

INDRAPRASTHA INSTITUTE OF INFORMATION TECHNOLOGY DELHI

ECE111: Digital Circuits

Quiz 1 Solution (10 points)

Exam Date: February 6, 2022

Note:

1. The exam will start at 12:00 p.m.
2. After 12:20 p.m, start submitting the same on the classroom.
3. Any submission after 12:30 p.m will be counted under late submission, with 1 mark as penalty for each minute till 12:35 p.m.
4. All submission after 12:35 p.m will be graded zero.

Rubrics:

1. Both parts carry 5 points each.
2. Solving expression carry 3 points and the circuit carry 2 points.

Penalties:

1. Point 3 & 4 from 'Note' part.
2. If you have drawn the correct circuit without solving the expression, then you will get only 1 point for that particular question, as it is not possible to draw the circuit without expression.
3. We are not giving penalty for naming convention/not submitting PDF file this time, but make sure to read and follow the instructions carefully for future submissions.
4. These are final remarks and no email regarding the same will be entertained.

SOLUTIONS

1. Implement the following functions using minimum number of 2-input NOR gates. You can use axioms, postulates and expression mentioned below and the DeMorgan's law and any other Theorem to simplify the expression. You can also use associativity of XOR operation.

Solutions

$$a) f(x, y, z) = (x \cdot z) \oplus [(x + y) \cdot z] \oplus [(x + y) \cdot (x + \bar{y}) \cdot (\overline{x \cdot \bar{z}})]$$

$$f(x, y, z) = (x \cdot z) \oplus [(x + y) \cdot z] \oplus [x \cdot (\overline{x \cdot \bar{z}})] \quad \text{used } x + (y \cdot z) = (x + y) \cdot (x + z) \text{ and } x \cdot \bar{x} = 0$$

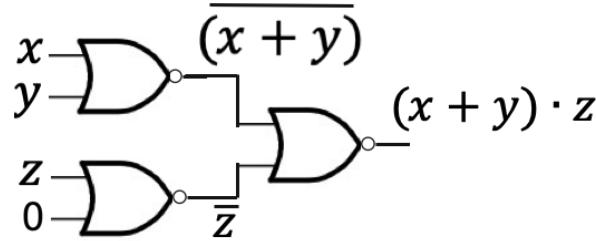
$$f(x, y, z) = (x \cdot z) \oplus [(x + y) \cdot z] \oplus [x \cdot (\bar{x} + z)] \quad \text{used De Morgan's Law}$$

$$f(x, y, z) = (x \cdot z) \oplus [(x + y) \cdot z] \oplus [x \cdot z] \quad \text{used } x \cdot (y + z) = x \cdot y + x \cdot z \text{ and } x \cdot \bar{x} = 0$$

$$f(x, y, z) = (x \cdot z) \oplus (x \cdot z) \oplus [(x + y) \cdot z] \quad \text{used } A \oplus B = B \oplus A$$

$$f(x, y, z) = 0 \oplus [(x + y) \cdot z] \quad \text{used } A \oplus A = 0$$

$$f(x, y, z) = [(x + y) \cdot z] \quad \text{used } 0 \oplus A = A$$



$$b) f(x, y, z) = z \cdot \bar{y} \oplus x \cdot \bar{y} \oplus (\bar{x} + y) \oplus y \cdot \bar{x} \oplus \bar{z} \cdot \bar{y}$$

$$f(x, y, z) = z \cdot \bar{y} \oplus x \cdot \bar{y} \oplus \overline{(\bar{x} + y)} \oplus y \cdot \bar{x} \oplus \bar{z} \cdot \bar{y}$$

$$f(x, y, z) = z \cdot \bar{y} \oplus x \cdot \bar{y} \oplus \overline{(x \cdot \bar{y})} \oplus y \cdot \bar{x} \oplus \bar{z} \cdot \bar{y}$$

used $A \oplus \bar{A} = 1$

$$f(x, y, z) = z \cdot \bar{y} \oplus 1 \oplus y \cdot \bar{x} \oplus \bar{z} \cdot \bar{y}$$

$$f(x, y, z) = \bar{z} \cdot \bar{y} \oplus y \cdot \bar{x} \oplus \bar{z} \cdot \bar{y}$$

used $A \oplus 1 = \bar{A}$

$$f(x, y, z) = \bar{z} \cdot \bar{y} \oplus \bar{z} \cdot \bar{y} \oplus y \cdot \bar{x}$$

used $A \oplus B = B \oplus A$

$$f(x, y, z) = \overline{\bar{z} \cdot \bar{y}} \cdot (\bar{z} \cdot \bar{y}) + (\bar{z} \cdot \bar{y}) \cdot (\overline{\bar{z} \cdot \bar{y}}) \oplus y \cdot \bar{x}$$

used $x \oplus y = \bar{x} \cdot y + x \cdot \bar{y}$

$$f(x, y, z) = (z \cdot \bar{y}) \cdot (\bar{z} \cdot \bar{y}) + (\bar{z} + y) \cdot (z + y) \oplus y \cdot \bar{x}$$

$$f(x, y, z) = (\bar{z} + y) \cdot (z + y) \oplus y \cdot \bar{x}$$

used $x \cdot \bar{x} = 0$ and $x \cdot y = y \cdot x$

$$f(x, y, z) = (y + z \cdot \bar{z}) \oplus y \cdot \bar{x}$$

used $x + y = y + x$ and $(x + y) \cdot (x + z) = (x + yz)$

$$f(x, y, z) = y \oplus y \cdot \bar{x}$$

used $x \cdot \bar{x} = 0$

$$f(x, y, z) = y \cdot \bar{y} \cdot \bar{x} + \bar{y} \cdot (y \cdot \bar{x})$$

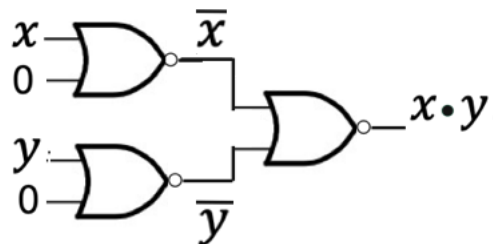
used $x \oplus y = \bar{x} \cdot y + x \cdot \bar{y}$

$$f(x, y, z) = y \cdot (\bar{y} + x)$$

used $x \cdot \bar{x} = 0$

$$f(x, y, z) = xy = \overline{\bar{x}\bar{y}} = \overline{(\bar{x} + \bar{y})}$$

used $x \cdot \bar{x} = 0$



Axioms, Postulates and Logical Expression:

- $0 \cdot 0 = 0, 1 \cdot 1 = 1, 0 \cdot 1 = 1 \cdot 0 = 0$
- $0 + 0 = 0, 1 + 1 = 1, 0 + 1 = 1 + 0 = 1$
- $x + 0 = x, x \cdot 1 = x$
- $x \cdot y = y \cdot x, x + y = y + x$
- $x \cdot (y + z) = x \cdot y + x \cdot z$

- $x + (y \cdot x) = (x + y) \cdot (x + z)$
- $x \cdot \bar{x} = 0, \quad x + \bar{x} = 1$
- $x \oplus y = \bar{x} \cdot y + x \cdot \bar{y}$