

# Selection Sort e Insertion Sort

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# Agenda

1 Selection Sort

2 Insertion Sort

3 Exercícios

4 Referências

# Selection Sort

- Busca pelo menor elemento no vetor;

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- Depois posiciona ele na primeira posição;

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- Busca pelo menor elemento no vetor;
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- Realiza novamente o processo para todos elementos até  $n - 1$ ;

# Selection Sort

- Busca pelo menor elemento no vetor;
- Depois posiciona ele na primeira posição;
- Realiza novamente o processo para todos elementos até  $n - 1$ ;
- Complexidade dele:  $O(n^2)$ .

# Selection Sort

Vamos ordenar este vetor!

|    |   |    |   |    |
|----|---|----|---|----|
| 20 | 4 | 15 | 7 | 10 |
| 0  | 1 | 2  | 3 | 4  |

# Selection Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 20 | 4 | 15 | 7 | 10 |
| 0  | 1 | 2  | 3 | 4  |

↑    ↑

*i*    *j*

*troca* = 0

- inicializa  $i = 0$ ;  $j = i + 1$ ;



# Selection Sort

|          |          |    |   |    |
|----------|----------|----|---|----|
| 20       | 4        | 15 | 7 | 10 |
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| ↑        | ↑        |    |   |    |
| <i>i</i> | <i>j</i> |    |   |    |

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- $20 > 4$  ? Sim

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- $troca = j$

# Selection Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 20 | 4 | 15 | 7 | 10 |
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↑

*i*

↑

*j*

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# Selection Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 20 | 4 | 15 | 7 | 10 |
| 0  | 1 | 2  | 3 | 4  |
| ↑  |   | ↑  |   |    |
| i  |   | j  |   |    |

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|    |   |    |   |    |
|----|---|----|---|----|
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- próximo

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*troca = 1*

- finalizou o vetor

# Selection Sort

|    |   |    |   |    |
|----|---|----|---|----|
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| ↑  |   |    |   | ↑  |
| i  |   |    |   | j  |

*troca* = 1

- finalizou o vetor
- $swap(vetor[i], vetor[troca])$

# Selection Sort

|          |   |    |   |          |
|----------|---|----|---|----------|
| 20       | 4 | 15 | 7 | 10       |
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| ↑        |   |    |   | ↑        |
| <i>i</i> |   |    |   | <i>j</i> |

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- $swap(vetor[i], vetor[troca])$
- $i = i + 1; j = i + 1; troca = i$

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- $20 > 15$  ? Sim
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# Selection Sort

|   |    |    |   |    |
|---|----|----|---|----|
| 4 | 20 | 15 | 7 | 10 |
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↑

i

↑

j

*troca* = 2

- $j = j + 1;$

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|   |    |    |   |    |
|---|----|----|---|----|
| 4 | 20 | 15 | 7 | 10 |
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|   | i  |    |   | j  |

*troca* = 3

- $j = j + 1;$

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|   |    |    |   |    |
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| 4 | 20 | 15 | 7 | 10 |
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| 4 | 7 | 10 | 15 | 20 |
| 0 | 1 | 2  | 3  | 4  |

Vetor Ordenado

# Selection Sort

```
vetor[] = {20, 4, 15, 7, 10}
```

```
for (i = 0; i < vetor.length - 1; i++)  
    indice_menor = i  
    for (j = i + 1; j < vetor.length; j++)  
        if (vetor[j] < vetor[indice_menor])  
            indice_menor = j  
    swap(vetor[j], vetor[j + 1])
```

# Insertion Sort

- Utilizando um vetor auxiliar;



# Insertion Sort

- Utilizando um vetor auxiliar;
- Os elementos são inseridos na posição correta;

# Insertion Sort

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# Insertion Sort

Vamos ordenar este vetor!

