





COMPILER CONSTRUCTION

Scanning













Chapter 3 Theory and Practice of Scanning













Scanner Generator

- All scanners perform much the same function
 - except for the tokens to be recognized
- A scanner generator helps eliminate the redundant effort of building a scanner
 - One can simply specifying which tokens the scanner is to recognize, and leaves the rest to the generator
 - E.g., Lex, Flex
- Programming a scanner generator is an example of declarative programming
 - we do not tell a scanner generator **how** (procedural programming) to scan but simply **what** to scan



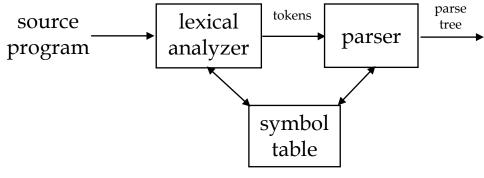






Overview of a Scanner

- A scanner transforms a character stream of source program into a token stream
 - Also called a lexical analyzer or lexer
- Reasons to separate lexical analysis
 - Simpler design is the most import consideration
 - Compiler efficiency is improved
 - Compiler portability is enhanced













Definition of Tokens

- Formal definitions of tokens helps:
 - avoid writing lexical analysers (scanners) by hand; possible errors
 - simplify **specification** and implementation
 - understand the underlying techniques and technologies
- For example, virtually all languages specify certain kinds of rational constants, which are often specified using decimal numerals such as 0.1 and 10.01
- Can .1 or 10. be allowed?
- **→**C, C++, Java say **YES**
- →But, Pascal and Ada say **NO**

Because 1..10 should be interpreted as a range specifier (1 to 10) in Pascal and Ada

If .1 and 10. are allowed, then we'll have **two constants** (i.e., 1. and .10), which will lead to immediate **grammar error** after the ``two constants''













Outline

- In the following pages, we introduces:
 - Regular Expression
 - Finite Automata
 - Deterministic Finite Automata
 - Nondeterministic Finite Automata
- The above techniques are the key to a computer program (e.g., scanner) to recognize the given token automatically













Regular Expression (RE)

- RE
 - Is a way to specify various sets of strings
 - Can specify the structure of the tokens used in a programming language

- In this course, we simply walk through the basic RE concepts required to build a scanner
 - as it should be covered thoroughly in Computing Theory













Regular Expression (Cont'd)

- Regular set
 - A set of strings defined by a regular expression
- Token class
 - A regular set whose structure is defined by a RE
- Lexeme
 - A particular instance of a token class; or, instance of the token

Token class	Sample Lexemes	Informal Description of Pattern
const	const	const
if	if	if
relop	<, <=, =, <>, >, >=	< or <= or = or <> or > or >=
id	pi, count, D2	letter followed by letters and digits
num	0, 3.14, 6.02E23	any number constant













Regular Expression (Cont.)

- Vocabulary, denoted Σ (Sigma)
 - A finite character set
 - Normally the character set used by a computer, e.g., the ASCII character set, which contains 128 characters
 - Java, however, uses the Unicode character set, including ASCII characters and a wide variety of other characters
- Empty (or null) string, denoted λ (Lambda)
 - represents an empty buffer in which no characters have yet been matched
 - represents also an optional part of a token
 - E.g., an integer literal may begin with a plus or minus; or, if it is unsigned, it may begin with λ











Regular Expression (Meta-character)

- Meta-character
 - Any punctuation character or regular expression operator
 - When used as an ordinary character, a meta-character must be quoted to avoid ambiguity
- The six symbols are meta-characters
 - () ' * + |
 - NOTE: the symbol ' is the Apostrophe character as used in don't
- The four single-character tokens are often used in a programming language
 - '(' | ')' | ';' | ',' (left parenthesis, right parenthesis, semicolon, and comma)
 - Parentheses are used to delimit expressions













Regular Expression (Operations)

