

Syntax Analysis | Neso Academy

 nesoacademy.org/cs/12-compiler-design/ppts/02-syntaxanalysis



Syntax Analysis Neso Academy CHAPTER-2



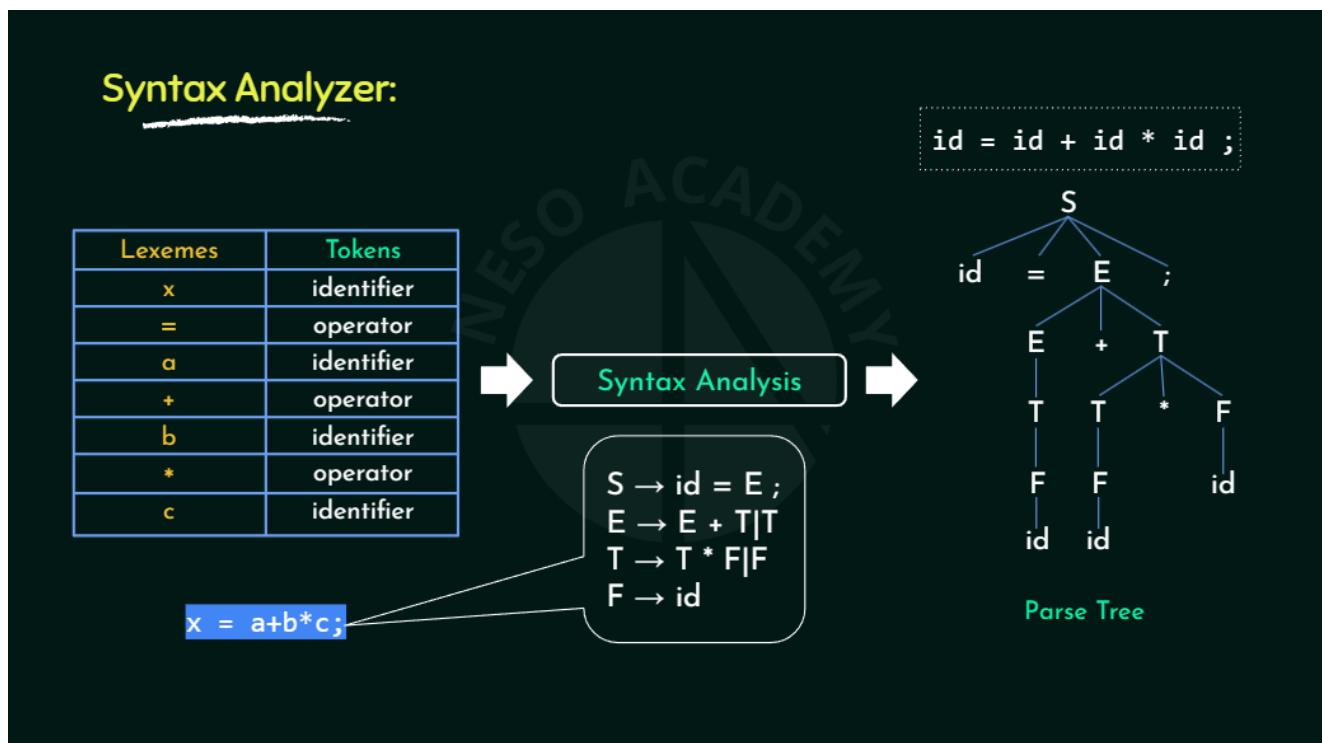
Compiler Design Introduction to Formal Grammars



Outcome

- ☆ Understanding of Formal Grammars

Outcome☆Understanding of Formal Grammars



Syntax Analysis Syntax

Analyzer: Lexemes Tokens identifier=operator identifier+operator identifier*operator identifier
 $x = a+b*c;$; $S \rightarrow id = E ;$ $E \rightarrow E + T | T$ $T \rightarrow T * F | F$ $F \rightarrow id$
Parse Tree $id = id + id * id ;$

$$\begin{aligned} S &\rightarrow id = E ; \\ E &\rightarrow E + T | T \\ T &\rightarrow T * F | F \\ F &\rightarrow id \end{aligned}$$

Context Free Grammar
(CFG)

$S \rightarrow id = E ; E \rightarrow E + T | T T \rightarrow T * F | F F \rightarrow id$ Context Free Grammar(CFG)

Grammar:

Learners are awesome.
Neso is good

Grammar:Learners are awesome.Nesoisgood

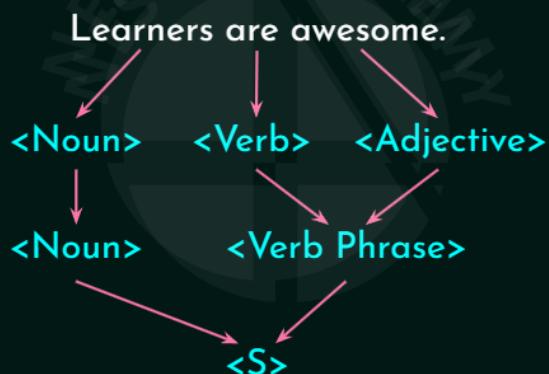
Grammar:

Learners are awesome.

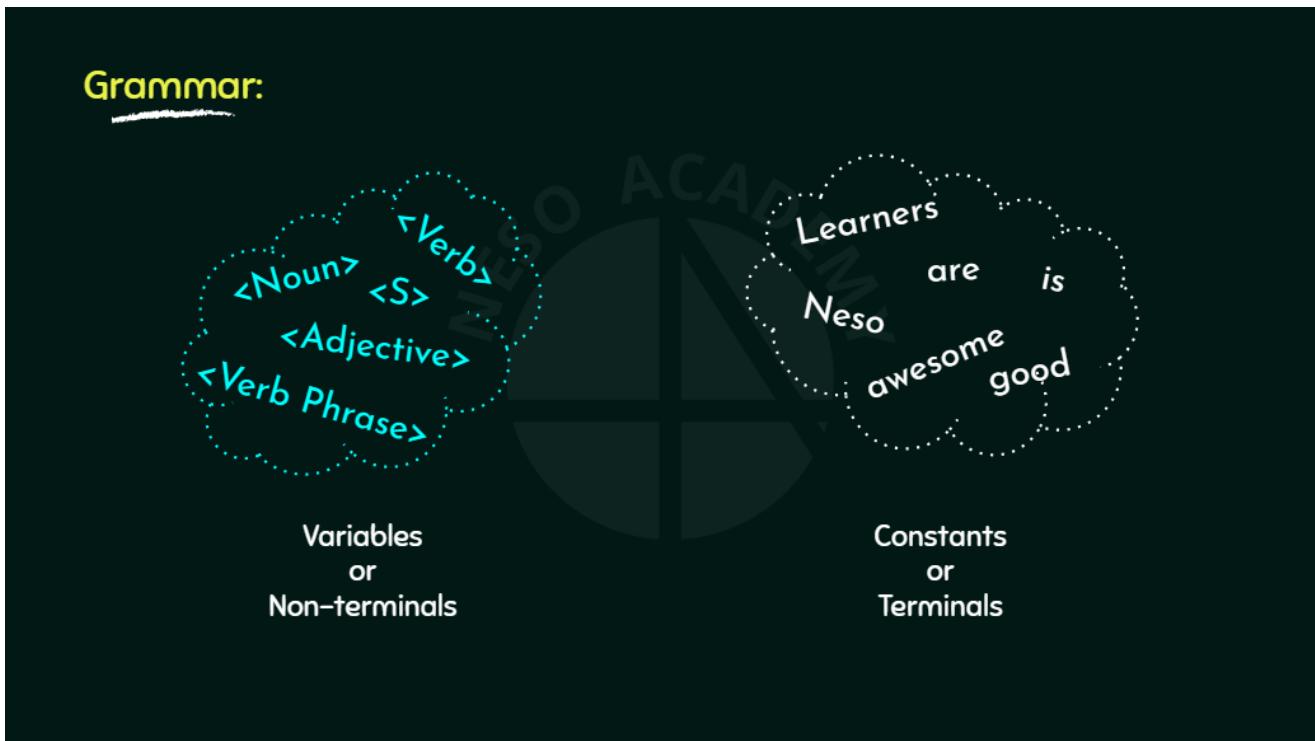
Neso is good.

Learners are awesome.Grammar:Neso is good.

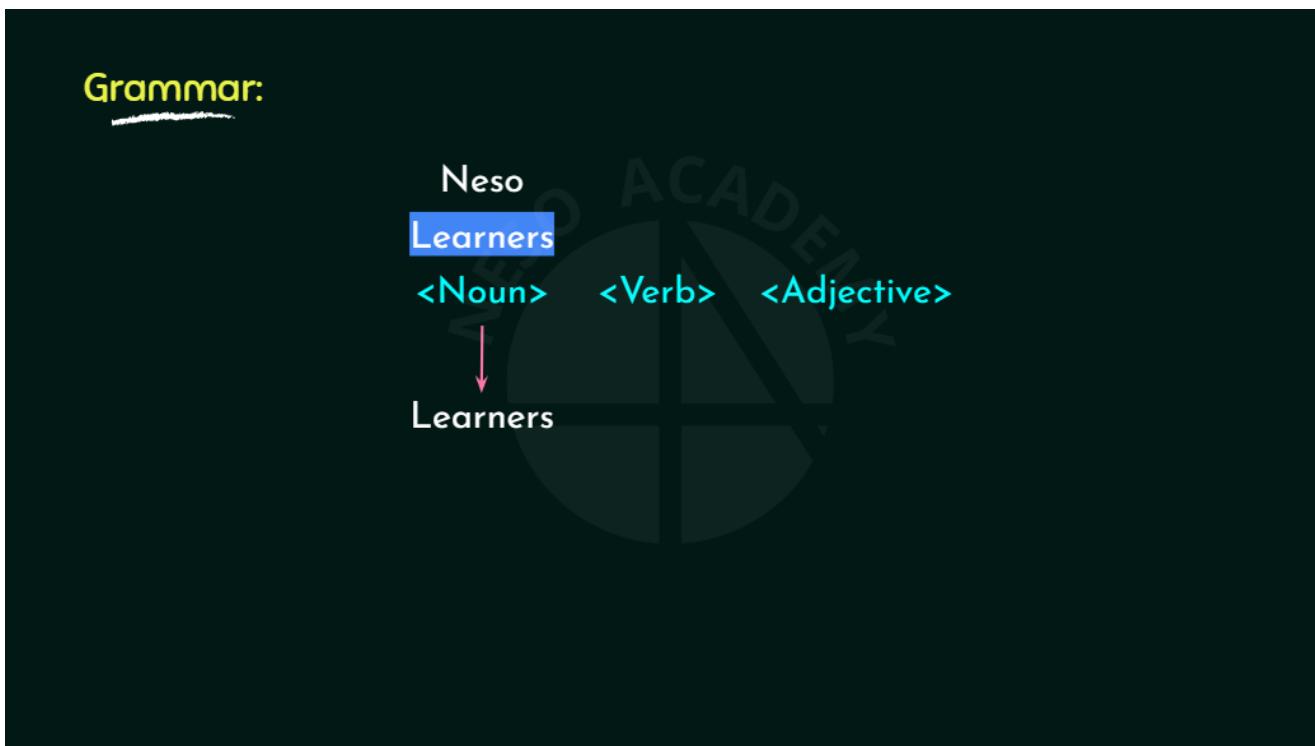
Grammar:



Learners are awesome.Grammar:<Noun><Verb><Adjective><Verb Phrase><Noun><S>

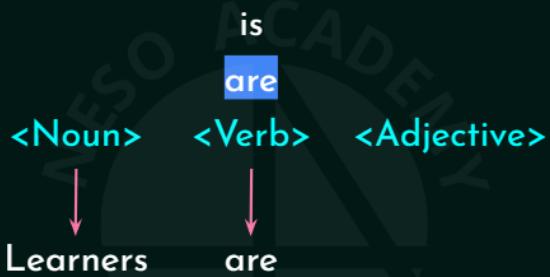


Grammar:NesoisgoodLearnersareawesomeVariablesor Non-terminalsConstantsor
Terminals<Noun><Verb><Adjective><Verb Phrase><S>