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| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

|  |  |  |  |  |
|--|--|--|--|--|
|  |  |  |  |  |
|--|--|--|--|--|

# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |



|    |  |  |  |  |
|----|--|--|--|--|
| 20 |  |  |  |  |
|----|--|--|--|--|



*ordenando = 20*

- inicializa  $i = 0$ ; inicializa  $j = i - 1$

# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |



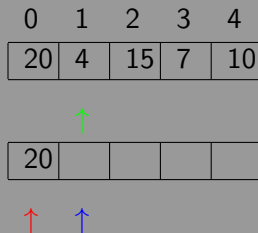
|    |  |  |  |  |
|----|--|--|--|--|
| 20 |  |  |  |  |
|----|--|--|--|--|



*ordenando* = 20

- inicializa  $i = 0$ ; inicializa  $j = i - 1$
- $j = -1$  então copia *ordenando* na posição  $j + 1$

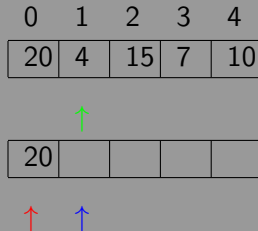
# Insertion Sort



*ordenando = 4*

- $i = i + 1$ ; inicializa  $j = i - 1$

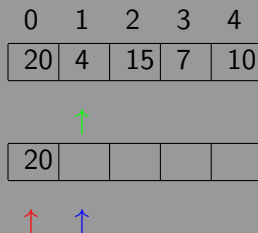
# Insertion Sort



*ordenando = 4*

- $i = i + 1$ ; inicializa  $j = i - 1$
- $4 < 20$  ? Sim

# Insertion Sort



*ordenando = 4*

- $i = i + 1$ ; inicializa  $j = i - 1$
- $4 < 20$  ? Sim
- copia 20 para a posição  $i$



# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

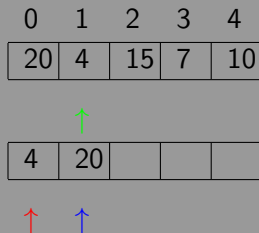
|   |    |  |  |  |
|---|----|--|--|--|
|   |    |  |  |  |
| 4 | 20 |  |  |  |



*ordenando = 4*

- $j = j - 1$

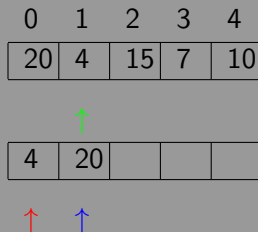
# Insertion Sort



*ordenando = 4*

- $j = j - 1$
- acabou vetor

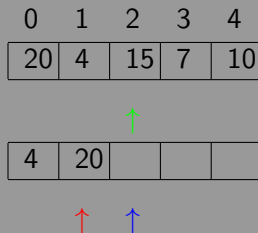
# Insertion Sort



*ordenando* = 4

- $j = j - 1$
- acabou vetor
- copia *ordenando* na posição  $j + 1$

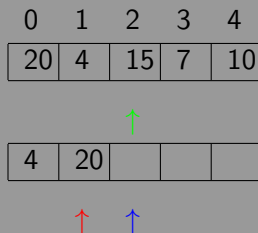
# Insertion Sort



*ordenando = 15*

- $i = i + 1; j = i - 1$

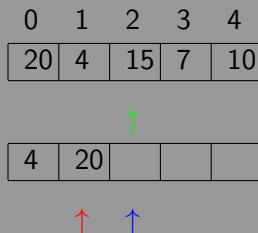
# Insertion Sort



*ordenando = 15*

- $i = i + 1; j = i - 1$
- $15 < 20$  ? Sim

# Insertion Sort



*ordenando = 15*

- $i = i + 1; j = i - 1$
- $15 < 20$  ? Sim
- copia 20 para a posição  $i$

# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

|   |  |    |  |  |
|---|--|----|--|--|
| 4 |  | 20 |  |  |
|---|--|----|--|--|

- $j = j - 1$

# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

|   |  |    |  |  |
|---|--|----|--|--|
| 4 |  | 20 |  |  |
|---|--|----|--|--|

- $j = j - 1$
- $15 < 4$  ? Não



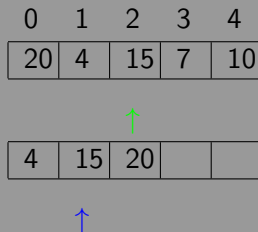
# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

