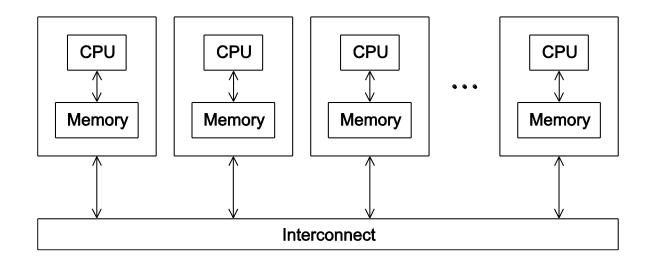
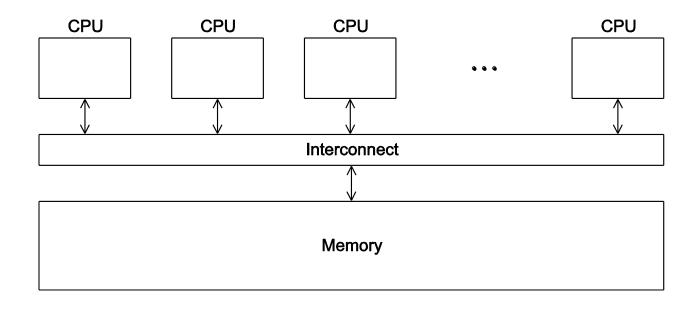
Chapter 3 Distributed Memory Programming with MPI

A distributed memory system



A shared memory system



Hello World!

```
#include <stdio.h>
int main(void) {
   printf("hello, world\n");
   return 0;
}
```



(a classic)

Identifying MPI processes

 Common practice to identify processes by nonnegative integer ranks.

• p processes are numbered 0, 1, 2, .. p-1

Our first MPI program

```
#include < stdio.h>
   #include <string.h> /* For strlen
   #include <mpi.h> /* For MPI functions, etc */
   const int MAX STRING = 100;
   int main(void) {
      char
                 greeting[MAX_STRING];
      int
                 comm_sz; /* Number of processes */
                 my rank; /* My process rank
      int
11
12
      MPI_Init(NULL, NULL);
13
      MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
      MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
15
16
      if (mv rank != 0) {
17
         sprintf(greeting, "Greetings from process %d of %d!",
18
               my_rank, comm_sz);
         MPI_Send(greeting, strlen(greeting)+1, MPI_CHAR, 0, 0,
19
20
               MPI_COMM_WORLD);
21
      } else {
         printf("Greetings from process %d of %d!\n", my_rank, comm_sz);
         for (int q = 1; q < comm_sz; q++) {
            MPI_Recv(greeting, MAX_STRING, MPI_CHAR, g,
25
               0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
26
            printf("%s\n", greeting);
28
29
30
      MPI Finalize():
31
      return 0:
      /* main */
```





Compilation

wrapper script to compile

source file mpiicc -g -Wall -o mpi_hello mpi_hello.c produce create this executable file name debugging (as opposed to default a.out) information

turns on all warnings



Execution

mpiexec -n <number of processes> <executable>

mpiexec -n 1 ./mpi_hello

run with 1 process

mpiexec -n 4 ./mpi_hello

run with 4 processes

Execution

mpiexec -n 1 ./mpi_hello

Greetings from process 0 of 1!

mpiexec -n 4 ./mpi_hello

Greetings from process 0 of 4!

Greetings from process 1 of 4!

Greetings from process 2 of 4!

Greetings from process 3 of 4!



• Written in C.

- - Has main.
 - Uses stdio.h, string.h, etc.
- Need to add mpi.h header file.
- Identifiers defined by MPI start with "MPI"
- First letter following underscore is uppercase.
 - For function names and MPI-defined types.
 - Helps to avoid confusion.



MPI Components

- MPI_Init
 - Tells MPI to do all the necessary setup.

- MPI_Finalize
 - Tells MPI we' re done, so clean up anything allocated for this program.

```
int MPI_Finalize(void);
```



Basic Outline

```
#include <mpi.h>
int main(int argc, char* argv[]) {
   /* No MPI calls before this */
   MPI_Init(&argc, &argv);
   MPI_Finalize();
   /* No MPI calls after this */
   return 0;
```

Communicators

- A collection of processes that can send messages to each other.
- MPI_Init defines a communicator that consists of all the processes created when the program is started.
- Called MPI_COMM_WORLD.

Communicators

```
int MPI_Comm_size(
    MPI_Comm comm /* in */,
    int* comm_sz_p /* out */);
```

number of processes in the communicator

SPMD

- Single-Program Multiple-Data
- We compile <u>one</u> program.
- Process 0 does something different.
 - Receives messages and prints them while the other processes do the work.
- The if-else construct makes our program SPMD.

Communication

```
int MPI_Send(
```



Data types

MPI datatype	C datatype
MPI_CHAR	signed char
MPI_SHORT	signed short int
MPI_INT	signed int
MPI_LONG	signed long int
MPI_LONG_LONG	signed long long int
MPI_UNSIGNED_CHAR	unsigned char
MPI_UNSIGNED_SHORT	unsigned short int
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long int
MPI_FLOAT	float
MPI_DOUBLE	double
MPI_LONG_DOUBLE	long double
MPI_BYTE	
MPI_PACKED	



Communication



Message matching

```
MPI_Send(send_buf_p, send_buf_sz, send_type, dest, send_tag,
        send_comm);
                MPI_Send
                src = q
MPI_Recv(recv_buf_p, recv_buf_sz, recv_type, src, recv_tag
         recv_comm, &status);
```

Receiving messages

- A receiver can get a message without knowing:
 - the amount of data in the message,
 - the sender of the message,
 - or the tag of the message.





status_p argument



MPI_Status*



MPI_Status* status;

status.MPI_SOURCE status.MPI_TAG

MPI_SOURCE MPI_TAG MPI_ERROR



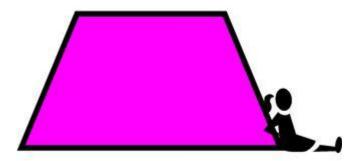
How much data am I receiving?



Issues with send and receive

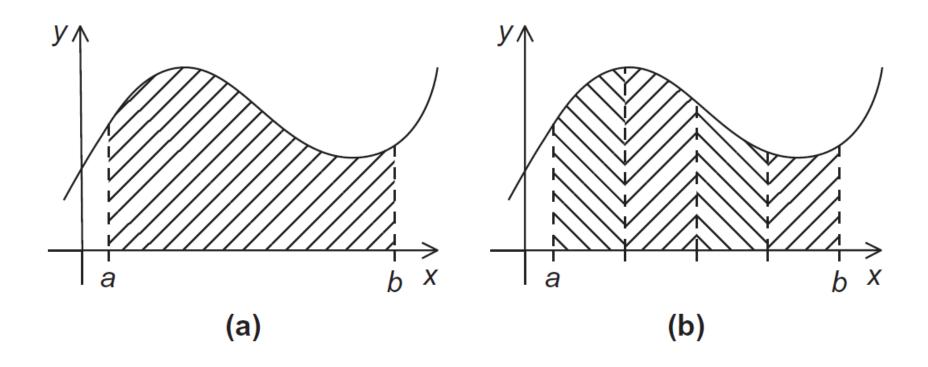
- Exact behavior is determined by the MPI implementation.
- MPI_Send may behave differently with regard to buffer size, cutoffs and blocking.
- MPI_Recv always blocks until a r nessage is received.
- Know your implementation; don't make assumptions!





