

## Topics to discuss

Solve  $T(n) = \begin{cases} 1 & \text{if } n=1 \\ T(n-1) + n(n-1) & \text{if } n \geq 2 \end{cases}$

by substitution Method

### Problem 3:

$$T(n) = \begin{cases} 1 & , \text{ if } n=1 \\ T(n-1) + n(n-1) & , \text{ if } n \geq 2 \end{cases}$$

$$T(n) = 1, n=1 \\ \underline{T(1) = 1.}$$

Solution :-  $T(n) = T(n-1) + n(n-1)$  — (1)

Assume,  $n-k=1$   
 $k = n-1$

Put,  $n \rightarrow n-1$   
 $T(n-1) = T(n-2) + (n-1)(n-2)$

Put,  $n \rightarrow n-2$   
 $T(n-2) = T(n-3) + (n-2)(n-3)$

Substitute in eqn. — (1)

$$\begin{aligned} T(n) &= T(n-1) + n(n-1) \\ &= T(n-2) + (n-1)(n-2) + n(n-1) \\ &= T(n-3) + (n-2)(n-3) + (n-1)(n-2) + n(n-1) \\ &= T(n-3) + (n-3)(n-2) + (n-2)(n-1) + (n-1)n \\ &\vdots \\ &= T(n-k) + (n-k)(n-k+1) + (n-k+1)(n-k+2) + \dots + (n-1)n \end{aligned}$$

$$T(n) = T(n-k) + (n-k)(n-k+1) + (n-k+1)(n-k+2) + \dots + (n-1)n$$

$$\approx T(1) + 1 \cdot 2 + 2 \cdot 3 + \dots + (n-1)n.$$

$$= 1 + \sum_{i=1}^n i(i-1)$$

$$= 1 + \sum_{i=1}^n i^2 - \sum_{i=1}^n i$$

$$= 1 + \frac{n(n+1)(2n+1)}{6} - \frac{n(n+1)}{2}$$

$$T(n) \approx O(n^3)$$

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