- Large (or infinite) sets are conveniently represented by operations on finite sets of characters and strings
- The three essential operations for RE Let r_1 , r_2 be REs
 - 1. Catenation. r_1r_2
 - **2.** Alternation. $r_1 \mid r_2$ denotes either r_1 or r_2
 - **3. Kleene closure**. r_1^* denotes zero or more occurrences of r_1

| and * are the operators for Alternation and Kleene Closure, respectively













Regular Expression (Catenation)

- Catenation, an operation
 - Strings are built from characters in the character set Σ via catenation

- As characters are catenated to a string, it grows in length
 - For example, the string `do' is built by first catenating d to λ and then catenating o to the string d
 - The null string λ , when catenated with any string s, yields s
 - That is, $s\lambda \equiv \lambda s \equiv s$













Regular Expression (Catenation) (Cont'd)

- Catenation can be extended to sets of strings
 - Small finite sets are conveniently represented by listing their elements, which can be individual characters or strings of characters

- Let P and Q be sets of strings, and the symbol ∈ represents **set membership**
 - E.g., if s1 ∈ P and s2 ∈ Q, then string s1s2 ∈ (PQ)













Regular Expression (Alternation)

- **Alternation** " | " can be extended to sets of strings
- Examples
- 1. Let P and Q be sets of strings The string $s \in (P | Q)$ if, and only if, $s \in P$ or $s \in Q$
- 2. Let D be the set of the ten single digits
 D is defined as D= (0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9)
 - Note that the textbook often uses abbreviations such **as (0 | ...**
 - . | 9) rather than enumerate a complete list of alternatives
 - The . . . symbol is not part of the regular expression notation











Regular Expression (Kleene Closure)

Kleene closure

- ``*'' postfix operator, representing zero or more occurrences of the *decorated* character/string

Examples

- 1.Let P be a set of strings P represents all strings formed by the catenation of zero or more selections (possibly repeated) from P Zero selections are represented by λ
- 2.LC* is the set of all words composed only of **lowercase letters** and of **any length** (including the zero-length word, λ)













Regular Expression (More Examples)

- Let $\Sigma = \{a, b\}$
 - The regular expression *a* | *b* denotes {a, b}
 - (a | b)(a | b) denotes {aa, ab, ba, bb}
 - i.e., the set of all 2-letter strings of a's and b's
 - Another form is aa | ab | ba | bb
 - a* denotes the set of all strings of a's
 - i.e. $\{\lambda, a, aa, aaa, ...\}$
 - $-(a \mid b)^*$ denotes the set of all strings of a's and b's
 - Another form is (a*b*)*
 - $-a \mid a*b$ denotes the set containing the string a and all strings consisting of zero or more a's and followed by b











Formal Definition

- Ø is a regular expression denoting the **empty set** (the set containing no strings)
- λ is a regular expression denoting the set that contains only the empty string
 - This set is not the same as the empty set because it does contain one element
- The symbol s ($s \in \Sigma$) is a regular expression denoting $\{s\}$,
 - which refers to a **set** containing the single symbol
- If A and B are regular expressions then A | B, AB, and A* are also regular expressions They denote 3 operators:
 - 1) alternation, 2) catenation, and 3) Kleene closure of the corresponding regular sets, respectively











Formal Definition (Cont'd)

Additional operators:

- P+, sometimes called **positive closure** denotes all strings consisting of **one or more strings** in P catenated together: P*= (P+ $\mid \lambda$) and P+ = PP*
- If A is a set of characters, Not(A), denotes (Σ A), all characters in Σ , but not in A
- If k is a constant, then the set A^k represents all strings formed by catenating k (possibly different) strings from A, i.e., $A^k = (AAA ...)$, k copies of A













Regular Expression (Another Example)

- A Java or C++ single-line comment that begins with // and ends with Eol
 - \rightarrow Comment = //(Not(EoI))*EoI
 - The above RE represents that a comment begins with two slashes and ends at the first end-of-line
 - Within the comment, any sequence of characters is allowed that does not contain an end-of-line
 - This guarantees that the first end-of-line we see ends the comment













Regular Expression (Extra Example)