TRAPEZOIDAL RULE IN MPI

The Trapezoidal Rule



The Trapezoidal Rule

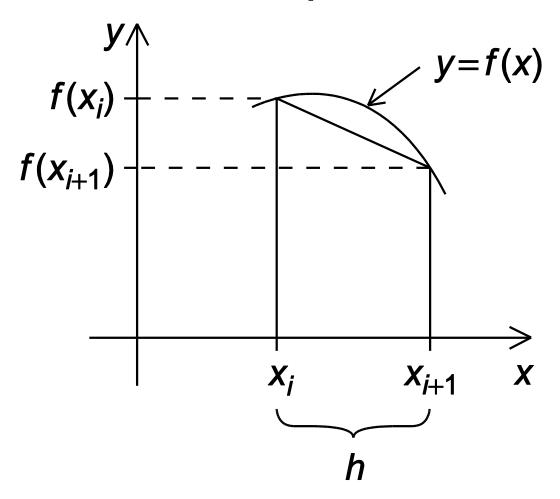
Area of one trapezoid
$$=\frac{h}{2}[f(x_i)+f(x_{i+1})]$$

$$h = \frac{b-a}{n}$$

$$x_0 = a$$
, $x_1 = a + h$, $x_2 = a + 2h$, ..., $x_{n-1} = a + (n-1)h$, $x_n = b$

Sum of trapezoid areas = $h[f(x_0)/2 + f(x_1) + f(x_2) + \dots + f(x_{n-1}) + f(x_n)/2]$

One trapezoid



Pseudo-code for a serial program

```
/* Input: a, b, n */
h = (b-a)/n;
approx = (f(a) + f(b))/2.0;
for (i = 0; i \le n-1; i++)
   x i = a + i*h;
   approx += f(x i);
approx = h*approx;
```

Parallelizing the Trapezoidal Rule

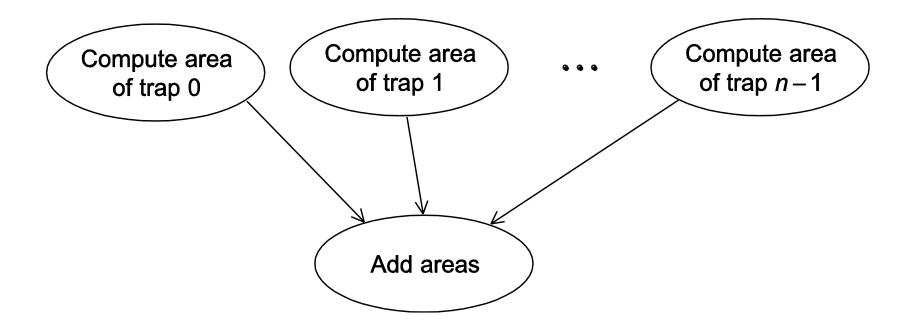
- 1. Partition problem solution into tasks.
- 2. Identify communication channels between tasks.
- 3. Aggregate tasks into composite tasks.
- 4. Map composite tasks to cores.

Parallel pseudo-code

```
Get a, b, n;
      h = (b-a)/n;
      local_n = n/comm_sz;
4
      local_a = a + my_rank*local_n*h;
5
      local_b = local_a + local_n*h;
6
      local_integral = Trap(local_a, local_b, local_n, h);
7
      if (my_rank != 0)
8
         Send local integral to process 0;
9
      else /* my_rank == 0 */
10
         total_integral = local_integral;
11
         for (proc = 1; proc < comm_sz; proc++) {</pre>
12
            Receive local integral from proc;
13
            total_integral += local_integral;
14
15
16
      if (my_rank == 0)
17
         print result;
```



Tasks and communications for Trapezoidal Rule



First version (1)

```
int main(void) {
      int my rank, comm sz, n = 1024, local n;
      double a = 0.0, b = 3.0, h, local a, local b;
      double local int, total int;
      int source:
      MPI Init(NULL, NULL);
8
      MPI Comm rank (MPI COMM WORLD, &my rank);
9
      MPI Comm size (MPI COMM WORLD, &comm sz);
10
      h = (b-a)/n; /* h is the same for all processes */
11
      local n = n/comm sz; /* So is the number of trapezoids */
12
13
14
      local a = a + mv rank*local n*h;
15
      local b = local a + local n*h;
16
      local int = Trap(local a, local b, local n, h);
17
18
      if (mv rank != 0) {
         MPI_Send(&local_int, 1, MPI DOUBLE, 0.0.
19
20
               MPI COMM WORLD);
```



First version (2)

```
21
      } else {
22
         total int = local int;
23
         for (source = 1; source < comm sz; source++) {
24
             MPI Recv(&local int, 1, MPI DOUBLE, source, 0,
25
                   MPI COMM WORLD, MPI STATUS IGNORE);
26
             total int += local int;
27
28
29
30
      if (mv rank == 0) {
31
         printf("With n = %d trapezoids, our estimate \n", n);
32
         printf("of the integral from %f to %f = %.15e\n",
33
              a, b, total int);
34
35
      MPI_Finalize();
      return 0:
36
37
        main */
```



First version (3)

```
double Trap(
         double left endpt /* in */,
         double right_endpt /* in */,
         int trap_count /* in */,
         double base_len /* in */) {
6
      double estimate, x;
      int i:
8
9
      estimate = (f(left\_endpt) + f(right\_endpt))/2.0;
10
      for (i = 1; i <= trap count -1; i++) {
11
         x = left endpt + i*base len;
12
         estimate += f(x);
13
14
      estimate = estimate * base len;
15
16
      return estimate:
17
     /* Trap */
```

Dealing with I/O

```
#include < stdio.h>
#include <mpi.h>
                                  Each process just
                                  prints a message.
int main(void) {
   int my_rank, comm_sz;
   MPI Init(NULL, NULL);
   MPI Comm size (MPI COMM WORLD, &comm sz);
   MPI Comm rank (MPI COMM WORLD, &my rank);
   printf("Proc %d of %d > Does anyone have a toothpick?\n",
         my rank, comm sz);
   MPI Finalize();
   return 0;
   /* main */
```

Running with 6 processes

```
Proc 0 of 6 > Does anyone have a toothpick?

Proc 1 of 6 > Does anyone have a toothpick?

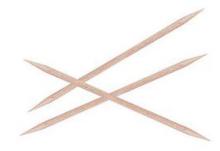
Proc 2 of 6 > Does anyone have a toothpick?

Proc 4 of 6 > Does anyone have a toothpick?

Proc 3 of 6 > Does anyone have a toothpick?

Proc 5 of 6 > Does anyone have a toothpick?
```

unpredictable output



Input

- Most MPI implementations only allow process 0 in MPI_COMM_WORLD access to stdin.
- Process 0 must read the data (scanf) and send to the other processes.

```
MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
Get_data(my_rank, comm_sz, &a, &b, &n);
h = (b-a)/n;
. . .
```