<Noun><Verb><Adjective>Grammar:NesoLearnersLearners

Grammar:



<Noun><Verb><Adjective>Grammar:Learnersisareare

Grammar:



<Noun><Verb><Adjective>Grammar:Learnersaregoodawesomeawesome

Grammar:



<Noun><Verb><Adjective>Grammar:LearnersareawesomeVariablesor Non- terminalsConstantsor Terminals

Grammar:



Grammar:NesoisgoodLearnersareawesomeVariablesor Non-terminalsConstantsor Terminals<Noun><Verb><Adjective><Verb Phrase><S>

Grammar:

(N, T, P, S)

$\langle S \rangle \rightarrow \langle \text{Noun} \rangle \langle \text{Verb Phrase} \rangle$
 $\langle \text{Verb Phrase} \rangle \rightarrow \langle \text{Verb} \rangle \langle \text{Adjective} \rangle$
 $\langle \text{Noun} \rangle \rightarrow \text{Learners} \mid \text{Neso}$
 $\langle \text{Verb} \rangle \rightarrow \text{are} \mid \text{is}$
 $\langle \text{Adjective} \rangle \rightarrow \text{awesome} \mid \text{good}$



Grammar:NesoisgoodLearnersareawesomeTerminalsNon-terminals<Noun><Verb>
 <Adjective><Verb Phrase><S><S><Noun><Verb Phrase><Verb><Adjective><Verb Phrase>
 <Noun>Learners|<Verb>are|is<Adjective>awesome|good(N, T, P, S)Neso

Grammar:

A **phrase structure grammar** (or simply **grammar**) is (N, T, P, S) where

- i. N is a finite, non-empty set of Non-terminals.
- ii. T is a finite, non-empty set of Terminals.
- iii. $N \cap T = \emptyset$
- iv. S is a special non-terminal (i.e. $S \in N$), called Start symbol.
- v. P is a finite set whose elements are of the form, $\alpha \rightarrow \beta$

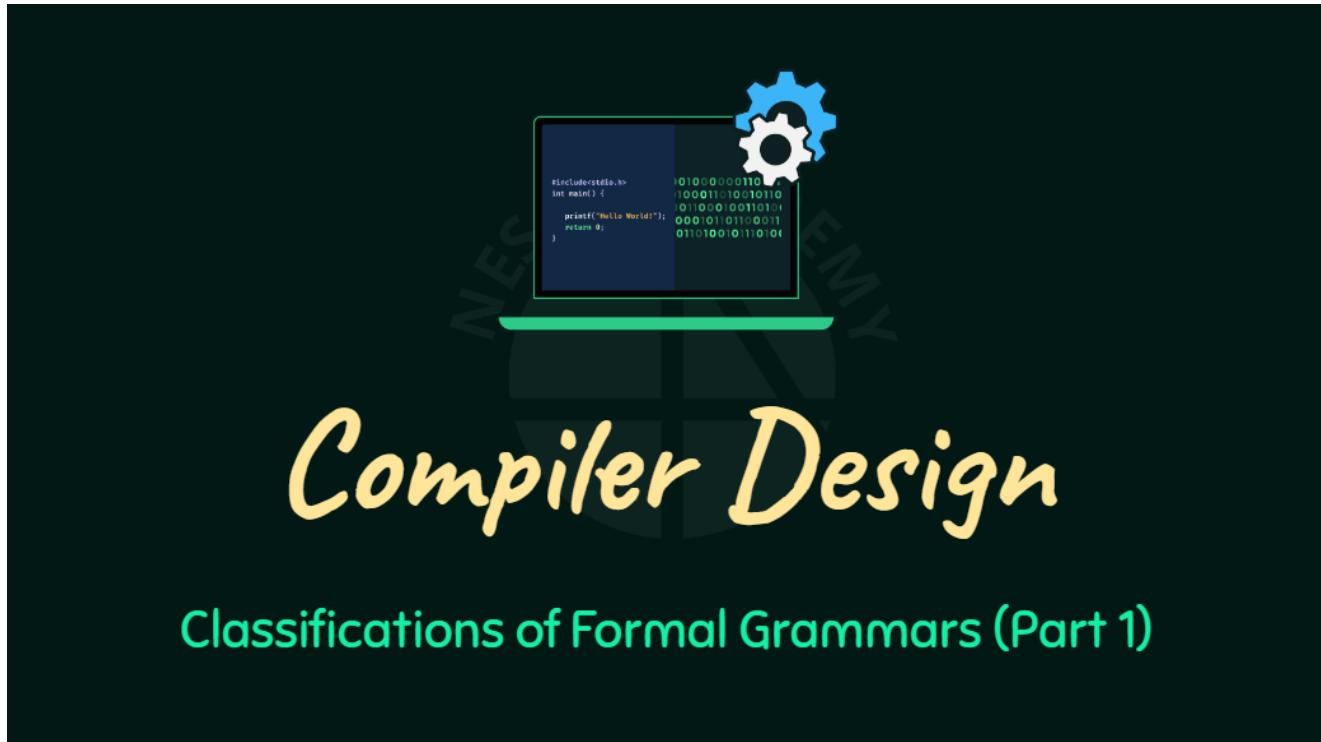


NUT

Production Rules

Grammar:A phrase structure grammar (or simply grammar)is (N, T, P, S) i. N is a finite, non-empty set of Non-terminals. ii. T is a finite, non-empty set of Terminals. iii. $N \cap T = \emptyset$ iv. S is a special non-terminal (i.e. $S \in N$), called Start symbol. v. P is a finite set whose elements are of

the form, $\alpha \rightarrow \beta$ NUT Production Rules where

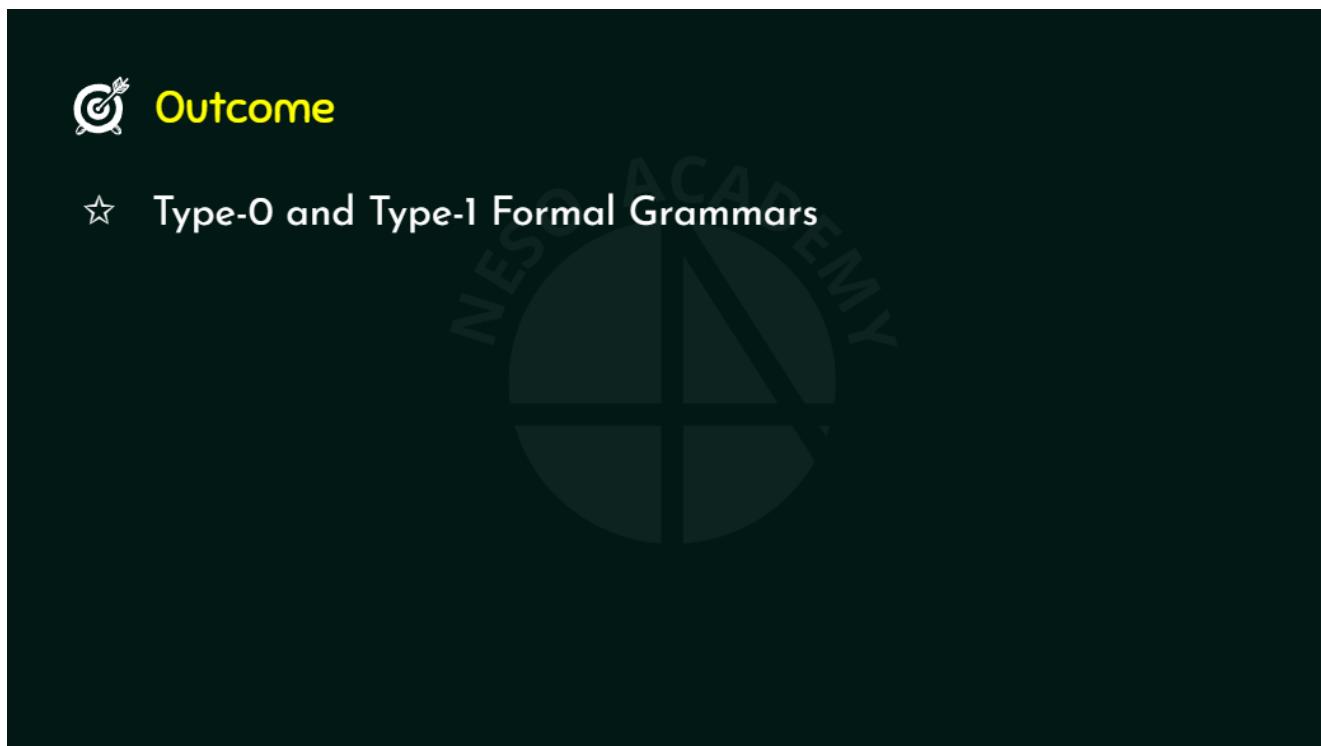


A slide titled "Compiler Design" featuring a central gear icon above a code editor window showing C code for "Hello World". Below the title is the subtitle "Classifications of Formal Grammars (Part 1)".

Compiler Design

Classifications of Formal Grammars (Part 1)

Compiler Design Classifications of Formal Grammars (Part 1)



A slide titled "Outcome" with the subtitle "Type-0 and Type-1 Formal Grammars".

Outcome

- ☆ Type-0 and Type-1 Formal Grammars

Outcome ☆ Type-0 and Type-1 Formal Grammars

Grammar:

A **phrase structure grammar** (or simply **grammar**) is (N, T, P, S) where

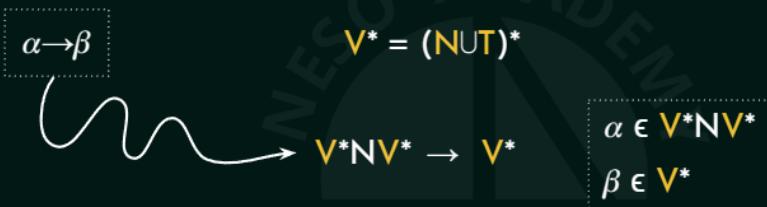
- i. N is a finite, non-empty set of **Non-terminals**.
- ii. T is a finite, non-empty set of **Terminals**.
- iii. $N \cap T = \emptyset$
- iv. S is a special non-terminal (i.e. $S \in N$), called **Start symbol**.
- v. P is a finite set **Production Rules** of the form,

$$\alpha \rightarrow \beta$$

Grammar: A phrase structure grammar (or simply grammar) is (N, T, P, S) where
i. N is a finite, non-empty set of Non-terminals.
ii. T is a finite, non-empty set of Terminals.
iii. $N \cap T = \emptyset$
iv. S is a special non-terminal (i.e. $S \in N$), called Start symbol.
v. P is a finite set Production Rules of the form, $\alpha \rightarrow \beta$

Grammar:

1. Type-0 / Unrestricted Grammar:



G:

$$P: abABcde \rightarrow abXcde \quad AB \Rightarrow X$$

$(NUT)^*$ Grammar: 1. Type-0 / Unrestricted Grammar: $\alpha \rightarrow \beta$ $NUTV^* = V^*NV^* \rightarrow V^*$ $\alpha \in V^*NV^*$ $\beta \in V^*$
 $V^*G:P:abABcde \rightarrow abXcde$ $AB \Rightarrow X$

Grammar:

2. Type-1:

$$\alpha A\beta \rightarrow \alpha\gamma\beta$$

$$|\alpha A\beta| \leq |\alpha\gamma\beta|$$

$$\begin{array}{l} A \in N \\ \alpha, \beta, \gamma \in V^* \end{array}$$

$$\text{Type-0: } V^* N V^* \rightarrow V^*$$

G:

$$P: abABcde \rightarrow abXcde$$

$$\begin{array}{c} V^* N V^* \rightarrow V^* \\ \downarrow \quad \downarrow \quad \downarrow \\ \alpha A \beta \rightarrow \alpha \gamma \beta \end{array}$$

Grammar: 2. Type-1: $V^* N V^* \rightarrow V^*$ G: P: abABcde \rightarrow abXcde
 Type-0: $\alpha, \beta, \gamma \in V^* A \in N$
 $\alpha A \beta \rightarrow \alpha \gamma \beta | \alpha A \beta | \alpha \gamma \beta | \dots$ K: $V^* N V^* \rightarrow V^*$ $\alpha A \beta \rightarrow \alpha \gamma \beta$

