

Experiment No. 6

Refractive Index and Cauchy's constants

Aim:

Determination of the refractive index μ of glass for different wavelengths λ , and Cauchy's constant a, b with the help of a prism.

Apparatus Required:

A white light source (Mercury Vapor lamp)
Prism
Spectrometer

Formulas used:

$$S_{\min} = 2(O_i - O_r)$$

$O_i = \angle$ of incidence
 $O_r = \angle$ of refraction

$$\mu = \frac{\sin\left(\frac{A + S_{\min}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$S_{\min} = \text{min. } \angle \text{ of deviation}$

$A = \text{angle of prism}$

$\mu = \text{refractive index}$

$$\mu = a + \frac{b}{\lambda^2}$$

Table 1: Measurement of angle of prism(A)

Position 1 O_1 in deg	Position 2 O_2 in deg	$2A = O_2 - O_1$ in deg.	Prism angle A (in deg)
120°	240°	120°	60°

Table 2: Measurement of angle of minimum deviation
(S_{min})
[Angle of undeviated ray (O') = 0°]

S.No	Color	Angle of deviated ray (O)	$S_{min} =$ $O - O'$ (in deg)	Refractive (in deg)	λ (nm)	$1/\lambda^2$ (nm^{-2})
1	Indigo	40.4	40.4	1.536	453.83	5.26×10^{-5}
2	Blue	40.1	40.1	1.533	491.66	4.13×10^{-5}
3	Green	39.6	39.6	1.527	546.07	3.35×10^{-5}
4	Yellow	39.4	39.4	1.525	578.0	2.99×10^{-5}
5	Orange	39.1	39.1	1.522	615.2	2.64×10^{-5}
6	Red	39	39	1.521	690.25	2.09×10^{-5}

Calculations :

$$\begin{aligned}\mu \text{ for Indigo} &= \frac{\sin\left(\frac{A + \delta_{\text{min}}}{2}\right)}{\sin\left(\frac{A}{2}\right)} \\&= \frac{\sin\left(\frac{60 + 40.4}{2}\right)}{\sin\left(\frac{60}{2}\right)} = \frac{\sin(50.2) \times 2}{\sin(30)} \\&= 1.536\end{aligned}$$

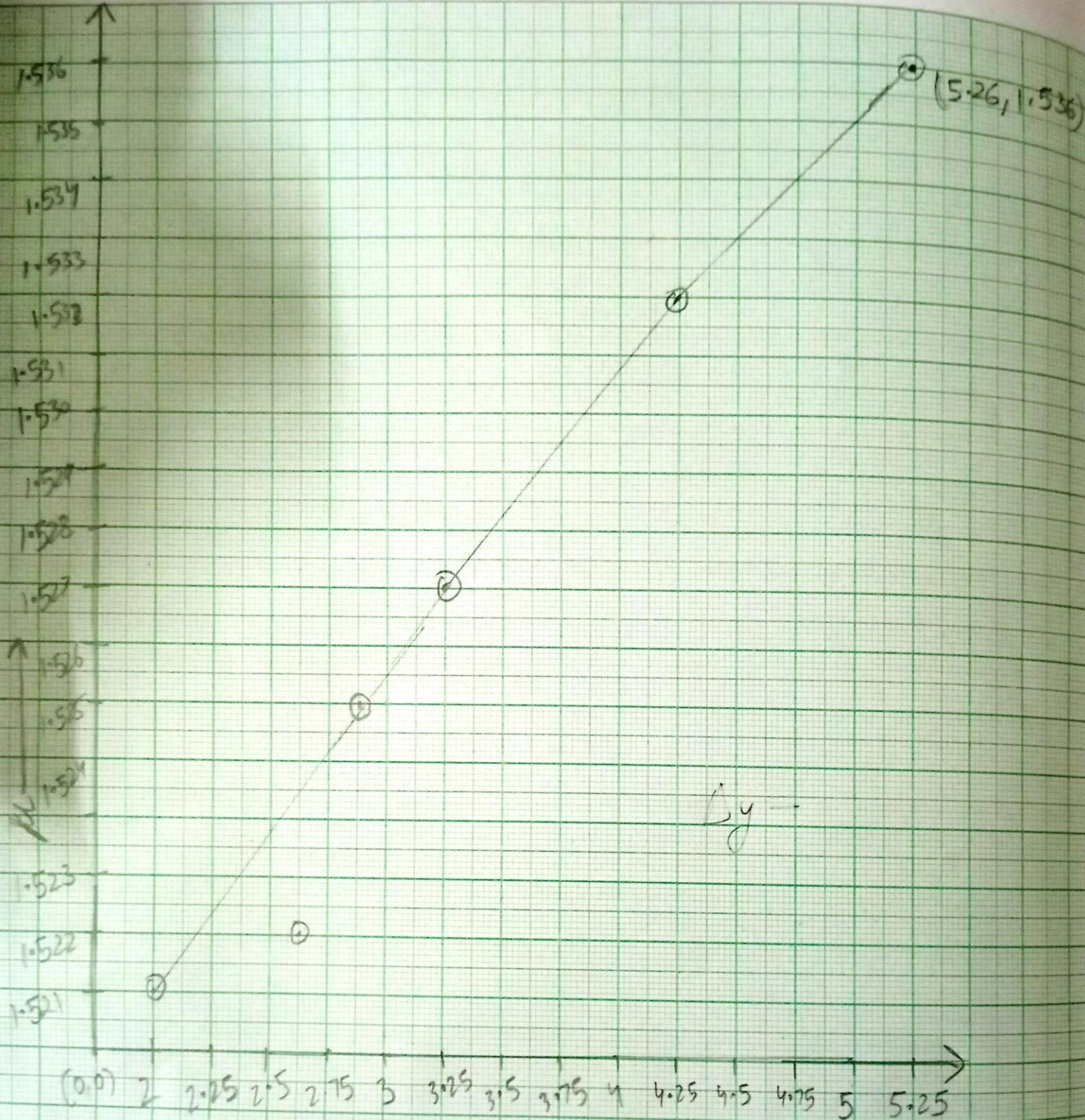
$$\begin{aligned}\mu \text{ for Blue} &= \left(\frac{\sin 100.1}{2}\right) 2 = \sin(50.05) \times 2 \\&= 1.533\end{aligned}$$

