

# EPE AND SPEED ADAPTIVE EXTENDED KALMAN FILTER FOR VEHICLE POSITION AND ATTITUDE ESTIMATION WITH LOW COST GNSS AND IMU SENSORS

## INTRODUCTION

This poster presents a novel approach for an adaptive Extended Kalman Filter (EKF), which is able to handle bad signal quality caused by shading or loss of Doppler Effect for low cost Global Navigation Satellite System (GNSS) receiver and Inertial Measurement Unit (IMU) sensors, fused in a loosely coupled way. It uses the estimated position error (EPE) from the GNSS device as well as the velocity to calculate the standard deviation for the measurement uncertainty matrix of the Kalman Filter. It estimates the position of a vehicle and its attitude (roll, pitch), as shown in Fig. 1.

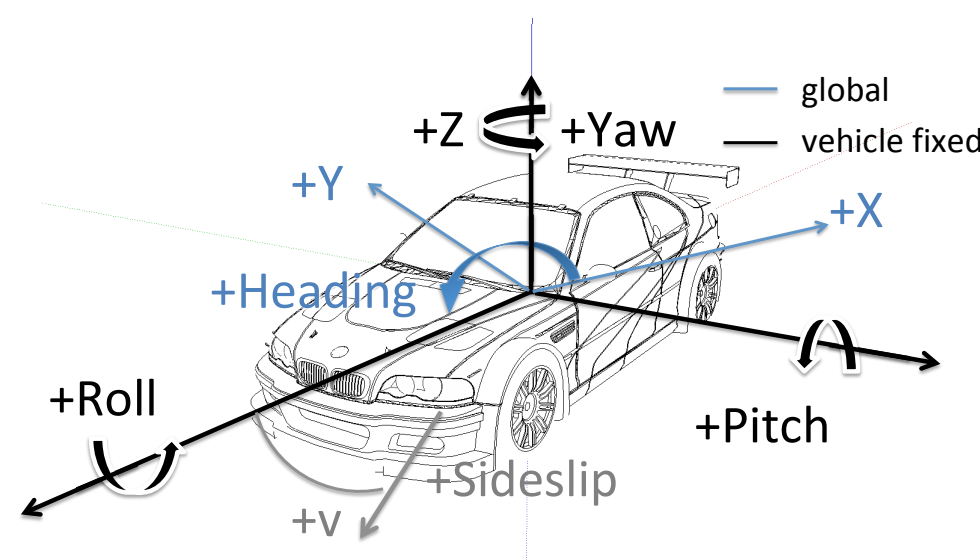


Fig. 1: Vehicle with coordinate system

## ADAPTIVE EXTENDED KALMAN FILTER

The state transition function is defined by

$$\mathbf{x}_{k+1} = \begin{bmatrix} x + \frac{v}{\psi} \left( -\sin(\psi) + \sin(T\dot{\psi} + \psi) \right) \\ y + \frac{v}{\psi} \left( \cos(\psi) - \cos(T\dot{\psi} + \psi) \right) \\ v + T\dot{a}_x \\ \psi + T\dot{\psi} \\ \phi + T\dot{\phi} \\ \Theta + T\dot{\Theta} \end{bmatrix} \quad (1)$$

The positions  $x$  and  $y$ , the speed and heading are measured with a low cost GNSS receiver. The attitude is calculated with an orientation filter (presented in (Madgwick, 2010) and improved by this work).