Grammar:

2. Type-1 / Context Sensitive Grammar:

$$\alpha A\beta \rightarrow \alpha\gamma\beta$$

$$|\alpha A\beta| \leq |\alpha\gamma\beta|$$

$$\begin{array}{l} A \in N \\ \alpha, \beta, \gamma \in V^* \end{array}$$

G:

$$P: Ac \rightarrow Bbcc$$

$$A \Rightarrow Bbcc$$

Grammar: 2. Type-1 / Context Sensitive Grammar: $\alpha, \beta, \gamma \in V^* A \in N$
 $\alpha A \beta \rightarrow \alpha \gamma \beta | \alpha A \beta | \alpha \gamma \beta | \dots$ G: P: Ac \rightarrow Bbcc A \Rightarrow Bbcc



Compiler Design

Classifications of Formal Grammars (Part 2)

Compiler Design Classifications of Formal Grammars (Part 2)



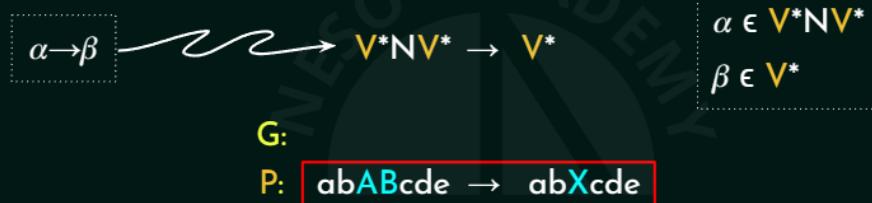
Outcome

- ☆ Type-2 and Type-3 Formal Grammars

Outcome ☆ Type-2 and Type-3 Formal Grammars

Grammar:

1. Type-0 / Unrestricted Grammar:



2. Type-1 / Context Sensitive Grammar:

$$\alpha A \beta \rightarrow \alpha \gamma \beta$$

$|aA\beta| \leq |a\gamma\beta|$

$A \in N$
 $\alpha, \beta, \gamma \in V^*$

Grammar: 1. Type-0 / Unrestricted Grammar: $\alpha \rightarrow \beta V^* N V^* \rightarrow V^*$ $\alpha \in V^* N V^* \beta \in V^*$
G:P:abABcde→abXcde
2. Type-1 / Context Sensitive Grammar: $\alpha, \beta, \gamma \in V^*$ $A \in N$
 $aA\beta \rightarrow a\gamma\beta$ $|aA\beta| \leq |a\gamma\beta|$

Grammar:

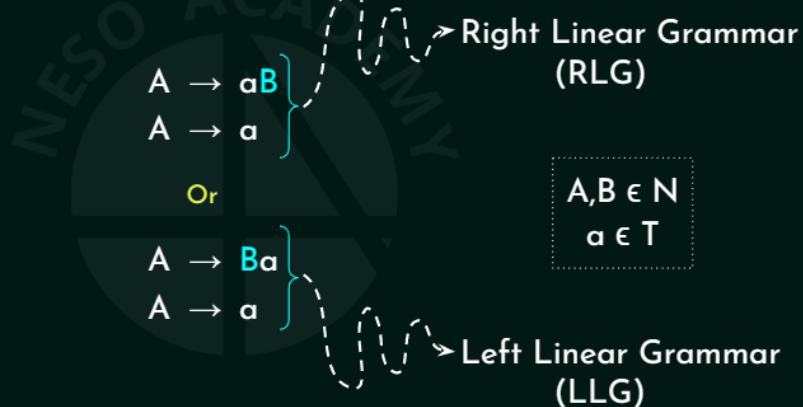
3. Type-2 / Context Free Grammar:



Grammar: 3. Type-2 / Context Free Grammar: $\alpha \in V^*$ $A \in N$ $\alpha \rightarrow G$: P: $S \rightarrow ABa$ $A \rightarrow aB$ $B \rightarrow abc$ $S \rightarrow id = E ;$ $E \rightarrow E + T | T$ $T \rightarrow T * F | F$ $F \rightarrow id$

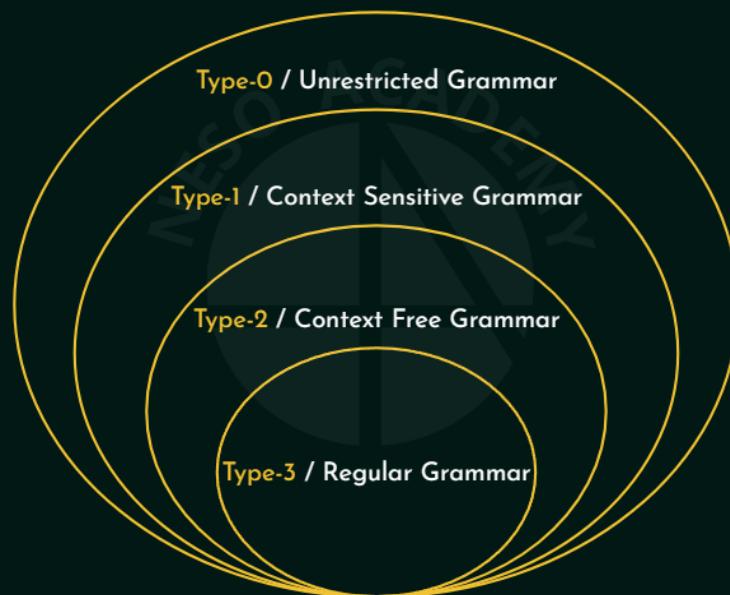
Grammar:

4. Type-3 / Regular Grammar:



$a \in T$ $A, B \in N$ Grammar: 4. Type-3 / Regular Grammar: $AaB \rightarrow Aa \rightarrow ABa \rightarrow Aa \rightarrow$ Or Right Linear Grammar (RLG) Left Linear Grammar (LLG)

Grammar:



Type-0 / Unrestricted Grammar
Type-1 / Context Sensitive Grammar
Type-2 / Context Free Grammar
Type-3 / Regular Grammar



Compiler Design

Derivations of CFGs

Compiler Design Derivations of CFGs

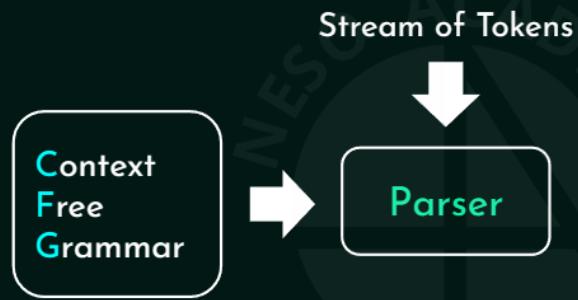


Outcome

- ☆ Understanding Left & Right Most Derivations.
- ☆ Derivations using Parse tree.

Outcome ☆ Understanding Left & Right Most Derivations. ☆ Derivations using Parse tree.

Syntax Analyzer:



Syntax Analyzer: Parser Stream of Tokens Context Free Grammar

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$

id + id x id

Left Most Derivation:

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow id + E \\ &\Rightarrow id + E \times E \\ &\Rightarrow id + id \times E \\ &\Rightarrow id + id \times id \end{aligned}$$

Right Most Derivation:

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow E + E \times E \\ &\Rightarrow E + E \times id \\ &\Rightarrow E + id \times id \\ &\Rightarrow id + id \times id \end{aligned}$$

Parse Tree Derivation:





Compiler Design

Ambiguity in CFGs

Compiler Design Ambiguity in CFGs



Outcome

- ☆ Understanding of Ambiguity in Context Free Grammars.

Outcome ☆ Understanding of Ambiguity in Context Free Grammars.

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$

$id + id \times id$

Left Most Derivation:

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow id + E \\ &\Rightarrow id + E \times E \\ &\Rightarrow id + id \times E \\ &\Rightarrow id + id \times id \end{aligned}$$

Right Most Derivation:

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow E + E \times E \\ &\Rightarrow E + E \times id \\ &\Rightarrow E + id \times id \\ &\Rightarrow id + id \times id \end{aligned}$$

Parse Tree Derivation:



Context Free Grammar:

$E \rightarrow E + E \mid E \times E \mid id$

$id + id \times id$

Left Most Derivation:

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow id + E \\ &\Rightarrow id + E \times E \\ &\Rightarrow id + id \times E \\ &\Rightarrow id + id \times id \end{aligned}$$
$$\begin{aligned} E &\Rightarrow E \times E \\ &\Rightarrow E + E \times E \\ &\Rightarrow id + E \times E \\ &\Rightarrow id + id \times E \\ &\Rightarrow id + id \times id \end{aligned}$$

Right Most Derivation:

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow E + E \times E \\ &\Rightarrow E + E \times id \\ &\Rightarrow E + id \times id \\ &\Rightarrow id + id \times id \end{aligned}$$
$$\begin{aligned} E &\Rightarrow E \times E \\ &\Rightarrow E \times id \\ &\Rightarrow E + E \times id \\ &\Rightarrow E + id \times id \\ &\Rightarrow id + id \times id \end{aligned}$$

Parse Tree Derivation:





Compiler Design

Ambiguity in CFGs – Solved Problems (Set 1)

Compiler Design Ambiguity in CFGs - Solved Problems (Set 1)



Outcome

- ☆ Two solved PYQs on finding ambiguous CFGs.

Outcome ☆ Two solved PYQs on finding ambiguous CFGs.

Q1: Determine whether the following grammar is suitable for predictive parsing,

$$S \rightarrow (S) \mid SS \mid \epsilon$$

UGC-NET
DEC 2018

Sol. Parse Tree Derivation: ()()()



Q1:Determine whether the following grammar is suitable for predictive parsing,
 $S \rightarrow (S) \mid SS \mid \epsilon$
Sol.UGC-NETDEC 2018Parse Tree Derivation:()()()SSS(S)(S)(S)SS $\epsilon\epsilon\epsilon$ SSS(S) ϵ (S)(S)SS $\epsilon\epsilon$

Q2: Consider the following two Grammars,

G1: $S \rightarrow SbS \mid a$

G2: $S \rightarrow aB \mid ab, A \rightarrow AB \mid a, B \rightarrow ABb \mid b$

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JUNE 2018

Which of the following option is correct?

- (A) Only G1 is ambiguous
- (B) Only G2 is ambiguous
- (C) Both G1 and G2 are ambiguous**
- (D) Both G1 and G2 are unambiguous

Q2:Consider the following two Grammars,G1: $S \rightarrow SbS \mid a$ G2: $S \rightarrow aB \mid ab, A \rightarrow AB \mid a, B \rightarrow ABb \mid b$ Which of the following option is correct?UGC-NETJUNE 2018(A) Only G1 is ambiguous(B) Only G2 is ambiguous(C) Both G1 and G2 are ambiguous(D) Both G1 and G2

are unambiguous

Q2: Consider the following two Grammars,

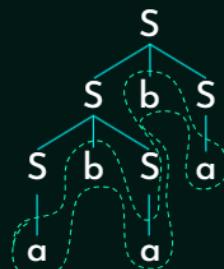
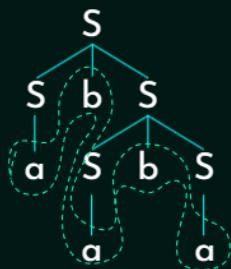
$$G1: S \rightarrow SbS \mid a$$

$$G2: S \rightarrow aB \mid ab, A \rightarrow AB \mid a, B \rightarrow ABb \mid b$$

Which of the following option is correct?

Sol. G1: $S \rightarrow SbS \mid a$

ababa



Q2: Consider the following two Grammars,
G1: $S \rightarrow SbS \mid a$
G2: $S \rightarrow aB \mid ab, A \rightarrow AB \mid a, B \rightarrow ABb \mid b$
Which of the following option is correct?
Sol. G1: $S \rightarrow SbS \mid a$
ababa
S b S
S a S a S a
S a a S a a S a a

Q2: Consider the following two Grammars,

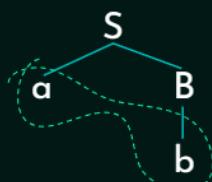
$$G1: S \rightarrow SbS \mid a$$

$$G2: S \rightarrow aB \mid ab, A \rightarrow AB \mid a, B \rightarrow ABb \mid b$$

Which of the following option is correct?

