774 0.076026 .
## log(rad)
                                       -0.297 0.766731
                  -0.32827
                              1.10659
## log(tax)
                  40.22883
                             12.16325
                                        3.307 0.000942 ***
                                      -2.545 0.010917 *
## log(ptratio) -105.88067
                             41.59776
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 626.60 on 451 degrees of freedom
## Residual deviance: 141.42 on 438 degrees of freedom
## AIC: 169.42
##
## Number of Fisher Scoring iterations: 11
```

Next we can check if the logistic regression model m6 is adequate or not by doing marginal model plots. From the figure below, it shows both the loess estimate curve and the fitted values curve are in agreement, and that indicates the model m6 is a valid model.

```
mmps(m6, layout=c(4,4))
```



We can further check the validity of model m6 by plotting leverage values versus standardized deviance. The average leverage is equal to (p + 1)/n = (14 + 1)/466 = 0.032. The p value here is the number of predictors from m6 including the intercept. So the usual cut-off is, 0.064, equal to twice the average leverage value. There are number of high leverage points can be seen in the figure below and can be removed at the data preparation step.



Select Models

we will compare various metrics for all six models. We check models' confusion matrix, accuracy, classification error rate, precision, sensitivity, specificity, F1 score, and AUC.

	Model 1	Model 2	Model 3	Model 4	Model 5	Model 6
Accuracy	0.9181416	0.9269912	0.9247788	0.9181416	0.9247788	0.9424779
Class. Error	0.0818584	0.0730088	0.0752212	0.0818584	0.0752212	0.0575221
Rate						
Sensitivity	0.9162996	0.9162996	0.9207048	0.9162996	0.9207048	0.9251101
Specificity	0.9200000	0.9377778	0.9288889	0.9200000	0.9288889	0.9600000
Precision	0.9203540	0.9369369	0.9288889	0.9203540	0.9288889	0.9589041
F1	0.9183223	0.9265033	0.9247788	0.9183223	0.9247788	0.9417040
AUC	0.9811650	0.9802252	0.9814978	0.9811650	0.9814978	0.9863142

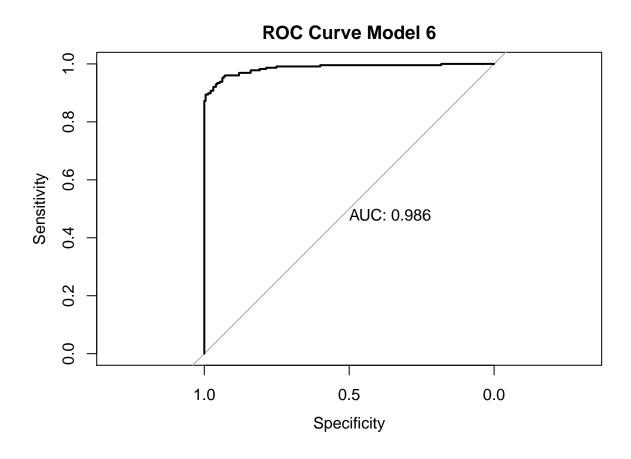
Model 6 performs the highest in all metrics except Class. Error Rate.

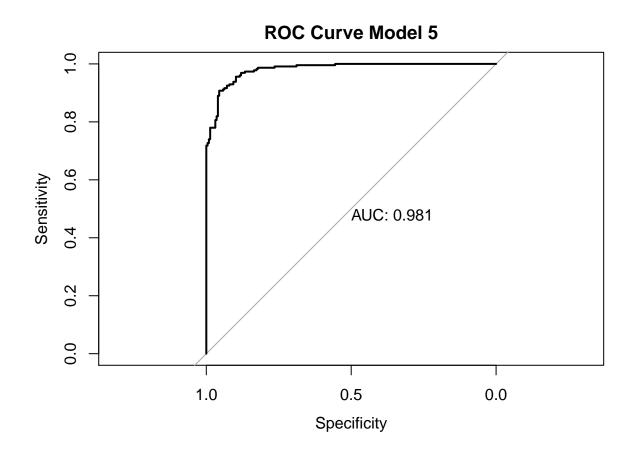
Model 1 and 4 perform the same.

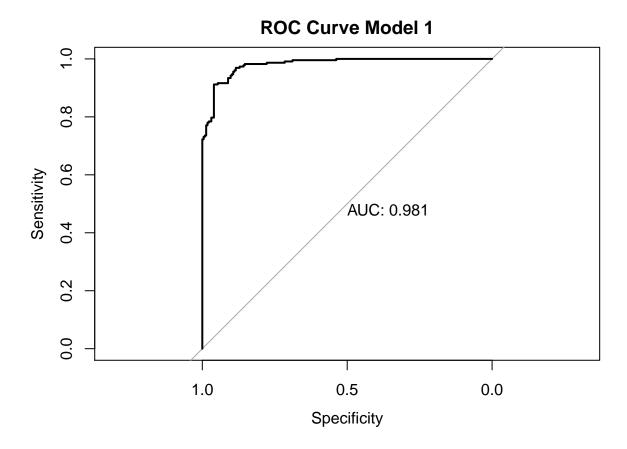
Model 3 and 5 perform the same.

Model 5 is pretty much close to all other metrics.

Let's look at the roc curve to help us make the best selection.







As we can see, the model 6 is the best model. Let's now using the evaluation dataset to evaluate the model.