Function for reading user input

```
void Get input(
          my_rank /* in */,
     int
         comm_sz /*in */.
     int
     double* a_p /* out */,
     double* b_p /* out */,
     int * n_p /* out */) {
  int dest:
  if (my rank == 0) 
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", ap, bp, np);
     for (dest = 1; dest < comm sz; dest++) {
        MPI_Send(a_p, 1, MPI_DOUBLE, dest, 0, MPI_COMM_WORLD);
        MPI Send(b p, 1, MPI DOUBLE, dest, 0, MPI COMM WORLD);
        MPI Send(n p, 1, MPI INT, dest, 0, MPI COMM WORLD);
  else { /* my\_rank != 0 */}
     MPI_Recv(a_p, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD,
           MPI_STATUS_IGNORE);
     MPI Recv(b p, 1, MPI DOUBLE, 0, 0, MPI COMM WORLD,
           MPI STATUS IGNORE);
     MPI_Recv(n_p, 1, MPI_INT, 0, 0, MPI_COMM_WORLD,
           MPI STATUS IGNORE);
  /* Get_input */
```



COLLECTIVE COMMUNICATION

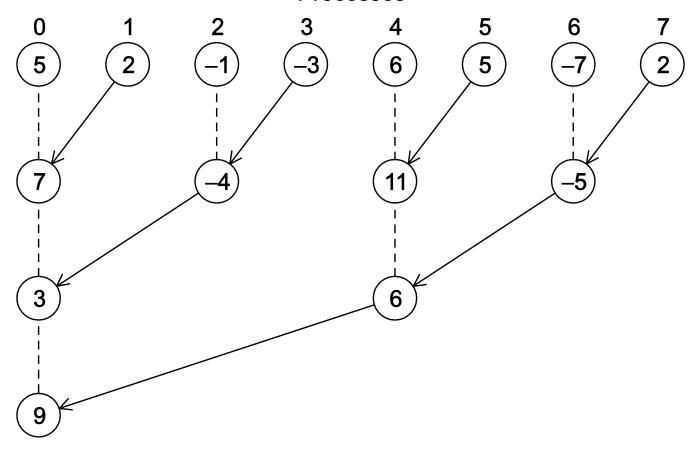


Tree-structured communication

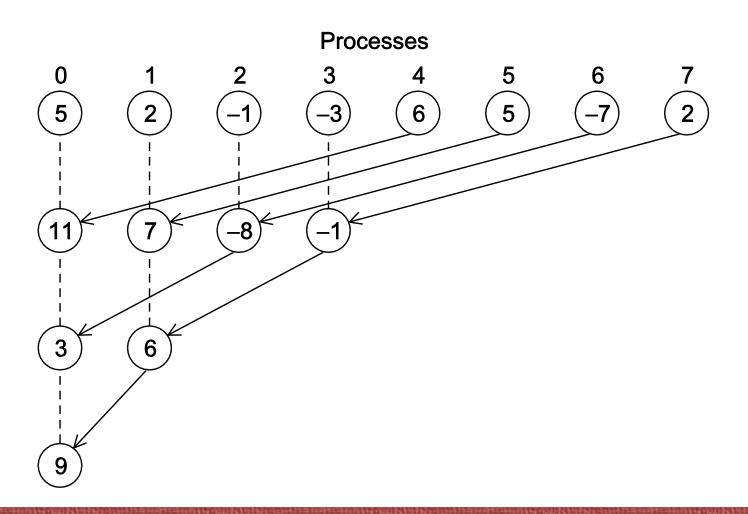
- 1. In the first phase:
 - (a) Process 1 sends to 0, 3 sends to 2, 5 sends to 4, and 7 sends to 6.
 - (b) Processes 0, 2, 4, and 6 add in the received values.
 - (c) Processes 2 and 6 send their new values to processes 0 and 4, respectively.
 - (d) Processes 0 and 4 add the received values into their new values.
- 2. (a) Process 4 sends its newest value to process 0.
 - (b) Process 0 adds the received value to its newest value.

A tree-structured global sum

Processes



An alternative tree-structured global sum



MPI_Reduce

```
\label{eq:mpi_reduce} \begin{split} \texttt{MPI\_Reduce}(\&\texttt{local\_int}\,,\,\,\&\texttt{total\_int}\,,\,\,1\,,\,\,\texttt{MPI\_DOUBLE}\,,\,\,\texttt{MPI\_SUM}\,,\,\,0\,,\\ \texttt{MPI\_COMM\_WORLD}\,); \end{split}
```



Predefined reduction operators in MPI

Operation Value	Meaning
MPI_MAX	Maximum
MPI_MIN	Minimum
MPI_SUM	Sum
MPI_PROD	Product
MPI_LAND	Logical and
MPI_BAND	Bitwise and
MPI_LOR	Logical or
MPI_BOR	Bitwise or
MPI_LXOR	Logical exclusive or
MPI_BXOR	Bitwise exclusive or
MPI_MAXLOC	Maximum and location of maximum
MPI_MINLOC	Minimum and location of minimum



 All the processes in the communicator must call the same collective function.

 For example, a program that attempts to match a call to MPI_Reduce on one process with a call to MPI_Recv on another process is erroneous, and, in all likelihood, the program will hang or crash.



- The arguments passed by each process to an MPI collective communication must be "compatible."
- For example, if one process passes in 0 as the dest_process and another passes in 1, then the outcome of a call to MPI_Reduce is erroneous, and, once again, the program is likely to hang or crash.



- The output_data_p argument is only used on dest_process.
- However, all of the processes still need to pass in an actual argument corresponding to output_data_p, even if it's just NULL.

 Point-to-point communications are matched on the basis of tags and communicators.

- Collective communications don't use tags.
- They' re matched solely on the basis of the communicator and the order in which they' re called.



Example (1)

Time	Process 0	Process 1	Process 2			
0	a = 1; c = 2	a = 1; c = 2	a = 1; c = 2			
1	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)			
2	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)			

Multiple calls to MPI_Reduce

Example (2)

 Suppose that each process calls MPI_Reduce with operator MPI_SUM, and destination process 0.

 At first glance, it might seem that after the two calls to MPI_Reduce, the value of b will be 3, and the value of d will be 6.

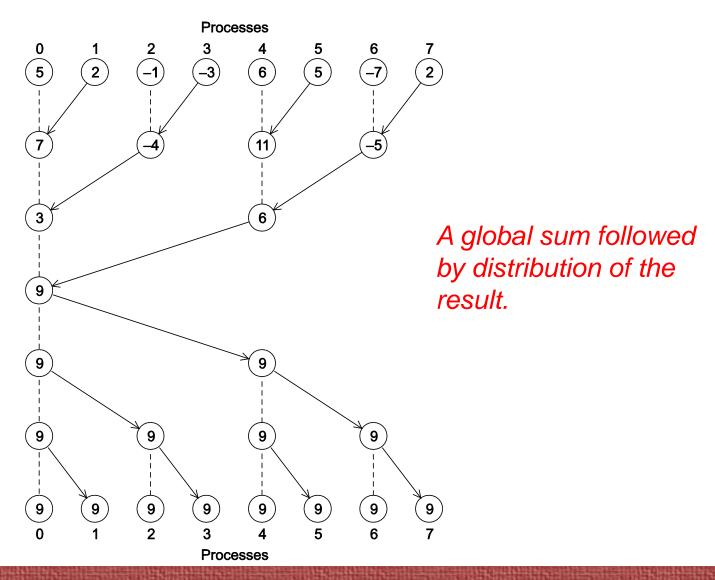
Example (3)

- However, the names of the memory locations are irrelevant to the matching of the calls to MPI_Reduce.
- The order of the calls will determine the matching so the value stored in b will be 1+2+1=4, and the value stored in d will be 2+1+2=5.

