

TUTORIAL 3 SOLUTION

Q1)

Q-1. (a) $(17)_{10} \rightarrow (?)_2$

2	17		Remainder
2	8	-	1
2	4	-	0
2	2	-	0
	1	-	0

MSB

LSB

Read from the bottom (MSB) to top (LSB)
as $(10001)_2$.

$$(17)_{10} \rightarrow (10001)_2$$

(b) $(33)_{10} \rightarrow (?)_2$

2	33		
2	16	-	1
2	8	-	0
2	4	-	0
2	2	-	0
	1	-	0

$\Rightarrow (100001)_2$

(c) $(67)_{10} \rightarrow (?)_2$

2	67		
2	33	-	1
2	16	-	1
2	8	-	0
2	4	-	0
2	2	-	0
	1	-	0

$\Rightarrow (1000011)_2$

$$(d) (130)_{10} \rightarrow (?)_2$$

2	130	
2	65	-0
2	32	-1
2	16	-0
2	8	-0
2	4	-0
2	2	-0
	1	-0

$$\Rightarrow (10000010)_2$$

$$(e) (2560)_{10} \rightarrow (?)_2$$

2	2560	
2	1280	-0
2	640	-0
2	320	-0
2	160	-0
2	80	-0
2	40	-0
2	20	-0
2	10	-0
2	5	-0
2	2	-1
	1	-0

$$\Rightarrow (101000000000)_2$$

Q2)

Q-2. (a) $(270)_{10}$

first, convert the decimal number into Binary.

2	270	
2	135	-0
2	67	-1
2	33	-1
2	16	-1
2	8	-0
2	4	-0
2	2	-0
	1	-0

$$\Rightarrow (100001110)_2$$

Minimum no. of bits needed to represent $(270)_{10}$ is 9 bits.

(b) $(520)_{10}$

2	520	
2	260	- 0
2	130	- 0
2	65	- 0
2	32	- 1
2	16	- 0
2	8	- 0
2	4	- 0
2	2	- 0
	1	- 0

$\Rightarrow (1000001000)_2$

Minimum
no. of bits \Rightarrow 10 bits
Required

(c) $(780)_{10}$

2	780	
2	390	- 0
2	195	- 0
2	97	- 1
2	48	- 1
2	24	- 0
2	12	- 0
2	6	- 0
2	3	- 0
	1	- 1

$\Rightarrow (1100001100)_2$

Min. no. of
bits required \Rightarrow 10 bits

(d) $(1029)_{10}$

2	1029	
2	514	- 1
2	257	- 0
2	128	- 1
2	64	- 0
2	32	- 0
2	16	- 0
2	8	- 0
2	4	- 0
2	2	- 0
	1	- 0

$\Rightarrow (10000000101)_2$

Min. no. of
bits required \Rightarrow 11 bits

Q3)

$$\underline{Q-3.} \quad (i) \quad (x_1 + x_3) \cdot (\bar{x}_1 + \bar{x}_3) = x_1 \cdot \bar{x}_3 + \bar{x}_1 \cdot x_3$$

$$\underline{L.H.S.} = (x_1 + x_3) (\bar{x}_1 + \bar{x}_3)$$

$$= x_1 \cdot \bar{x}_1 + x_1 \cdot \bar{x}_3 + x_3 \cdot \bar{x}_1 + x_3 \cdot \bar{x}_3$$

$$\{ \text{we know, } A \cdot \bar{A} = 0 \}$$

$$= 0 + x_1 \cdot \bar{x}_3 + x_3 \cdot \bar{x}_1 + \cancel{x_3 \cdot \bar{x}_3} 0$$

$$= x_1 \cdot \bar{x}_3 + x_3 \cdot \bar{x}_1$$

$$\Rightarrow \underline{R.H.S.}$$

$$(ii) \quad x_1 \cdot \bar{x}_3 + x_1 \cdot x_3 + \bar{x}_2 \cdot \bar{x}_3 + \bar{x}_2 \cdot x_3 = x_1 + \bar{x}_2$$