- A fixed-decimal literal (for example, 23.456) can be defined as
 - \rightarrow Lit = D+.D+
 - One or more digits must be on both sides of the decimal point, so .12 and 35. are excluded

- Note: All **finite** sets are regular
 - However, some (but not all) infinite sets are regular













Beyond Regular Expression

- All regular sets can be defined by Context-Free Grammars (CFGs)
- CFGs are more powerful descriptive mechanism than regular expressions
 - REs are quite adequate for specifying **token-level** syntax
- For every regular expression we can create an efficient device, finite automaton,
 - which recognizes exactly those strings that match the regular expression's pattern













Finite Automata and Scanners

- A **finite automation** (FA) can be used to help **recognize** the tokens specified by a regular expression
 - To see if the given strings are belonging to the regular sets
- An FA consists of:
 - A finite set of *states*
 - A finite *vocabulary*, denoted Σ
 - A set of *transitions* (or moves) from one state to another, labeled with characters in Σ
 - A special state called the *start* state
 - A subset of the states called the *accepting*, or *final*, states
- An FA can also be represented graphically using a transition diagram, composed of the components shown in Fig. 3.1



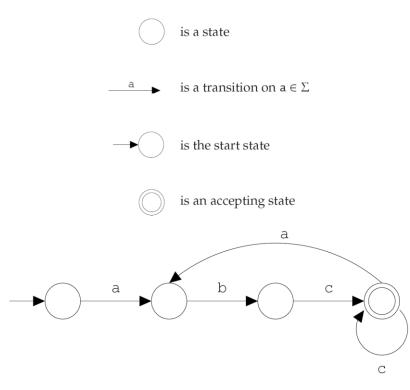






A Finite Automaton

- An FA also can be represented graphically using a transition diagram
 - In practice, we first build the corresponding FA based on the given RE
 - Then, the built FA is used to determine if the given string is a valid token



• We now build the FA for the RE: (abc+)+

Figure 3.1: Components of a finite automaton drawing and their use to construct an automaton that recognizes $(a b c^+)^+$.













- Regular expression: (abc+)+
- The character to be read:
 - None

- Graph:
 - Add the starting state









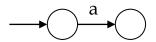






- Regular expression: (abc+)+
- The character to be read:
 - (a

Graph:









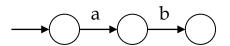






- Regular expression: (abc+)+
- The character to be read:
 - (ab

• Graph:















27

Example: Build A Finite Automaton (Cont'd)

- Regular expression: (abc+)+
- The character to be read:
 - (abc

• Graph:



→ It looks like the string, ``abc'', is accepted by the regular expression, so we mark the current state as the accepting state







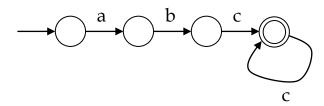






- Regular expression: (abc+)+
- The character to be read:
 - (abc+

• Graph:













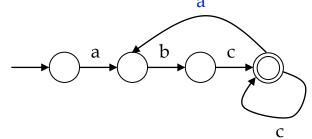


- Regular expression: (abc+)+
- The character to be read:

-(abc+)+

• Graph:

→ To have more ``(abc+)'' string, we add the transition on a









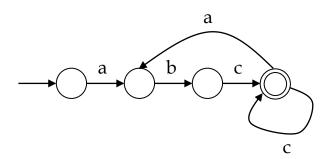






- Regular expression: (abc+)+
- The character to be read:
 - (abc+)+

Graph:













Example: Recognize the Token

- Given an input string and a RE: (abc+)+
 - 1. It starts from the **start state**
 - 2. Does the next input character match the label on a transition from the current state?