|   |  |    |  |  |
|---|--|----|--|--|
| 4 |  | 20 |  |  |
|---|--|----|--|--|

- $j = j - 1$
- $15 < 4$  ? Não
- acabou iteração

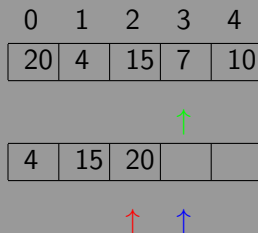
# Insertion Sort



*ordenando* = 15

- copia *ordenando* na posição  $j + 1$

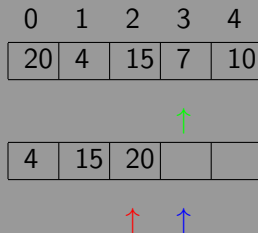
# Insertion Sort



*ordenando = 7*

- $i = i + 1; j = i - 1$

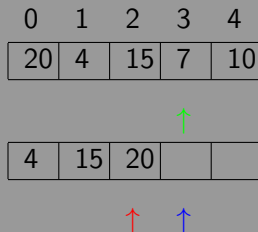
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*ordenando = 7*

- $i = i + 1; j = i - 1$
- $7 < 20$  ? Sim

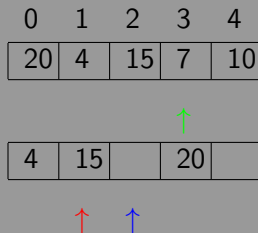
# Insertion Sort



*ordenando = 7*

- $i = i + 1; j = i - 1$
- $7 < 20$  ? Sim
- copia 20 para a posição  $i$

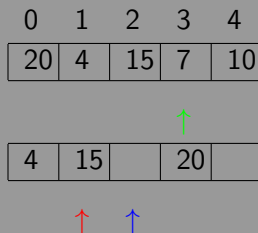
# Insertion Sort



*ordenando = 7*

- $j = i - 1$

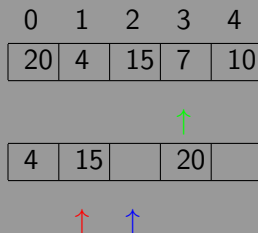
# Insertion Sort



*ordenando = 7*

- $j = i - 1$
- $7 < 15$  ? Sim

# Insertion Sort



*ordenando = 7*

- $j = i - 1$
- $7 < 15$  ? Sim
- copia 15 para a posição  $i - 1$



# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

|   |  |    |    |  |
|---|--|----|----|--|
|   |  |    | ↑  |  |
| 4 |  | 15 | 20 |  |



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|----|---|----|---|----|
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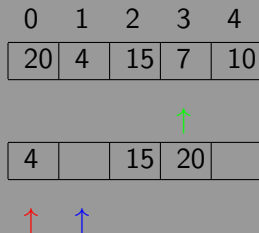
|   |  |    |    |  |
|---|--|----|----|--|
|   |  |    | ↑  |  |
| 4 |  | 15 | 20 |  |



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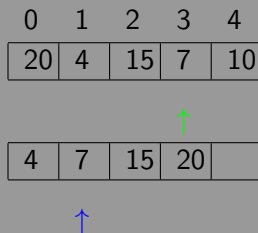
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- $7 < 4$  ? Não
- acabou iteração