```
##
      zn indus chas
                      nox
                             rm age
                                         dis rad tax ptratio 1stat medv TARGET
                                                        17.8 4.03 34.7
## 1
         7.07
                  0 0.469 7.185 61.1 4.9671
                                               2 242
## 2
       0
          8.14
                  0 0.538 6.096 84.5 4.4619
                                               4 307
                                                        21.0 10.26 18.2
                                                                              1
                                               4 307
## 3
         8.14
                  0 0.538 6.495 94.4 4.4547
                                                        21.0 12.80 18.4
## 4
       0
          8.14
                  0 0.538 5.950 82.0 3.9900
                                               4 307
                                                        21.0 27.71 13.2
                                                                              1
## 5
         5.96
                  0 0.499 5.850 41.5 3.9342
                                                        19.2 8.77 21.0
                                               5 279
## 6
      25
         5.13
                  0 0.453 5.741 66.2 7.2254
                                               8 284
                                                        19.7 13.15 18.7
## 7
          5.13
                  0 0.453 5.966 93.4 6.8185
                                               8 284
      25
                                                        19.7 14.44 16.0
## 8
          4.49
                  0 0.449 6.630 56.1 4.4377
                                               3 247
                                                        18.5 6.53 26.6
                  0 0.449 6.121 56.8 3.7476
## 9
          4.49
                                               3 247
                                                        18.5 8.44 22.2
## 10
         2.89
                  0 0.445 6.163 69.6 3.4952
                                               2 276
                                                        18.0 11.34 21.4
```

write.csv(evaluation\$TARGET,paste0(getwd(),"/Evaluation_Target.csv"),row.names = FALSE)

Appendix

```
train <- read.csv("https://raw.githubusercontent.com/ahussan/DATA_621_Group1/main/HW3/crime-training-dar
print(head(train, 10))</pre>
```