MPI_Allreduce

 Useful in a situation in which all of the processes need the result of a global sum in order to complete some larger computation.

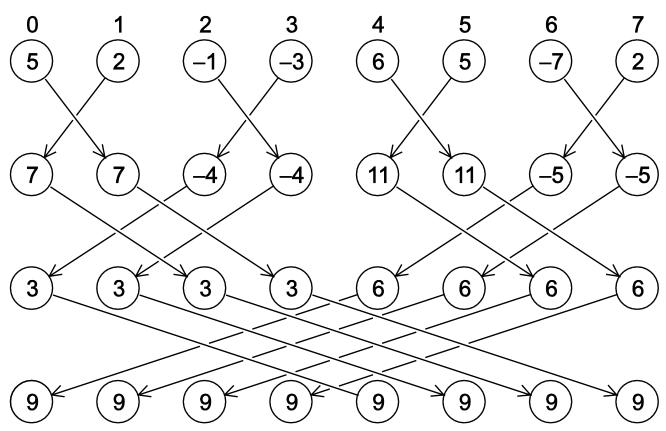
```
int MPI_Allreduce(
        void*
                     input_data_p /* in
                                          */,
        void*
                     output_data_p /* out */,
                                 /* in */,
        int
                    count
                              /* in */,
        MPI_Datatype datatype
                                   /* in */,
        qO I 9M
                     operator
                                   /* in */);
        MPI Comm
                     comm
```







Processes

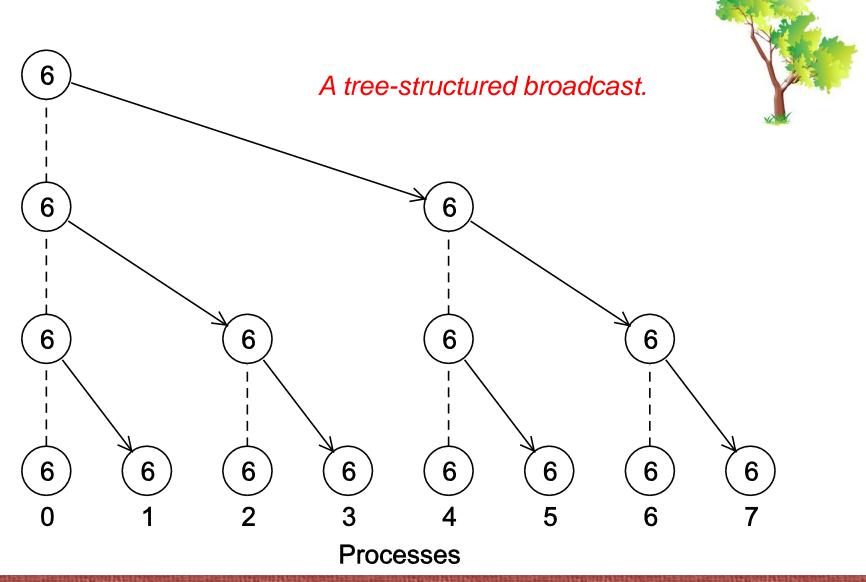


A butterfly-structured global sum.



Broadcast

 Data belonging to a single process is sent to all of the processes in the communicator.





A version of Get_input that uses MPI_Bcast

```
void Get_input(
          my_rank /* in */,
     int
     int comm_sz /* in */,
     double * a_p /* out */,
     double* b_p /* out */,
     int * n_p /* out */) {
  if (my_rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a_p, b_p, n_p);
  MPI_Bcast(a_p, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
  MPI_Bcast(b_p, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
  MPI_Bcast(n_p, 1, MPI_INT, 0, MPI_COMM_WORLD);
 /* Get_input */
```

Data distributions

$$\mathbf{x} + \mathbf{y} = (x_0, x_1, \dots, x_{n-1}) + (y_0, y_1, \dots, y_{n-1})$$

$$= (x_0 + y_0, x_1 + y_1, \dots, x_{n-1} + y_{n-1})$$

$$= (z_0, z_1, \dots, z_{n-1})$$

$$= \mathbf{z}$$

Compute a vector sum.

Serial implementation of vector addition

```
void Vector_sum(double x[], double y[], double z[], int n) {
  int i;

for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
} /* Vector_sum */</pre>
```

Different partitions of a 12component vector among 3 processes

	Components											
								Block-cyclic				
Process	Block				Cyclic				Blocksize = 2			
0	0	1	2	3	0	3	6	9	0	1	6	7
1	4	5	6	7	1	4	7	10	2	3	8	9
2	8	9	10	11	2	5	8	11	4	5	10	11

Partitioning options

- Block partitioning
 - Assign blocks of consecutive components to each process.
- Cyclic partitioning
 - Assign components in a round robin fashion.
- Block-cyclic partitioning
 - Use a cyclic distribution of blocks of components.



Data Layout

- When allocating ensemble memory, an array is divided into layers, where each layer is KP array elements, spread evenly across the P processors.
 - Layer /= floor(i/KP)
 - Processor p=floor((i mod KP)/K)
 - Offset $f=i \mod K$ where i is the index offset of array.

Example (1/2)

 Show how to find an element of an array A[2:100] distributed over eight processors with a block size of five.

Solution

Element k will be found in layer floor((k-2)/40), at processor floor((k-2)mod 40)/5) with offset (k-2)mod 5.

Example (2/2)

	4	86	91	96					
layer 2	3	85	90	95	100				
	2	84	89	94	99				
	1	83	88	93	98				
	0	82	87	92	97				
	4	46	51	56	61	66	71	76	81
_	3	45	50	55	60	65	70	75	80
layer 1	2	44	49	54	59	64	69	74	79
	1	43	48	53	58	63	68	73	78
	0	42	47	52	57	62	67	72	77
	4	6	11	16	21	26	31	36	41
layer 0	3	5	10	15	20	25	30	35	40
	2	4	9	14	19	24	29	34	39
	1	3	8	13	18	23	28	33	38
	0	2	7	12	17	22	27	32	37
		PE0	PE1	PE2	PE3	PE4	PE5	PE6	PE7



Parallel implementation of vector addition

```
void Parallel_vector_sum(
    double local_x[] /* in */,
    double local_y[] /* in */,
    double local_z[] /* out */,
    int local_n /* in */) {
    int local_i;

    for (local_i = 0; local_i < local_n; local_i++)
        local_z[local_i] = local_x[local_i] + local_y[local_i];
} /* Parallel_vector_sum */</pre>
```

