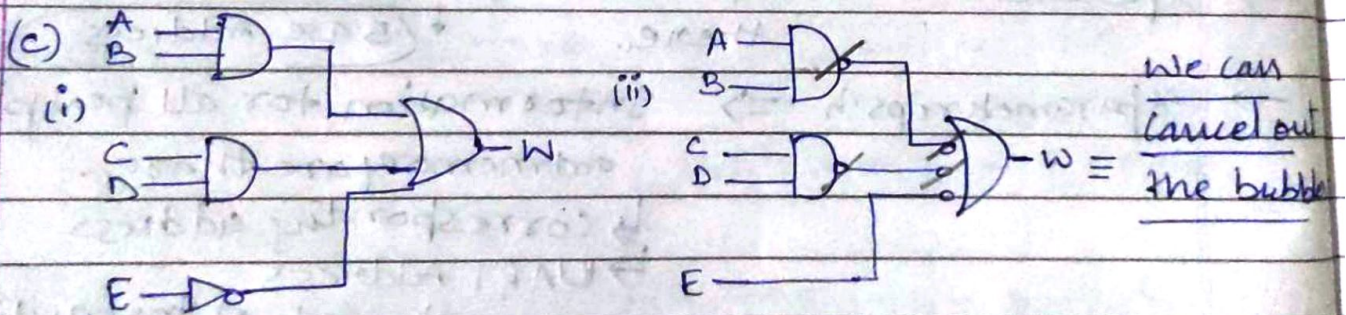


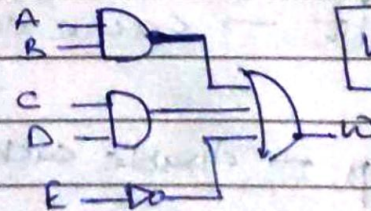
Practice Problem-1

Ans 1 : (a) $\begin{matrix} a \\ b \end{matrix} \Rightarrow \text{AND} \Rightarrow c$ $\begin{matrix} a \\ b \end{matrix} \Rightarrow \text{NAND} \Rightarrow c$
 $c = \overline{ab}$ $c = \overline{a+b}$ Both are
 $c = \overline{ab}$ \therefore equal
 (using De-Morgan)

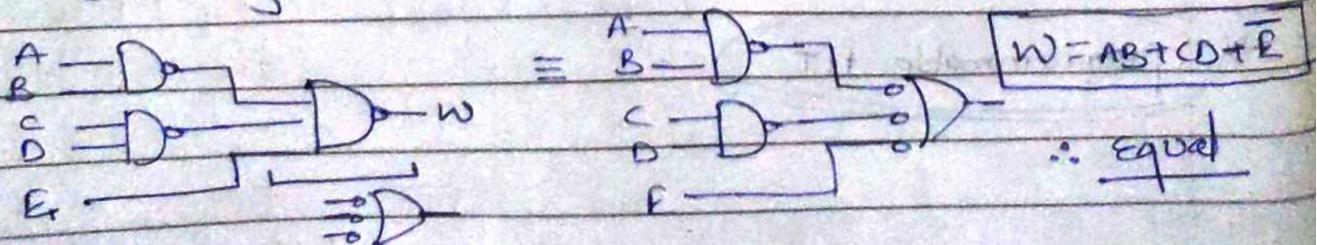
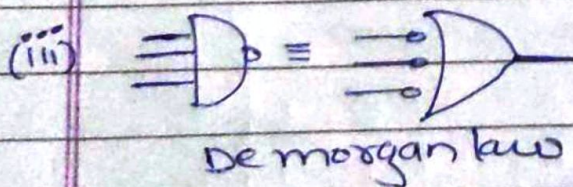
(b) $\begin{matrix} a \\ b \end{matrix} \Rightarrow \text{OR} \Rightarrow c$ $\begin{matrix} a \\ b \end{matrix} \Rightarrow \text{NAND} \Rightarrow c$
 $c = \overline{a+b}$ $c = \overline{a} \cdot \overline{b} = \overline{a+b}$ (De-morgan law)



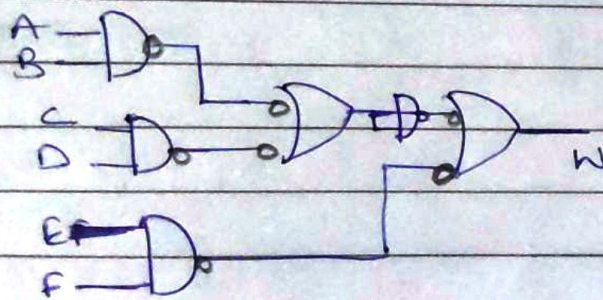
$$W = AB + CD + \overline{E}$$




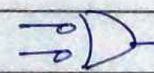
$$W = AB + CD + \overline{E}$$



Ans 2 : $W = AB + CD + EF$



 NAND

 NAND

(Due to De-Morgan's law)

Ans 3: $\overline{W}\overline{Y} + W\overline{Y} + XY = X + \overline{Y}$

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LHS: $(\overline{W} + W)\overline{Y} + XY \Rightarrow \overline{Y} + XY \Rightarrow (\overline{Y} + X)(\overline{Y} + Y)$
 $\Rightarrow \overline{Y} + X$ (LHS = RHS)
Proved

Truth Table:

Truth Table:

$$\overline{x}\overline{y}\overline{w} + \overline{x}\overline{y}\overline{w} + x\overline{y}w + \overline{x}\overline{y}w + x\overline{y}w + x\overline{y}\overline{w}$$

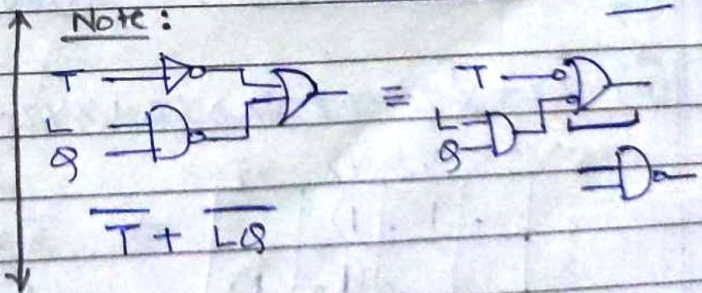
$$(100) \quad (000) \quad (101) \quad (001) \quad (111) \quad (110)$$

| | | | | |
|---|----|----|----|----|
| | yz | 01 | 11 | 10 |
| x | 0 | 1 | 1 | 0 |
| | 1 | 1 | 1 | 1 |

$$\therefore \boxed{X + \overline{Y}} \quad \underline{\text{Ans}}$$

Ans 4 : (a) $Z = AB \cdot [\overline{B} + \overline{C}] \Rightarrow AB[\overline{BC}] \Rightarrow AB\overline{B} + AB\overline{C}$
 $Z = AB\overline{C} \quad \underline{\text{Ans}}$

(b) $M = FT + \overline{L}\overline{Q}\overline{T} + Q$
 $= FT + \overline{L}\overline{1}\overline{Q} + \overline{T} + Q$
 $\Rightarrow (F + \overline{T}) + \overline{L} \quad \underline{\text{Ans}}$



(c) $\overline{\overline{A} \cdot \overline{B}} \equiv \overline{\overline{A}} + \overline{\overline{B}} \equiv A + B$ [De-morgan]
 $P = \overline{W}X + \overline{X}Z\overline{Y} + \overline{X}YZ$
 $\equiv \overline{W}X + \overline{X}Z + \overline{X}Y \quad \underline{\text{Ans}}$

(d) $P = \overline{x}y\overline{w} + x\overline{w} + \overline{x}\overline{y}z \quad \underline{\text{Ans}}$

(e) $P = (w + x + \overline{y})(\overline{w} + \overline{x})(x + y + z) \quad \underline{\text{Ans}}$

Ans 5:

$$S = ABC + \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} \quad C = AB + BC_{in} + AC_{in}$$

| ABC_{in} | C | S |
|------------|-----|-----|
| 000 | 0 | 0 |
| 001 | 0 | 1 |
| 010 | 0 | 1 |
| 011 | 1 | 0 |
| 100 | 0 | 1 |
| 101 | 1 | 0 |
| 110 | 1 | 0 |
| 111 | 1 | 1 |

→ It is acting as a full-Adder

→ S = sum

→ C = carry

Ans 6:

A 0 0 0 0 1 1 1 1 0

B 0 0 1 1 0 0 1 1 0

Cin 0 1 0 1 0 1 0 1 0

S 0 1 1 0 1 0 0 1 0

Carry 0 0 1 0 1 1 1 1 0

Ans 7: (i) $A + AB' + ABC'$

$$\Rightarrow ABC + \overline{A}BC + A\overline{B}C + AB\overline{C} + A\overline{B}\overline{C} + A\overline{B}C + A\overline{B}\overline{C} + A\overline{B}\overline{C}$$

| A \ BC | $\overline{B}C$ | $\overline{A}C$ | BC | $B\overline{C}$ |
|----------------|-----------------|-----------------|------|-----------------|
| \overline{A} | 0 | 0 | 0 | 0 |
| A | 1 | 1 | 1 | 1 |

$\Rightarrow A$ Ans
(Proved)

(ii) $XY + X'Z + Y \cdot Z \Rightarrow XYZ + XY\overline{Z} + \overline{X}YZ + \overline{X}\overline{Y}Z + XYZ + \overline{X}YZ$

| X \ YZ | $\overline{Y}Z$ | $\overline{Y}\overline{Z}$ | YZ | $Y\overline{Z}$ |
|----------------|-----------------|----------------------------|------|-----------------|
| \overline{X} | 0 | 1 | 1 | 0 |
| X | 1 | 0 | 1 | 1 |

$\Rightarrow \overline{X}Z + XY$ Ans
(Proved)

Ans 8: (i) $A + A\overline{B} + ABC \Rightarrow A + A\overline{B}C \Rightarrow A(1 + \overline{B}C) \Rightarrow A$
 \rightarrow Truth table proof is in Ans 7.

(ii) $XY + YZ + \overline{X}Z \Rightarrow XY + XYZ + \overline{X}YZ + \overline{X}Z \Rightarrow XY + \overline{X}Z$ Ans
 \rightarrow Truth table proof is in Ans 7.

(iii) $X + \overline{X}Y = (X + \overline{X})(X + Y) \Rightarrow X + Y$ Ans

| X \ Y | 0 | 1 |
|-------|---|---|
| 0 | 0 | 1 |
| 1 | 1 | 1 |

$X + Y$ (Proved)