The novel approach, presented in this work, are the easy to implement and fast to calculate adaptive standard deviations for the measurement noise covariance matrix  $R$ .

$$R = \text{diag} [\sigma_x^2 \ \sigma_y^2 \ \sigma_v^2 \ \sigma_\psi^2 \ \sigma_\phi^2 \ \sigma_\Theta^2] \quad (2)$$

### Position Measurement Uncertainties

In every EKF filterstep, the standard deviations for  $\sigma_x$  and  $\sigma_y$  are calculated, depending on the speed and on the estimated position error (EPE), which is provided by the GNSS module itself.

$$\sigma_x^2 = \sigma_y^2 = c \cdot \sigma_v^2 + \sigma_{EPE}^2 \quad (3)$$

with

$$\sigma_v = (v + \epsilon)^{-\xi} \quad (4)$$

$$\sigma_{EPE} = \zeta \cdot EPE \quad (5)$$

Resulting shape of  $\sigma_x^2$  and  $\sigma_y^2$  as  $f(v, EPE)$  is shown in Fig. 2

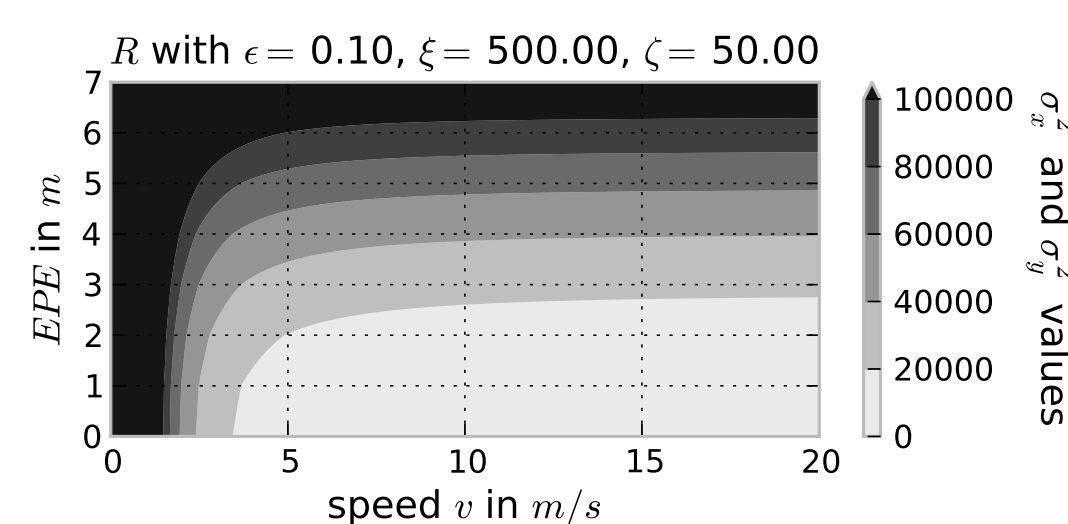


Fig. 2: Adaptive  $\sigma_x^2$  and  $\sigma_y^2$  as  $f(v, EPE)$

### Attitude Measurement Uncertainties

The uncertainties for roll and pitch are adaptively calculated, like suggested by (Madgwick, 2010), depending on the vehicle accelerations in the appropriate directions.

$$\sigma_\Theta = (\rho + \gamma \cdot a_y)^2 \quad (6)$$

$$\sigma_\psi = (\rho + \gamma \cdot a_x)^2 \quad (7)$$

To evaluate the proposed filter, multiple simulations and real world measurements were conducted.

## SIMULATION

To evaluate the adaptive EKF, a typical urban scenario, with shading from a building, as well as a vehicle stop and cornering, was simulated (see Fig. 3).