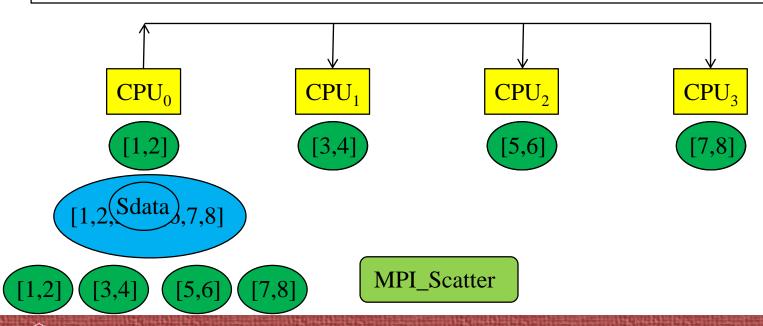
Scatter

 MPI_Scatter can be used in a function that reads in an entire vector on process 0 but only sends the needed components to each of the other processes.

```
int MPI Scatter(
    void*
               send_buf_p /* in */,
    int
                send_count /* in */,
               send_type /*in */,
    MPI_Datatype
    void*
               recv_buf_p /* out */,
    int
               recv_count /* in */,
    MPI_Datatype recv_type /*in */,
    int
                src_proc /* in */,
                comm /* in */):
    MPI Comm
```

MPI_Scatter

```
int Sdata[8] = {1,2,3,4,5,6,7,8}, Rdata[2];
int Send_cnt = 2, Recv_cnt = 2, src = 0;
MPI_Scatter( Sdata, Send_cnt, MPI_INTEGER, Rdata, Recv_cnt,
MPI_INTEGER , src, MPI_COMM_WORLD);
```





Reading and distributing a vector

```
void Read vector(
     double local a[] /* out */,
             local n /*in */,
     int
                    /* in */
     int
             n
     char vec name [] /* in */,
     int my_rank /* in */,
     MPI_Comm comm /*in */) {
  double* a = NULL;
  int i:
  if (mv rank == 0) {
     a = malloc(n*sizeof(double));
     printf("Enter the vector %s\n", vec name);
     for (i = 0; i < n; i++)
        scanf("%lf", &a[i]);
     MPI Scatter(a, local n, MPI DOUBLE, local a, local n, MPI DOUBLE,
          0, comm);
     free(a);
  } else {
     MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local n, MPI DOUBLE,
           0. \text{comm}):
  /* Read_vector */
```

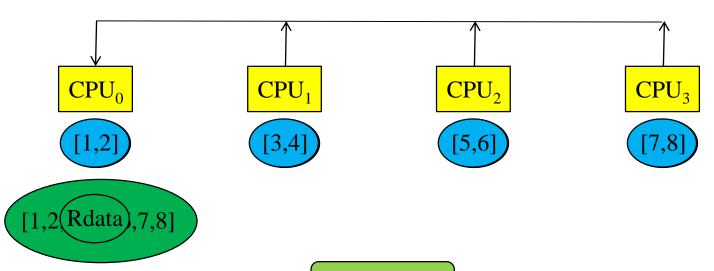


Gather

 Collect all of the components of the vector onto process 0, and then process 0 can process all of the components.

MPI_Gather

int Send_cnt = 2, Recv_cnt = 2, dest = 0;
MPI_Gather (Sdata, Send_cnt, MPI_INTEGER, Rdata, Recv_cnt,
MPI_INTEGER , dest, MPI_COMM_WORLD);





Print a distributed vector (1)

```
void Print_vector(
    double local_b[] /* in */,
    int local_n /* in */,
               /* in */,
    int
    char title[] /* in */,
    int
       my_rank /* in */,
    MPI Comm comm /*in */) {
  double*b = NULL;
  int i;
```

Print a distributed vector (2)

```
if (my_rank == 0) 
  b = malloc(n*sizeof(double));
  MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
         0, comm);
  printf("%s\n", title);
  for (i = 0; i < n; i++)
      printf("%f ", b[i]);
  printf("\n");
  free(b);
} else {
  MPI Gather (local b, local n, MPI DOUBLE, b, local n, MPI DOUBLE,
         0, comm);
/* Print_vector */
```

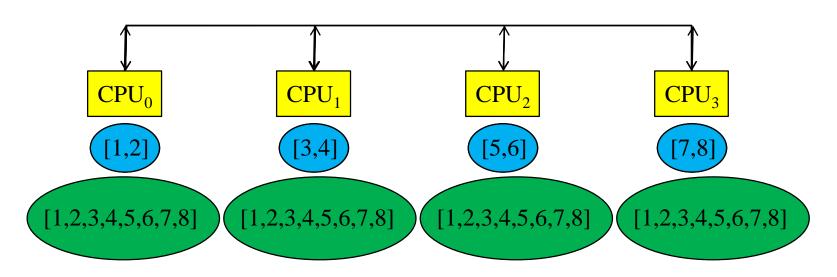
Allgather

- Concatenates the contents of each process' send_buf_p and stores this in each process' recv_buf_p.
- As usual, recv_count is the amount of data being received from each process.



MPI_Allgather

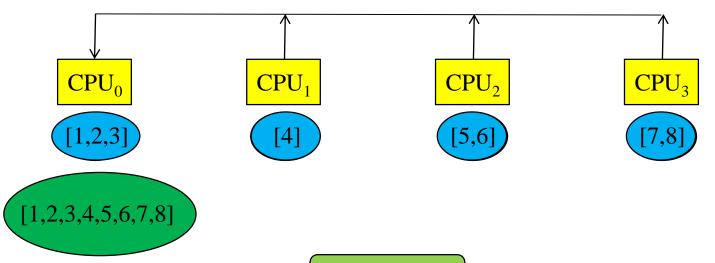
int Send_cnt = 2, Recv_cnt = 8;
MPI_Allgather (Sdata, Send_cnt, MPI_INTEGER, Rdata, Recv_cnt,
MPI_INTEGER , MPI_COMM_WORLD);





MPI_Gatherv

```
int dest = 0, Send_cnt = sizeof(Sbuf);
int rc[4] = {3,1,2,2}, disp[4] = {0,3,4,6};
MPI_Gatherv (Sbuf, Send_cnt, MPI_INTEGER, Rbuf, rc, disp,
MPI_INTEGER, dest, MPI_COMM_WORLD);
```





MPI_Scatterv

 int MPI_Scatterv(const void *sendbuf, const int *sendcounts, const int *displs, MPI_Datatype sendtype, void *recvbuf, int recvcount, MPI_Datatype recvtype, int root, MPI_Comm comm)

Matrix-vector multiplication

$$A = (a_{ij})$$
 is an $m \times n$ matrix

 \mathbf{x} is a vector with n components

y = Ax is a vector with m components

$$y_i = a_{i0}x_0 + a_{i1}x_1 + a_{i2}x_2 + \cdots + a_{i,n-1}x_{n-1}$$

i-th component of y

Dot product of the ith row of A with x.