 Yes, we move to the state pointed by the next character and set the next character as current character; otherwise, we stop

 This step runs iteratively until no next character or no suitable transition
 - 3. If we finish (or stop) in an accepting state, the sequence of the characters forms a valid token; otherwise, a valid token has not been seen













- Regular expression: (abc+)+
- The given string: abc
- The character to be read:
 - None (at starting state)

• Graph:

a

b

c

c









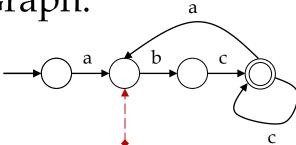




- Regular expression: (abc+)+
- The given string: abc
- The character to be read:

- a

Graph:









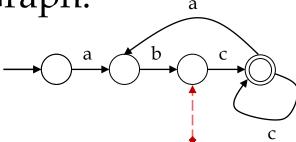






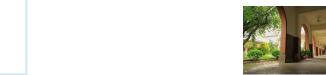
- Regular expression: (abc+)+
- The given string: abc
- The character to be read:
 - ab

Graph:













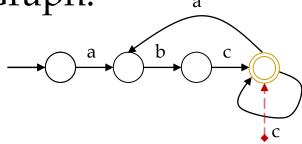


- Regular expression: (abc+)+
- The given string: abc
- The character to be read:



→ We have read out the characters and are at the accepting state, so we say the given string is a valid token.

Graph:













Deterministic Finite Automata (DFA)

 A DFA is an FA that always allows a unique transition for a given state and character

 DFA is simple to program and are often used to drive a scanner

• DFA is conveniently represented in a computer by a transition table













Transition Table for DFA

- A transition table, *T*, is a two-dimensional array
 - indexed by a DFA state and a vocabulary symbol
 - Entries are either a **DFA state** or an **error flag** (often represented as a blank table entry)

Example

- If we are in state s and read character c,
 - then T[s, c] will be the next state we visit,
 - or T[s, c] will contain an error flag indicating that c cannot extend the current token









Example: DFA for the Single-Line Comment

 The single-line comment for Java or C++ can be represented by the regular expression

(a) / 2 / S Eol (4) Not(Eol)

 \rightarrow // (Not (EoI))* EoI

Fig. 3.2 is the corresponding (b)
DFA. (a) transition graph, & (b) transition table

State	Character						
	/	Eol	a	b			
1	2						
2	3						
3	3	4	3	3	3		
4							

- Initial state: 1 Figure 3.2: DFA for recognizing a single-line comment. (a) transition diagram; (b) corresponding transition table.

- Accepting state: 4

- Empty entries indicate error flag





T[]

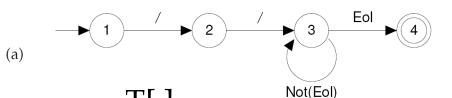




Example: DFA for the Single-Line Comment (Cont'd)

(b)

- T[1, /]
 - Initially, we are at the **state 1** and
 - if we have the next input character \'/'
 - The next state is **state 2** T[1, /]=2
- T[3, d]
 - If we are at the **state 3** and
 - have the next input character `d'
 - The next state is **state 3** \rightarrow T[3, d]=3
- T[3, **Eol**]
 - If we are at the **state 3** and
 - have the next input character Eol
 - The next state is **state 4** \rightarrow T[3, Eol]=4



_	· [/]							
	State	Character						
ſ		_	Eol	a	b			
Γ	1	2						
Γ	2	3						
	3	3	4	3	3	(3)		
Γ	4							

Figure 3.2: DFA for recognizing a single-line comment. (a) transition diagram; (b) corresponding transition table.









Coding the DFA

- A DFA can be coded in one of two forms:
 - Table-driven
 - Explicit control
 - A scanner could be built with either one of the two forms
- The *table-driven* based scanner is shown in Fig. 3.3
 - the transition table that defines the **transitions** in a DFA are **explicitly represented** in a runtime table that is "interpreted" by a driver program

```
/★ Assume CurrentChar contains the first character to be scanned ★/
State ← StartState
while true do

NextState ← T[State, CurrentChar]

if NextState = error
then break
State ← NextState
CurrentChar ← READ()

if State ∈ AcceptingStates
then /★ Return or process the valid token ★/
else /★ Signal a lexical error ★/
```

Figure 3.3: Scanner driver interpreting a transition table.