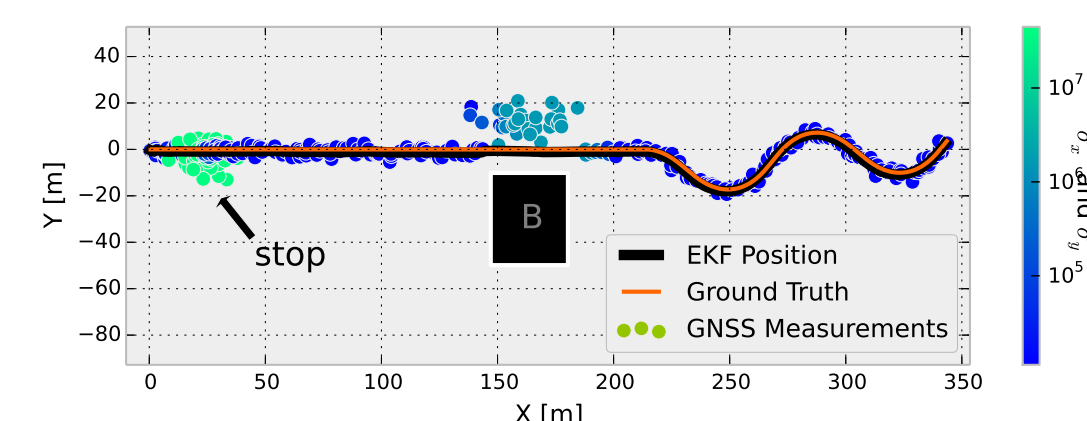


Fig. 3: Simulated urban scenario data

To quantify the filter performance with respect to ground truth (GT) trajectory, the cross track error is introduced.

$$CTE_x = x_{GT} - x \quad (8)$$

To compare the estimated trajectory with a non-adaptive EKF, the position estimation was performed with several datasets for GNSS

position measurements, generated by random Gaussian noise around the ground truth position. The resulting cross track errors (CTE) are shown in Fig. 4.

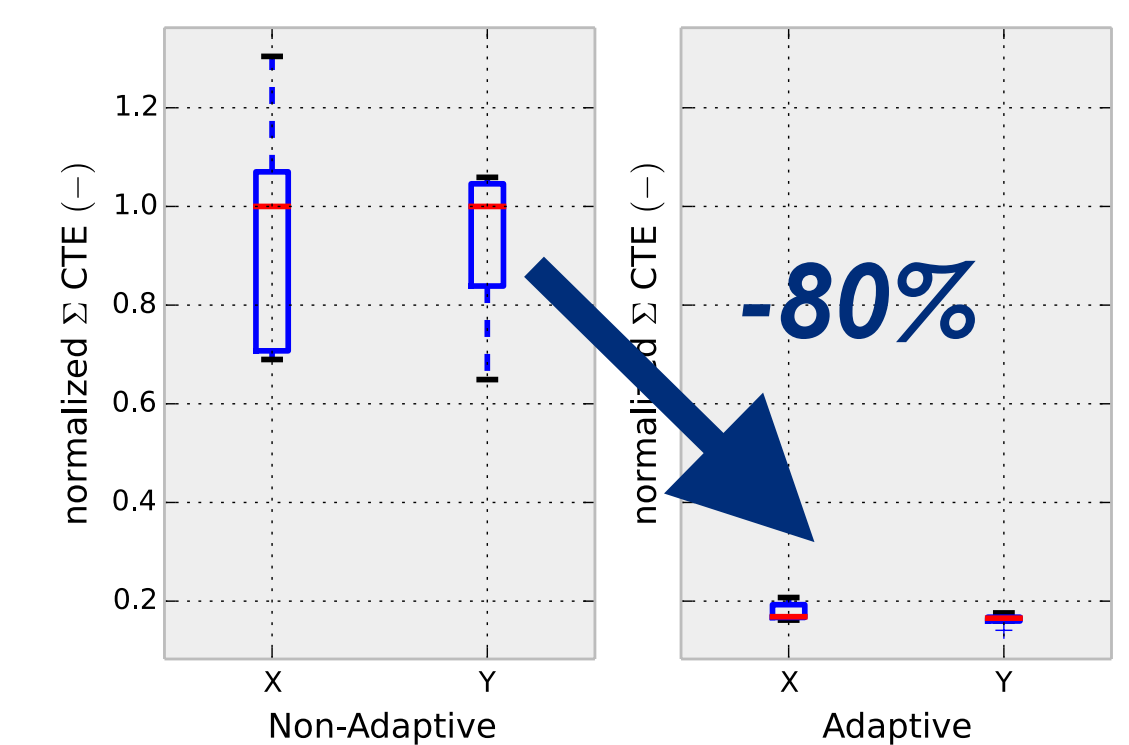


Fig. 4: Cross-track-error of standard and adaptive EKF: 80% reduction.

