Genome Assembly

From theory to practice (and back)



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Outline

- 1. The problem
- 2. Practical issues
- 3. Theoretical problem formulations
- 4. Practical genome assembly
 - Contig assembly
 - Scaffolding
 - Gap filling
- 5. And back: a more "practical" theoretical formulation

LECTURE
Theory + Abstract view



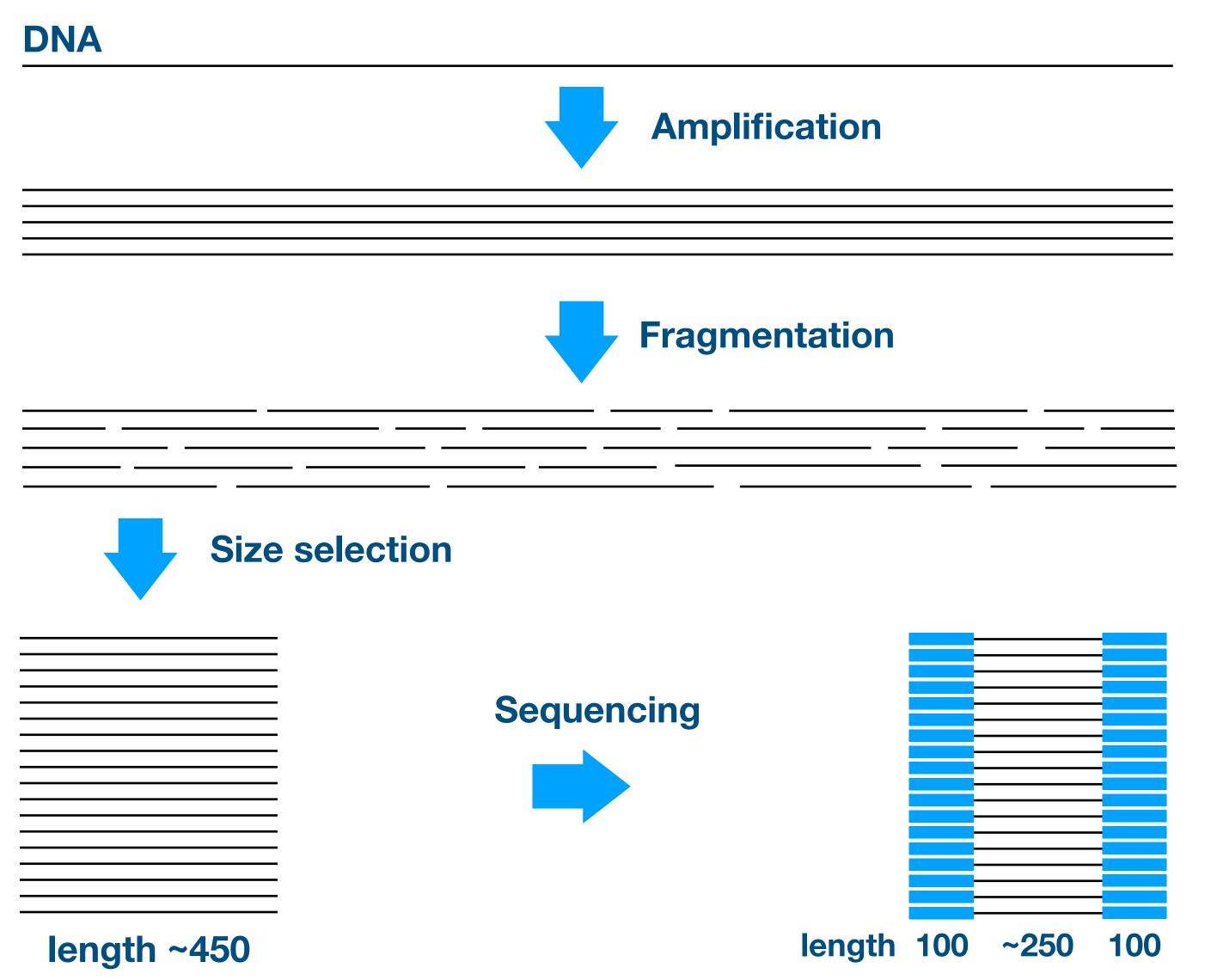
ASSIGNMENT
Practical + Hands-on view

The problem

(A general description of the input and output)

Short-read sequencing

(Third-generation sequencing)



INPUT: A collection of paired-end reads

OUTPUT: The genome from which they were sequenced

(we will see precise computational formulations later)

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ACTAGTGCTAGATGCTCGAGCTAGCT

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(we will see precise computational formulations later)

•		•	CTAGC
		•	- CTAGC
			GAGCT
			GCTCG
		•	GCTAG
			AGCTA
			TCGAG
			TAGCT
			CTAGC
			CTAGC
			GAGCT
		•	- CGAGC
		•	CTAGC
			TAGCT
			GCTCG
			TGCTA

Practical issues

(several of which are not covered in this course)



• If every substring of the genome of length = read length - 1 is unique, then assembly is trivial

AATTGAATTTACACCAC

```
AATTGA
TGAAT
TGAAT
GAATT
GAATT
AATTT
ATTTA
TTTAC
TTACA
TACAC
ACACC
ACACC
ACACCA
ACCAC
```



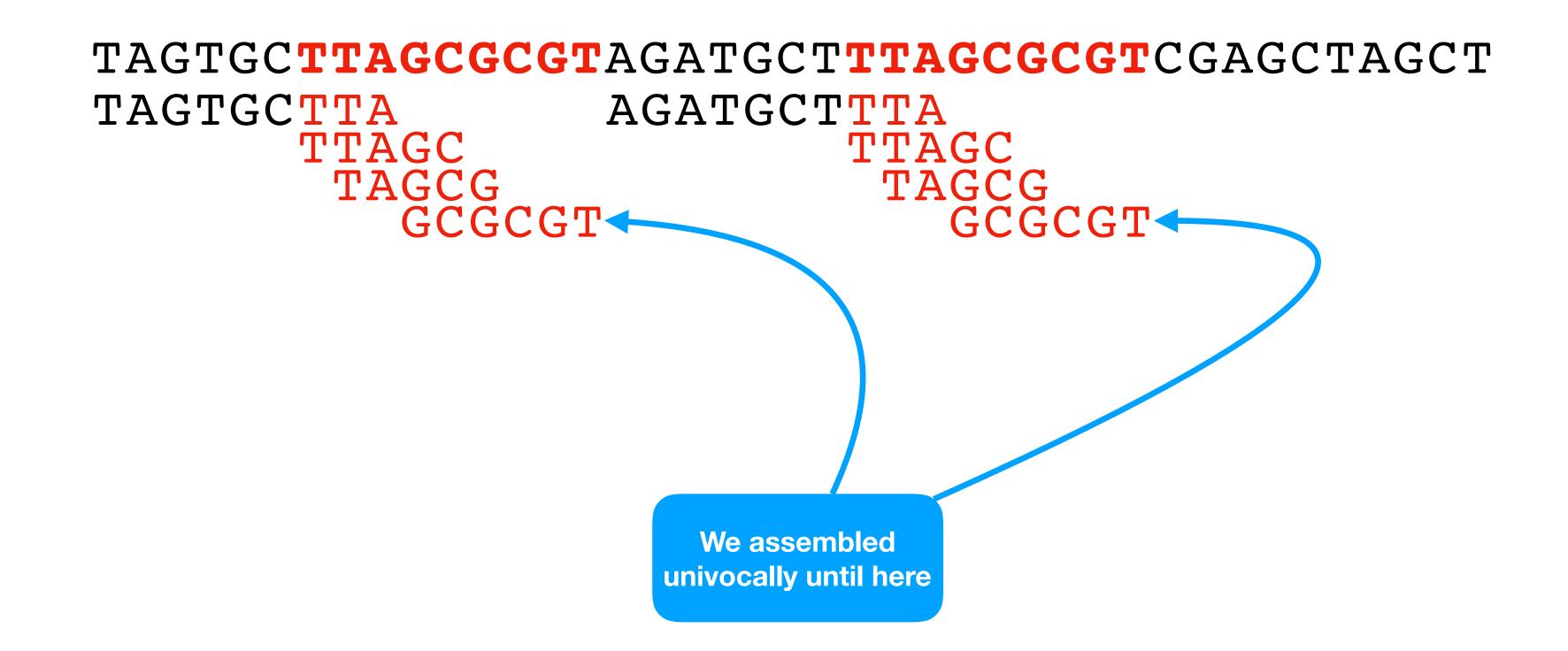
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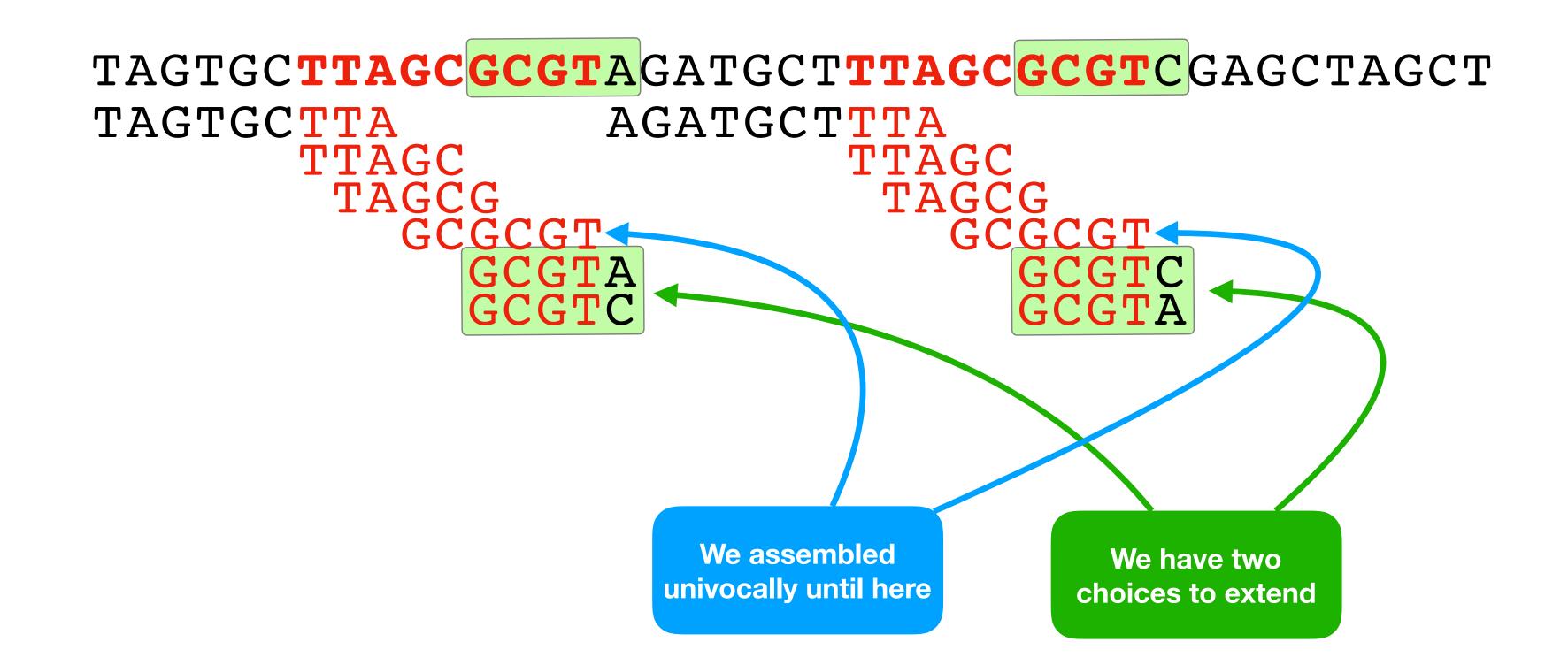


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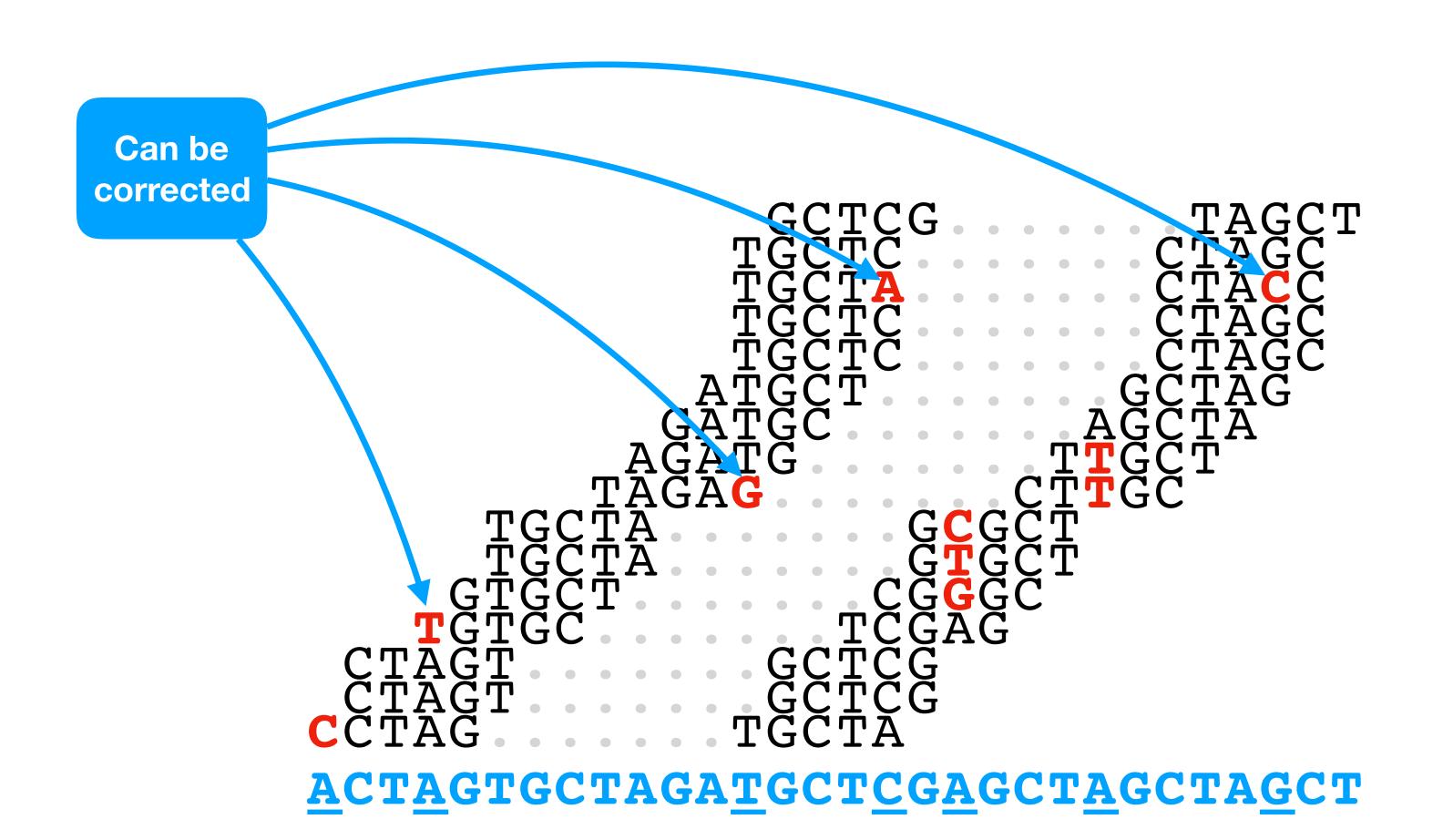


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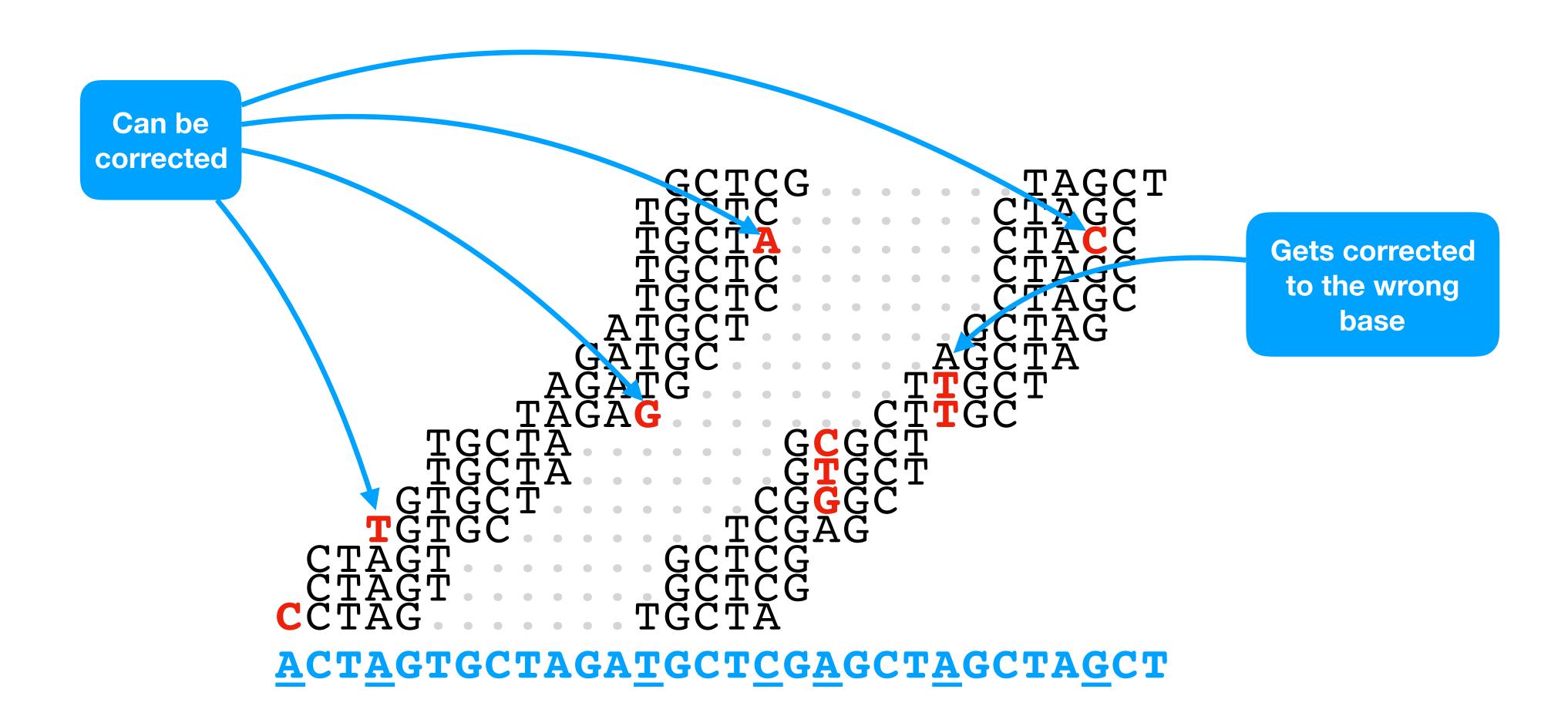


ASSIGNMENT

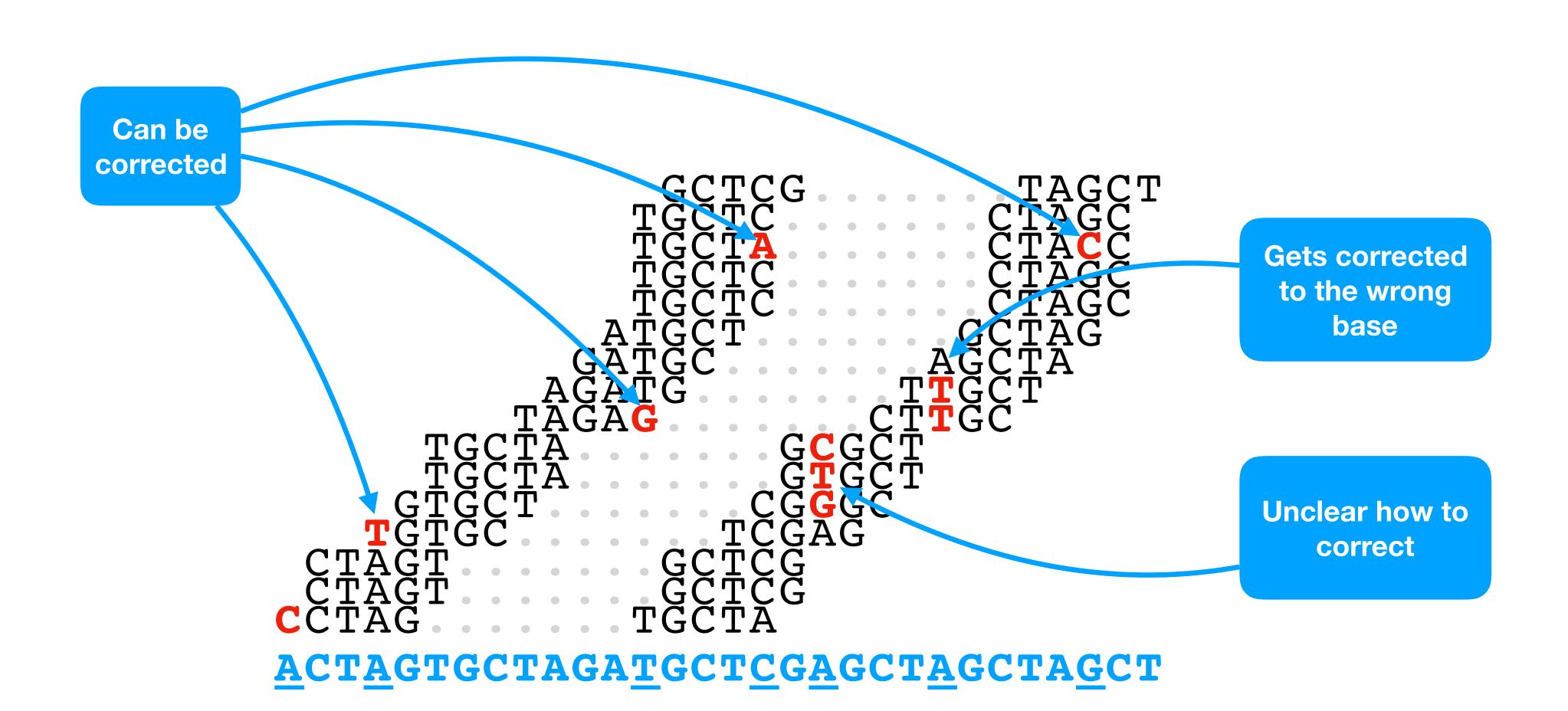




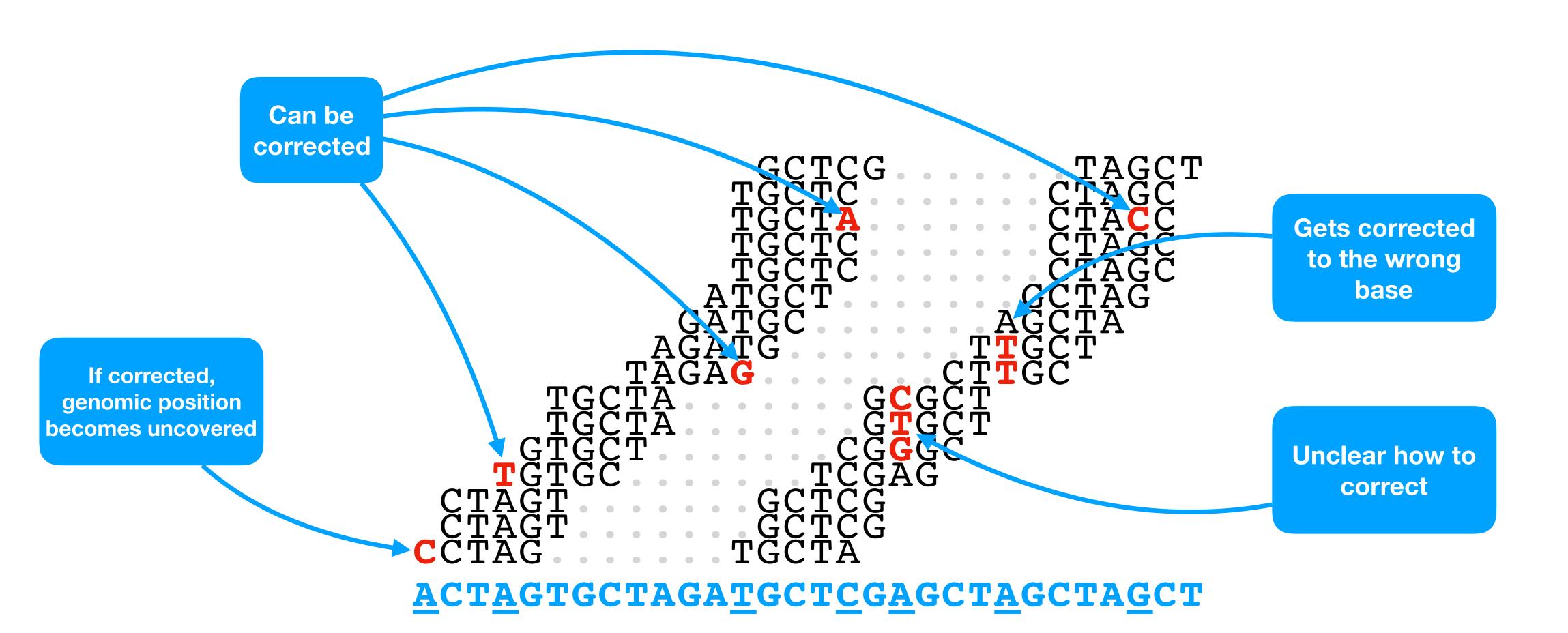












Polyploidy

LATER IN THE LECTURE

Mother ACTACTGCTAGAAGCTCGAGCTAGCTAGCT
Father ACTAGTGCTAGATGCTCGAGCTAGCTAGCT

Polyploidy

LATER IN THE LECTURE

```
GCTCG TAGCC
CTAGCC
CTAGCC
CTAGCC
CTAGCC
CTAGCC
CTAGCC
CTAGCC
CCTAGC
CCTAGC
AGCTC
AGCTC
AGCTA
AGCTA
CCTAGC
CTAGC
CTAGC
CCTAGC
CCTAGC
CCTAGC
CCTAGC
CCTAGC
CCTAGC
CCTAGC
CCTAGC
CCTAGC
ACCTC
CCTAGC
CCTAGC
ACCTC
ACCT
ACCTC
ACCT
```

Mother ACTACTGCTAGAAGCTCGAGCTAGCTAGCT
Father ACTAGTGCTAGATGCTCGAGCTAGCTAGCT

- Sequencing errors + polyploidy at the same time
- Phasing SNPs (C and A from same haplotype, NOT e.g. C and T) is a separate problem, called haplotype assembly or haplotype phasing

Unsequenced areas

```
GCTCG TAGCT
TGCTC CTAGC
TGCTC CTAGC
TGCTC CTAGC
CTAGC
CTAGC
CTAGC
CTAGC
ATGCT AGCTA
AGATG TAGCT
TAGAT
TAGAT
```

```
CTAGT GCTCG
CTAGT GCTCG
ACTAG TGCTA

ACTAGT TAGATGCTCG CTAGCTAGCT
```

Non uniform paired-end distance

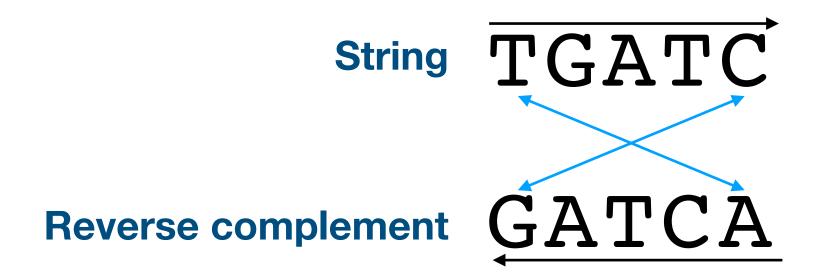
```
GCTCG TAGCT
TGCTC CTAGC
TGCTC CTAGC
TGCTC CTAGC
TGCTC CTAGC
TGCTC CTAGC
TGCTC AGCTAG
AGATG AGCTA
TGCTA TCGAG
TGCTA TCGAGCT
TGCTA TCGAGCT
AGTGC ATGCT
AGTGC ATGCT
AGTGC ATGCT
ACTAGT AGATG
ACTAGT AGATG
ACTAGTGCTAGATGCTCGAGCTAGCT
```