Sol. G2: $S \rightarrow aB \mid ab, A \rightarrow AB \mid a, B \rightarrow ABb \mid b$

ab



Q2: Consider the following two Grammars, G1: $S \rightarrow SbS \mid a$ G2: $S \rightarrow aB \mid ab$, $A \rightarrow AB \mid a$, $B \rightarrow ABb \mid b$
Which of the following option is correct? Sol. G2: $S \rightarrow aB \mid ab$, $A \rightarrow AB \mid a$, $B \rightarrow ABb \mid bab$



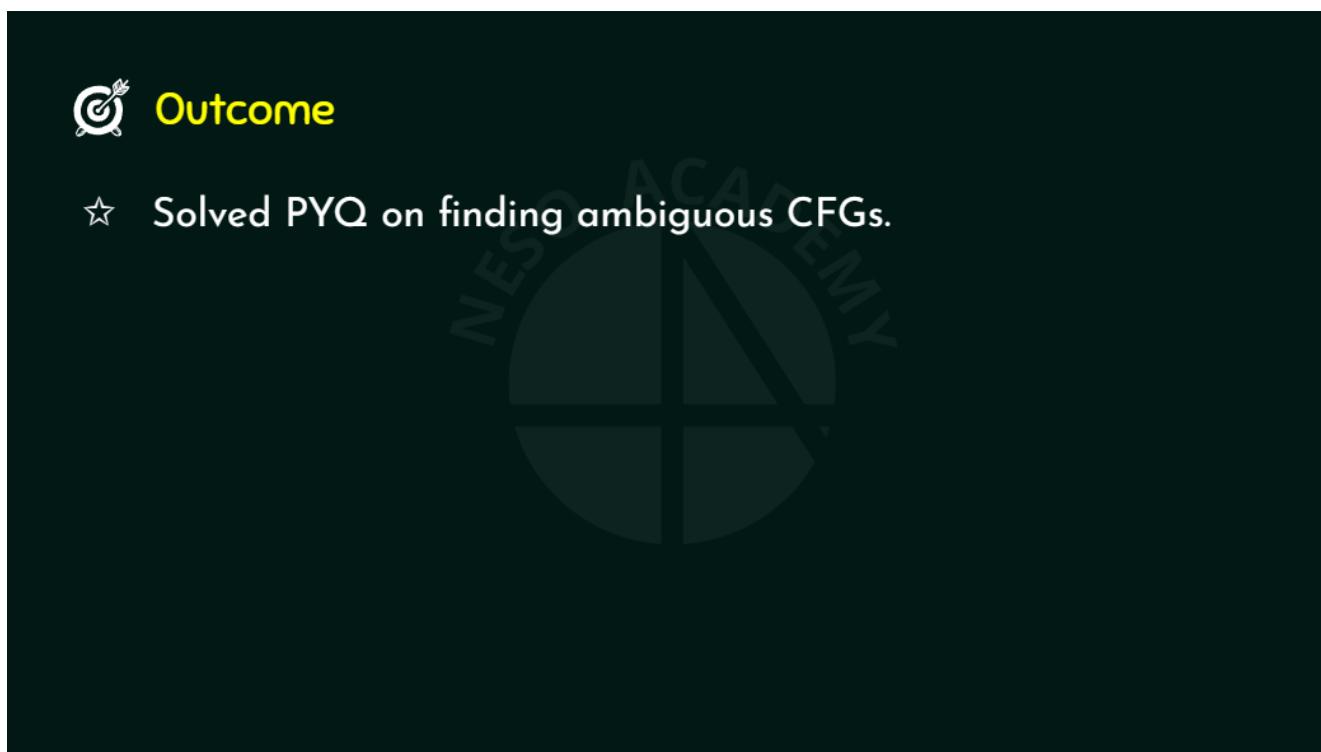
A slide titled "Compiler Design" featuring a blue gear icon above a code editor window showing C code for "Hello World". The code is:`#include<stdio.h>
int main() {
 printf("Hello World");
 return 0;
}`

The binary representation of the assembly code is shown to the right of the assembly code.

Compiler Design

Ambiguity in CFGs – Solved Problems (Set 2)

Compiler Design Ambiguity in CFGs - Solved Problems (Set 2)



Outcome

- ☆ Solved PYQ on finding ambiguous CFGs.

Outcome ☆ Solved PYQ on finding ambiguous CFGs.

Q: Which of the following grammars is (are) ambiguous?

- ✓(A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
- ✓(B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
- ✓(C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$

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NOV 2020

Where λ denotes empty string.

- 1. (A) and (C) only
- 2. (B) only
- 3. (B) and (C) only
- 4. (A) and (B) only

Q: Which of the following grammars is (are) ambiguous?
(A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
(B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
(C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$
Where λ denotes empty string.
UGC-NET NOV 2020
1. (A) and (C) only
2. (B) only
3. (B) and (C) only
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- (B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
- (C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$

Where λ denotes empty string.

Sol. (A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$

λ



Q: Which of the following grammars is (are) ambiguous?
(A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
(B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
(C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$
Where λ denotes empty string.
Sol. (A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
 $\lambda SSSS\lambda\lambda\lambda$

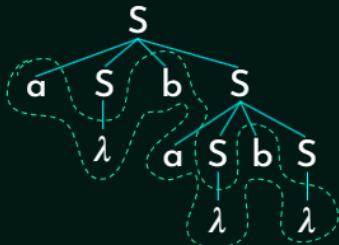
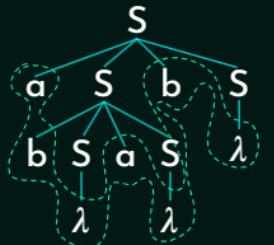
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- ✓(A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
- ✓(B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
- (C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$

Where λ denotes empty string.

Sol. (B) $S \rightarrow aSbS \mid bSaS \mid \lambda$

abab



Q: Which of the following grammars is (are) ambiguous?
 (A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
 (B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
 (C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$
 Where λ denotes empty string.
Sol. (B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
 abab
 $SS \lambda a S b S b S a S \lambda \lambda a S b S b S \lambda \lambda \lambda$

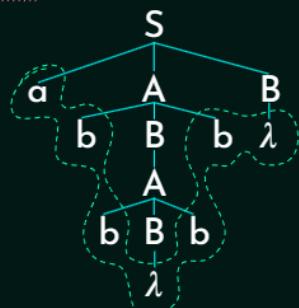
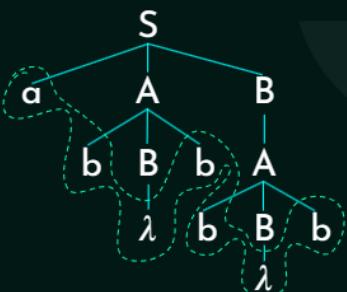
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- ✓(A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
- ✓(B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
- ✓(C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$

Where λ denotes empty string.

Sol. (C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$

abbbb



Q: Which of the following grammars is (are) ambiguous?
 (A) $S \rightarrow SS \mid aSb \mid bSa \mid \lambda$
 (B) $S \rightarrow aSbS \mid bSaS \mid \lambda$
 (C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$
 Where λ denotes empty string.
Sol. (C) $S \rightarrow aAB, A \rightarrow bBb, B \rightarrow A \mid \lambda$
 abbbb
 $S \lambda A \lambda a A B b B b B b S a A B \lambda b B b A B \lambda b B b \lambda$



Compiler Design

Problems of Ambiguity in CFGs

Compiler Design Problems of Ambiguity in CFGs



Outcome

- ☆ Problem due to Ambiguity.
- ☆ Associativity Property Violation.
- ☆ Precedence Property Violation.

Outcome ☆ Problem due to Ambiguity. ☆ Associativity Property Violation. ☆ Precedence Property Violation.

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$



$E \rightarrow E + E$ $E \rightarrow E \times E$ $E \rightarrow id$
Context Free Grammar: $id + id \times id$

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$

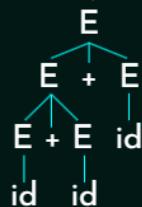


$E \rightarrow E + E$ $E \rightarrow E \times E$ $E \rightarrow id$
Context Free Grammar: $3 + 4 \times 5$ $5 \times E$ $5 \times 4 \times E$ $7 \times E$ $23 \times E$ $23 \times 20 \times E$

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$

id + id + id



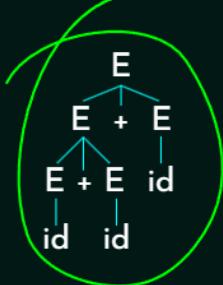
$E \rightarrow E + E$
 $E \rightarrow E \times E$
 $E \rightarrow id$ Context Free Grammar: id + id + id

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$

id + id + id

(id + id) + id
Associativity Property Violation



+ id $E \rightarrow E + E$
 $E \rightarrow E \times E$
 $E \rightarrow id$ Context Free Grammar: id + id + id (id + id) Associativity Property Violation

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$



$E \rightarrow E + E$
 $E \rightarrow E \times E$
 $E \rightarrow id$ Context Free Grammar: $id + id \times id$

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow E \times E$
3. $E \rightarrow id$



$E \rightarrow E + E$
 $E \rightarrow E \times E$
 $E \rightarrow id$ Context Free Grammar: $id + id \times id$ Precedence Property Violation



Compiler Design

Associativity violation and solution in CFGs

Compiler DesignAssociativity violation and solution in CFGs



Outcome

- ☆ Reason for Associativity violation.
- ☆ Solution to Associativity violation.

Outcome☆Reason for Associativity violation.☆Solution to Associativity violation.

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow id$



$E \rightarrow E + E$
 $E \rightarrow id$ Context Free Grammar:
 $id + id + id$

Context Free Grammar:

1. $E \rightarrow E + E$
2. $E \rightarrow id$



$E \rightarrow E + E$
 $E \rightarrow id$ Context Free Grammar:
 $id + (id + id) + id$

Context Free Grammar:

1. $E \rightarrow E + E$
 2. $E \rightarrow id$

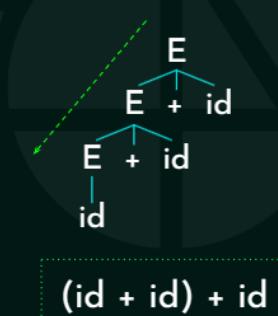
1. $E \rightarrow E + id$
 2. $E \rightarrow id$

1.E → E + E
2.E → id
Context Free Grammar: 1.E → E + id
2.E → id

Context Free Grammar:

1. $E \rightarrow E + id$
 2. $E \rightarrow id$

Left Recursive



$E \rightarrow E + id$ $id \in \{1, E\}$ $\rightarrow E + id2.E \rightarrow id$
Context Free Grammar:
 $id + id + id(id + id) + idE + idLeft$
Recursive



Compiler Design

Precedence violation and solution in CFGs

Compiler Design Precedence violation and solution in CFGs



Outcome

- ☆ Reason for Precedence violation.
- ☆ Solution to Precedence violation.

Outcome ☆ Reason for Precedence violation. ☆ Solution to Precedence violation.

Context Free Grammar:

$$E \rightarrow E + E \mid E \times E \mid id$$



$E \rightarrow E + E \mid E \times E \mid id$
Context Free Grammar:
 $id + id \times id \rightarrow E + E \mid E \times E \mid id$

Context Free Grammar:

$$E \rightarrow E + E \mid E \times E \mid id$$



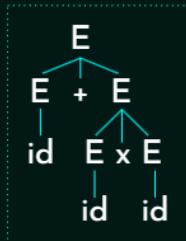
Precedence
Property
Violation



$E \rightarrow E + E \mid E \times E \mid id$
Context Free Grammar:
 $id + id \times id \rightarrow E + E \mid E \times E \mid id$

Context Free Grammar:

$$E \rightarrow E + E \mid E \times E \mid id$$



1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow id$

Context Free Grammar:
 $E \rightarrow E + E \mid E \times E \mid id$
1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow id$

Context Free Grammar:

1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow id$

Defining Levels

`id + id * id`



Context Free Grammar:
1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow id$
Defining Levels



Compiler Design

Associativity and Precedence in CFGs

Compiler Design Associativity and Precedence in CFGs



Outcome

- ☆ Determining Associativity and Precedence from a given CFG.
- ☆ Ambiguous Grammar to Unambiguous Grammar conversion.

Outcome
☆ Determining Associativity and Precedence from a given CFG.
☆ Ambiguous Grammar to Unambiguous Grammar conversion.

Context Free Grammar:

1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow G^* \mid G$
4. $G \rightarrow id$

Determine Associativity and Precedence of the operators:



1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow G^* \mid G$

Context Free Grammar:
 1. $E \rightarrow E + T \mid T$
 2. $T \rightarrow T \times F \mid F$
 3. $F \rightarrow G^* \mid G$
 4. $G \rightarrow id$
 Determine Associativity and Precedence of the operators: + , x , ^.
 1. $E \rightarrow E + T \mid T$ Left Associative
 Right Associative
 3. $F \rightarrow G^* \mid G$
 2. $T \rightarrow T \times F \mid F$

Context Free Grammar:

1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow G^* \mid G$
4. $G \rightarrow id$

Determine Associativity and Precedence of the operators:



1. $E \rightarrow E + T \mid T$
2. $T \rightarrow T \times F \mid F$
3. $F \rightarrow G^* \mid G$
4. $G \rightarrow id$

► Precedence: $\begin{array}{c} ^ \\ \text{High} \end{array} \quad \begin{array}{c} x \\ | \\ \text{Low} \end{array} \quad \begin{array}{c} + \\ | \\ \text{Low} \end{array}$

1. $E \rightarrow E + T \mid T$
 2. $T \rightarrow T \times F \mid F$
 3. $F \rightarrow G^* \mid G$
 4. $G \rightarrow id$
 Context Free Grammar:
 1. $E \rightarrow E + T \mid T$
 2. $T \rightarrow T \times F \mid F$
 3. $F \rightarrow G^* \mid G$
 4. $G \rightarrow id$
 Determine Associativity and Precedence of the operators: + , x , ^.
 Left Associative
 Right Associative
 ► Precedence: ^+xHighLow

Context Free Grammar:

Consider the following ambiguous CFG on boolean expressions:

$bExp \rightarrow bExp \text{ AND } bExp \mid bExp \text{ OR } bExp \mid \text{NOT } bExp \mid \text{True} \mid \text{False}$

The precedence of the boolean operators are NOT, AND, OR (high to low). AND, OR have left to right associativity.

1. $bExp \rightarrow bExp \text{ OR } bExp1 \mid bExp1$
2. $bExp1 \rightarrow bExp1 \text{ AND } bExp2 \mid bExp2$
3. $bExp2 \rightarrow \text{NOT } bExp2$
4. $bExp2 \rightarrow \text{True}$
5. $bExp2 \rightarrow \text{False}$

1. $bExp \rightarrow bExp \text{ OR } bExp1$
Context Free Grammar: Consider the following ambiguous CFG on boolean expressions: $bExp \rightarrow bExp \text{ AND } bExp \mid bExp \text{ OR } bExp \mid \text{NOT } bExp \mid \text{True} \mid \text{False}$
The precedence of the boolean operators are NOT, AND, OR (high to low). AND, OR have left to right associativity.
2. $bExp1 \rightarrow bExp1 \text{ AND } bExp2$
3. $bExp2 \rightarrow \text{NOT } bExp2$
4. $bExp2 \rightarrow \text{True}$
5. $bExp2 \rightarrow \text{False}$
 $bExp1 \mid bExp2$

Context Free Grammar:

Consider the following ambiguous CFG on boolean expressions:

$bExp \rightarrow bExp \text{ AND } bExp \mid bExp \text{ OR } bExp \mid \text{NOT } bExp \mid \text{True} \mid \text{False}$

The precedence of the boolean operators are NOT, AND, OR (high to low). AND, OR have left to right associativity.

1. $bExp \rightarrow bExp \text{ OR } bExp1 \mid bExp1$
2. $bExp1 \rightarrow bExp1 \text{ AND } bExp2 \mid bExp2$
3. $bExp2 \rightarrow \text{NOT } bExp2 \mid \text{True} \mid \text{False}$

Context Free Grammar: Consider the following ambiguous CFG on boolean expressions:
 $bExp \rightarrow bExp \text{ AND } bExp \mid bExp \text{ OR } bExp \mid \text{NOT } bExp \mid \text{True} \mid \text{False}$
The precedence of the boolean operators are NOT, AND, OR (high to low). AND, OR have left to right associativity.
1. $bExp \rightarrow bExp \text{ OR } bExp$
2. $bExp_1 \rightarrow bExp_1 \text{ AND } bExp_2$
3. $bExp_2 \rightarrow \text{NOT } bExp_2 \mid \text{True} \mid \text{False}$
 $bExp_1 \mid bExp_2$

Context Free Grammar:

Home work
Problem

Consider the following ambiguous CFG on regular expressions:

$$R \rightarrow R + R \mid R \cdot R \mid R^* \mid a \mid b \mid c$$

The precedence of the operators are * (Kleene star), . (AND), + (OR) (high to low). All the operators have left to right associativity.

Context Free Grammar: Consider the following ambiguous CFG on regular expressions: $R \rightarrow R + R \mid R \cdot R \mid R^* \mid a \mid b \mid c$
The precedence of the operators are * (Kleene star), . (AND), + (OR) (high to low). All the operators have left to right associativity. Home work Problem



Compiler Design

Associativity and Precedence – Solved Problems (Set 1)

Compiler DesignAssociativity and Precedence - Solved Problems (Set 1)



Outcome

- ☆ Three solved PYQs on determining associativity and precedence.

Outcome☆Three solved PYQs on determining associativity and precedence.

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')

$$\begin{aligned}S &\rightarrow T \times P \\T &\rightarrow U \mid T \times U \\P &\rightarrow Q + P \mid Q \\Q &\rightarrow \text{id} \\U &\rightarrow \text{id}\end{aligned}$$

GATE
2014

Which of the following is TRUE?

- (A) '+' is left associative, while 'x' is right associative
- (B) '+' is right associative, while 'x' is left associative**
- (C) Both '+' and 'x' are right associative
- (D) Both '+' and 'x' are left associative

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')
 $S \rightarrow T \times P \quad T \rightarrow U \mid T \times U \quad P \rightarrow Q + P \mid Q \quad Q \rightarrow \text{id}$

Which of the following is TRUE?
GATE 2014
(A) '+' is left associative, while 'x' is right associative
(B) '+' is right associative, while 'x' is left associative
(C) Both '+' and 'x' are right associative
(D) Both '+' and 'x' are left associative

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')

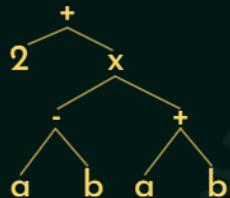
$$\begin{array}{ll}S \rightarrow T \times P & \text{Left recursive} \\T \rightarrow U \mid T \times U & T \rightarrow T \times U \\P \rightarrow Q + P \mid Q & P \rightarrow Q + P \\Q \rightarrow \text{id} & \text{Right recursive} \\U \rightarrow \text{id} &\end{array}$$

► Precedence: + x
 |-----|
 High Low

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')
 $S \rightarrow T \ x \ PT \rightarrow U \mid T \ x \ UP \rightarrow Q \ + \ P \mid QQ \rightarrow idU \rightarrow id$
Precedence: + > x
Left recursive
 $T \rightarrow T \ x \ U \mid P$
Right recursive

Q2: Consider the parse tree

TIFR PHD CS 2012



Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$).

Consider

- (i) $2 + a - b$
- (ii) $2 + a - b \times a + b$
- (iii) $(2 + ((a - b) \times (a + b)))$
- (iv) $2 + (a - b) \times (a + b)$

The parse tree corresponds to

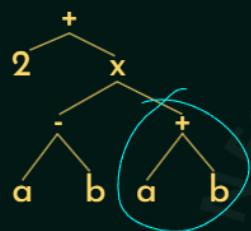
- (A) Expression (i) only
- (B) Expression (ii) only
- (C) Expression (iv) only
- (D) Expressions (ii), (iii) and (iv)
- (E) Expressions (iii) and (iv) only

Q2: Consider the parse tree TIFR PHD CS 2012
 $+ - x 2 a b a b$
Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$).

Consider
(i) $2 + a - b$
(ii) $2 + a - b \times a + b$
(iii) $(2 + ((a - b) \times (a + b)))$
(iv) $2 + (a - b) \times (a + b)$

The parse tree corresponds to
(A) Expression (i) only
(B) Expression (ii) only
(C) Expression (iv) only
(D) Expressions (ii), (iii) and (iv)
(E) Expressions (iii) and (iv) only

Q2: Consider the parse tree



Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$).

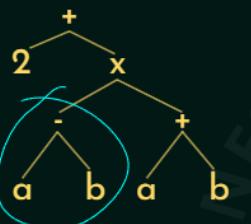
Consider

- (i) $2 + a - b$
- (ii) $2 + a - b \times a + b$
- (iii) $(2 + ((a - b) \times (a + b)))$
- (iv) $2 + (a - b) \times (a + b)$

$(a + b)$

Q2: Consider the parse tree $+ - x 2 ab ab$. Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$). Consider
(i) $2 + a - b$
(ii) $2 + a - b \times a + b$
(iii) $(2 + ((a - b) \times (a + b)))$
(iv) $2 + (a - b) \times (a + b)$

Q2: Consider the parse tree



Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$).

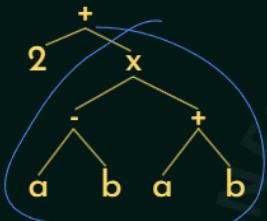
Consider

- (i) $2 + a - b$
- (ii) $2 + a - b \times a + b$
- (iii) $(2 + ((a - b) \times (a + b)))$
- (iv) $2 + (a - b) \times (a + b)$

$(a - b) (a + b)$

Q2: Consider the parse tree $+ - x 2 ab ab$. Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$). Consider
(i) $2 + a - b$
(ii) $2 + a - b \times a + b$
(iii) $(2 + ((a - b) \times (a + b)))$
(iv) $2 + (a - b) \times (a + b)$

Q2: Consider the parse tree



Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$).

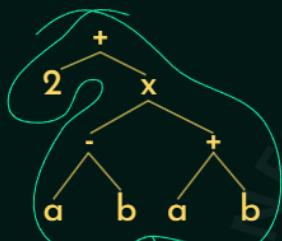
Consider

- (i) $2 + a - b$
- (ii) $2 + a - b \times a + b$
- (iii) $(2 + ((a - b) \times (a + b)))$
- (iv) $2 + (a - b) \times (a + b)$

$$(a - b) \times (a + b)$$

Q2: Consider the parse tree $+ - x 2 abab$. Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$). Consider
(i) $2 + a - b$
(ii) $2 + a - b \times a + b$
(iii) $(2 + ((a - b) \times (a + b)))$
(iv) $2 + (a - b) \times (a + b)$

Q2: Consider the parse tree



Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$).

Consider

- (i) $2 + a - b$
- (ii) $2 + a - b \times a + b$
- (iii) $(2 + ((a - b) \times (a + b)))$
- (iv) $2 + (a - b) \times (a + b)$

$$2 + ((a - b) \times (a + b))$$

Q2: Consider the parse tree $+ - x 2 abab$. Assume that 'x' has higher precedence than '+', '-' and operators associate right to left (i.e. $a+b+c = (a+(b+c))$). Consider
(i) $2 + a - b$
(ii) $2 + a - b \times a + b$
(iii) $(2 + ((a - b) \times (a + b)))$
(iv) $2 + (a - b) \times (a + b)$

Q3: Given the following expression grammar:

$$\begin{array}{l} E \rightarrow E \times F \mid F + E \mid F \\ F \rightarrow F - F \mid id \end{array}$$

Which of the following is true?

