

If X_1, \dots, X_n random sample
WITHOUT REPLACEMENT
from $\{y_1, \dots, y_N\}$

$$E(\bar{x}) = \bar{y} = \mu$$

$$\sigma^2 = \frac{1}{N} \sum_{j=1}^N (y_j - \bar{y})^2$$

$$\rightarrow \text{Var}(\bar{x}) = \frac{\sigma^2}{n} \left(\frac{N-n}{N-1} \right)$$

NOT
EXAMINABLE!!

$$\approx \frac{\sigma^2}{n} \left(\frac{N-n}{N} \right) = \frac{\sigma^2}{n} \left(1 - \frac{n}{N} \right)$$