$$\underline{L.H.S.} : = x_1 \cdot \bar{x}_3 + x_1 \cdot x_3 + \bar{x}_2 \cdot \bar{x}_3 + \bar{x}_2 \cdot x_3$$

$$= x_1 \cdot (\bar{x}_3 + x_3) + \bar{x}_2 \cdot (\bar{x}_3 + x_3)$$

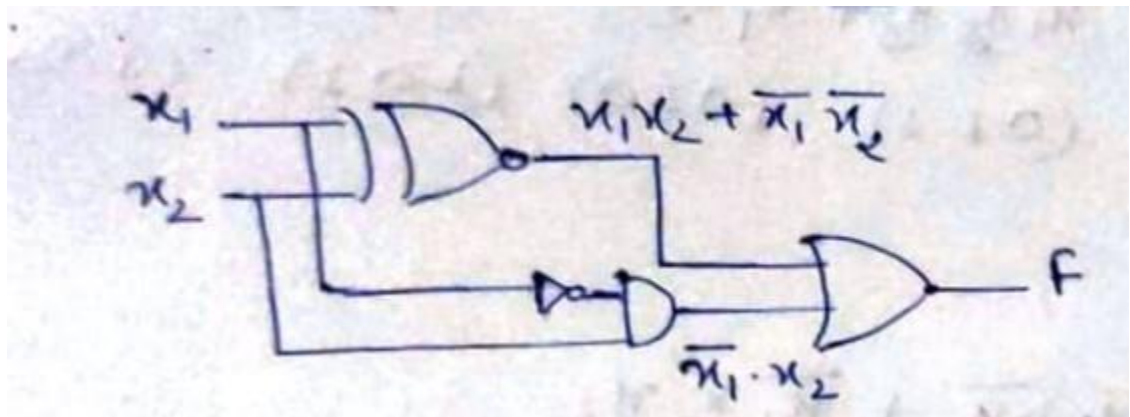
$$\{ \text{we know, } A + \bar{A} = 1 \}$$

$$= x_1 \cdot 1 + \bar{x}_2 \cdot 1$$

$$= x_1 + \bar{x}_2$$

$$\Rightarrow \underline{R.H.S.}$$

Q4)
(i)



(ii)

(ii) $f(s_1, s_2, s_3) = \bar{s}_1 \cdot \bar{s}_2 \cdot s_3 + \bar{s}_1 \cdot s_2 \cdot s_3 + s_1 \cdot \bar{s}_2 \cdot s_3 + s_1 s_2 \bar{s}_3 + s_1 s_2 s_3$

We can write it in SOP:

$$f(s_1, s_2, s_3) = \sum (001, 011, 101, 110, 111)$$

$$= \sum (1, 3, 5, 6, 7) \quad \left[\begin{array}{l} \text{we can minimize} \\ \text{it through K-map} \\ \text{Also} \end{array} \right]$$

or

$$f(s_1, s_2, s_3) = \bar{s}_1 \cdot s_3 (\bar{s}_2 + s_2) + s_1 s_3 (\bar{s}_2 + s_2) + s_1 s_2 \bar{s}_3$$

$$= \bar{s}_1 \cdot s_3 + s_1 s_3 + s_1 s_2 \bar{s}_3$$

$$= s_3 (\bar{s}_1 + s_1) + s_1 s_2 \bar{s}_3$$

$$f(s_1, s_2, s_3) \Rightarrow s_3 + s_1 s_2 \bar{s}_3$$

Q5)

Ans 5:

(i) $(x+y)(x+y) = x+y$; To Prove

LHS: $(x+y)(x+y) = x \cdot x + x \cdot y + y \cdot x + y \cdot y = x + y + xy$
 $= x(1+y) + y \Rightarrow x+y$ (therefore $LHS = RHS$)