• Distance between each pair not known "exactly" from sequencer

Double-stranded DNA

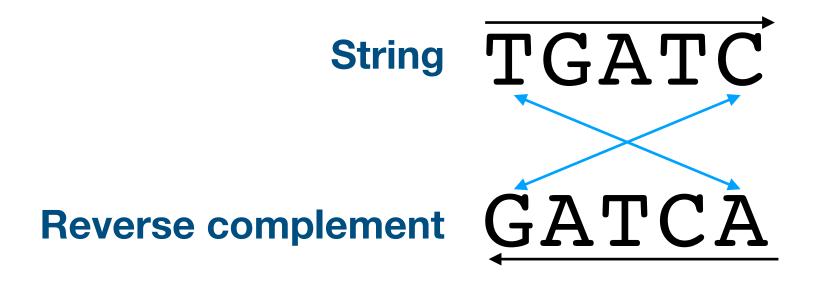
NOT IN THE LECTURE

Reads consist of strings and their reverse complements:



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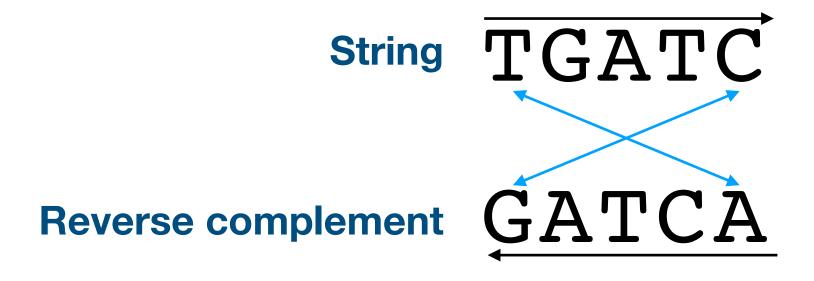


TGCTA GAGCT TGCTA CGAGCT CGAGC AGTGC TCGAG CTAGT GCTCG CTAGT GCTCG ACTAG TGCTA
ACTAGTGCTAGATGCTCGAGCT
TGATCACGATCTACGAGCTCGA
ACGAT CTCGA CTCGA CTCGA CTCGA GCTCG GCTCG GCTCG GCTCG GCTCG GATCA CGAGC CGAGC TGATC ACGAG

NOT IN THE LECTURE

Double-stranded DNA

Reads consist of strings and their reverse complements:



TGCTA TGCTA GAGCT GAGCT CGAGC CGAGC TCGAG	
ACTAGTGCTAGATGCTCGAGCT	
TGATCACGATCTACGAGCTCGA	
ACGAT CTCGA CTCGA CTCGA CACGA GCTCG TCACGA GCTCG GATCA CGAGC GATCA CGAGC TGATC ACGAG	

TGCTATGCTAGCTAGCTAGCTAGCTAGCTAGCTAGCTAGC	•	•	•	•	•	CTGG	AGGACTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT	CUUUU
			??	?				
AGCTC AGCTCG CCACC	•	•	•	•	•	T A C	GCA GCA GCA GCA	A C C

Large amount of data



	Genome length	Total bases at 30x coverage	Size if each base takes 2 bits
E. coli	4.6 • 10 ⁶	138 • 106	34 MBytes
Human	3.2 · 10 ⁹	96 • 10 ⁹	24 GBytes
Spruce	25 · 10 ⁹	750 · 10 ⁹	187.5 GBytes
Axoloti	32 · 10 ⁹	960 • 10 ⁹	240 GBytes

Theoretical problem formulations

("Classical" computational formulations of how to obtain the output from the input)

INPUT: A collection of strings (the reads)

OUTPUT: A string S such that every given string is a substring of S (S is a superstring),

and S is shortest

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TAGA ATAG CATA TCAT

TCATAGA

Input

Output S

A collection of strings (the reads) INPUT:

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TAGA
ATAG
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Input
Output S

- NP-hard to compute (i.e. it cannot be solved efficiently)
- Not practical: it collapses repeats (main drawback)

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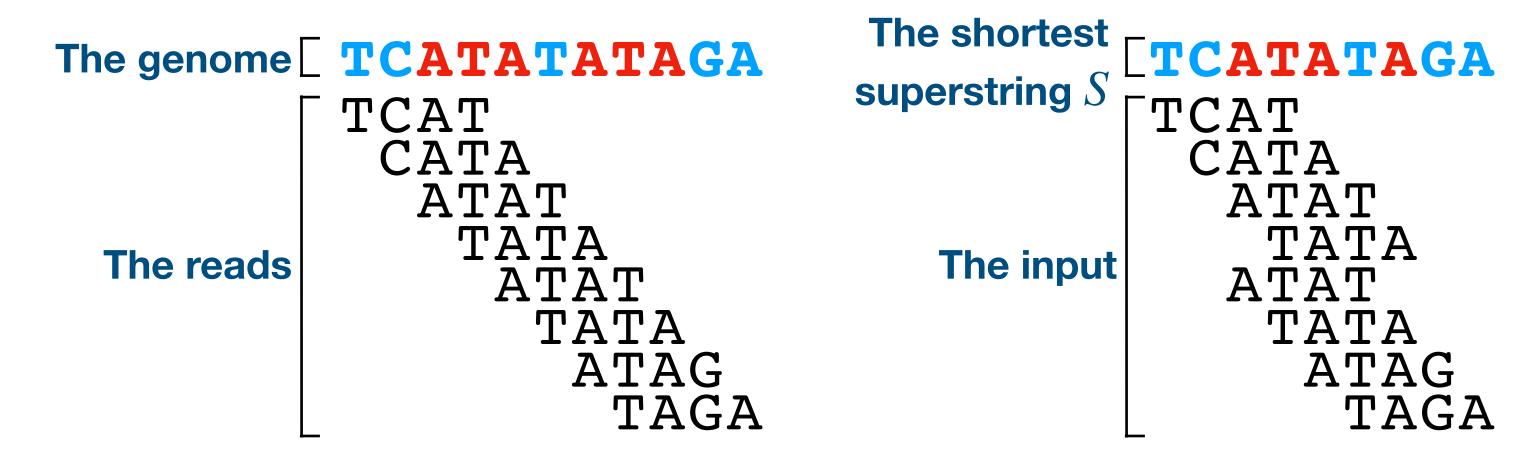
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Overlap graphs + Hamiltonian path

ACTAGACTAGACC ACTA

Overlap graphs + Hamiltonian path

ACTAGAC TAGAC C

INPUT: Overlap graph of order *t*:

- Every read is a node
- Every suffix-prefix overlap of length $\geq t$ is an edge

OUTPUT: A path going through every node (i.e. read) exactly one (*Hamiltonian*)

Overlap graphs + Hamiltonian path

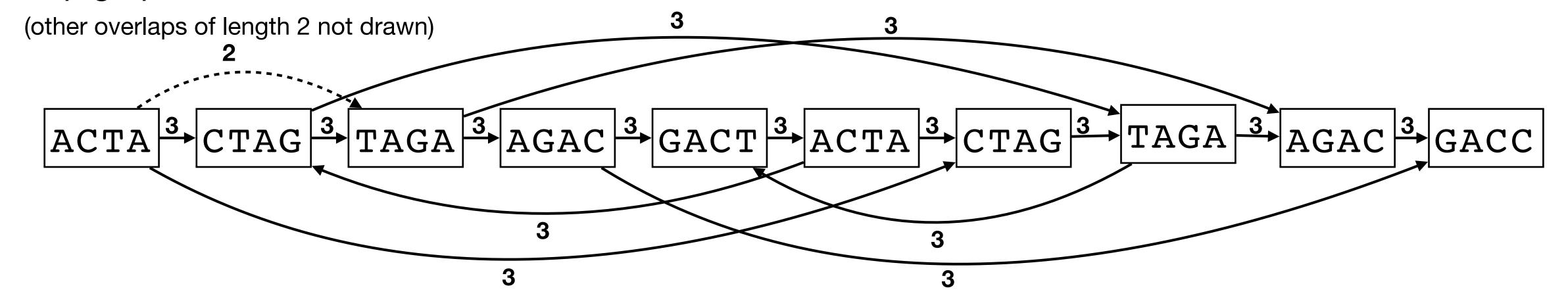
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Overlap graph of order 2:



Overlap graphs + Hamiltonian path

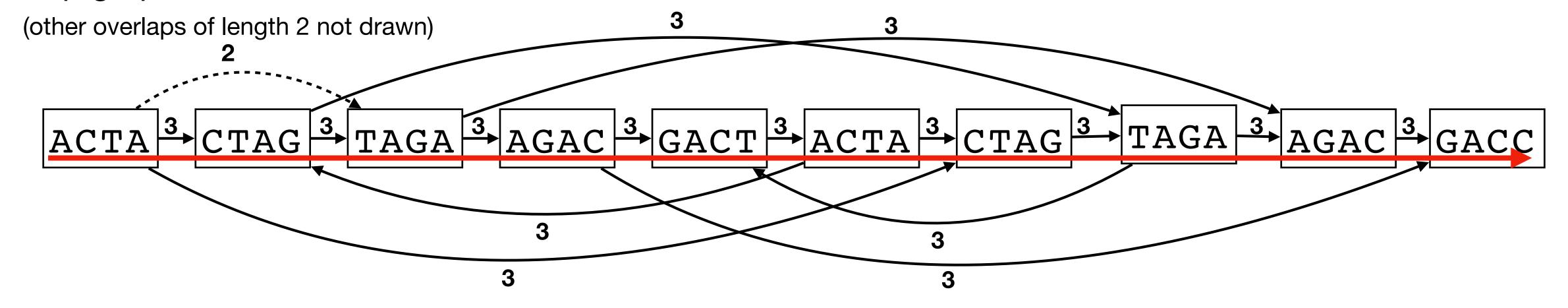
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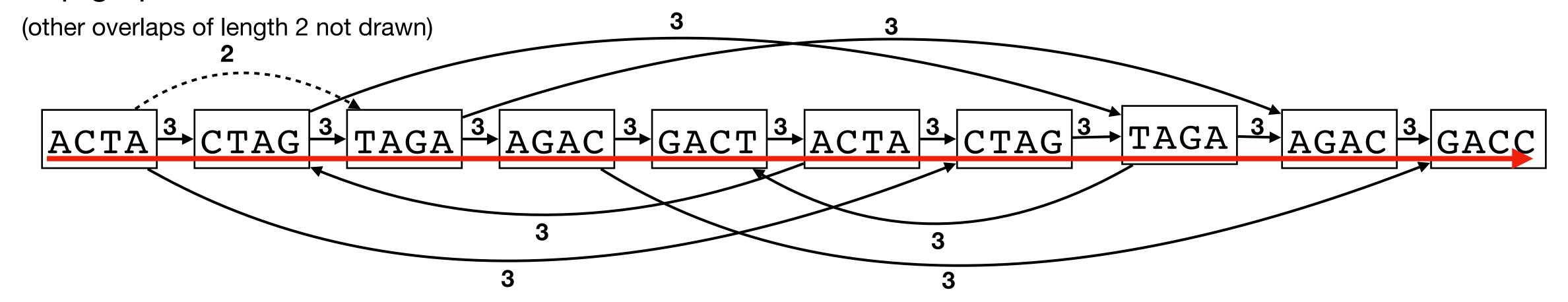
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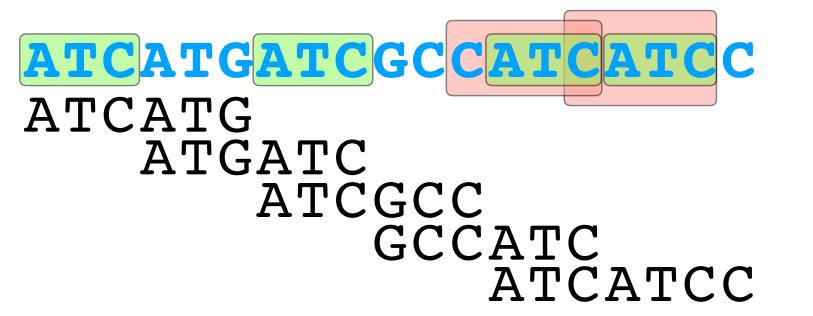
OUTPUT: A path going through every node (i.e. read) exactly one (*Hamiltonian*)

- NP-hard to compute
- Not practical: usually graph has no Hamiltonian path (missing coverage, errors)

Overlap graph of order 2:



```
ATCATGATCGCCATCATCC
ATCATG
ATGATC
ATCGCC
ATCGCC
ATCATCC
ATCATCC
```

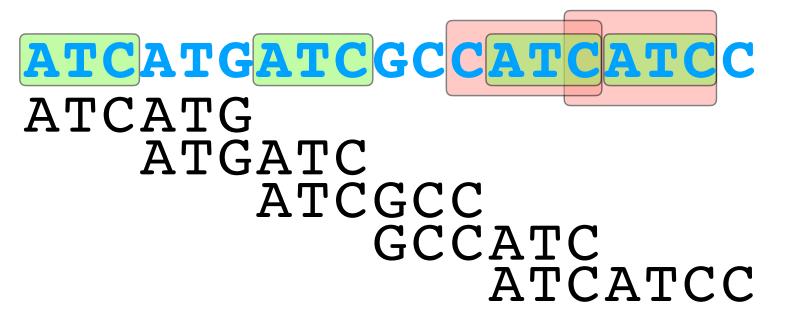


INPUT: De Bruijn graph of order k:

- Every k-mer (substring of length k) in the reads is a **single** node
- Every (k+1)-mer is a *different* arc from its length-k prefix to its length-k suffix

ASSUMPTION: Every length-k interval of the genome appears exactly the same number of times in the reads (*uniform coverage*)

OUTPUT: A path going through every **edge** (i.e. k-mer) exactly one (*Eulerian*)

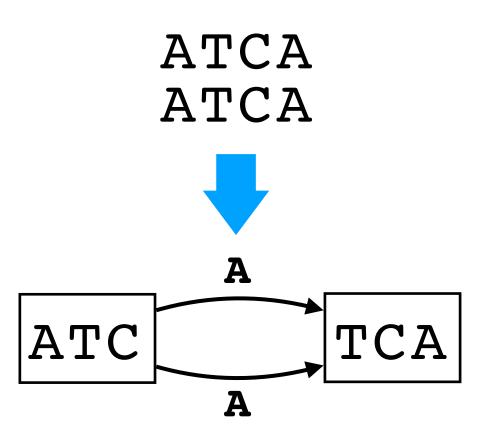


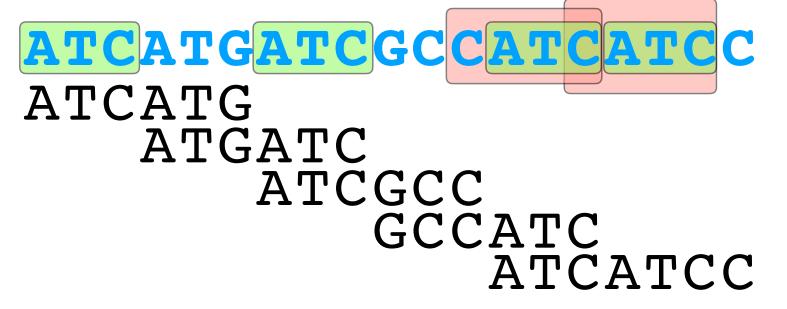
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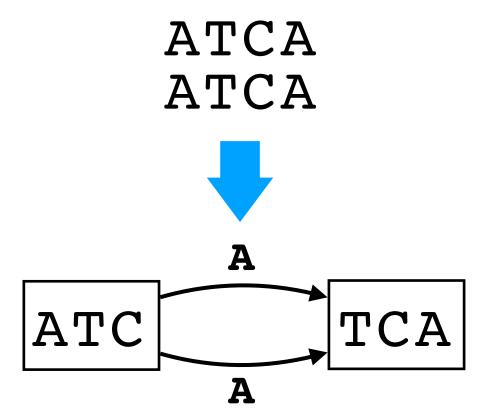
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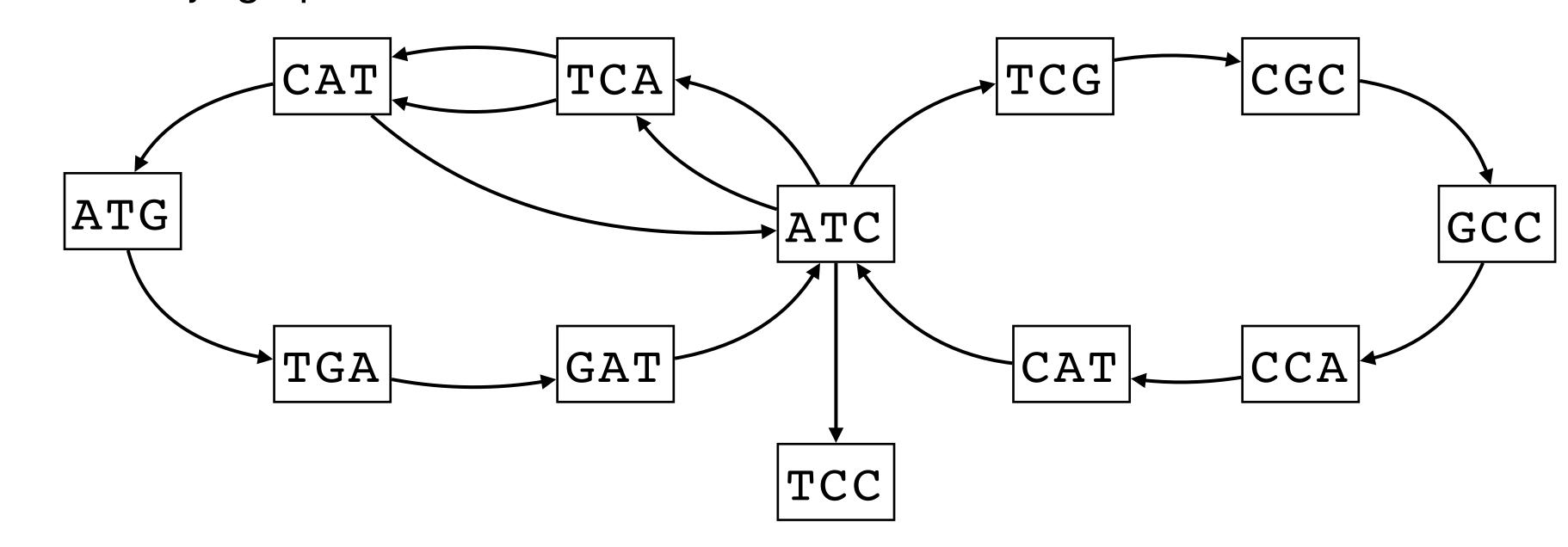
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De Bruijn graph of order 3:







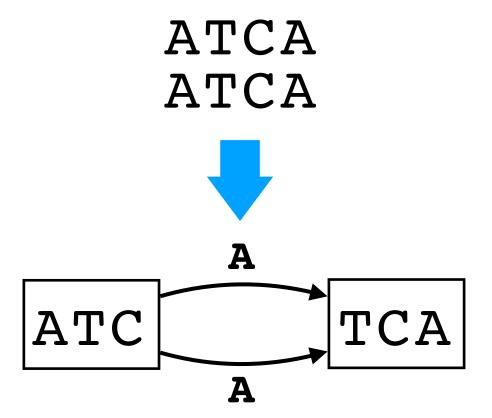
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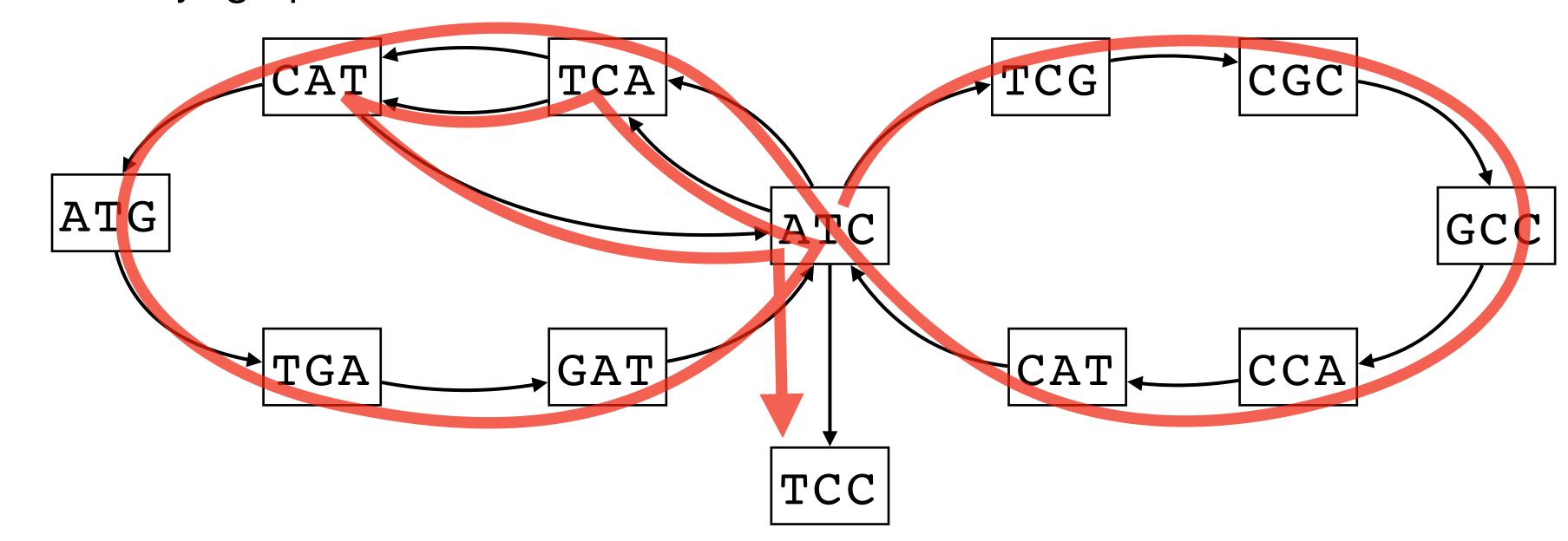
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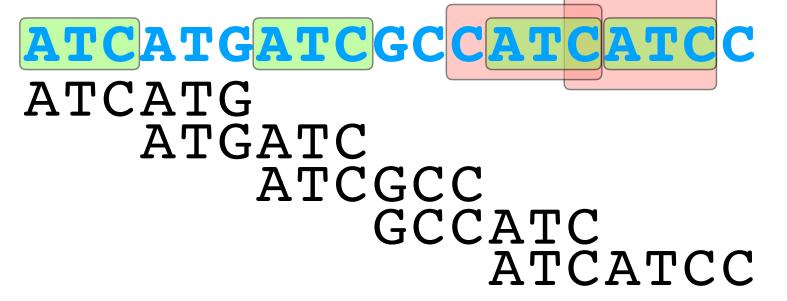
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De Bruijn graph of order 3:







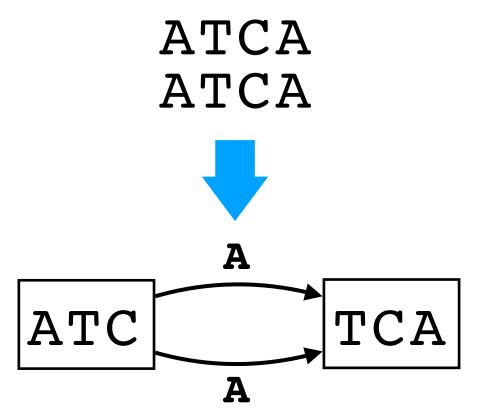
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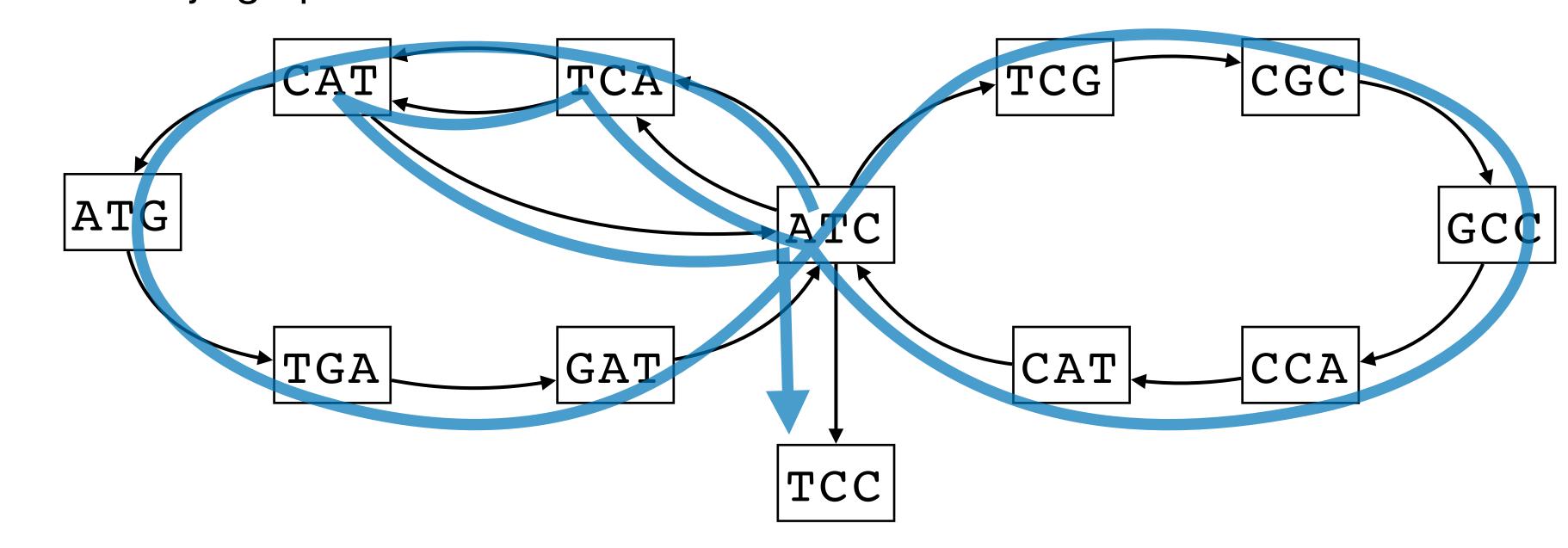
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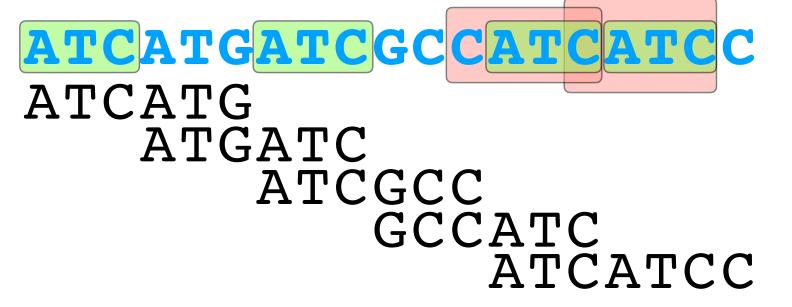
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De Bruijn graph of order 3:







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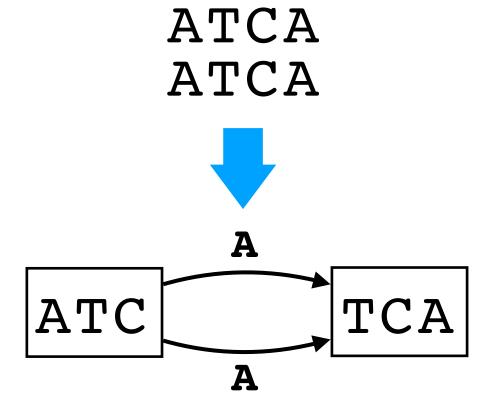
TCA