Matrix-vector multiplication

<i>a</i> ₀₀	<i>a</i> ₀₁	• • • •	$a_{0,n-1}$
a_{10}	a_{11}	:	$a_{1,n-1}$
:	•••		:
a_{i0}	a_{i1}	• • •	$a_{i,n-1}$
a_{i0}	a_{i1} :	•••	$a_{i,n-1}$:

Wo.	Ī
<i>x</i> ₀	
<i>x</i> ₁	
:	
x_{n-1}	
	۰

У0
У1
:
$y_i = a_{i0}x_0 + a_{i1}x_1 + \cdots + a_{i,n-1}x_{n-1}$
:
<i>y</i> _m −1

Multiply a matrix by a vector

```
/* For each row of A */
for (i = 0; i < m; i++) {
    /* Form dot product of ith row with x */
    y[i] = 0.0;
    for (j = 0; j < n; j++)
        y[i] += A[i][j]*x[j];
}</pre>
```

Serial pseudo-code

C style arrays

0 1 2 3 4 5 6 7 8 9 10 11

Serial matrix-vector multiplication

```
void Mat_vect_mult(
     double A[] /* in */,
     double x[] /* in */,
     double y[] /* out */,
     int m /*in */,
     int n /* in */) {
  int i, j;
  for (i = 0; i < m; i++)
     y[i] = 0.0;
     for (j = 0; j < n; j++)
        y[i] += A[i*n+j]*x[j];
  /* Mat_vect_mult */
```

An MPI matrix-vector multiplication function (1)

```
void Mat_vect_mult(
    double local_A[] /* in */,
    double local_x[] /* in */,
    double local_y[] /* out */,
    int local_m /* in */,
    int n
              /* in */,
    int local_n /* in */,
    MPI_Comm comm /* in */) {
  double * x;
  int local_i, j;
  int local_ok = 1;
```

An MPI matrix-vector multiplication function (2)



MPI DERIVED DATATYPES

Derived datatypes

- Used to represent any collection of data items in memory by storing both the types of the items and their relative locations in memory.
- The idea is that if a function that sends data knows this information about a collection of data items, it can collect the items from memory before they are sent.
- Similarly, a function that receives data can distribute the items into their correct destinations in memory when they' re received.

Derived datatypes

- Formally, consists of a sequence of basic MPI data types together with a displacement for each of the data types.
- Trapezoidal Rule example:

Variable	Address
a	24
b	40
n	48

 $\{(MPI_DOUBLE, 0), (MPI_DOUBLE, 16), (MPI_INT, 24)\}$

MPI_Type create_struct

 Builds a derived datatype that consists of individual elements that have different basic types.

```
int MPI_Type_create_struct(
     int
                                            /* in
                   count
     int
                   array_of_blocklengths[]
                                                   */,
                                            /* in
     MPI_Aint
                   array_of_displacements[]
                                            /* in
                                                   */,
                                          /* in */.
     MPI_Datatype array_of_types[]
     MPI_Datatype* new_type_p
                                            /* out */);
```

MPI_Get_address

- Returns the address of the memory location referenced by location_p.
- The special type MPI_Aint is an integer type that is big enough to store an address on the system.

```
int MPI_Get_address(
    void* location_p /* in */,
    MPI_Aint* address_p /* out */);
```

MPI_Type_commit

 Allows the MPI implementation to optimize its internal representation of the datatype for use in communication functions.

```
int MPI_Type_commit(MPI_Datatype* new_mpi_t_p /* in/out */);
```

MPI_Type_free

 When we' re finished with our new type, this frees any additional storage used.

```
int MPI_Type_free(MPI_Datatype* old_mpi_t_p /* in/out */);
```

Get input function with a derived datatype (1)

Get input function with a derived datatype (2)

Get input function with a derived datatype (3)

```
void Get_input(int my_rank, int comm_sz, double* a_p, double* b_p,
     int* n_p) {
  MPI Datatype input mpi t;
  Build_mpi_type(a_p, b_p, n_p, &input_mpi_t);
   if (my rank == 0) 
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a_p, b_p, n_p);
  MPI_Bcast(a_p, 1, input_mpi_t, 0, MPI_COMM_WORLD);
  MPI Type free(&input mpi t);
  /* Get_input */
```

MPI Datatype

- An MPI data is recursively defined as:
 - Predefined, corresponding to a data type from the language (e.g., MPI_INT, MPI_DOUBLE_PRECISION)
 - A strided block of datatypes
 - A contiguous array of MPI datatypes
 - An indexd array of blocks of datatypes
 - An arbitrary structure of datatypes
- There are MPI functions to construct custom datatypes, such an array of (int, float) pairs, or a row of a matrix stored columnwise.

MPI_Type_contiguous

Include a fixed amount of continuous array which have the same data type.

```
int err, count;
MPI_Datatype oldtype, newtype;
err = MPI_Type_contiguous( count, oldtype, &newtype);
```

	count	The size of array.
•	oldtype	The old data type.
	newtype	The new data type.

MPI_Type_contiguous

```
int count = 3;
MPI_Datatype newtype;
err = MPI_Type_contiguous( count, MPI_INTEGER, &newtype);
```

Old: INTEGER

New: INTEGER INTEGER INTEGER \bullet element \bullet element \bullet element \bullet



MPI_Type_vector

• Include a fixed size of interval of discontinuous array which have the same data type.

```
int err, count, blocklength, stride;
MPI_Datatype oldtype, newtype;
err = MPI_Type_vector( count, blocklength, stride, oldtype, &newtype);
```

•	count	The amount of block.
	blocklength	The amount of data with old data type at a block.
	stride	The distance of block, and using old data type as unit.
	oldtype	The old data type.
	newtype	The new data type.

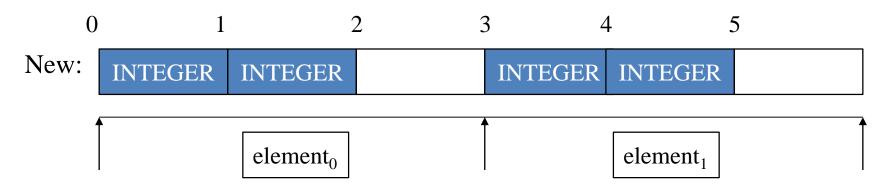
MPI_Type_vector

 $int\ count = 2,\ blocklength = 2,\ stride = 3;$

MPI_Datatype newtype;

MPI_Type_vector(count, blocklength, stride, MPI_INTEGER, &newtype);

Old: INTEGER





MPI_Type_indexed

• Include an any distance and discontinuous array which have the same data type.

```
int err, count, length[], disp[];
MPI_Datatype oldtype, newtype;
err = MPI_Type_indexed( count, length, disp, oldtype, &newtype);
```

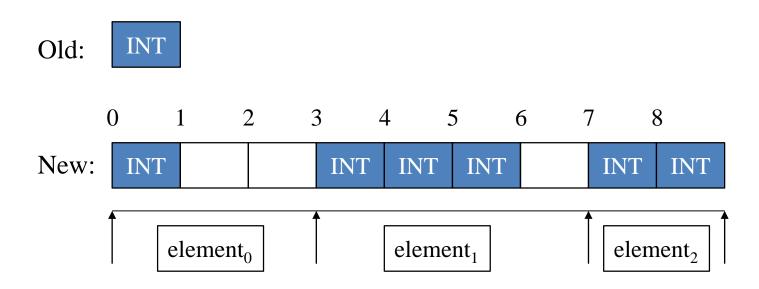
•	count	The amount of block.
	length	The amount of data with old data type at a block.
	disp	The location of block, and using old data type as unit.
	oldtype	The old data type.
	newtype	The new data type.