(ii) $x \cdot y + y \cdot z + \bar{x} \cdot z = x \cdot y + \bar{x} \cdot z$

LHS: $x \cdot y + y \cdot z + \bar{x} \cdot z =$ we need to remove yz from LHS
 \therefore we will use $(x + \bar{x} = 1)$

$$\begin{aligned} x \cdot y + yz(x + \bar{x}) + \bar{x} \cdot z &\Rightarrow x \cdot y + xyz + \bar{x}yz + \bar{x} \cdot z \\ &\Rightarrow xy(1+z) + \bar{x}z(1+y) \\ &\Rightarrow \underline{xy + \bar{x}z} \quad \boxed{LHS = RHS} \\ &\quad \text{Proved} \end{aligned}$$

Q6)

Q6

(a) $\bar{x}_1 x_3 + x_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 + x_1 \bar{x}_2 = \bar{x}_2 x_3 + x_1 \bar{x}_3 + x_2 \bar{x}_3 + \bar{x}_1 x_2 x_3$

LHS $\bar{x}_1 x_3 + x_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 + x_1 \bar{x}_2$

$= \bar{x}_1 x_3 (x_2 + \bar{x}_2) + x_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 (x_3 + \bar{x}_3) + x_1 \bar{x}_2 (x_3 + \bar{x}_3)$

$= \bar{x}_1 x_2 x_3 + \bar{x}_1 \bar{x}_2 x_3 + x_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 x_3 + \bar{x}_1 \bar{x}_2 x_3 + x_1 \bar{x}_2 x_3 + x_1 x_2 \bar{x}_3$

$= (011) \quad (001) \quad (110) \quad (011) \quad (010) \quad (101) \quad (100)$

$= \sum m(1, 2, 3, 4, 5, 6)$

RHS

$(x_1 + \bar{x}_1) \bar{x}_2 x_3 + x_1 (x_2 + \bar{x}_2) \bar{x}_3 + (x_1 + \bar{x}_1) x_2 \bar{x}_3 + \bar{x}_1 x_2 x_3$

$= x_1 \bar{x}_2 x_3 + \bar{x}_1 \bar{x}_2 x_3 + x_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 \bar{x}_3 + x_1 x_2 x_3 + \bar{x}_1 x_2 \bar{x}_3 + \bar{x}_1 x_2 x_3$

$= (101) \quad (001) \quad (110) \quad (100) \quad (110) \quad (010) \quad (011)$

$= \sum m(1, 2, 3, 4, 5, 6) \quad \text{SOP of RHS} = \text{SOP of LHS}$

\therefore Same function.

(b)

$$(b) \quad x_1 \bar{x}_3 + x_2 x_3 + \bar{x}_2 \bar{x}_3 = (x_1 + \bar{x}_2 + x_3)(x_1 + x_2 + \bar{x}_3)(\bar{x}_1 + x_2 + \bar{x}_3)$$

LHS:

$$x_1 \bar{x}_3 + x_2 x_3 + \bar{x}_2 \bar{x}_3$$

$$x_1(x_2 + \bar{x}_2)\bar{x}_3 + (x_1 + \bar{x}_1)x_2 x_3 + (x_1 + \bar{x}_1)\bar{x}_2 \bar{x}_3$$

$$x_1 x_2 \bar{x}_3 + x_1 \bar{x}_2 \bar{x}_3 + x_1 x_2 x_3 + \bar{x}_1 x_2 x_3 + x_1 \bar{x}_2 \bar{x}_3 + \bar{x}_1 \bar{x}_2 \bar{x}_3$$

$$LHS = \sum m(110, 100, 111, 011, 100, 000)$$

$$LHS = \sum m(6, 4, 7, 3, 4, 0) \Rightarrow \pi M(1, 2, 5) \quad \underline{\text{Ans}}$$

$$RHS = \pi M(010, 001, 101)$$

$$RHS = \pi M(2, 1, 5)$$

$$\boxed{RHS = LHS}$$

(c)

$$(c) \quad (x_1 + x_3)(\bar{x}_1 + \bar{x}_2 + \bar{x}_3)(\bar{x}_1 + x_2)$$

LHS:

$$\left. \begin{array}{l} 010 \\ 000 \end{array} \right\} (x_1 + x_3)$$

$$\left. \begin{array}{l} 111 \end{array} \right\} (\bar{x}_1 + \bar{x}_2 + \bar{x}_3)$$

$$\left. \begin{array}{l} 100 \\ 101 \end{array} \right\} (\bar{x}_1 + x_2)$$

$$LHS = \pi M(010, 000, 111, 100, 101)$$

$$LHS = \pi M(2, 0, 7, 4, 5)$$

RHS:

$$\left. \begin{array}{l} 001 \\ 000 \end{array} \right\} (x_1 + x_2)$$

$$\left. \begin{array}{l} 000 \\ 100 \end{array} \right\} (x_2 + x_3)$$

$$\left. \begin{array}{l} 101 \\ 111 \end{array} \right\} (\bar{x}_1 + \bar{x}_3)$$

$$RHS = \pi M(000, 001, 100, 101, 111)$$

$$RHS = \pi M(0, 1, 4, 5, 7)$$

$$\boxed{RHS \neq LHS}$$

Ans

Q7)

Sol 7

S_1 = weight
 S_2 = small diameter
 S_3 = large diameter.

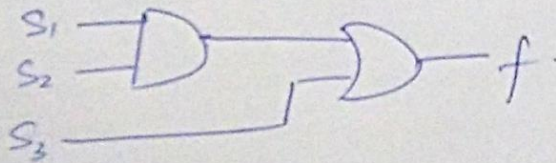
S_1	S_2	S_3	f	
0	0	0	0	m_0
0	0	1	1	m_1
0	1	0	0	m_2
0	1	1	1	m_3
1	0	0	0	m_4
1	0	1	1	m_5
1	1	0	1	m_6
1	1	1	1	m_7

f is 1 if gumball is too large i.e. $S_3 = 1$ OR when gumball is small and light i.e. $S_1 = 1$ and $S_2 = 1$

therefore from the truth table

	$S_2 S_3 \bar{S}_1$	$\bar{S}_2 S_3$	$S_2 S_2$	$S_1 \bar{S}_3$
\bar{S}_1		1	1	
S_1	1	1	1	1

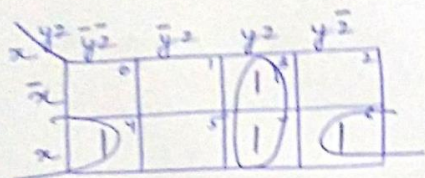
$$f = S_3 + S_1 S_2$$



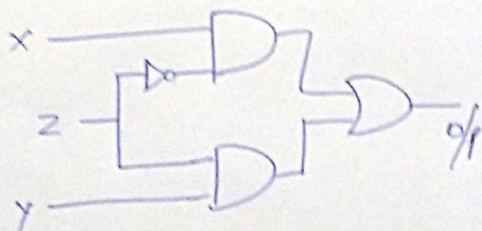
Q8)

Sol 8

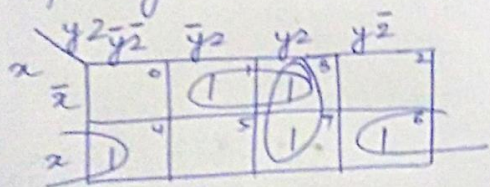
i) $f(x, y, z) = \sum m(3, 4, 6, 7)$



$$f(x, y, z) = yz + \bar{z}x$$

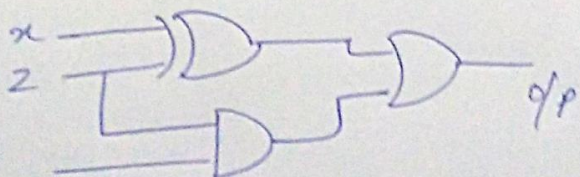


ii) $f(x, y, z) = \sum m(1, 3, 4, 6, 7)$



$$f(x, y, z) = yz + x\bar{z} + \bar{x}z$$

$$= x \oplus z + yz$$



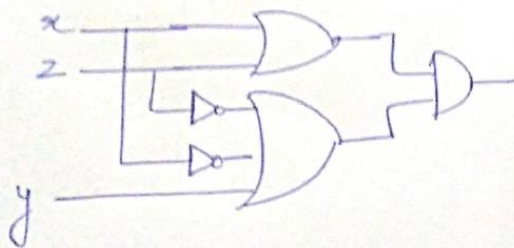
Q9)