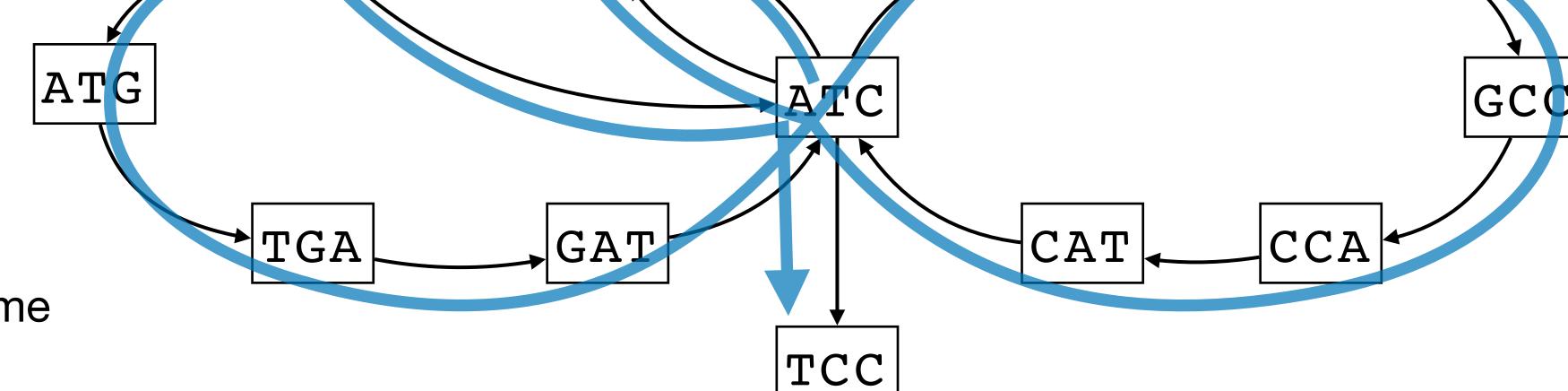
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De Bruijn graph of order 3:





CGC

TCG

- Can be solved in O(|edges|) time
- Too restrictive assumption

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- Computational complexity ranges from NP-hard to linear
- Not robust to practical issues, and hard to integrate them into the formulations
- Most importantly (even if the above are solved):
 - Many solutions, which one is the true genome?
 - ► We will see a different "theoretical" approach, closer to practice AT END OF LECTURE

Practical genome assembly

(The sequence of algorithmic steps behind "real" genome assemblers)

Focus on single-end reads

Assembling a full genomic sequence in one shot is hopeless



Forget about the assembly model (i.e. the problem formulation)

Focus on single-end reads

Assembling a full genomic sequence in one shot is hopeless



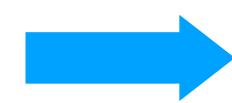
Forget about the assembly model (i.e. the problem formulation)

Assemble only parts about which we are sure (contigs → contiguous sequences)

• Assume an assembly graph (here de Bruijn with parallel edges collapsed into one)

Focus on single-end reads

Assembling a full genomic sequence in one shot is hopeless

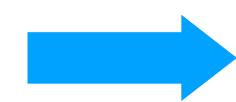


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- Unitig =_{def} "non-branching" path

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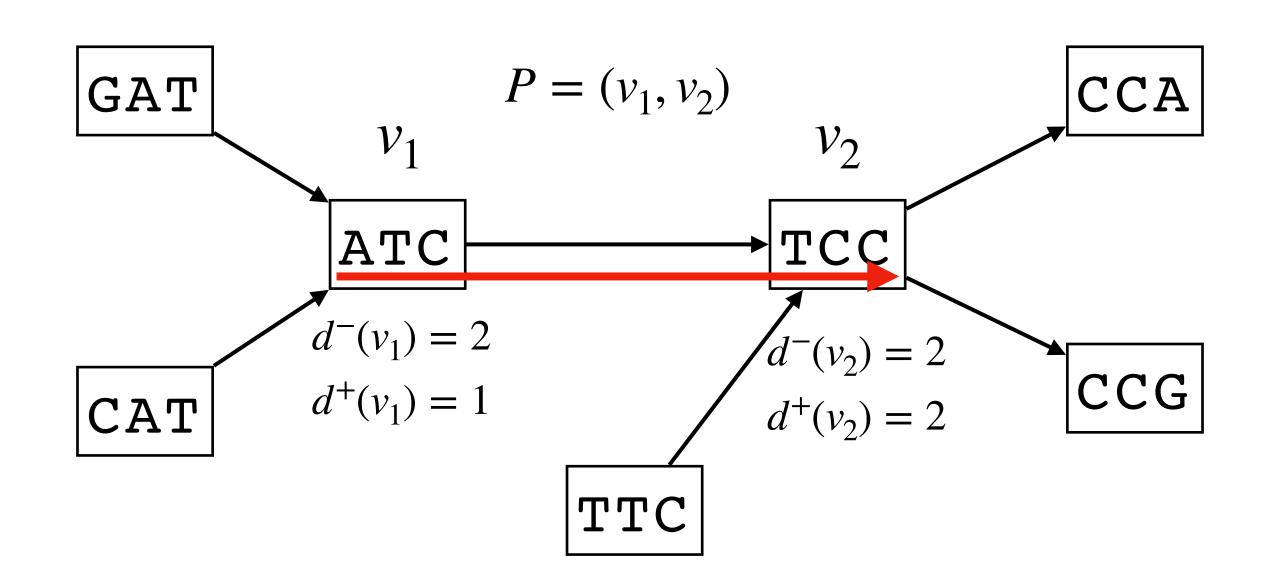
- Assume an assembly graph (here de Bruijn with parallel edges collapsed into one)
- Focus on *unitigs*: non-branching paths
- Unitig =_{def} "non-branching" path
- (Usually) Contig = def unitig in a graph "corrected" for polyploidy

• Let $P = (v_1, v_2, ..., v_{t-1}, v_t)$ be a path. We say that P is a *unitig* if either:

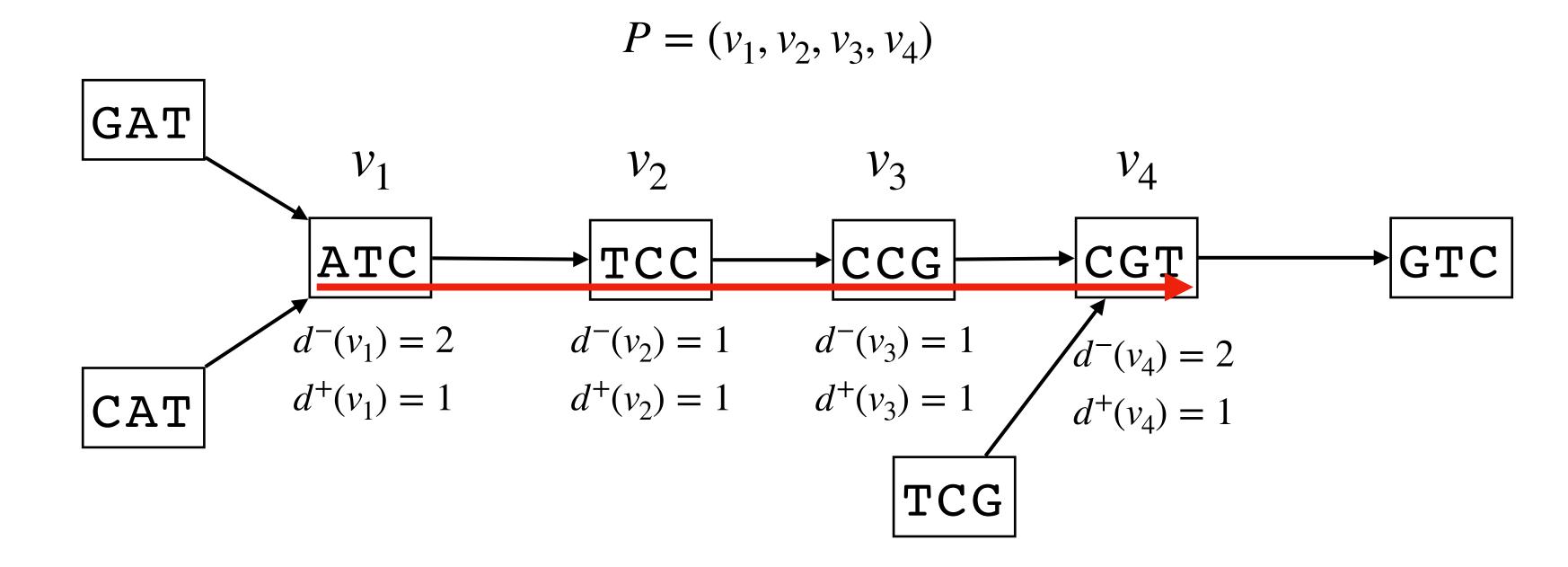
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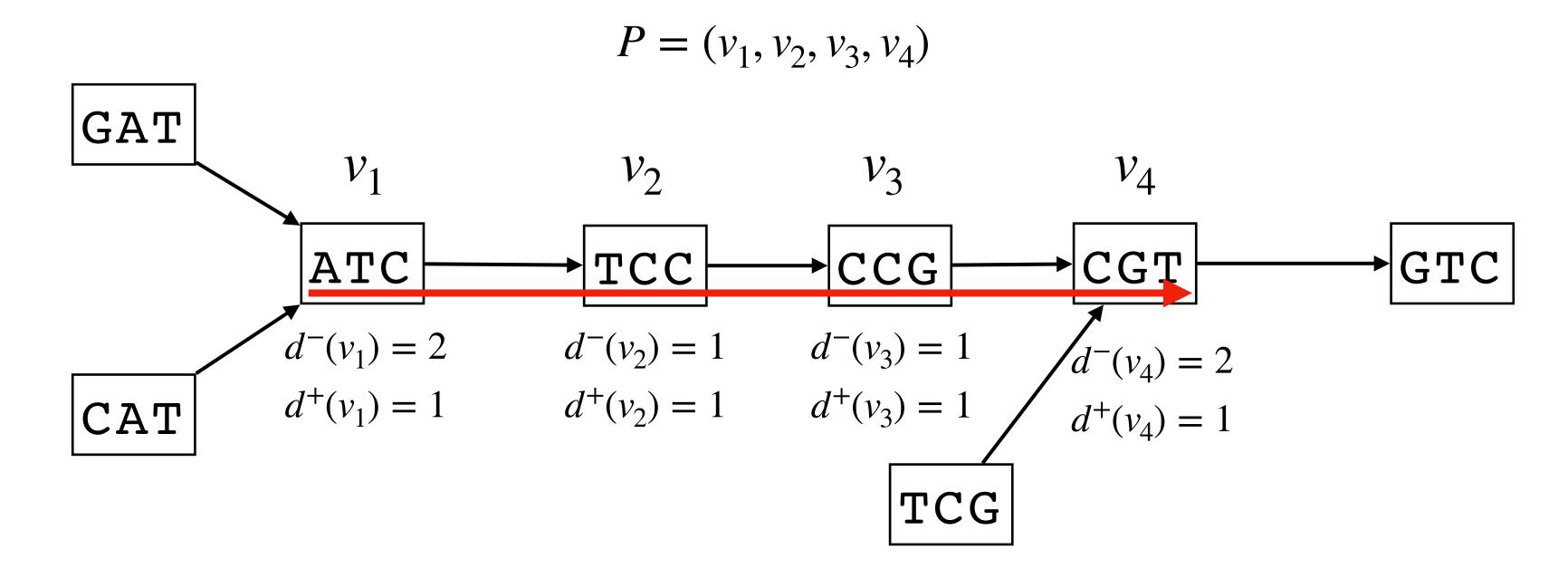
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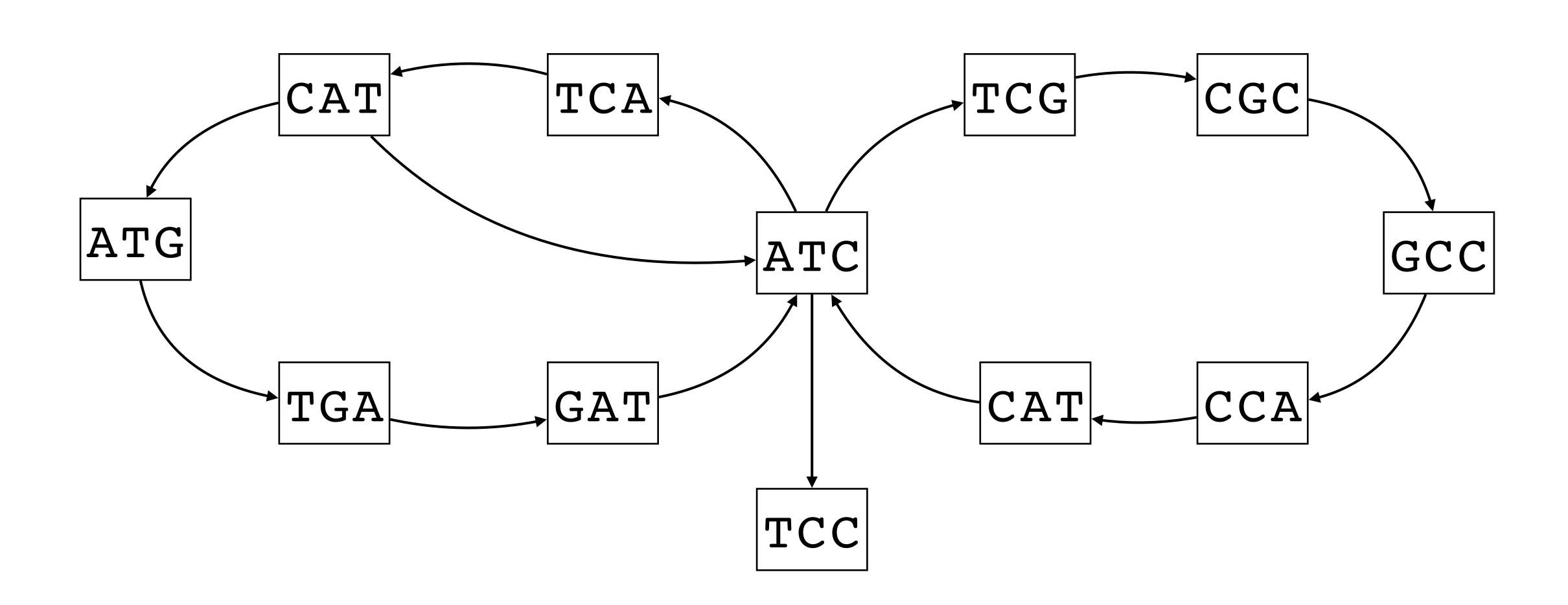
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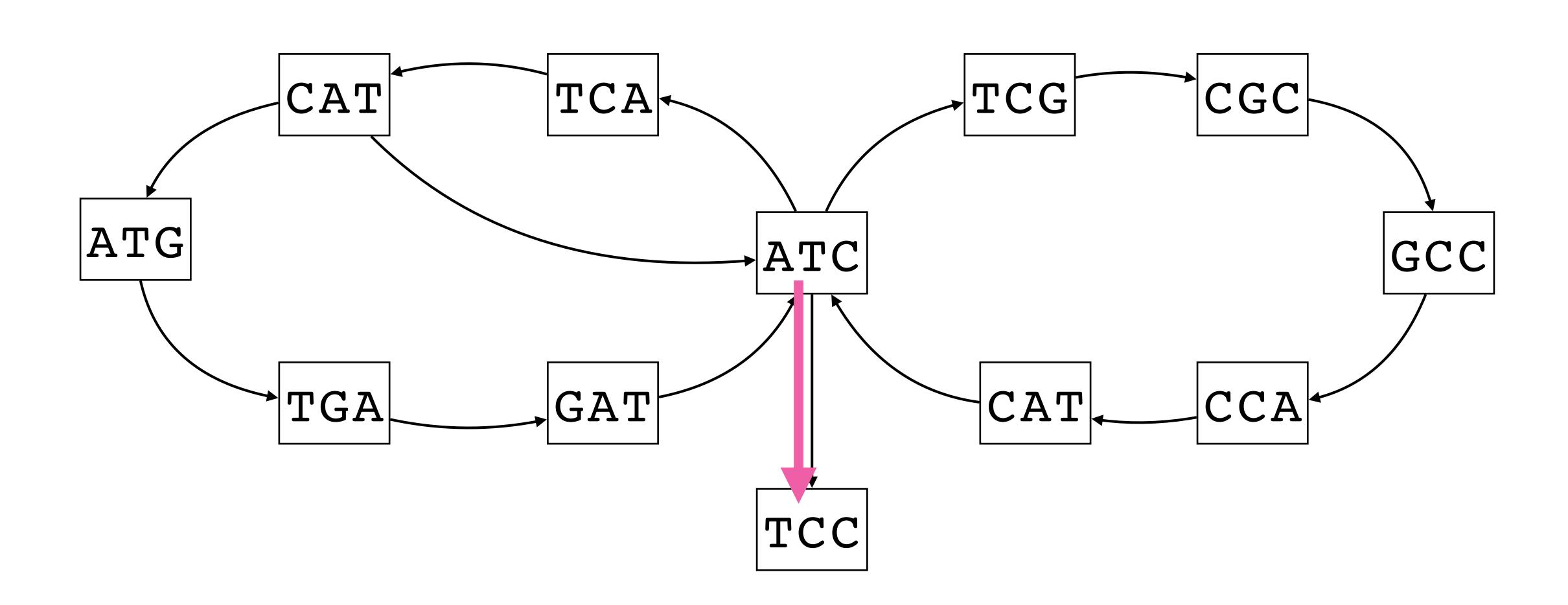


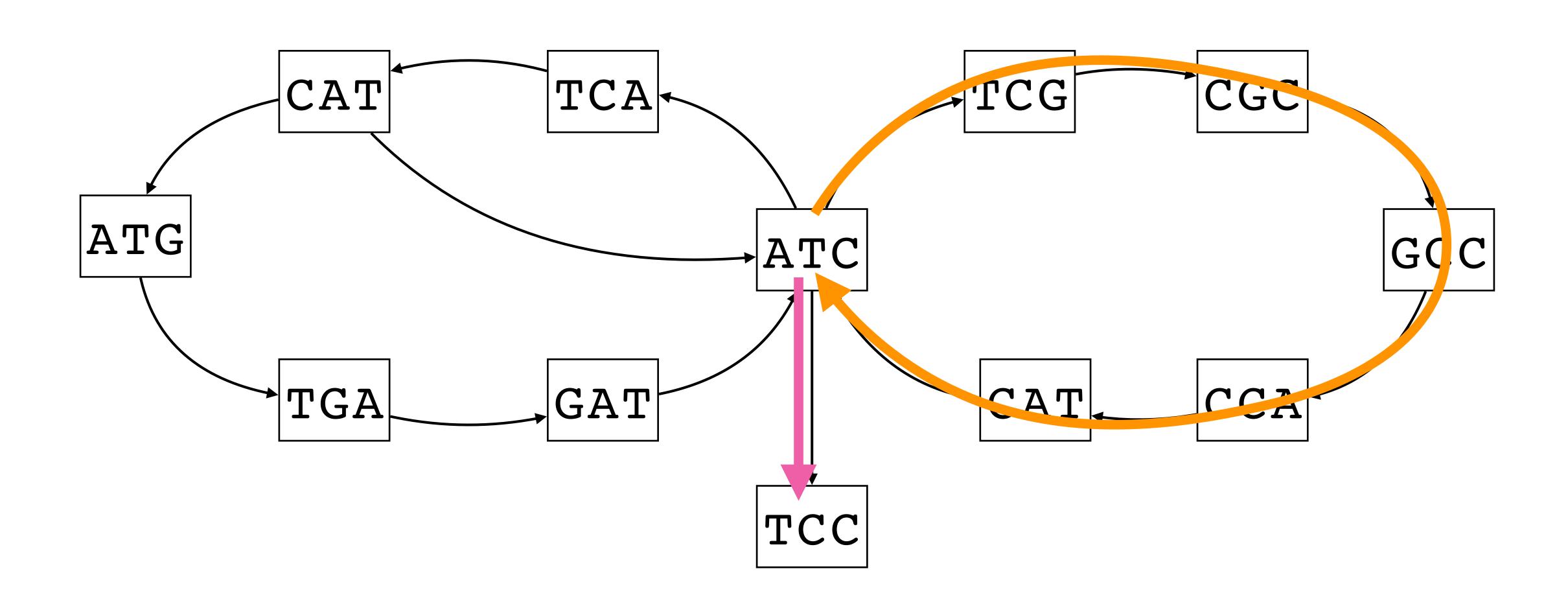
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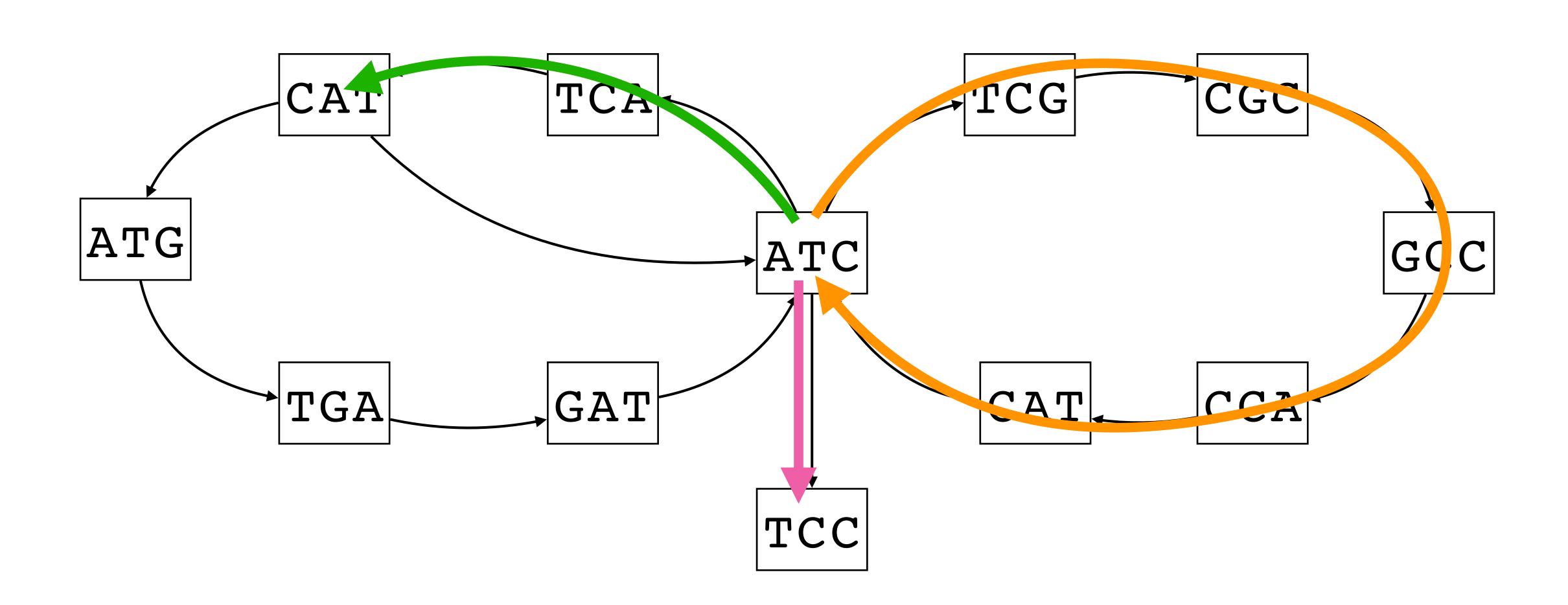