MPI_Type_indexed

 $int\ count = 3,\ length[3] = \{1,3,2\},\ disp[3] = \{0,3,7\};$

MPI_Datatype newtype;

MPI_Type_indexed(count, length, disp, MPI_INTEGER, &newtype);





MPI_Datatype_struct

Any combination of data types.

```
int err, count, length[];
MPI_Aint disp[];
MPI_Datatype oldtype[], newtype;
err = MPI_Type_struct( count, length, disp, oldtype, &newtype);
```

	count	The amount of block.
•	length	The amount of data with old data type at a block.
	disp	The location of block, and using type as unit.
	oldtype	The old data types.
	newtype	The new data type.

MPI_Datatype_struct

```
int count = 2, length[2] = {2,4}, disp[2] = {0, extent(MPI_INTEGER)*2};
MPI_Datatype oldtype[2] = {MPI_INTEGER, MPI_DOUBLE}, newtype;
MPI_Type_struct( count, length, disp, oldtype, &newtype);
```

Old:

INT

Double

New: INT INT Double Double Double Double element₀



MPI_Type_extent

For using to know the memory size of a specifies data type.

```
MPI_Datatype type;
MPI_Aint extent;
int err = MPI_Type_extent( type, &extent);
```

•	type	Data type.	
	extent	The memory size of an data type unit.	



PERFORMANCE EVALUATION

Elapsed parallel time

 Returns the number of seconds that have elapsed since some time in the

nact

Elapsed serial time

- In this case, you don't need to link in the MPI libraries.
- Returns time in microseconds elapsed from some point in the past.

```
#include "timer.h"
. . .
double now;
. . .
GET_TIME(now);
```



Elapsed serial time

```
#include "timer.h"
. . .
double start, finish;
. . .
GET_TIME(start);
/* Code to be timed */
. . .
GET_TIME(finish);
printf("Elapsed time = %e seconds\n", finish-start);
```

MPI_Barrier

 Ensures that no process will return from calling it until every process in the communicator has started calling it.

```
int MPI_Barrier(MPI_Comm comm /* in */);
```



MPI_Barrier

```
double local_start, local_finish, local_elapsed, elapsed;
MPI Barrier(comm);
local start = MPI Wtime();
/* Code to be timed */
local finish = MPI Wtime();
local_elapsed = local_finish - local_start;
MPI Reduce(&local elapsed, &elapsed, 1, MPI DOUBLE,
  MPI MAX, 0, comm);
if (my rank == 0)
  printf("Elapsed time = %e seconds\n", elapsed);
```

Run-times of serial and parallel matrix-vector multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	4.1	16.0	64.0	270	1100
2	2.3	8.5	33.0	140	560
4	2.0	5.1	18.0	70	280
8	1.7	3.3	9.8	36	140
16	1.7	2.6	5.9	19	71

(Seconds)

Speedup

$$S(n, p) = \frac{T_{\text{serial}}(n)}{T_{\text{parallel}}(n, p)}$$

Efficiency

$$E(n,p) = \frac{S(n,p)}{p} = \frac{T_{\text{serial}}(n)}{p \times T_{\text{parallel}}(n,p)}$$

Speedups of Parallel Matrix-Vector Multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	1.0	1.0	1.0	1.0	1.0
2	1.8	1.9	1.9	1.9	2.0
4	2.1	3.1	3.6	3.9	3.9
8	2.4	4.8	6.5	7.5	7.9
16	2.4	6.2	10.8	14.2	15.5

Efficiencies of Parallel Matrix-Vector Multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	1.00	1.00	1.00	1.00	1.00
2	0.89	0.94	0.97	0.96	0.98
4	0.51	0.78	0.89	0.96	0.98
8	0.30	0.61	0.82	0.94	0.98
16	0.15	0.39	0.68	0.89	0.97

Scalability

 A program is scalable if the problem size can be increased at a rate so that the efficiency doesn't decrease as the number of processes increase.



Scalability

- Programs that can maintain a constant efficiency without increasing the problem size are sometimes said to be strongly scalable.
- Programs that can maintain a constant efficiency if the problem size increases at the same rate as the number of processes are sometimes said to be weakly scalable.

A PARALLEL SORTING ALGORITHM

Sorting

- n keys and p = comm sz processes.
- n/p keys assigned to each process.
- No restrictions on which keys are assigned to which processes.
- When the algorithm terminates:
 - The keys assigned to each process should be sorted in (say) increasing order.
 - If 0 ≤ q < r < p, then each key assigned to process q should be less than or equal to every key assigned to process r.



Serial bubble sort

```
void Bubble sort(
     int a[] /* in/out */,
     int n /* in */) {
  int list_length, i, temp;
  for (list_length = n; list_length \geq 2; list_length--)
     for (i = 0; i < list_length -1; i++)
        if (a[i] > a[i+1]) {
           temp = a[i];
           a[i] = a[i+1];
           a[i+1] = temp;
  /* Bubble_sort */
```

Odd-even transposition sort

- A sequence of phases.
- Even phases, compare swaps:

$$(a[0], a[1]), (a[2], a[3]), (a[4], a[5]), \dots$$

Odd phases, compare swaps:

$$(a[1], a[2]), (a[3], a[4]), (a[5], a[6]), \dots$$

Example

Start: 5, 9, 4, 3

Even phase: compare-swap (5,9) and (4,3) getting the list 5, 9, 3, 4

Odd phase: compare-swap (9,3) getting the list 5, 3, 9, 4

Even phase: compare-swap (5,3) and (9,4) getting the list 3, 5, 4, 9

Odd phase: compare-swap (5,4) getting the list 3, 4, 5, 9

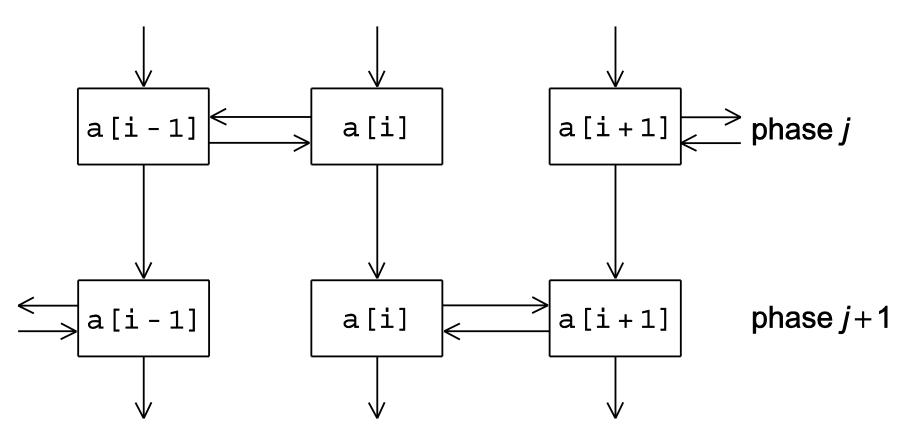


Serial odd-even transposition sort

```
void Odd even sort(
      int a [] /* in/out */,
      int n /* in */) {
   int phase, i, temp;
  for (phase = 0; phase < n; phase++)
      if (phase % 2 == 0) { /* Even phase */
         for (i = 1; i < n; i += 2)
            if (a[i-1] > a[i]) {
              temp = a[i];
               a[i] = a[i-1];
              a[i-1] = temp;
      } else { /* Odd phase */
         for (i = 1; i < n-1; i += 2)
            if (a[i] > a[i+1]) {
              temp = a[i];
               a[i] = a[i+1];
               a[i+1] = temp;
  /* Odd_even_sort */
```



Communications among tasks in odd-even sort



Tasks determining a[i] are labeled with a[i].