Coding the DFA (Explicit Control)

- The *explicit control* based scanner is shown in Fig. 3.4
 - the transition table that defines a DFA's actions appears implicitly as the control logic of the program

```
/★ Assume CurrentChar contains the first character to be scanned ★/

if CurrentChar = '/'

then

CurrentChar ← READ()

if CurrentChar = '/'

then

repeat

CurrentChar ← READ()

until CurrentChar ∈ { Eol, Eof }

else /★ Signal a lexical error ★/

else /★ Signal a lexical error ★/

if CurrentChar = Eol

then /★ Finished recognizing a comment ★/

else /★ Signal a lexical error ★/
```

Figure 3.4: Explicit control scanner.













About Lex Scanner Implementation

- Sec. 3.5 Lex Scanner Generator
 - will be covered when we announce the programming homework #1
 - You could read it first by yourself
- Sec. 3.6 Other Scanner Generators
 - Is optional
- Sec. 3.7 Practical Considerations of Building **Scanners**
 - should be read if you want to implement a more complex and efficient scanner













Regular Expression and Finite Automata

- REs are equivalent to FAs
- The main job of **scanner** is to
 - transform a RE into an equivalent FA

- Making an FA from a regular expression proceeds in two steps:
 - 1. It transforms the regular expression into an NFA
 - 2. It transforms the NFA into a DFA

 $RE \rightarrow NFA \rightarrow DFA$













Nondeterministic Finite Automaton (NFA)

- An NFA needs not make a unique (deterministic)
 choice of which state to visit
 - when reading a particular input
 - E.g., an NFA accepts λ transitions
- In other words
 - FAs that contain no λ transitions and that always have unique successor states for any symbol are **deterministic**









Example: NFAs

Fig. 3.17

- -The NFA below is allowed to have a state that has two transitions coming out of it, labeled by the same symbol a Fig. 3.18
- -The NFA may also have transitions labeled with λ

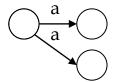


Figure 3.17: An NFA with two a transitions.

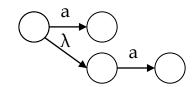


Figure 3.18: An NFA with a λ transition.









Key Elements of REs

- Recall that a regular expression is built of:
 - the *atomic* regular expressions a (a character in Σ) and λ (shown in Fig. 3.19)
 - with the **three operations**: AB, A | B, and A*
 - Other operations, such as A+, are just abbreviation for the combinations for the above operations

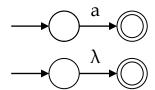


Figure 3.19: NFAs for a and λ .









Transforming RE to NFA

- Suppose we have FAs for A and B
 - The NFA for **A** | **B** (shown in Fig. 3.20)
 - The states labeled A and B were the accepting states of the automata for A and B
 - we create a new accepting state for the combined FA
 - The NFA for AB (shown in Fig. 3.21)
 - The accepting state of the combined FA is the same as the accepting state of B
 - The NFA for A* is (shown in Fig. 3.22)
 - The start state is an accepting state, so λ is accepted

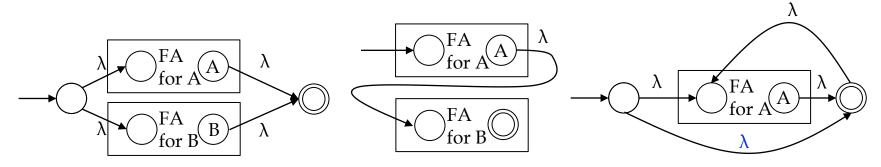


Figure 3.20: An NFA for A | B.

Figure 3.21: An NFA for AB.

Figure 3.22: An NFA for A*.









