工程力學

Exam. #3 (12/17/2018)

- 1. (30pts) Using the method of joints, determine the force in each member of the truss shown in **Fig. 1**. State whether each member is in tension or compression.
- 2. (15pts) Determine the force in members CE and EF of the truss shown in Fig. 2.
- 3. (15pts) Determine the components of all forces acting on member ABCD when $\theta = 90^{\circ}$ shown in Fig. 3.
- 4. (15pts) In using the bolt cutter as shown in Fig. 4, a worker applied two 300-N forces to the handles. Determine the magnitude of the forces exerted by the cutter on the bolt.
- 5. (25pts) The bucket of the front-end loader shown in **Fig. 5** carries a 16-kN load. The motion of the bucket is controlled by two identical mechanisms, only one of which is shown. Knowing that the mechanism shown supports one-half of the 16-kN load, determine the force exerted (a) by cylinder *CD*, (b) by cylinder *FH*.

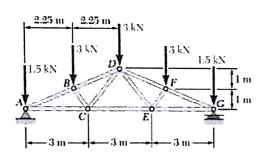


Fig. 1

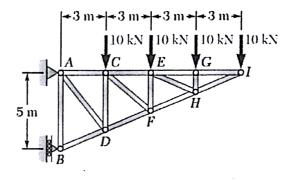


Fig. 2

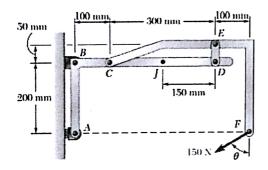


Fig. 3

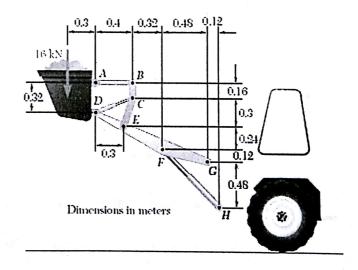


Fig. 5

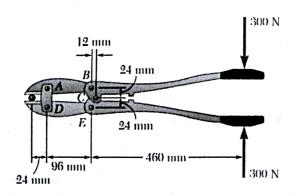


Fig. 4

107 上 微積分 第三次期中考 12/21

考試時間:15:10~17:00

1 D為直線 y=x, 曲線 $y = \frac{2}{x} - 1$ 與 x 軸圍成的區域

- a. 求出 D 之面積
- a 10% b, c 對一題得 10% 兩題得 15%
- b. 利用圓盤法求出 D對 X 軸旋轉之旋轉體體積
- C. 利用剝殼法求出 D 對 X 軸旋轉之旋轉體體積

求以下各積分 2

30%

a.
$$\int_0^{\frac{\pi}{2}} \sin x \cos x \ dx$$
 b. $\int \frac{1}{x^2 - 1} dx$ c. $\int \frac{1}{x^2 + 2x + x} dx$

b.
$$\int \frac{1}{x^2 - 1} dx$$

$$c. \int \frac{1}{x^2 + 2x + x} dx$$

d.
$$\int_{-2}^{-1} \frac{1}{x} dx$$

d.
$$\int_{-2}^{-1} \frac{1}{x} dx$$
 e. $\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \frac{1 + 4 \cot x}{4 - \cot x} dx$ f. $\int \sqrt{1 - \sin x} dx$

f.
$$\int \sqrt{1-\sin x} \, dx$$

求以下各瑕積分 3

10%

a.
$$\int_0^\infty x e^{-x} dx$$

b.
$$\int_0^1 \frac{x}{\sqrt{x-1}} dx$$

求以下各極限

15%

a.
$$\lim_{x \to 0} \frac{1 - \cos x}{x^2}$$

b.
$$\lim_{x \to \infty} x^2 e^{-x}$$

a.
$$\lim_{x\to 0} \frac{1-\cos x}{x^2}$$
 b. $\lim_{x\to \infty} x^2 e^{-x}$ c. $\lim_{x\to 0^+} (1+rx)^{\frac{1}{x}}$ r 為實數

利用分部積分法求出積分 5

20%

a. 用分部積分求出 $\int \sqrt{1-x^2} dx$

$$\left(\frac{d}{dx}sin^{-1}x = \frac{1}{\sqrt{1-x^2}}, 且被積函數為 1 和 \sqrt{1-x^2} 之積\right)$$

b. 函數 f(x) 定義為 $f(x) = \int_1^x sin\pi t^3 dt$

求出
$$\int_0^1 x f(x) dx$$