```
print(colMeans(train))
print(apply(train, 2, sd))
print(apply(train, 2, median))
boxplot(train, use.cols = TRUE)
train.cor = cor(train)
print(train.cor)
corrgram(train, order=TRUE, lower.panel=panel.shade,
  upper.panel=panel.pie, text.panel=panel.txt,
  main="visualize the data in correlation matrices ")
knitr::kable(table(train$target))
plot_histogram(train)
relationships <- train
relationships$chas <- NULL
pairs(train %>% select_if(is.numeric))
#convert features to factor and add a dataset feature
train$chas <- as.factor(train$chas)</pre>
train$target <- as.factor(train$target)</pre>
train$dataset <- 'train'</pre>
plotfontsize <- 8</pre>
train_int_names <- train %>% select_if(is.numeric)
int_names <- names(train_int_names)</pre>
for (i in int_names) {
  assign(paste0("var_",i), ggplot(train, aes_string(x = train$target, y = i)) +
          geom_boxplot(color = 'steelblue',
                       outlier.color = 'firebrick',
                       outlier.alpha = 0.35) +
#scale_y_continuous
          labs(title = paste0(i,' vs target'), y = i, x= 'target') +
          theme_minimal() +
          theme(
            plot.title = element_text(hjust = 0.45),
            panel.grid.major.y = element_line(color = "grey", linetype = "dashed"),
            panel.grid.major.x = element_blank(),
            panel.grid.minor.y = element_blank(),
            panel.grid.minor.x = element_blank(),
            axis.ticks.x = element line(color = "grey"),
            text = element_text(size=plotfontsize)
          ))
gridExtra::grid.arrange(var_age, var_dis, var_indus,var_lstat,
                        var_medv,var_nox,var_ptratio,var_rad,
                        var_rm, var_tax, var_zn, nrow=4)
numeric_values <- train %>% select_if(is.numeric)
```

```
train_cor <- cor(numeric_values)</pre>
corrplot.mixed(train_cor, tl.col = 'black', tl.pos = 'lt')
test_url <- 'https://raw.githubusercontent.com/ahussan/DATA_621_Group1/main/HW3/crime-evaluation-data_m
test <- read.csv(test_url, header=TRUE)</pre>
trainchas <- as.factor(train$chas)</pre>
train$chas <- NULL
traintarget <- as.factor(train$target)</pre>
train$target <- traintarget</pre>
testchas <- as.factor(test$chas)</pre>
test$chas <- NULL
attach(train)
p0 <- ggplot(train, aes(factor(target), indus)) + geom_boxplot()</pre>
train <- train[-which(target==0 & indus > 20),]
p1 <- ggplot(train, aes(factor(target), indus)) + geom_boxplot()</pre>
grid.arrange(p0, p1,ncol=2,nrow=1)
detach(train)
attach(train)
p0 <- ggplot(train, aes(factor(target), dis)) + geom_boxplot()</pre>
train <- train[-which(target==0 & dis > 11),]
train <- train[-which(target==1 & dis > 7.5),]
p1 <- ggplot(train, aes(factor(target), dis)) + geom_boxplot()</pre>
grid.arrange(p0, p1, ncol=2,nrow=1)
detach(train)
names(train)
dim(train)
m1 = glm(target ~ zn + indus + nox + rm + age + dis + rad + tax + ptratio + lstat + medv, data=train, f
summary(m1)
m2 = glm(target ~ indus + nox + age + rad + tax + ptratio + lstat + medv, data=train, family=binomial)
summary(m2)
m3 = stepAIC(m1, direction='backward', trace=FALSE)
summary(m3)
m4 = stepAIC(m1, direction='forward', trace=FALSE)
summary(m4)
m5 = stepAIC(m1, direction='both', trace=FALSE)
summary(m5)
anova(m5,m1, test="Chi")
par(mfrow=c(2,4))
boxplot(zn~target, ylab="Zn",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
boxplot(nox~target, ylab="Nox",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
```