Soln

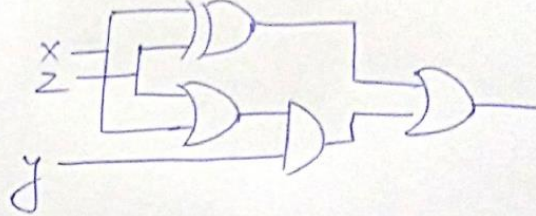
i) $f(x, y, z) = \prod M(0, 2, 5)$

$z \backslash y$	$y+z$	$y+\bar{z}$	$\bar{y}+z$	$\bar{y}+\bar{z}$
x	0			0
\bar{x}		0		

$f(x, y, z) = (x+z)(\bar{x}+y+\bar{z})$



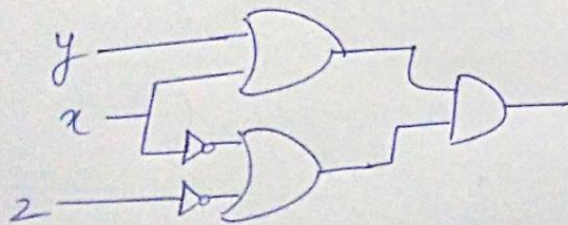
OR
 $= (x+z)(\bar{x}+\bar{z}) + y(x+z)$
 $= x \oplus z + y(x+z)$



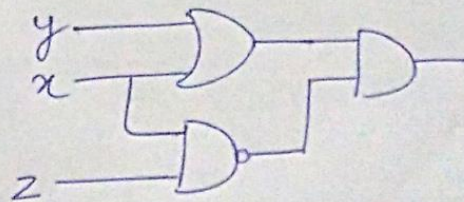
ii) $f(x, y, z) = \prod M(0, 1, 5, 7)$

$z \backslash y$	$y+z$	$y+\bar{z}$	$\bar{y}+z$	$\bar{y}+\bar{z}$
x	0	0		
\bar{x}		0	0	

$f(x, y, z) = (x+y)(\bar{x}+\bar{z})$



OR
 $= (\bar{x}\bar{z})(x+y)$



Q10)

$$10) \quad f(w, x, y, z) = w \cdot \bar{y} \cdot \bar{z} + x \cdot \bar{y} \cdot z + w \cdot \bar{x} \cdot \bar{y}$$

$w \backslash x$	$y \cdot z$	$\bar{y} \cdot \bar{z}$	$\bar{y} \cdot z$	$y \cdot \bar{z}$
$\bar{w} \cdot \bar{x}$				
$\bar{w} \cdot x$			1	
$w \cdot \bar{x}$	1	1	1	
$w \cdot x$	1	1		

$$= w \cdot \bar{y} + x \cdot \bar{y} \cdot z$$

Q11)

$$11) \quad f(w, x, y, z) = (w + y + z) \cdot (x + y + z) \cdot (w + x + y)$$

$w \backslash x$	$y \cdot z$	$y \cdot \bar{z}$	$\bar{y} \cdot \bar{z}$	$\bar{y} \cdot z$
$w + x$	0	0		
$w + \bar{x}$	0			
$\bar{w} + \bar{x}$				
$\bar{w} + x$	0			

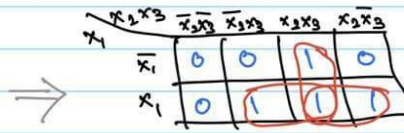
The expression can't be simplified further

It contains 3 terms

Q12)

12)

x_1	x_2	x_3	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1



$$\Rightarrow F(x_1, x_2, x_3) = x_1 \cdot x_3 + x_1 \cdot x_2 + x_2 \cdot x_3$$