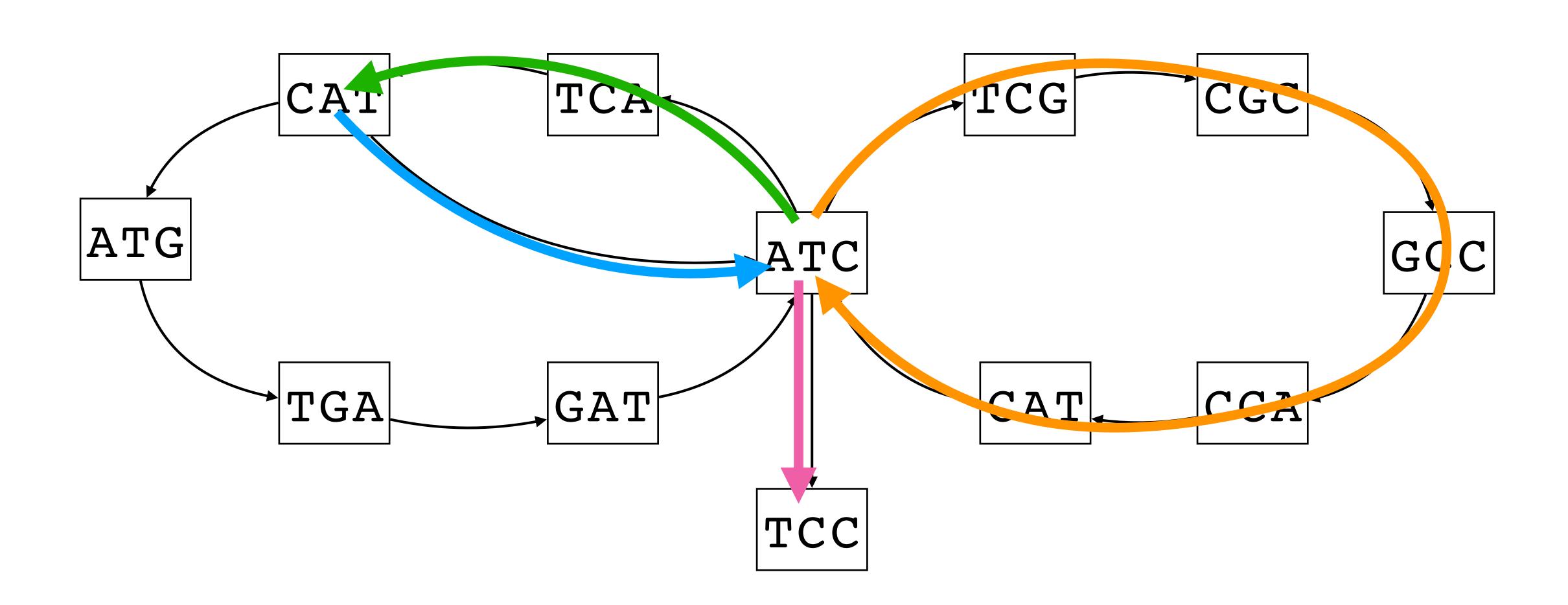
We want maximal (longest) unitigs

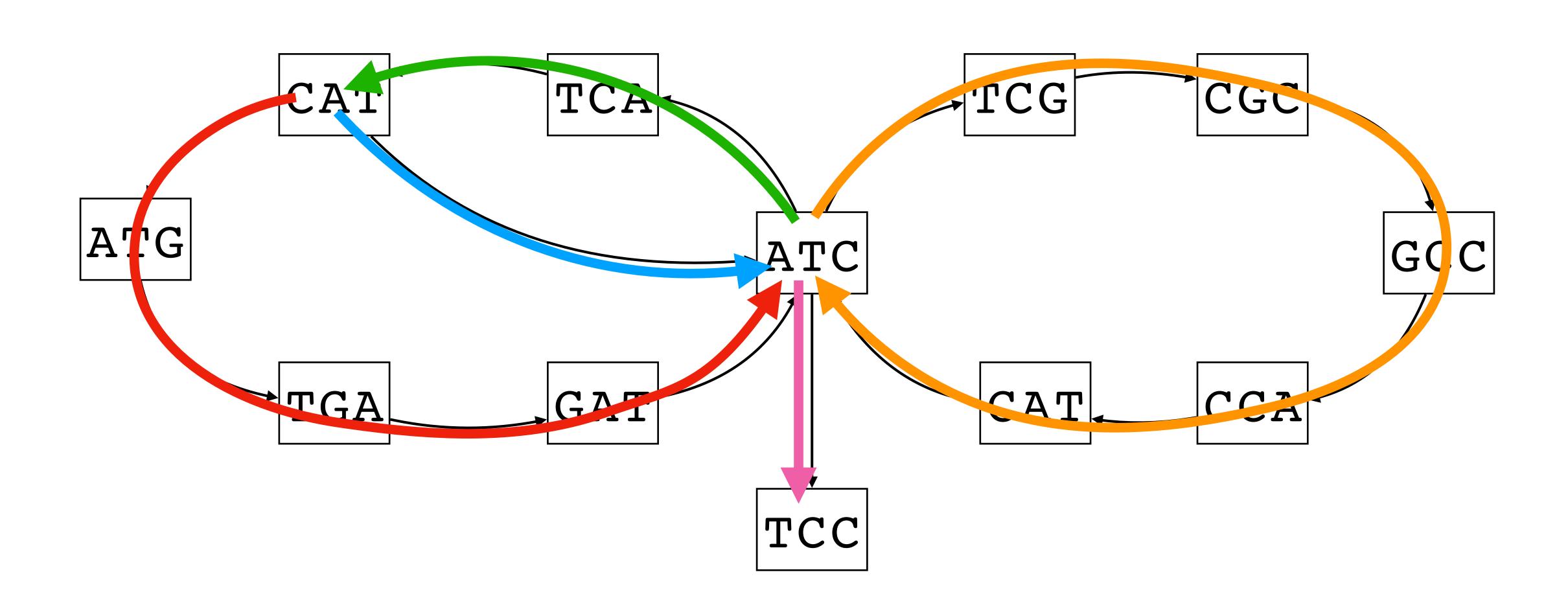


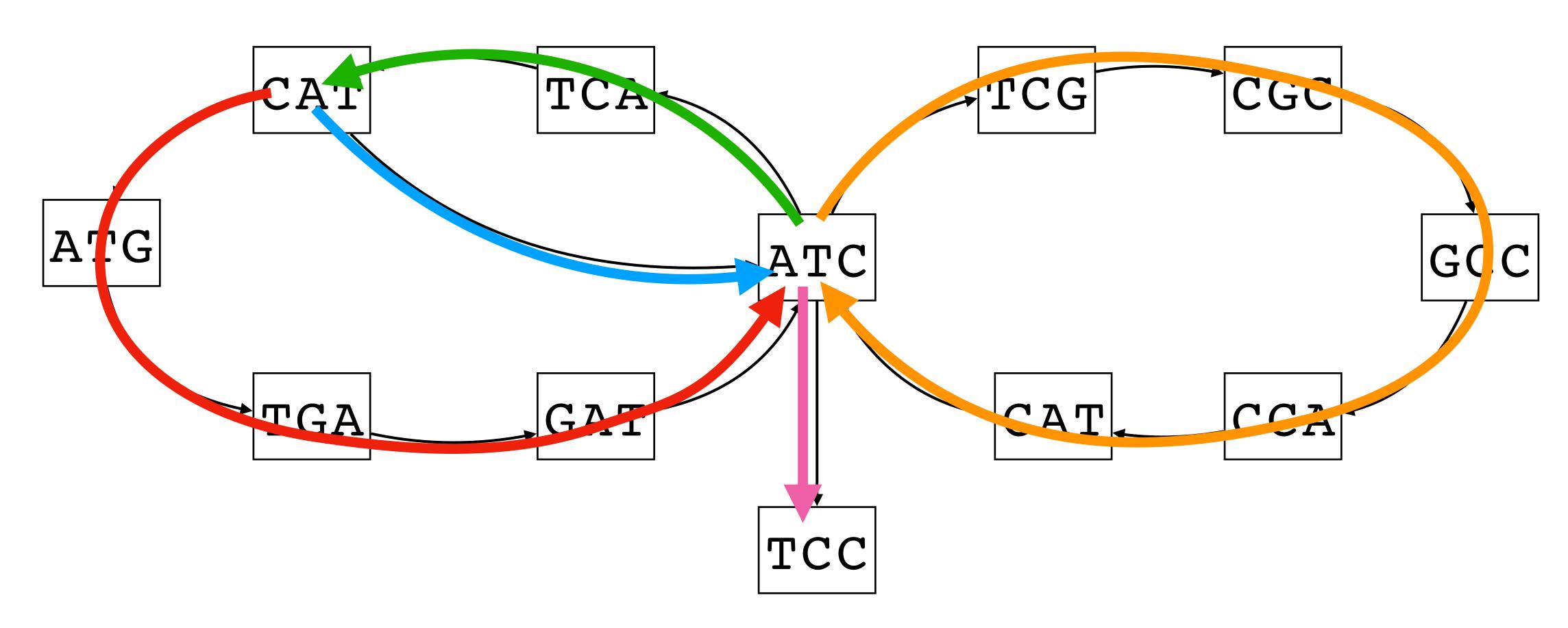








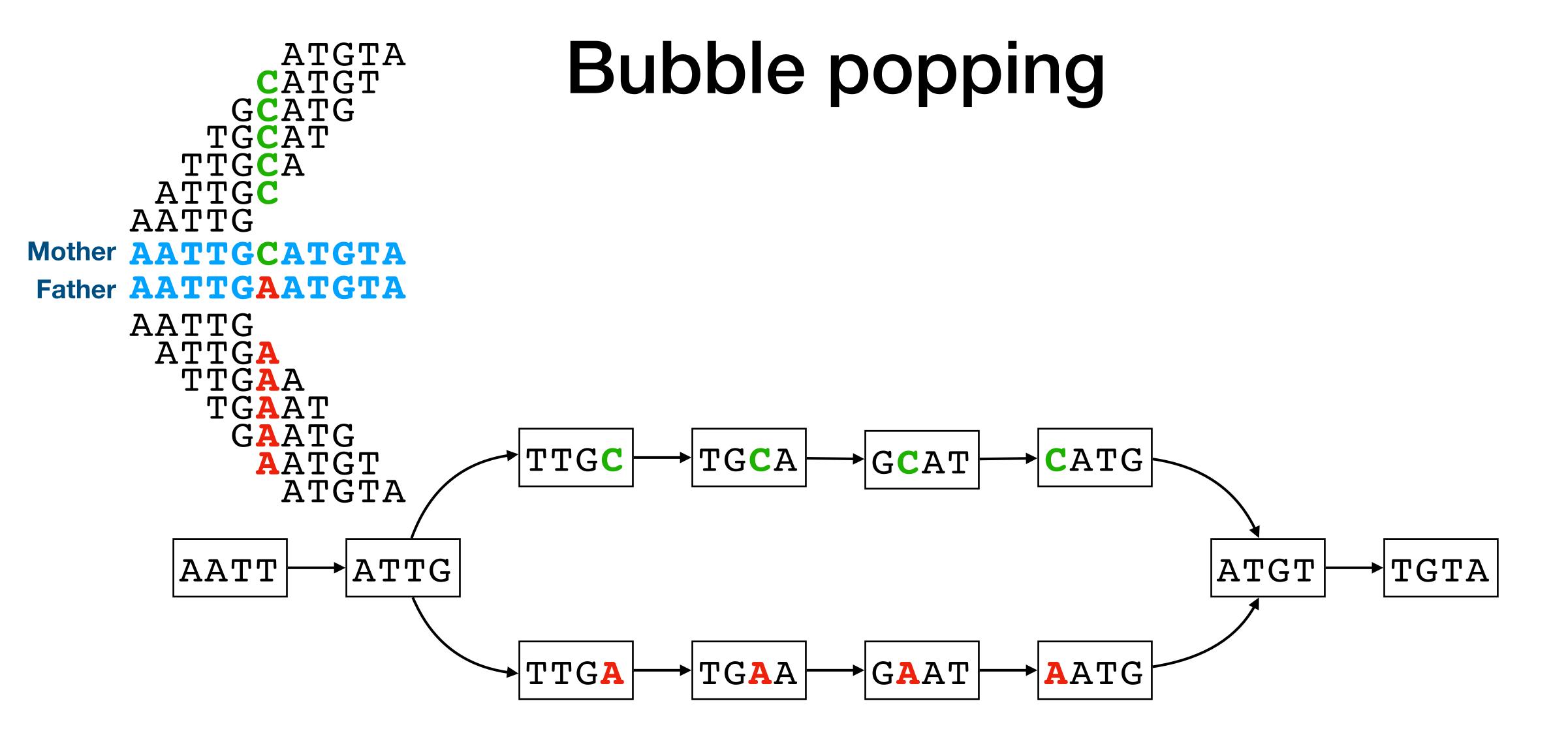




• Unitigs can be found in O(|edges|) time

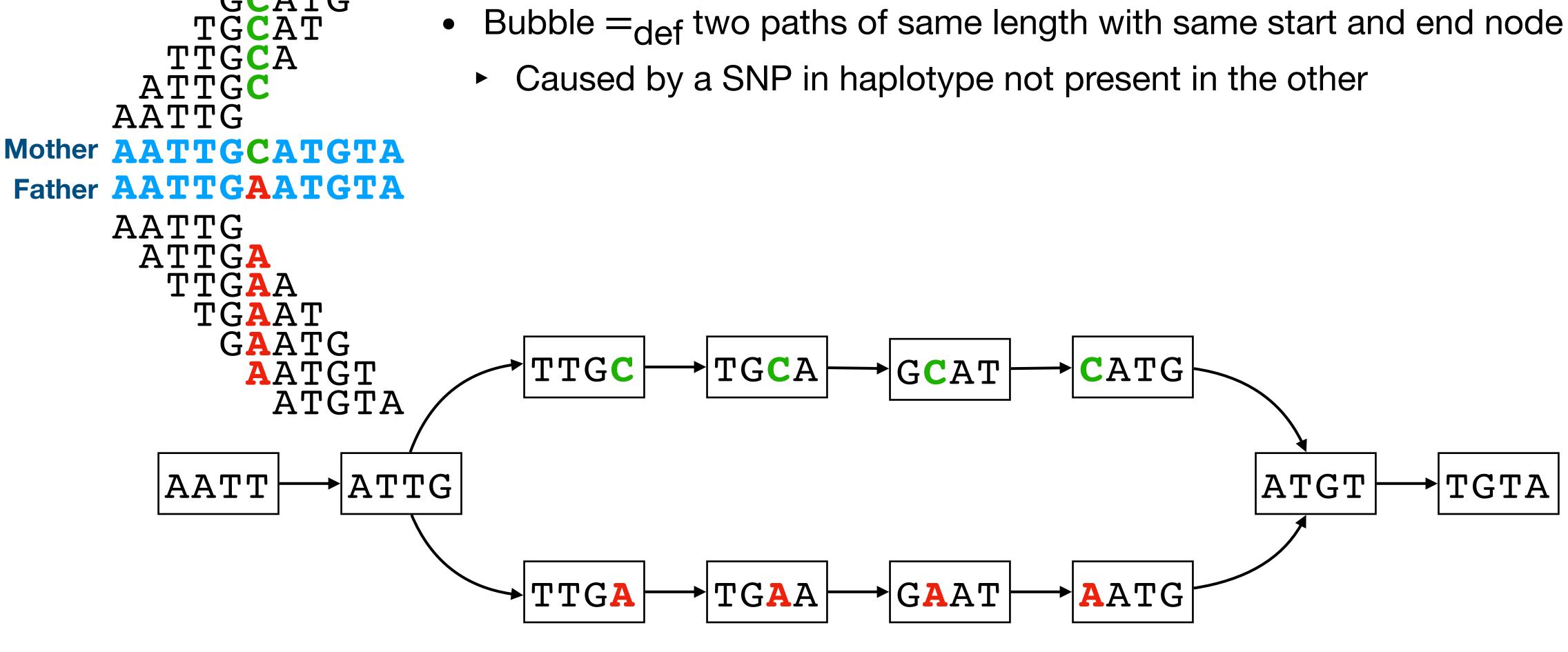
```
ATGTA
          CATGT
         GCATG
        TGCAT
      TTGCA
     ATTGC
    AATTG
Mother AATTGCATGTA
Father AATTGAATGTA
    AATTG
     ATTGA
       TTGAA
        TGAAT
         GAATG
          AATGT
           ATGTA
```

Bubble popping



ATGTA CATGT GCATG TGCAT TTGCA ATTGC

Bubble popping

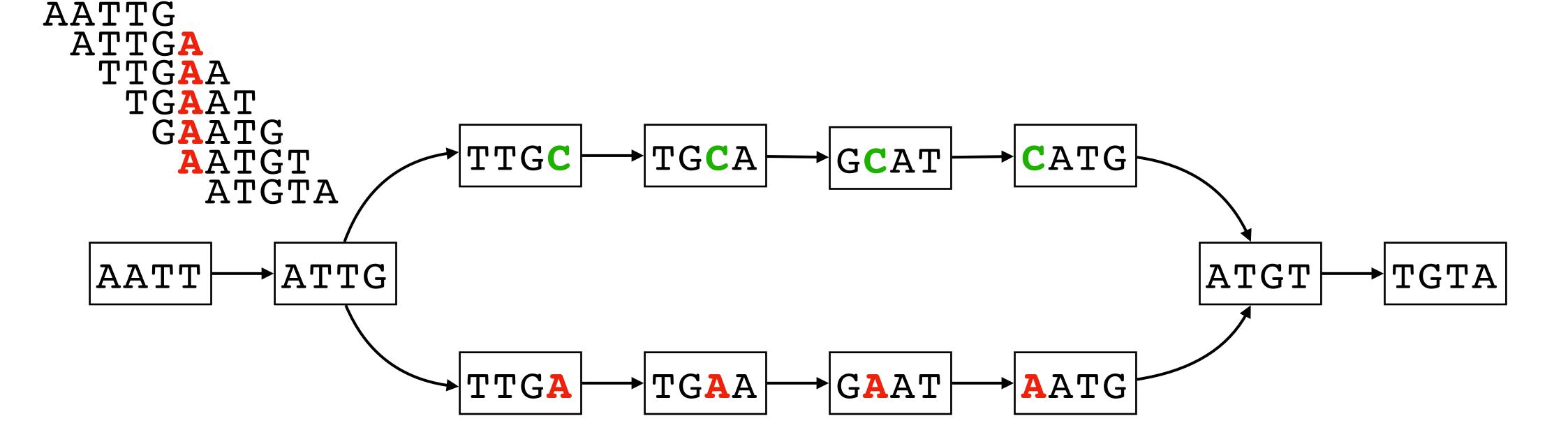


ATGTA CATGT GCATG TGCAT TTGCA ATTGC AATTGC AATTGC AATTGC AATTGCATGTA

Father **AATTGAATGTA**

Bubble popping

- Bubble = def two paths of same length with same start and end node
 - Caused by a SNP in haplotype not present in the other
- Leads to shorter unitigs (poliploidy can be solved later)

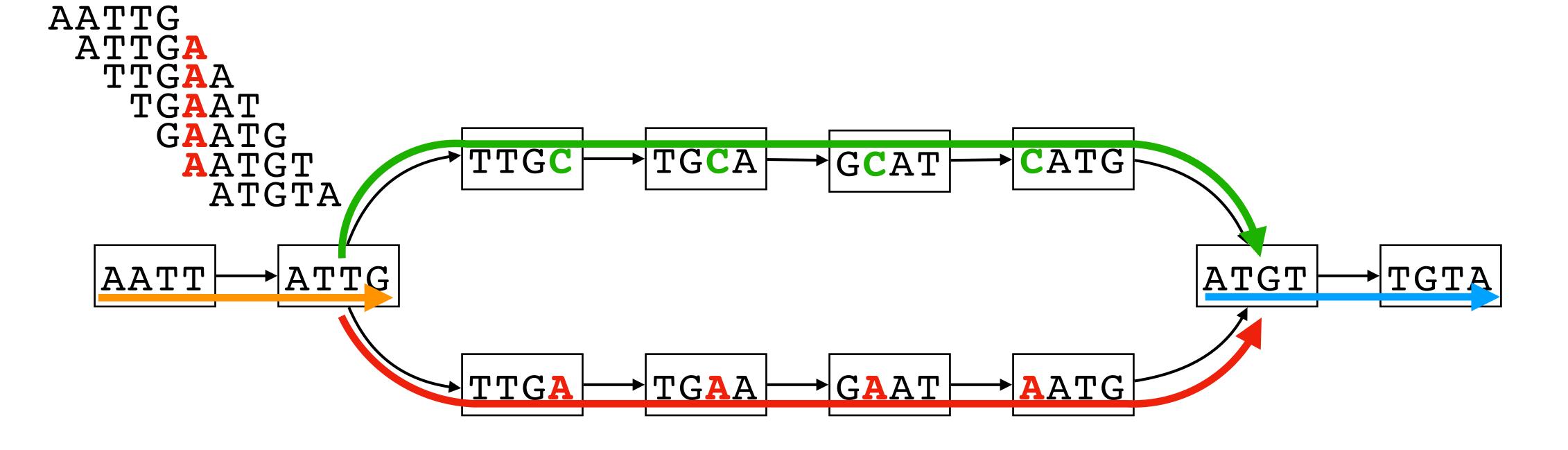


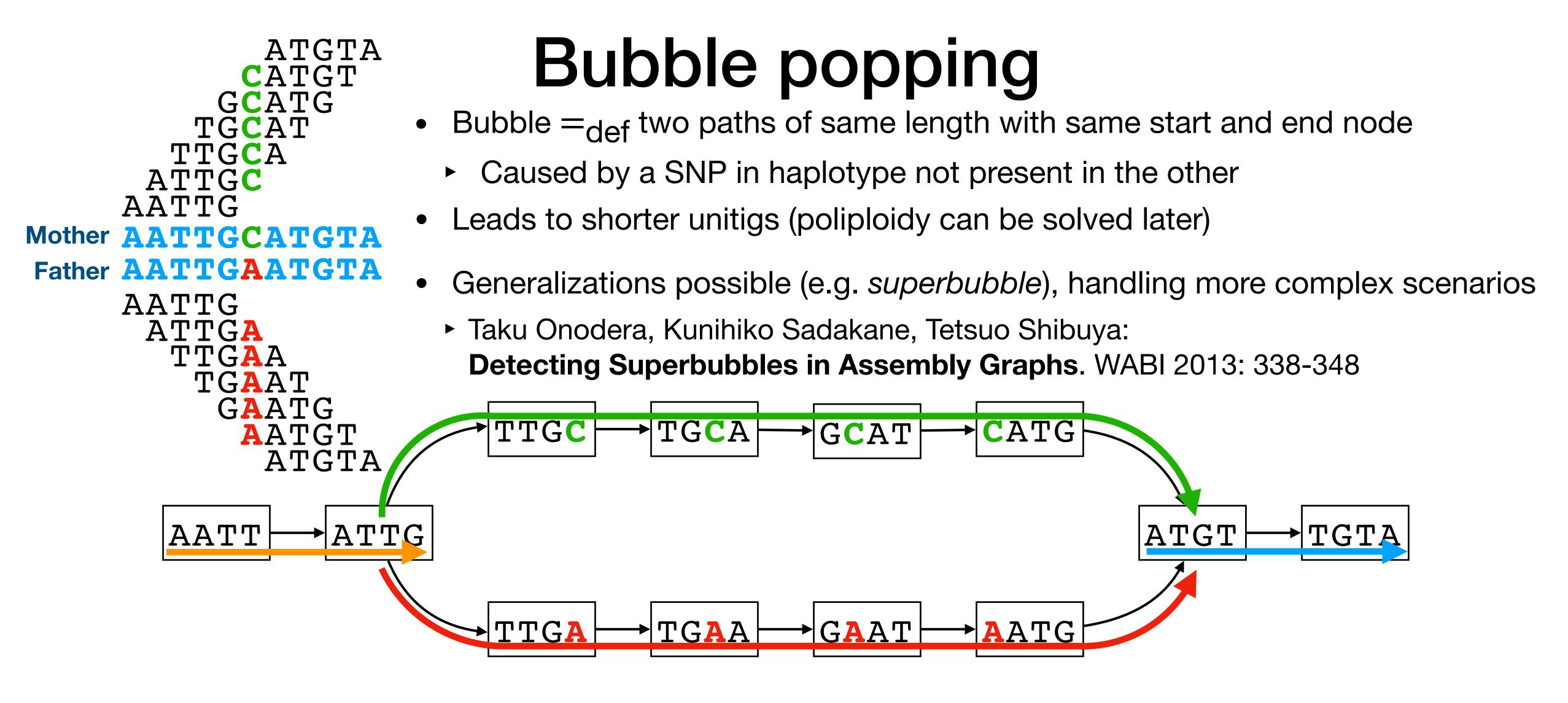
ATGTA CATGT GCATG TGCAT TTGCA ATTGC AATTGC AATTGC AATTGCATGTA

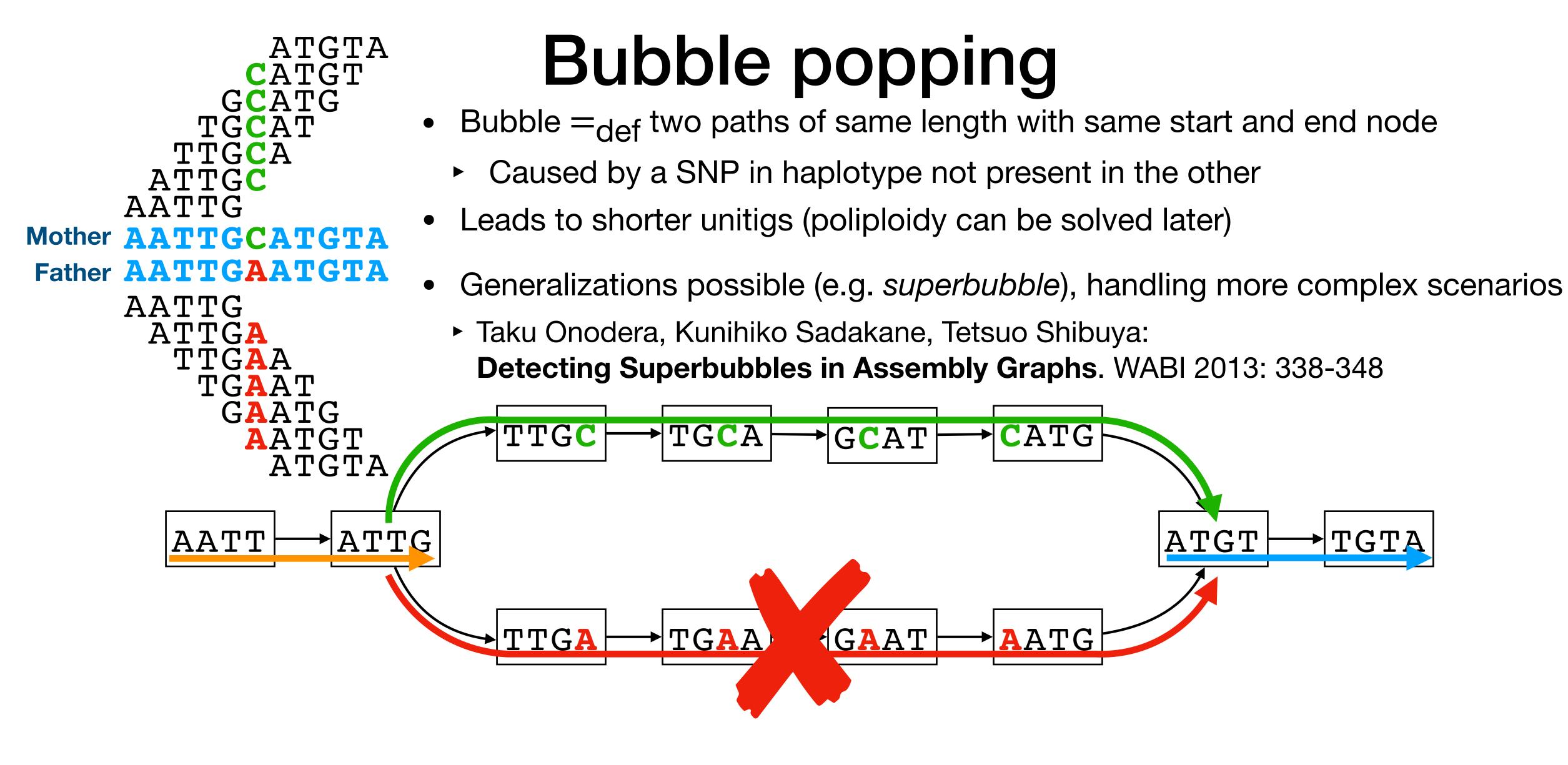
Father **AATTGAATGTA**

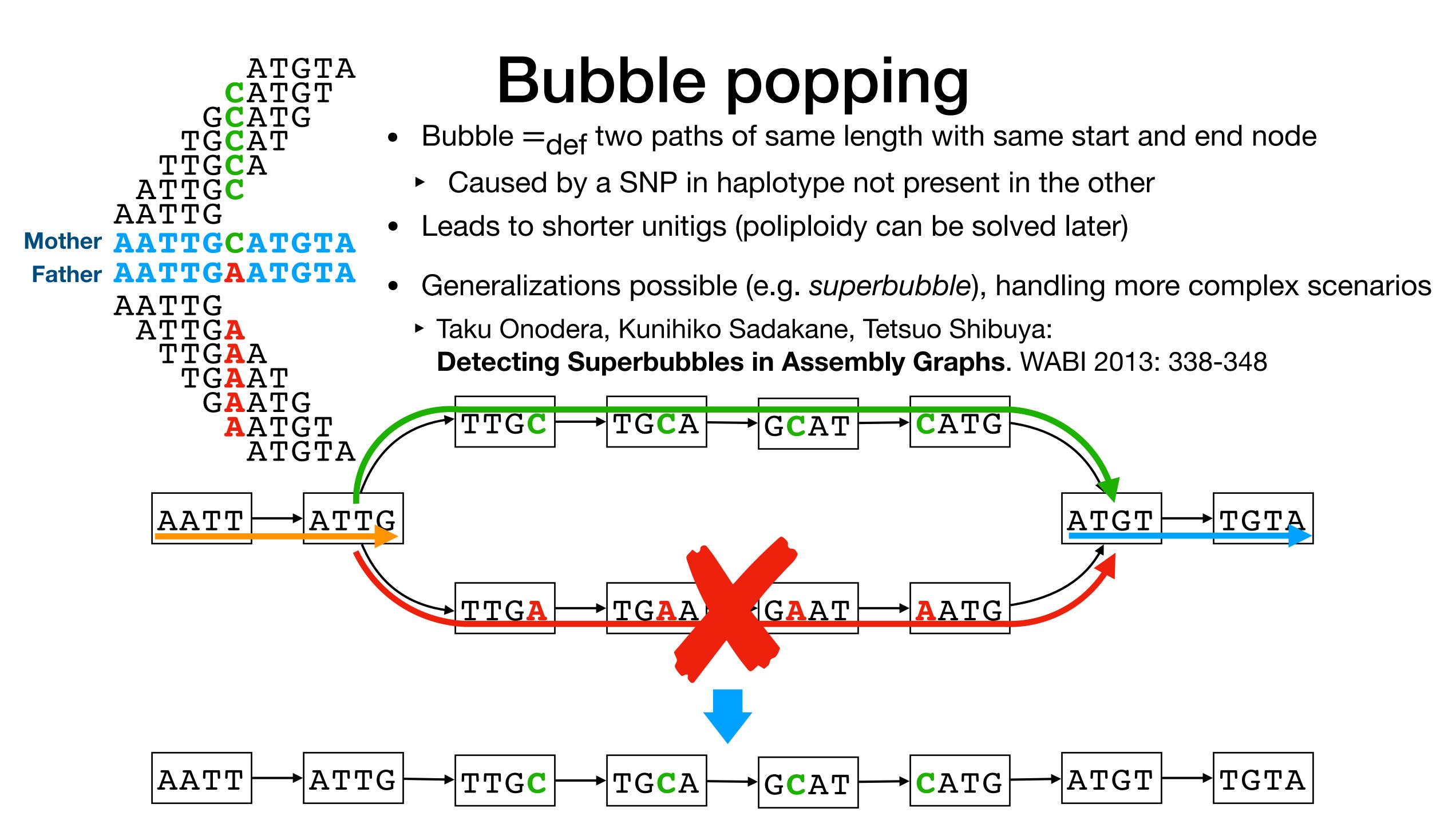
Bubble popping

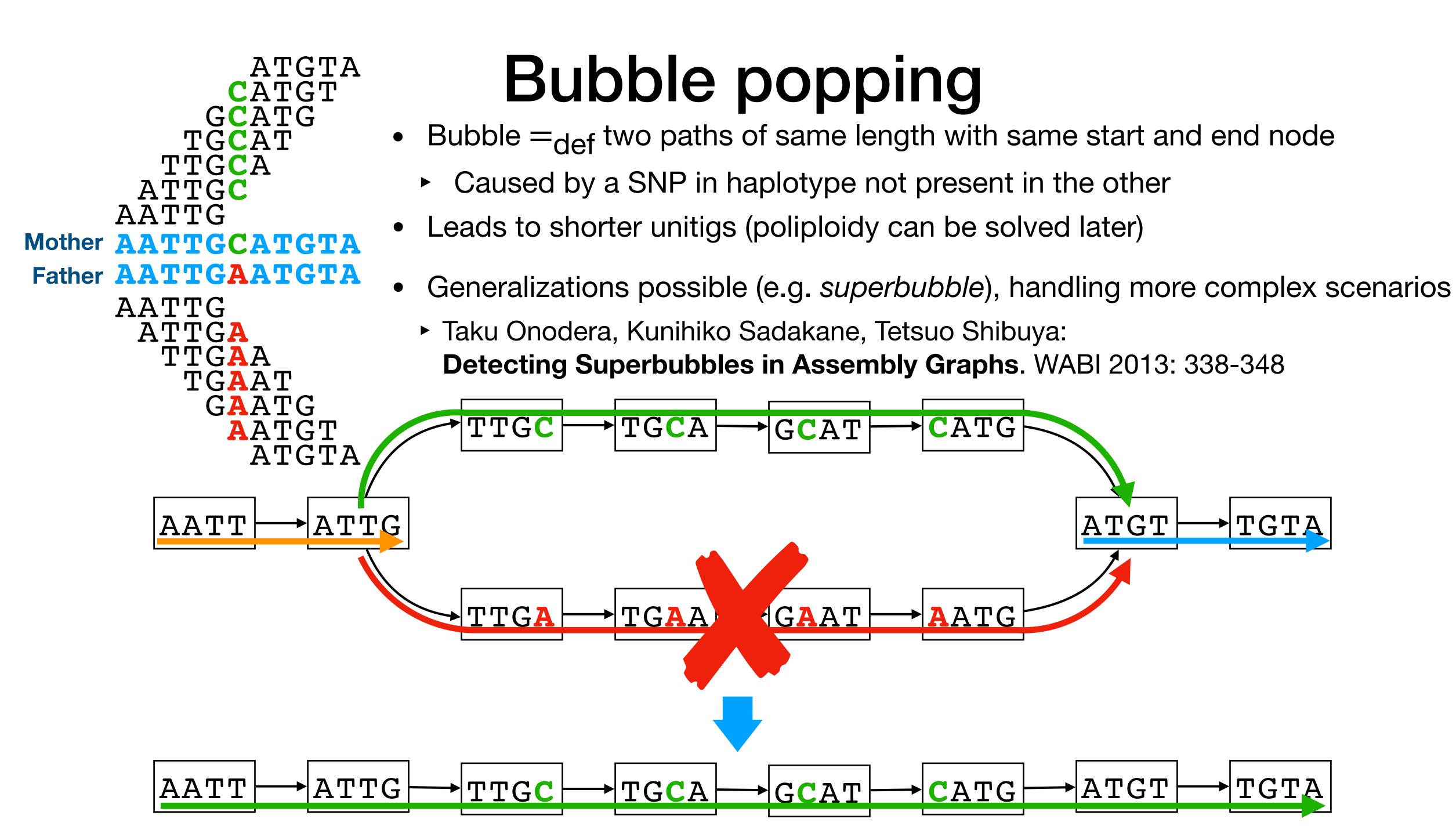
- Bubble = def two paths of same length with same start and end node
 - Caused by a SNP in haplotype not present in the other
- Leads to shorter unitigs (poliploidy can be solved later)





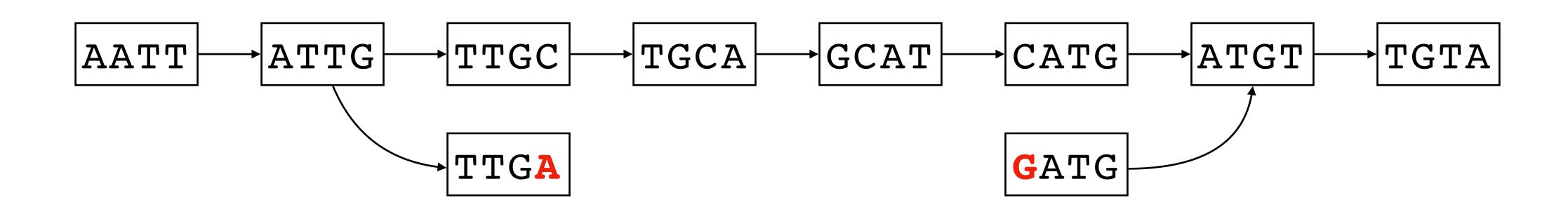






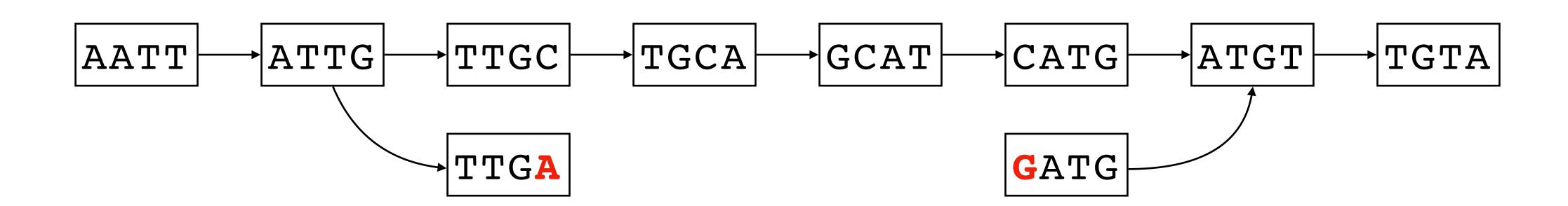
```
GATGT
GCATG
TGCAT
TTGCA
ATTGC
ATTGA
AATTGCATGTA
```

```
GATGT GCATG TGCAT TTGCA ATTGCA ATTGA AATTGCATGA AATTGCATGTA
```



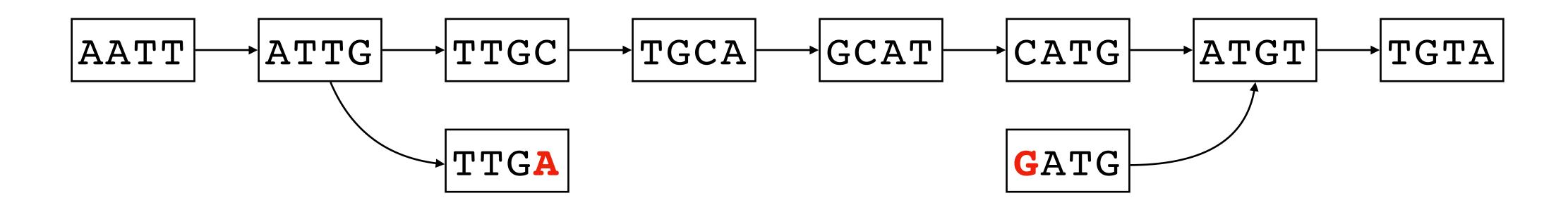
GATGT
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TGCA
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ATTGA
AATTGCATGTA

- Tip $=_{def}$ a "short" path that either:
 - ends in a sink v (i.e. $d^+(v) = 0$)
 - starts in a source v (i.e. $d^-(v) = 0$)



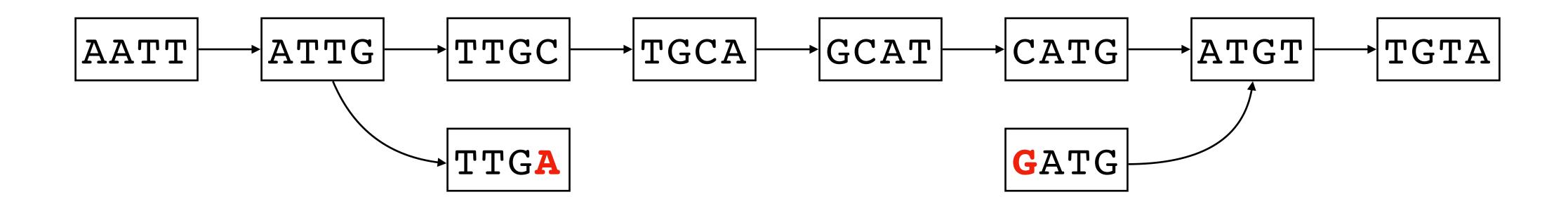
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- Caused by sequencing errors that remain after error correction



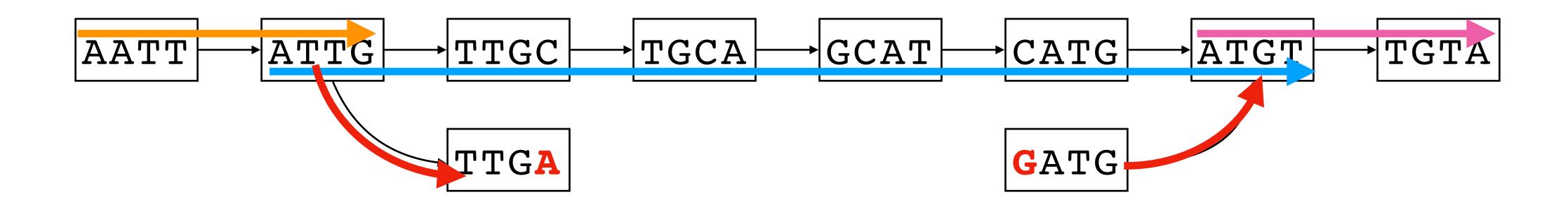
GATGT GCATG TGCAT TTGCA ATTGA AATTGCAATTGAAATTG

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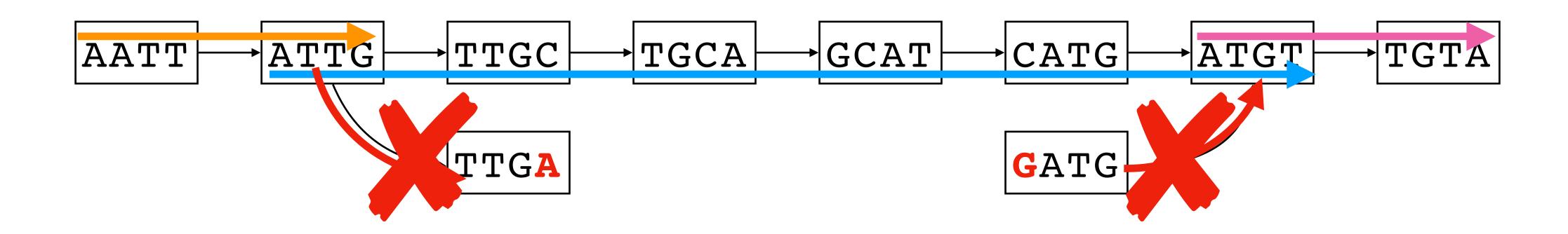
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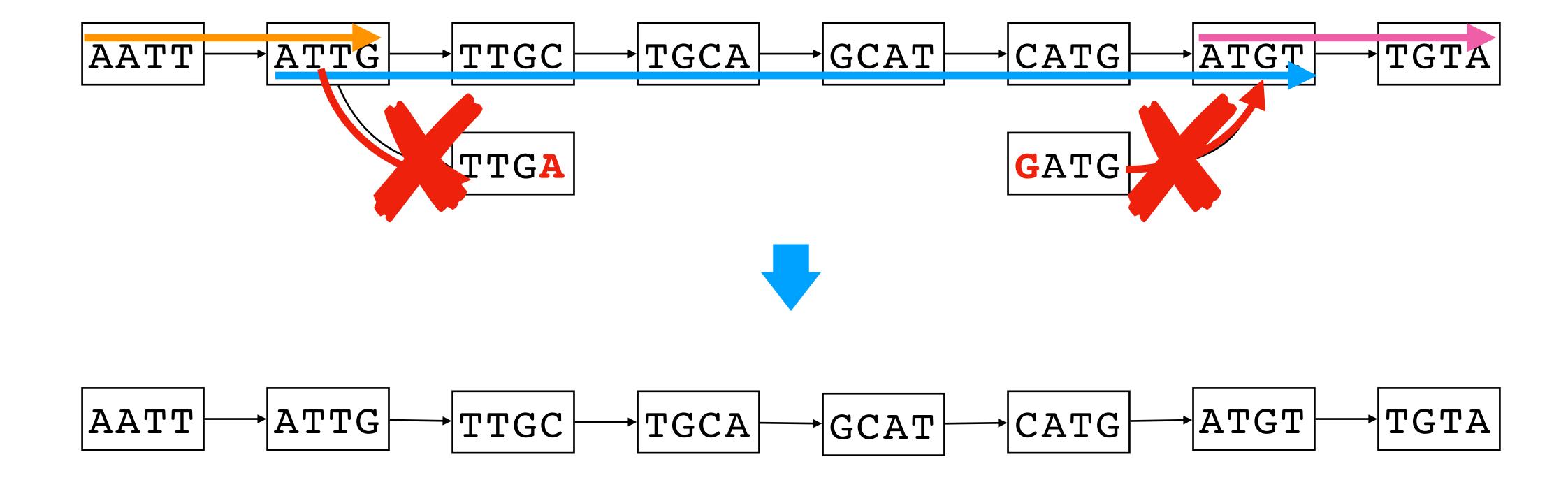
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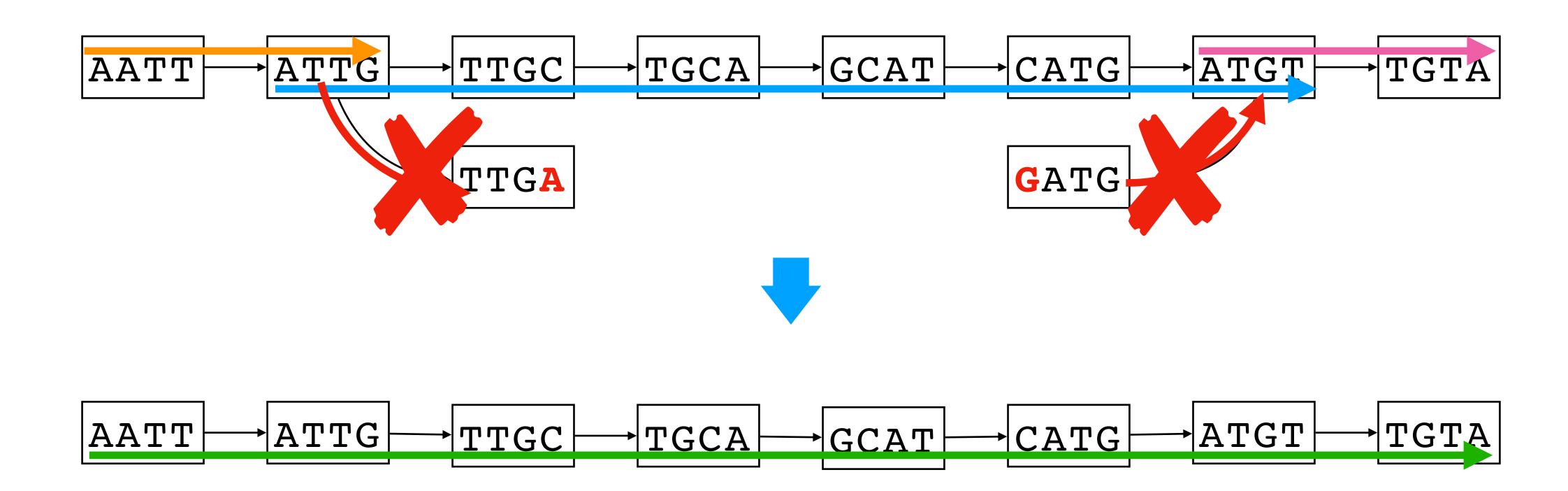


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GCATG
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TTGCA
ATTGC
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ATTGC
ATTGC

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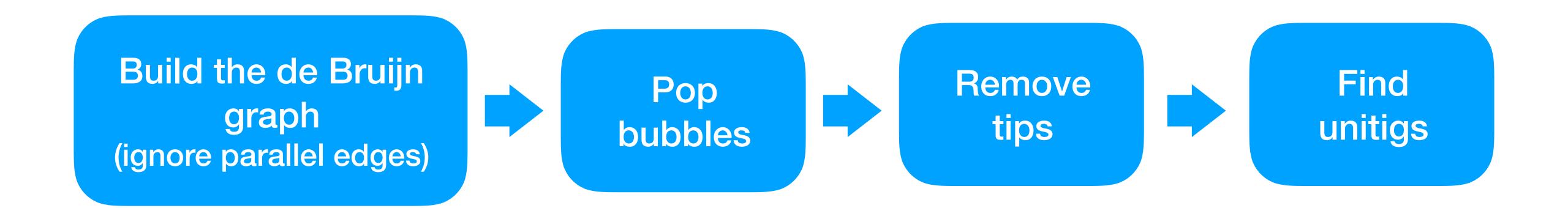


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Contigs assembly

(simplified to ignore some practical issues e.g. errors, reverse complements)



Output the unitigs as "contigs"

Scaffolding

Bring in paired-end information

Align reads to contigs

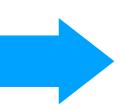


Chain (order) the contigs

Output chains of contigs with "gaps" (NNNN...) between them

Contigs

TCGATAGCTAAAA AATTGT ATAGAGATATTT ATATCGCTAGA



Scaffolds

TCGATAGCTAAAANNNNNNNNNNAATTGTNNNATAGAGATATTT ATATCGCTAGA

```
ATATA.....15.....TGCAA

AGAAT.....24......GTAAT

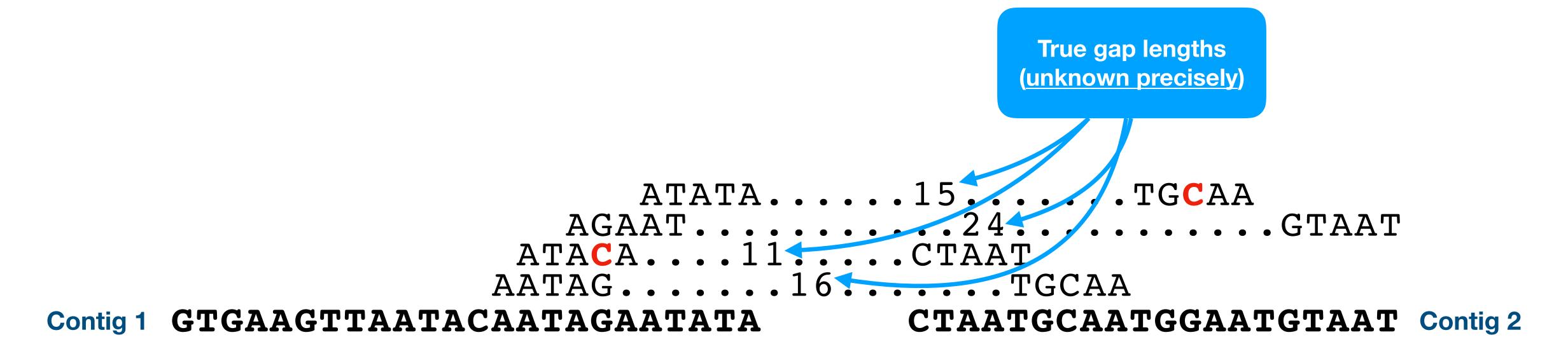
ATACA....11....CTAAT

AATAG......16.....TGCAA

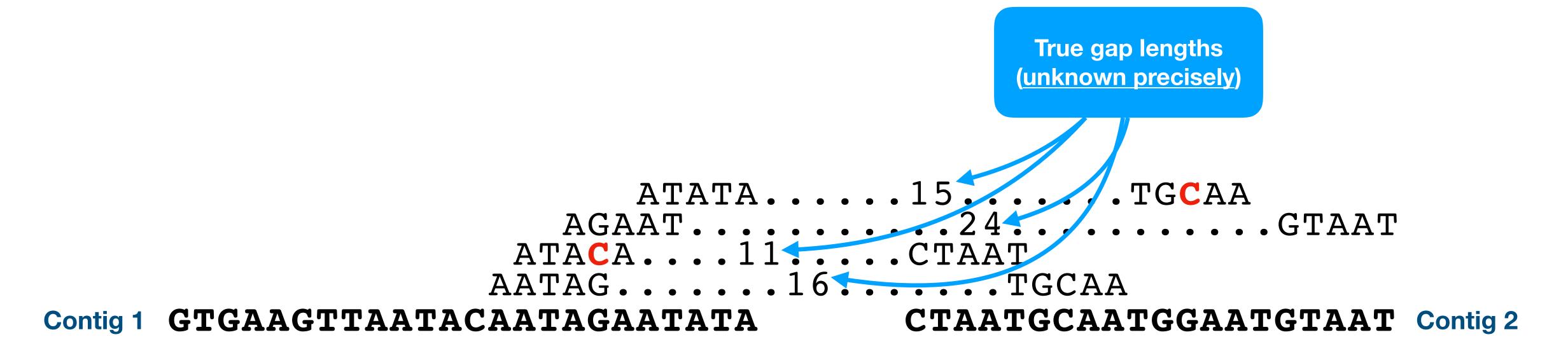
Contig 1 GTGAAGTTAATACAATAGAATATA

CTAATGCAATGGAATGTAAT Contig 2
```

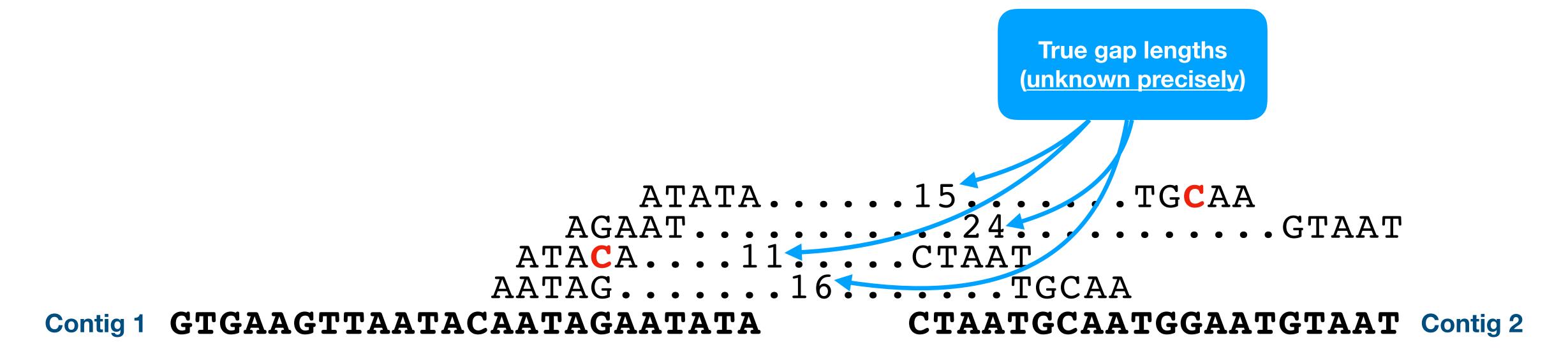
Align paired-end reads to contigs, focus on read pairs aligning to different contigs



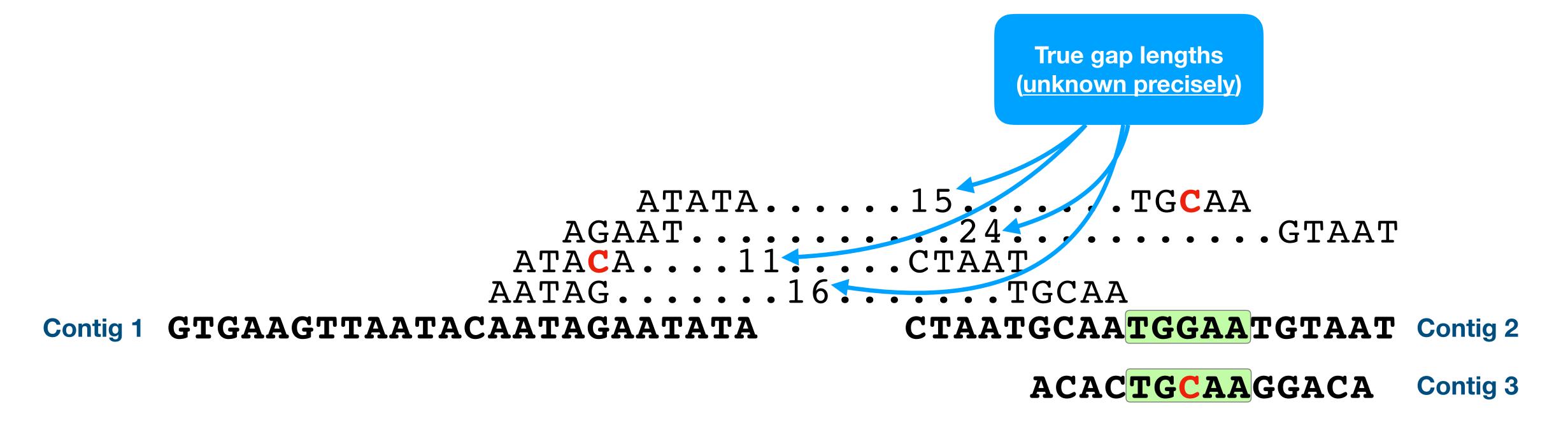
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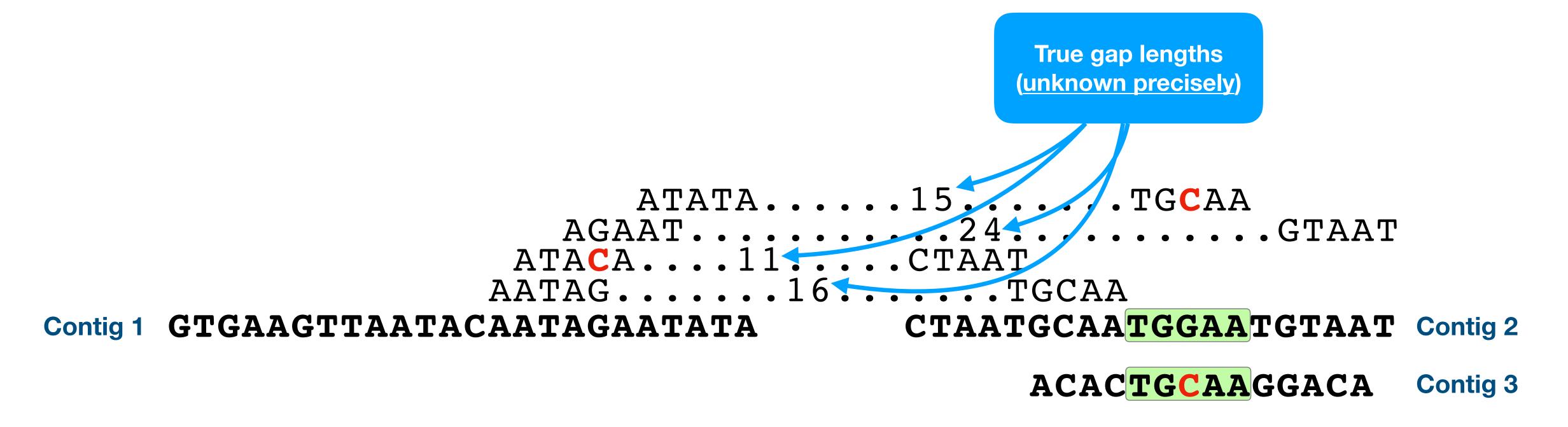
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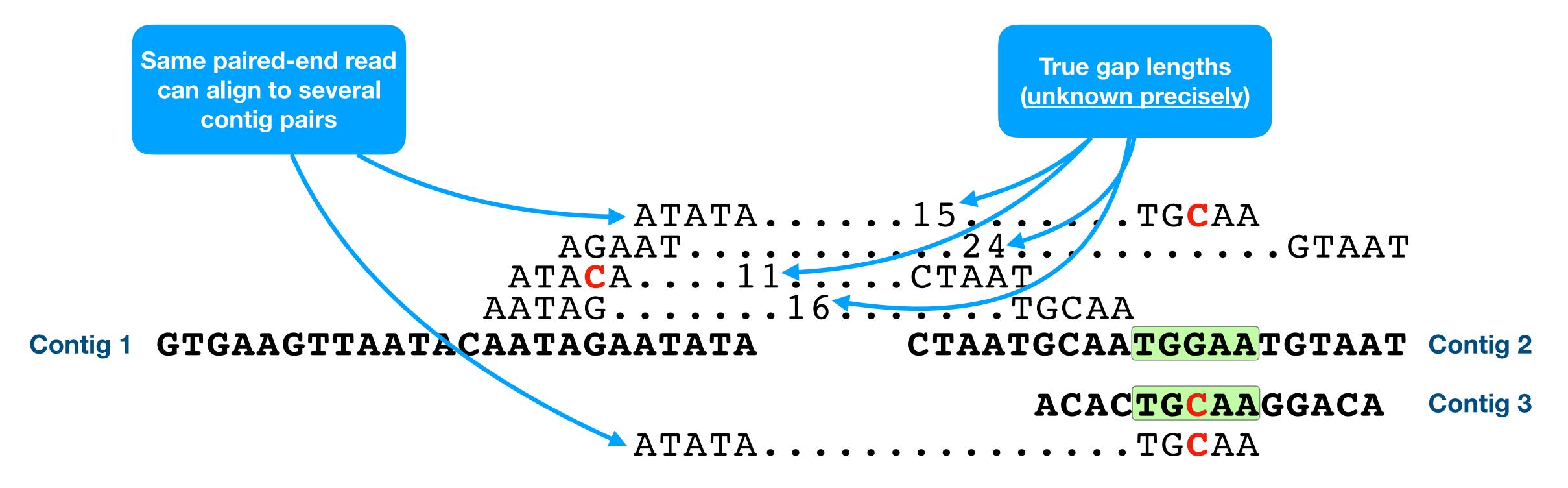
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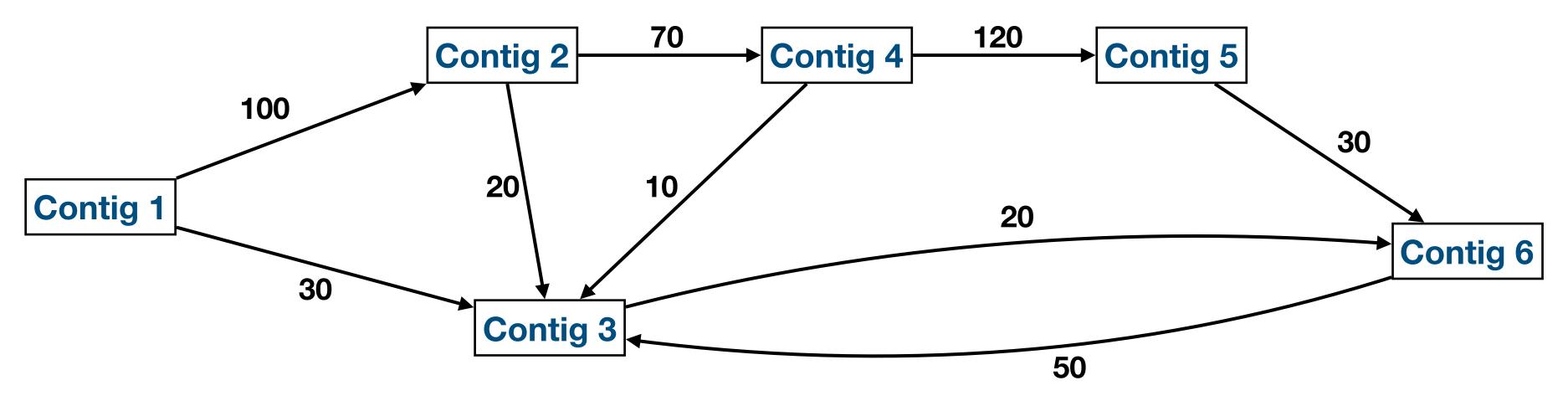
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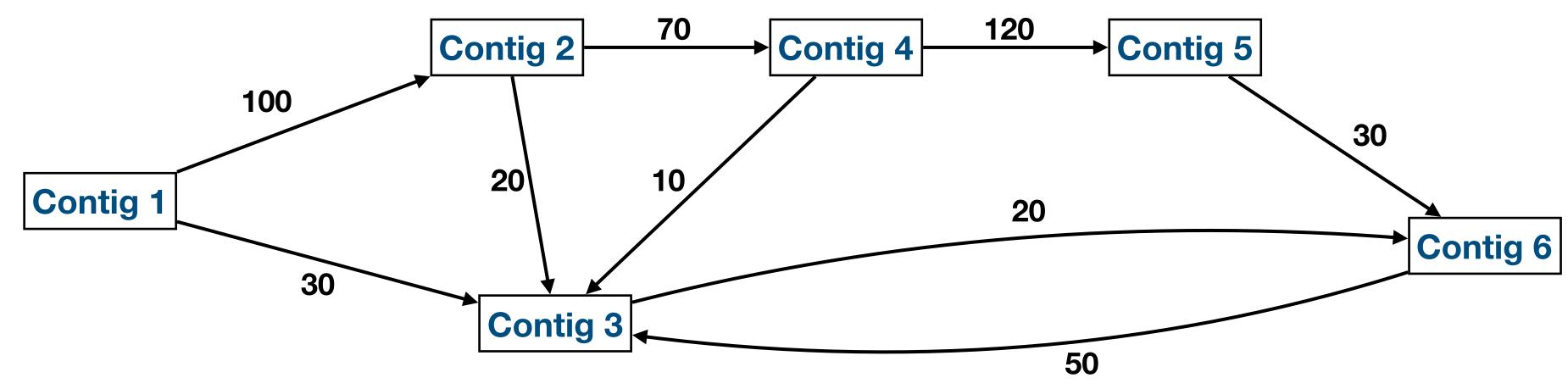


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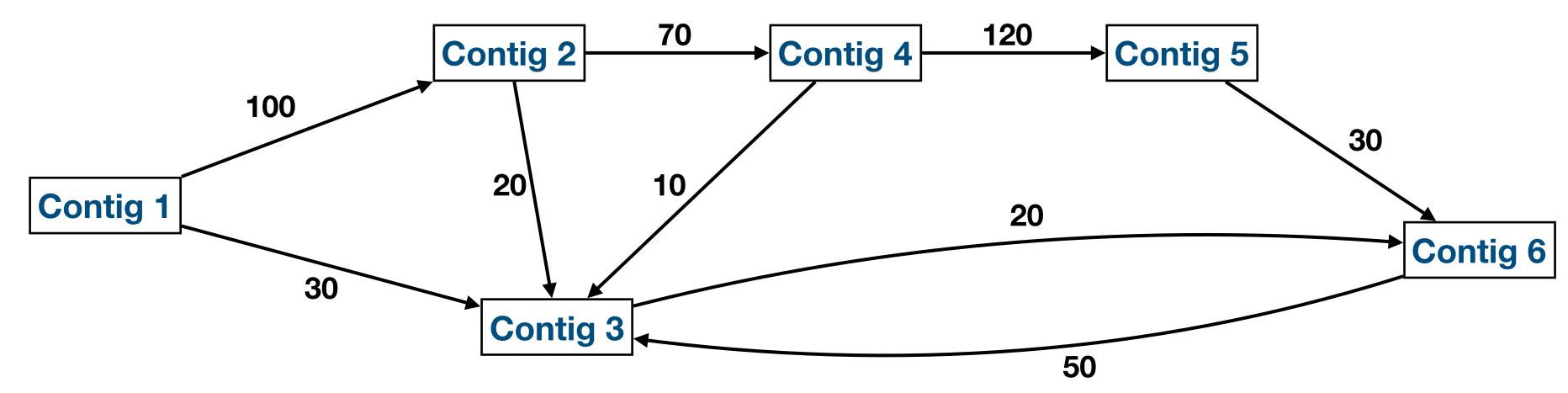


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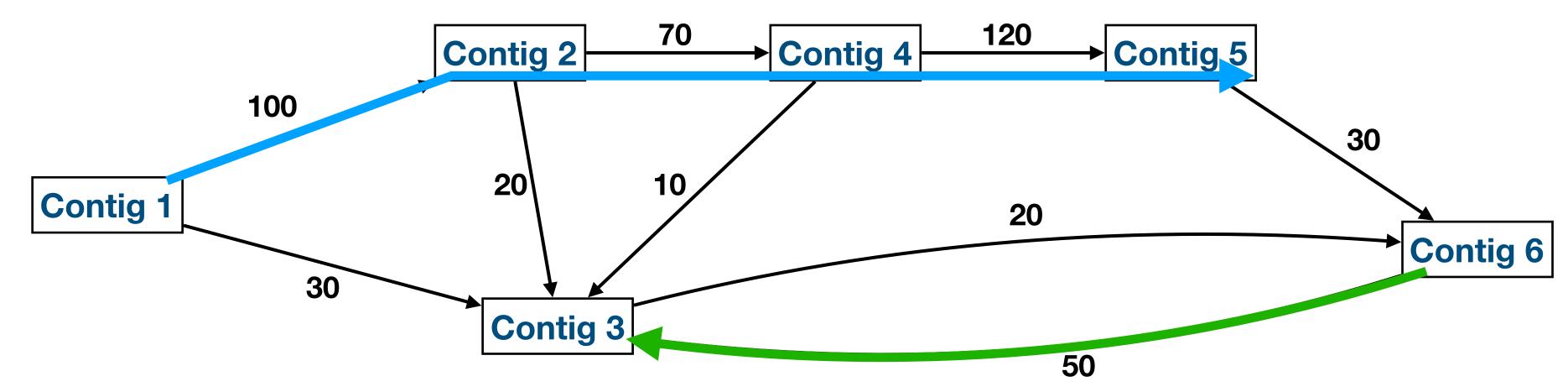




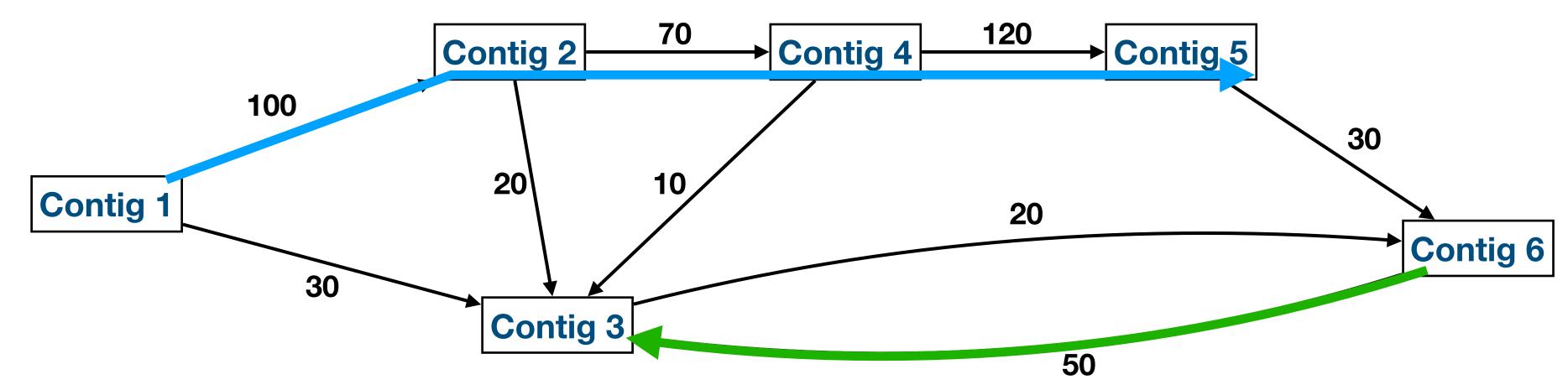
Another contig assembly-like problem



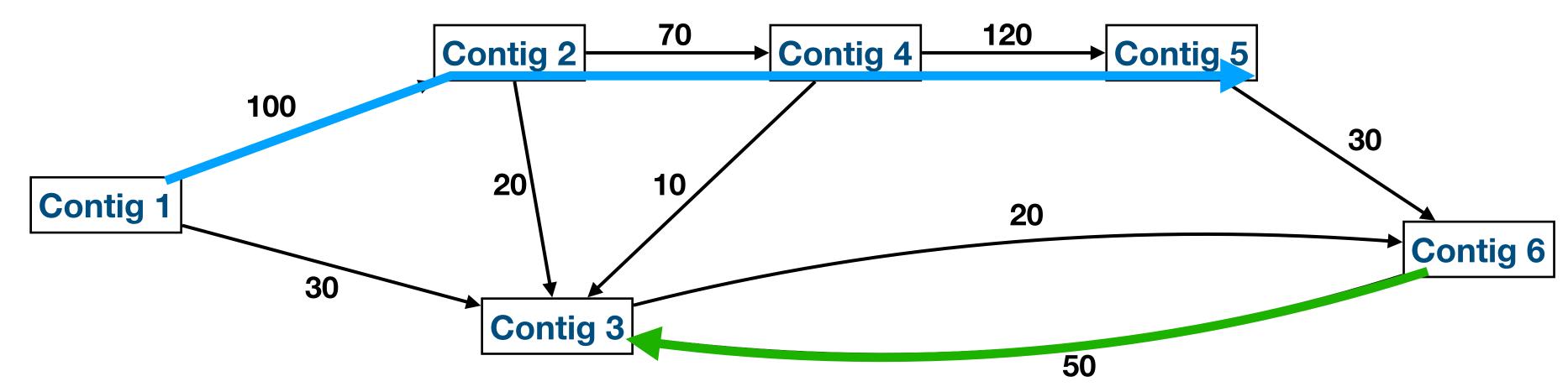
- Another contig assembly-like problem
- Now weights on edges (how much "evidence" there is): new problem formulations



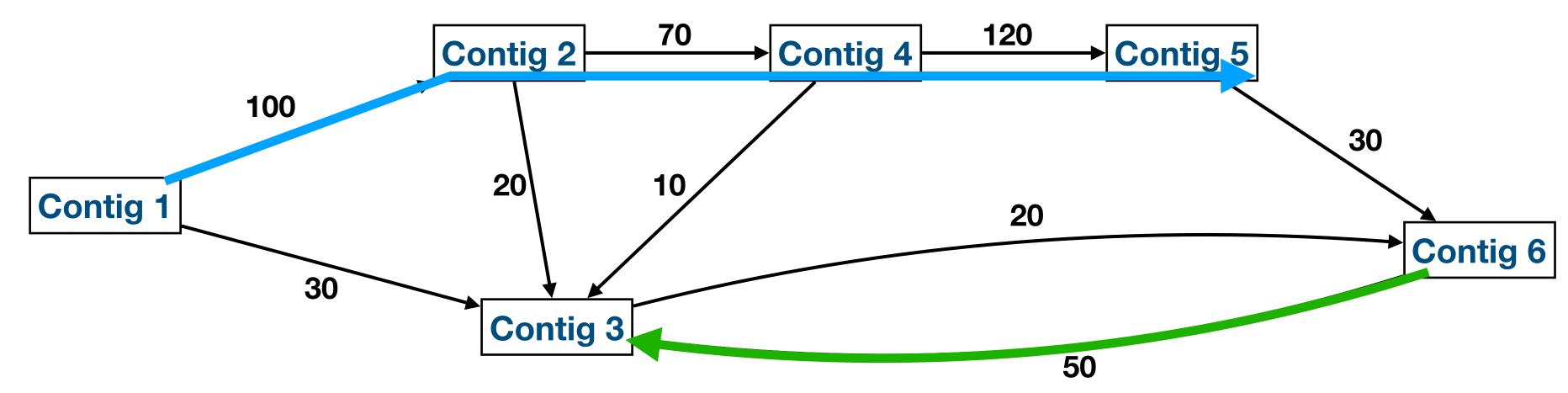
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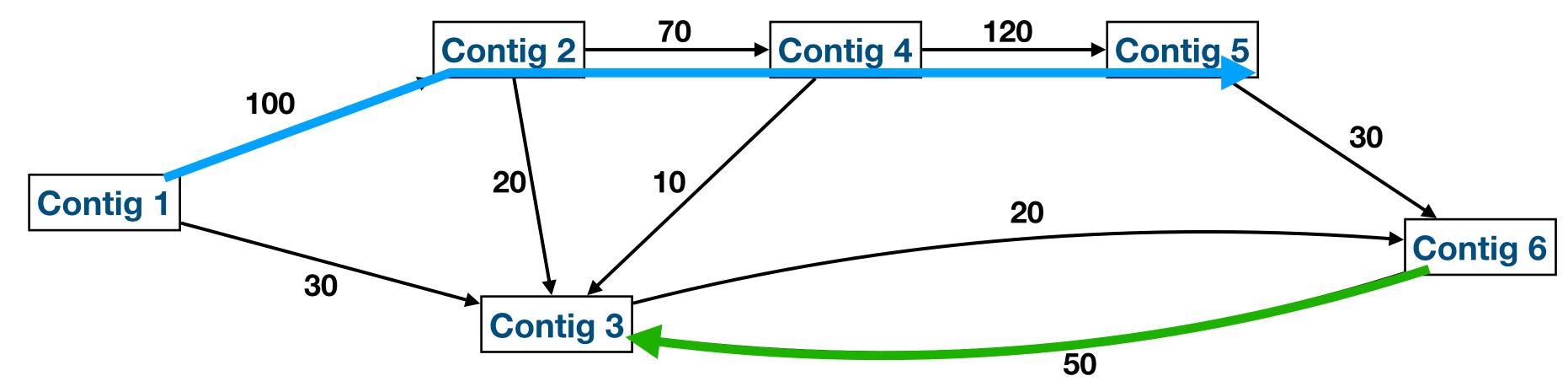
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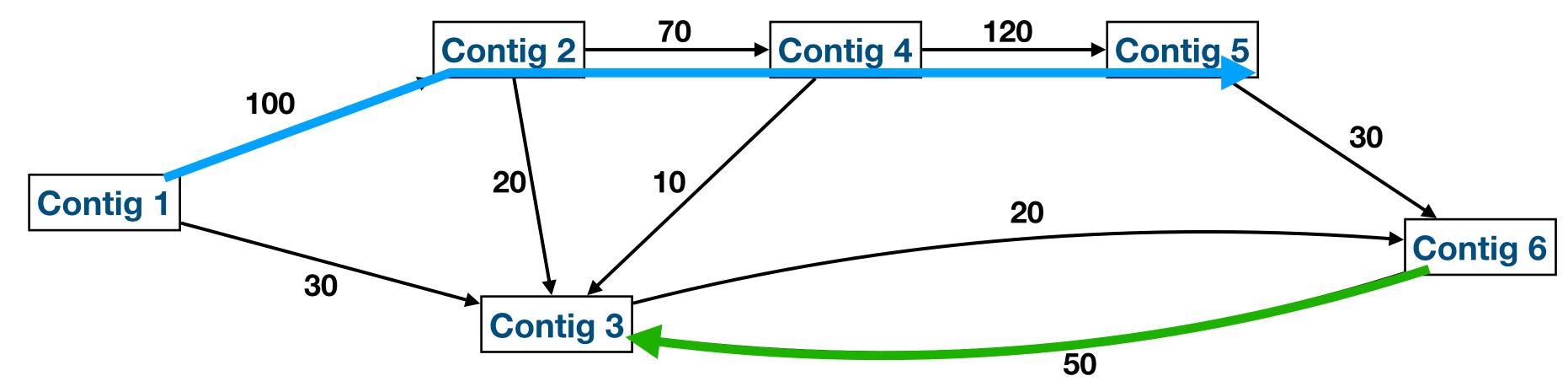
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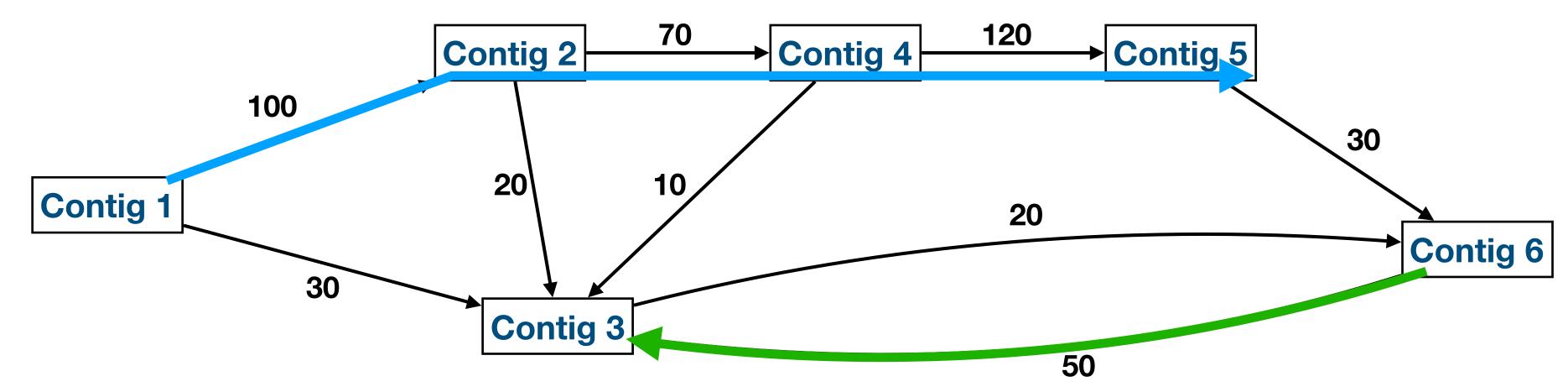
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 - Igor Mandric, Alex Zelikovsky:
 ScaffMatch: Scaffolding Algorithm Based on Maximum Weight Matching. RECOMB 2015: 222-223

Gap filling

Scaffolds contain gap length estimates (number of Ns)

Bring back all reads



Find filling paths from the assembly graph

Output the scaffolds in which some gaps are "filled"

TCGATAGCTAAAANNNNNNNNNNAATTGTNNNATAGAGATATTT

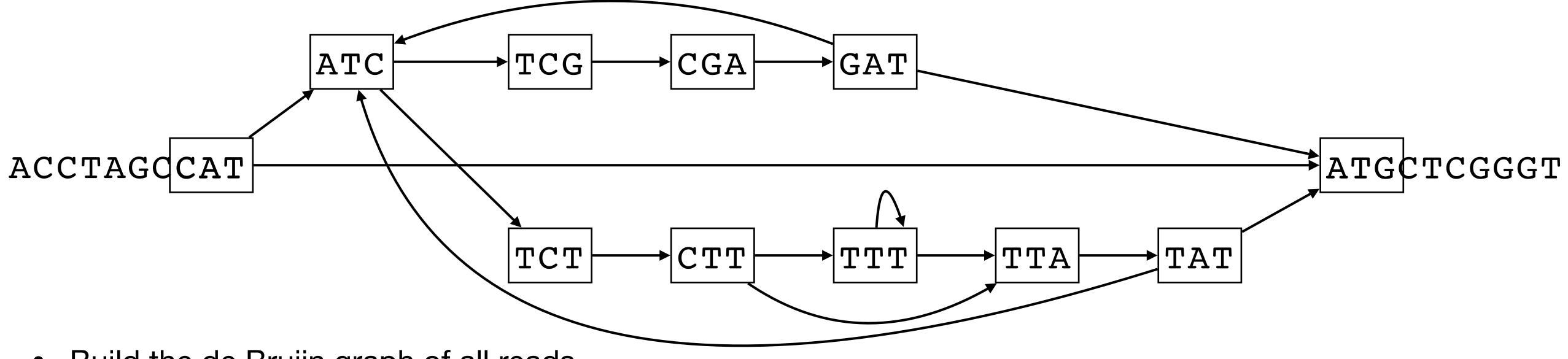


TCGATAGCTAAAATGCCGTTCGGAATTGTNNNATAGAGATATTT

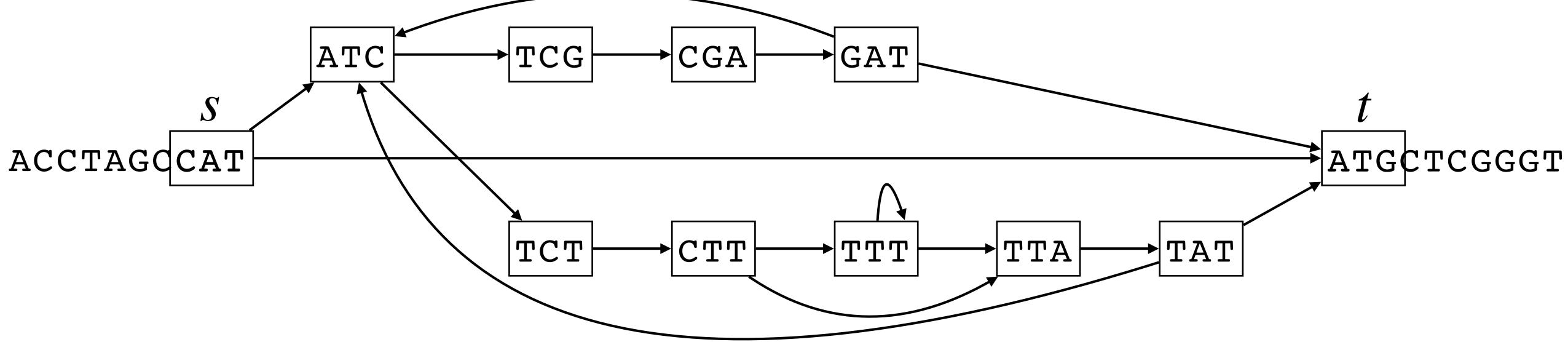
Find path of given length

ACCTAGCCAT

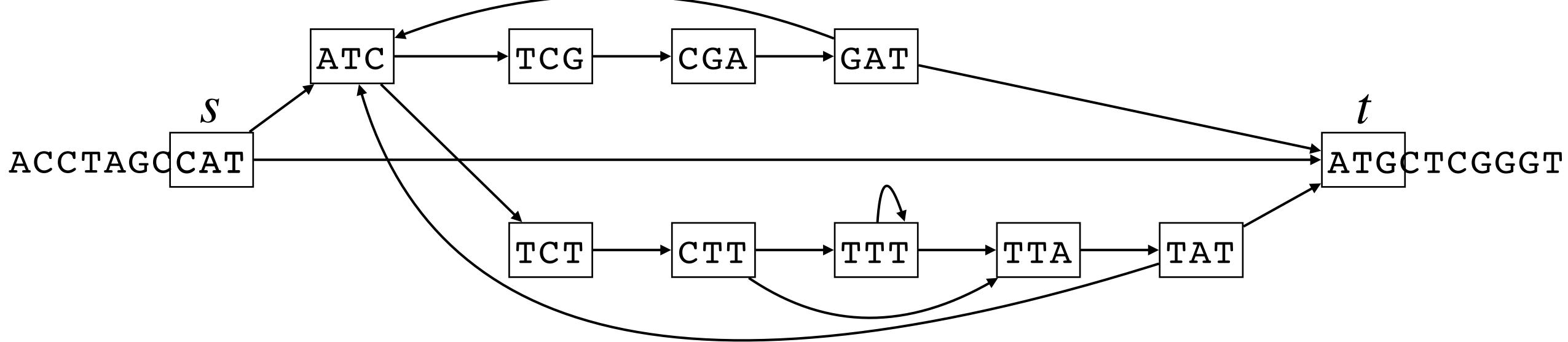
→ ATGCTCGGGT



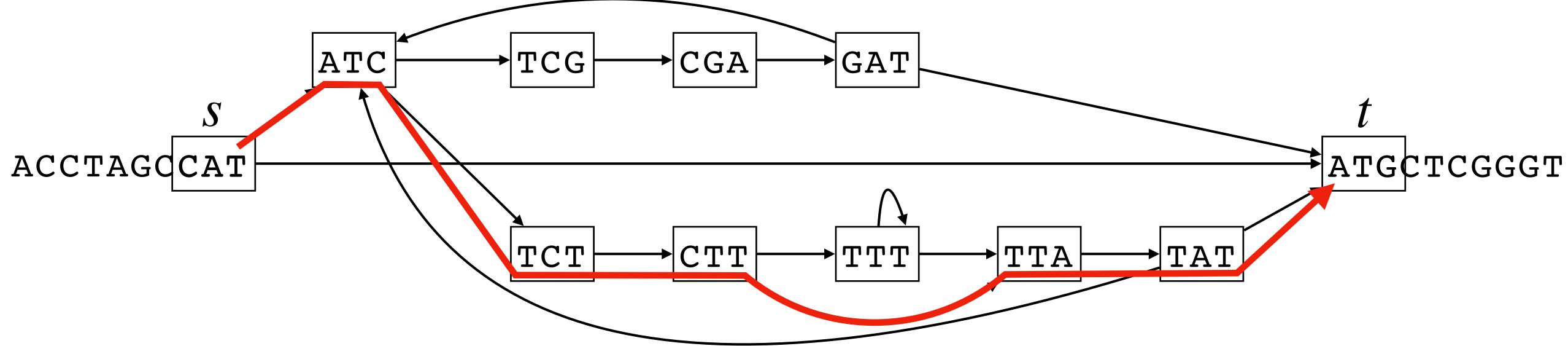
• Build the de Bruijn graph of all reads



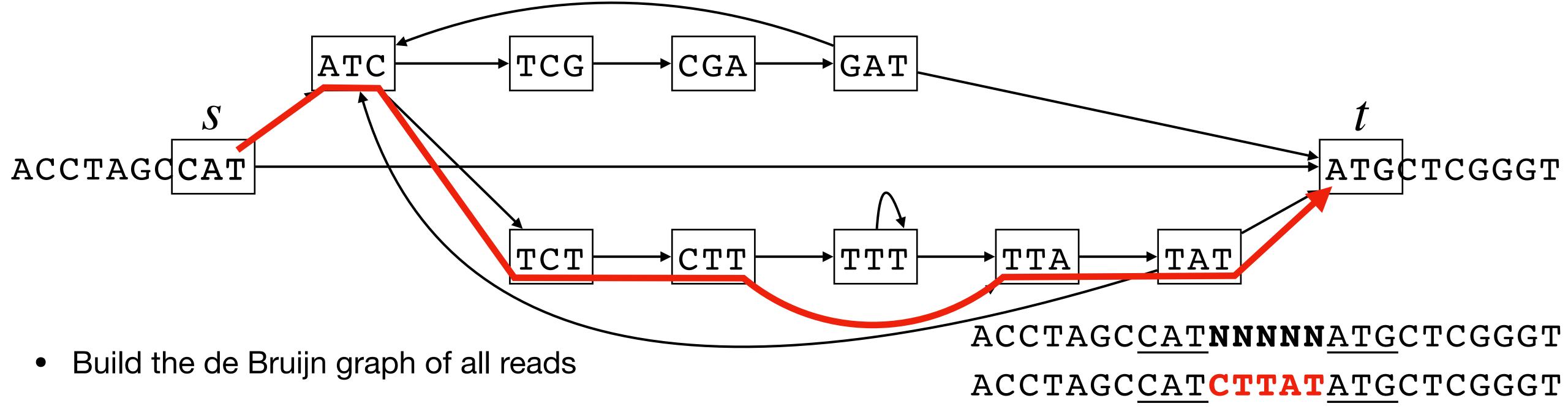
- Build the de Bruijn graph of all reads
- Take the last k-mer of the 1st contig (node s) and the first k-mer of the second contig (node t)



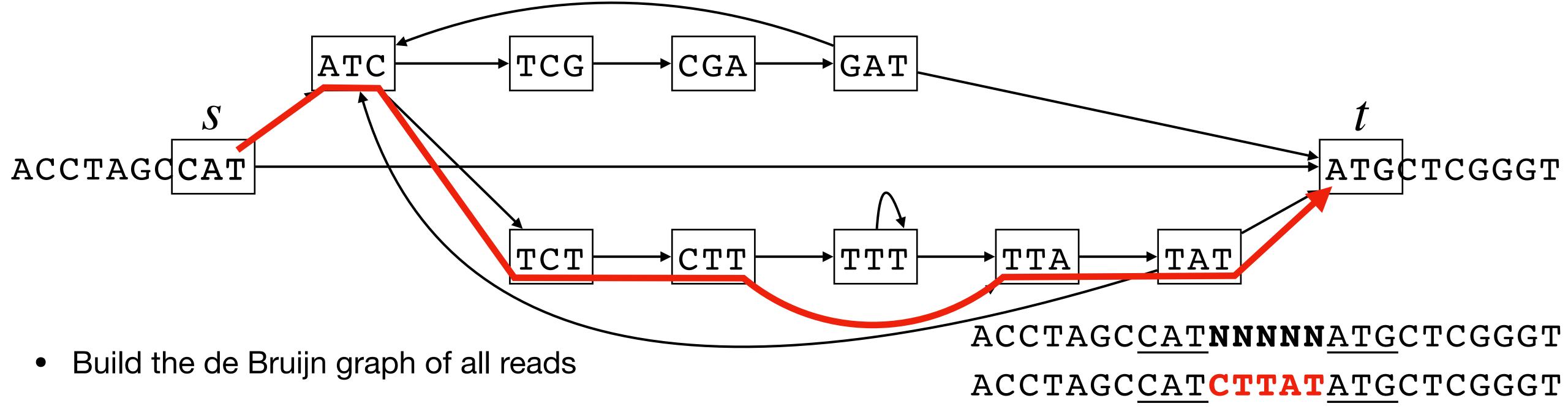
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 - If gap length estimate is d, how long should be the path? ASSIGNMENT



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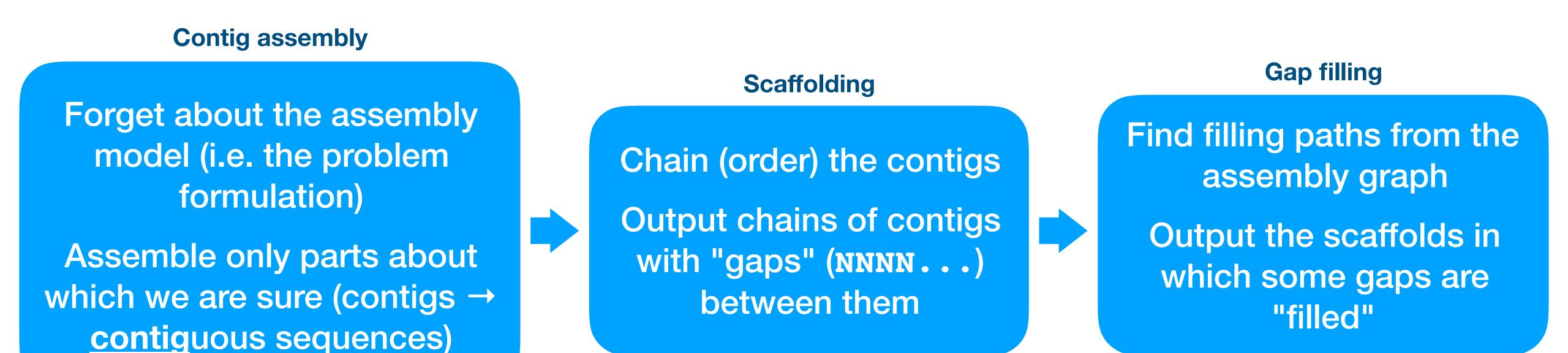


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- Can be solved by dynamic programming in time $O(d \mid edges \mid)$
 - Leena Salmela, Kristoffer Sahlin, Veli Mäkinen, Alexandru I. Tomescu:
 Gap Filling as Exact Path Length Problem. RECOMB 2015: 281-292

Section summary



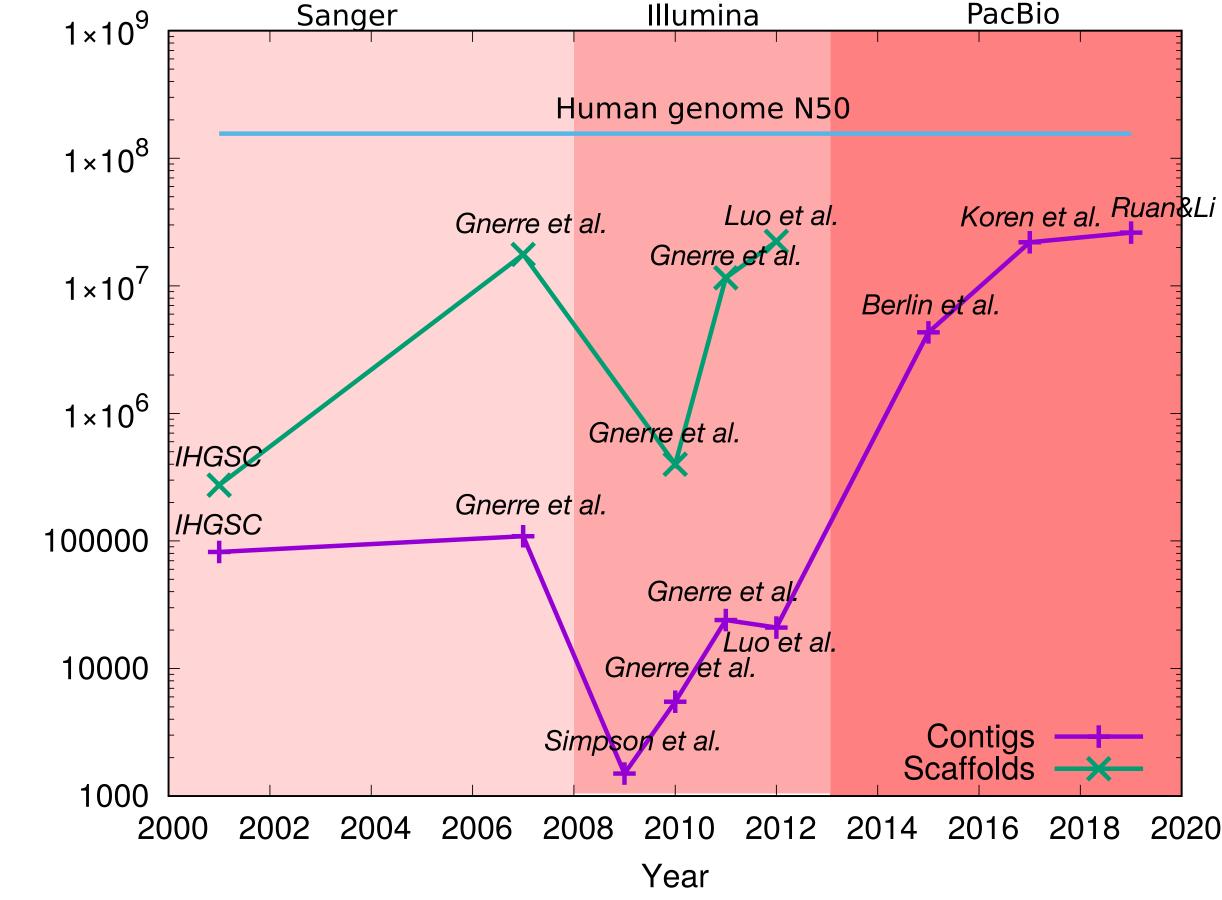
- A natural decomposition into subproblems based on the available paired-end information
- One can improve each step individually, thus improving the overall result

Long-read sequencing

(Third-generation sequencing)

- No paired-end reads (focus is on contig assembly)
- Higher error rate: 15% compared to 0.1% for short reads
 - Still developing: accurate PacBio HiFi reads
- No "clear" best strategy
- Short reads still relevant for some scenarios (e.g. metagenomic sequencing)





N50 measure → **ASSIGNMENT**

A more "practical" theoretical formulation

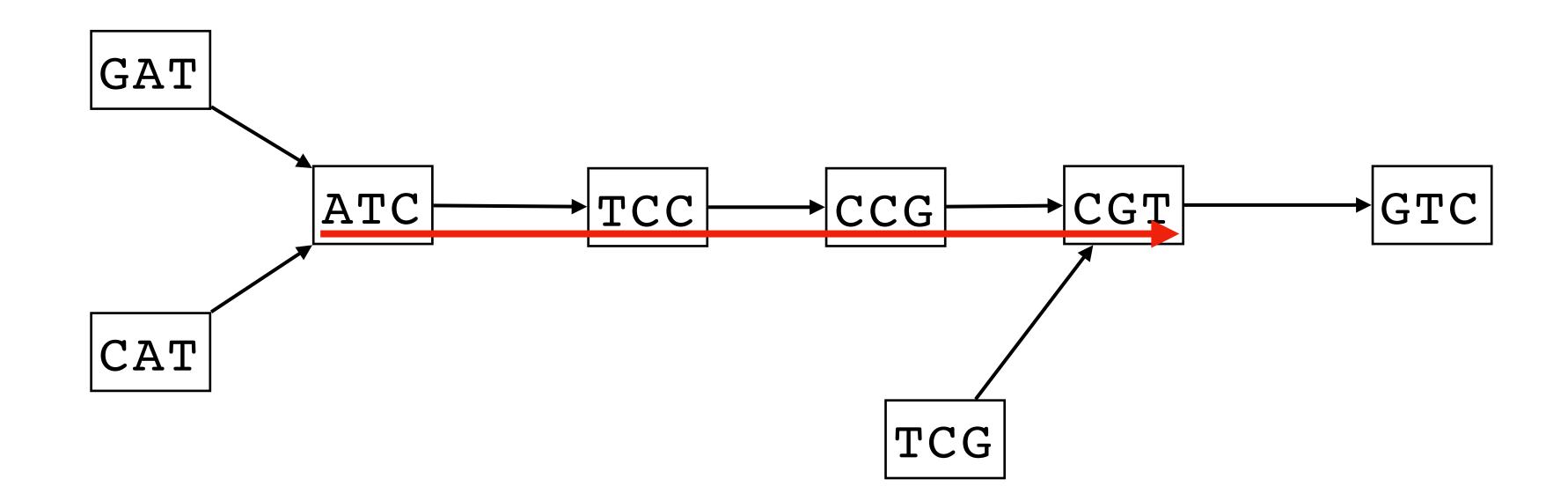
(A principled approach to contig assembly)

Goal: obtain sequences that are "guaranteed" to occur in the genome

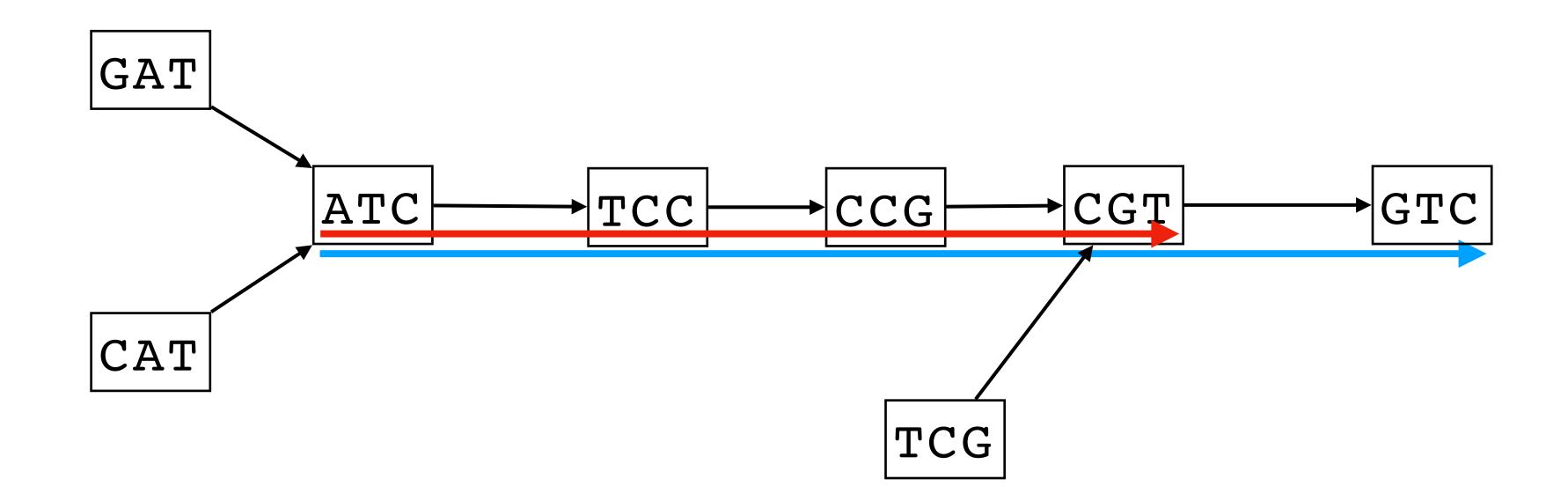
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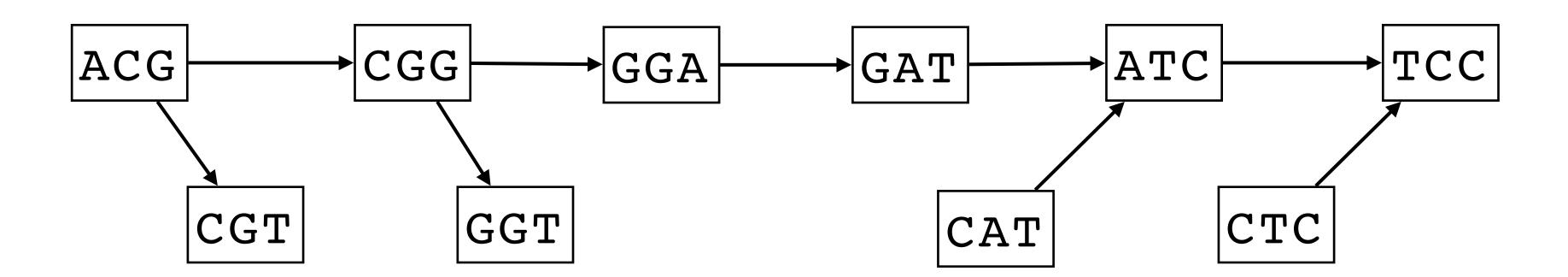


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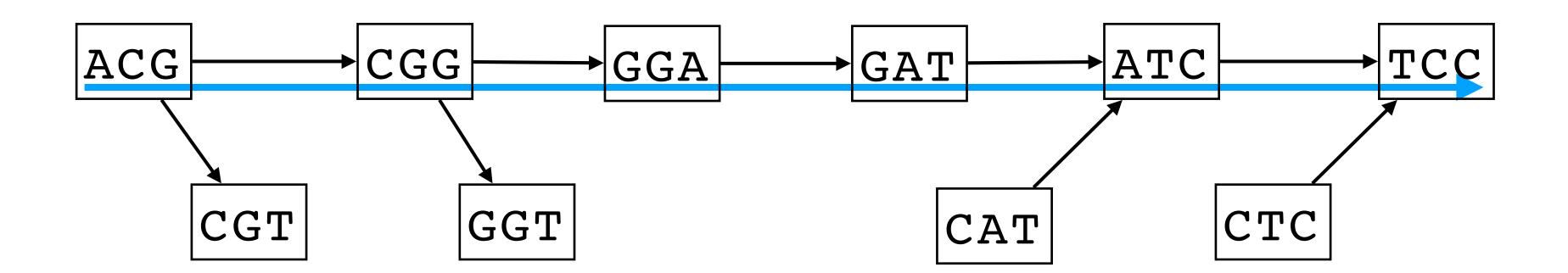


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- Is there something more to assemble?

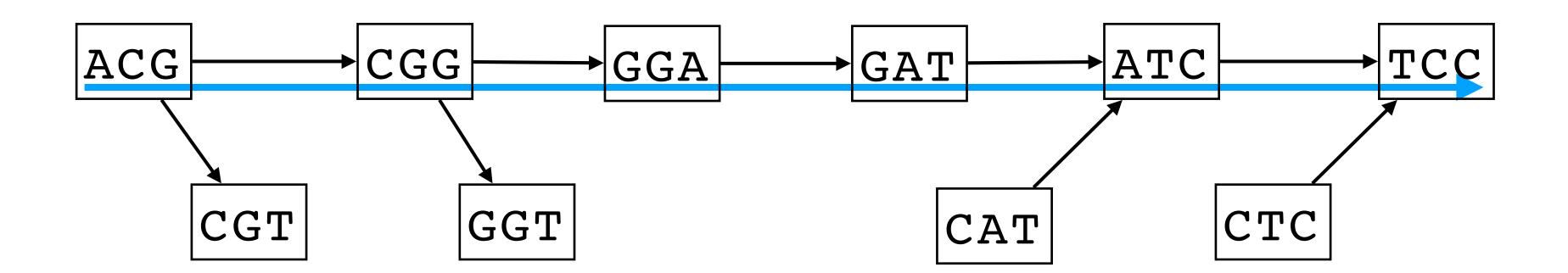
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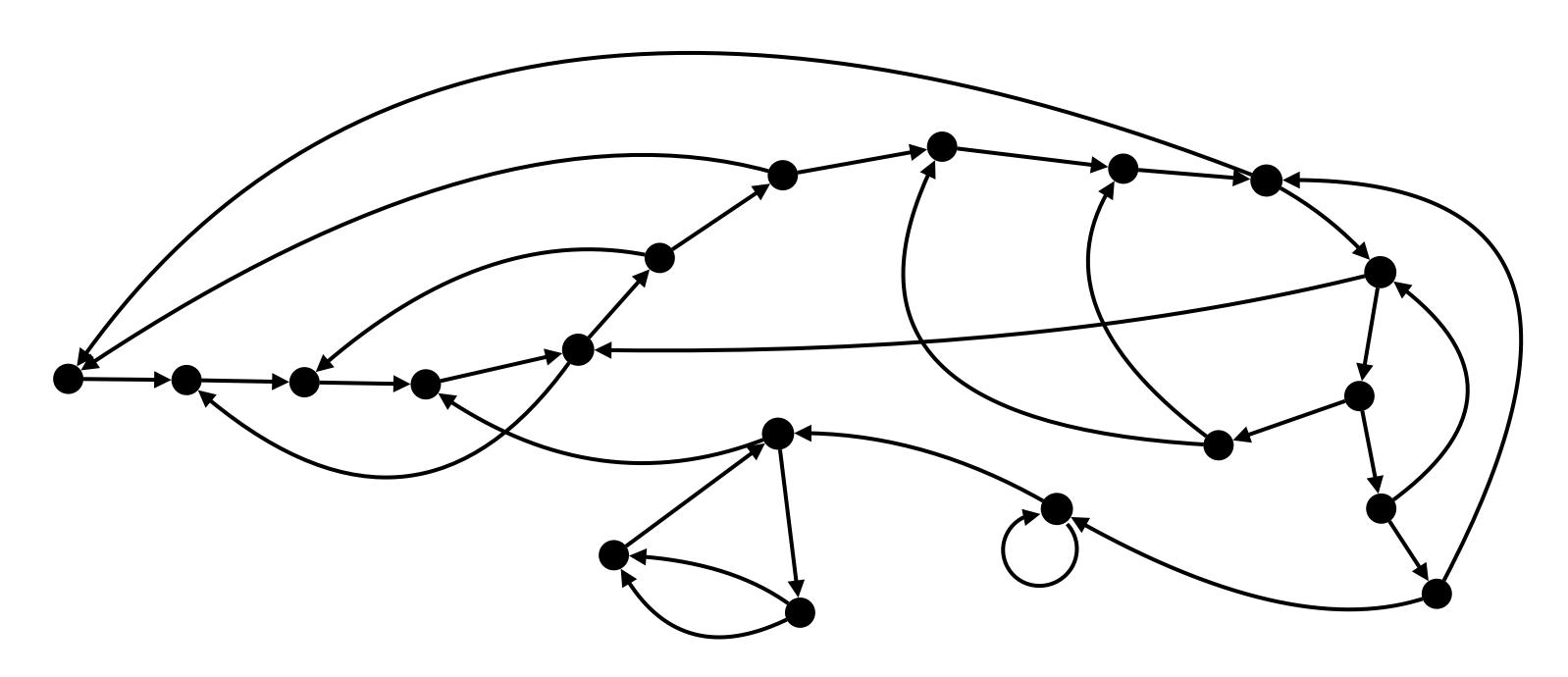


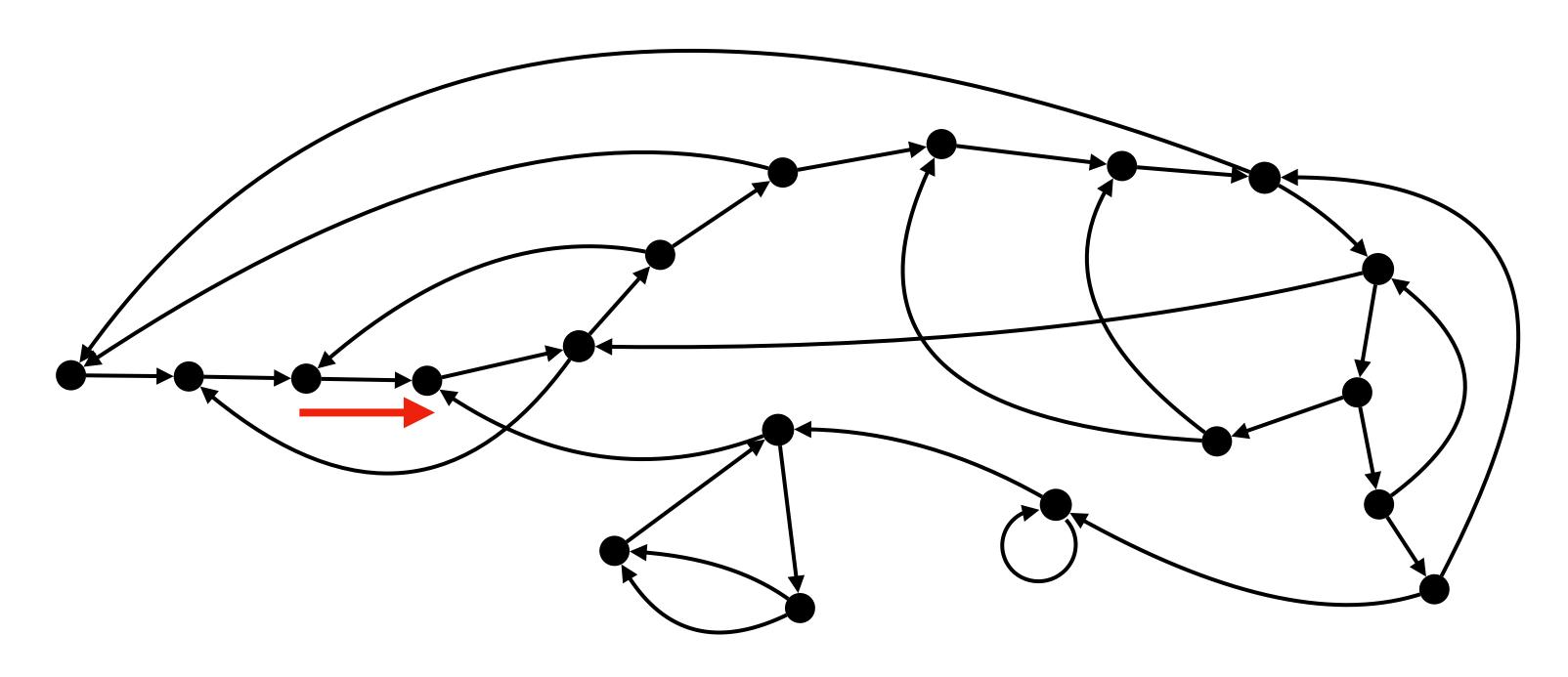
- Assume that the "genome assembly solution" is a circular walk covering every edge at least once (walk can repeat nodes)
 - Trivial to find one, exponential to find all
 - Makes sense for single circular chromosomes (i.e. most bacteria), full coverage, no errors

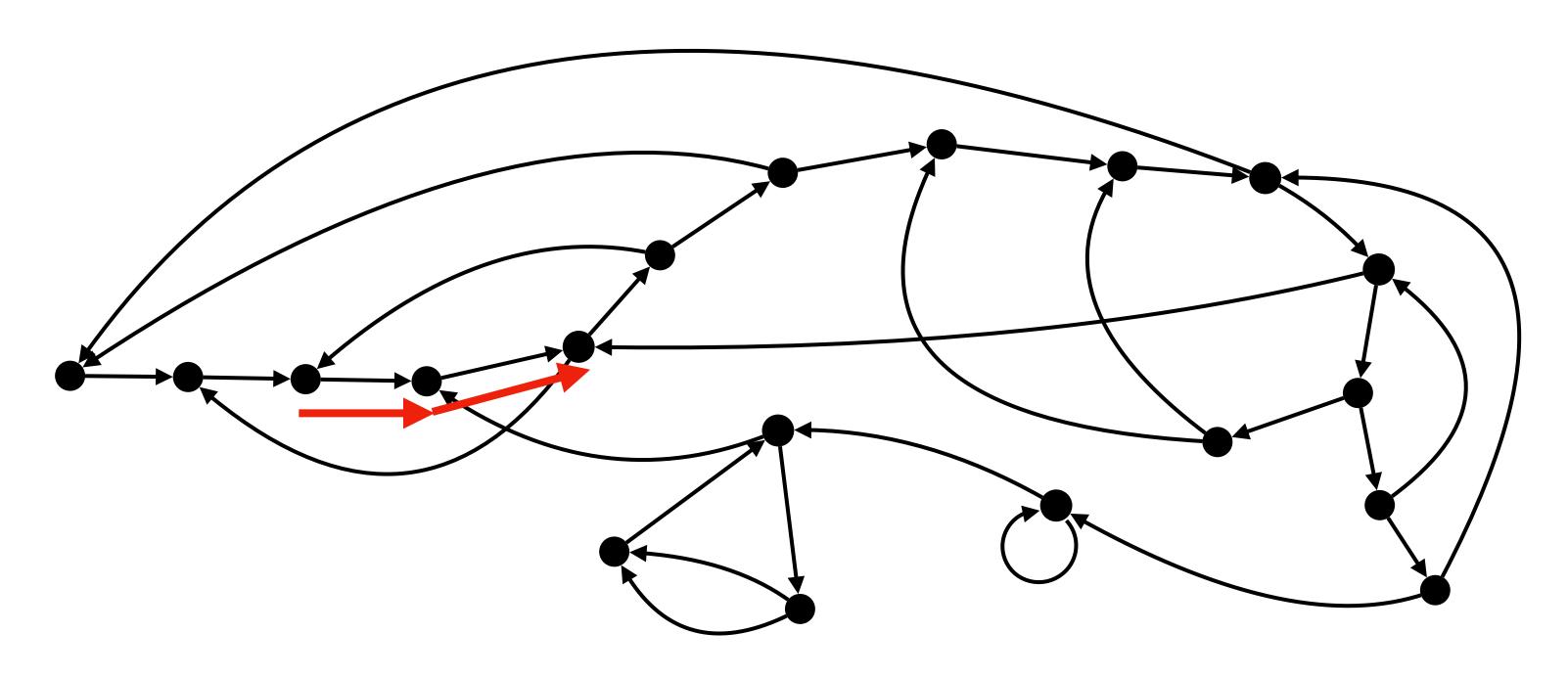
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 - Omnitigs are all that can be correctly assembled

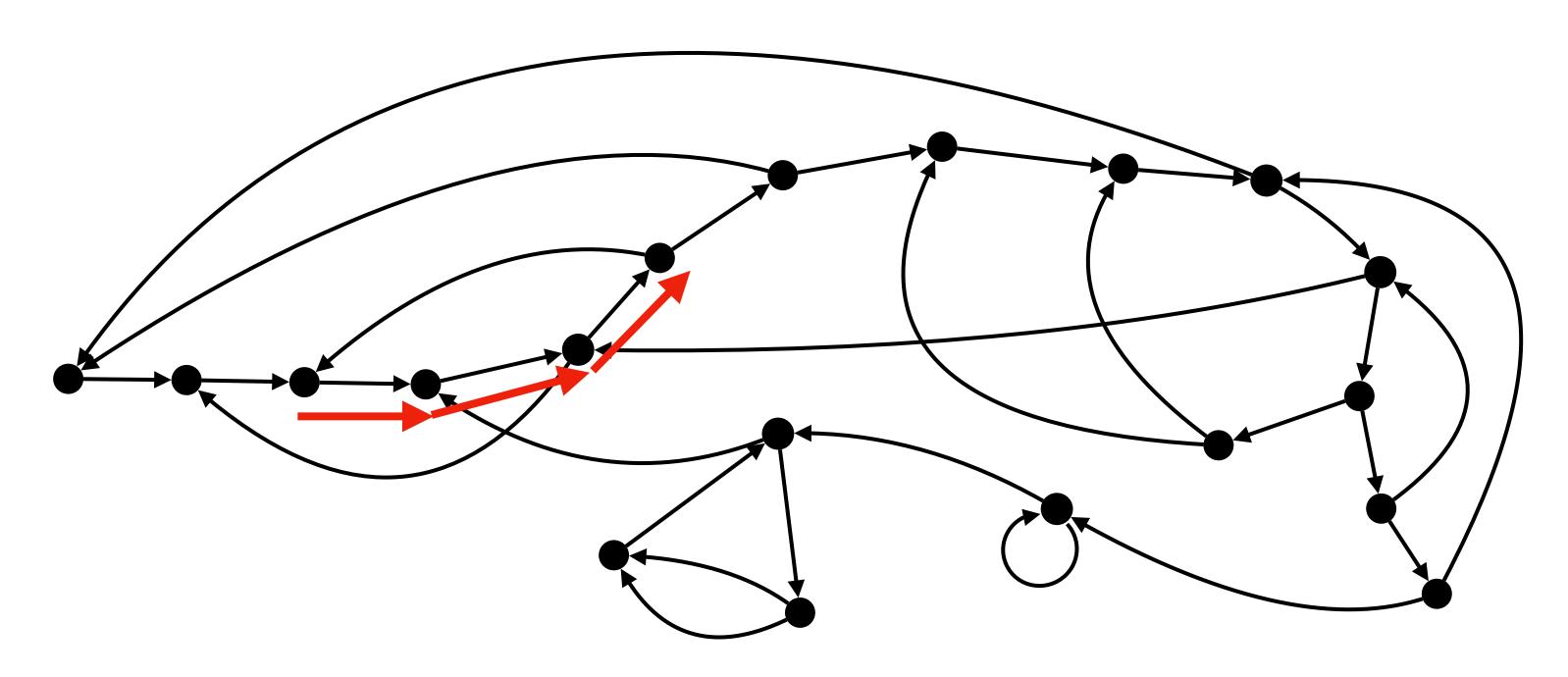
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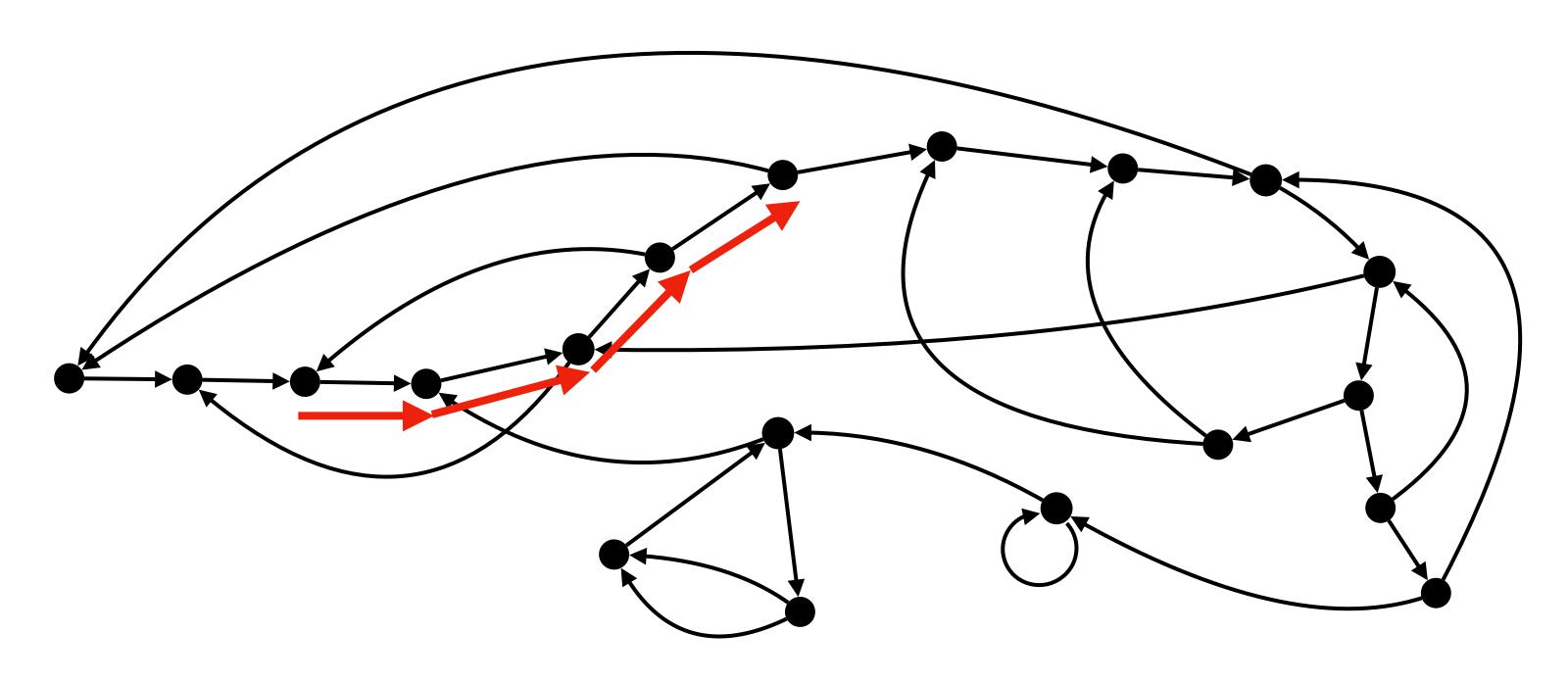
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- Can be adapted to deal with practical issues (ongoing work)
 - ► Subprojects available as Master thesis topics

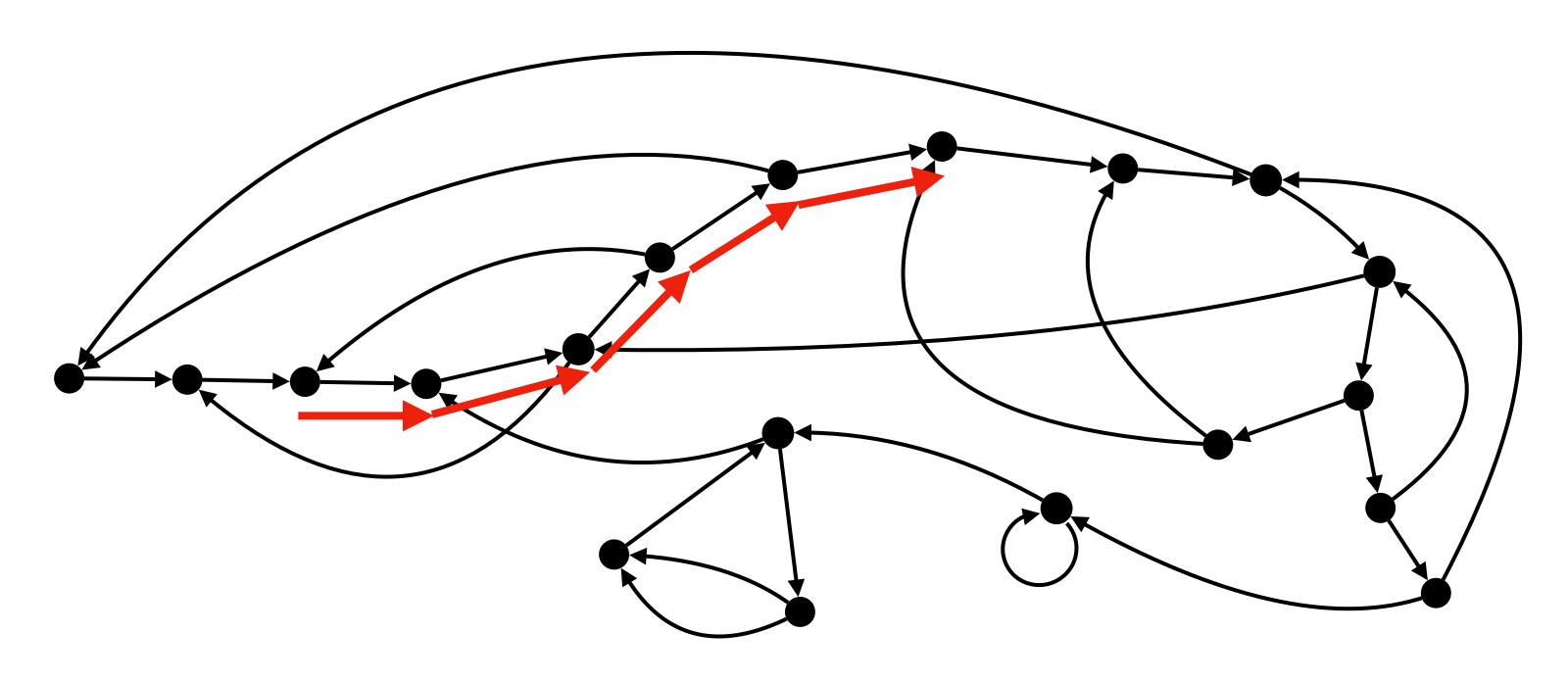


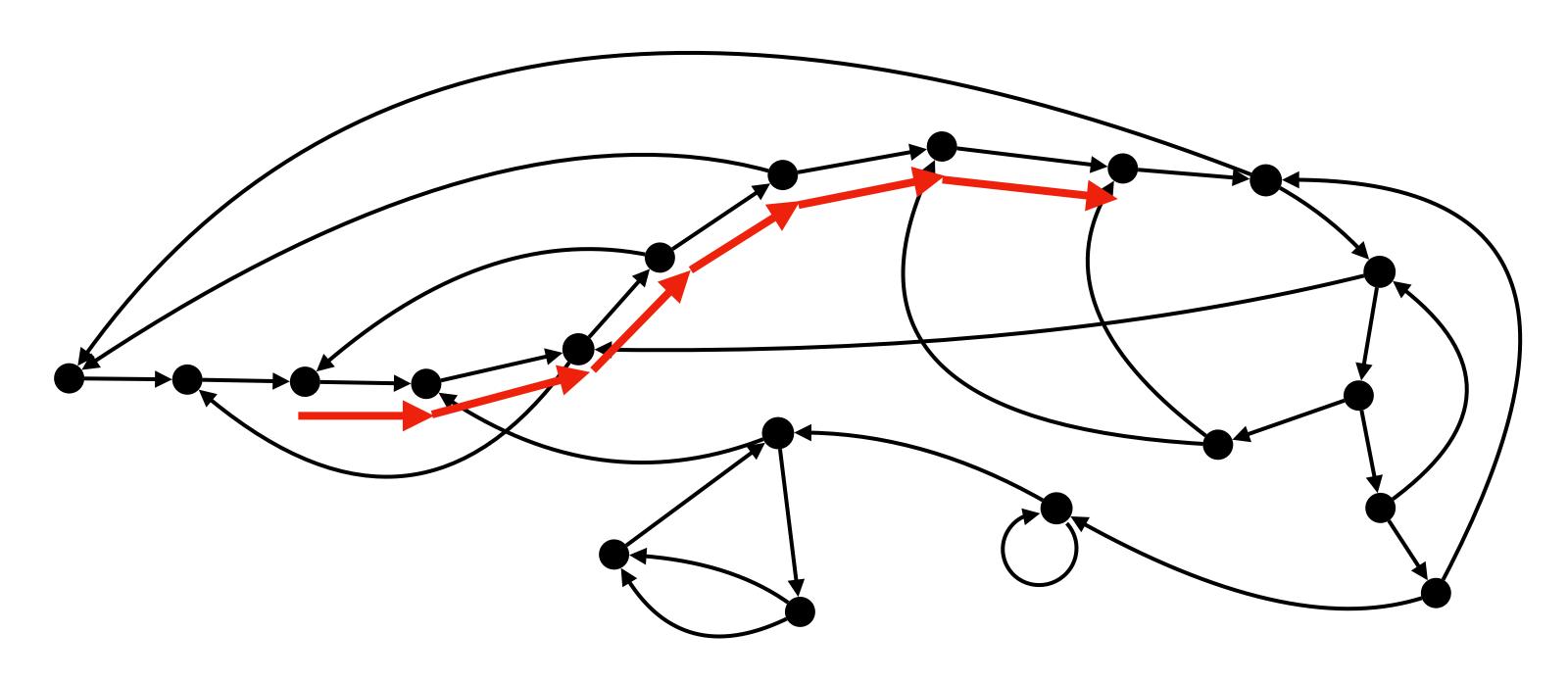


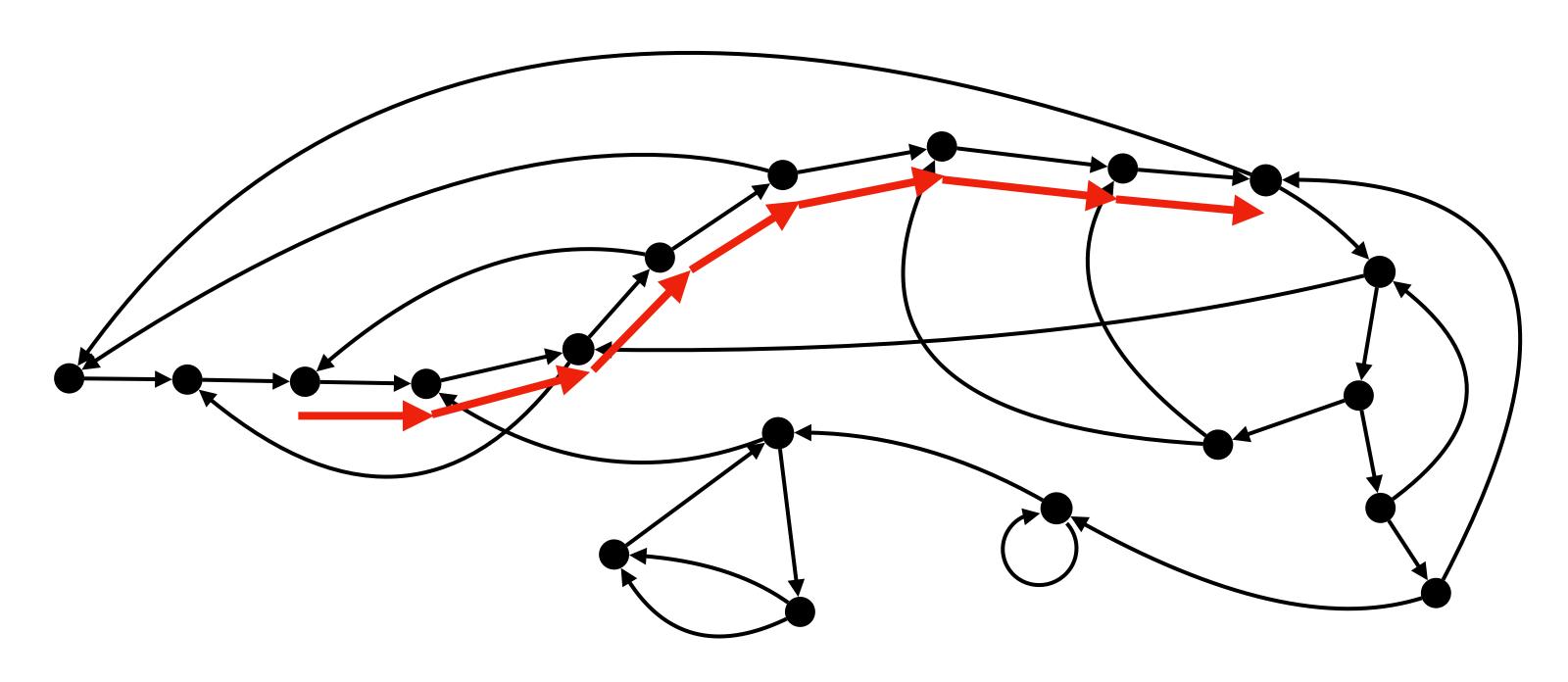


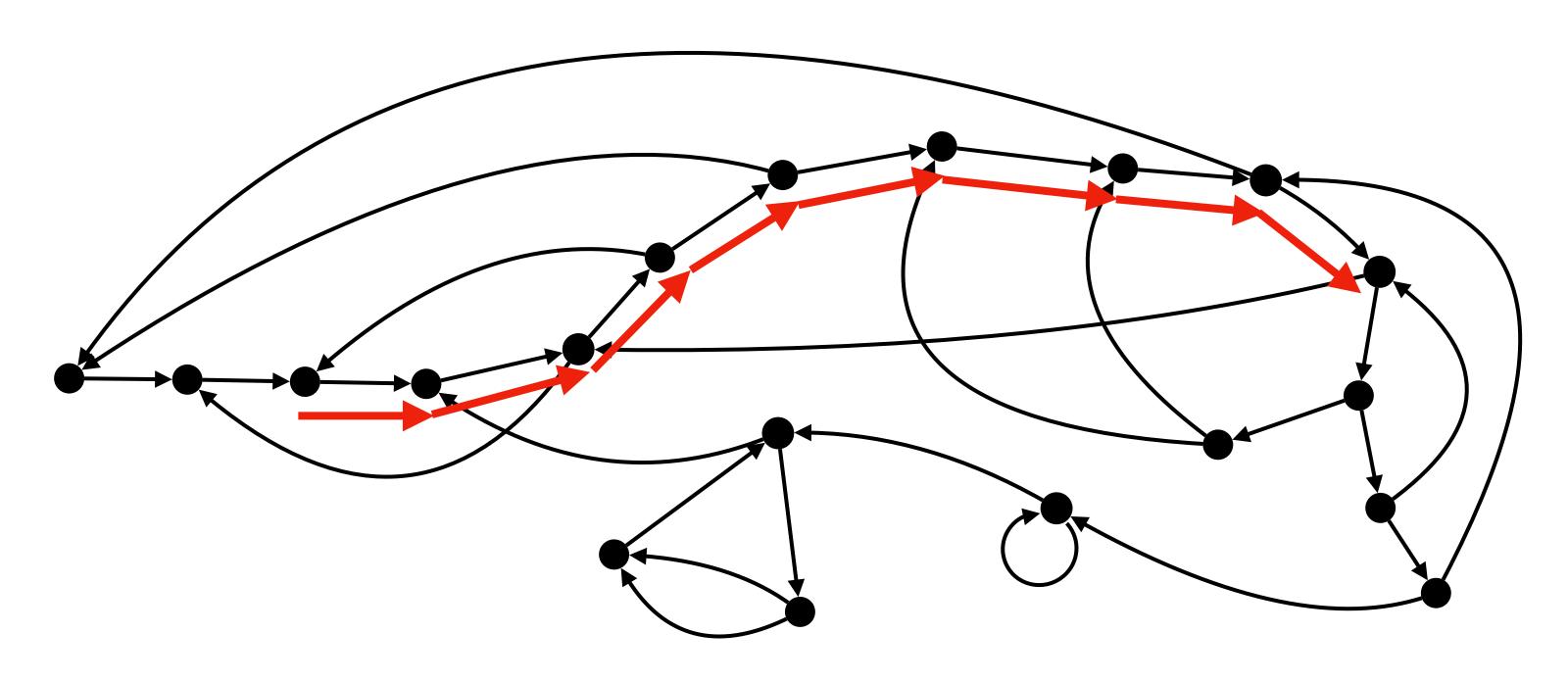


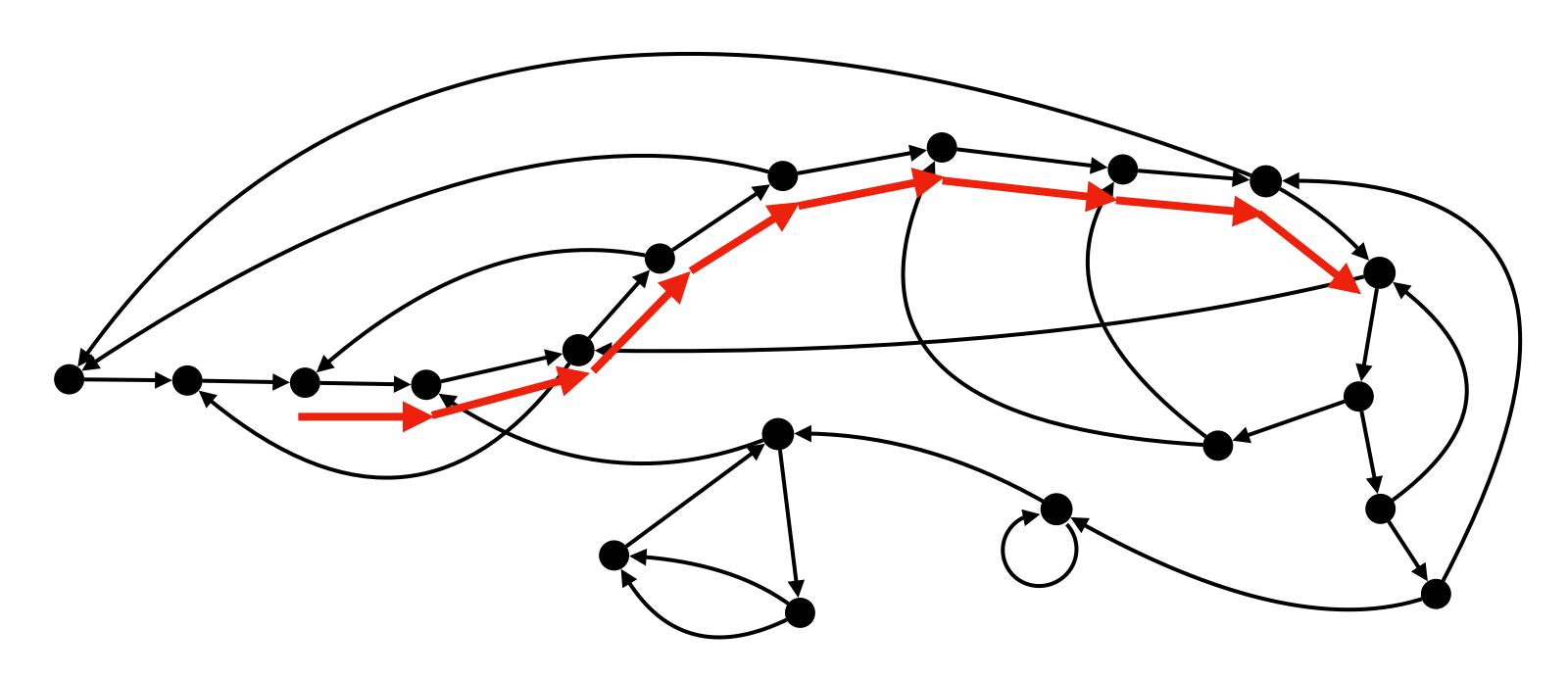












chr10, length 135M	#Strings	Avg. length	Avg. #SNPs / string
unitigs	260K	546	26
omnitigs	158K (- 40 %)	887 (+ 62 %)	41 (+58%)

Section summary

Theory is important, but more so when it is motivated by practice