- (A) 'x' has higher precedence than '+'
 - (B) '-' has higher precedence than 'x'
 - (C) '+' and '-' have same precedence
 - (D) '+' has higher precedence than 'x'

GATE 2000

UGC-NET
Dec 2012

ISRO CS
2015

(A) ‘x’ has higher precedence than ‘+’(B) ‘-’ has higher precedence than ‘x’(C) ‘+’ and ‘-’ have same precedence(D) ‘+’ has higher precedence than ‘x’Q3:Given the following expression grammar:
 $E \rightarrow E \times F \mid F + E \mid FF$
 $F \rightarrow F - F \mid id$ Which of the following is true?GATE 2000ISRO
CS 2015UGC-NET Dec 2012



Compiler Design

Associativity and Precedence – Solved Problems (Set 2)

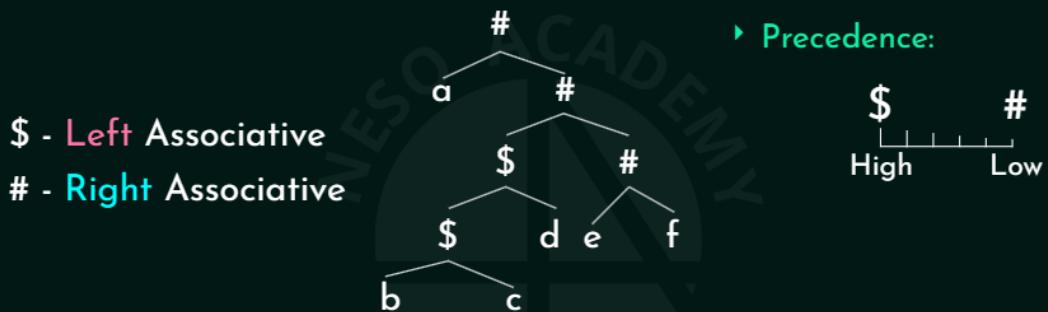


Outcome

- ★ Four solved PYQs on determining associativity and precedence.

Outcome★Four solved PYQs on determining associativity and precedence.

Q1: Consider the following parse tree for the expression $a\#b\$c\$d\#e\#f$, involving two binary operators \$ and #.



- (A) '\$' has higher precedence and is left associative; '#' is right associative
(B) '#' has higher precedence and is left associative; '\$' is right associative
(C) '\$' has higher precedence and is left associative; '#' is left associative
(D) '#' has higher precedence and is right associative; '#' is left associative

Q1: Consider the following parse tree for the expression $a\#b\$c\$d\#e\#f$, involving two binary operators \$ and #. Precedence: #>\$. Left Associative - Right Associative
(A) '\$' has higher precedence and is left associative; '#' is right associative
(B) '#' has higher precedence and is left associative; '\$' is right associative

has higher precedence and is left associative; '\$' is right associative(C) '\$' has higher precedence and is left associative; '#' is left associative(D) '#' has higher precedence and is right associative; '#' is left associative

Q2: Which of the following expression is represented by the parse tree?



UGC-NET
JUN 2010

- (A) $(A + B) \times C$
- (B) $A + x BC$
- (C) $A + B \times C$
- (D) $A \times C + B$

Q2:(x)CAB(A) (A + B) x C(B) A + x BC(C) A + B x C(D) A x C + B(+)
UGC-NET JUN 2010(A + B) x CWhich of the following expression is represented by the parse tree?

Q3: Given the grammar:

$$\begin{array}{ll} S \rightarrow T x S \mid T & S \rightarrow T x \overset{\circ}{S} \\ T \rightarrow U + T \mid U & T \rightarrow U + \overset{\circ}{T} \\ U \rightarrow id & \end{array}$$

Right recursive



ISRO CS
2020

Which of the following statements is wrong?

- (A) Grammar is not ambiguous
- (B) Priority of '+' over 'x' is ensured
- (C) Right to left evaluation of 'x' and '+' happens
- (D) None of these

(A) Grammar is not ambiguous
 (B) Priority of '+' over 'x' is ensured
 (C) Right to left evaluation of 'x' and '+' happens
 (D) None of these

Q3: Given the grammar:
 $S \rightarrow T x S \mid TT \rightarrow U + T \mid UU \rightarrow id$

Which of the following statements is wrong?

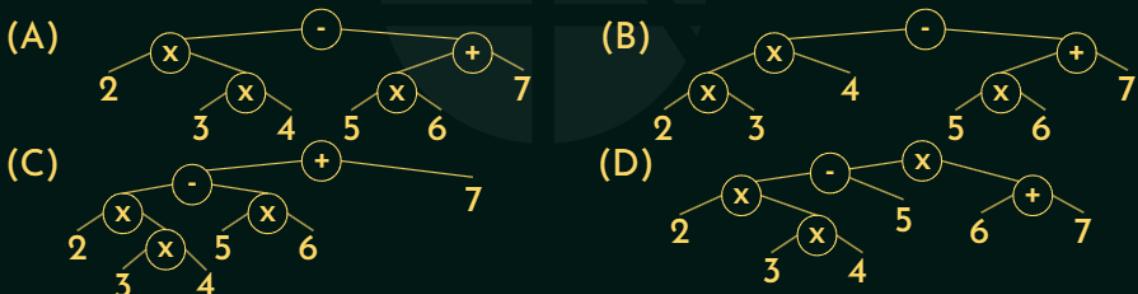
ISRO CS 2020
 $S \rightarrow T x ST \rightarrow U + TR$
 Right recursive
 +xHighLow
 Precedence:

Q4: Consider the following grammar (the start symbol is E) for generating expressions.

$$\begin{aligned} E &\rightarrow T - E \mid T + E \mid T \\ T &\rightarrow T \times F \mid F \\ T &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

TIFR PHD CS 2015

With respect to this grammar, which of the following tree is valid evaluation tree for the expression $2 \times 3 \times 4 - 5 \times 6 + 7$?



3x4732x(A)Q4: Consider the following grammar (the start symbol is E) for generating expressions.
 $E \rightarrow T - E \mid T + E \mid TT \rightarrow T \times F \mid FT \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$
With respect to this grammar, which of the following tree is valid evaluation tree for the expression
 $2 \times 3 \times 4 - 5 \times 6 + 7$?
TIFR PHD CS 2015(B)(C)(D)-x+x276543x-x+x7654+-65xx2-x243xx5+76

Q4: Consider the following grammar (the start symbol is E) for generating expressions.

$$\begin{aligned} E &\rightarrow T - E \mid T + E \quad \text{Right recursive} \\ T &\rightarrow T \times F \mid F \quad \text{Left recursive} \\ T &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

TIFR PHD CS 2015

With respect to this grammar, which of the following tree is valid evaluation tree for the expression $((2 \times 3) \times 4) - ((5 \times 6) + 7)$?

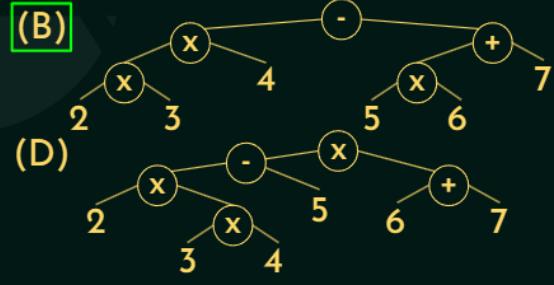
(A)



(C)



(B)



(D)



3x4732x(A)Q4:Consider the following grammar (the start symbol is E) for generating expressions.
 $E \rightarrow T - E \mid T + E \mid TT \rightarrow T \times F \mid FT \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$
 With respect to this grammar, which of the following tree is valid evaluation tree for the expression $((2 \times 3) \times 4) - ((5 \times 6) + 7)$?
 TIFR PHD CS 2015(B)(C)(D)-x+x276543x-x+x7654+-65xx2-x243xx5+76
 Left recursive
 Right recursive



Compiler Design

Recursion in CFGs



Outcome

- ☆ Understanding left and right recursion.

Outcome☆Understanding left and right recursion.

Q1: Consider the grammar defined by the following production rules,
(with two operators 'x' and '+')

$$\begin{aligned}S &\rightarrow T \times P \\T &\rightarrow U \mid T \times U \\P &\rightarrow Q + P \mid Q \\Q &\rightarrow \text{id} \\U &\rightarrow \text{id}\end{aligned}$$

GATE
2014

Which of the following is TRUE?

- (A) '+' is left associative, while 'x' is right associative
- (B) '+' is right associative, while 'x' is left associative
- (C) Both '+' and 'x' are right associative
- (D) Both '+' and 'x' are left associative

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')
 $S \rightarrow T \times P \mid T \times U$
 $T \rightarrow Q + P \mid Q$
 $P \rightarrow \text{id}$
 $U \rightarrow \text{id}$

Which of the following is TRUE?

GATE 2014

- (A) '+' is left associative, while 'x' is right associative
- (B) '+' is right associative, while 'x' is left associative
- (C) Both '+' and 'x' are right associative
- (D) Both '+' and 'x' are left associative

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')

$$S \rightarrow T x P \quad \text{Left recursive}$$

$$T \rightarrow U \mid T x U$$

$$P \rightarrow Q + P \mid Q$$

$$Q \rightarrow \text{id}$$

$$U \rightarrow \text{id}$$

Right recursive

Q1: Consider the grammar defined by the following production rules, (with two operators 'x' and '+')
 $S \rightarrow T x P \rightarrow U \mid T x U \rightarrow Q + P \mid Q$
 $Q \rightarrow \text{id}$
 $U \rightarrow \text{id}$

Left Recursion

$$A \beta$$

$$A \rightarrow A\alpha \mid \beta$$

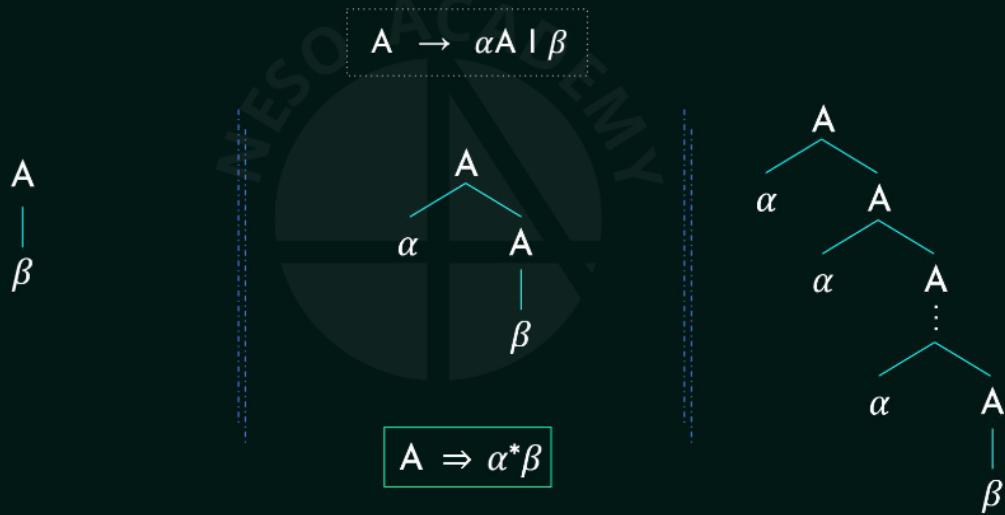
$$\begin{array}{c} A \\ \swarrow \quad \searrow \\ A \quad \alpha \\ | \\ \beta \end{array}$$

$$A \Rightarrow \beta\alpha^*$$

$$\begin{array}{c} A \\ \swarrow \quad \searrow \\ A \quad \alpha \\ \vdots \\ A \quad \alpha \\ | \\ \beta \end{array}$$

$A\beta\alpha^* \Rightarrow \text{Left Recursion}$
 $A \rightarrow A\alpha \mid \beta$
 $\beta A \beta A \alpha A A \alpha A \alpha \beta A \alpha \beta$

Right Recursion



Compiler Design

Problem of Left Recursion and Solution in CFGs

Compiler Design Problem of Left Recursion and Solution in CFGs

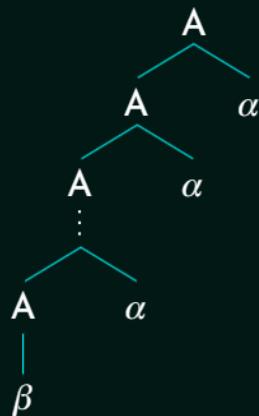


Outcome

- ☆ Problem due to Left recursion.
- ☆ Solution provided by Right recursion.
- ☆ Conversion of Left recursion to Right recursion.