## EXPERIMENTAL RESULTS

The ground truth was determined with a multi-frequency aerial antenna (Javad GrAnt-G3T) and receiver (Javad Delta), corrected with a virtual reference station (VRS) and Satellite Positioning Service of the German State Survey (SAPOS) data via GPRS modem (come2ascos GenPro). Fig. 5 shows the trajectory of the adaptive EKF and the ground truth.

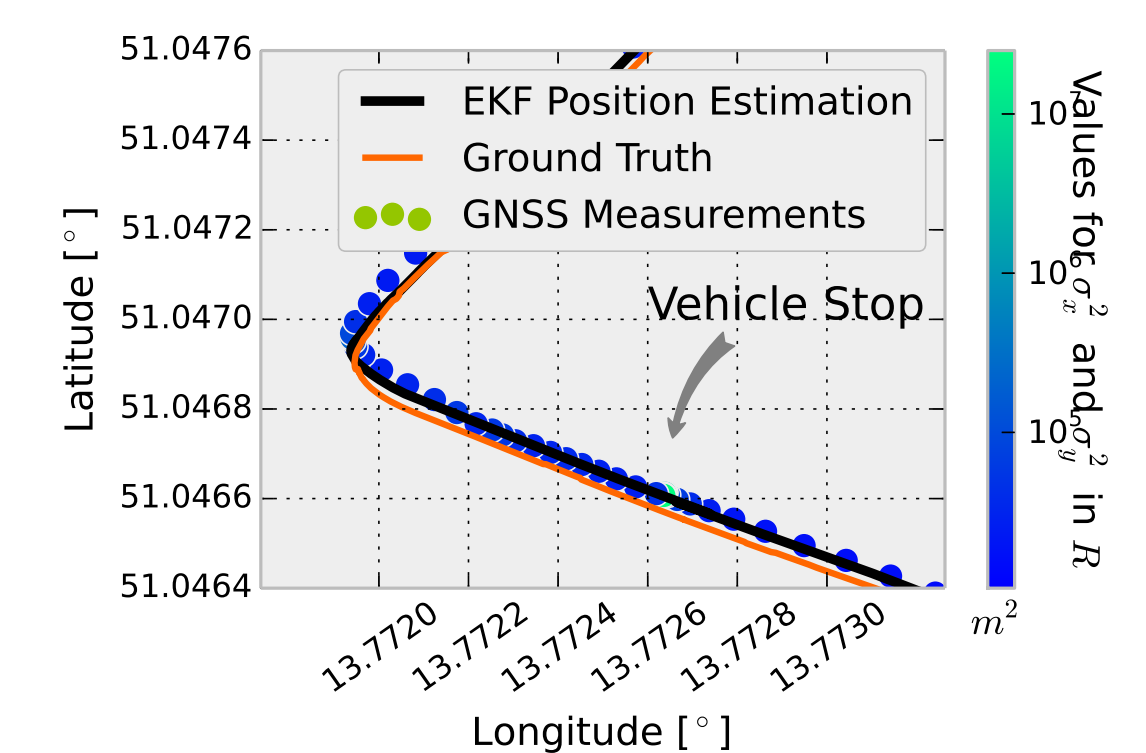


Fig. 5: Part of a test drive with adaptive values of measurement uncertainty values for matrix  $R$

The filter improves the position estimation under partly bad signal quality. In addition to that, the filter also performs pretty well on dynamic situations and is not losing the ability to follow dynamic vehicle movements.

Implementation, data and figures are available: <https://github.com/balzer82/ICINCO-2014>

## REFERENCES

Madgwick, S. (2010). An efficient orientation filter for inertial and inertial/magnetic sensor arrays. Report x-io and University of Bristol.