Algorithm design for ACM-ICPC

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Introduction •00





Introduction •00





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- 3 students compete in a team, using only 1 machine.
- About 10 problems and 5 hours are given.
- Judgement is in real-time. A balloon is awarded for accepted solutions.

Picture from World Finals 2008-2009



Problem: Room Assignments

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WSAC 2011 is going to be held, from last year's success.

Lastly, Wonha has been asked to assign rooms to participants.

But in this time, we're able to assign exactly one room for each participant.

Organizer has reserved rooms as many as the number of the participants.



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At the registration time, every participant chooses two preferred rooms, and writes down their numbers on both side of the coin.

And then, everyone throws their own coin.

If there is no conflict, assignment is done... but otherwise, everyone should re-throw their coin until assignment is done.

This approach ensures uniformness of the assignment!



Wonha, a little undergraduate, is also participant too.

He already rated the preference of each room in a numerical way.

Formally speaking, he rated the preference of room k by integer v_k .



Problem description

Problem: Room Assignments (cont.)

- Wonha, a little undergraduate, is also participant too.
- He already rated the preference of each room in a numerical way.
- Formally speaking, he rated the preference of room k by integer v_k .
- As a moderator, he knows all others' preference; so he's going to
- have some advantage!
- Help him to maximize expected rating of assigned room.



```
Input
```

```
C # Number of test cases (1 <= C <= 200)

N # Number of rooms (2 <= N <= 50000)

a_1 b_1 # Preferred two rooms

a_2 b_2 # 1 <= a_k < b_k <= N

...

a_N-1 b_N-1

v_1 v_2 ... v_N # Rating (1 <= v_k <= 1000000)
```

Output

For each test case.

- Print a single line containing the two different room numbers a and b, which should be selected by Wonha.
- If there is more than one optimal selection, break ties by choosing lexicographically smallest solution.
- If there is no way to select two rooms such that an assignment is possible, print "impossible" instead.



Constructing a solution

- Vertex each room
- (undirected) Edge each person.
 - Endpoint of edge selected rooms
 - Direction of edge result of coin toss

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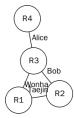
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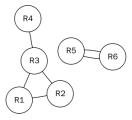
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Observation: independence

Two disconnected components are independent.



We should focus on each component.



Observation: classifying components

$$V = E + 1 \dots \text{tree!}$$

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Constructing a solution

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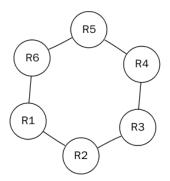
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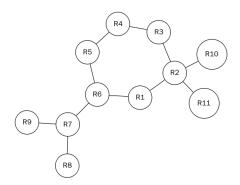
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ullet $V < E \dots$ by pigeonhole principle, assignment is impossible.

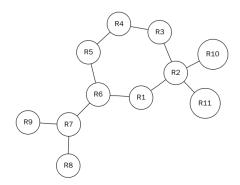
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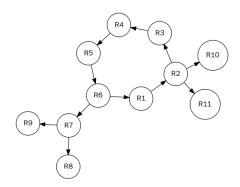
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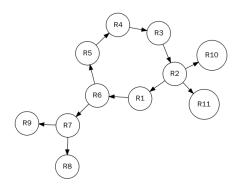
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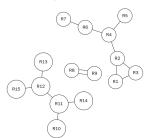
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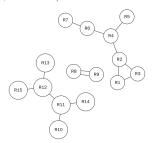
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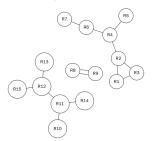
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(Note: there exists one and only tree component for every "valid"

graph.)



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- Tree-to-Other: One endpoint will never be selected Expectation is equal to other endpoint's rating.
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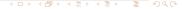
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- Submatrix version (Taiwan 2001)
- Binary sequence version (Seoul 2009)



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Naïve approaches

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- **Evaluating** $\mu_{i,j+1}$ or $\mu_{i+1,j+1}$ from $\mu_{i,j}$ isn't difficult.
- It leads overall time complexity to $O(n^2)$.



Key observation:

- For a subsequence S[i...j], with length $\geq 2L$.
- Split that one into two subsequences, like $\mu_{i,i+L-1}$ and $\mu_{i+L,j}$
- One of them has bigger mean
- \blacksquare ... leads to O(NL), infeasible for L=O(N).
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- Converting the problem into decision problem:
 - Is m upper bound for means of all subsequences? $m > \frac{\sum_{i \in S^l} S[i]}{n}$
 - In other words, $f(S') = \sum_{i \in S'} (m S[i]) \ge 0$. We have to find minimum of f(S').
 - If we define T[i] := m S[i], the problem is essentially same as minimum sum subsequence problem. Easy.
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Reinterpreting the problem

- Maximize $\frac{\sum_{i \in S'} S[i]}{|S'|}$, among all possible subsequence S'.
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Removing blocks from the list



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Remove first block when it's better not to use.

Example #2 0000000



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- Why? These blocks are never useful, because we're looking for maximum!



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- Each block is removed at most once.



Inserting new element into the list



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Linear time algorithm

Managing the list of blocks (cont.)

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- Merge some rear blocks to be in order of its means like this:
- Shifting base window increments the number of blocks.
- Merging two blocks decrements the number of blocks.
- Using data structures like deque, we achieve O(N)!



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- Any language can be used. Competitor downloads input, runs it in one's own machine, and uploads the result with code.



Photo from Google Code Jam 2008





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 - Packaging a medkit, hosted by NASA.

