

PHYS 1901 – Physics 1A (Advanced) Mechanics module

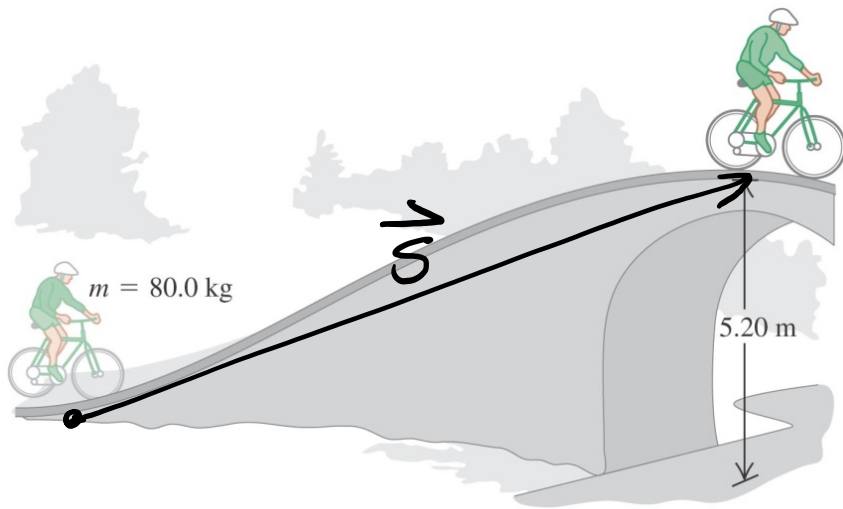


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Problem 6.73



Speed at base: 5.00 m/s Speed at top: 1.50 m/s

Ignore any inefficiencies (e.g. energy lost to heat)

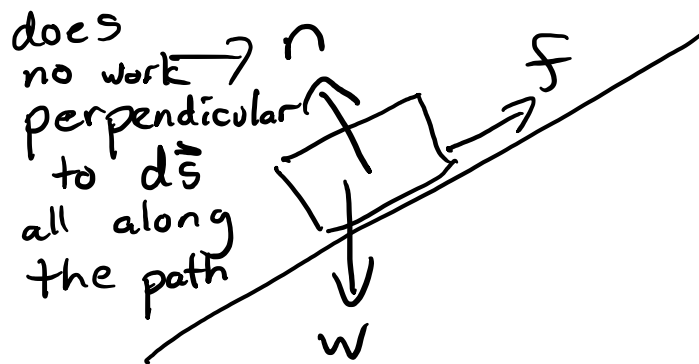
- a) What is the total work done on you and your bike?
- b) How much work have you done?

$$\text{a) } W_{\text{total}} = \Delta K = K_f - K_i = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 = -910 \text{ J}$$

$$\text{b) } W_{\text{total}} = -910 \text{ J} = \cancel{W_n} + W_g + W_f$$

$$W_g = \vec{w} \cdot \vec{s} = -(80.0 \text{ kg})(9.8 \text{ m/s}^2)(5.20 \text{ m}) = -4077 \text{ J}$$

$$W_f = 3167 \text{ J}$$



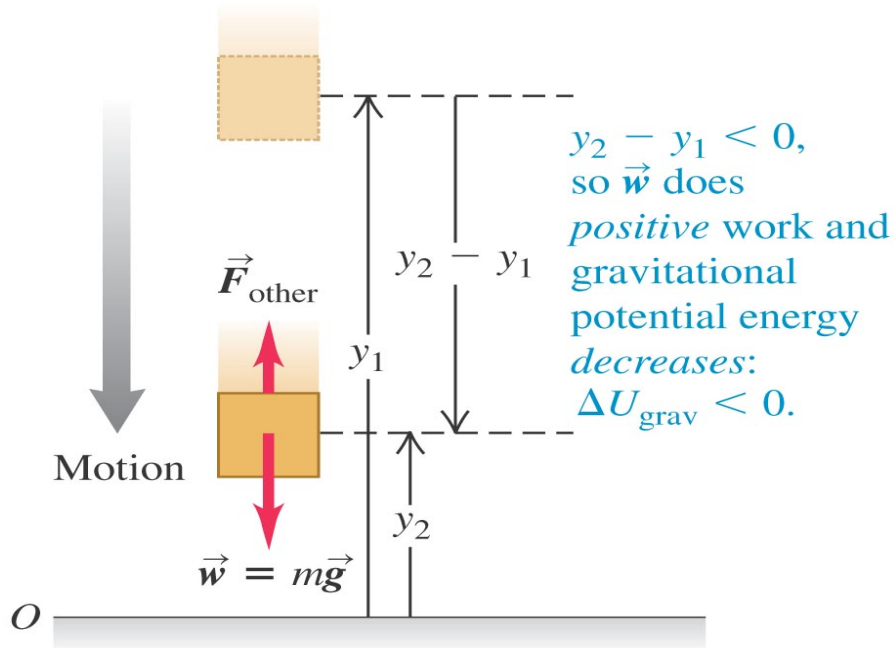
Potential Energy and Energy Conservation