Parallel odd-even transposition sort

	Process					
Time	0	1	2	3		
Start	15, 11, 9, 16	3, 14, 8, 7	4, 6, 12, 10	5, 2, 13, 1		
After Local Sort	9, 11, 15, 16	3, 7, 8, 14	4, 6, 10, 12	1, 2, 5, 13		
After Phase 0	3, 7, 8, 9	11, 14, 15, 16	1, 2, 4, 5	6, 10, 12, 13		
After Phase 1	3, 7, 8, 9	1, 2, 4, 5	11, 14, 15, 16	6, 10, 12, 13		
After Phase 2	1, 2, 3, 4	5, 7, 8, 9	6, 10, 11, 12	13, 14, 15, 16		
After Phase 3	1, 2, 3, 4	5, 6, 7, 8	9, 10, 11, 12	13, 14, 15, 16		

Pseudo-code

```
Sort local keys;
for (phase = 0; phase < comm_sz; phase++) {
   partner = Compute_partner(phase, my_rank);
   if (I'm not idle) {
      Send my keys to partner;
      Receive keys from partner;
      if (my_rank < partner)</pre>
         Keep smaller keys;
      else
         Keep larger keys;
```

Compute_partner

```
if (phase % 2 == 0) /* Even phase */
  if (my_rank % 2 != 0) /* Odd rank */
     partner = my_rank - 1;
  else
                            /* Even rank */
     partner = my_rank + 1;
                       /* Odd phase */
else
   if (my_rank % 2 != 0)  /* Odd rank */
     partner = my_rank + 1;
  else
                            /* Even rank */
     partner = my_rank - 1;
if (partner == -1 || partner == comm_sz)
  partner = MPI_PROC_NULL;
```

- The MPI standard allows MPI_Send to behave in two different ways:
 - it can simply copy the message into an MPI managed buffer and return,
 - or it can block until the matching call to MPI Recv starts.

- Many implementations of MPI set a threshold at which the system switches from buffering to blocking.
- Relatively small messages will be buffered by MPI_Send.
- Larger messages, will cause it to block.

- If the MPI_Send executed by each process blocks, no process will be able to start executing a call to MPI_Recv, and the program will hang or deadlock.
- Each process is blocked waiting for an event that will never happen.

(see pseudo-code)

 A program that relies on MPI provided buffering is said to be unsafe.

 Such a program may run without problems for various sets of input, but it may hang or crash with other sets.

MPI_Ssend

- An alternative to MPI_Send defined by the MPI standard.
- The extra "s" stands for synchronous and MPI_Ssend is guaranteed to block until the matching receive starts.



Restructuring communication

```
\label{eq:mpi_send} \begin{split} \text{MPI\_Send(msg, size, MPI\_INT, (my\_rank+1) \% comm\_sz, 0, comm);} \\ \text{MPI\_Recv(new\_msg, size, MPI\_INT, (my\_rank+comm\_sz-1) \% comm\_sz,} \\ 0, comm, MPI\_STATUS\_IGNORE. \end{split}
```





MPI_Sendrecv

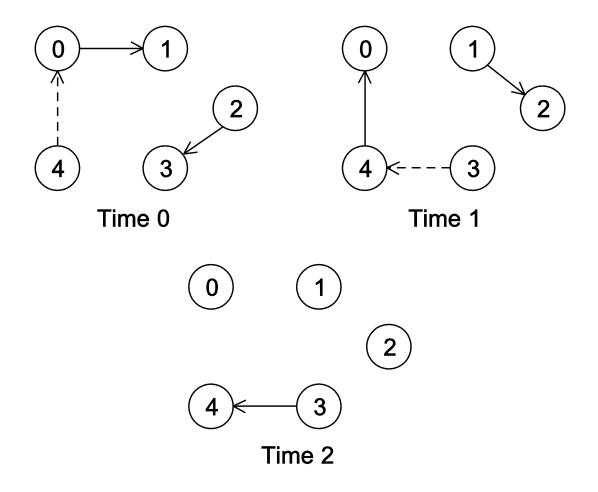
- An alternative to scheduling the communications ourselves.
- Carries out a blocking send and a receive in a single call.
- The dest and the source can be the same or different.
- Especially useful because MPI schedules the communications so that the program won't hang or crash.



MPI_Sendrecv

```
int MPI_Sendrecv(
     void*
                  send_buf_p /*in */,
                  send_buf_size /*in */,
     int
     MPI_Datatype send_buf_type /*in */,
                               /* in */,
     int
                  dest
     int
                               /* in */,
                  send_tag
                  recv_buf_p /* out */,
     void*
                  recv_buf_size /* in */,
     int
     MPI_Datatype recv_buf_type /*in */,
                                /* in */,
     int
                  source
     int
                  recv_tag /*in */,
                  communicator /*in */,
     MPI Comm
                               /* in */);
     MPI Status*
                  status p
```

Safe communication with five processes



Parallel odd-even transposition sort

```
void Merge_low(
     int my_{keys}[], /* in/out */
     int recv_keys[], /* in */
     int temp_keys[], /* scratch */
     int local_n /* = n/p, in */) {
  int mi, ri, ti;
  m i = r i = t i = 0;
  while (t_i < local_n) {
     if (my_keys[m_i] \le recv_keys[r_i]) 
        temp keys[t i] = my keys[m i];
        t i++; m i++;
     } else {
        temp_keys[t_i] = recv_keys[r_i];
       t_i++; r_i++;
  for (m_i = 0; m_i < local_n; m_i++)
     my_{keys}[m_i] = temp_{keys}[m_i];
  /* Merge_low */
```



Run-times of parallel odd-even sort

	Number of Keys (in thousands)				
Processes	200	400	800	1600	3200
1	88	190	390	830	1800
2	43	91	190	410	860
4	22	46	96	200	430
8	12	24	51	110	220
16	7.5	14	29	60	130

(times are in milliseconds)

Concluding Remarks (1)

- MPI or the Message-Passing Interface is a library of functions that can be called from C, C++, or Fortran programs.
- A communicator is a collection of processes that can send messages to each other.
- Many parallel programs use the singleprogram multiple data or SPMD approach.



Concluding Remarks (2)

- Most serial programs are deterministic: if we run the same program with the same input we' Il get the same output.
- Parallel programs often don't possess this property.
- Collective communications involve all the processes in a communicator.

Concluding Remarks (3)

- When we time parallel programs, we' re usually interested in elapsed time or "wall clock time".
- Speedup is the ratio of the serial runtime to the parallel run-time.
- Efficiency is the speedup divided by the number of parallel processes.

Concluding Remarks (4)

- If it's possible to increase the problem size (n) so that the efficiency doesn't decrease as p is increased, a parallel program is said to be scalable.
- An MPI program is unsafe if its correct behavior depends on the fact that MPI_Send is buffering its input.