Example: RE to NFA

- Two steps for converting the regular expression, (a|b)*abb, to the corresponding NFA:
 - 1. We create the NFA for a, b, a | b, (a | b)*
 - 2. We create NFA for "abb"





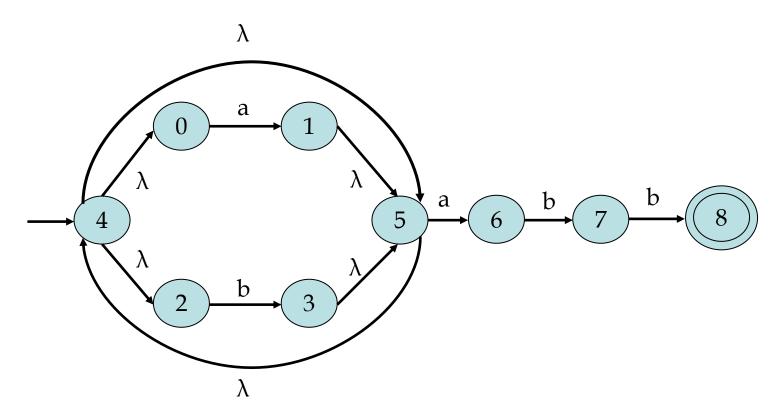






Example: RE to NFA (Cont'd)

- Regular expression: (a | b)*abb
- 1. NFA for a, b, $a \mid b$, $(a \mid b)^*$
- 2. NFA for "abb"
- 3. NFA for (a | b)*abb













Transforming NFA to DFA

- Subset construction algorithm
 - transforming an NFA N to an equivalent DFA D
 - given in Fig. 3.23

N

D

Example of N and D

Key idea

- To construct each state of *D* with a *subset* of states of *N*
- D will be in the state {x,y,z} after reading a given input character, if and only if N could be in any of the states x,y,or z













Notation

N: NFA (non-deterministic finite automata)

D: DFA (deterministic finite automata)

s→t: In N under char c, state s transits to t

 $S\rightarrow T$: In D, under char c, state S transits to T S is a subset of {s | s in N}













Start State

The start state of D

- is the set of all states to which N can transition without reading any input characters
- that is, the set of states reachable from the start state of N following only λ transitions
- Algorithm Close(S,T)
 - computes those **states** that can be reached after only λ transitions, also known as λ -successors
 - shown in Fig. 3.23
- Once the start state of D is built, we begin to create successor states







Step 1: Find **char successors**

Step 2: Find λ successors



Successor States of the Start State

- Place each state S of D on a **work list** when it is created
 - For each state S on the work list and each character c in the vocabulary,

 General tips:
 - we compute S's successor under c ($S \rightarrow T$)
 - S is identified with some set of N's states {n1, n2, . . .}
 - 1. We find all of the possible successor states to {n1, n2, . . .} under **c** and
 - 2. We include the λ -successors of $\{m1, m2, \ldots\}$

obtain a set $\{m1, m2, \ldots\}$

- The resulting set of NFA states is included as a state T in D, and a transition from S to T, labeled with c, is added to D
- We continue adding states and transitions to D until all possible successors to existing states are added
 - Because each state corresponds to a finite subset of N's states, the process of adding new states to D must eventually terminate













Accepting State

- An accepting state of D is any set that contains an accepting state of N
- This reflects the convention that N accepts if there is any way it could get to its accepting state by choosing the "right" transitions











Example: NFA to DFA

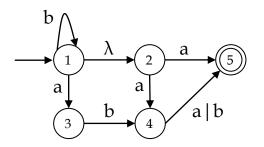


Figure 3.24: An NFA showing how subset construction operates.

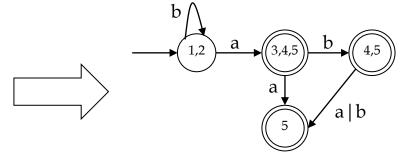


Figure 3.25: DFA created for NFA of Figure 3.24.

```
function makeDeterministic(N) returns DFA
    D.StartState \leftarrow recordState(\{N.StartState\})
    foreach S \in WorkList do
         WorkList \leftarrow WorkList - \{S\}
          for each c \in \Sigma do D.T(S, c) \leftarrow \text{recordState}(T \leftarrow \bigcup_{s \in S} t(s, c))
    D.AcceptStates \leftarrow \{S \in D.States \mid S \cap N.AcceptStates \neq \emptyset\}
end
           λ-successors
function close(S, T) return Set
    ans \leftarrow S
    repeat
        changed ← false
         foreach s \in ans do
              foreach t \in T(s, \lambda) do
6
                    if t \notin ans
                    then
                        ans \leftarrow ans \cup \{t\}
                        changed \leftarrow true
    until not changed
    return (ans)
end
function recordState(S) retur
8 S \leftarrow \operatorname{close}(S, T)
9 If S \notin D. States
    then
        D.States \leftarrow D.States \cup \{S\}
       WorkList \leftarrow WorkList \cup \{S\}
    return (S)
end
```