```
boxplot(age~target, ylab="Age",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
boxplot(dis~target, ylab="Dis",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
boxplot(rad~target, ylab="Rad",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
boxplot(tax~target, ylab="Tax",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
boxplot(ptratio~target, ylab="Ptratio",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
boxplot(medv~target, ylab="Medv",xlab="At Risk for High Crime? (0=No, 1=Yes)", data=train)
m6 = glm(target~zn+nox+age+dis+rad+tax+ptratio+medv+log(zn+1)+log(nox)+log(rad)+log(tax)+log(ptratio),f
summary(m6)
mmps(m6, layout=c(4,4))
hvalues <- influence(m6)$hat
stanresDeviance <- residuals(m6)/sqrt(1-hvalues)</pre>
plot(hvalues, stanresDeviance, ylab="Standardized Deviance Residuals", xlab="Leverage Values", ylim=c(-3,4)
abline(v=2*15/length(train$target),lty=2)
# comparing all models using various measures
CM1 <- confusionMatrix(as.factor(as.integer(fitted(m1) > .5)), as.factor(m1$y), positive = "1")
CM2 <- confusionMatrix(as.factor(as.integer(fitted(m2) > .5)), as.factor(m2\$y), positive = "1")
CM3 <- confusionMatrix(as.factor(as.integer(fitted(m3) > .5)), as.factor(m3$y), positive = "1")
CM4 <- confusionMatrix(as.factor(as.integer(fitted(m4) > .5)), as.factor(m4$y), positive = "1")
CM5 <- confusionMatrix(as.factor(as.integer(fitted(m5) > .5)), as.factor(m5$y), positive = "1")
CM6 <- confusionMatrix(as.factor(as.integer(fitted(m6) > .5)), as.factor(m6$y), positive = "1")
Roc1 <- roc(train$target, predict(m1, train, interval = "prediction"))</pre>
Roc2 <- roc(train$target, predict(m2, train, interval = "prediction"))</pre>
Roc3 <- roc(train$target, predict(m3, train, interval = "prediction"))</pre>
Roc4 <- roc(train$target, predict(m4, train, interval = "prediction"))</pre>
Roc5 <- roc(train$target, predict(m5, train, interval = "prediction"))</pre>
Roc6 <- roc(train$target, predict(m6, train, interval = "prediction"))</pre>
metrics1 <- c(CM1$overall[1], "Class. Error Rate" = 1 - as.numeric(CM1$overall[1]), CM1$byClass[c(1, 2,
metrics2 <- c(CM2$overall[1], "Class. Error Rate" = 1 - as.numeric(CM2$overall[1]), CM2$byClass[c(1, 2,
metrics3 <- c(CM3$overall[1], "Class. Error Rate" = 1 - as.numeric(CM3$overall[1]), CM3$byClass[c(1, 2,
metrics4 <- c(CM4$overall[1], "Class. Error Rate" = 1 - as.numeric(CM4$overall[1]), CM4$byClass[c(1, 2,</pre>
metrics5 <- c(CM5$overall[1], "Class. Error Rate" = 1 - as.numeric(CM5$overall[1]), CM5$byClass[c(1, 2,
metrics6 <- c(CM6$overall[1], "Class. Error Rate" = 1 - as.numeric(CM6$overall[1]), CM6$byClass[c(1, 2,</pre>
kable(cbind(metrics1, metrics2, metrics3, metrics4, metrics5, metrics6), col.names = c("Model 1", "Mode
 kable styling(full width = T)
# plotting roc curve of model 6
plot(roc(train$target, predict(m6, train, interval = "prediction")), print.auc = TRUE, main='ROC Curve
# plotting roc curve of model 5
plot(roc(train$target, predict(m5, train, interval = "prediction")), print.auc = TRUE, main='ROC Curve
```

```
# plotting roc curve of model 4
plot(roc(train$target, predict(m4, train, interval = "prediction")), print.auc = TRUE, main='ROC Curve

evaluation <- read.csv("https://raw.githubusercontent.com/ahussan/DATA_621_Group1/main/HW3/crime-evaluation$TARGET <- predict(m6, evaluation, type="response")
    evaluation$TARGET <- ifelse(evaluation$TARGET > 0.5, 1, 0)
    print(head(evaluation,10))

write.csv(evaluation$TARGET,paste0(getwd(),"/Evaluation_Target.csv"),row.names = FALSE)
```