

Table 3.1 Mellin transform of commonly used probability distributions. Note that $\delta, \omega, \omega_1, \omega_2 > 0$ and $-\infty < v < \infty, (a)_n = a(a-1)\dots(a-n+1)$ is Pochhammer notation [166], $a!!$ denotes the double factorial, and $\mathcal{M}[f_V^+(v)](s)$ denotes the Mellin transform of the PDF $f_V^+(v)$ whereby V is a random variable with a standard tabulated distribution.

Positive-half PDF $f_V^+(v)$ of V	$M_V^+(s) = \mathcal{M}[f_V^+(v)](s)$	Simplified form of $M_V^+(m+1)$ when $m \in \mathbb{Z}^+$
Normal: $\frac{1}{\delta\sqrt{2\pi}} \exp\left(-\frac{v^2}{2\delta^2}\right)$	$\delta^{s-1} \left[\frac{2^{(s-3)/2} \Gamma(\frac{s}{2})}{\sqrt{\pi}} \right]$	$\delta^m \left[\frac{2^{m/2-1} (\frac{m-1}{2})!}{\sqrt{\pi}} \right]$
Student's t : $\frac{\Gamma(\frac{\omega+1}{2})}{2\delta\sqrt{\omega\pi}\Gamma(\frac{\omega}{2})} (1 + \frac{v}{\omega}(\frac{v}{\delta})^2)^{-\frac{\omega+1}{2}}$	$\delta^{s-1} \left[\frac{\omega^{(s-1)/2} \Gamma(\frac{s}{2}) \Gamma(\frac{\omega+1}{2} - \frac{s}{2})}{2\sqrt{\pi}\Gamma(\frac{\omega}{2})} \right]$	$\delta^m \left[\frac{\omega^{(m/2-1)} \Gamma(\frac{m+1}{2}) \Gamma(\frac{\omega-m}{2})}{2\sqrt{\pi}\Gamma(\frac{\omega}{2})} \right]$
Triangular: $\begin{cases} \frac{1}{\delta} (1 - \frac{ v }{\delta}) & \text{if } v \leq \delta \\ 0 & \text{otherwise} \end{cases}$	$\delta^{s-1} \left[\frac{\Gamma(s)}{\Gamma(2+s)} \right]$	$\delta^m \left[\frac{1}{m^2 + 3m + 2} \right]$
Trapezoidal: $\begin{cases} \frac{1}{\delta(1+\omega)} & \text{if } v \leq \omega \\ \frac{\delta- v }{\delta^2(1-\omega^2)} & \text{if } \omega < v \leq \delta \\ 0 & \text{otherwise} \end{cases}$	$\delta^{s-1} \left[\frac{1-\omega^{s+1}}{1-\omega^2} \frac{\Gamma(s)}{\Gamma(2+s)} \right]$	$\delta^m \left[\frac{(1-\omega^{m+2})/(1-\omega^2)}{m^2 + 3m + 2} \right]$

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Beta:	$\frac{1}{2\delta B(\omega_1, \omega_2)} \left(\frac{ v }{\delta}\right)^{\omega_1-1} \left(1 - \frac{ v }{\delta}\right)^{\omega_2-1}$	$\delta^{s-1} \left[\frac{\Gamma(\omega_1 + \omega_2) \Gamma(\omega_1 - 1 + s)}{2\Gamma(\omega_1) \Gamma(\omega_1 + \omega_2 - 1 + s)} \right]$	$\delta^m \left[\frac{(\omega_1 + m - 1)_m}{2(\omega_1 + \omega_2 + m - 1)_m} \right]$
Uniform:	$\frac{1}{2\delta}$	$\delta^{s-1} \left[\frac{\Gamma(s)}{2\Gamma(1+s)} \right]$	$\delta^m \left[\frac{1/2}{m+1} \right]$
Gamma:	$\frac{1}{2\delta\Gamma(\omega)} \left(\frac{ v }{\delta}\right)^{\omega-1} e^{-\frac{ v }{\delta}}$	$\delta^{s-1} \left[\frac{\Gamma(\omega - 1 + s)}{2\Gamma(\omega)} \right]$	$\delta^m \left[\frac{(\omega + m - 1)_m}{2} \right]$
Laplace:	$\frac{1}{2\delta} e^{-\frac{ v }{\delta}}$	$\delta^{s-1} \left[\frac{\Gamma(s)}{2} \right]$	$\delta^m \left[\frac{m!}{2} \right]$
Weibull:	$\frac{\omega}{\delta} \left(\frac{ v }{\delta}\right)^{\omega-1} e^{-\left(\frac{ v }{\delta}\right)^\omega}$	$\delta^{s-1} \left[\frac{\omega}{2} \Gamma\left(1 - \frac{1}{\omega} + \frac{s}{\omega}\right) \right]$	$\delta^m \left[\frac{\omega \Gamma(\frac{m}{\omega} + 1)}{2} \right]$
Maxwell:	$\frac{1}{\delta} \sqrt{\frac{2}{\pi}} \left(\frac{v}{\delta}\right)^2 e^{-\frac{v^2}{2\delta^2}}$	$\delta^{s-1} \left[\frac{2^{(s+1)/2}}{\sqrt{\pi}} \Gamma\left(1 + \frac{s}{2}\right) \right]$	$\delta^m \left[\frac{2^{m/2-1} (\frac{m-1}{2})!}{\sqrt{\pi}} \right]$
Lognormal:	$\frac{1}{v\delta\sqrt{2\pi}} e^{\frac{-\ln^2(v)}{2\delta^2}}$	$\exp\left(\frac{(s-1)^2 \delta^2}{2}\right)$	$\exp\left(\frac{m^2 \delta^2}{2}\right)$