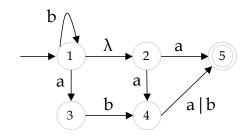


Figure 3.24: An NFA showing how subset construction operates.

To construct the start state of DFA:

{1}

- → To find the set of states reachable from the start state of N following only λ transitions.
- Start with state 1, the start state of N, and call RecordState(state 1) to find its λ -successors (Marker 1)
- RecordState() calls Close(state1, T). T includes states 2 and 3
- In Close(), set ans to state 1 (S). And then for state 1 in ans (Marker 5) find the successor of state 1 via λ -transition, $t \in T(\text{state } 1, \lambda)$ (Marker 6). Add t to ans, which is state 2 (Marker 7).
 - After that, return the ans set, states {1,2}, to RecordState() (Marker 8).
- Then, RecordState() will determine whether the set is in D.States (Marker 9). It is not, so it will be stored into D.States and WorkList (Marker 9).
- Now, we have constructed DFA's start state as states {1,2}.

```
Find all of the possible
function makeDeterministic(N) returns DFA
                                                      successor states under c of
   D.StartState \leftarrow recordState(\{N.StartState\})
                                                        N with the given states,
   foreach S \in WorkList do
                                                           including \lambda states.
                                                                                                            a | b
        WorkList \leftarrow WorkList - \{S\}
        for each c \in \Sigma do D.T(S, c) \leftarrow \text{recordState}(\Gamma) \leftarrow \bigcup_{s \in S} t(s, c)
                                                                                           Figure 3.24: An NFA showing how subset
   D.AcceptStates \leftarrow \{S \in D.States \mid S \cap N.AcceptStates \neq \emptyset\}
                                                                                           construction operates.
end
                                      Construct the successors of the start state S = \{1, 2\} of
function close(S, T) return Set
   ans \leftarrow S
                                      DFA:
   repeat
                                      for each S in WorkList (S = \{1, 2\}) do (Marker 2)
       changed \leftarrow false
                                         under char "a"
       foreach s \in ans do
                                             find S's successor D.T(S, c), where S is {1, 2} and c
           foreach t \in T(s, \lambda) do
6
                                          is a (Marker 3):
                if t \notin ans
                then
                                             state 1 transits to 3,
                    ans \leftarrow ans \cup \{t\}
                                             state 2 transits to 4,
                   changed \leftarrow true
                                             state 2 transits to 5, we got T = \{3,4,5\}
   until not changed
                                           RecordStates ({3,4,5})
   return (ans)
end
                                              add {3,4,5} to D.States and WorkList
function recordState(S) return Set
                                         under char "b"
8 S \leftarrow \operatorname{close}(S, T)
                                             find S's successor D.T(S, c), where S is {1, 2} and c
9 If S \notin D. States
                                          is b):
   then
                                             state 1 transits to 1, we got T=\{1\}
      D.States \leftarrow D.States \cup \{S\}
      WorkList \leftarrow WorkList \cup \{S\}
                                           RecordStates (\{1\}) calls Close(), we got T=\{1,2\}
   return (S)
                                              {1,2} is already in D.States, so do not add it to
end
                                           D.States and WorkList
```