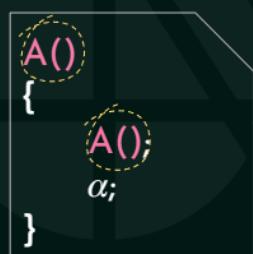
Outcome
☆ Problem due to Left recursion.
☆ Solution provided by Right recursion.
☆ Conversion of Left recursion to Right recursion.

Left Recursion



$$A \rightarrow A\alpha \mid \beta$$

$$A \Rightarrow \beta\alpha^*$$

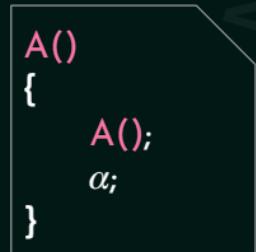


$A\beta\alpha^* \Rightarrow$ Left Recursion $A \rightarrow A\alpha \mid \beta$ $A A\alpha A\alpha\beta A\alpha\beta A() \{ A(); \alpha; \}$

Left Recursion

$$A \rightarrow A\alpha \mid \beta$$

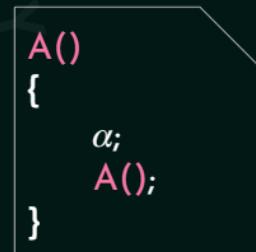
$$A \Rightarrow \beta\alpha^*$$



Right Recursion

$$A \rightarrow \alpha A \mid \beta$$

$A \Rightarrow \alpha^* \beta$



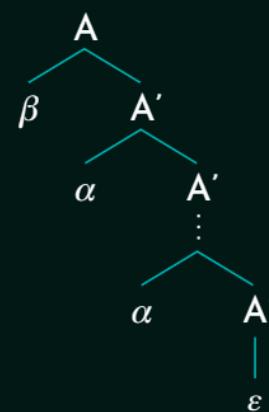
Left Recursion $A \rightarrow A\alpha \mid \beta A\beta\alpha^* \Rightarrow A() \{A();\alpha;\}$ Right Recursion $A \rightarrow \alpha A \mid \beta A\alpha^*\beta \Rightarrow A() \{\alpha;A();\beta\}$

Conversion

$$A \rightarrow A\alpha \mid \beta$$

$$A \Rightarrow \beta\alpha^*$$

$$A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \varepsilon$$



Conversion $A \rightarrow A\alpha \mid \beta A \beta \alpha^* \Rightarrow A \rightarrow \beta A' \alpha \rightarrow \alpha A' \mid \varepsilon A A' \beta A' \alpha \varepsilon A' \alpha \varepsilon A' \beta A$



Compiler Design

Elimination of Left Recursion – Solved Problems

Compiler Design Elimination of Left Recursion - Solved Problems



Outcome

- ☆ Four solved examples on eliminating Left recursion.

Outcome ☆ Four solved examples on eliminating Left recursion.

Eliminate Left Recursion

Ex1: $P \rightarrow P + Q \mid Q$
 $A \rightarrow A \alpha \mid \beta$

$A \rightarrow \beta A'$
 $A' \rightarrow \alpha A' \mid \epsilon$

$P \rightarrow QP'$
 $P' \rightarrow +QP' \mid \epsilon$

+QP' Ex1: $P \rightarrow P + Q \mid Q$ Eliminate Left Recursion
AA $\alpha \rightarrow \beta$ IA $\rightarrow \beta A'$ A $\rightarrow \alpha A' \mid \epsilon$ P $\rightarrow QP' \rightarrow I \epsilon P'$

Eliminate Left Recursion

Ex2: $S \rightarrow S0S1S \mid 01$
 $A \rightarrow A \alpha \mid \beta$

$A \rightarrow \beta A'$
 $A' \rightarrow \alpha A' \mid \epsilon$

$S \rightarrow 01S'$
 $S' \rightarrow 0S1SS' \mid \epsilon$

Ex2: $S \rightarrow S0S1S \mid 01$ Eliminate Left Recursion
AA $\alpha \rightarrow \beta$ IA $\rightarrow \beta A'$ A $\rightarrow \alpha A' \mid \epsilon$ S $\rightarrow 01S'$ S $\rightarrow 0S1S'$

Eliminate Left Recursion

Ex3: $A \rightarrow (B) \mid b$
 $B \rightarrow B \times A \mid A$
 $A \rightarrow A \alpha \mid \beta$

$A \rightarrow \beta A'$
 $A' \rightarrow \alpha A' \mid \varepsilon$

$A \rightarrow (B) \mid b$
 $B \rightarrow AB'$
 $B' \rightarrow xAB' \mid \varepsilon$

$A \rightarrow (B) \mid b$ Ex3:
A → (B) | b
B → B × A | A
A → Aα | β
Eliminate Left Recursion
A → βA'
A' → αA' | ε
B → AB'
B' → xAB' | ε
AA → βIB'

Eliminate Left Recursion

Ex4: $A \rightarrow A\alpha_1 \mid A\alpha_2 \mid A\alpha_3 \mid \dots \mid \beta_1 \mid \beta_2 \mid \beta_3 \mid \dots$

$A \rightarrow \beta A'$
 $A' \rightarrow \alpha A' \mid \varepsilon$

$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \beta_3 A' \mid \dots$
 $A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \alpha_3 A' \mid \dots \mid \varepsilon$

$\alpha_1 A'$ Ex4:
A → Aα1 | Aα2 | Aα3 | ... | β1 | β2 | β3 | Eliminate Left Recursion
A → βA'
A' → αA' → | β1A' | β2A' | β3A' | ... | α2A' | α3A' | ... | ε



Compiler Design

Non-deterministic CFGs

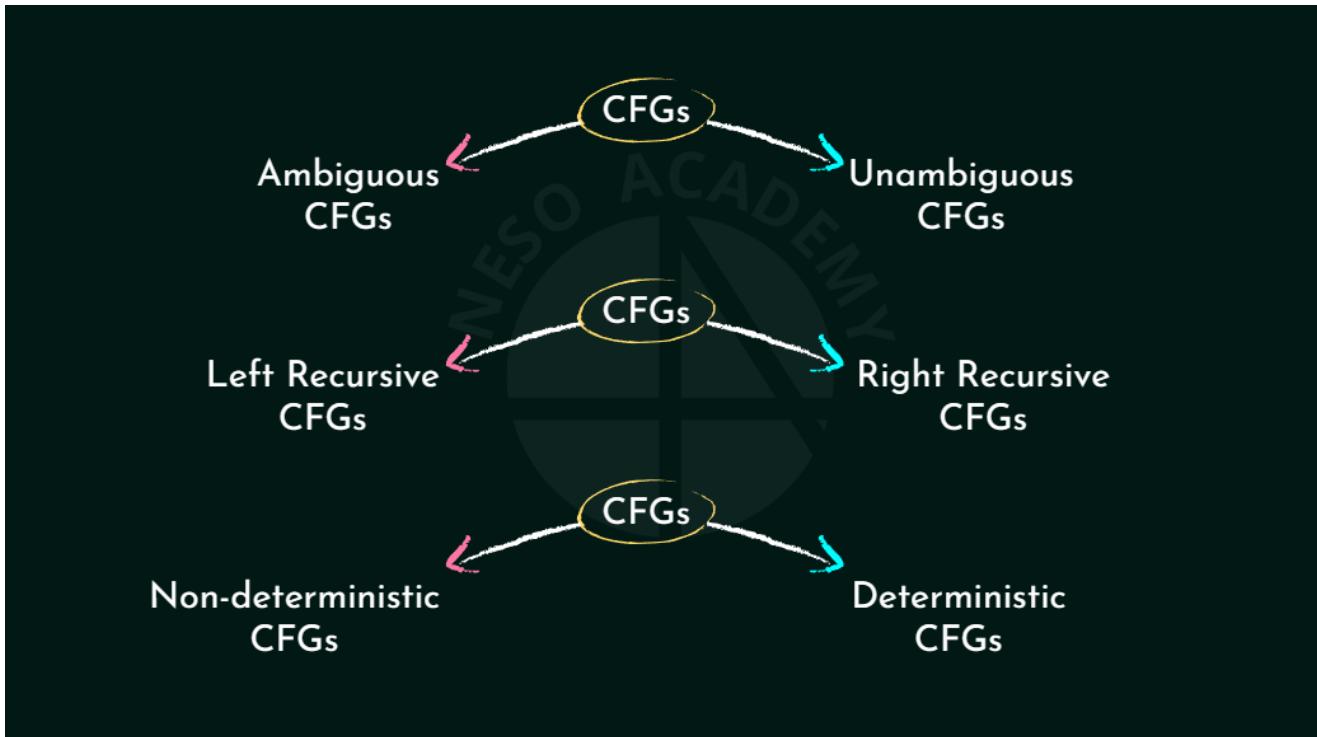
Compiler Design Non-deterministic CFGs



Outcome

- ☆ Different classifications of CFGs.
- ☆ Understanding Non-determinism.
- ☆ Left factoring procedure.

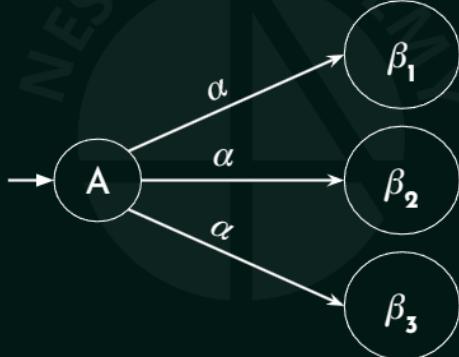
Outcome ☆ Different classifications of CFGs. ☆ Understanding Non-determinism. ☆ Left factoring procedure.



CFGs
Ambiguous CFGs
Unambiguous CFGs
Left Recursive CFGs
Right Recursive CFGs
Non-deterministic CFGs
Deterministic CFGs

Non-deterministic CFGs:

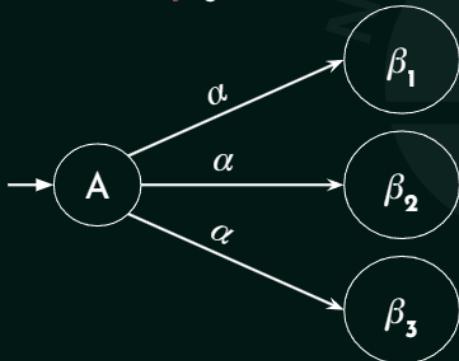
1. $A \rightarrow \alpha\beta_1$
2. $A \rightarrow \alpha\beta_2$
3. $A \rightarrow \alpha\beta_3$



Non-deterministic CFGs:
1. $A \rightarrow \alpha\beta_1$
2. $A \rightarrow \alpha\beta_2$
3. $A \rightarrow \alpha\beta_3$

Non-deterministic CFGs:

1. $A \rightarrow \alpha\beta_1$
2. $A \rightarrow \alpha\beta_2$
3. $A \rightarrow \alpha\beta_3$



$\alpha\beta_3$



Non-deterministic CFGs:
1. $A \rightarrow \alpha\beta_1$
2. $A \rightarrow \alpha\beta_2$
3. $A \rightarrow \alpha\beta_3$

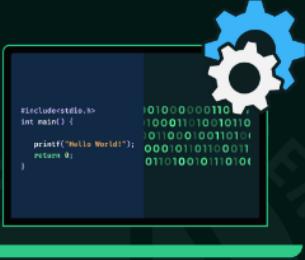
Non-deterministic CFGs:

1. $A \rightarrow \alpha\beta_1$
2. $A \rightarrow \alpha\beta_2$
3. $A \rightarrow \alpha\beta_3$

$A \rightarrow \alpha A'$
 $A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$

Left Factoring

Non-deterministic CFGs:
1. $A \rightarrow \alpha\beta_1$
2. $A \rightarrow \alpha\beta_2$
3. $A \rightarrow \alpha\beta_3$
 $A \rightarrow \alpha A' \rightarrow A' \mid \beta_3$
Left Factoring



Compiler Design

Non-deterministic CFGs – Solved Problems (Set 1)

Compiler Design Non-deterministic CFGs - Solved Problems (Set 1)



Outcome

- ☆ Two solved examples on Left factoring.
- ☆ Proof: Determinism cannot remove ambiguity.

Outcome
☆ Two solved examples on Left factoring.
☆ Proof: Determinism cannot remove ambiguity.

Eliminate non-determinism:

Ex1: $A \rightarrow aAB \mid aBc \mid aAc$

$A \rightarrow aA'$

$A' \rightarrow AB \mid Ac \mid Bc$

$A \rightarrow aA'$
 $A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$

$A \rightarrow aA'$
 $A' \rightarrow AA'' \mid Bc$
 $A'' \rightarrow B \mid c$

$A \rightarrow aA'A' \rightarrow AA'' \mid BcA'' \rightarrow B \mid c$
A → aAB | aBc | aAc
Ex1: Eliminate non-determinism:
 $\beta_2\beta_1A \rightarrow aA' \rightarrow A' \mid \beta_3A \rightarrow aA'A' \rightarrow AB \mid Ac \mid Bc$

Eliminate non-determinism:

Ex2: $S \rightarrow iEtS \mid iEtSeS \mid a$
 $E \rightarrow b$

$S \rightarrow iEtS_\varepsilon \mid iEtSeS \mid a$
 $A \rightarrow \alpha \quad \beta_1 \mid \alpha \quad \beta_2$

$A \rightarrow aA'$
 $A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$

$S \rightarrow iEtSS' \mid a$
 $S' \rightarrow \varepsilon \mid eS$
 $E \rightarrow b$

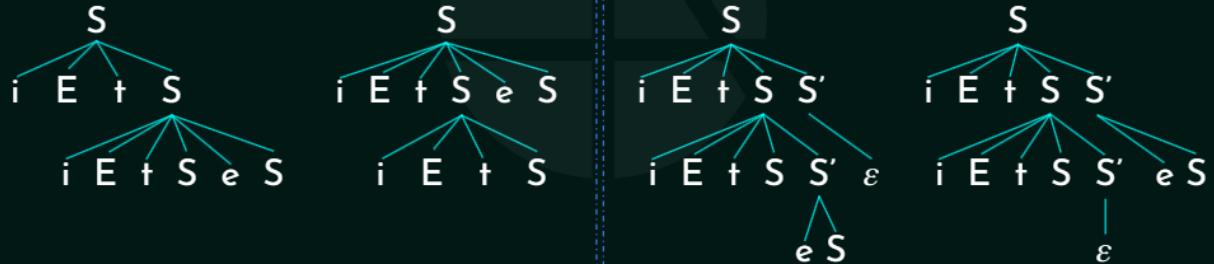
Ex2: Eliminate non-determinism:
 $S \rightarrow iEtS \mid iEtSeS \mid aE \rightarrow bI \beta_2\beta_1A \rightarrow aA' \rightarrow A' \mid \beta_3S \rightarrow iEtSS' \mid aS' \rightarrow \varepsilon \mid eSE \rightarrow bS \rightarrow iEtS_\varepsilon \mid iEtSeS \mid a \rightarrow Aa\beta_1\mid a\beta_2$

Determinism vs Ambiguity:

$S \rightarrow iEtS \mid iEtSeS \mid a$
 $E \rightarrow b$

iEt*iEtSeS*

$$\begin{array}{l} S \rightarrow iEtSS' \mid a \\ S' \rightarrow \varepsilon \mid eS \\ E \rightarrow b \end{array}$$

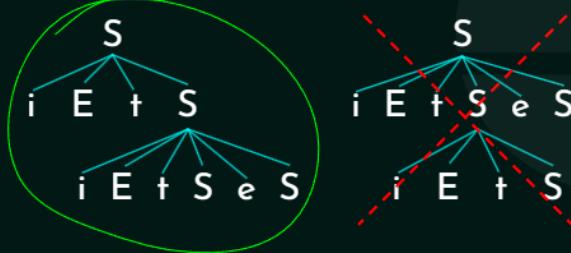


Determinism vs Ambiguity:
 $S \rightarrow iEtSS' \mid aS' \rightarrow \epsilon \mid eSE \rightarrow bS \rightarrow iEtS \mid iEtSeS \mid aE \rightarrow bSi \mid E t$
 $Si \mid E t S \mid e SSi \mid E t Si \mid E t S \mid e SSi \mid E t S \mid S \mid S'i \mid E t S \mid S \mid S'i \mid E t S \mid S \mid S'e \mid S \mid e Si \mid E t SeS$

Reason for Ambiguity:

$S \rightarrow iEtS \mid iEtSeS \mid a$
 $E \rightarrow b$

iEt*iEtSeS*



```
if(E)  
{  
    if(E)  
        { S }  
    else  
        { S }  
}
```

$S \rightarrow iEtS \mid iEtSeS \mid aE \rightarrow bSi \mid E \mid t \mid S \mid e \mid Si \mid E \mid t \mid S \mid e \mid Si \mid Et \mid Se \mid Sif(E) \{ if(E) \{ S \} else \{ S \} \}$ Reason for Ambiguity:



Compiler Design

Non-deterministic CFGs – Solved Problems (Set 2)

Compiler Design Non-deterministic CFGs - Solved Problems (Set 2)



Outcome

- ☆ Three solved examples on Left factoring.

Outcome ☆ Three solved examples on Left factoring.

Eliminate non-determinism:

Ex1: $S \rightarrow aSSbS \mid aSaSb \mid abb \mid b$

$$A \rightarrow \alpha \beta_1 \mid \alpha \beta_2 \mid \alpha \beta_3$$

$$\begin{aligned} A &\rightarrow \alpha A' \\ A' &\rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \end{aligned}$$

$$\begin{aligned} S &\rightarrow aS' \mid b \\ S' &\rightarrow SSbS \mid SaSb \mid bb \end{aligned}$$

$S \rightarrow aSSbS \mid aSaSb \mid abb \mid b$
 Ex1: Eliminate non-determinism:
 $\rightarrow A\alpha\alpha\alpha\beta_1\beta_2\beta_3$
 $\beta_2\beta_1A \rightarrow aA' \rightarrow A'\beta_3$
 $S \rightarrow aS' \mid bS' \rightarrow SSbS \mid SaSb \mid bb$

Eliminate non-determinism:

Ex1: $S \rightarrow aSSbS \mid aSaSb \mid abb \mid b$

$$\begin{aligned} S &\rightarrow aS' \mid b \\ S' &\rightarrow SSbS \mid SaSb \mid bb \\ A &\rightarrow \alpha \beta_1 \mid \alpha \beta_2 \end{aligned}$$

$$\begin{aligned} A &\rightarrow \alpha A' \\ A' &\rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \end{aligned}$$

$$\begin{aligned} S &\rightarrow aS' \mid b \\ S' &\rightarrow SS'' \mid bb \\ S'' &\rightarrow SbS \mid aSb \end{aligned}$$

$S \rightarrow aS' \mid bS' \rightarrow SS'' \mid bbS'' \rightarrow SbS \mid aSbS \rightarrow aS' \mid bS' \rightarrow SSbS \mid SaSb \mid bbS \rightarrow aSSbS \mid aSaSb \mid abb \mid b$
 Ex1: Eliminate non-determinism:
 $\rightarrow A\alpha\beta_1\beta_2 \mid \beta_2\beta_1A \rightarrow aA' \rightarrow A'\beta_3 \mid \alpha$

Eliminate non-determinism:

Ex2: $S \rightarrow bSSaaS \mid bSSaSb \mid bSb \mid a$

$$A \rightarrow \alpha \quad \beta_1 \quad \mid \quad \alpha \quad \beta_2 \quad \mid \quad \alpha \quad \beta_3$$

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$$

$$S \rightarrow bSS' \mid a$$

$$S' \rightarrow SaaS \mid SaSb \mid b$$

Ex2: Eliminate non-determinism:
 $\beta_2 \beta_1 A \rightarrow \alpha A' \rightarrow A' \mid \beta_3$
 $S \rightarrow bSSaaS \mid bSSaSb \mid bSb \mid a$
 $A \rightarrow \alpha \beta_1 \beta_2 \beta_3 \alpha \alpha S \rightarrow bSS' \mid aS' \rightarrow SaaS \mid SaSb \mid b$

Eliminate non-determinism:

Ex2: $S \rightarrow bSSaaS \mid bSSaSb \mid bSb \mid a$

$$S \rightarrow bSS' \mid a$$

$$S' \rightarrow SaaS \mid SaSb \mid b$$

$$A \rightarrow \alpha \quad \beta_1 \quad \mid \quad \alpha \quad \beta_2$$

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$$

$$S \rightarrow bSS' \mid a$$

$$S' \rightarrow SaS'' \mid b$$

$$S'' \rightarrow aS \mid Sb$$

Eliminate non-determinism:

Ex3: $S \rightarrow a \mid ab \mid abc \mid abcd$

$$S \rightarrow a\epsilon \mid ab \mid abc \mid abcd$$

$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \alpha\beta_3 \mid \alpha\beta_4$

$A \rightarrow aA'$
$A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$

$$S \rightarrow aS'$$

$$S' \rightarrow \epsilon \mid b \mid bc \mid bcd$$

$I \alpha a S \rightarrow a\epsilon \mid ab \mid abc \mid abcd$
 Ex3: Eliminate non-determinism:
 $I \beta 2 \beta 1 A \rightarrow aA' \rightarrow A' I \beta 3 S \rightarrow a \mid ab \mid abc \mid abcd$
 $\rightarrow A\beta_1 \beta_2 \mid a\beta_3 \beta_4 \mid S \rightarrow aS' \rightarrow \epsilon \mid b \mid bc \mid bcd$

Eliminate non-determinism:

Ex3: $S \rightarrow a \mid ab \mid abc \mid abcd$

$$S \rightarrow aS'$$

$$S' \rightarrow b\epsilon \mid bc \mid bcd \mid \epsilon$$

$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \alpha\beta_3$

$A \rightarrow aA'$
$A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$

$$S' \rightarrow bS'' \mid \epsilon$$

$$S'' \rightarrow \epsilon \mid c \mid cd$$

$I \beta 2 \beta 1 A \rightarrow aA' \rightarrow A' I \beta 3 S \rightarrow a \mid ab \mid abc \mid abcd$
 $S \rightarrow aS' \mid S' \rightarrow b\epsilon \mid bc \mid bcd \mid \epsilon$
 $A \rightarrow a\beta_1 \beta_2 \mid a\beta_3 \beta_4 \mid S'' \rightarrow \epsilon \mid c \mid cd$

Eliminate non-determinism:

Ex3: $S \rightarrow a \mid ab \mid abc \mid abcd$

$S \rightarrow aS'$

$S' \rightarrow bS'' \mid \varepsilon$

$S'' \rightarrow c\varepsilon \mid cd \mid \varepsilon$

$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$

$A \rightarrow \alpha A'$

$A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$

$S \rightarrow aS'$

$S' \rightarrow bS'' \mid \varepsilon$

$S'' \rightarrow cS''' \mid \varepsilon$

$S''' \rightarrow d \mid \varepsilon$

$S \rightarrow aS'S' \rightarrow bS'' \mid \varepsilon S'' \rightarrow cS''' \mid \varepsilon S''' \rightarrow d \mid \varepsilon$

Ex3: Eliminate non-determinism: l

$\beta_2 \beta_1 A \rightarrow \alpha A' \rightarrow A' \mid \beta_3 S \rightarrow a \mid ab \mid abc \mid abcd$

$A \alpha \rightarrow \beta_2 S \rightarrow aS'S' \rightarrow bS'' \mid \varepsilon S'' \rightarrow c\varepsilon \mid cd \mid \varepsilon$