Calculation of a and b

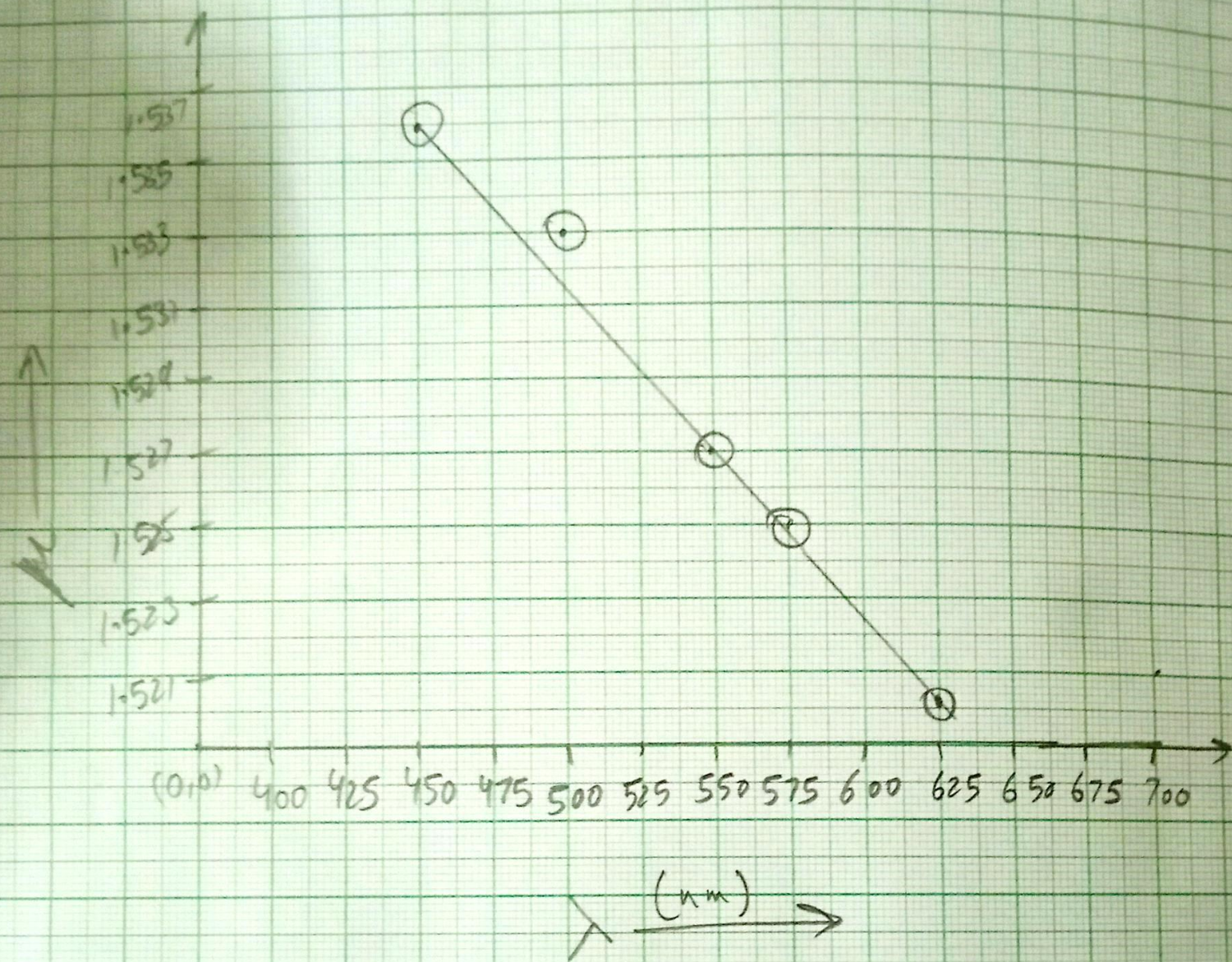
$$\begin{aligned}\Delta y &= 0.010 \\ \Delta n &= 1.5 \times 10^{-6}\end{aligned}$$

$$\begin{aligned}\frac{\Delta y}{\Delta n} &= 0.00667 \times 10^6 \\ \Rightarrow b &= 6.67 \times 10^3 \text{ nm}^2\end{aligned}$$

$$\begin{aligned}1.521 &= a + \left[6.67 \times 10^3 \times 2.09 \times 10^{-6} \right] \\ 1.521 &= a + 0.01384 \Rightarrow a = 1.507\end{aligned}$$



$$\frac{1}{\lambda^2} \rightarrow (\text{nm}^{-2}) (\times 10^{-6})$$



Result and conclusion

We have found out the refractive indexes and the cauchy constants with the help of a prism