March 19, 2020

57

```
function makeDeterministic(N) returns DFA
    D.StartState \leftarrow recordState(\{N.StartState\})
    foreach S \in WorkList do
                                                                                                                          a | b
         WorkList \leftarrow WorkList - \{S\}
         for each c \in \Sigma do D.T(S, c) \leftarrow \text{recordState}(T \leftarrow \bigcup_{s \in S} t(s, c))
                                                                                                      Figure 3.24: An NFA showing how subset
    D.AcceptStates \leftarrow \{S \in D.States \mid S \cap N.AcceptStates \neq \emptyset\}
                                                                                                      construction operates.
end
function close(S, T) return Set
                                          Construct the successors of the start state S = \{1, 2\} of
   ans \leftarrow S
                                           DFA:
   repeat
                                          for each S in WorkList (S = \{1, 2\}) do (Marker 2)
        changed \leftarrow false
                                              under char "a"
        foreach s \in ans do
             foreach t \in T(s, \lambda) do
                  if t \notin ans
                  then
                      ans \leftarrow ans \cup \{t\}
                      changed \leftarrow true
                                                   state 2 transits to 5, we got T=
                                                                                                   {3,4,5}
   until not changed
                                                                                                   \{1,2\} \xrightarrow{a} \{3,4,5\}
                                                      What we have established so far.
   return (ans)
                                                   add \{3,4,5\} to D.States and wo D.T(\{1,2\}, a) \leftarrow \{3,4,5\}
end
function recordState(S) return Set
                                              under char "b"
8 S \leftarrow \operatorname{close}(S, T)
9 If S \notin D. States
   then
       D.States \leftarrow D.States \cup \{S\}
                                                 recordStates (\{1\}) calls close(), we got T=\{1,2\}
      WorkList \leftarrow WorkList \cup \{S\}
                                                   \{1,2\} is already in D.States, so \{1,2\} \xrightarrow{b} \{1,2\} it to
   return (S)
end
                                                                                                   D.T(\{1,2\}, b) \leftarrow \{1,2\}
```

March 19, 2020

58





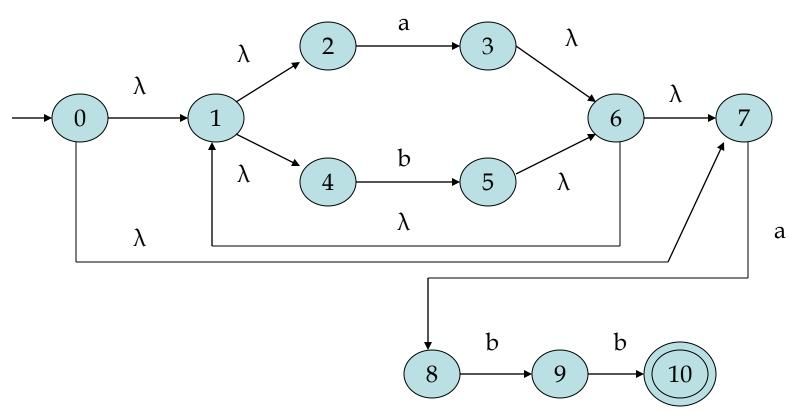




59

Your Exercise

Given the NFA below, find its DFA.









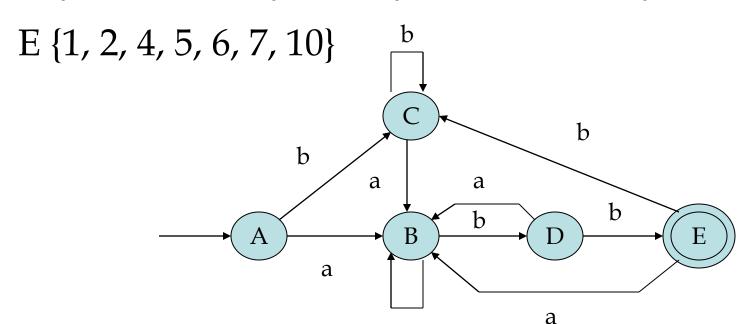


Your Exercise (Cont'd)

The resulting DFA is:

A {0, 1, 2, 4, 7} B {1, 2, 3, 4, 6, 7, 8}

C {1, 2, 4, 5, 6, 7} D {1, 2, 4, 5, 6, 7, 9}



a March 19, 2020

60











QUESTIONS?