Chapter

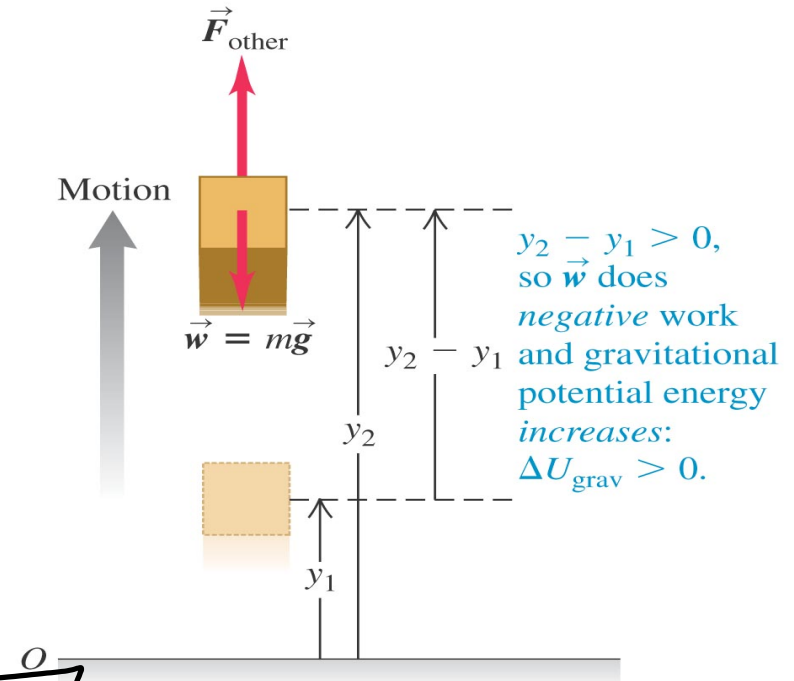
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Gravitational Potential Energy

(a) A body moves downward



(b) A body moves upward



$$W_g > 0$$

Potential energy
is being used

$$\Delta U_g + W_g = 0$$

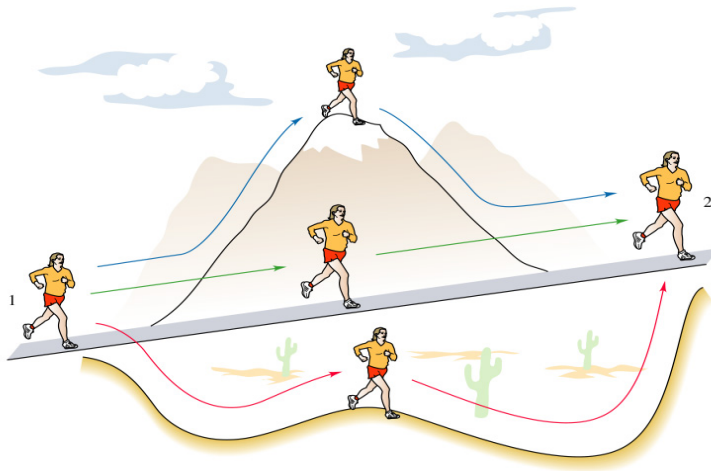
$$W_g < 0$$

Energy is being
stored as potential
energy

So, the energy extracted by gravity is somehow stored in the gravitational field.

Using conservation of energy, we can define the change in **gravitational potential energy** to be

As well as putting energy into the gravitational field, we can extract it; the force is **conservative**

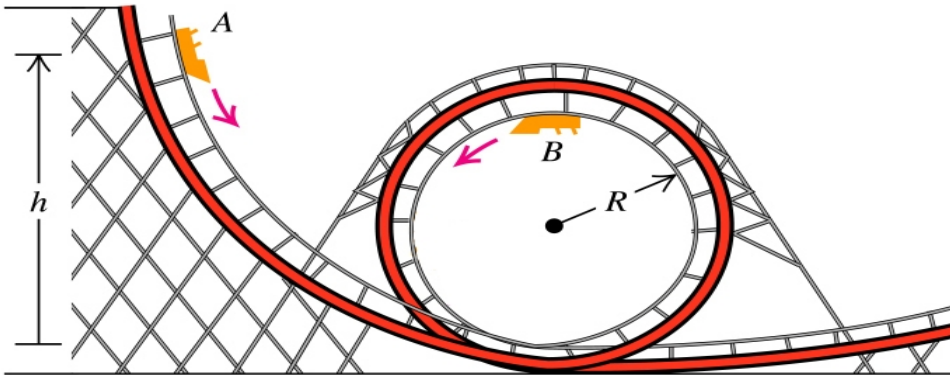


The change in gravitational potential is the same for each.

- › Energy depends only on the difference between the initial and final states
- › Independent of the path
- › Reversible
- › If start point and end point are the same, then the work done is zero
- › Can define a potential energy function

Conservative forces allow energy storage!

Example



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Initial: A
Final: B

$$\begin{aligned}
 W_g &= -\Delta U_g \\
 &= -mg\Delta h \\
 &= -mg(h_B - h_A) \\
 &= -mg(2R - h) \\
 &= mg(h - 2R)
 \end{aligned}$$

W-E theorem

$$\begin{aligned}
 \Delta K &= W_g \\
 K_B - K_A &= W_g = mg(h - 2R)
 \end{aligned}$$

A cart at rest is released from a height h and slides down a frictionless track. It encounters a loop of radius R .

What is its velocity at the top of the loop?
(Assume the cart is fixed to the track).

What happens if we consider friction?

$$\Delta U = mg\Delta h$$

$$\begin{aligned}
 \frac{1}{2}mv_B^2 &= mg(h - 2R) \\
 v_B &= \sqrt{2g(h - 2R)} \quad (\text{left})
 \end{aligned}$$