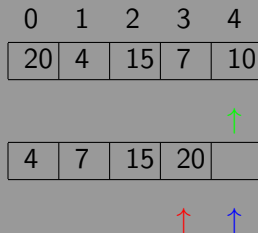
# Insertion Sort



*ordenando = 7*

- copia *ordenando* na posição  $j + 1$

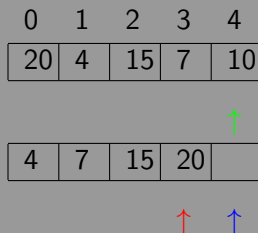
# Insertion Sort



*ordenando = 10*

- $i = i + 1; j = i - 1$

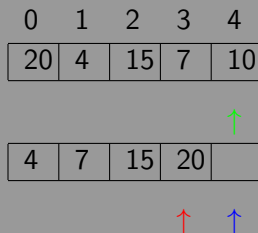
# Insertion Sort



*ordenando = 10*

- $i = i + 1; j = i - 1$
- $10 < 20$  ? Sim

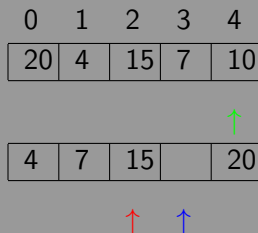
# Insertion Sort



*ordenando = 10*

- $i = i + 1; j = i - 1$
- $10 < 20$  ? Sim
- copia 20 para a posição  $i$

# Insertion Sort

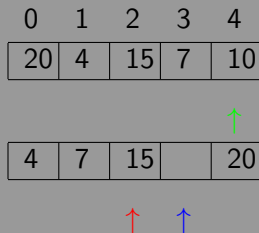


*ordenando = 10*

- $j = i - 1$



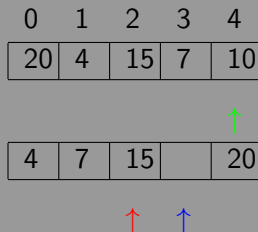
# Insertion Sort



*ordenando = 10*

- $j = i - 1$
- $10 < 15$  ? Sim

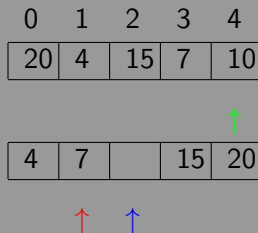
# Insertion Sort



*ordenando = 10*

- $j = i - 1$
- $10 < 15$  ? Sim
- copia 15 para a posição  $i - 1$

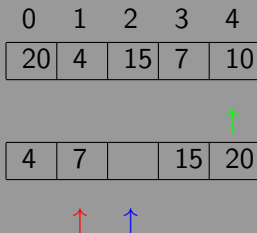
# Insertion Sort



*ordenando = 10*

- $j = i - 1$

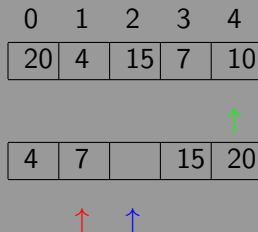
# Insertion Sort



*ordenando = 10*

- $j = i - 1$
- $10 < 7$  ? Não

# Insertion Sort



*ordenando = 10*

- $j = i - 1$
- $10 < 7$  ? Não
- acabou iteração

# Insertion Sort

|    |   |    |   |    |
|----|---|----|---|----|
| 0  | 1 | 2  | 3 | 4  |
| 20 | 4 | 15 | 7 | 10 |

|   |   |    |    |    |
|---|---|----|----|----|
| 4 | 7 | 10 | 15 | 20 |
|---|---|----|----|----|



*ordenando* = 10

- copia *ordenando* na posição  $j + 1$

# Insertion Sort

|   |   |    |    |    |
|---|---|----|----|----|
| 0 | 1 | 2  | 3  | 4  |
| 4 | 7 | 10 | 15 | 20 |

Acabou! Vetor Auxiliar Ordenado!

# Insertion Sort

```
vetor[] = {20, 4, 15, 7, 10}
```

```
for (int i = 0; i < array.length; i++)  
    int a = array[i]  
    for (int j = i - 1; j >= 0 & array[j] > a; j--)  
        array[j + 1] = array[j]  
        array[j] = a
```



# Exercícios

- 1 Implemente o método de ordenação Selection Sort.
- 2 Implemente o método de ordenação Insertion Sort.
- 3 Teste todos os algoritmos em um algoritmo principal

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- ③ Ascencio, Ana Fernanda Gomes, and Graziela Santos de Araújo. “Estruturas de Dados: algoritmos, análise da complexidade e implementações em JAVA e C/C++.” São Paulo: Perarson Prentice Halt 3 (2010).