

Cost Function (Squared Error Function)

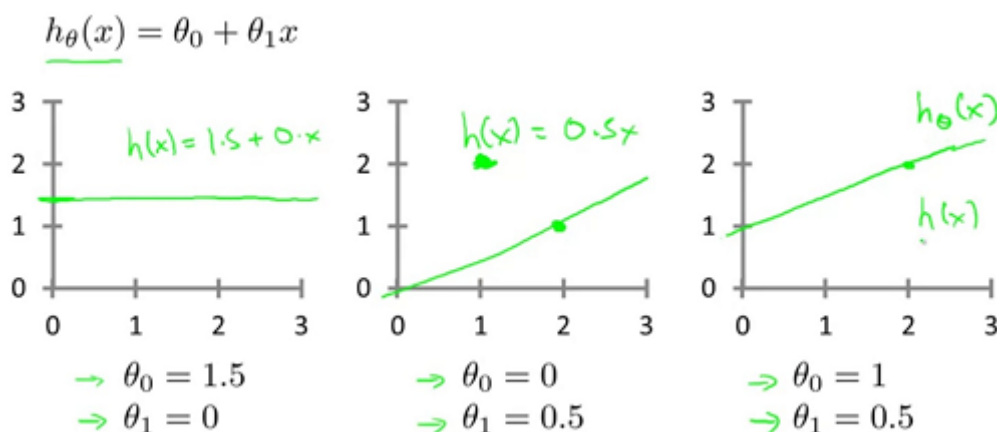
In linear progression, we have a training set. And the form of our hypothesis (h_θ), which we use to make predictions is the linear function: $h_\theta(x) = \theta_0 + \theta_1 x$.

$$\text{Hypothesis: } h_\theta(x) = \theta_0 + \theta_1 x$$

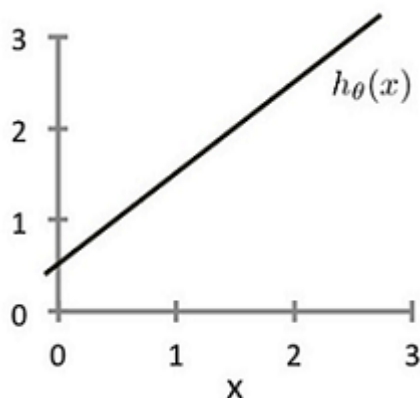
θ_i 's: Parameters

How to choose θ_i 's?

With different choices of the parameter's θ_0 and θ_1 , we get different hypothesis, different hypothesis functions.



Video Question: Consider the plot below of $h_\theta(x) = \theta_0 + \theta_1 x$. What are θ_0 and θ_1 ?



$$\theta_0 = 0, \theta_1 = 1$$

$$\theta_0 = 0.5, \theta_1 = 1$$

$$\theta_0 = 1, \theta_1 = 0.5$$

$$\theta_0 = 1, \theta_1 = 1$$

In linear regression, we have a training set and what we want to do, is come up with values for the parameters θ_0 and θ_1 so that the straight line we get, corresponds to a straight line that somehow fits the data well. So, how do we come up with values, θ_0 , θ_1 , that corresponds to a good fit to the data? The idea is we get to choose our parameters θ_0 , θ_1 so that $h_\theta(x)$ is close to "y" for our training examples (x, y) . In our training set, we've given a number of examples where we know x decides the wholes and we know the actual price is was sold for.

In linear regression, what we're going to do is, we're going to want to solve a **minimization problem**. We want to minimize the sum of my training set, sum from $i = 1, \dots, M$, of the difference of the squared error, the square difference between the predicted price of a house, and the price that it was actually sold for.

$$\boxed{\text{minimize } \theta_0, \theta_1} \quad \frac{1}{2m} \sum_{i=1}^m \left(\underbrace{h_{\theta}(x^{(i)})}_{\theta_0 + \theta_1 x^{(i)}} - y^{(i)} \right)^2$$

#training examples

By convention we usually define a **cost function**, and what we want to do is minimize over θ_0 and θ_1 . This cost function is also called the **squared error function**. When sometimes called the **squared error cost function** and it turns out that why do we take the squares of the errors. It turns out that the squared error cost function is a reasonable choice and works well for problems for most regression programs.

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

minimize $J(\theta_0, \theta_1)$
 θ_0, θ_1 Cost function
 Squared error function

Summary

We can measure the accuracy of our hypothesis function by using a cost function. This takes an average difference (actually a fancier version of an average) of all the results of the hypothesis with inputs from x 's and the actual output y 's.

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (\hat{y}_i - y_i)^2 = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x_i) - y_i)^2$$

To break it apart, it is $\frac{1}{2} \bar{x}$ where \bar{x} is the mean of the squares of $h_{\theta}(x_i) - y_i$, or the difference between the predicted value and the actual value. This function is otherwise called the **"Squared error function"**, or **"Mean squared error"**. The mean is halved ($\frac{1}{2}$) as a convenience for the computation of the **gradient descent**, as the derivative term of the square function will cancel out the $\frac{1}{2}$ term. The following image summarizes what the cost function does:

