

 nesoacademy.org/cs/12-compiler-design/ppts/03-top-downparsers





Outcome

- ☆ Definition of Parser.
- ☆ Ways of generating Parse trees.
- ☆ Classification of Parsers.

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Parser:

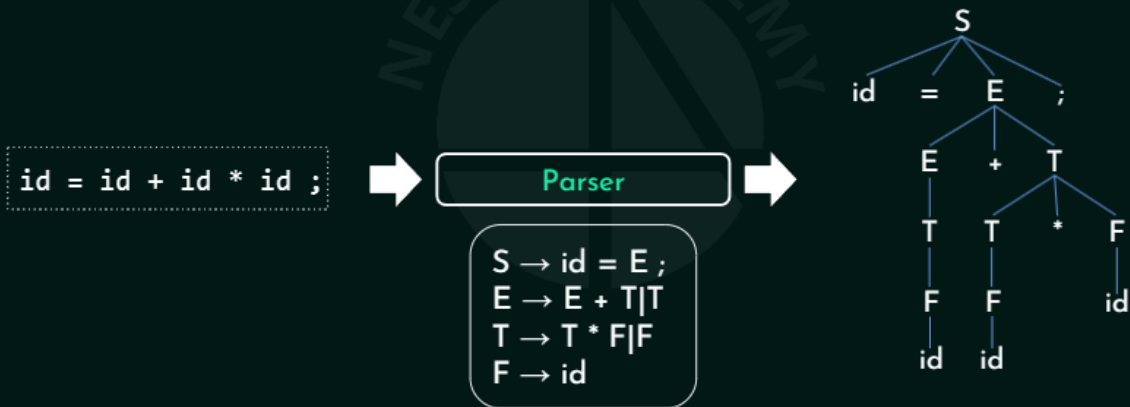
A parser is a program that generates a parse tree for the given string, if the string is generated from the underlying grammar.

```
x = a+b*c;
```

Parser: A parser is a program that generates a parse tree for the given string, if the string is generated from the underlying grammar. $x = a + b * c;$

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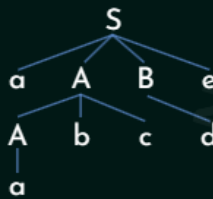
`id = id + id * id ;`Parser:A parser is a program that generates a parse tree for the given string, if the string is generated from the underlying grammar.ParserSid= E ; $E \rightarrow T \mid T + E$; $T \rightarrow F \mid F * T$; $F \rightarrow id$

Generation of Parse Tree:

$S \rightarrow aABe$, $A \rightarrow Abc \mid a$, $B \rightarrow d$

`aabcde`

Top down approach:



$S \Rightarrow aABe$
 $\Rightarrow aAbcBe$
 $\Rightarrow aabcBe$
 $\Rightarrow aabcde$

(Left most Derivation)

Decision:

Which production to use.

Bottom up approach:



$S \Rightarrow aABe$
 $\Rightarrow aAde$
 $\Rightarrow aAbcde$
 $\Rightarrow aabcde$

(Right most Derivation) - In reverse.

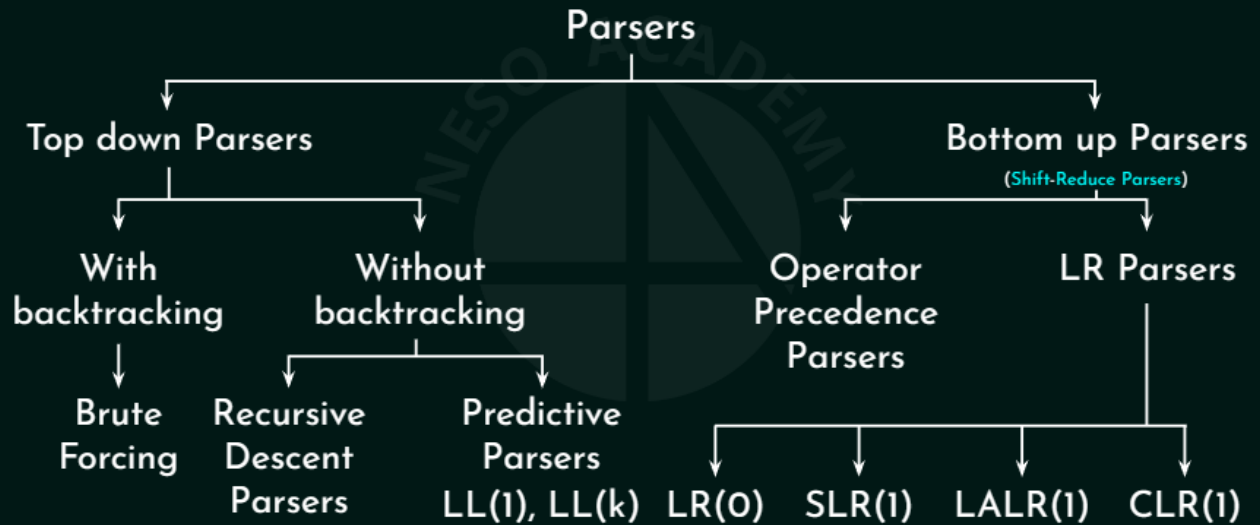
Decision:

When to reduce.

Generation of Parse Tree:Top down approach:Bottom up approach:`aabcde` $S \Rightarrow aABe \Rightarrow aAbcBe \Rightarrow aabcBe \Rightarrow aabcde$ $S \Rightarrow aABe \Rightarrow aAde \Rightarrow aAbcde \Rightarrow aabcde$ Decision:Which production to use.Decision: $S \Rightarrow aABe \Rightarrow aAde \Rightarrow aAbcde \Rightarrow aabcde$ When to reduce. $S \Rightarrow aABe \Rightarrow aAbcBe \Rightarrow aabcBe \Rightarrow aabcde$

aabcde(Left most Derivation)(Right most Derivation)- In reverse. $S \rightarrow aABe$, $A \rightarrow Abc \mid a$, $B \rightarrow d$

Classification of Parsers:



Classification of Parsers:ParsersTop down ParsersBottom up Parsers(Shift-Reduce Parsers)With backtrackingWithout backtrackingBrute ForcingLR ParsersOperator Precedence ParsersLR(0)CLR(1)LALR(1)SLR(1)Recursive Descent ParsersPredictive ParsersLL(1), LL(k)

Compiler Design

Top down Parsers – Recursive Descent Parsers

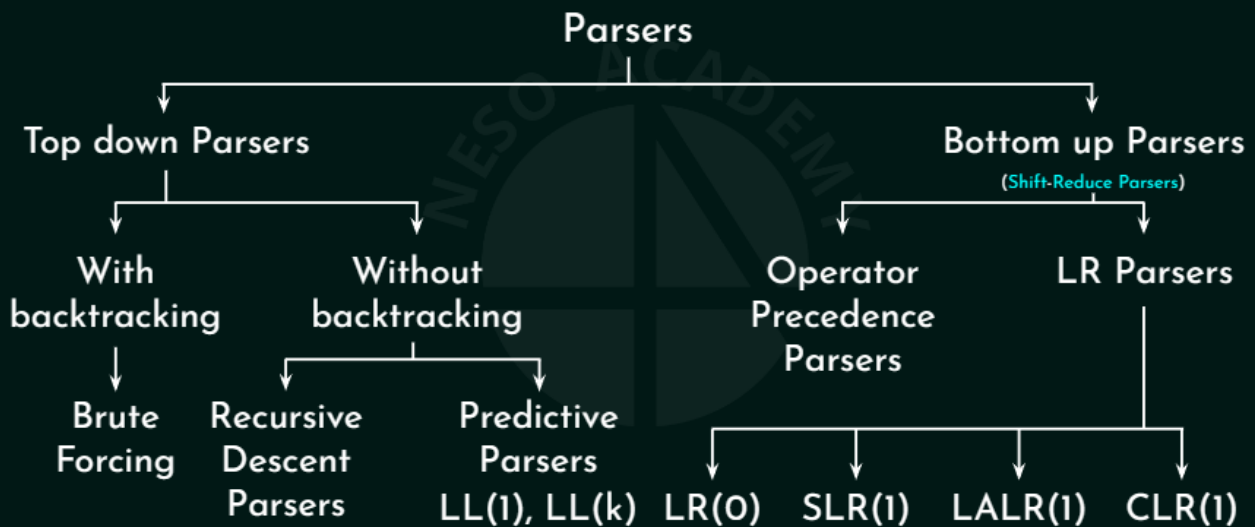


Outcome

- ☆ Top down Parsers.
- ☆ Example of Recursive Descent Parser.

Outcome☆Top down Parsers. ☆Example of Recursive Descent Parser.

Classification of Parsers:



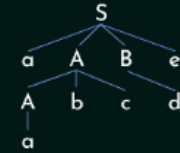
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Top down Parser:

In order to construct Top down parsers the Context Free Grammars should **not** have,

1. Left Recursion,
2. Non-determinism.

Top down approach:



$S \Rightarrow aABe$
 $\Rightarrow aAbcBe$
 $\Rightarrow aabcBe$
 $\Rightarrow aabcde$

(Left most Derivation)

Decision:

Which production
to use.

Top down Parser: In order to construct Top down parsers the Context Free Grammars should not have, 1. Left Recursion, 2. Non-determinism.

Recursive Descent Parser:

A recursive descent parser is a top-down parser built from a set of mutually recursive procedures (or a non-recursive equivalent) where each such procedure implements one of the non-terminals of the grammar. Thus the structure of the resulting program closely mirrors that of the grammar it recognizes.

Consider the following grammar having rules,

$$E \rightarrow iE'$$

$$E' \rightarrow +iE' \mid \varepsilon$$

A recursive descent parser is a top-down parser built from a set of mutually recursive procedures (or a non-recursive equivalent) where each such procedure implements one of the non-terminals of the grammar. Thus the structure of the resulting program closely mirrors

that of the grammar it recognizes. Recursive Descent Parser: Consider the following grammar having rules, $E \rightarrow iE'E' \rightarrow +iE' \mid \varepsilon$

Recursive Descent Parser:

$E \rightarrow iE'$
 $E' \rightarrow +iE' \mid \varepsilon$

```

1. E()
2. {
3.     if(look_ahead=='i')
4.     {
5.         match('i');
6.         E'();
7.     }
8. }

1. E'()
2. {
3.     if(look_ahead=='+')
4.     {
5.         match('+');
6.         match('i');
7.         E'();
8.     }
9.     else
10.    return;
11. }

1. match(char c)
2. {
3.     if(look_ahead==c)
4.         look_ahead = getchar();
5.     else
6.         printf("ERROR!");
7. }

1. main()
2. {
3.     E();
4.     if(look_ahead=='$')
5.         printf("Parsing Successful!");
6. }

```

Recursive Descent Parser: $E \rightarrow iE'E' \rightarrow +iE' \mid \varepsilon$

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7.         E'();
8.     }
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10.    return;
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```

Input: i + i \$

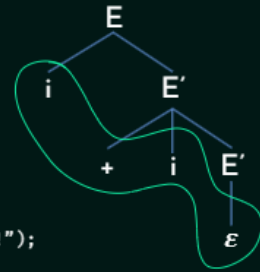
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$E \rightarrow iE'$
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Recursive Descent Parser: 1.E()2.{3.if(look_ahead=='i')4.{5.match('i');6.E'();7.}8.}1.E'()2.{3.if(look_ahead=='+')4.{5.match('+');6.match('i');7.E'();8.}9.else10.return;11.}1.match(char c)2.{3.if(look_ahead==c)4.look_ahead = getchar();5.else6.printf("ERROR!");7.}1.main()2.{3.E();4.if(look_ahead=='\$')5.printf("Parsing Successful!");6.} $E \rightarrow iE'$ $E' \rightarrow +iE' \mid \varepsilon$ Input: i + i \$ $EiE'+iiiiE'\varepsilon$



Compiler Design

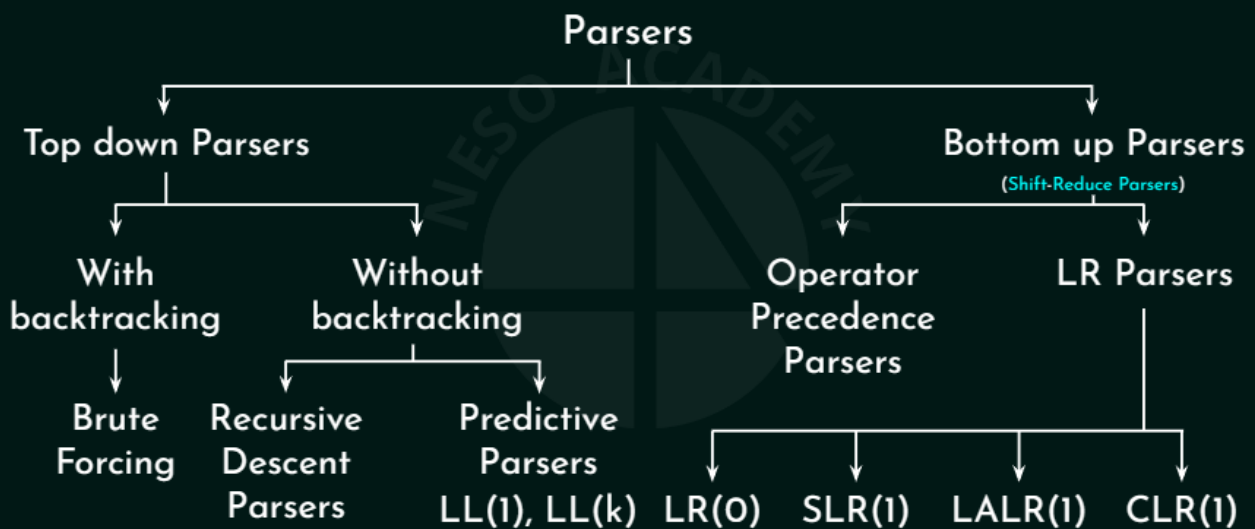
Top down Parsers – LL(1) Parsers

Outcome

- ☆ Organization of LL(1) Parser.
- ☆ Understanding the concepts of FIRST & FOLLOW.

Outcome ☆ Organization of LL(1) Parser. ☆ Understanding the concepts of FIRST & FOLLOW.

Classification of Parsers:



Classification of Parsers: Parsers
Top down Parsers
Bottom up Parsers (Shift-Reduce Parsers)
With backtracking
Without backtracking
Brute Forcing
LR Parsers
Operator Precedence Parsers
LR(0)
CLR(1)
LALR(1)
SLR(1)
Recursive Descent Parsers
Predictive Parsers
LL(1), LL(k)

Recursive Descent Parser:

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Input: i + i \$

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Recursive Descent Parser:

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Input: i + i \$

Recursive Descent Parser: $E \rightarrow iE'E' \rightarrow +iE' \mid \varepsilon$ Input: i + i \$

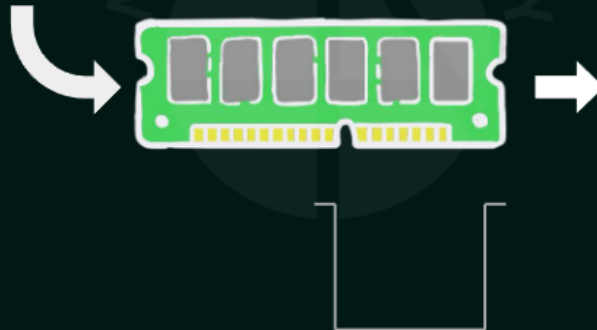
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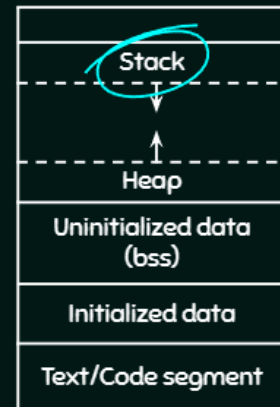
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Input: i + i \$

$E \rightarrow iE'$
 $E' \rightarrow +iE' \mid \varepsilon$



Recursive Descent Parser:
 $E \rightarrow iE'$
 $E' \rightarrow +iE' \mid \varepsilon$
 Input: i + i \$
 Stack
 Heap
 Uninitialized data (bss)
 Initialized data
 Text/Code segment

Recursive Descent Parser:

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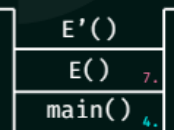
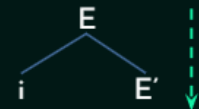
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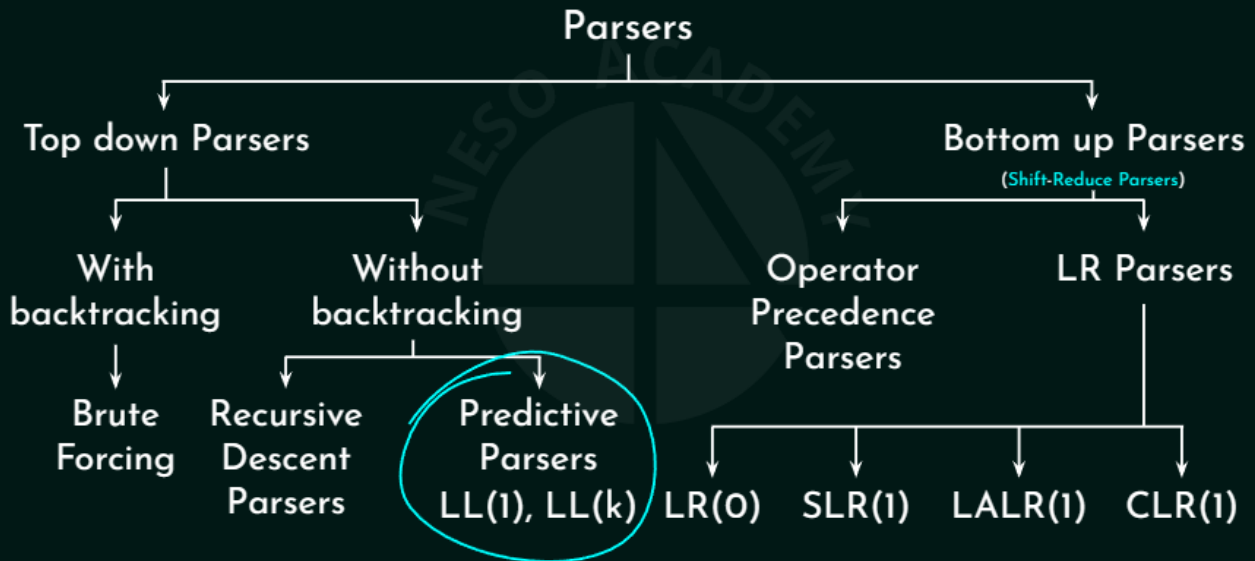
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Recursive Descent Parser:
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 8.}
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 4.if(look_ahead=='\$')
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 6.}

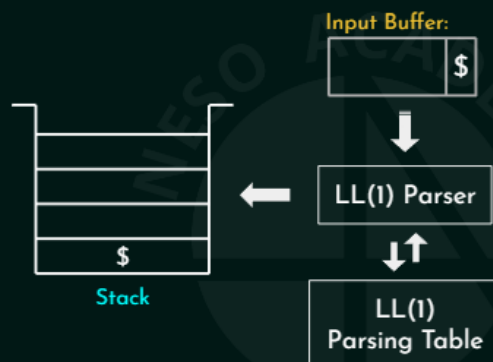
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\$EiE'main()E()4.7.E'()

Classification of Parsers:

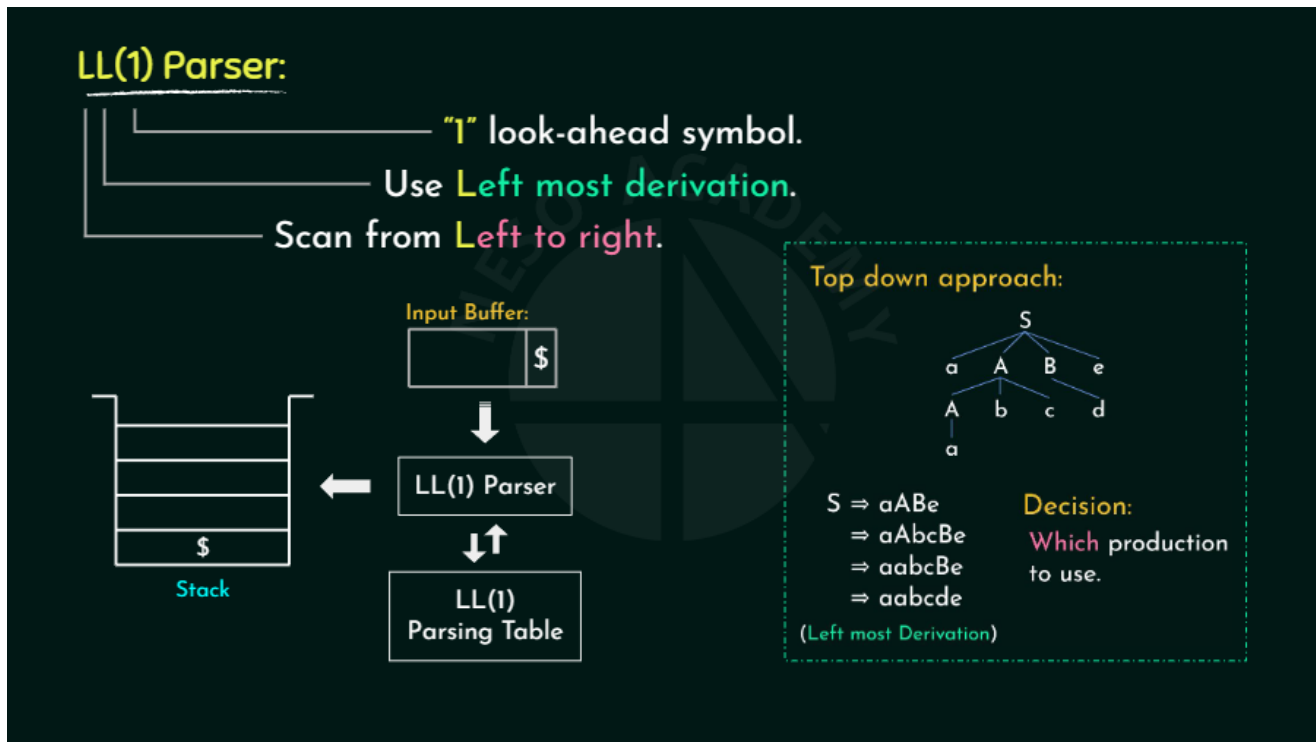


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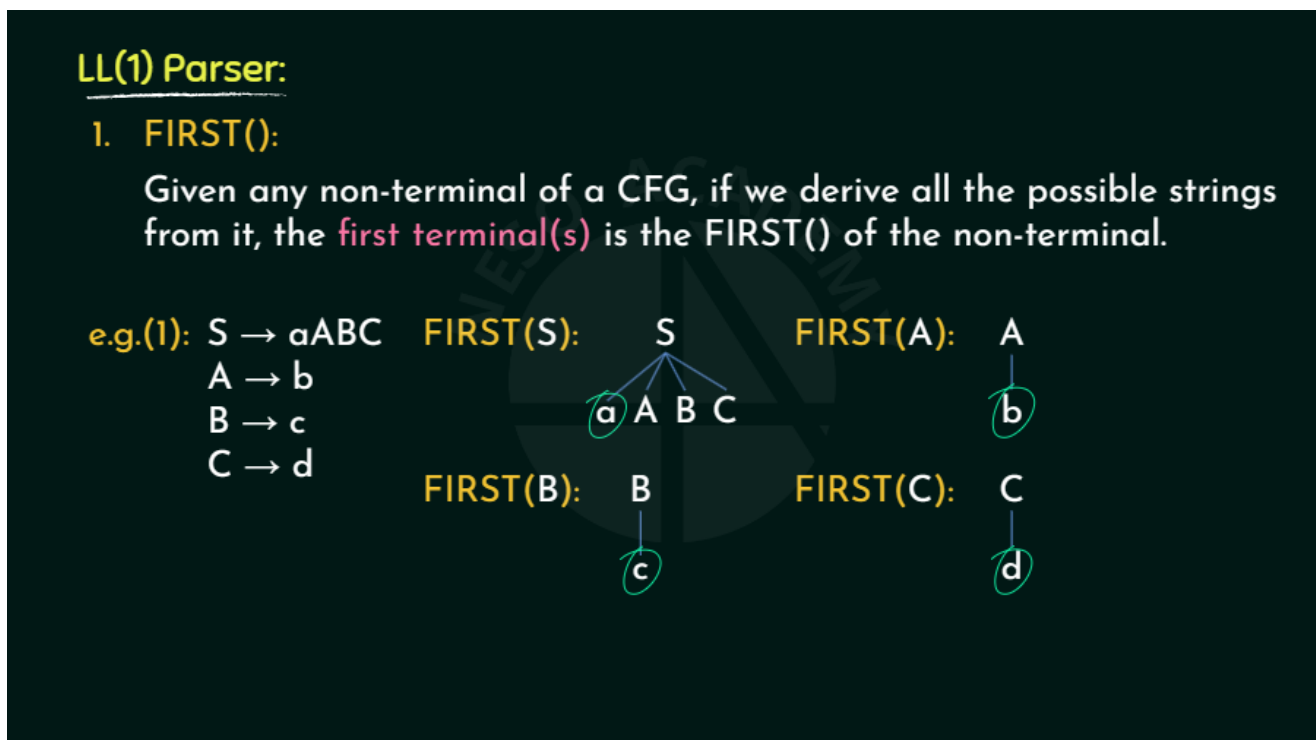
LL(1) Parser:



LL(1) Parser:\$LL(1) ParserLL(1) Parsing TableStack\$Input Buffer:



LL(1) Parser:\$LL(1) ParserLL(1) Parsing TableInput Buffer:StackScan from Left to right.Use Left most derivation."1" look-ahead symbol.



LL(1) Parser:1.FIRST():Given any non-terminal of a CFG, if we derive all the possible strings from it, the first terminal(s) is the FIRST() of the non-terminal. $S \rightarrow aABCA \rightarrow bB \rightarrow cC \rightarrow de$.g.(1):FIRST(S): SaABCFIRST(A): AbFIRST(B): BcFIRST(C): Cd

LL(1) Parser:

1. FIRST():

Given any non-terminal of a CFG, if we derive all the possible strings from it, the **first terminal(s)** is the FIRST() of the non-terminal.

e.g.(2): $S \rightarrow ABC$
 $A \rightarrow a \mid \epsilon$
 $B \rightarrow b$
 $C \rightarrow c$

FIRST(S): { a, b }



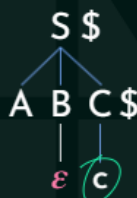
LL(1) Parser:1.FIRST():Given any non-terminal of a CFG, if we derive all the possible strings from it, the first terminal(s) is the FIRST() of the non-terminal. $S \rightarrow ABCA \rightarrow a \mid \epsilon B \rightarrow bC \rightarrow c$ e.g.(2):FIRST(S): $S\epsilon ABC\{ a, b \}b$

LL(1) Parser:

2. FOLLOW():

During the process of derivation, the **terminal(s) that could follow** the non-terminal are to be considered as FOLLOW() of the non-terminal.

e.g.: $S \rightarrow ABC$
 $A \rightarrow a$
 $B \rightarrow b \mid \epsilon$
 $C \rightarrow c$



FOLLOW(S): { \$ }

FOLLOW(A): { b, c }

FOLLOW(B): { c }

FOLLOW(C): { \$ }

cLL(1) Parser:2.FOLLOW():During the process of derivation, the terminal(s) that could follow the non-terminal are to be considered as FOLLOW() of the non-terminal. $S \rightarrow ABCA \rightarrow a B \rightarrow b \mid \epsilon C \rightarrow c$ e.g.:FOLLOW(S): $SABC\epsilon\{ \$ \}\$$ FOLLOW(A): { b, c }{ c }FOLLOW(B):

FOLLOW(C): { \$ }



Compiler DesignFirst & Follow

 **Outcome**

- ☆ Step by step derivation of FIRST and FOLLOW.

A faint 'NESO ACADEMY' watermark is visible in the background.

Outcome☆Step by step derivation of FIRST and FOLLOW.

Derivation of FIRST:

$E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \varepsilon$
T $\rightarrow FT'$
 $T' \rightarrow *FT' \mid \varepsilon$
 $F \rightarrow id \mid (E)$

$FIRST(F) = \{id, (\}$
 $FIRST(T') = \{+, \varepsilon\}$
 $FIRST(T) = \{id, (\}$

$$FIRST(T) = FIRST(F) = \{id, (\}$$

Derivation of FIRST: $E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid$

$(E)*FIRST(T)FIRST(F) = \{id, (\} = FIRST(F) = \{id, (\} FIRST(T) = \{id, (\} FIRST(T') = \{+, \varepsilon\}^*$

Derivation of FIRST:

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E $\rightarrow +TE' \mid \varepsilon$
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$$FIRST(E') = \{+, \varepsilon\}$$

Derivation of FIRST: $E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid$

$(E)*FIRST(E')FIRST(F) = \{id, (\} FIRST(T) = \{id, (\} FIRST(T') = \{+, \varepsilon\}^* = \{+, \varepsilon\} FIRST(E') = \{+, \varepsilon\}$

Derivation of FIRST:

$E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \varepsilon$
 $T \rightarrow FT'$
 $T' \rightarrow *FT' \mid \varepsilon$
 $F \rightarrow id \mid (E)$

$FIRST(F) = \{id, (\}$
 $FIRST(T') = \{*, \varepsilon\}$
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Derivation of FIRST: $E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid$

$(E)*FIRST(E)FIRST(F) = \{id, (\}FIRST(T) = \{id, (\}FIRST(T') = \{+, \varepsilon\}*FIRST(E') = \{+, \varepsilon\}=$
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	FIRST
$E \rightarrow TE'$	$\{id, (\}$
$E' \rightarrow +TE' \mid \varepsilon$	$\{+, \varepsilon\}$
$T \rightarrow FT'$	$\{id, (\}$
$T' \rightarrow *FT' \mid \varepsilon$	$\{*, \varepsilon\}$
$F \rightarrow id \mid (E)$	$\{id, (\}$

Derivation of FIRST: $E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid (E)*FIRST(F) = \{id, (\}FIRST(T) = \{id, (\}FIRST(T') = \{+, \varepsilon\}*FIRST(E') = \{+, \varepsilon\}FIRST(E) = \{id, (\}E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid (E)*\{id, (\}\{+, \varepsilon\}\{id, (\}\{+, \varepsilon\}\{id, (\}FIRST*$

Derivation of FOLLOW:

	FIRST	FOLLOW
$E \rightarrow TE'$	{id, (}	{\$,)}
$E' \rightarrow +TE' \mid \varepsilon$	{+, ε }	{\$,)}
$T \rightarrow FT'$	{id, (}	{+, \$,)}
$T' \rightarrow *FT' \mid \varepsilon$	{*, ε }	
$F \rightarrow id \mid (E)$	{id, (}	

$$FOLLOW(T) = FIRST(E') = \{ +, \varepsilon \}$$

1. The following terminal symbol will be selected as FOLLOW.
2. The FIRST of the following non-terminal will be selected as FOLLOW.
3. If it is the right most in the RHS, the FOLLOW of the LHS will be selected.

= { +, ε },) } Derivation of FOLLOW: $E \rightarrow TE' \rightarrow +TE' \mid \varepsilon T \rightarrow FT' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid (E) * FIRST FOLLOW \{ \$, \$,) \} \{ +, \$,) \}$ FOLLOW(T) = FIRST(E')

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{id, (} {+, ε } {id, (} {+, ε } {id, (} *

Derivation of FOLLOW:

	FIRST	FOLLOW
$E \rightarrow TE'$	{id, (}	{\$,)}
$E' \rightarrow +TE' \mid \varepsilon$	{+, ε }	{\$,)}
$T \rightarrow FT'$	{id, (}	{+, \$,)}
$T' \rightarrow *FT' \mid \varepsilon$	{*, ε }	{+, \$,)}
$F \rightarrow id \mid (E)$	{id, (}	{*, +, \$,)}

$$\begin{aligned}
 FOLLOW(F) &= FIRST(T') = \{ *, \varepsilon \} \\
 &= \{ * \} \cup FOLLOW(T) \cup FOLLOW(T') \\
 &= \{ *, +, \$,) \}
 \end{aligned}$$

Derivation of FOLLOW: $E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid (E)^*$
 $FOLLOW\{ \$,), \} = \{ +, \$,), \}$
 $FOLLOW(T) = \{ +, \$,), \}$
 $FOLLOW(T') = \{ +, \$,), \}$

Derivation of FIRST & FOLLOW:

	FIRST	FOLLOW
$E \rightarrow TE'$	$\{id, (\}$	$\{ \$,) \}$
$E' \rightarrow +TE' \mid \varepsilon$	$\{ +, \varepsilon \}$	$\{ \$,) \}$
$T \rightarrow FT'$	$\{id, (\}$	$\{ +, \$,) \}$
$T' \rightarrow *FT' \mid \varepsilon$	$\{ *, \varepsilon \}$	$\{ +, \$,) \}$
$F \rightarrow id \mid (E)$	$\{id, (\}$	$\{ *, +, \$,) \}$

Derivation of FIRST & FOLLOW: $E \rightarrow TE'E' \rightarrow +TE' \mid \varepsilon T \rightarrow FT'T' \rightarrow +FT' \mid \varepsilon F \rightarrow id \mid (E)^*$
 $FOLLOW\{ \$,), \} = \{ +, \$,), \}$
 $FOLLOW(T) = \{ +, \$,), \}$
 $FOLLOW(T') = \{ +, \$,), \}$

Compiler Design

First & Follow – Solved Problems (Set 1)

Outcome

- ☆ Three solved problems for determining First and Follow.

Outcome ☆ Three solved problems for determining First and Follow.

Q1: Consider the following grammar:

$P \rightarrow xQRS$

$Q \rightarrow yz \mid z$

$R \rightarrow w \mid \varepsilon$

$S \rightarrow y$

What is FOLLOW(Q)?

(A) {R}

(B) {w}

(C) {w, y}

(D) {w, ε }

GATE 2017

Q1: Consider the following grammar: $P \rightarrow xQRS$ $Q \rightarrow yz \mid z$ $R \rightarrow w \mid \varepsilon$ $S \rightarrow y$ What is FOLLOW(Q)? (A) {R} (B) {w} (C) {w, y} (D) {w, ε } GATE 2017

Q1: Consider the following grammar:

$P \rightarrow xQRS$

$Q \rightarrow yz \mid z$

$R \rightarrow w \mid \varepsilon$

$S \rightarrow y$

What is FOLLOW(Q)?

(A) {R}

(B) {w}

(C) {w, y}

(D) {w, ε }

FOLLOW(Q) = {w, y}

FIRST(R) = {w, ε }

FIRST(S) = {y}

Q1: Consider the following grammar: $P \rightarrow xQRS$ $Q \rightarrow yz \mid z$ $R \rightarrow w \mid \varepsilon$ $S \rightarrow y$
What is FOLLOW(Q)?
(A) {R} (B) {w} (C) {w, y} (D) {w, ε }
FOLLOW(Q) FIRST(R) = {w, ε } = {w, y} FIRST(S) = {y}

Q2: Find the FIRST and FOLLOW of all the non-terminals:

$S \rightarrow ABCDE$

$A \rightarrow a \mid \varepsilon$

$B \rightarrow b \mid \varepsilon$

$C \rightarrow c$

$D \rightarrow d \mid \varepsilon$

$E \rightarrow e \mid \varepsilon$

Q2: Find the FIRST and FOLLOW of all the non-terminals: $S \rightarrow ABCDE$ $A \rightarrow a \mid \varepsilon$ $B \rightarrow b \mid \varepsilon$ $C \rightarrow c$ $D \rightarrow d \mid \varepsilon$ $E \rightarrow e \mid \varepsilon$

Q2: Find the FIRST and FOLLOW of all the non-terminals:

	FIRST	FOLLOW
$S \rightarrow ABCDE$	$\{a, b, c\}$	$\{\$ \}$
$A \rightarrow a \mid \varepsilon$	$\{a, \varepsilon\}$	$\{b, c\}$
$B \rightarrow b \mid \varepsilon$	$\{b, \varepsilon\}$	$\{c\}$
$C \rightarrow c$	$\{c\}$	$\{d, e, \$ \}$
$D \rightarrow d \mid \varepsilon$	$\{d, \varepsilon\}$	$\{e, \$ \}$
$E \rightarrow e \mid \varepsilon$	$\{e, \varepsilon\}$	$\{\$ \}$

Find the FIRST and FOLLOW of all the non-terminals:
 $S \rightarrow ABCDE$
 $A \rightarrow a \mid \varepsilon$
 $B \rightarrow b \mid \varepsilon$
 $C \rightarrow c$
 $D \rightarrow d \mid \varepsilon$
 $E \rightarrow e \mid \varepsilon$
 FIRST FOLLOW, $\$$
 $\{a\}$
 $\{e, \varepsilon\}$
 $\{d, \varepsilon\}$
 $\{b, \varepsilon\}$
 $\{a, \varepsilon\}$
 $\{c\}$
 $\{b, c\}$
 $\{\$ \}$
 $\{b, c\}$
 $\{c\}$
 $\{d, e, \$ \}$
 $\{e, \$ \}$
 $\{e, \$ \}$

Q3: Find the FIRST and FOLLOW of all the non-terminals:

$S \rightarrow Bb \mid Cd$

$B \rightarrow aB \mid \varepsilon$

$C \rightarrow cC \mid \varepsilon$

Q3: Find the FIRST and FOLLOW of all the non-terminals:
 $S \rightarrow Bb \mid Cd$
 $B \rightarrow aB \mid \varepsilon$
 $C \rightarrow cC \mid \varepsilon$

Q3: Find the FIRST and FOLLOW of all the non-terminals:

	FIRST	FOLLOW
$S \rightarrow Bb \mid Cd$	$\{a, b, c, d\}$	$\{\$ \}$
$B \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{b\}$
$C \rightarrow cC \mid \epsilon$	$\{c, \epsilon\}$	$\{d\}$

Find the FIRST and FOLLOW of all the non-terminals:
 $S \rightarrow Bb \mid Cd$
 $B \rightarrow aB \mid \epsilon$
 $C \rightarrow cC \mid \epsilon$
 ϵ
 FIRST FOLLOW Q3: $\{c, \epsilon\}$ $\{a, \epsilon\}$ $\{a, b, c, d\}$ $\{\$ \}$ $\{d\}$ $\{b\}$



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First & Follow – Solved Problems (Set 2)

Compiler Design First & Follow - Solved Problems (Set 2)

Outcome

- ☆ Two solved problems for determining First and Follow.

Outcome ☆ Two solved problems for determining First and Follow.

Q1: Find the FIRST and FOLLOW of all the non-terminals:

$S \rightarrow aBDh$

$B \rightarrow cC$

$C \rightarrow bC \mid \epsilon$

$D \rightarrow EF$

$E \rightarrow g \mid \epsilon$

$F \rightarrow f \mid \epsilon$

Q1: Find the FIRST and FOLLOW of all the non-terminals: $S \rightarrow aBDh$ $B \rightarrow cC$ $C \rightarrow bC \mid \epsilon$ $D \rightarrow EF$ $E \rightarrow g \mid \epsilon$ $F \rightarrow f \mid \epsilon$

Q1: Find the FIRST and FOLLOW of all the non-terminals:

	FIRST	FOLLOW
$S \rightarrow aBDh$	$\{a\}$	$\{\$ \}$
$B \rightarrow cC$	$\{c\}$	$\{g, f, h\}$
$C \rightarrow bC \mid \varepsilon$	$\{b, \varepsilon\}$	$\{g, f, h\}$
$D \rightarrow EF$	$\{g, f, \varepsilon\}$	$\{h\}$
$E \rightarrow g \mid \varepsilon$	$\{g, \varepsilon\}$	$\{f, h\}$
$F \rightarrow f \mid \varepsilon$	$\{f, \varepsilon\}$	$\{h\}$

Find the FIRST and FOLLOW of all the non-terminals:
 $S \rightarrow aBDh$
 $B \rightarrow cC$
 $C \rightarrow bC \mid \varepsilon$
 $D \rightarrow EF$
 $E \rightarrow g \mid \varepsilon$
 $F \rightarrow f \mid \varepsilon$
 FIRST FOLLOW Q1: $\{f, \varepsilon\}$ $\{g, \varepsilon\}$ $\{b, \varepsilon\}$ $\{c\}$ $\{\$ \}$, h $\{f\{h\}$ $\{g, f, \varepsilon\}$ $\{a\}$ $\{g, h\}$, f $\{g, h\}$, f $\{h\}$

Q2: Find the FIRST and FOLLOW of all the non-terminals:

$S \rightarrow ACB \mid CbB \mid Ba$
 $A \rightarrow da \mid BC$
 $B \rightarrow g \mid \varepsilon$
 $C \rightarrow h \mid \varepsilon$

Q2: Find the FIRST and FOLLOW of all the non-terminals:
 $S \rightarrow ACB \mid CbB \mid Ba$
 $A \rightarrow da \mid BC$
 $B \rightarrow g \mid \varepsilon$
 $C \rightarrow h \mid \varepsilon$

Q2: Find the FIRST and FOLLOW of all the non-terminals:

	FIRST	FOLLOW
$S \rightarrow ACB \mid CbB \mid Ba$	$\{d, g, h, b, a, \epsilon\}$	$\{\$ \}$
$A \rightarrow da \mid BC$	$\{d, g, h, \epsilon\}$	$\{h, g, \$ \}$
$B \rightarrow g \mid \epsilon$	$\{g, \epsilon\}$	$\{\$, a, h, g\}$
$C \rightarrow h \mid \epsilon$	$\{h, \epsilon\}$	$\{g, \$, b, h\}$

FIRST FOLLOW Find the FIRST and FOLLOW of all the non-terminals:
 $S \rightarrow ACB \mid CbB \mid Ba$
 $A \rightarrow da \mid BC$
 $B \rightarrow g \mid \epsilon$
 $C \rightarrow h \mid \epsilon$
 Q2: $\{g, \epsilon\}$ $\{\$ \}$ $\{h, \epsilon\}$ $\{d, g, h, \epsilon\}$ $\{d, g, h, b, a, \epsilon\}$ $\{h, g, \$ \}$ $\{\$, a, h, g\}$ $\{g, \$, b, h\}$

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LL(1) Parsing Table

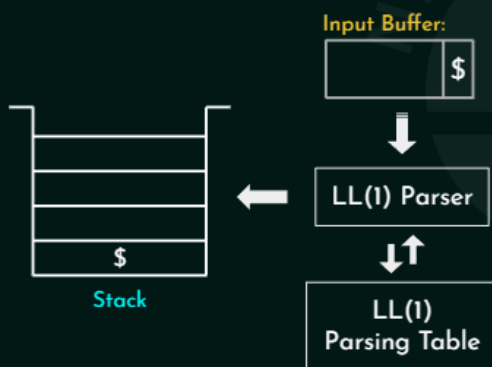
Outcome

- ☆ Construction of LL(1) Parsing table.

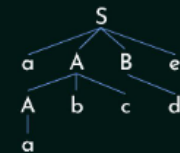
Outcome ☆ Construction of LL(1) Parsing table.

LL(1) Parser:

- “1” look-ahead symbol.
- Use Left most derivation.
- Scan from Left to right.



Top down approach:



$S \Rightarrow aABe$
 $\Rightarrow aAbcBe$
 $\Rightarrow aabcBe$
 $\Rightarrow aabcde$

(Left most Derivation)

Decision:
Which production to use.

LL(1) Parser: \$ \$ LL(1) Parser LL(1) Parsing Table Input Buffer: Stack Scan from Left to right. Use Left most derivation. “1” look-ahead symbol.

Construction of LL(1) Parsing table:

	FIRST	FOLLOW
$E \rightarrow TE'$	{id,(}	{\$,)}
$E' \rightarrow +TE' \mid \epsilon$	{+, ϵ }	{\$,)}
$T \rightarrow FT'$	{id,(}	{+,\$,)}
$T' \rightarrow *FT' \mid \epsilon$	{*, ϵ }	{+,\$,)}
$F \rightarrow id \mid (E)$	{id,(}	{*,+,\$,)}

Construction of LL(1) Parsing table:,))E → TE'E' → +TE' | εT → FT'T' → +FT' | εF → id |
 (E)*FIRSTFOLLOW{\$(\$,){+, \$,)}{+, \$,)}{+*, +\$,)}{id,}{+, ε}id,{+, ε}id,{*,

Construction of LL(1) Parsing table:

	id	()	*	+	\$
E	$E \rightarrow TE'$	$E \rightarrow TE'$				
E'			$E' \rightarrow \varepsilon$		$E' \rightarrow +TE'$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$	$T \rightarrow FT'$				
T'			$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$	$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow \text{id}$	$F \rightarrow (E)$				

Rules:

1. All the ϵ -productions are placed under FOLLOW sets.
2. Remaining productions are placed under the FIRSTs.

	FIRST	FOLLOW
$E \rightarrow TE'$	{id, (}	{\$,)}
$E' \rightarrow +TE' \mid \varepsilon$	{+, ε }	{\$,)}
$T \rightarrow FT'$	{id, (}	{+, \$,)}
$T' \rightarrow *FT' \mid \varepsilon$	{*, ε }	{+, \$,)}
$F \rightarrow id \mid (E)$	{id, (}	{+, *, \$,)}

Construction of LL(1) Parsing table: $EE'TT'FF \rightarrow idE \rightarrow TE'T \rightarrow FT'T' \rightarrow +FT'*E' \rightarrow \varepsilon T' \rightarrow \varepsilon E' \rightarrow +TE'T' \rightarrow \varepsilon E' \rightarrow \varepsilon T' \rightarrow \varepsilon E \rightarrow TE'T \rightarrow FT'F \rightarrow (E)id()*+ \$$ Rules: 1. All the ε -productions are placed under FOLLOW sets. 2. Remaining productions are placed under the FIRSTs.



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LL(1) Parsing

Compiler DesignLL(1) Parsing



Outcome



Illustration of LL(1) parsing procedure.

Outcome☆Illustration of LL(1) parsing procedure.

LL(1) Parsing:

$S \rightarrow aABb$
 $A \rightarrow c \mid \epsilon$
 $B \rightarrow d \mid \epsilon$

i/p Buffer:

a d b \$

LL(1) Parser

LL(1) Parsing Table

Stack

LL(1) Parsing: \$ LL(1) Parser LL(1) Parsing Table Stack $S \rightarrow aABb$ $A \rightarrow c \mid \epsilon$ $B \rightarrow d \mid \epsilon$ a d b \$ i/p Buffer: \$

LL(1) Parsing:

$S \rightarrow aABb$
 $A \rightarrow c \mid \epsilon$
 $B \rightarrow d \mid \epsilon$

FIRST FOLLOW

	FIRST	FOLLOW
$S \rightarrow aABb$	{a}	{ \$ }
$A \rightarrow c \mid \epsilon$	{c, ϵ }	{d, b}
$B \rightarrow d \mid \epsilon$	{d, ϵ }	{b}

i/p Buffer:

a d b \$

LL(1) Parser

LL(1) Parsing Table

Stack

	a	b	c	d	\$
S	$S \rightarrow aABb$				
A		$A \rightarrow \epsilon$	$A \rightarrow c$	$A \rightarrow \epsilon$	
B		$B \rightarrow \epsilon$		$B \rightarrow d$	

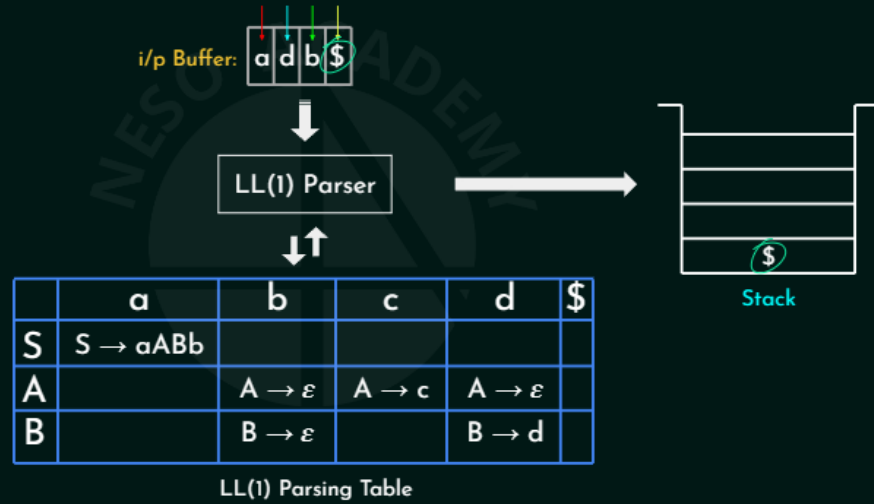
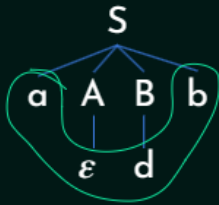
$S \rightarrow aABb$ $A \rightarrow \epsilon$ LL(1) Parsing: \$ LL(1) Parser LL(1) Parsing Table Stack $S \rightarrow aABb$ $A \rightarrow c \mid \epsilon$ $B \rightarrow d \mid \epsilon$ a d b \$ i/p Buffer: {d \$} $S \rightarrow aABb$ $A \rightarrow c \mid \epsilon$ $B \rightarrow d \mid \epsilon$ FIRST FOLLOW { \$ } {b} {a, ϵ } {c {d, ϵ }, b} a S A B A $\rightarrow \epsilon$ B $\rightarrow \epsilon$ b c d A $\rightarrow c$ B $\rightarrow d$

LL(1) Parsing:

$S \rightarrow aABb$

$A \rightarrow c \mid \epsilon$

$B \rightarrow d \mid \epsilon$



LL(1) Parsing: \$ LL(1) Parser LL(1) Parsing Table Stack
 $S \rightarrow aABb$
 $A \rightarrow c \mid \epsilon$
 $B \rightarrow d \mid \epsilon$
 a d b \$ i/p Buffer: a
 $S \rightarrow aABb$
 $A \rightarrow \epsilon$
 $B \rightarrow d$
 $SAB\$$
 $cA \rightarrow cb$
 $A \rightarrow \epsilon$
 $B \rightarrow \epsilon$
 $SaABb\epsilon d$

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LL(1) Parsing – Solved Problems (Set 1)



Outcome

- ☆ Five solved problems on whether the grammar is LL(1).

Outcome ☆ Five solved problems on whether the grammar is LL(1).

Q1: Find out whether the following grammar is LL(1):
 $S \rightarrow aSbS \mid bSaS \mid \epsilon$

Q1: Find out whether the following grammar is LL(1):

$$S \rightarrow aSbS \mid bSaS \mid \epsilon$$

Sol. FIRST(S): {a, b, ϵ }

FOLLOW(S): {\$, b, a}

Not LL(1) Grammar

	a	b	\$
S	$S \rightarrow aSbS$ $S \rightarrow \epsilon$	$S \rightarrow bSaS$ $S \rightarrow \epsilon$	$S \rightarrow \epsilon$

{\$, ϵ } Find out whether the following grammar is LL(1): $S \rightarrow aSbS \mid bSaS \mid \epsilon$

Q1: Sol. FIRST(S): {a, b} FOLLOW(S): {, b, a} $S \rightarrow aSbSS \rightarrow \epsilon$ $S \rightarrow bSaSS \rightarrow \epsilon$ $S \rightarrow \epsilon aSb Not LL(1) Grammar

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow (S) \mid \epsilon$$

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow (S) \mid \varepsilon$$

Sol. FIRST(S): {(, ε }

FOLLOW(S): {\$,)}

LL(1) Grammar

	()	\$
S	$S \rightarrow (S)$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$

FOLLOW(S): {\$, ε } Find out whether the following grammar is LL(1): $S \rightarrow (S) \mid \varepsilon$

Q2: Sol. FIRST(S): {(,)} $S \rightarrow (S) S \rightarrow \varepsilon S \rightarrow \varepsilon (S\$)$ LL(1) Grammar

Q3: Find out whether the following grammar is LL(1):

$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow \varepsilon$$

$$B \rightarrow \varepsilon$$

Q3: Find out whether the following grammar is LL(1):

$S \rightarrow AaAb \mid BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow AaAb \mid BbBa$	{a, b}	{\$}
$A \rightarrow \epsilon$	{ε}	{a, b}
$B \rightarrow \epsilon$	{ε}	{b, a}

	a	b	\$
S	$S \rightarrow AaAb$	$S \rightarrow BbBa$	
A	$A \rightarrow \epsilon$	$A \rightarrow \epsilon$	
B	$B \rightarrow \epsilon$	$B \rightarrow \epsilon$	

{aFind out whether the following grammar is LL(1): $S \rightarrow AaAb \mid BbBa$ $A \rightarrow \epsilon$ $B \rightarrow \epsilon$ Q3:Sol. $S \rightarrow AaAb \mid BbBa$ $A \rightarrow \epsilon$ $B \rightarrow \epsilon$ FIRSTFOLLOW{\$}{ε}{ε}, b){a, b){b, a}LL(1) Grammar $S \rightarrow AaAb$ $S \rightarrow BbBa$ a\$bSABA $\rightarrow \epsilon$ $B \rightarrow \epsilon$ $A \rightarrow \epsilon$ $B \rightarrow \epsilon$

Q4: Find out whether the following grammar is LL(1):

$S \rightarrow A \mid a$

$A \rightarrow a$

Q4: Find out whether the following grammar is LL(1):

$$\begin{aligned} S &\rightarrow A \mid a \\ A &\rightarrow a \end{aligned}$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow A \mid a$	{a}	{}
$A \rightarrow a$	{a}	{}

$S \rightarrow A \mid a$
 $A \rightarrow a$
 FIRST FOLLOW {a} {}
 Find out whether the following grammar is LL(1):
 $S \rightarrow A \mid a$
 $A \rightarrow a$
 Q4: Sol. {} {} Not LL(1) Grammar {}

Q5: Find out whether the following grammar is LL(1):

$$\begin{aligned} S &\rightarrow aB \mid \epsilon \\ B &\rightarrow bC \mid \epsilon \\ C &\rightarrow cS \mid \epsilon \end{aligned}$$

Q5: Find out whether the following grammar is LL(1):

$S \rightarrow aB \mid \epsilon$

$B \rightarrow bC \mid \epsilon$

$C \rightarrow cS \mid \epsilon$

LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{\$, \epsilon\}$
$B \rightarrow bC \mid \epsilon$	$\{b, \epsilon\}$	$\{\$, \epsilon\}$
$C \rightarrow cS \mid \epsilon$	$\{c, \epsilon\}$	$\{\$, \epsilon\}$

	a	b	c	\$
S	$S \rightarrow aB$			$S \rightarrow \epsilon$
B		$B \rightarrow bC$		$B \rightarrow \epsilon$
C			$C \rightarrow cS$	$C \rightarrow \epsilon$

$S \rightarrow aB \mid \epsilon$
 $B \rightarrow bC \mid \epsilon$
 $C \rightarrow cS \mid \epsilon$
 FIRST FOLLOW
 {a, ϵ } {b, ϵ } {c, ϵ }
 { ϵ } { ϵ } { ϵ }
 { ϵ } { ϵ } { ϵ }
 $S \rightarrow aB$
 $B \rightarrow bC$
 $C \rightarrow cS$
 $S \rightarrow \epsilon$
 $B \rightarrow \epsilon$
 $C \rightarrow \epsilon$

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LL(1) Parsing – Solved Problems (Set 2)

Outcome

- ☆ Four solved problems on whether the grammar is LL(1).

Outcome ☆ Four solved problems on whether the grammar is LL(1).

Q1: Find out whether the following grammar is LL(1):

$S \rightarrow AB$

$A \rightarrow a \mid \epsilon$

$B \rightarrow b \mid \epsilon$

Q1: Find out whether the following grammar is LL(1):

$$S \rightarrow AB$$
$$A \rightarrow a \mid \varepsilon$$
$$B \rightarrow b \mid \varepsilon$$

LL(1) Grammar

	FIRST	FOLLOW
Sol. $S \rightarrow AB$	$\{a, b, \epsilon\}$	$\{\$ \}$
$A \rightarrow a \mid \epsilon$	$\{a, \epsilon\}$	$\{b, \$ \}$
$B \rightarrow b \mid \epsilon$	$\{b, \epsilon\}$	$\{\$ \}$

	a	b	\$
S	$S \rightarrow AB$	$S \rightarrow AB$	$S \rightarrow AB$
A	$A \rightarrow a$	$A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$
B		$B \rightarrow b$	$B \rightarrow \varepsilon$

Find out whether the following grammar is LL(1):

$$S \rightarrow AB \quad A \rightarrow a \mid \varepsilon \quad B \rightarrow b \mid \varepsilon$$

Q1: Sol. $\{ \$ \} \{ a, \varepsilon \} \{ b, \varepsilon \} \{ \$ \}$

$$S \rightarrow ABS \rightarrow ABa\$B\$ABA \rightarrow \varepsilon \quad A \rightarrow a \quad B \rightarrow b \quad A \rightarrow \varepsilon \quad B \rightarrow \varepsilon$$

LL(1) Grammar

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow aSA \mid \varepsilon$$
$$A \rightarrow c \mid \varepsilon$$

Q2: Find out whether the following grammar is LL(1):

$$S \rightarrow aSA \mid \varepsilon$$

$$A \rightarrow c \mid \varepsilon$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aSA \mid \varepsilon$	$\{a, \varepsilon\}$	$\{\$, c\}$
$A \rightarrow c \mid \varepsilon$	$\{c, \varepsilon\}$	$\{\$, c\}$

	a	c	\$
S	$S \rightarrow aSA$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$
A		$A \rightarrow c$ $A \rightarrow \varepsilon$	$A \rightarrow \varepsilon$

$S \rightarrow aSA \mid \varepsilon$
 $A \rightarrow c \mid \varepsilon$
 FIRST FOLLOW
 Find out whether the following grammar is LL(1):
 $S \rightarrow aSA \mid \varepsilon$
 $A \rightarrow c \mid \varepsilon$
 Q2: Sol. $\{\$, c\}$ $\{a, \varepsilon\}$ $\{c, \varepsilon\}$
 $S \rightarrow aSA$ $S \rightarrow \varepsilon$ $a\$cS$ $AA \rightarrow \varepsilon$ $A \rightarrow c$ $A \rightarrow \varepsilon$ Not LL(1) Grammar
 $\{\$, c\}$ $S \rightarrow \varepsilon$

Q3: Find out whether the following grammar is LL(1):

$$S \rightarrow A$$

$$A \rightarrow Bb \mid Cd$$

$$B \rightarrow aB \mid \varepsilon$$

$$C \rightarrow cC \mid \varepsilon$$

Q3: Find out whether the following grammar is LL(1):

$S \rightarrow A$
 $A \rightarrow Bb \mid Cd$
 $B \rightarrow aB \mid \epsilon$
 $C \rightarrow cC \mid \epsilon$

	FIRST	FOLLOW
Sol. $S \rightarrow A$	{a, b, c, d}	{ ϵ }
$A \rightarrow Bb \mid Cd$	{a, b, c, d}	{ ϵ }
$B \rightarrow aB \mid \epsilon$	{a, ϵ }	{b}
$C \rightarrow cC \mid \epsilon$	{c, ϵ }	{d}

Find out whether the following grammar is LL(1):
 $S \rightarrow AA \rightarrow Bb \mid Cd$
 $B \rightarrow aB \mid \epsilon$
 $C \rightarrow cC \mid \epsilon$
 Sol. FOLLOW { ϵ } FIRST {a, b, c, d} FOLLOW {a, ϵ } FIRST {c, ϵ } FOLLOW {a, b, c, d} FIRST { ϵ }

Q3: Find out whether the following grammar is LL(1):

	FIRST	FOLLOW
Sol. $S \rightarrow A$	{a, b, c, d}	{ ϵ }
$A \rightarrow Bb \mid Cd$	{a, b, c, d}	{ ϵ }
$B \rightarrow aB \mid \epsilon$	{a, ϵ }	{b}
$C \rightarrow cC \mid \epsilon$	{c, ϵ }	{d}

	a	b	c	d	\$
S	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	
A	$A \rightarrow Bb$	$A \rightarrow Bb$	$A \rightarrow Cd$	$A \rightarrow Cd$	
B	$B \rightarrow aB$	$B \rightarrow \epsilon$			
			$C \rightarrow cC$	$C \rightarrow \epsilon$	

Find out whether the following grammar is LL(1):
 Q3: Sol. $S \rightarrow AA \rightarrow Bb \mid Cd$
 $B \rightarrow aB \mid \epsilon$
 $C \rightarrow cC \mid \epsilon$
 FOLLOW { ϵ } FIRST {a, b, c, d} FOLLOW {a, ϵ } FIRST {c, ϵ } FOLLOW {a, b, c, d} FIRST { ϵ }

Q3: Find out whether the following grammar is LL(1):

$S \rightarrow A$

$A \rightarrow Bb \mid Cd$

$B \rightarrow aB \mid \epsilon$

$C \rightarrow cC \mid \epsilon$

LL(1) Grammar

Sol.

	a	b	c	d	\$
S	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	$S \rightarrow A$	
A	$A \rightarrow Bb$	$A \rightarrow Bb$	$A \rightarrow Cd$	$A \rightarrow Cd$	
B	$B \rightarrow aB$	$B \rightarrow \epsilon$			
C			$C \rightarrow cC$	$C \rightarrow \epsilon$	

Find out whether the following grammar is LL(1): $S \rightarrow AA \rightarrow Bb \mid Cd$ $B \rightarrow aB \mid \epsilon$ $C \rightarrow cC \mid \epsilon$

Q3: Sol. $S \rightarrow AS \rightarrow AS \rightarrow AS \rightarrow AA \rightarrow BbA \rightarrow BbA \rightarrow CdA \rightarrow CdB \rightarrow aB$ $B \rightarrow \epsilon$ $C \rightarrow cCC \rightarrow \epsilon$ $S A B C a b c d \$$ LL(1) Grammar

Q4: Find out whether the following grammar is LL(1):

$S \rightarrow aAa \mid \epsilon$

$A \rightarrow abS \mid \epsilon$

Q4: Find out whether the following grammar is LL(1):

$$S \rightarrow aAa \mid \varepsilon$$

$$A \rightarrow abS \mid \varepsilon$$

Not LL(1) Grammar

Sol.

	FIRST	FOLLOW
$S \rightarrow aAa \mid \varepsilon$	$\{a, \varepsilon\}$	$\{\$, a\}$
$A \rightarrow abS \mid \varepsilon$	$\{a, \varepsilon\}$	$\{a\}$

Find out whether the following grammar is LL(1):
 $S \rightarrow aAa \mid \varepsilon$
 $A \rightarrow abS \mid \varepsilon$
 Q4: Sol. $S \rightarrow aAa \mid \varepsilon$
 $A \rightarrow abS \mid \varepsilon$
 FIRST FOLLOW
 $\{a\}$ $\{a, \varepsilon\}$ $\{a, \varepsilon\}$
 Not LL(1) Grammar $\{\$, a\}$

Home-work Problem:

Find out whether the following grammar is LL(1):

$$S \rightarrow iEtSS' \mid a$$

$$S' \rightarrow eS \mid \varepsilon$$

$$E \rightarrow b$$

Find out whether the following grammar is LL(1):
 $S \rightarrow iEtSS' \mid a$
 $S' \rightarrow eS \mid \varepsilon$
 $E \rightarrow b$
 Home-work Problem: